

# Hadroproduction measurements for simulations of neutrino beams

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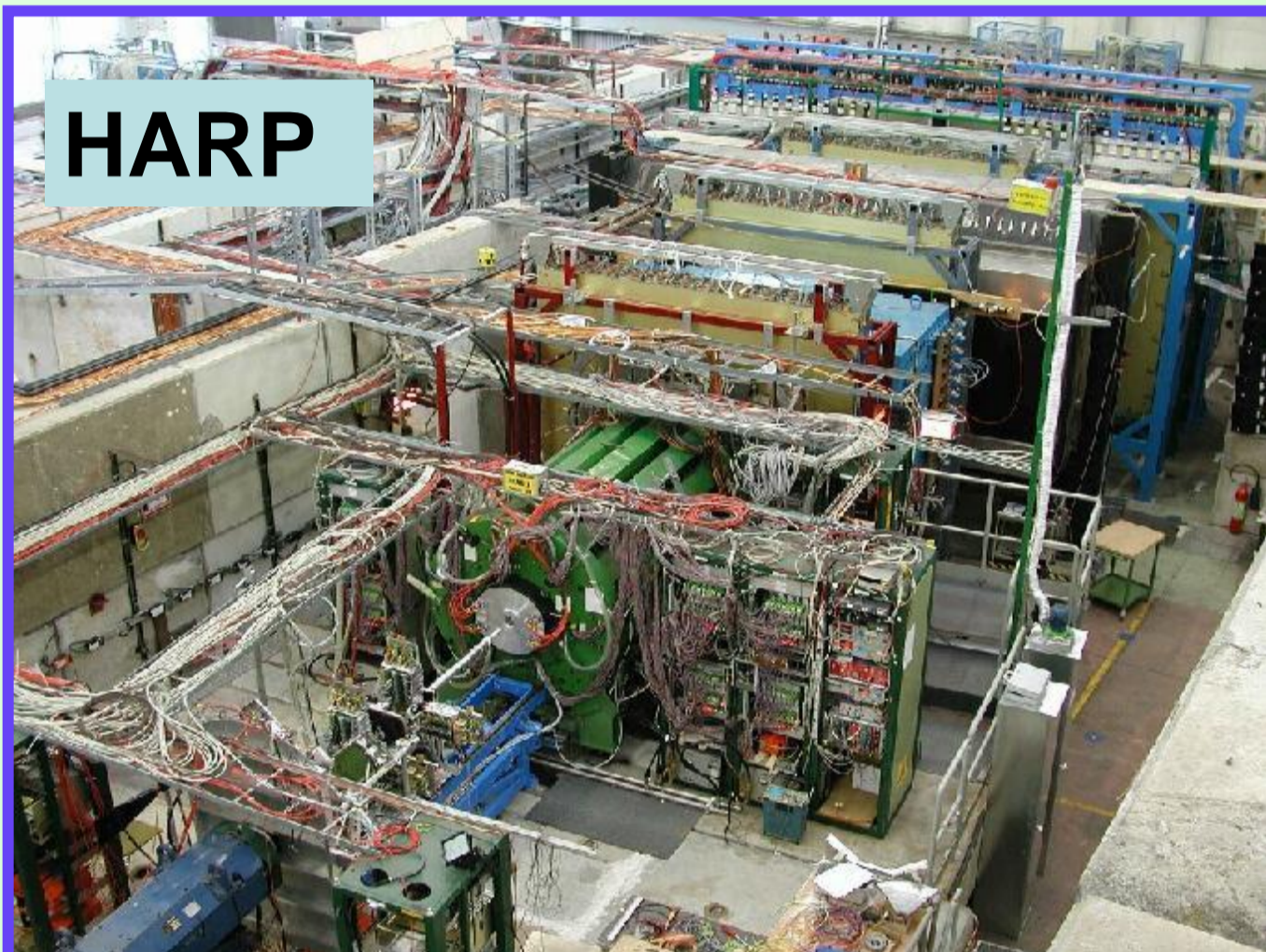
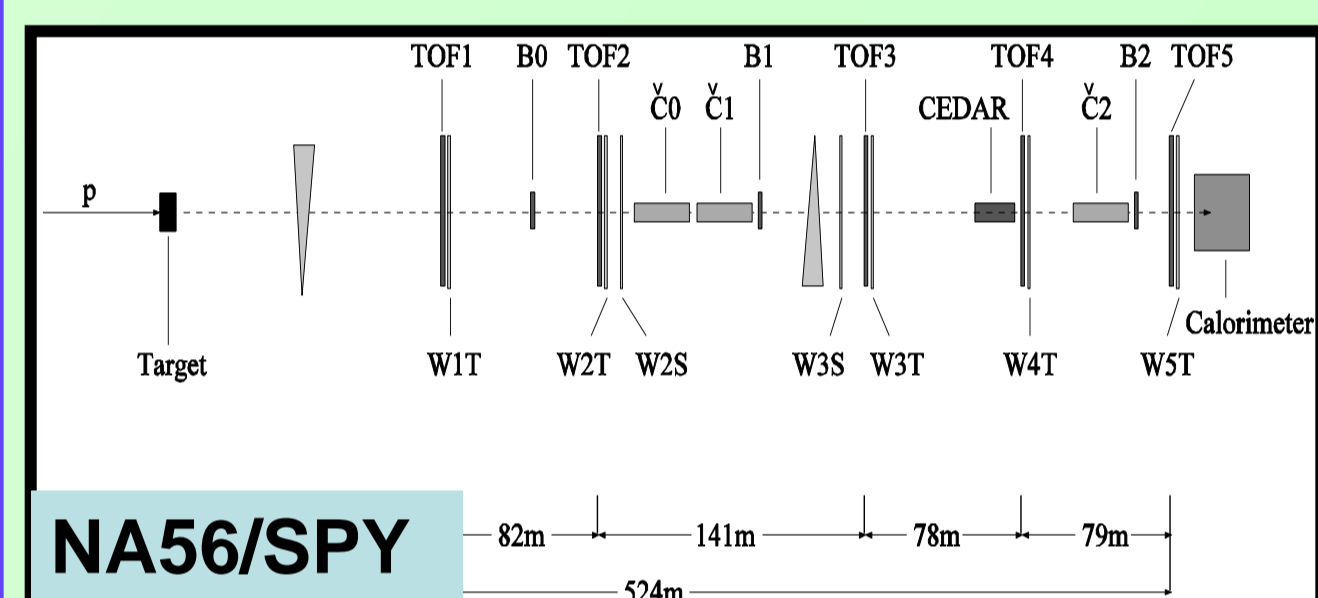
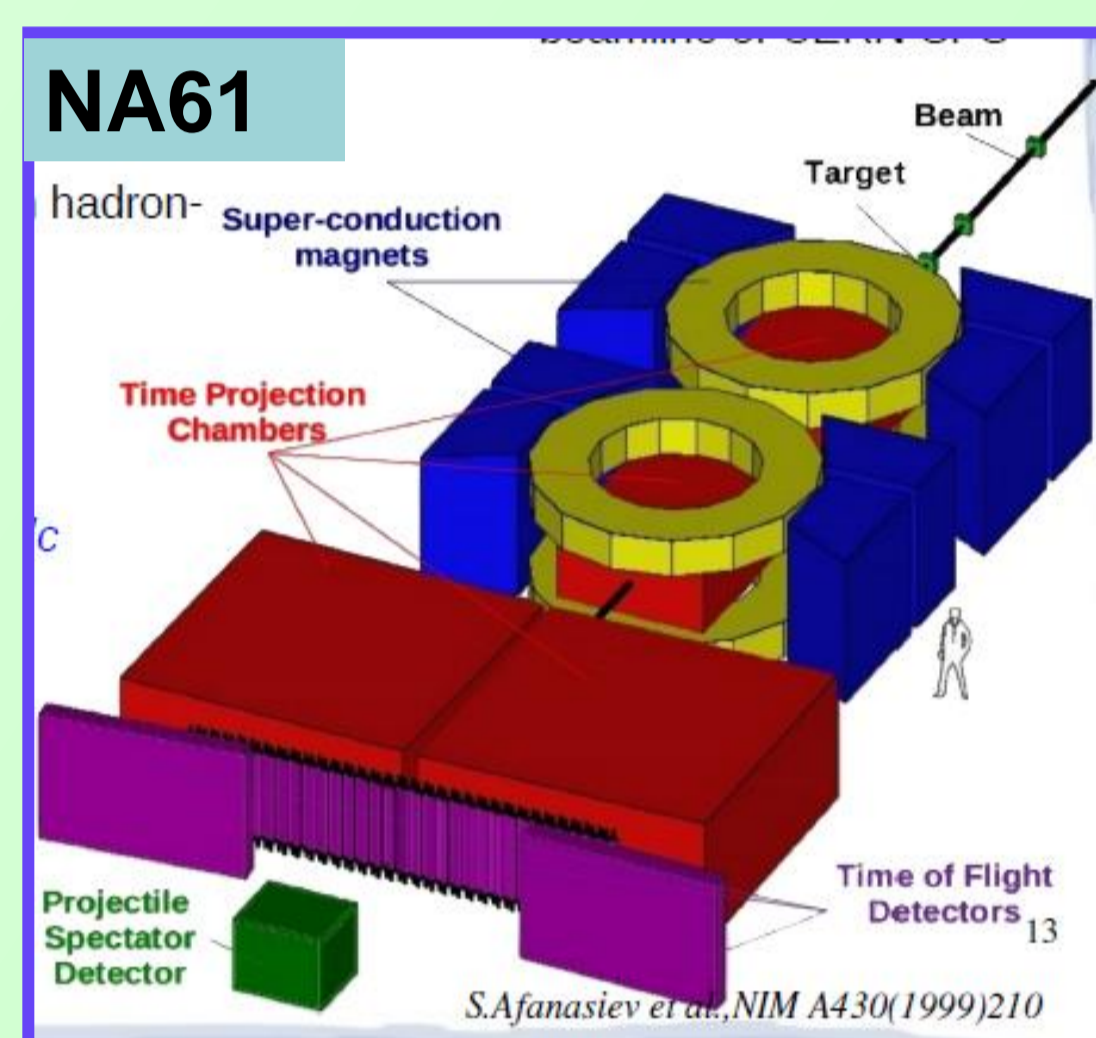
- $\pi$  and K production in the target are the ultimate source of neutrino flux.
- Knowledge and understanding of this is important for  $\nu$  oscillation experiments
- Two type of modelling (using experimental data on hadroproduction as input) :
  - **Hadronic cascade Monte Carlo** (MARS, GEANT4, FLUKA) tuned to experimental data. Tend to be black boxes and errors are hard to factorize
  - **Parametrized simulations** based on parametrizations of hadron production data (BMPT, SW, ...) . Provide experimenter with functions, errors. They are FAST.

