

# PROBING EWSB AND FUTURE HIGGS PHYSICS

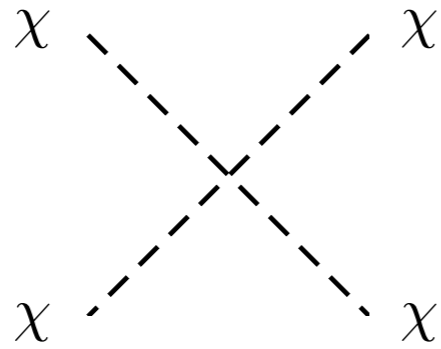
Roberto Contino

Università di Roma La Sapienza & INFN Roma

EPSHEP 2013 Stockholm, Sweden, 18-24 July, 2013

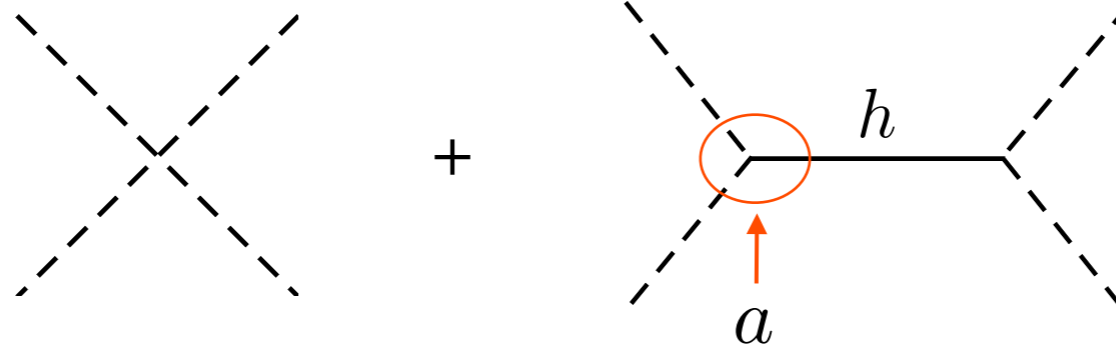
# Strong vs Weak EWSB

In the {SM-H}



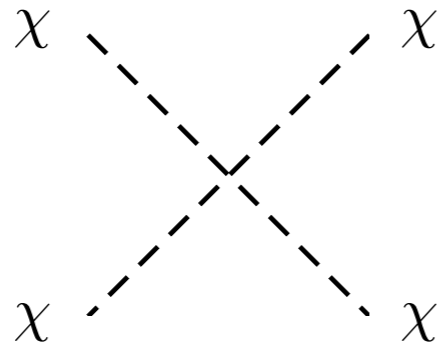
$$A(W_L W_L \rightarrow W_L W_L) = A(\chi\chi \rightarrow \chi\chi) \sim \frac{E^2}{v^2} \equiv g^2(E)$$

In the {SM-H} + H



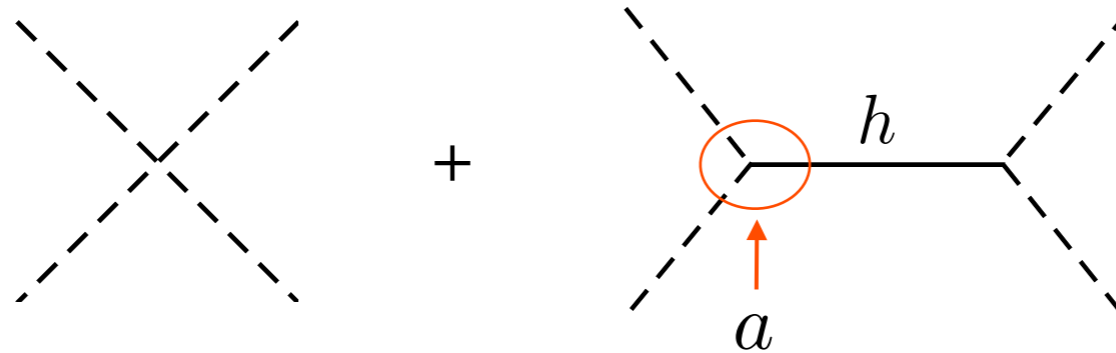
$$A \sim \frac{E^2}{v^2} (1 - a^2) - a^2 \frac{m_h^2}{v^2} \frac{s}{s - m_h^2}$$

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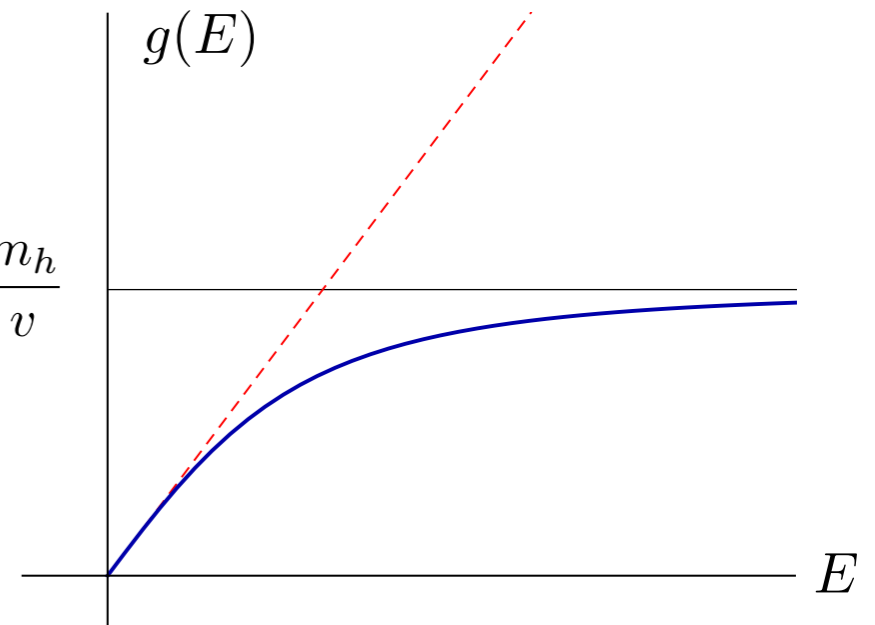
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$\underbrace{\hspace{10em}}_{= 0}$

