

Analysis of oscillations with 3 and 3+N neutrinos

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I. Conventional three-neutrino oscillations

II. Models with extra sterile neutrinos

Summary

General three-neutrino framework

- Equation of motion: **6 parameters** (including **Dirac** and neglecting **Majorana** phases):

$$i \frac{d\vec{\nu}}{dt} = H \vec{\nu}; \quad H = U_{\text{vac}} \cdot D_{\text{vac}} \cdot U_{\text{vac}}^\dagger \pm V_{\text{mat}};$$

$$U_{\text{vac}} = \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13} e^{-i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta_{\text{CP}}} & 0 & c_{13} \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} e^{i\eta_1} & 0 & 0 \\ 0 & e^{i\eta_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \vec{\nu} = \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix};$$

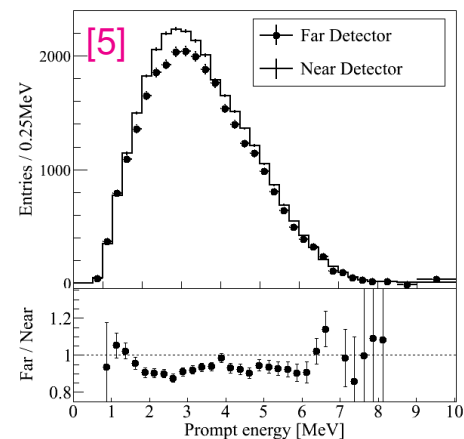
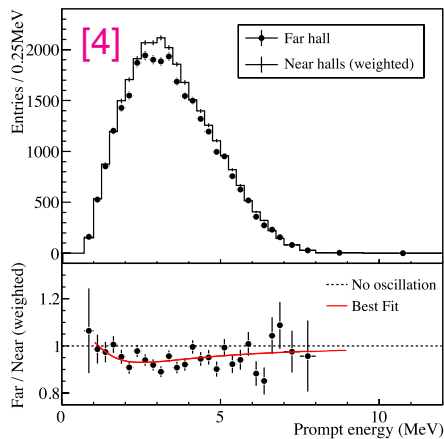
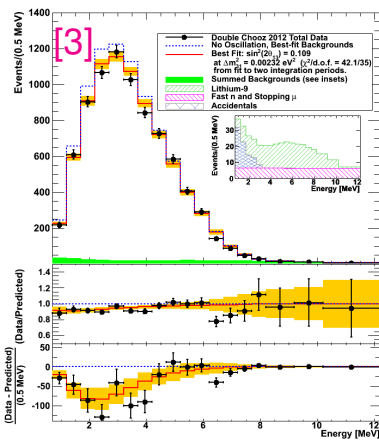
$$D_{\text{vac}} = \frac{1}{2E_\nu} \left[\text{diag} (0, \Delta m_{21}^2, \Delta m_{31}^2) + \cancel{m_1^2} \right]; \quad V_{\text{mat}} = \sqrt{2} G_F N_e \text{diag} (1, 0, 0).$$

6 parameters \iff 6 types of experiments

- SOLAR** sector:
 - solar experiments (mainly SNO) $\longrightarrow \theta_{12}$
 - reactor VLBL (KamLAND) $\longrightarrow \Delta m_{21}^2$
- REACT** sector:
 - reactor LBL (Double-Chooz, Daya-Bay, Reno) $\longrightarrow \theta_{13}$
- ATMOS** sector:
 - atmospheric experiments (SK) $\longrightarrow \theta_{23}$
 - accelerator LBL-DIS (Minos $\nu_\mu \rightarrow \nu_\mu$) $\longrightarrow \Delta m_{31}^2$
 - accelerator LBL-APP (Minos $\nu_\mu \rightarrow \nu_e$, T2K) $\longrightarrow \delta_{\text{CP}}$

Reactor sector: the 2012 revolution

- Until summer 2011, only CHOOZ [1] and PALO-VERDE [2] **upper limits** available;
- since then: **positive signal** from DOUBLE-CHOOZ [3], DAYA-BAY [4], RENO [5];
- present status: $\theta_{13} \neq 0 @ 9\sigma$ after inclusion of the data presented at Neutrino 2012.



[1] M. Apollonio *et al.* [CHOOZ], *Eur. Phys. J. C* **27** (2003) 331 [hep-ex/0301017].

[2] F. Boehm *et al.* [PALO-VERDE], *Phys. Rev. D* **64** (2001) 112001 [hep-ex/0107009].

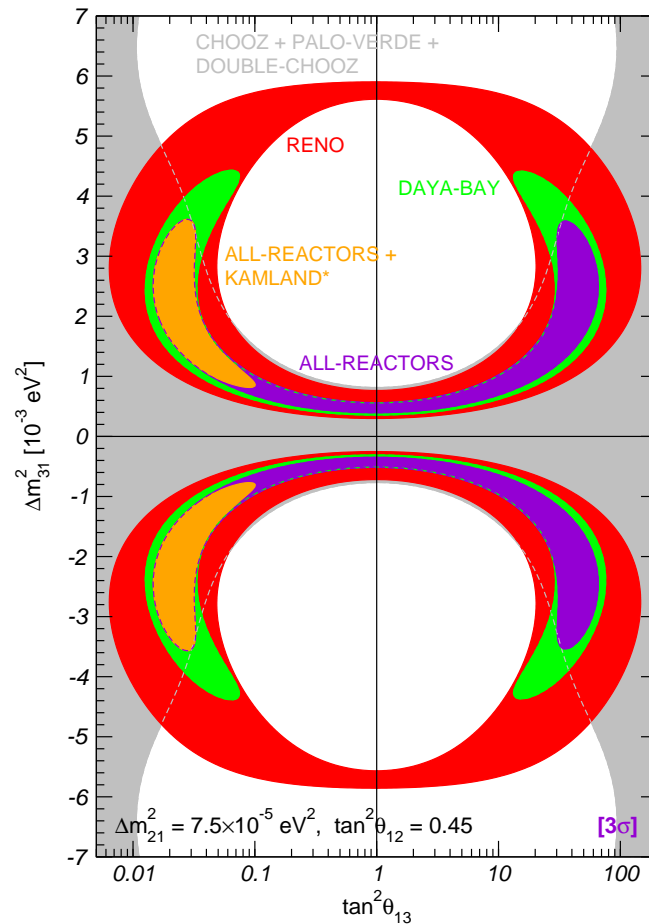
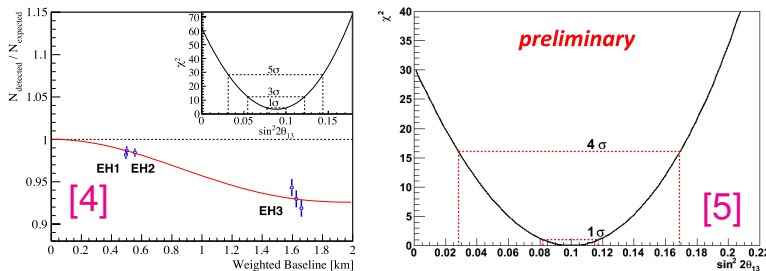
[3] M. Ishitsuka [DOUBLE-CHOOZ], talk presented at Neutrino 2012, Kyoto, Japan, June 3-9, 2012.

[4] D. Dwyer [DAYA-BAY], talk presented at Neutrino 2012, Kyoto, Japan, June 3-9, 2012.

[5] S.H. Seo [RENO], talk presented at Neutrino Telescopes 2013, Venice, Italy, March 11-15, 2013.

Measuring Δm_{31}^2 with reactors only

- Sizable deficit at the **far** detector \Rightarrow oscillations \Rightarrow **lower** bound on θ_{13} and Δm_{31}^2 ;
- smaller deficit at the **near** detector \Rightarrow not-too-much oscillations \Rightarrow **upper** bound on Δm_{31}^2 ;
- KamLAND spectrum \Rightarrow **upper** bound on θ_{13} .



[4] D. Dwyer [DAYA-BAY], talk presented at Neutrino 2012, Kyoto, Japan, June 3-9, 2012.

[5] S.H. Seo [RENO], talk presented at Neutrino Telescopes 2013, Venice, Italy, March 11-15, 2013.