## Available data for simulations of neutrino beamlines

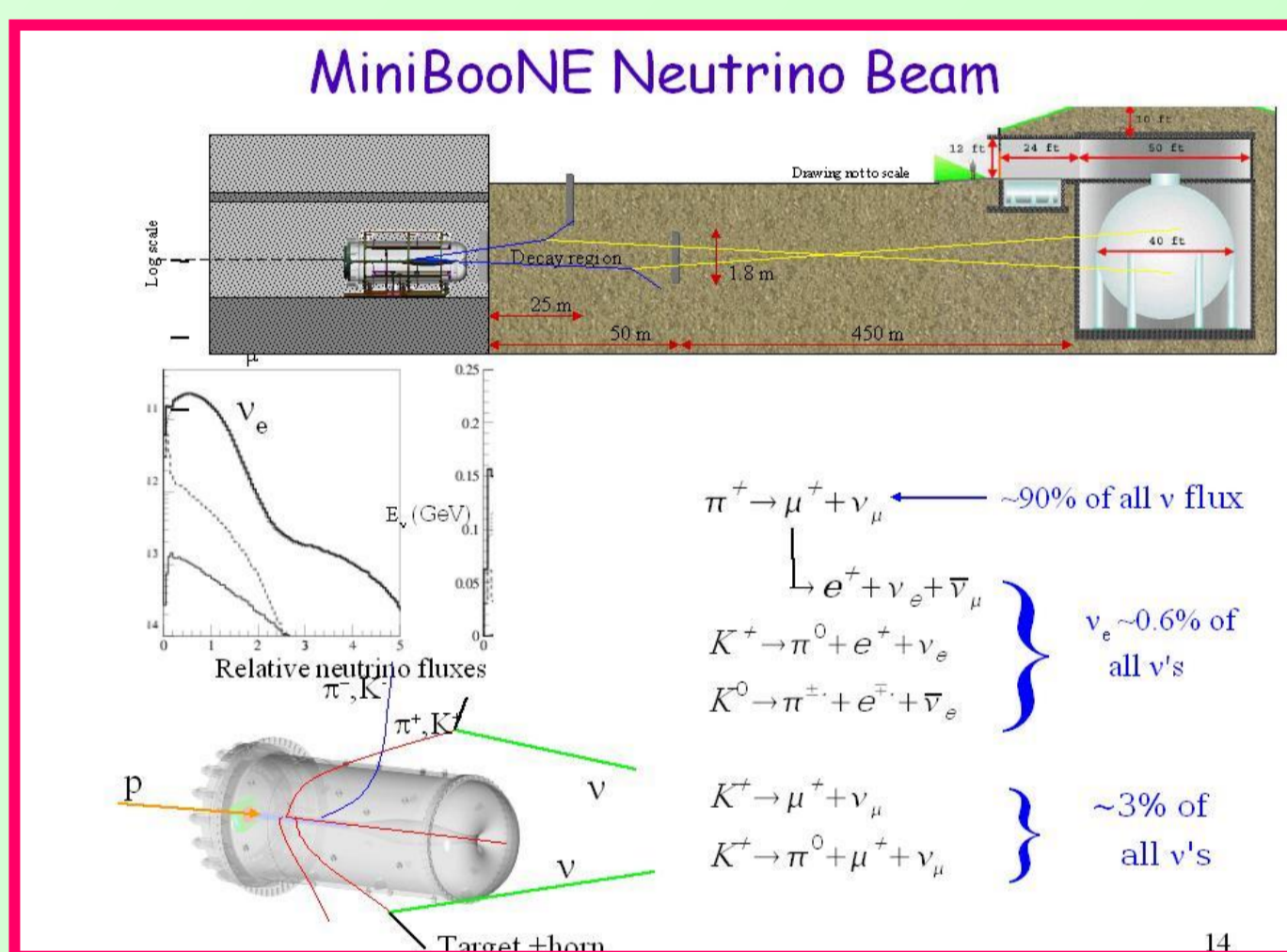
**Low energy  $\nu$  beams** (K2K, Nufact, MINIBOONE, MicroBoONE, SciBoONE); mainly HARP at CERN PS

**High energy  $\nu$  beams** (WANF, CNGS, NuMI, T2K..) : NA20, NA56/SPY, MIPP, NA61/SHINE

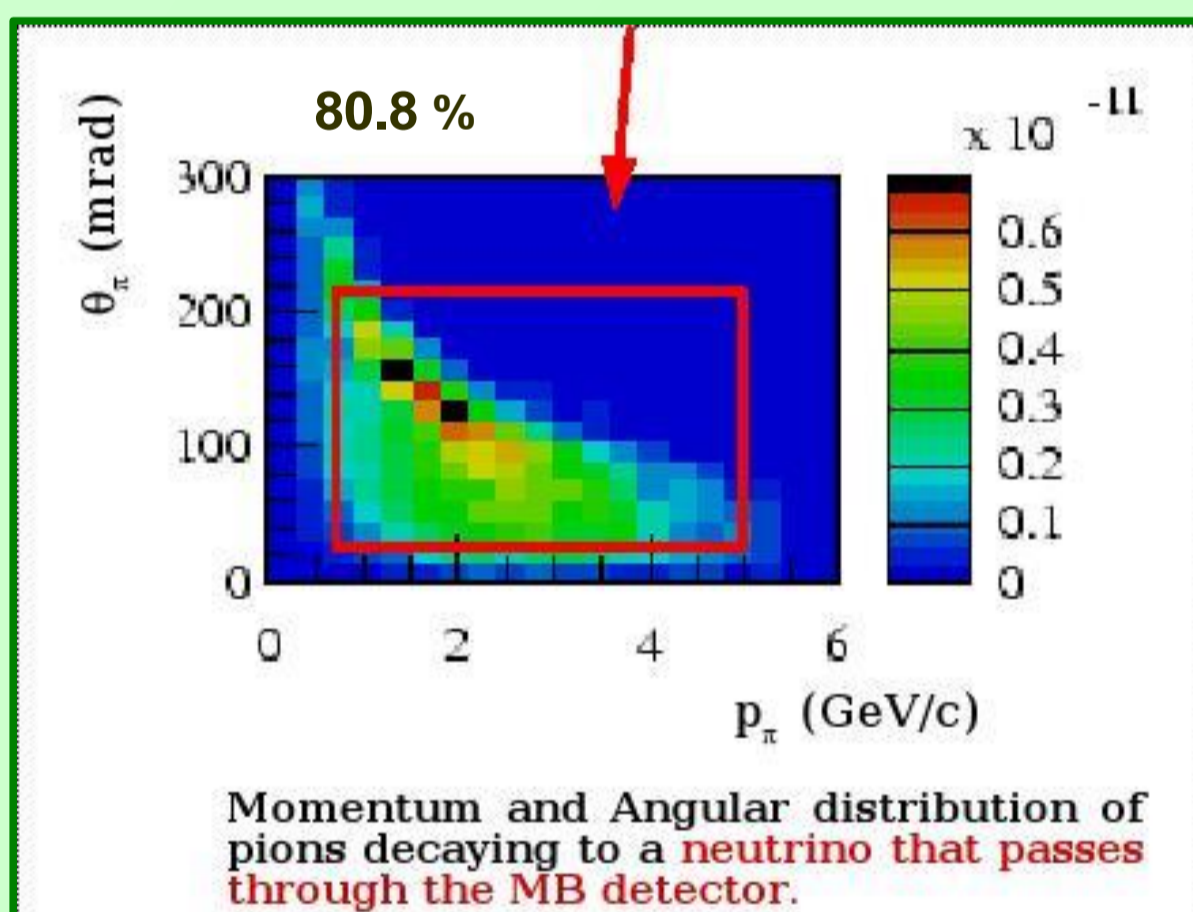
In addition a lot of old non-dedicated experiments with small statistics and high syst errors