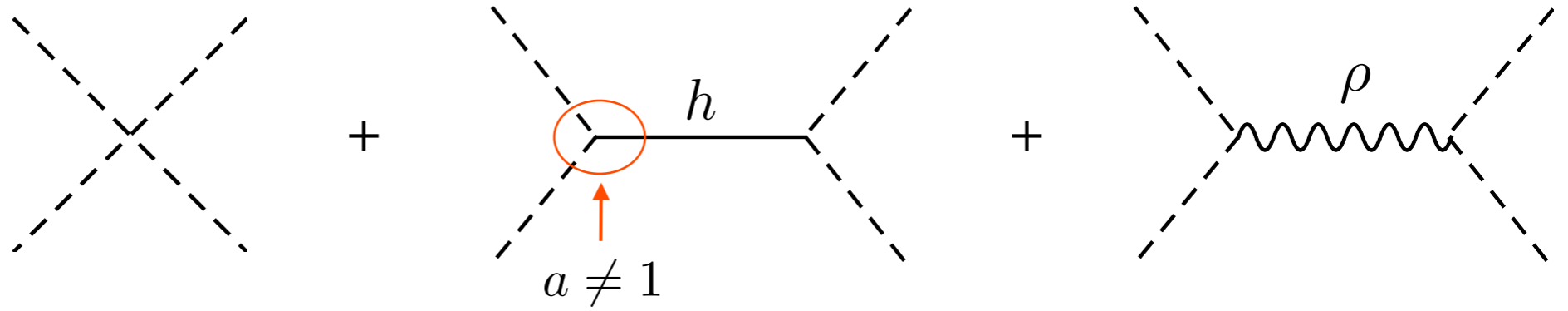
Elementary Higgs:

$a = 1$

weak  $\longrightarrow \frac{m_h}{v}$

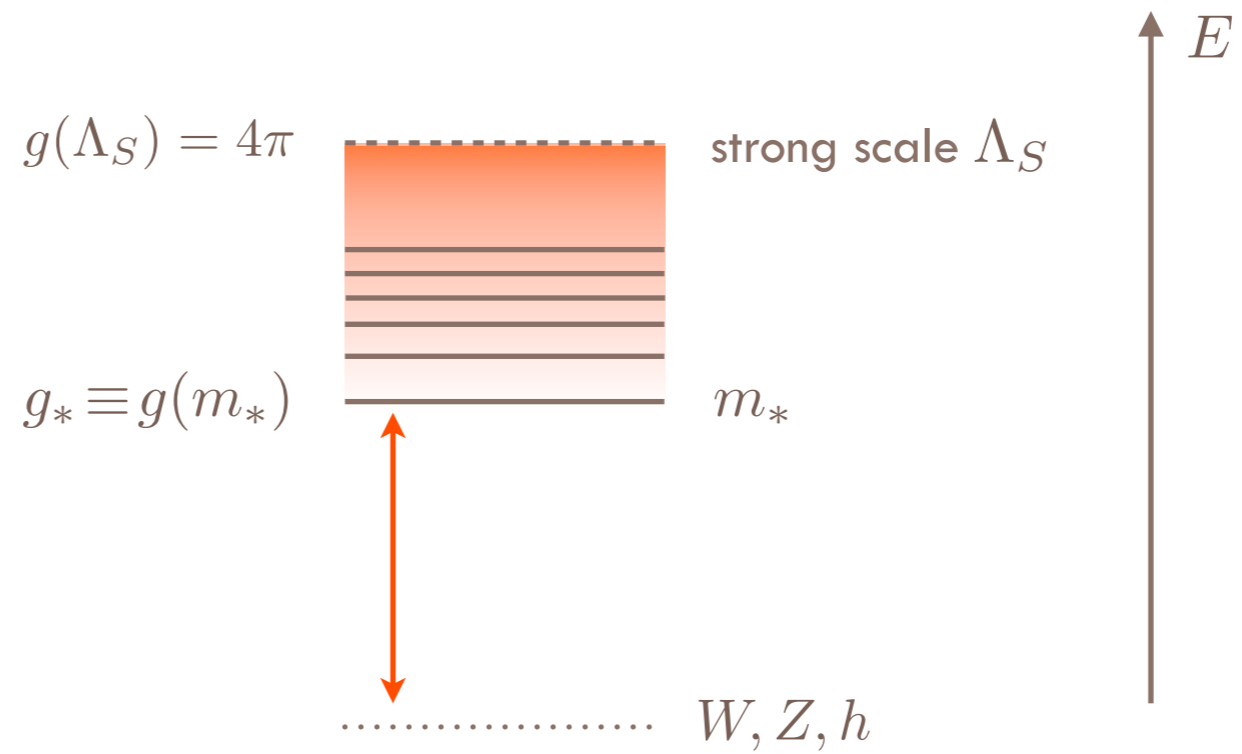


Composite Higgs:



coupling strength grows with energy and saturates at  $g_* \lesssim 4\pi$

Energy cartoon:



Analogy with  $\pi\pi$  scattering in QCD:  $h \leftrightarrow \sigma$



Q: why light and narrow ?