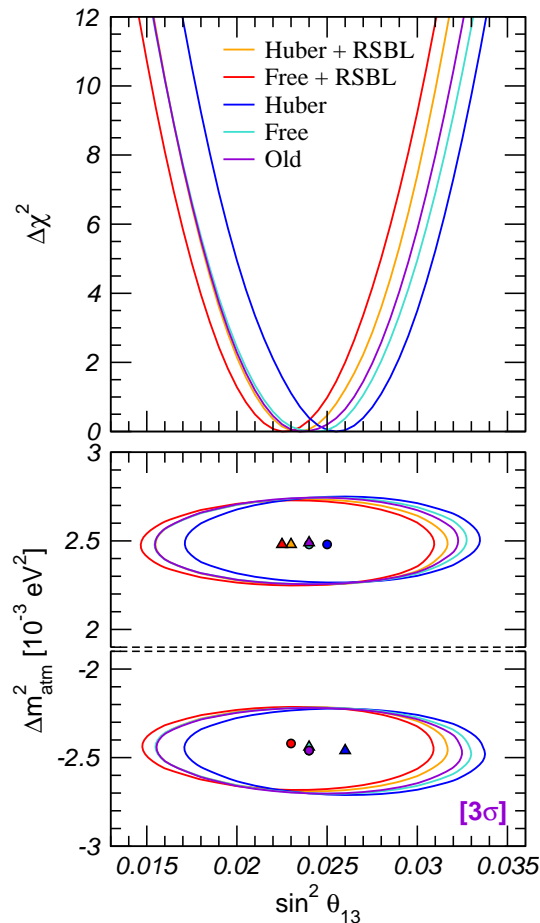
Impact of the reactor neutrino fluxes

- Analysis of reactor data require a precise knowledge of the reactor ν fluxes. We follow two approaches:
 - use the **flux calculations** presented in [7];
 - treat the fluxes as **free parameters** and fit them;
- The **reactor fluxes** in [6, 7] are quite **large**, hence they favor **large** suppression \Rightarrow **larger** θ_{13} ;
- including reactor short-baseline (**RSBL**) experiments in the fit [8] results in **smaller** fluxes \Rightarrow **smaller** θ_{13} ;
- once **RSBL** data are included, the specific prior on the reactor fluxes (**fixed** or **free**) has little impact;
- θ_{13} uncertainty from fluxes: $\delta(\sin^2 \theta_{13}) = \pm 0.002$.

[6] Mueller *et al.*, PRC **83** (2011) 054615 [arXiv:1101.2663].

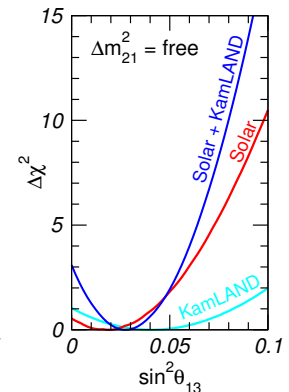
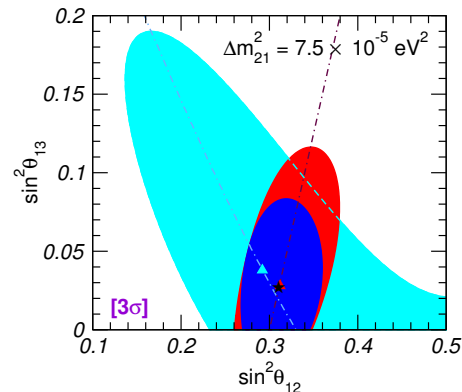
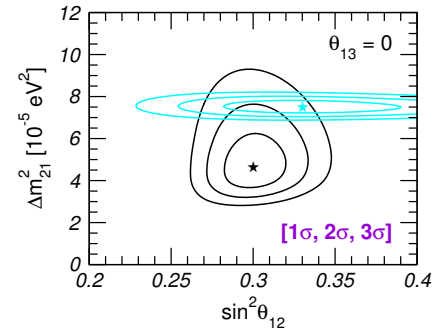
[7] Huber, PRC **84** (2011) 024617 [arXiv:1106.0687].

[8] Schwetz *et al.*, NJP **13** (2011) 063004 [arXiv:1103.0734].



Solar sector: effect of θ_{13} on SOL & KAM data

- For $\theta_{13} = 0$, we have $\sin^2 \theta_{12} = \begin{cases} 0.30 & \text{from solar data,} \\ 0.33 & \text{from KamLAND data;} \end{cases}$
- When θ_{13} increases:
 - KamLAND region definitely shifts to smaller θ_{12} ;
 - solar region slightly moves to larger θ_{12} (high-E data dominate over low-E ones);
- therefore, a non-zero value of θ_{13} reduces the tension between solar and KamLAND data [9, 10];
- new SNO (I+II+III) analysis favor smaller $\phi_{CC}/\phi_{NC} \Rightarrow$ smaller θ_{12} from solar \Rightarrow tension with KamLAND is increased \Rightarrow larger θ_{13} is preferred.

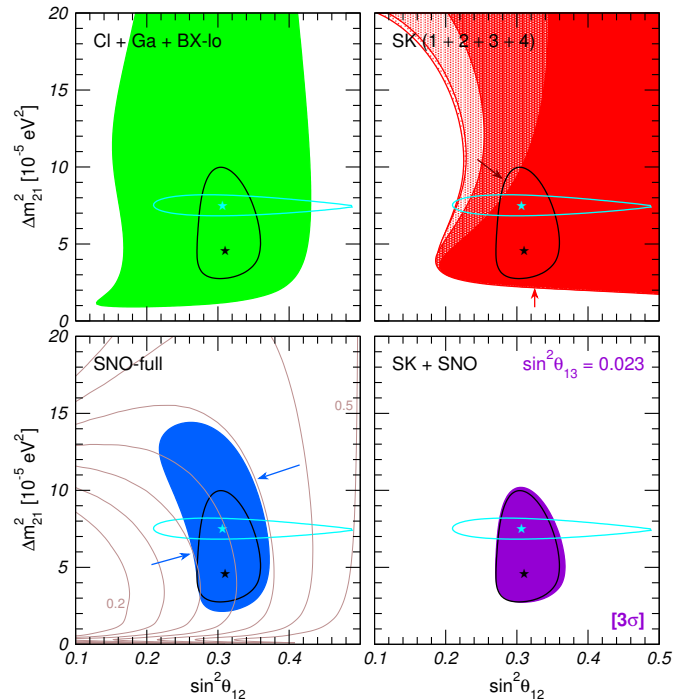


[9] G.L. Fogli *et al.*, Phys. Rev. Lett. **101** (2008) 141801 [arXiv:0806.2649].

[10] T. Schwetz, M.A. Tortola, J.W.F. Valle, New J. Phys. **10** (2008) 113011 [arXiv:0808.2016].

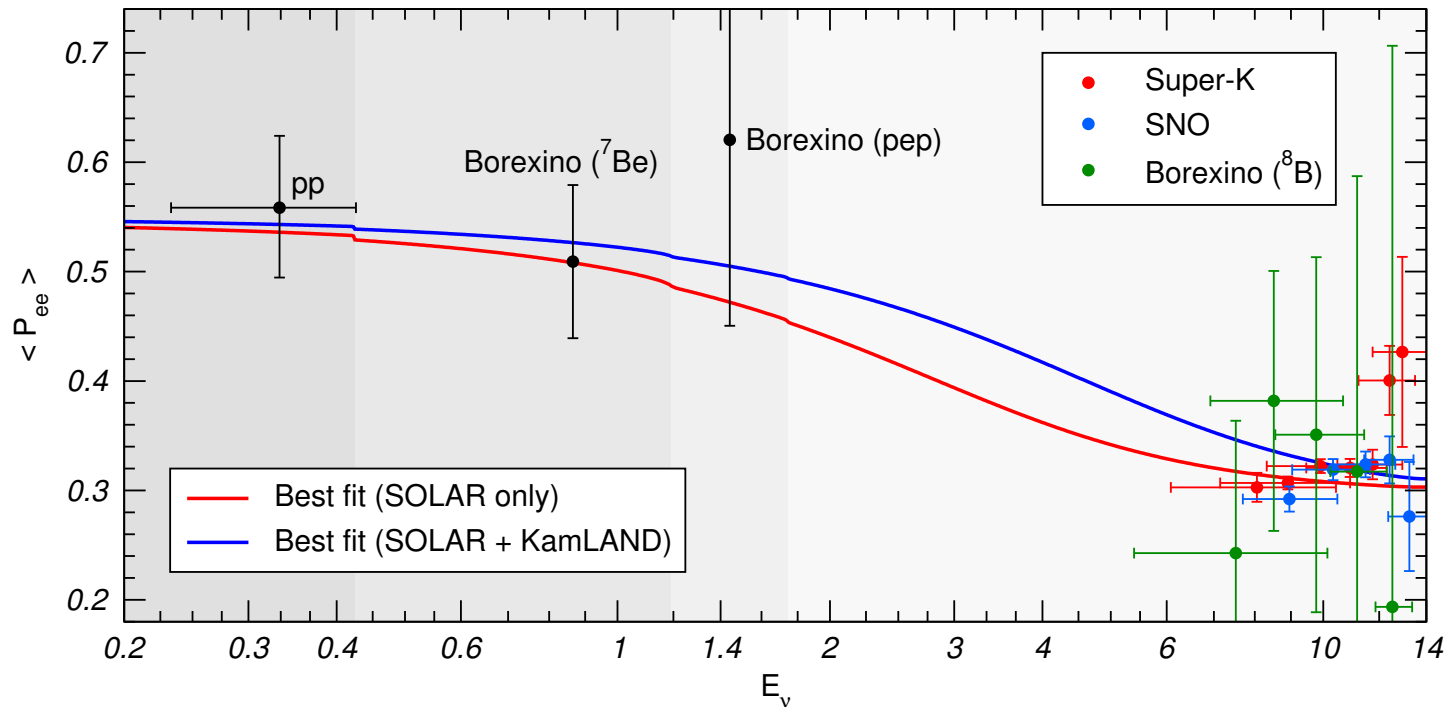
Relevance of solar data in the determination of Δm_{21}^2 and θ_{12}