## How to simulate a neutrino beam



**HARP p-Be  $\rightarrow$  p\*-X data 8.9 GeV/c:**  
M. G. Catanesi et al., Eur. Phys. J. **C52** (2007) 29  
**MiniBoONE with Harp input**,  
A.A.Aguilar-Arevalo et al., Phys. Rev. Lett. **98** (2007)



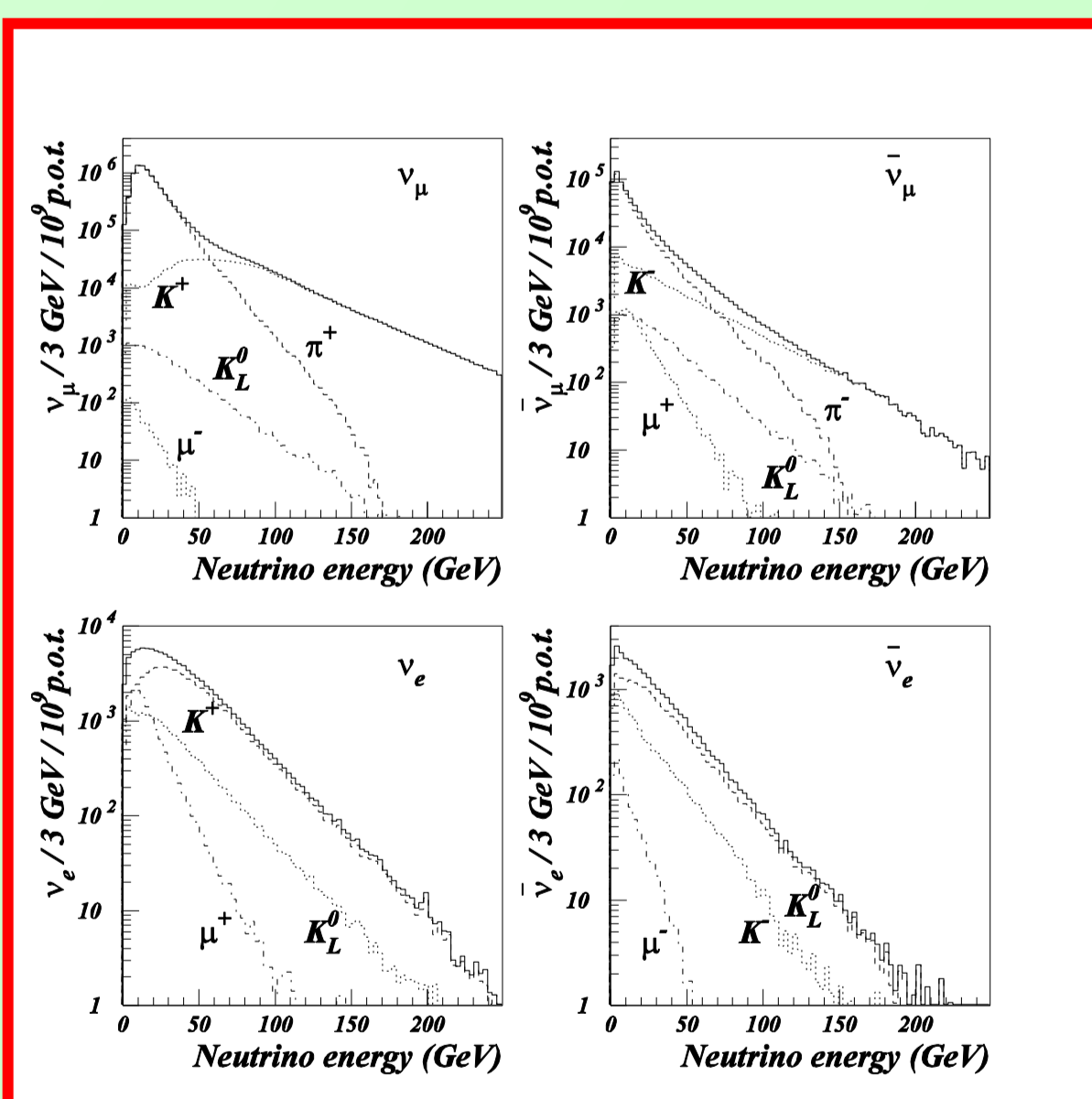
## Ingredients to compute a $\nu$ flux :

$\pi$ (and k) production cross section (use same target and proton energy as the proton driver of the experiment)