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A: the Higgs is itself a (pseudo) NG boson [ Georgi & Kaplan, '80 ]

ex:  $\frac{SO(5)}{SO(4)} \rightarrow$  4 NGBs transforming as a (2,2) of SO(4)

[ Agashe, RC, Pomarol  
NPB 719 (2005) 165 ]

$$f^2 \left| \partial_\mu e^{i\pi/f} \right|^2 = (\partial\pi)^2 + \frac{(\pi\partial\pi)^2}{f^2} + \frac{\pi^2(\pi\partial\pi)^2}{f^4} + \dots$$

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[ Giudice et al. JHEP 0706 (2007) 045 ]



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1.  $O(v^2/f^2)$  shifts in tree-level Higgs couplings. Ex:  $a = 1 - c_H \left( \frac{v}{f} \right)^2 + \dots$

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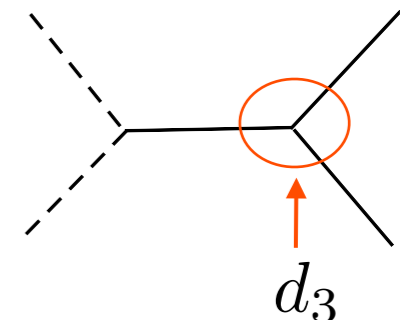
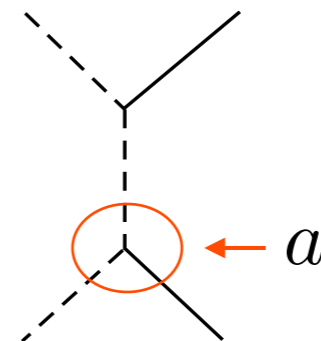
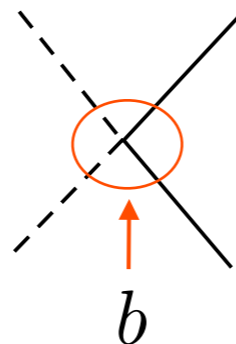
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2. Scatterings involving the Higgs also grow with energy

$$A(WW \rightarrow hh) \sim \frac{s}{v^2} (a^2 - b)$$



## How to test Higgs compositeness

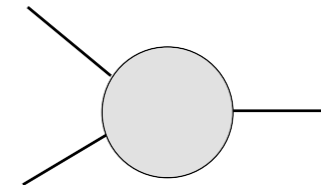
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2. **Indirect:** Precision measurement of low-energy quantities

# How to test Higgs compositeness

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2. **Indirect:** Precision measurement of low-energy quantities

i) virtual corrections to single-Higgs processes

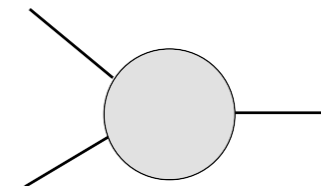


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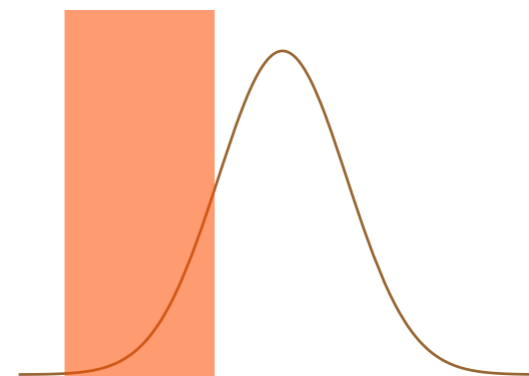
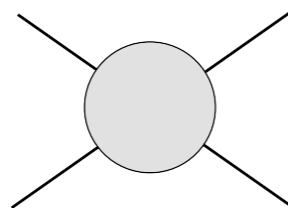
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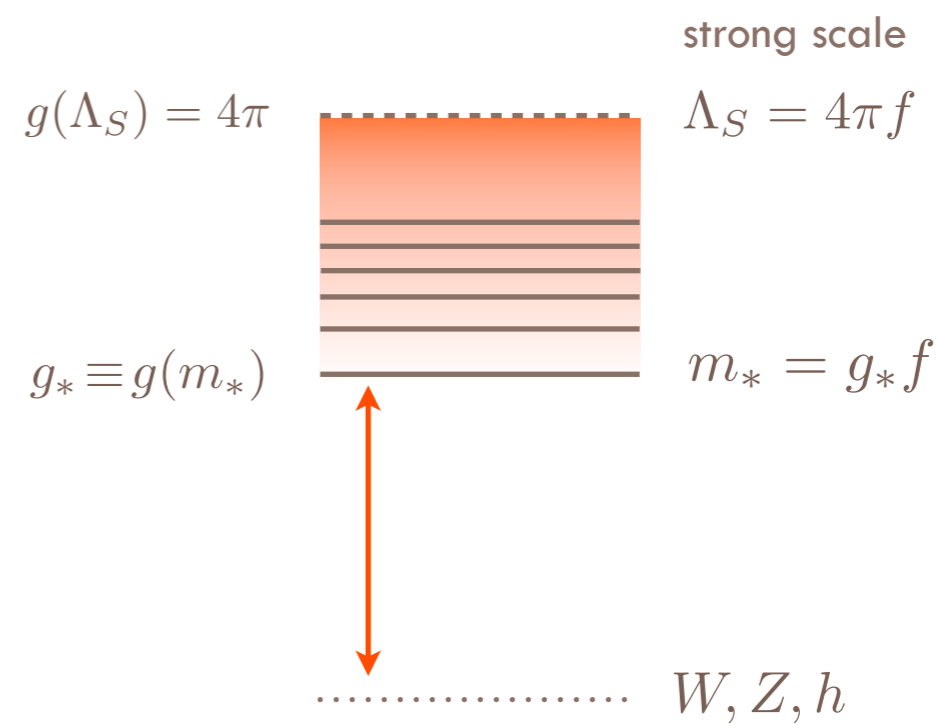
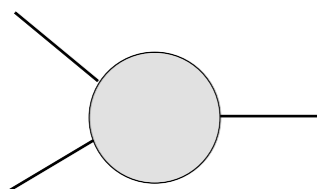