- $P_{ee} = c_{13}^4 P_{\text{eff}} + s_{13}^4$, $i \frac{d\vec{\nu}}{dt} = \left[\frac{\Delta m_{21}^2}{4E_\nu} \begin{pmatrix} -\cos 2\theta_{12} & \sin 2\theta_{12} \\ \sin 2\theta_{12} & \cos 2\theta_{12} \end{pmatrix} \pm \sqrt{2} G_F N_e \begin{pmatrix} c_{13}^2 & 0 \\ 0 & 0 \end{pmatrix} \right] \vec{\nu}$, $\vec{\nu} = \begin{pmatrix} \nu_e \\ \nu_a \end{pmatrix}$;
- $\nu_\mu \equiv \nu_\tau \Rightarrow$ no sensitivity to θ_{23} and δ_{CP} ;
- $\Delta m_{31}^2 \approx \infty \Rightarrow$ specific Δm_{31}^2 value irrelevant;
- \Rightarrow data only depend on Δm_{21}^2 , θ_{12} and θ_{13} ;
- $P_{ee} \approx \begin{cases} \text{Kam: } \cos^4 \theta_{13} \left(1 - \sin^2 2\theta_{12} \sin^2 \frac{\Delta m_{21}^2 L}{4E} \right), \\ \text{low-E: } \cos^4 \theta_{13} \left(1 - \frac{1}{2} \sin^2 2\theta_{12} \right), \\ \text{high-E: } \cos^4 \theta_{13} \sin^2 \theta_{12}; \end{cases}$
- param's: $\begin{cases} \theta_{12} \text{ dominated by SNO;} \\ \Delta m_{21}^2 \text{ dominated by KamLAND;} \end{cases}$
- solar region determined by high-E data, low-E contribution marginal;
- residual tension between solar and KamLAND not statistically significant.



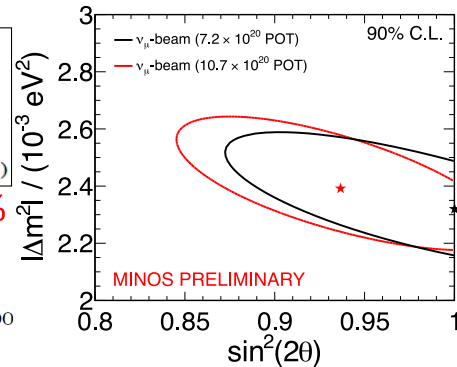
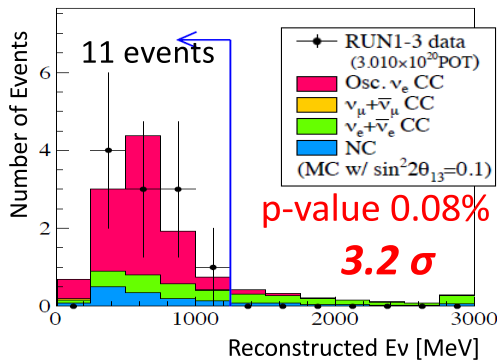
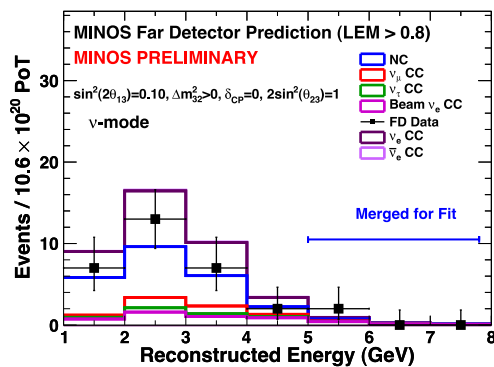
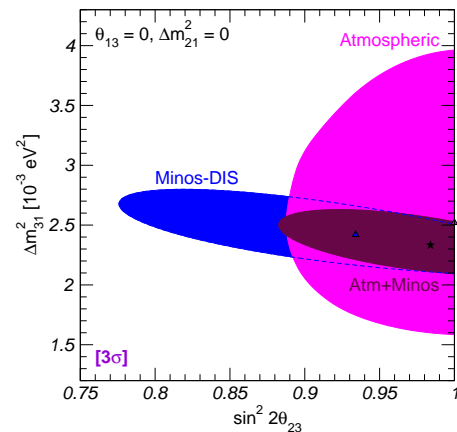
Transition between vacuum and MSW regime in solar data

- Tension between solar and KamLAND related to non-observation of low-E turn-up.



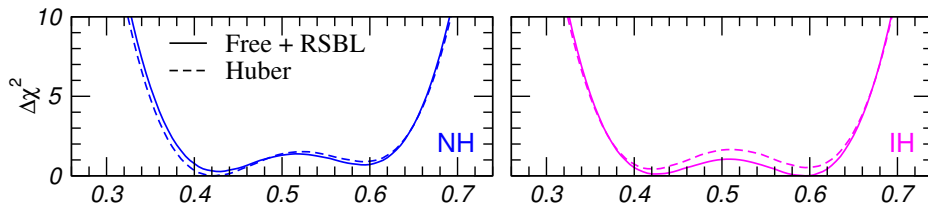
Atmospheric sector: general overview

- Δm_{31}^2 is now determined by **Minos-DIS** ($\nu_\mu \rightarrow \nu_\mu$) data;
- θ_{23} still dominated by **SK atmospheric** data;
- θ_{13} & δ_{CP} mostly visible in appearance ($\nu_\mu \rightarrow \nu_e$) data; hints of $\theta_{13} \neq 0$ from Minos-APP (2.1σ) and T2K (3.2σ);
- Δm_{21}^2 effects visible but only at subleading level;
- ★ **new result**: Minos disappearance data now slightly favor non-maximal θ_{23} mixing.

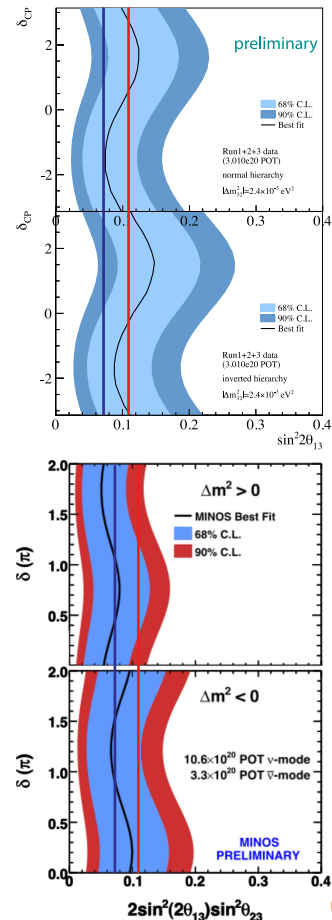


Octant discrimination with REA+LBL data

- In principle, REA + LBL-APP + LBL-DIS can fix the octant [11]:
 - REACTORS: measure $\sin^2(2\theta_{\text{rea}}) \equiv \sin^2(2\theta_{13})$;
 - LBL-DIS: measure $\sin^2(2\theta_{\text{dis}})$, with $\sin^2 \theta_{\text{dis}} \equiv \cos^2 \theta_{13} \sin^2 \theta_{23}$;
 - LBL-APP: measure $\sin^2(2\theta_{\text{app}}) \equiv \sin^2(2\theta_{13}) 2 \sin^2 \theta_{23}$ and δ_{CP} ;
- in practice, putting explicit numbers:
 - from REACTORS: $\sin^2(2\theta_{13}) \simeq 0.09$;
 - from LBL-DIS: $\sin^2(2\theta_{\text{dis}}) \simeq 0.96$ implies $\sin^2 \theta_{23} = 0.41$ or 0.61 ;
 - hence, REA + LBL-DIS imply $\sin^2(2\theta_{\text{app}}) = 0.074$ or 0.110 ;
- both values of $\sin^2(2\theta_{\text{app}})$ are in similar agreement with LBL-APP.