**Reinteractions:** take data with thin and thick target

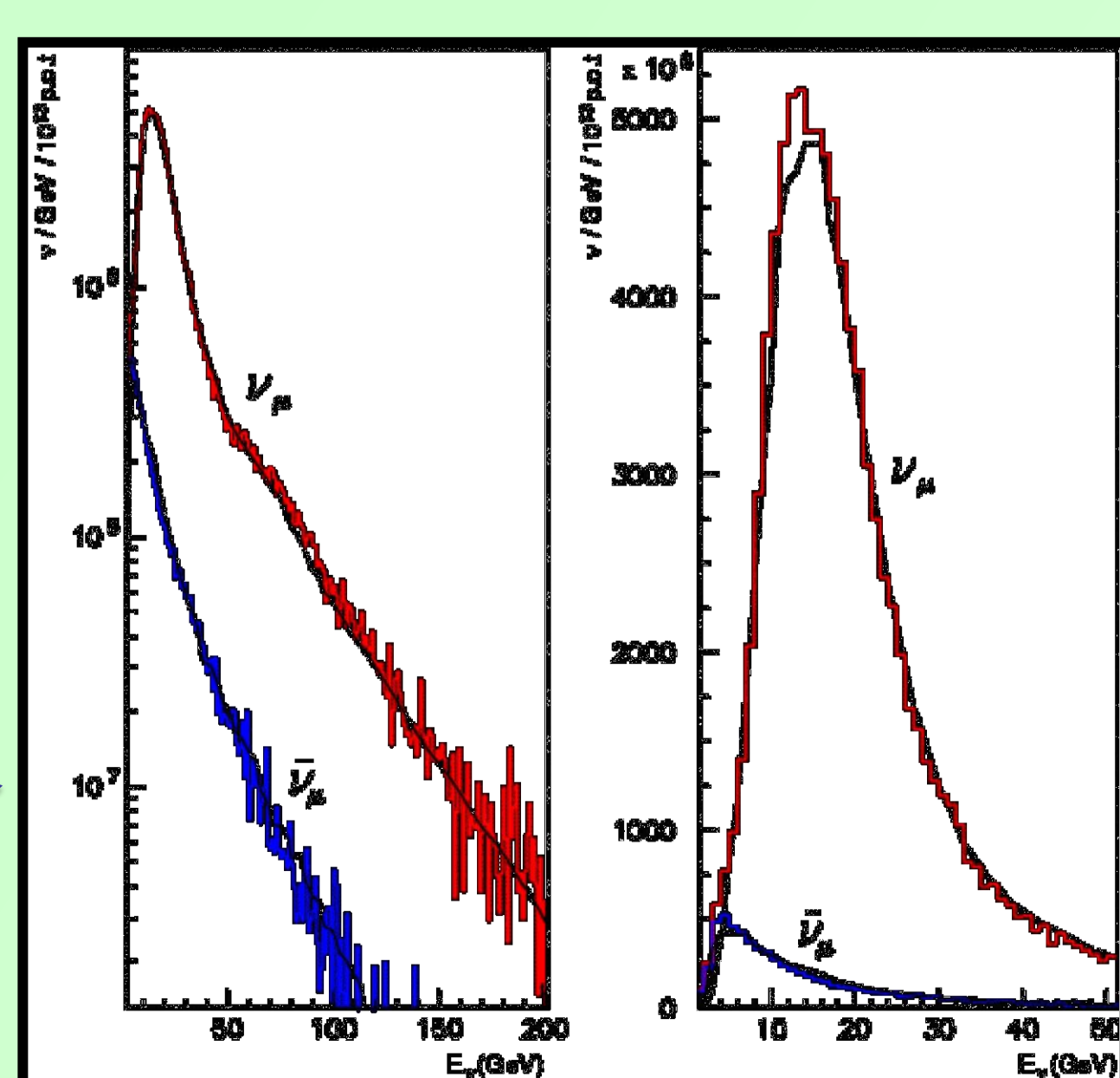
**All the rest:** simulation of the neutrino beamline: an "easy" problem.

**Two approaches:** full simulation with hadronic MC (GEANT4, MARS, FLUKA) , fast simulation based on parametrization of hadroproduction data (eg BMPT)



Fluka full simulation (+ reweighting with NA56/SPY data): WANF  $\nu$  beam for NOMAD

