

# TOPLHCWG

Combination of top observables  
at the Large Hadron Collider

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# What is the TOPLHCWG?

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## Top quark measurements at the LHC

- large top quark samples available at 7 and 8 TeV
- precise measurements at ATLAS and CMS (e.g.  $m_{\text{top}}$ ,  $\sigma(t\bar{t})$ , ...)

## TOPLHCWG

- forum for discussions (ATLAS+CMS+theory) on combinations and interpretation of top physics measurements at the LHC
- integrated into LPCC (LHC Physics Centre at CERN)
  - 20 closed and 3 open meetings

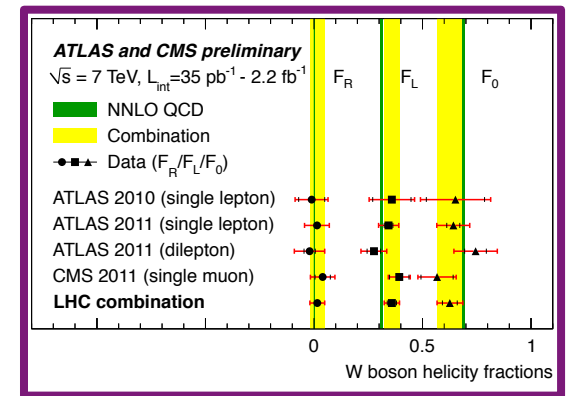
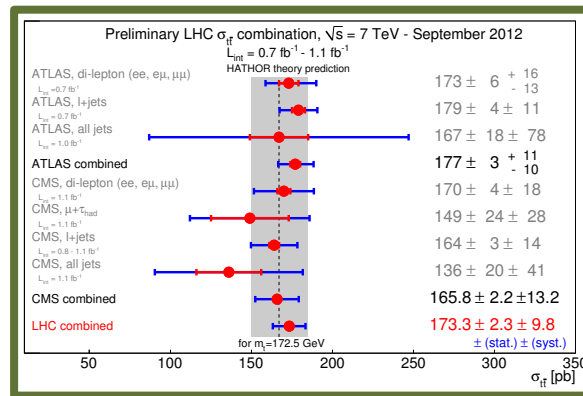
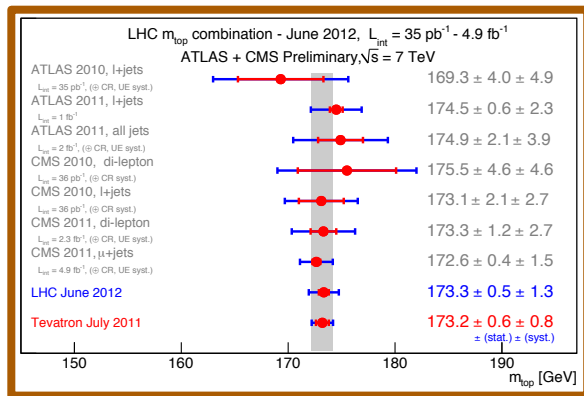
## Results released so far

- top quark mass, July-12
- $t\bar{t}$  cross-section, September-12
- W polarisation in top decays, March-13

see [http://lpcc.web.cern.ch/lpcc/index.php?page=top\\_wg\\_docs](http://lpcc.web.cern.ch/lpcc/index.php?page=top_wg_docs)

## First round of combinations

- allow to discuss/compare beyond the strict collaboration rules
- differences in systematics treatment identified
- recommendations for systematics of future measurements



## Importance of combinations

- beware: results shown here are mostly outdated, since more precise measurements have been released by the collaborations
- but: procedures, categorisations, initial agreements reached; further improvements agreed upon/being discussed

# Combination method: BLUE

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**BLUE method** = *Best Linear Unbiased Estimator*

- optimal set of coefficients (weights) in a linear combination of input measurements
- minimising total uncertainty on the combined result
- takes uncertainties and correlations into account
  - *categorisation done based on physics origin and on correlation pattern*

## Advantages

- well established, e.g. used for  $m_{\text{top}}$  at Tevatron
- makes future world averages technically easy

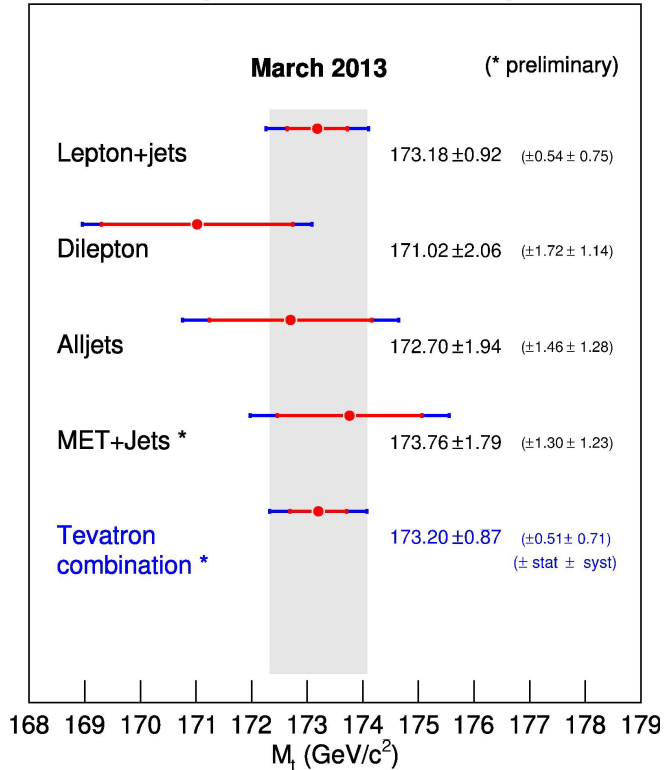
## Experience/Features

- need to provide correlations (sometimes a good guess)
- typically requires symmetric uncertainties
- can yield neg. weights for correlated, less precise measurements
- cannot (trivially) enforce physical constraints