ii) tails in scattering amplitudes



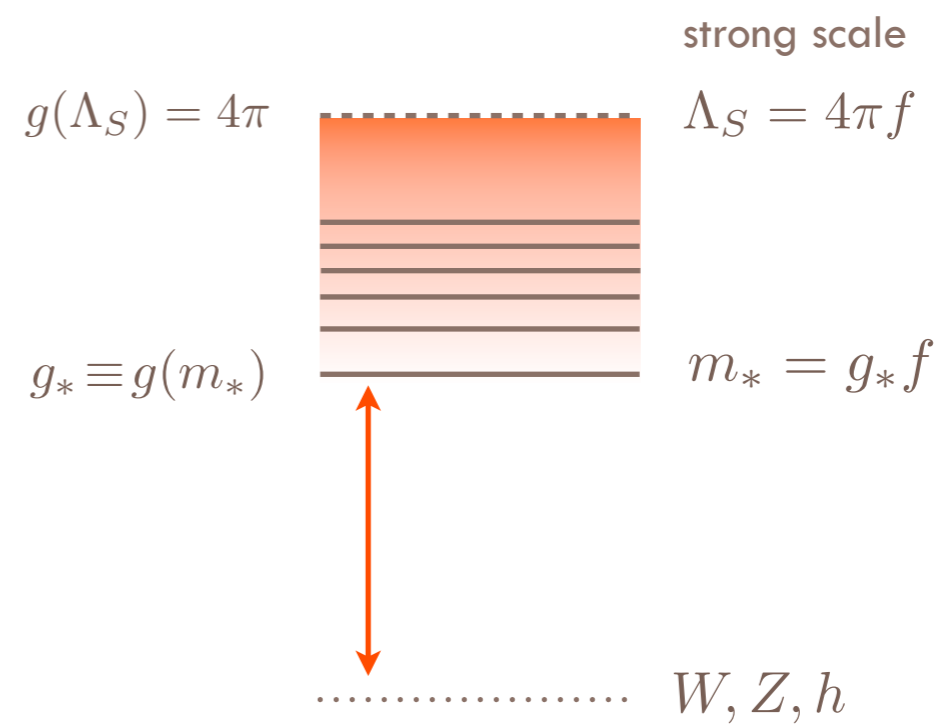
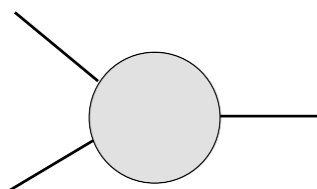
# Corrections to Higgs couplings

Precision measurement of Higgs couplings can give an appraisal of the strength of the underlying interactions



$$\frac{\delta\mathcal{O}}{\mathcal{O}} \sim \frac{v^2}{f^2} + \frac{g_*^2 v^2}{m_*^2}$$

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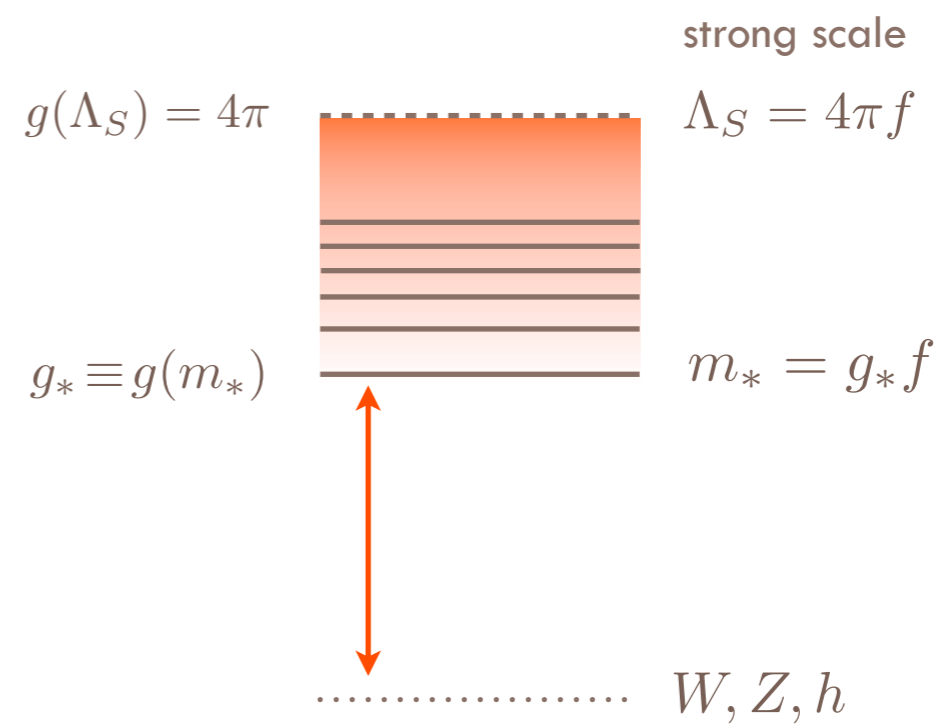
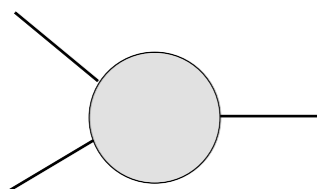