Both approaches needs good hadron production data

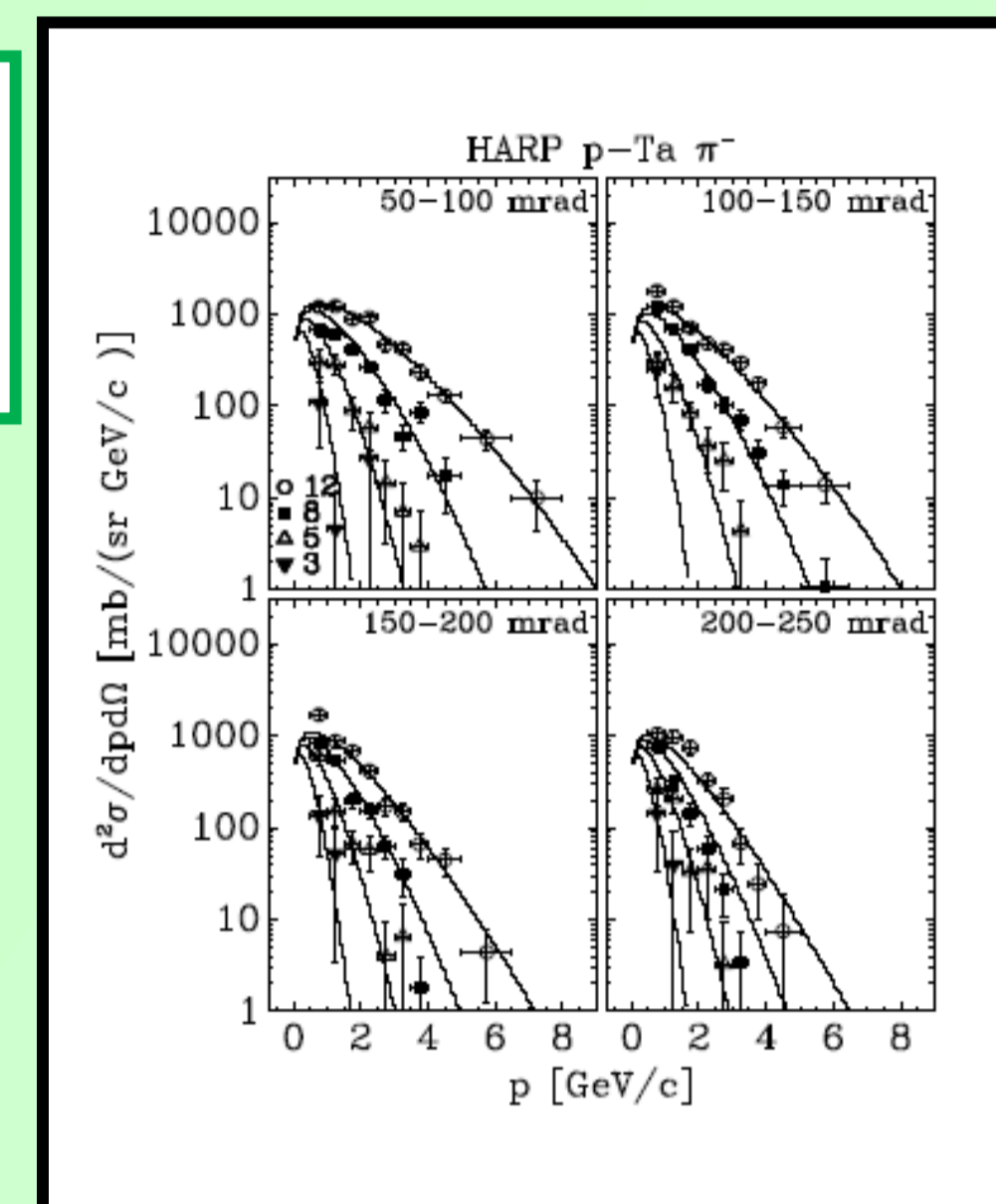


## Available hadron data parametrizations : SW and BMPT

1) **Sanford-Wang** empirical parametrization: 8 parameters, used for low energy beams (primary up to 30 GeV/c)

$$\frac{d^2\sigma}{dpd\Omega} = c_1 P_\pi^2 \left(1 - \frac{P_\pi}{P_p}\right) \times e^{\left(\frac{-c_3 p_\pi^4}{p_p^5} - c_6 \theta_x (P_\pi - c_7 P_p \cos^8 \theta_x)\right)}$$