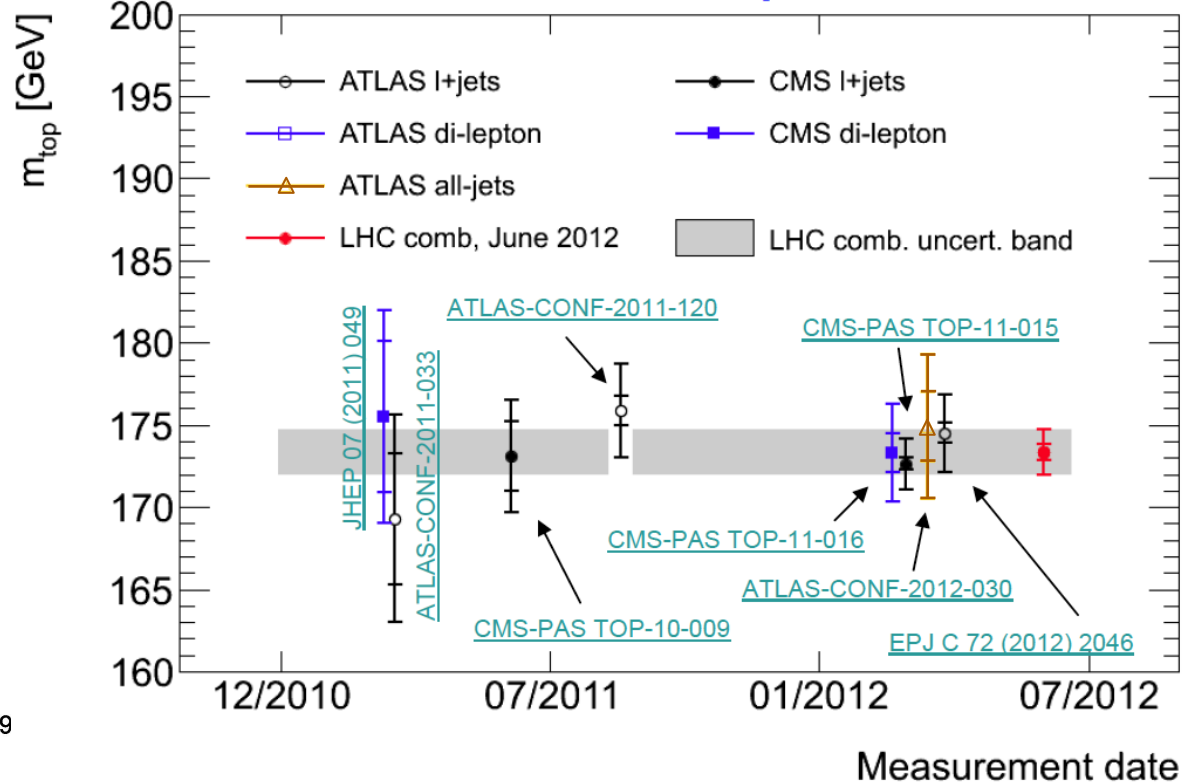
# Top quark mass

TeVWWG arXiv:1305.3929v1

Mass of the Top Quark in Different Decay Channels



Evolution of LHC top mass measurements



- LHC and best Tevatron measurements are systematics limited
- combination at Tevatron improves on best measurement  
*total uncert.: 1.11GeV (CDF  $\ell$ +jets)  $\rightarrow$  0.87GeV (average) due to uncorrelated/partially correlated systematics*

# Top mass combination

## Careful categorisation of uncertainties

- following Tevatron convention for Jet Energy Scale (JES) categories
- not all systematics can be easily matched 1:1

## Major numerical differences

- comparing best  $\ell$ +jets 2011 measurements with similar 2D techniques

bJES

– ATLAS: large uncert. from dead material

dJES

– CMS: performance of energy flow algorithm

MC

– ATLAS: hadronisation uncertainty (Pythia vs Herwig) in  $t\bar{t}$  events, in addition to hadronisation uncertainties included in JES

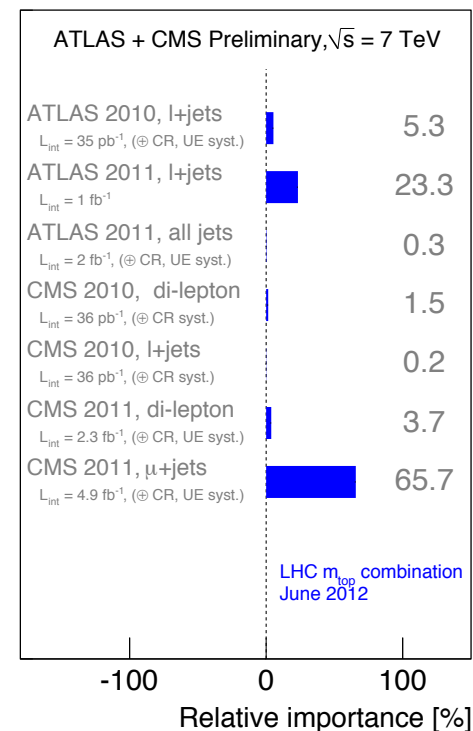
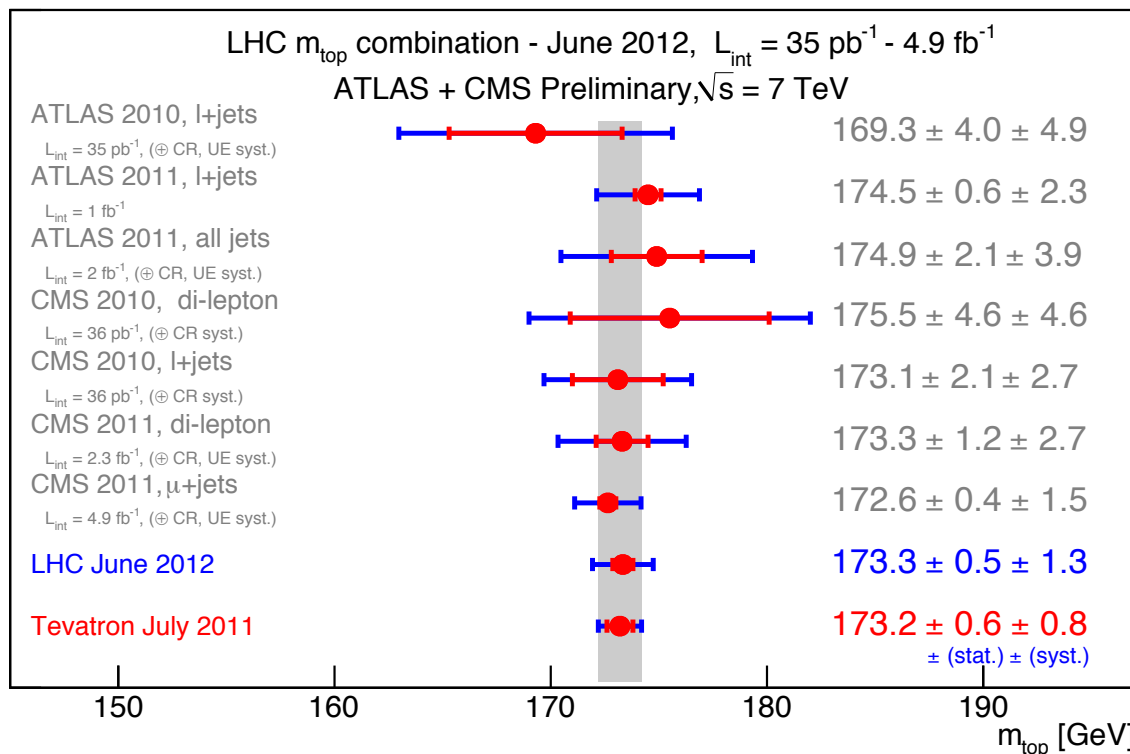
	ATLAS	CMS
bJES	1.6GeV	0.7GeV
dJES	0.7GeV	0.2GeV
MC	0.4GeV	n/e