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from NL sigma model



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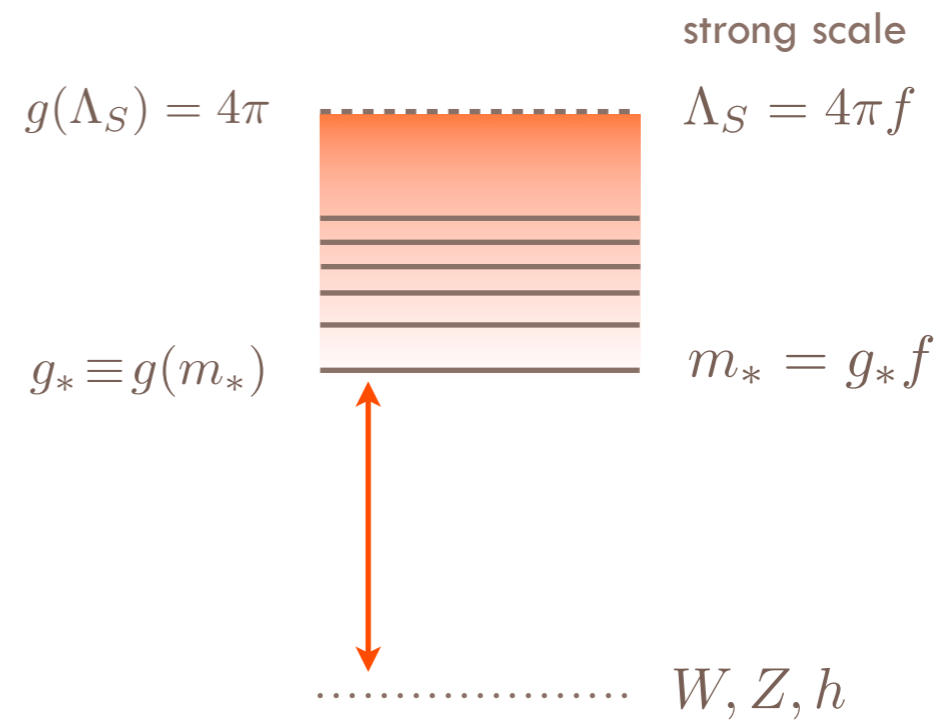
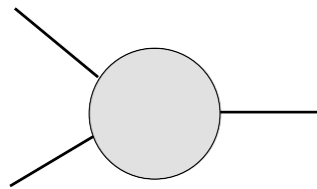


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Suppose we find:

$$\frac{\delta \mathcal{O}}{\mathcal{O}} \Big|_{exp} = \delta_{\mathcal{O}}^{exp}$$



$$g_* > \sqrt{\delta_{\mathcal{O}}^{exp}} \frac{M}{v}$$

$$m_* > M$$

(from direct searches)

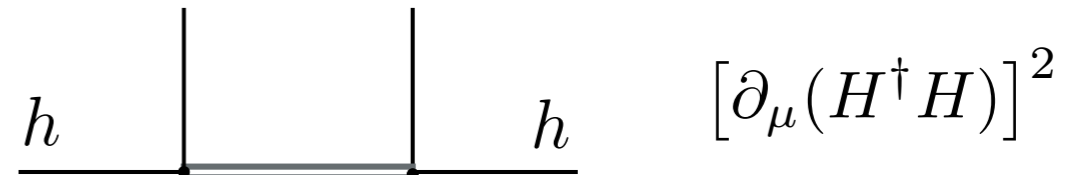
In practice resonance contribution is further suppressed:

$$\frac{\delta c}{c_{SM}} \sim \frac{v^2}{f^2} + \frac{g_*^2 v^2}{m_*^2} \times \frac{g_\phi^2}{g_*^2}$$

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tree-level coupling to vector bosons

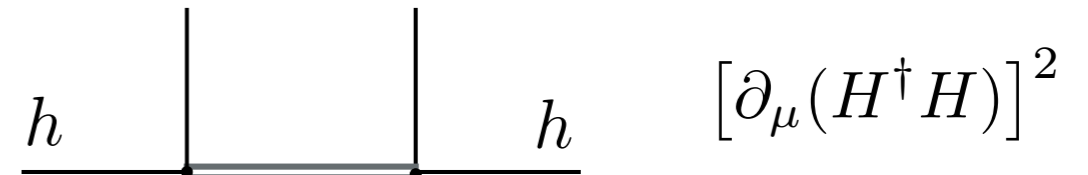


renormalization of NGB kinetic term requires breaking of Goldstone symmetry

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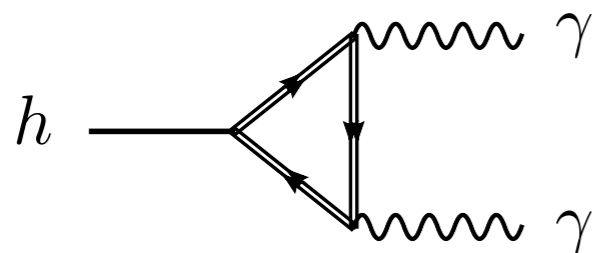
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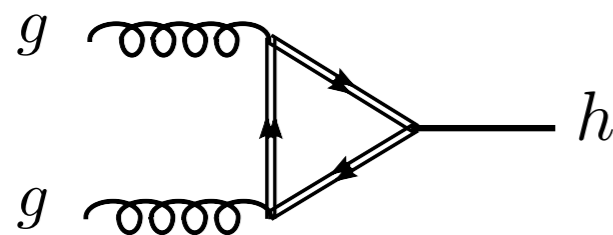