HARP data and many others have been parametrized with formulas of this type. It is only an empirical parametrization.



2) The **BMPT** parametrization : empirical formula based on general physical argument, for high energy beams (primary down to ~30 GeV)

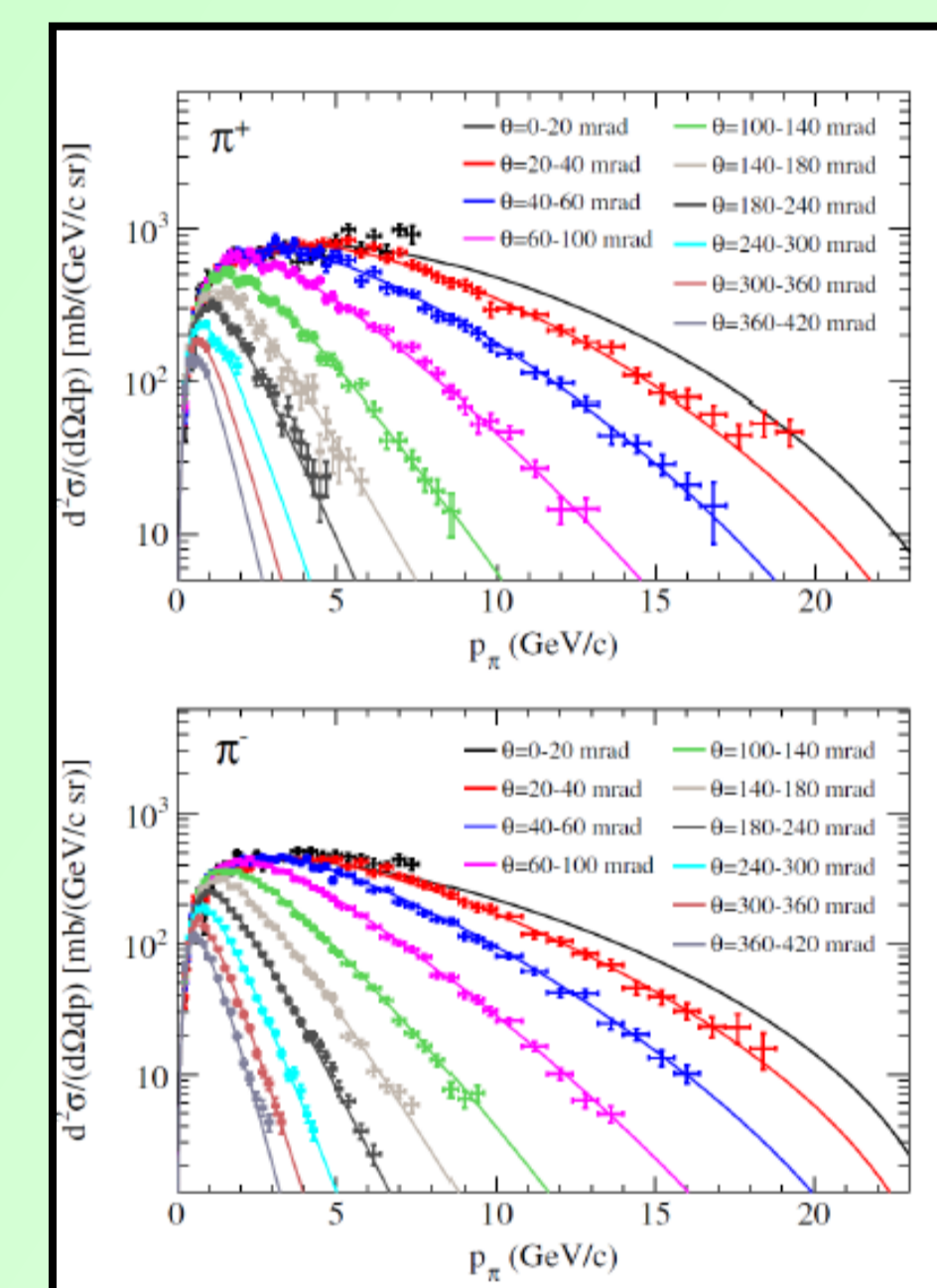
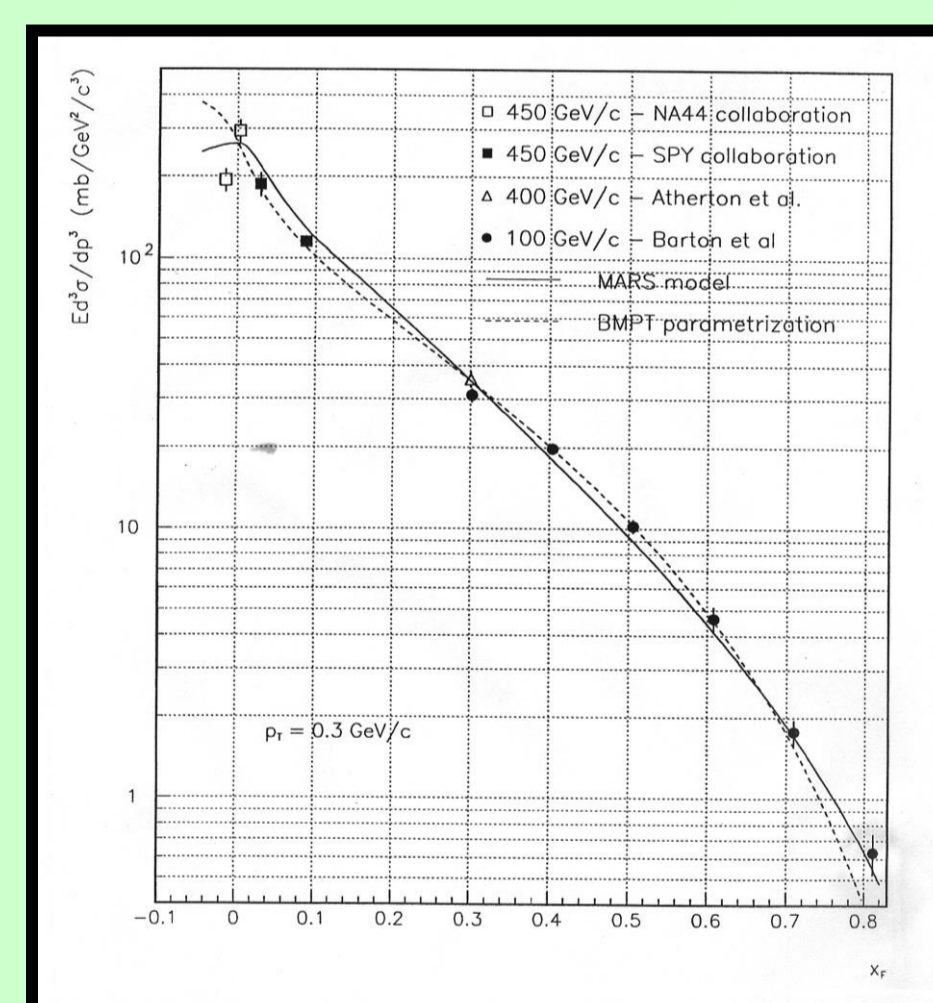
$$E \frac{d^3\sigma}{dp^3} = A(1 - x_R)^\alpha (1 + Bx_R) x_R^{-\beta} \times \left[1 + \frac{a}{x_R} p_T + \frac{a^2}{2x_R^2} p_T^2\right] e^{-a/x_R p_T}$$