# Top mass combination result

ATLAS-CONF-2012-095  
CMS PAS TOP-12-001

	ATLAS			CMS				LHC
	2010	2011		2010		2011		
	<i>l</i> +jets	<i>l</i> +jets	all jets	di- <i>l</i>	<i>l</i> +jets	di- <i>l</i>	$\mu$ +jets	comb.
[GeV]								
Measured $m_{\text{top}}$	169.3	174.5	174.9	175.5	173.1	173.3	172.6	173.34
Stat	4.0	0.6	2.1	4.6	2.1	1.2	0.4	0.47
iJES	n/a	0.4	n/a	n/a	n/a	n/a	0.4	0.38
aJES	n/a	n/a	n/a	n/a	n/a	n/a	n/a	n/a
bJES	2.5	1.6	1.4	0.9	0.9	1.1	0.7	0.68
cJES	n/a	n/a	n/a	n/a	n/a	n/a	n/a	n/a
dJES	2.1	0.7	2.1	2.1	2.1	2.0	0.2	0.07
rJES	n/a	n/a	n/a	3.3	n/a	n/a	n/a	0.06
Lept	n/e	n/e	n/e	0.3	n/e	0.2	n/e	0.01
MC	1.0	0.4	0.5	0.4	n/e	0.1	n/e	0.04
Rad	2.5	1.0	1.7	0.9	1.2	0.8	0.8	0.69
CR	0.6	0.6	0.6	0.5	0.5	0.5	0.5	0.55
PDF	0.5	0.1	0.6	0.5	0.1	0.4	0.1	0.01
DTMO	1.2	0.3	0.5	0.6	0.4	0.7	0.3	0.19
UE	0.6	0.6	0.6	1.4	0.2	0.6	0.6	0.47
BGMC	1.8	0.1	n/a	0.1	0.2	n/a	0.1	0.01
BGDT	0.6	0.5	1.9	n/a	0.4	0.4	n/a	0.16
Meth	0.4	0.1	1.0	0.3	0.1	0.4	0.2	0.13
MHI	0.7	< 0.05	n/e	1.0	0.1	0.2	0.4	0.25
[GeV]								
Total Syst. Unc	4.9	2.3	3.9	4.6	2.7	2.7	1.5	1.33
Total Unc.	6.3	2.4	4.4	6.5	3.4	3.0	1.5	1.40
Comb. Coeff.[%]	-6.8	29.9	-0.4	-1.9	-0.2	-4.8	84.3	$\chi^2/\text{ndf} = 2.5/6$
Relative importance[%]	5.3	23.3	0.3	1.5	0.2	3.7	65.7	$\chi^2$ prob = 87%

# Top mass summary



- combined LHC result is 9% more precise than best input (CMS  $\mu$ +jets)
- result is stable when varying the assumptions on correlations
- LHC  $m_{\text{top}}$  combination approaching Tevatron precision



# Plans for future top mass combination

## New results since first combination

- full 2011 dataset analysed by ATLAS and CMS
  - CMS average:  $173.54 \pm 0.33$  (stat.)  $\pm 0.96$  (syst.) GeV
  - ATLAS best  $\ell$ +jets  $172.31 \pm 0.75$  (stat.+JES+bJES)  $\pm 1.35$  (syst.) GeV
  - ATLAS dilepton  $173.09 \pm 0.64$  (stat.)  $\pm 1.50$  (syst.) GeV
- syst. uncert. cannot be directly compared due to different treatment
  - for instance hadronisation
- first 2012 analysis
  - CMS B hadron decay length:  $173.5 \pm 1.5$  (stat.)  $\pm 1.3$  (syst.)  $\pm 2.6$  ( $p_{T(\text{top})}$ ) GeV

## Next

- provide updated LHC combination
- combine with Tevatron  $\rightarrow$  world average

# Current work

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## Progress in categorisation of JES uncertainty

- methodologies and assumptions to derive corrections and uncertainties are not always directly comparable
- identified 5 categories according to physics and correlation

## JES categories

- uncorrelated
  - e.g. *statistical and detector-based components*
- common modeling in in-situ techniques ( $\rho = 0 - 0.5$ )
  - *$\gamma$ -jet and Z-jet direct balance*
- model-dependence of relative calibration corrections ( $\rho = 0.5 - 1$ )
- jet response on partonic flavour ( $\rho = 0 - 1$ )
- b-jet energy scale ( $\rho = 0.5 - 1$ )