[11] G.L. Fogli *et al.*, Phys. Rev. D **86** (2012) 013012 [arXiv:1205.5254].



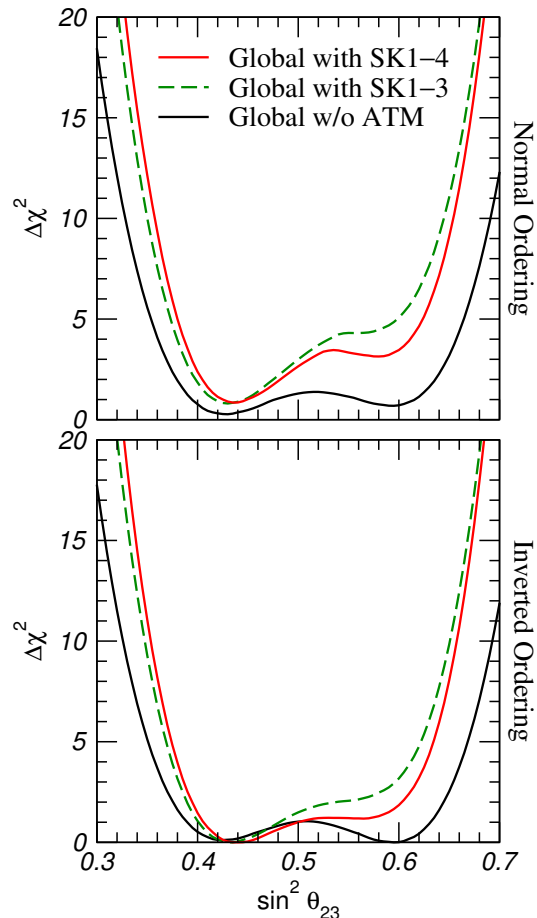
Octant and hierarchy: present status

θ_{23} octant

- Deviation of θ_{23} from maximal mixing is a **physical effect**, which follows from:
 - excess of events in sub-GeV *e-like* data;
 - zenith distortion in multi-GeV *e-like* data;
- the effect is not statistically significant, but it is well understood and clearly visible;
- found also by other Fogli *et al.* [11], but **not** by SK.

Mass hierarchy

- Matter effects enhanced for larger $\theta_{13} \Rightarrow$ sensitive to specific range of θ_{13} ;
- no meaningful preference for NH or for IH.



[11] G.L. Fogli *et al.*, PRD **86** (2012) 013012 [arXiv:1205.5254].

Neutrino oscillations: where we are

- Global 6-parameter fit (including δ_{CP}):
 - **Solar**: Cl + Ga + SK(1–4) + SNO-full (I+II+III) + Borexino;
 - **Atmospheric**: SK-1 + SK-2 + SK-3 + SK-4;
 - **Reactor**: KamLAND + Chooz + Palo-Verde
+ Double-Chooz + Daya-Bay + Reno;
 - **Accelerator**: Minos (DIS+APP) + T2K (DIS+APP);
- best-fit point and 1σ (3σ) ranges:

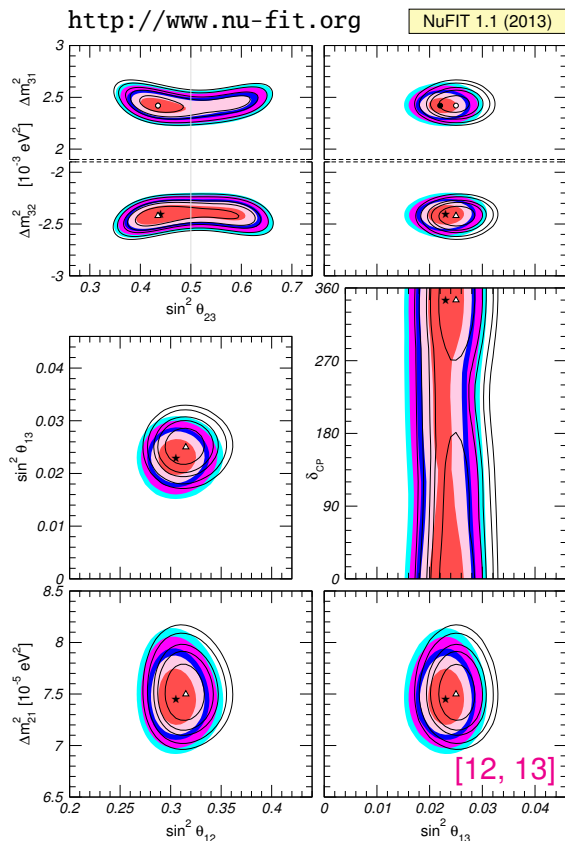
$$\theta_{12} = 33.57_{-0.75}^{+0.77} \left({}_{-2.19}^{+2.44} \right), \quad \Delta m_{21}^2 = 7.45_{-0.16}^{+0.19} \left({}_{-0.47}^{+0.60} \right) \times 10^{-5} \text{ eV}^2,$$

$$\theta_{23} = 41.4_{-1.8}^{+3.5} \left({}_{-4.7}^{+12.6} \right), \quad \Delta m_{31}^2 = \begin{cases} -2.403_{-0.063}^{+0.062} \left({}_{-0.193}^{+0.184} \right) \times 10^{-3} \text{ eV}^2, \\ +2.421_{-0.023}^{+0.022} \left({}_{-0.173}^{+0.191} \right) \times 10^{-3} \text{ eV}^2, \end{cases}$$

$$\theta_{13} = 8.75_{-0.44}^{+0.42} \left({}_{-1.46}^{+1.21} \right), \quad \delta_{\text{CP}} = 341_{-46}^{+58} \text{ (any)};$$

- neutrino mixing matrix:

$$|U|_{3\sigma} = \begin{pmatrix} 0.799 \rightarrow 0.844 & 0.515 \rightarrow 0.581 & 0.127 \rightarrow 0.173 \\ 0.218 \rightarrow 0.533 & 0.430 \rightarrow 0.719 & 0.591 \rightarrow 0.800 \\ 0.222 \rightarrow 0.534 & 0.431 \rightarrow 0.720 & 0.582 \rightarrow 0.793 \end{pmatrix}.$$



[12] M.C. Gonzalez-Garcia *et al.*, JHEP **12** (2012) 123 [arXiv:1209.3023].

[13] M.C. Gonzalez-Garcia *et al.*, NuFIT 1.1 (2013), <http://www.nu-fit.org>.

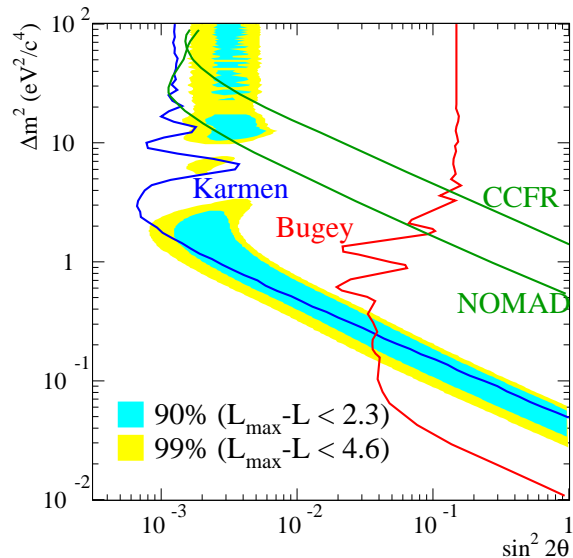
The LSND problem

- LSND observed $\bar{\nu}_e$ appearance in a $\bar{\nu}_\mu$ beam ($E_\nu \sim 30$ MeV, $L \simeq 35$ m);
- Karmen did not confirm the claim, but couldn't fully exclude it either;
- the signal is compatible with $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ oscillations provided that $\Delta m^2 \gtrsim 0.1$ eV²;
- on the other hand, other data give (at 3σ):