$$r(\pi) = r_0(1 + x_R)^{r_1}$$

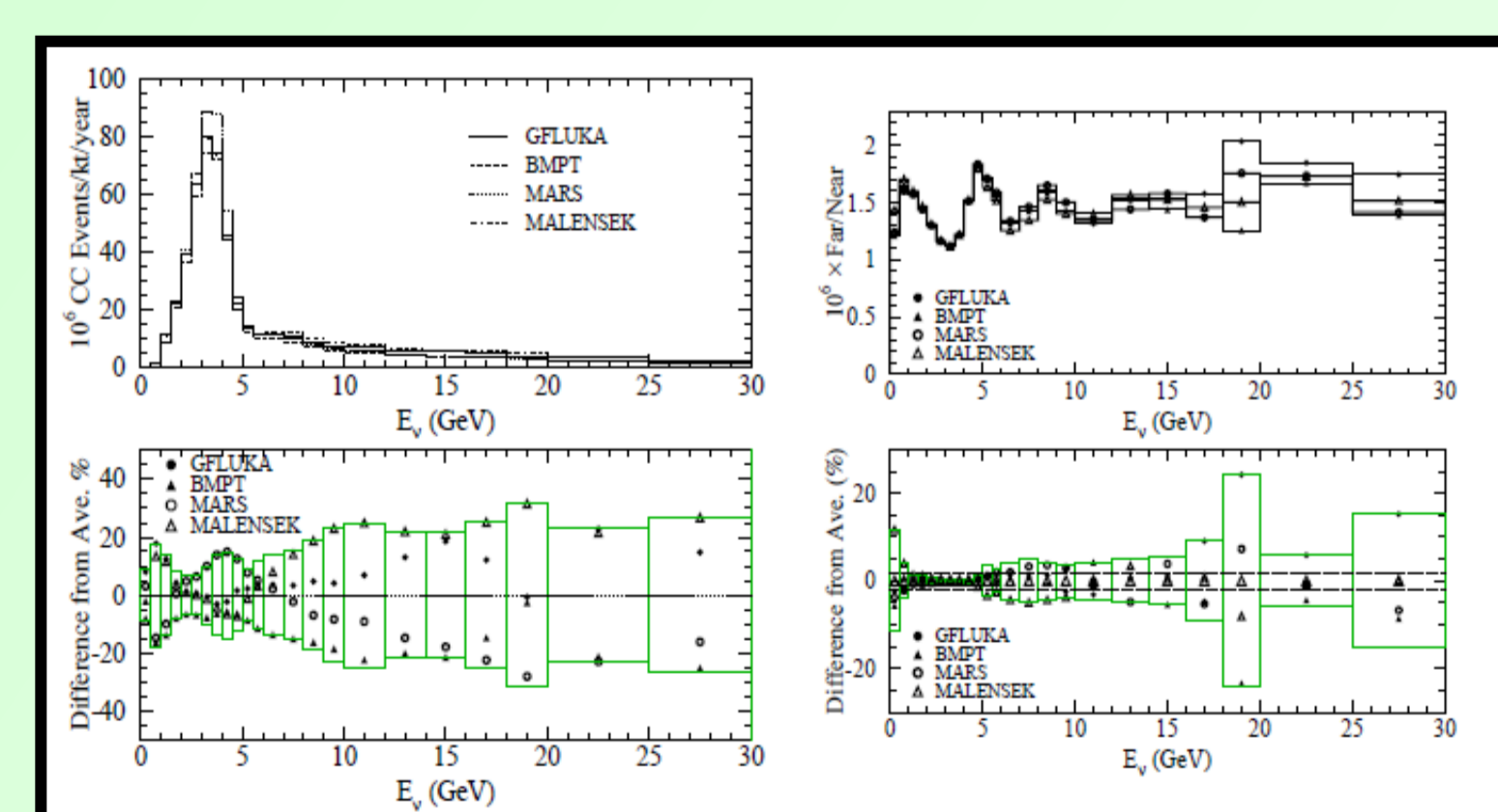
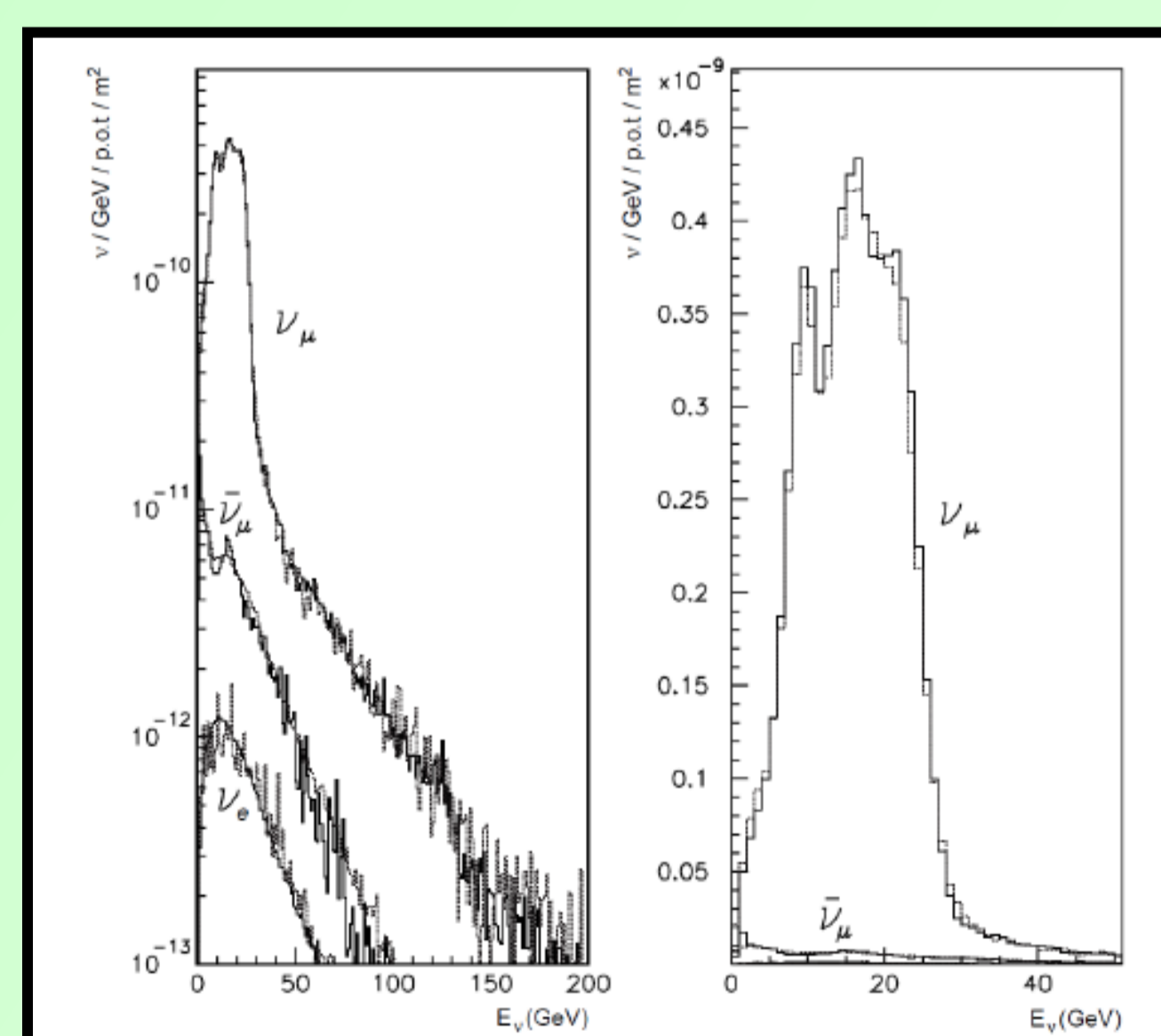
$$r(K) = r_0(1 - x_R)^{r_1}$$

Positive to negative ratio

- Approximate factorization in  $x$  and  $p_t$
- $(1-x)^2$  behavior in the forward direction for  $x \rightarrow 1$  (quark counting rule)
- $x^{-b}$  behavior in for  $x \rightarrow 0$  (non direct hadron formation mechanism)
- Exponential fall in  $p_t$  for soft interaction
- to go from original  $p_{beam} \sim 400$  GeV/c to much lower momenta best refit parameters



## Applications: two examples



## Useful references

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5. M. Bonesini, A. Marchionni, F. Pietropaolo, T. Tabarelli de Fatis, Eur. Phys. J. **C20** (2001) 13
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7. R. Plukett, Lectures at CTEQ 2007