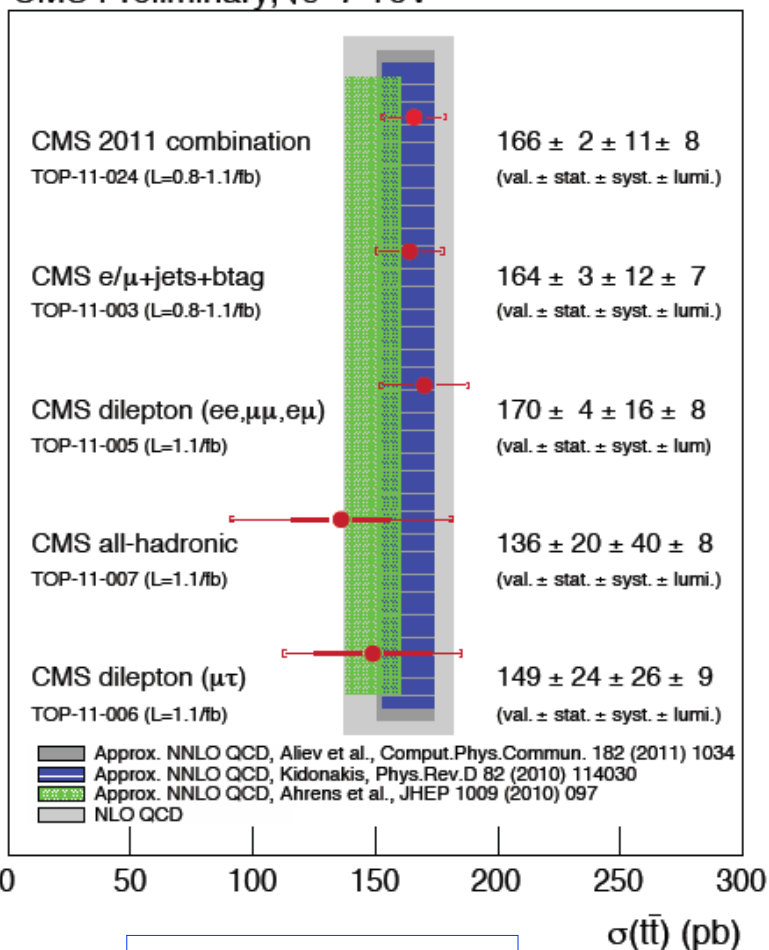
→ to be included in the next LHC top mass combination

*similar work ongoing for b-tagging uncertainties*

# Combination of $t\bar{t}$ production cross-section

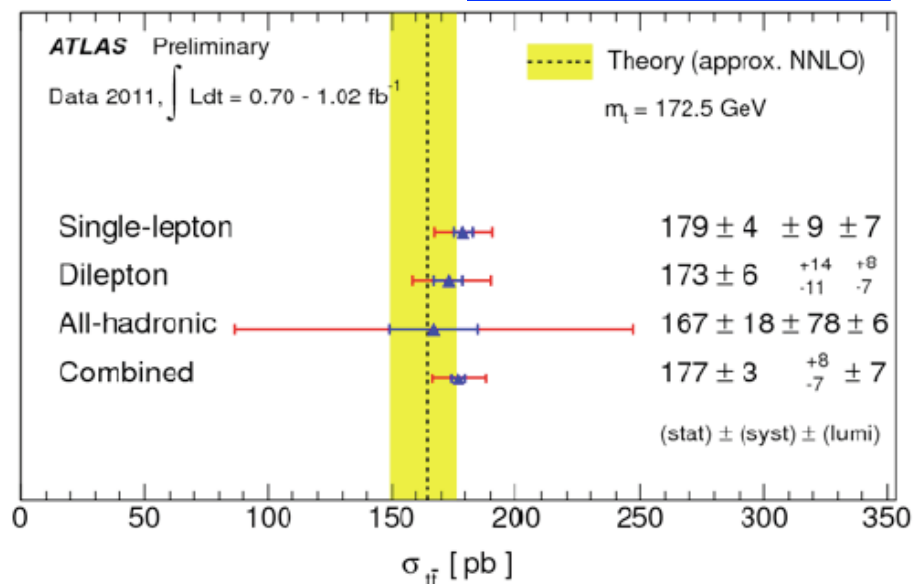
## Snapshot of 7 TeV results (Sept. 2012)

CMS Preliminary,  $\sqrt{s}=7$  TeV



CMS PAS TOP-11-024

ATLAS-CONF-2012-024



## Experiment combinations

ATLAS : 177 pb with 6.2% uncertainty

CMS: 166 pb with 8% uncertainty

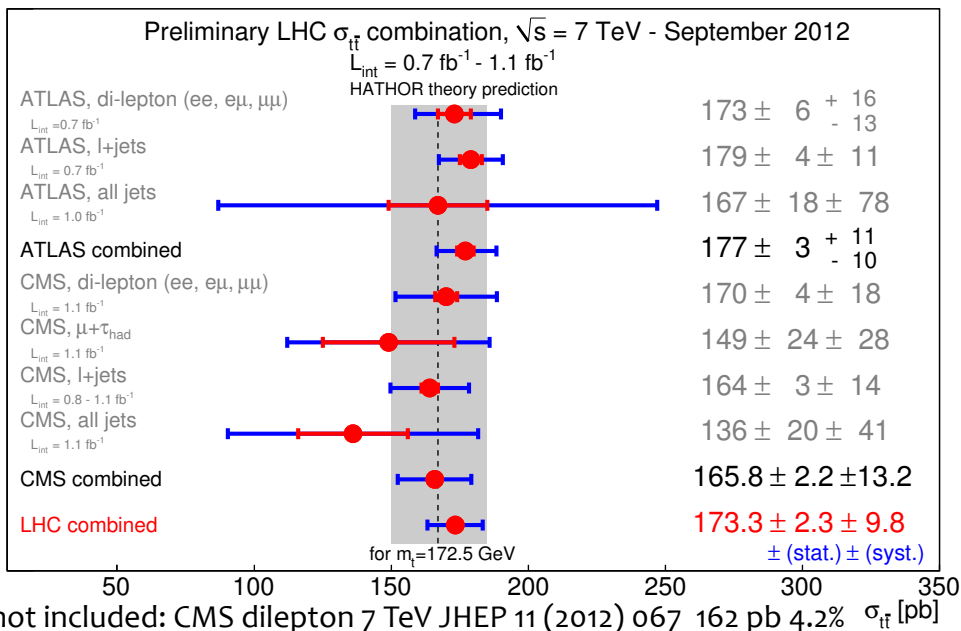
## Combination

- Similar procedure and issues as for top quark mass combination

## Luminosity uncertainty

- 53 (60)% of total uncertainty
- determined from van der Meer scans
  - bunch currents: fully correlated
  - experiment specific: uncorrelated