$$\Delta m_{\text{SOL}}^2 \simeq 7.5 \pm 0.6 \times 10^{-5} \text{ eV}^2,$$

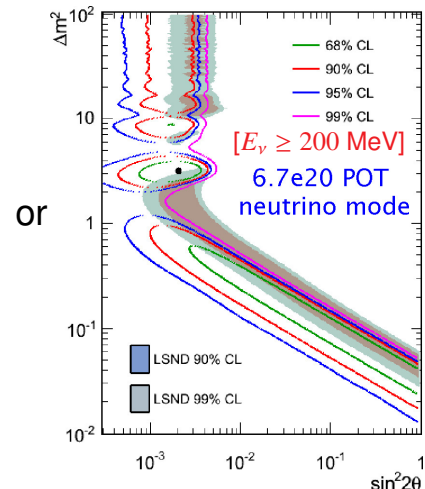
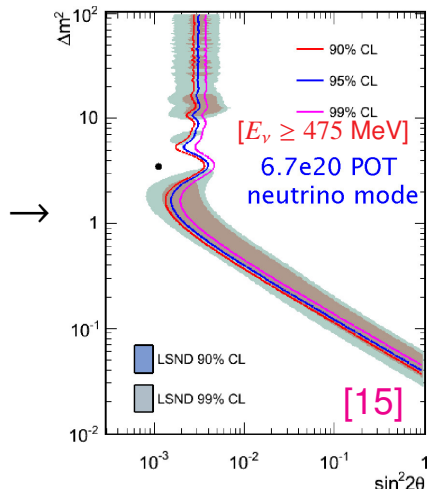
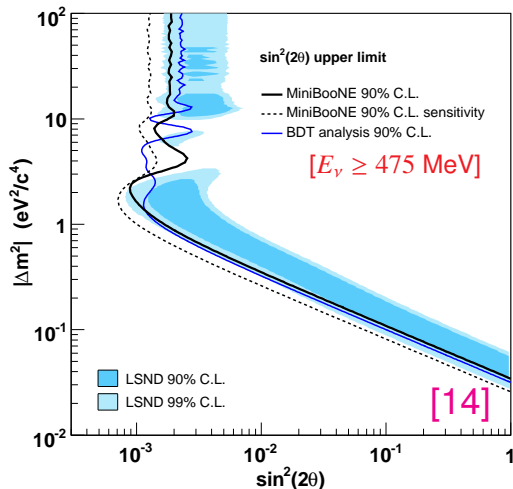
$$|\Delta m_{\text{ATM}}^2| \simeq 2.4 \pm 0.3 \times 10^{-3} \text{ eV}^2;$$

- in order to explain LSND with mass-induced neutrino oscillations one needs *at least one more* neutrino mass eigenstate;
- to check the LSND claim once and for all, the MiniBooNE experiment was built, with very different E_ν and L but similar L/E_ν .



MiniBooNE results: neutrino data

- Statistics: 5.58 (2007) \rightarrow 6.46 (2008) $\times 10^{20}$ POT, then just improved analysis;
- is ν signal compatible with 2ν oscillations? $\left\{ \begin{array}{l} 2007: P_{\text{osc}} \simeq 1\% \Rightarrow \text{no it isn't [14];} \\ 2012: P_{\text{osc}} \simeq 6\% \Rightarrow \text{maybe it is [15];} \end{array} \right.$
- do MB ν data rule out the LSND $\bar{\nu}$ signal? 2007: **yes [14]**; 2012: **not really [15]**.

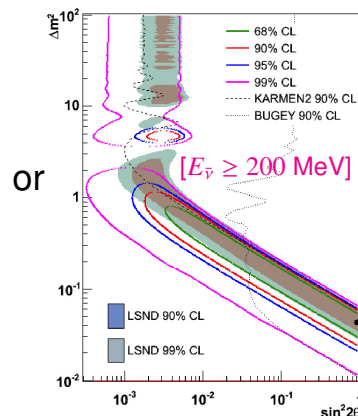
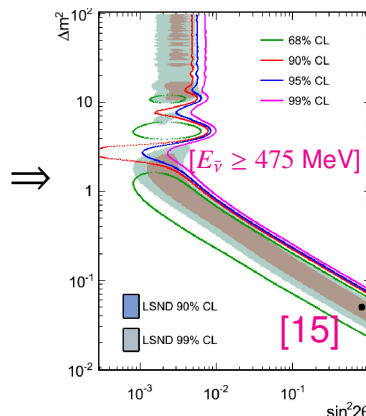
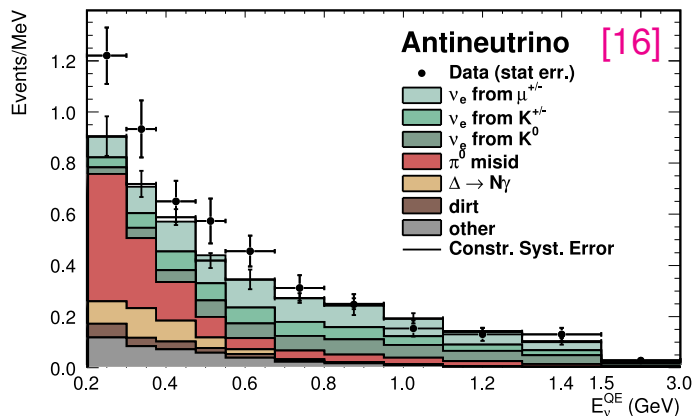


[14] A.A. Aguilar-Arevalo *et al.* [MiniBooNE collab], Phys. Rev. Lett. **98** (2007) 231801 [arXiv:0704.1500].

[15] C. Polly, talk at Neutrino 2012, Kyoto, Japan, June 3-9, 2012.

MiniBooNE results: antineutrino data

- New data presented at Neutrino 2012, statistics doubled ($\rightarrow 11.27 \times 10^{20}$ POT) [15];
- compatibility with ν data: $\left\{ \begin{array}{l} \text{low-energy excess increased} \Rightarrow \text{better agreement;} \\ \text{mid-energy excess reduced} \Rightarrow \text{better agreement;} \end{array} \right.$
- is $\bar{\nu}$ signal compatible with 2ν oscillations? $P_{\text{osc}} = 67.5\% \Rightarrow$ definitely yes [15, 16];
- is MB- $\bar{\nu}$ signal compatible with LSND? Yes, irrespective of the energy threshold.

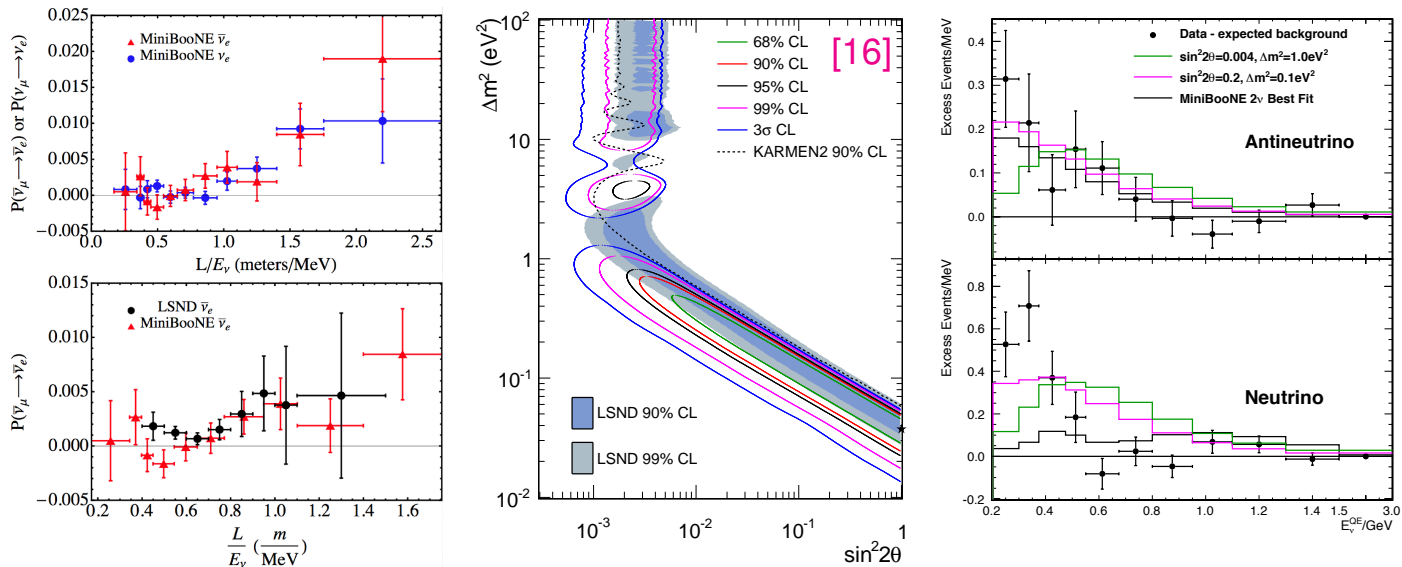


[15] C. Polly, talk at Neutrino 2012, Kyoto, Japan, June 3-9, 2012.