renormalization of NGB kinetic term requires breaking of Goldstone symmetry

loop-induced  $h \rightarrow \gamma\gamma, gg$



$$B_{\mu\nu}^2 H^\dagger H$$



$$G_{\mu\nu}^2 H^\dagger H$$

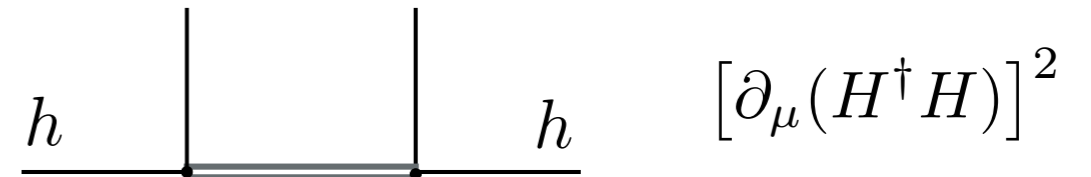
Effective operators violate the Higgs shift symmetry:

$$H^i \rightarrow H^i + \zeta^i$$

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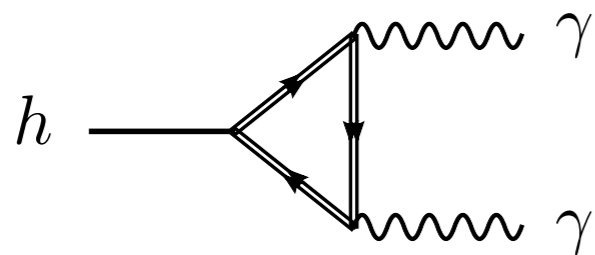
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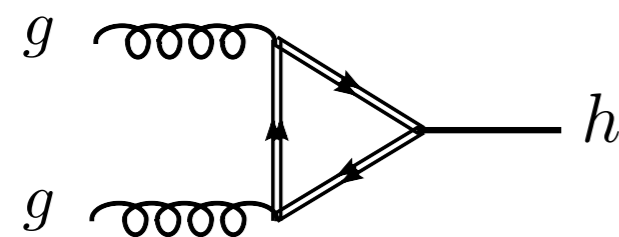


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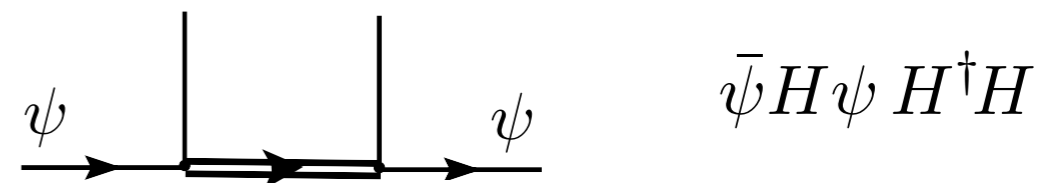


$$B_{\mu\nu}^2 H^\dagger H$$



$$G_{\mu\nu}^2 H^\dagger H$$

tree-level coupling to fermions



resonance corrections arise only from wavefunction renormalization in simplest models with partial compositeness

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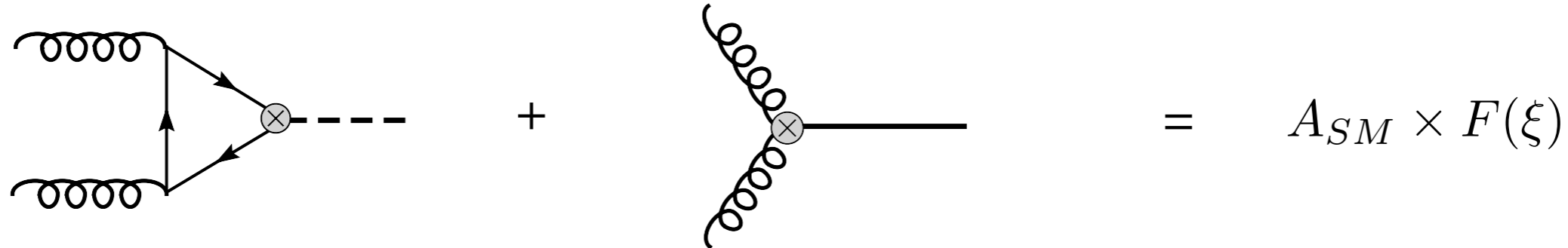
# Sum Rule for $h \rightarrow \gamma\gamma, gg$

relies on: Low Energy Theorem

$$A(gg \rightarrow h) \propto \frac{\partial}{\partial h} \log \det [\mathcal{M}^\dagger(h)\mathcal{M}(h)] \Big|_{h=v}$$

Partial compositeness

$$\det [\mathcal{M}^\dagger(h)\mathcal{M}(h)] \propto \lambda_L(h)\lambda_R(h)$$

$$A_{SM} \times c_t \quad \delta A = \frac{g_s^2}{16\pi^2} \times O\left(\frac{\lambda^2 v^2}{m_*^2}\right)$$


$$= A_{SM} \times F(\xi)$$

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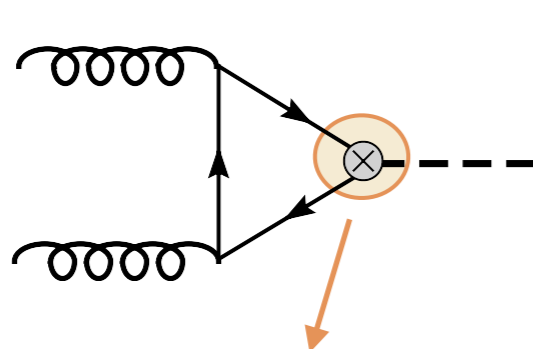
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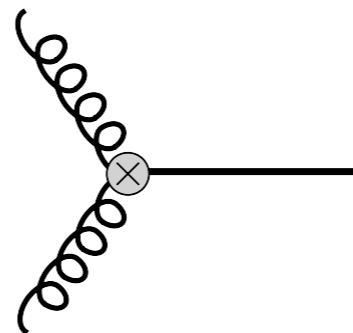
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+