	ATLAS	CMS	Correlation	LHC combination
Cross-section	177.0	165.8		173.3
<b>Uncertainty</b>				
Statistical	3.2	2.2	0	2.3
Jet Energy Scale	2.7	3.5	0	2.1
Detector model	5.3	8.8	0	4.6
•••				
Bunch current	5.3	5.1	1	5.3
Luminosity measurement	4.3	5.9	0	3.4
Total systematic	10.8	14.2		9.8
Total	11.3	14.4		10.1



## Result

- total uncertainty reduced to 5.8%

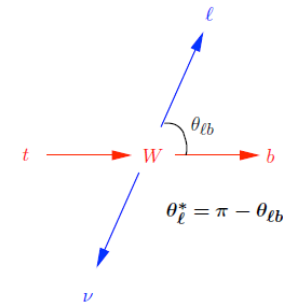
## Next step

- combine 8 TeV measurements

# W boson polarisation in top quark decays

## Precisely predicted in SM

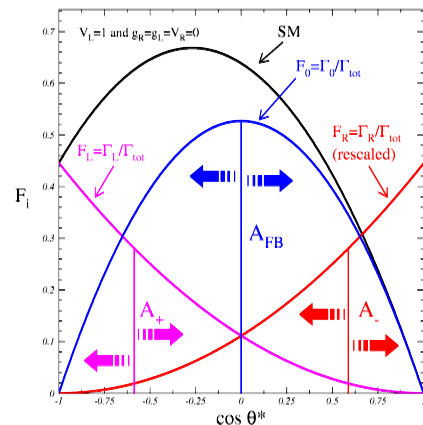
- right handed helicity  $F_R$  suppressed (V-A)
- measurements based on angle  $\vartheta^*(l,-b)$  in W rest frame



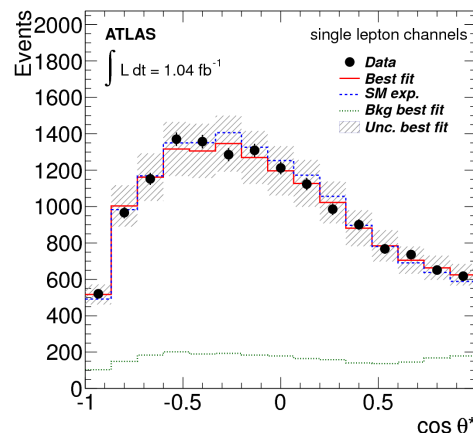
$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta^*} = \frac{3}{4} (1 - \cos^2 \theta^*) F_0 + \frac{3}{8} (1 - \cos \theta^*)^2 F_L + \frac{3}{8} (1 + \cos \theta^*)^2 F_R$$

## Use $\cos \theta^*$ distribution with different techniques

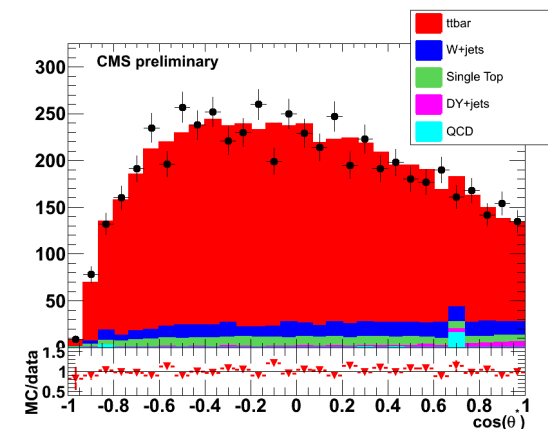
### Angular asymmetries



### Templates



### Reweighting



- ATLAS 2010  $\ell$ +jets: templates
- ATLAS 2011 dilepton &  $\ell$ +jets: templ./angular asymm.
- CMS 2011  $\mu$ +jets: reweighting

ATLAS-CONF-2011-037

JHEP 1206 (2012) 088

CMS PAS TOP-11-020

## Modifications to the original measurements

- categories of systematic uncertainties
  - *merge several sources, like other combinations*
- new estimates of correlations (ATLAS)
  - *most important modification*
- uncertainty on top mass (ATLAS and CMS)
  - *changed to 1.4 GeV*
- pre-combination (ATLAS)
  - *according to channel not to method*



<i>Detector modeling</i>
Detector model
Jet energy scale
Luminosity and pile-up
<i>Signal and background model</i>
Monte Carlo
Radiation
Top-quark mass
PDF
Background (MC QCD)
Background (MC W + jets)
Background (MC other)
Background (data-driven)
<i>Method-specific uncertainties</i>
Method

## Fit

- Simultaneous fit for  $F_0$  and  $F_L$
- Input to combination

*More recent CMS dilepton result not included*

Measurement	$F_0$	$F_L$	$F_R$
ATLAS 2010 (single lepton) [Alj2010]	$0.652 \pm 0.134 \pm 0.092$	$0.359 \pm 0.088 \pm 0.056$	$-0.011 \pm 0.060 \pm 0.046$
ATLAS 2011 (single lepton) [Alj2011]	$0.642 \pm 0.030 \pm 0.071$	$0.344 \pm 0.020 \pm 0.042$	$0.014 \pm 0.014 \pm 0.055$
ATLAS 2011 (dilepton) [Adil2011]	$0.744 \pm 0.050 \pm 0.087$	$0.276 \pm 0.031 \pm 0.051$	$-0.020 \pm 0.026 \pm 0.065$
CMS 2011 (single lepton) [Clj2011]	$0.567 \pm 0.074 \pm 0.048$	$0.393 \pm 0.045 \pm 0.024$	$0.040 \pm 0.035 \pm 0.043$

## Correlations

- $\rho(F_i, F_j)$  from uncertainty propagation or averaged over measurements
- $\rho(F_o, F_o) = \rho(F_L, F_L) = -\rho(F_o, F_L)$