[16] A.A. Aguilar-Arevalo et al. [MiniBooNE collab], arXiv:1207.4809 [hep-ex].

MiniBooNE results: global $\nu + \bar{\nu}$ appearance

- MiniBooNE ν and $\bar{\nu}$ no longer in open disagreement with LSND;
- however, dramatic change in interpretation **not** linked to dramatic change in data;
- problems still there ($P_{\text{osc}} \simeq 6.7\%$ [16]).



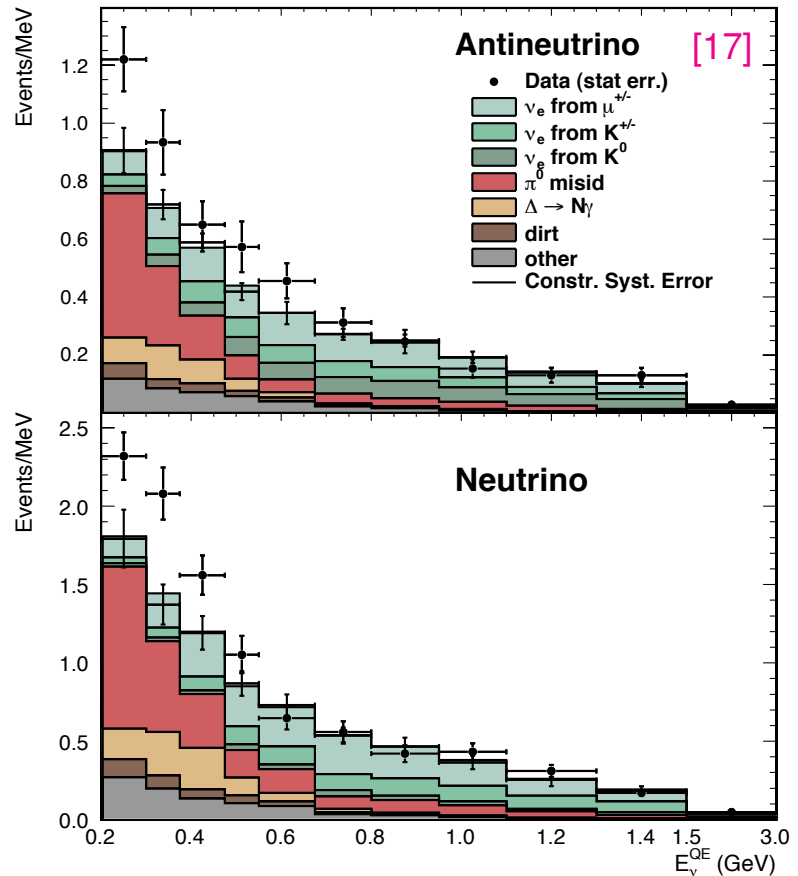
[16] A.A. Aguilar-Arevalo *et al.* [MiniBooNE collab], arXiv:1207.4809 [hep-ex].

The MiniBooNE excess

- MiniBooNE observed an overall 3.8σ excess, mostly at low energy [17];
- although no longer “*in open disagreement*”, ν and $\bar{\nu}$ signals are not really equivalent either. For example:

$$P_{2\nu} = \begin{cases} 6.1\% & \text{for } \nu; \\ 67.5\% & \text{for } \bar{\nu}; \end{cases}$$

- former omission of low-energy ν bins ($E_\nu^{\text{QE}} < 475$ MeV) based on the hypothesis of **two-flavor oscillations**;
- is it possible to do something better about low-energy data in **more sophisticated** models?



[17] A.A. Aguilar-Arevalo *et al.* [MiniBooNE collab], Phys. Rev. Lett. **110** (2013) 161801 [arXiv:1303.2588].

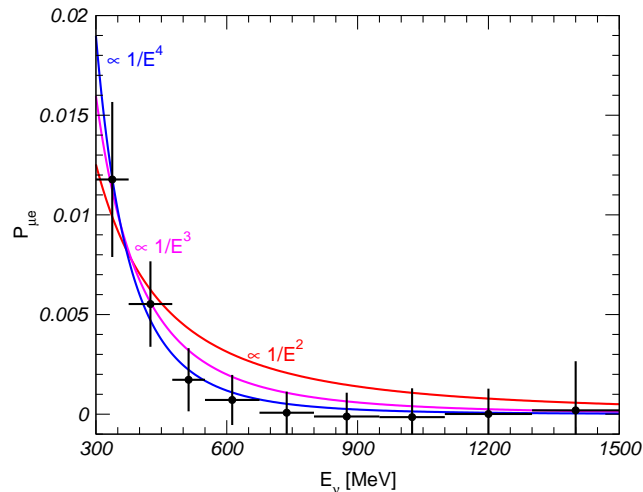
Explaining the MiniBooNE excess with two sterile neutrinos

- With *one* extra sterile neutrino, m_4 :

$$P_{\mu e}^{4\nu} = 4|U_{e4}|^2|U_{\mu4}|^2 \sin^2 \phi_{41} \quad \text{with} \quad \phi_{ij} \equiv \frac{\Delta m_{ij}^2 L}{4E};$$

- for large energy $P_{\mu e}^{4\nu}$ drops as $1/E^2$;
- however, the low-energy MB excess is much sharper ($\sim 1/E^4$);

⇒ **it is very hard to account for the MB excess with only one extra sterile neutrino.**



- On the other hand, with *two* extra neutrinos, m_4 and m_5 :

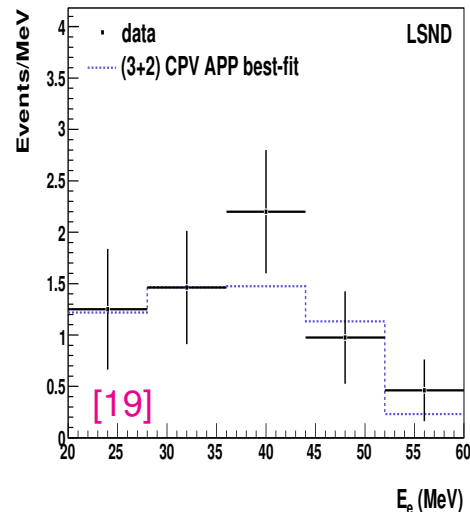
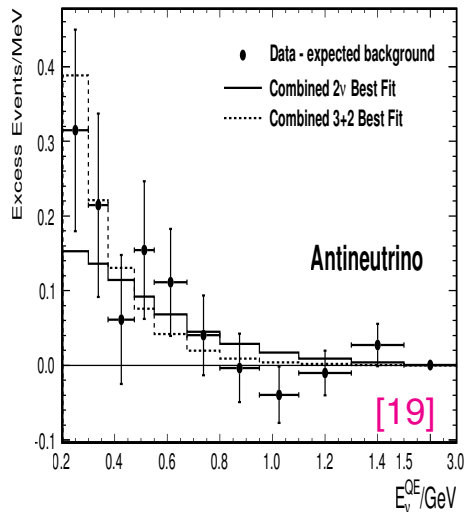
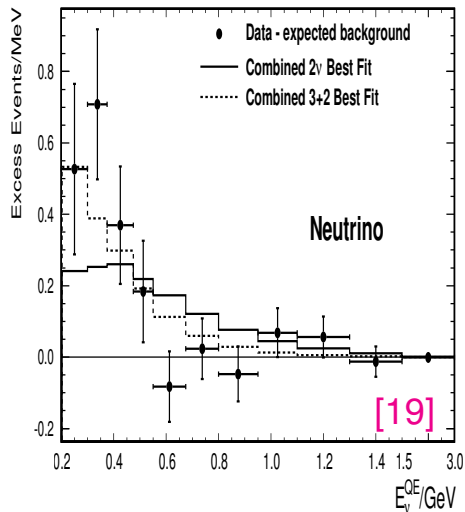
$$P_{\mu e}^{5\nu} = 4|U_{e4}|^2|U_{\mu4}|^2 \sin^2 \phi_{41} + 4|U_{e5}|^2|U_{\mu5}|^2 \sin^2 \phi_{51} + 8|U_{e4}U_{e5}U_{\mu4}U_{\mu5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54} - \delta);$$

- terms of order $1/E^2$ cancel if $\delta = \pi$ and $|U_{e4}U_{\mu4}\Delta m_{41}^2| = |U_{e5}U_{\mu5}\Delta m_{51}^2|$;

⇒ **with two extra sterile states it is possible to fit the MB low-energy excess [18].**

[18] M. Maltoni, T. Schwetz, Phys. Rev. **D76** (2007) 093005 [arXiv:0705.0107].