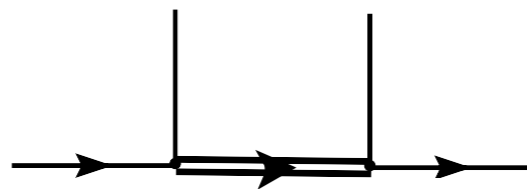
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$$c_t = \underbrace{F(\xi)}_{\text{from Higgs nl}\sigma\text{m}} + \underbrace{O\left(\frac{\lambda^2 v^2}{M^2}\right)}_{\text{from correction to wave-functions}}$$

from Higgs nl $\sigma$ m

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$$\xi \equiv \frac{v^2}{f^2}$$





# Sum Rule for $h \rightarrow \gamma\gamma, gg$

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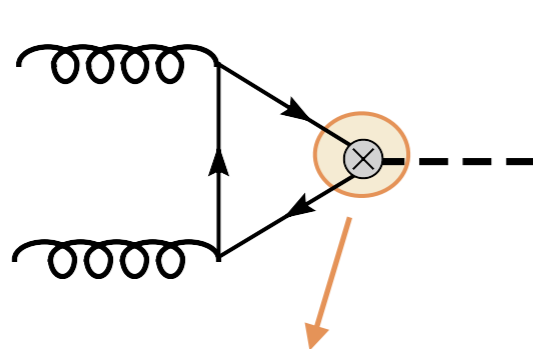
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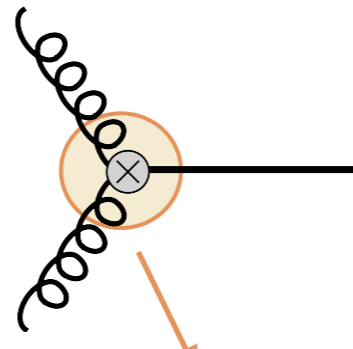
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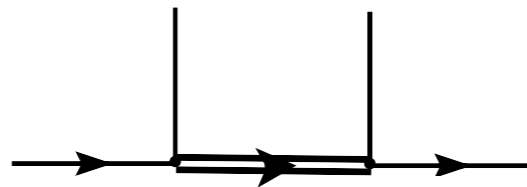
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$$c_t = F(\xi) + O\left(\frac{\lambda^2 v^2}{M^2}\right)$$

from Higgs nl $\sigma$ m

from correction to wave-functions

$$\xi \equiv \frac{v^2}{f^2}$$



Only exception is:  $h \rightarrow Z\gamma$

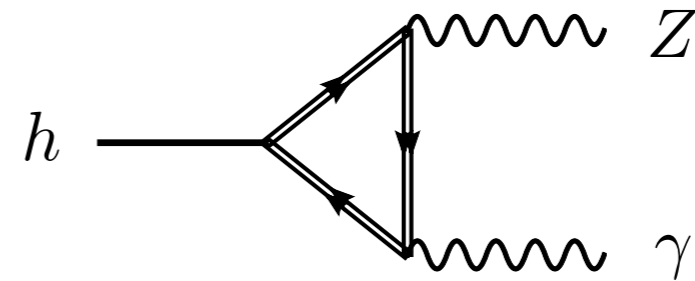
[ Azatov, RC , Di Iura, Galloway, work in progress]

$$\frac{\delta c_{Z\gamma}}{c_{Z\gamma}^{SM}} \sim \frac{v^2}{f^2} + \frac{g_*^2 v^2}{m_*^2}$$

Relevant operator is  $O_{HW} - O_{HB}$

$$O_{HB} = (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$

$$O_{HW} = (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i$$



1. Invariant under Higgs shift symmetry
2. Odd under LR exchange

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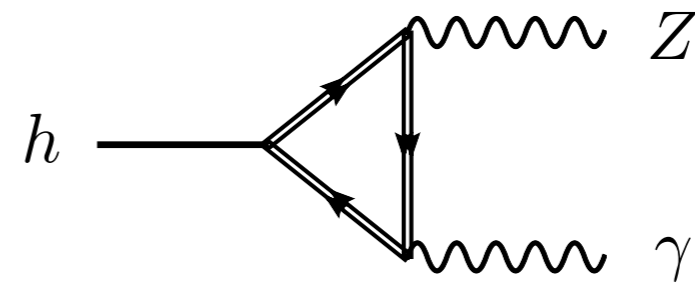
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Strong dynamics **MUST** break LR

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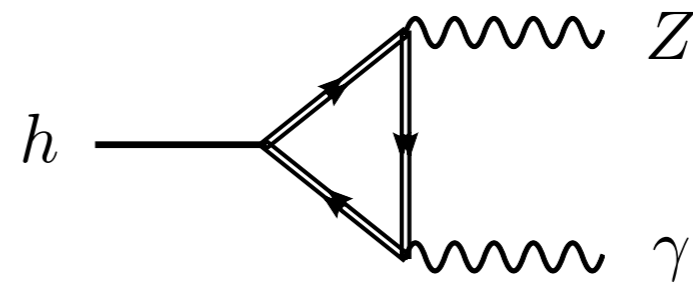
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Strong dynamics MUST break LR

$$A(h \rightarrow Z\gamma) = A_{SM} \times F(\xi) + \delta A$$

$$\frac{\delta A}{A_{SM}} \sim N_c N_F \left( \frac{g_*^2 v^2}{m_*^2} \right) \sim N_c N_F \frac{v^2}{f^2} \frac{\Delta m_*^2}{m_*^2}$$