## Main uncertainties

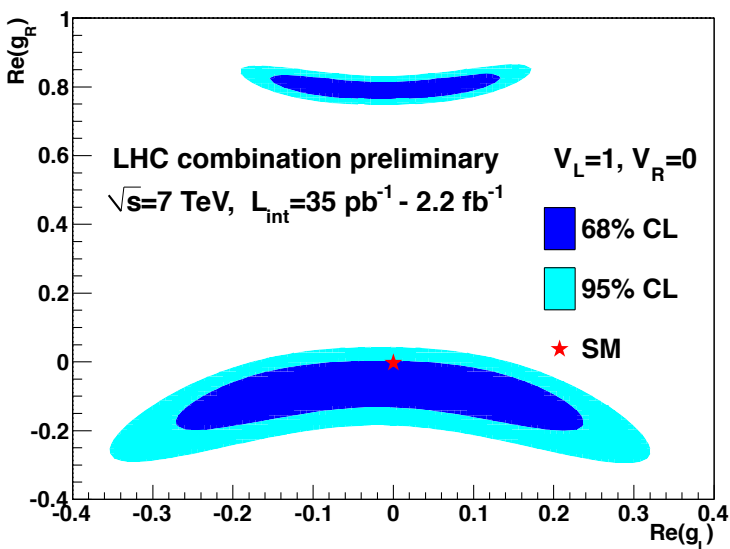
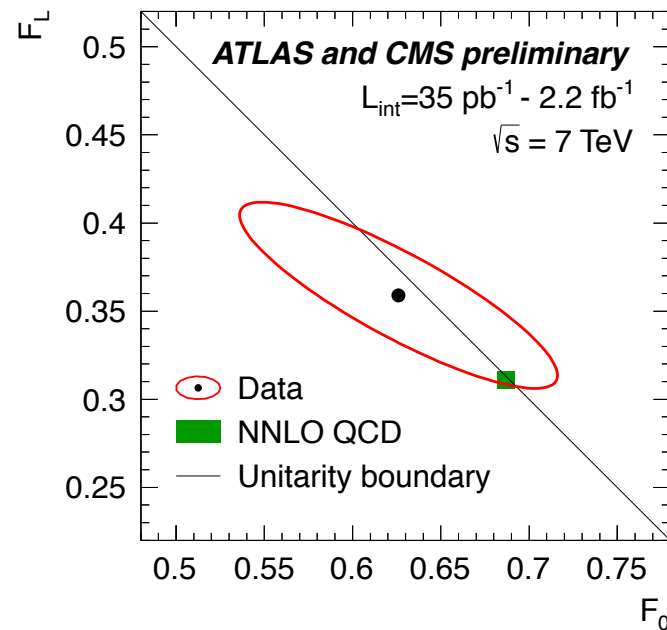
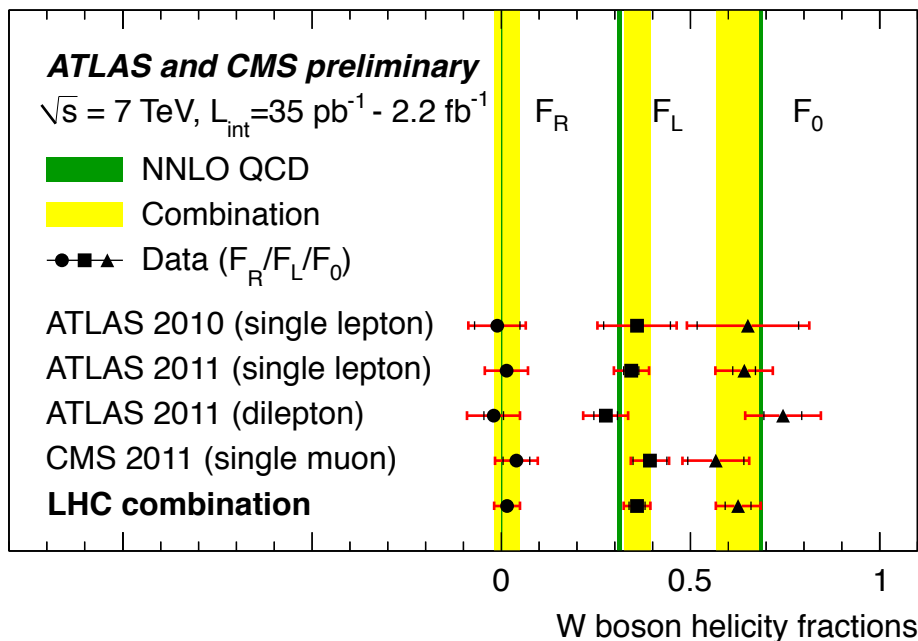
- statistical
- radiation and top quark mass
- detector model and JES

## Result

- $F_o = 0.626 \pm 0.034_{\text{stat}} \pm 0.048_{\text{syst}}$
- $F_L = 0.359 \pm 0.021_{\text{stat}} \pm 0.028_{\text{syst}}$
- $F_R = 0.015 \pm 0.034$

Category	LHC combination	
	$F_o$	$F_L$
<i>Detector modeling</i>		
Detector model	0.019	0.011
Jet energy scale	0.020	0.012
Luminosity and pile-up	0.006	0.003
<i>Signal and background modeling</i>		
Monte Carlo	0.012	0.008
Radiation	0.024	0.012
Top-quark mass	0.019	0.012
PDF	0.008	0.004
Background (MC QCD)	0.003	0.001
Background (MC W + jets)	0.007	0.002
Background (MC other)	0.011	0.006
Background (data-driven)	0.013	0.008
<i>Method-specific uncertainties</i>		
Method	0.008	0.005
<i>Total uncertainties</i>		
Total systematic uncertainty	0.048	0.028
Statistical uncertainty	0.034	0.021
Total uncertainty	0.059	0.035

# Result and interpretation



$$\mathcal{L}_{Wtb} = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu (V_L P_L + V_R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) t W_\mu^-$$

$$SM: V_L = V_{tb} \approx 1 \quad \text{Re}(g_R) = -0.10 \pm 0.06 \text{ (stat.) } {}^{+0.07}_{-0.08} \text{ (syst.)}$$

$$V_R = g_L = g_R = 0 \quad \frac{\text{Re}(C_{uW}^{33})}{\Lambda^2} = -1.1 \pm 0.6 \text{ (stat.) } {}^{+0.9}_{-1.0} \text{ (syst.) TeV}^{-2}$$



# Conclusion

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## First round of LHC top combinations

- $m_{\text{top}}$ ,  $\sigma_{t\bar{t}}$  (7TeV),  $W$  polarisation and anom. couplings

## Some lessons learnt

- very useful to compare and match systematics prescription
- results can be cross-checked and put on equal footing