Reconciling MiniBooNE and LSND in (3+2) models



- **Trick:** use the CP phase $\delta = \arg(U_{e4}^* U_{\mu 4} U_{e5} U_{\mu 5}^*)$ to differentiate ν (MB) from $\bar{\nu}$ (LSND):

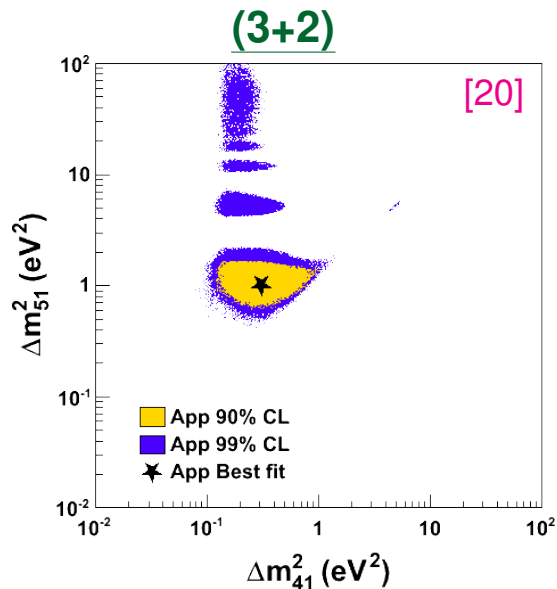
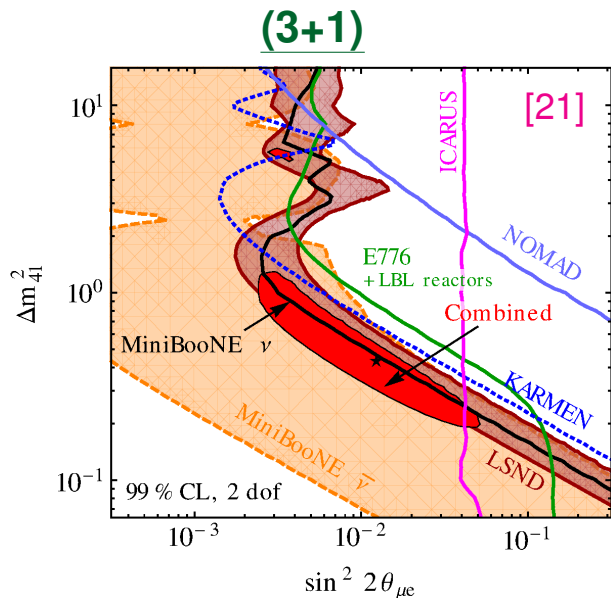
$$P_{\mu e}^{5\nu} = 4|U_{e4}|^2|U_{\mu 4}|^2 \sin^2 \phi_{41} + 4|U_{e5}|^2|U_{\mu 5}|^2 \sin^2 \phi_{51} + 8|U_{e4} U_{e5} U_{\mu 4} U_{\mu 5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54} - \delta);$$

- note that $\delta = \pi + \epsilon$ and $|U_{e4} U_{\mu 4}| \Delta m_{41}^2 \approx |U_{e5} U_{\mu 5}| \Delta m_{51}^2$ to suppress MB probability [18].

[18] M. Maltoni, T. Schwetz, Phys. Rev. **D76** (2007) 093005 [arXiv:0705.0107].

[19] J.M. Conrad, W.C. Louis, M.H. Shaevitz, Ann. Rev. Nucl. Part. Sci. **63** (2013) 45 [arXiv:1306.6494].

Fitting all $\nu_\mu \rightarrow \nu_e$ appearance data: (3+1) vs (3+2) models



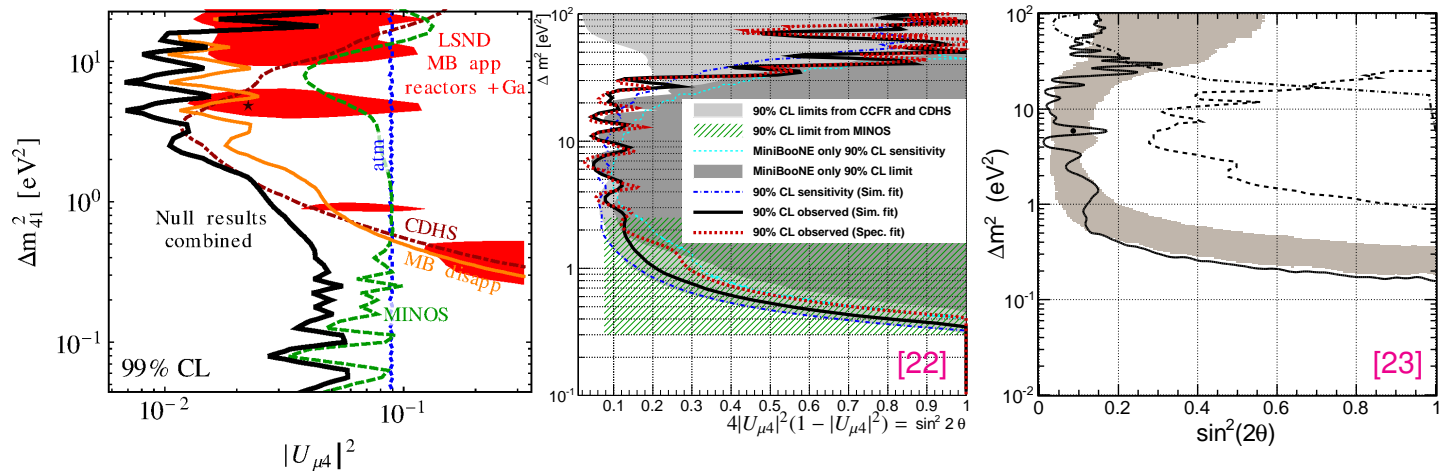
- $\chi^2_{\min}/\text{dof} = 87.9/(68 - 2) \Rightarrow \text{GOF} = 3.7\%$;
- $\chi^2_{\min}/\text{dof} = 72.7/(68 - 5) \Rightarrow \text{GOF} = 19\%$;
- the improvement of (3+2) over (3+1) is $\chi^2_{(3+1),\text{app}} - \chi^2_{(3+2),\text{app}} = 15.2$ [21].

[20] J.M. Conrad *et al.*, *Adv. High Energy Phys.* **2013** (2013) 163897 [arXiv:1207.4765].

[21] J. Kopp, P.A.N. Machado, M. Maltoni, T. Schwetz, *JHEP* **05** (2013) 050 [arXiv:1303.3011].

ν_μ disappearance: combined MiniBooNE & SciBooNE analysis

- In addition to atmospheric and MINOS data, a combined analysis of MiniBooNE & SciBooNE data has recently been presented, for both ν [22] and $\bar{\nu}$ [23];
- no hint of ν_μ disappearance has been found in either case, thus strengthening the bound in the large- Δm^2 region ($\Delta m_{41}^2 \gtrsim 1 \text{ eV}^2$).

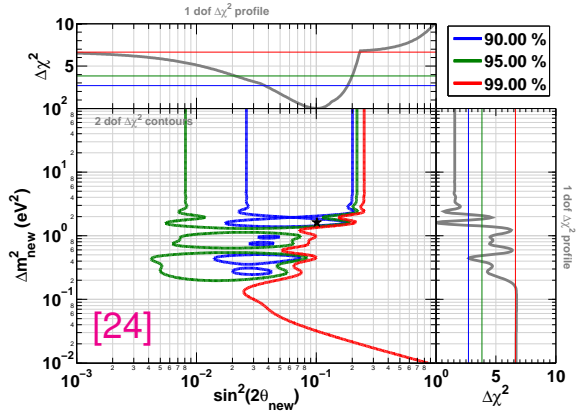
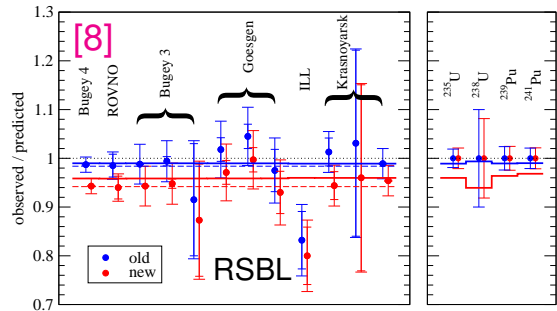


[22] K.B.M. Mahn *et al.* [SciBooNE & MiniBooNE collab], Phys. Rev. D **85** (2012) 032007 [arXiv:1106.5685].