## Prepare for next round of combinations

- important to determine correlations between measurements
  - *progress in JES and b-tagging categorisation*
- new CMS and ATLAS mass measurements
- $t\bar{t}$  cross-section determined at 8 TeV
- started discussing further combinations

## Links

- URL: [http://lpcc.web.cern.ch/LPCC/index.php?page=top\\_wg](http://lpcc.web.cern.ch/LPCC/index.php?page=top_wg)
- Open e-mail list: [lhc-toplhwcwg@cern.ch](mailto:lhc-toplhwcwg@cern.ch)

# Credits

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## Contributions in TOPLHCWG meetings from

M.Aldaya, W.Bell, D.Bloch, T.Carli, R.Chierici, T.Chwalek,  
G.Cortiana, M.Costa, M.Cristinziani, F.Déliot, D.Del Re, C.Doglioni,  
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M.Gosselink, K.Hatakeyama, D.Hirschebühl, J.Keaveney,  
H.Kirschenmann, K.Kröninger, P.Lenzi, L.Lista, B.Malaescu,  
M.Mangano, A.Meyer, L.Mijovic, A.Mitov, F.Moortgat, M.Mulders,  
P.Nason, J.Ott, M.Owen, F.Parodi, J.Rojo, F.P.Schilling,  
L.Scodellaro, M.Seidel, M.Senghi, E.Shabalina, P.Skands, F.Spanó,  
S.Strandberg, R.Tenchini, A.Valassi, W.Verkerke, M.Voutilainen,  
S.Wimpenny, J.C.Winter, M.zur Nedden

ATLAS    CMS    Theory

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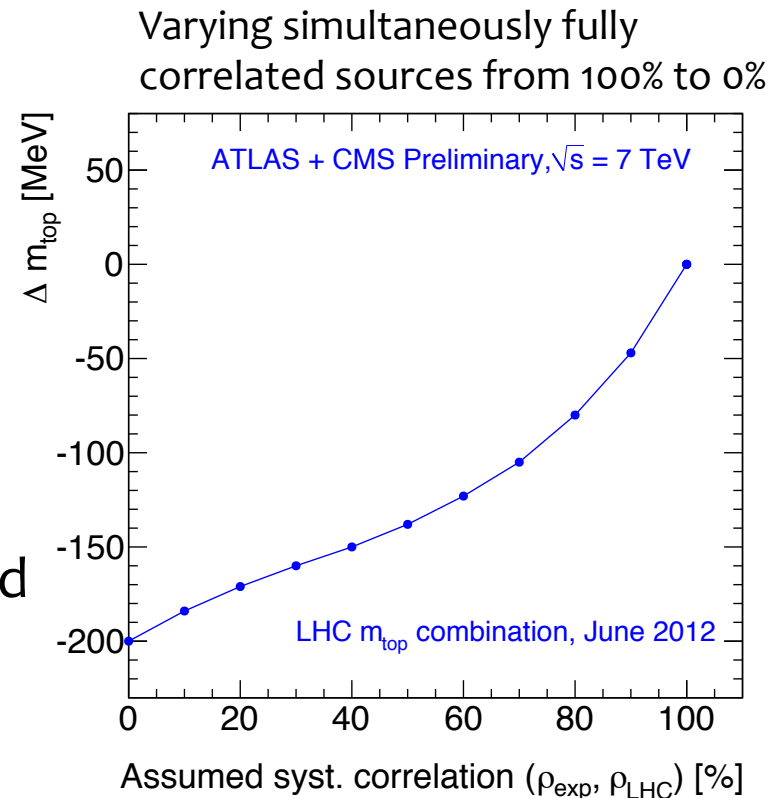
# Backup

## Assumptions on correlations

- reflect present knowledge and limitations
- impact of educated guess is evaluated by changing the assumed correlation across channels  $\rho_{\text{exp}}$  and experiments  $\rho_{\text{LHC}}$  in
  - MC ( $\rho=50\%$ )  $\rightarrow 0\%$  or  $100\%$
  - Rad ( $\rho=50\%$ )  $\rightarrow 0\%$  or  $100\%$
  - bJES ( $\rho=50\%$ )  $\rightarrow 0\%$  or  $100\%$
  - dJES ( $\rho=100\%$ )  $\rightarrow 50\%$
  - DetMod ( $\rho=100\%$ )  $\rightarrow 50\%$

## Effect

- no change within the number of quoted significant digits for the final result



# Mapping of uncertainty categories I

Uncertainty Categories			Size [GeV]							Correlation	
Tevatron	ATLAS	CMS	ATLAS			CMS				$\rho_{exp}$	$\rho_{LHC}$
			2010 <i>l+jets</i>	2011 <i>l+jets</i>	2011 all jets	2010 di- <i>l</i>	2010 <i>l+jets</i>	2011 di- <i>l</i>	2011 $\mu+jets$		
Statistics			4.0	0.6	2.1	4.6	2.1	1.2	0.4	0	0
iJES	Jet Scale Factor	Jet Scale Factor		0.4					0.4	0	0
aJES											
bJES	<i>JES<sub>b-jet</sub></i>	<i>JES<sub>b-jet</sub></i>	2.5	1.6	1.4	0.9	0.9	1.1	0.7	1	0.5 *
cJES											
dJES	<i>JES<sub>light-jet</sub></i>	<i>JES<sub>light-jet</sub></i>	2.1	0.7	2.1	2.1	2.1	2.0	0.2	1	0
rJES		residual- <i>JES</i>				3.3				0	0

\* assumed partially correlated

- **iJES**: from in-situ calibration procedure; stat.uncert. of Jet Scale Factor when using  $W \rightarrow jj$  invariant mass
- **bJES**: b-jet specific.
  - ATLAS: sizeable contribution from dead material.
  - CMS: flavor dependence of the jet response for b/light/gluon jets.
- **dJES**:  $p_T$  and  $\eta$  dependent calibration uncertainty
- **rJES**: fraction of JES not included above
  - used for CMS 2010 measurements
- other Tevatron categories (aJES, cJES) are not used

# Mapping of uncertainty categories II

Uncertainty Categories			Size [GeV]							Correlation	
Tevatron	ATLAS	CMS	ATLAS			CMS				$\rho_{exp}$	$\rho_{LHC}$
			2010 <i>l</i> +jets	2011 <i>l</i> +jets	2011 all jets	2010 di- <i>l</i>	2010 <i>l</i> +jets	2011 di- <i>l</i>	2011 $\mu$ +jets		
LepPt		Lepton $p_T$ Scale				0.3		0.2		1	0
MC	MC Generator	MC Generator	0.7	0.3	0.5	0.4		0.1			
	Hadronisation		0.7	0.2	(*)						
	Sum	Sum	1.0	0.4	0.5	0.4		0.1		1	0.5*
Rad	ISR/FSR	ISR/FSR	2.5	1.0	1.7	0.2	0.2				
		Q-Scale				0.6	1.1	0.4	0.8		
		Jet-Parton Scale				0.7	0.4	0.7	0.3		
	Sum	Sum	2.5	1.0	1.7	0.9	1.2	0.8	0.8	1	0.5*
CR	Colour Recon.		0.6	0.6	0.6	0.5	0.5	0.5	0.5	1	1
PDF	Proton PDF	Proton PDF	0.5	0.1	0.6	0.5	0.1	0.4	0.1	1	1
DetMod	Jet Energy Res.	Jet Energy Res.	0.9	0.1	0.3	0.5	0.1	0.3	0.2		
	Jet Rec. Eff.		0.5	< 0.05	0.2						
	<i>b</i> -tagging	<i>b</i> -tagging	0.5	0.3	0.3	0.4	0.1	0.5	0.2		
	$E_T^{miss}$	$E_T^{miss}$		0.1		0.1	0.4	0.4	0.1		
	Sum	Sum	1.2	0.3	0.5	0.7	0.4	0.7	0.3	1	0

\* assumed partially correlated

- **MC:** syst. uncert. due to the choice of generator/hadronization model  
– ATLAS baseline MC@NLO+Herwig; CMS baseline Madgraph+ Pythia
- **Rad:** Radiation  
– ISR/FSR, (Q-scale, jet/parton matching). Measured from  $t\bar{t}$  dilepton gap fraction
- **CR:** colour reconnection determined in 2011 and propagated to others
- **DetMod:** detector modeling systematics

# Mapping of uncertainty categories III

ATLAS-CONF-2012-095  
CMS PAS TOP-12-001

Uncertainty Categories			Size [GeV]							Correlation	
Tevatron	ATLAS	CMS	ATLAS			CMS				$\rho_{exp}$	$\rho_{LHC}$
			2010 <i>l+jets</i>	2011 <i>l+jets</i>	2011 all jets	2010 di- <i>l</i>	2010 <i>l+jets</i>	2011 di- <i>l</i>	2011 $\mu+jets$		
UE	Underlying Event	Underlying Event	0.6	0.6	0.6	1.4	0.2	0.6	0.6	1	0
BGMC	W+jet Norm. W+jet Shape	background	1.6 0.8	0.1		0.1	0.2		0.1		
	Sum		Sum	1.8	0.1		0.1	0.2		0.1	1
BGData	W+jet Norm.	QCD Norm.		0.4							
	QCD Norm.		0.5	0.2			0.4	0.4			
	QCD Shape		0.4	0.3	1.9						
	Sum	Sum	0.6	0.5	1.9		0.4	0.4		0	0
Method	Method Calib.	Method Calib.	0.4	0.1	1.0	0.3	0.1	0.4	0.2	0	0
MHI	Pile-up	Pile-up	0.7	< 0.05		1.0	0.1	0.2	0.4	1	1

- **UE:** underlying event, comparing different tunes
- **BGMC:** modeling of backgrounds from MC
  - *normalisation and shape*
- **BGData:** modeling of data-driven backgrounds
  - *normalisation and shape*
- **Method, MHI:** Method calibration and effects due to pile-up

# Top mass combination result

ATLAS-CONF-2012-095  
CMS PAS TOP-12-001

	ATLAS			CMS				LHC
	2010	2011		2010		2011		
	<i>l</i> +jets	<i>l</i> +jets	all jets	<i>di-l</i>	<i>l</i> +jets	<i>di-l</i>	$\mu$ +jets	comb.
[GeV]								
Measured $m_{\text{top}}$	169.3	174.5	174.9	175.5	173.1	173.3	172.6	173.34
Stat	4.0	0.6	2.1	4.6	2.1	1.2	0.4	0.47
iJES	n/a	0.4	n/a	n/a	n/a	n/a	0.4	0.38
aJES	n/a	n/a	n/a	n/a	n/a	n/a	n/a	n/a
bJES	2.5	1.6	1.4	0.9	0.9	1.1	0.7	0.68
cJES	n/a	n/a	n/a	n/a	n/a	n/a	n/a	n/a
dJES	2.1	0.7	2.1	2.1	2.1	2.0	0.2	0.07
rJES	n/a	n/a	n/a	3.3	n/a	n/a	n/a	0.06
Lept	n/e	n/e	n/e	0.3	n/e	0.2	n/e	0.01
MC	1.0	0.4	0.5	0.4	n/e	0.1	n/e	0.04
Rad	2.5	1.0	1.7	0.9	1.2	0.8	0.8	0.69
CR	0.6	0.6	0.6	0.5	0.5	0.5	0.5	0.55
PDF	0.5	0.1	0.6	0.5	0.1	0.4	0.1	0.01
DTMO	1.2	0.3	0.5	0.6	0.4	0.7	0.3	0.19
UE	0.6	0.6	0.6	1.4	0.2	0.6	0.6	0.47
BGMC	1.8	0.1	n/a	0.1	0.2	n/a	0.1	0.01
BGDT	0.6	0.5	1.9	n/a	0.4	0.4	n/a	0.16
Meth	0.4	0.1	1.0	0.3	0.1	0.4	0.2	0.13
MHI	0.7	< 0.05	n/e	1.0	0.1	0.2	0.4	0.25
[GeV]								
Total Syst. Unc	4.9	2.3	3.9	4.6	2.7	2.7	1.5	1.33
Total Unc.	6.3	2.4	4.4	6.5	3.4	3.0	1.5	1.40
Comb. Coeff.[%]	-6.8	29.9	-0.4	-1.9	-0.2	-4.8	84.3	$\chi^2/\text{ndf} = 2.5/6$
Relative importance[%]	5.3	23.3	0.3	1.5	0.2	3.7	65.7	$\chi^2$ prob = 87%