[23] G. Cheng *et al.* [MiniBooNE & SciBooNE collab], Phys. Rev. D **86** (2012) 052009 [arXiv:1208.0322].

ν_e disappearance: the reactor anomaly

- In [6, 7] the reactor $\bar{\nu}$ fluxes was reevaluated;
 - the new calculations result in a small increase of the flux by about **3.5%**;
 - hence, **all** reactor short-baseline (RSBL) finding **no evidence** are actually **observing a deficit**;
 - this deficit **could** be interpreted as being due to SBL neutrino oscillations;
 - no visible dependence on $L \Rightarrow \Delta m^2 \gtrsim 1 \text{ eV}^2$;
- \Rightarrow new “hint” in favor of SBL oscillations, **independent** of LSND & MiniBooNE.



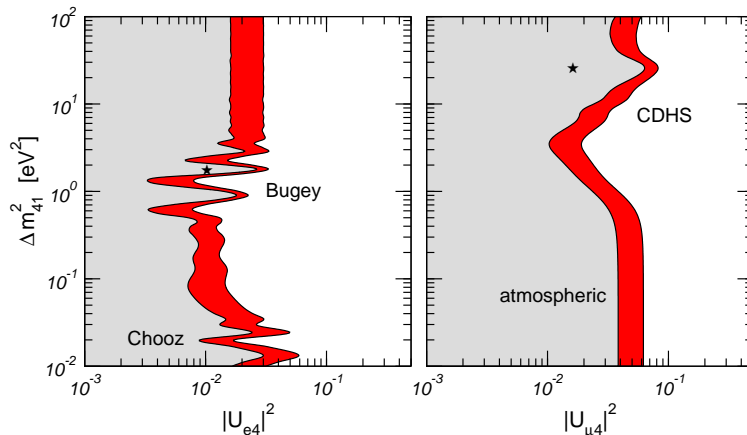
[6] T.A. Mueller *et al.*, Phys. Rev. **C83** (2011) 054615 [arXiv:1101.2663].
 [7] P. Huber, Phys. Rev. C **84** (2011) 024617 [arXiv:1106.0687].
 [8] T. Schwetz, M. Tortola, J.W.F. Valle, New J. Phys. **13** (2011) 063004 [arXiv:1103.0734].
 [24] G. Mention *et al.*, Phys. Rev. **D83** (2011) 073006 [arXiv:1101.2755].

**Disappearance data:
present status**

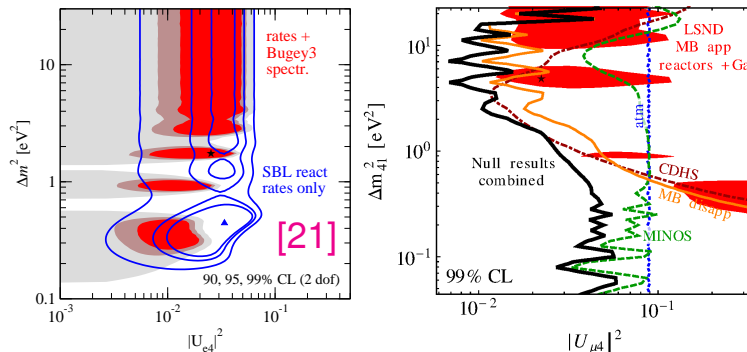
- As expected, the new reactor fluxes lead to a clear preference for $|U_{e4}|^2 \neq 0$;
- however, the upper bound on $|U_{e4}|^2$ is **not** dramatically reduced;
- combined with the limit on $|U_{\mu 4}|^2$, this implies an upper limit on $|U_{e4}U_{\mu 4}| \Rightarrow$ tension with appearance data;
- for (3+2) models the situation is qualitatively the same, except that $|U_{e5}|$ and $|U_{\mu 5}|$ are also involved.

[21] J. Kopp, P.A.N. Machado *et al.*, JHEP 05 (2013) 050 [arXiv:1303.3011].

Old reactor fluxes

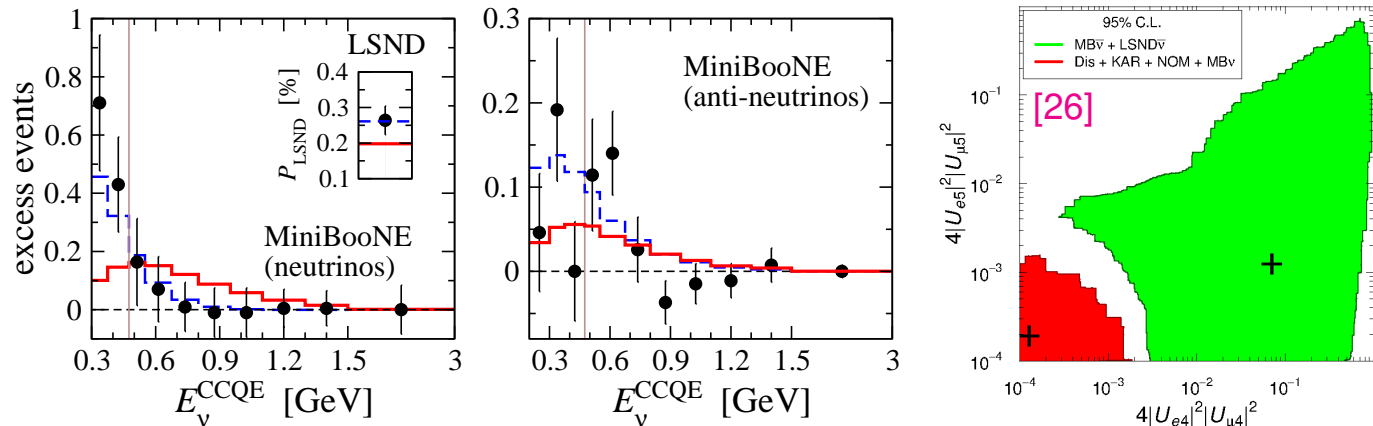


New reactor fluxes & MINOS



Status of (3+2) models from global data

- (3+2) models suffer from severe tension between APP and DIS data: PG=0.53% [25];
- the situation worsen when MiniBooNE low-E data are included: PG=0.0035% [21];
- (1+3+1) works slightly better (PG=0.21% [21]), but has stronger problems with cosmology since the sum of neutrino masses ($\sum m_\nu$) is larger.



[21] J. Kopp, P.A.N. Machado, M. Maltoni, T. Schwetz, JHEP **05** (2013) 050 [arXiv:1303.3011].

[25] J. Kopp, M. Maltoni and T. Schwetz, Phys. Rev. Lett. **107** (2011) 091801 [arXiv:1103.4570].

[26] C. Giunti, M. Laveder, Phys. Rev. D **84** (2011) 073008 [arXiv:1107.1452].

- Most of the present data from **solar**, **atmospheric**, **reactor** and **accelerator** experiments are well explained by the 3ν oscillation hypothesis;
- however, a few experiments exhibit deviations from the “standard” 3ν scenario:
 - **LSND** observed an excess of $\bar{\nu}_e$ events in a $\bar{\nu}_\mu$ beam;
 - **MiniBooNE** mildly “confirm” this excess: $\left\{ \begin{array}{l} \text{in both } \bar{\nu} \text{ mode and } \nu \text{ mode at low-E;} \\ \text{only in } \bar{\nu} \text{ mode at mid-E;} \end{array} \right.$
 - new fission $\bar{\nu}$ fluxes suggests that **all** SBL **reactor** experiments are observing a deficit;
- however, these “hints” for sterile neutrinos are **not** in agreement among them:
 - **MiniBooNE** asymmetry in $\nu/\bar{\nu}$ requires CP violation, hence at least **two sterile ν 's**;
 - (3+2) models reconcile **APP** data, but **DIS** ones still show strong tension;
 - attempts to include the low-E excess in the game further increase such tension;
 - new **reactor** fluxes reduce tension with **DIS** data only marginally;

⇒ **we are still quite far from the solution of the LSND puzzle!**