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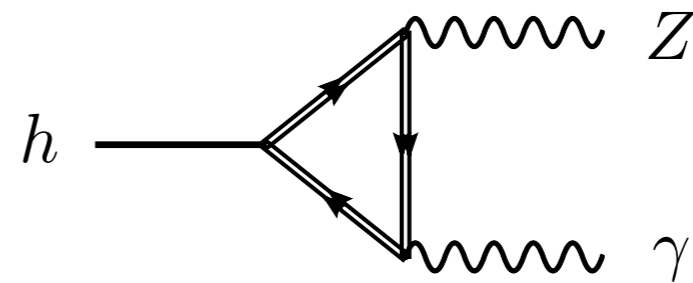
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shift of tree-level  
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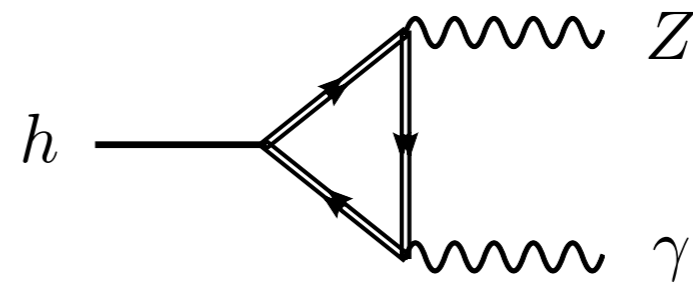
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multiplicity of composite states

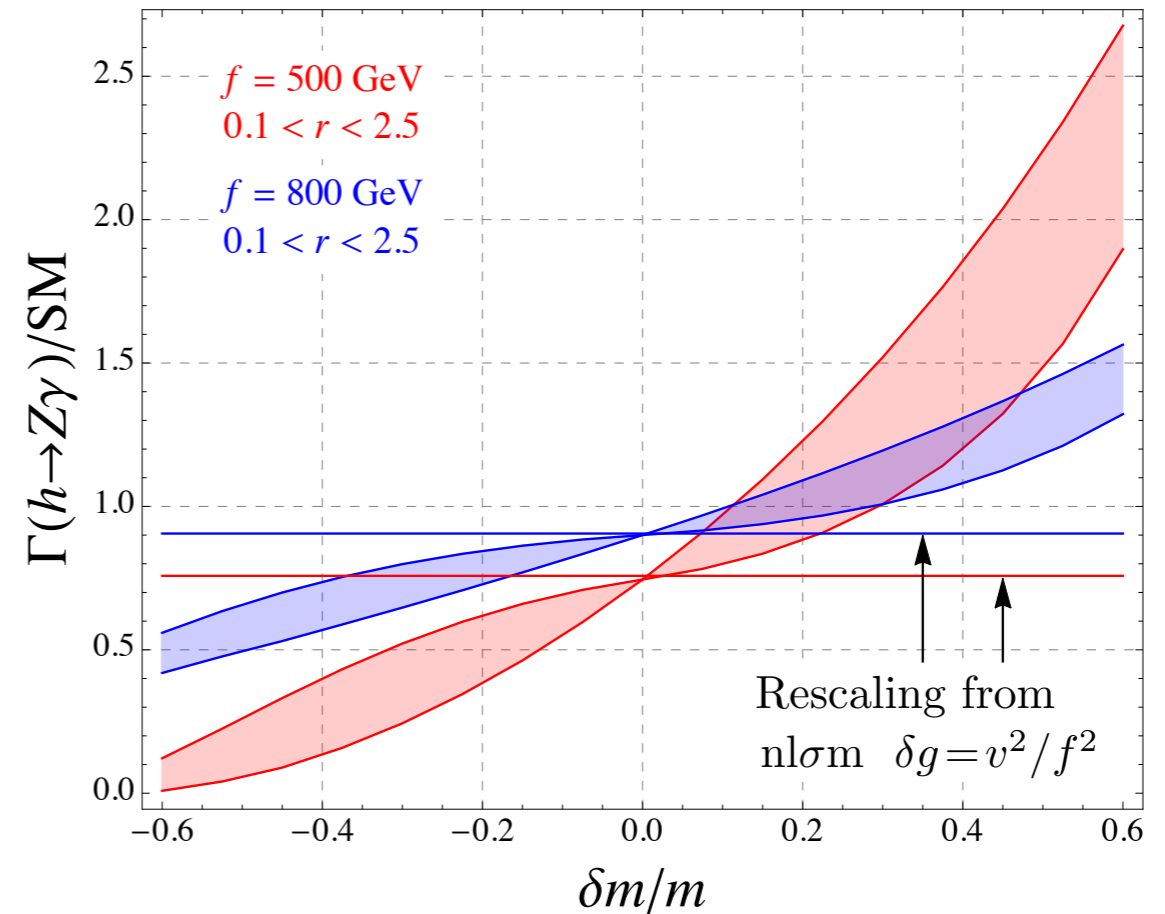
Only exception is:  $h \rightarrow Z\gamma$

[ Azatov, RC , Di Iura, Galloway, work in progress]

Relevant operator is  $O_{HW} - O_{HB}$

$$O_{HB} = (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$

$$O_{HW} = (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i$$



1. Invariant under Higgs shift symmetry

2. Odd under LR exchange



Strong dynamics MUST break LR

$$A(h \rightarrow Z\gamma) = A_{SM} \times F(\xi) + \delta A$$

shift of tree-level  
Higgs couplings  
from  $nI\sigma m$

$$1 + O\left(\frac{v^2}{f^2}\right)$$

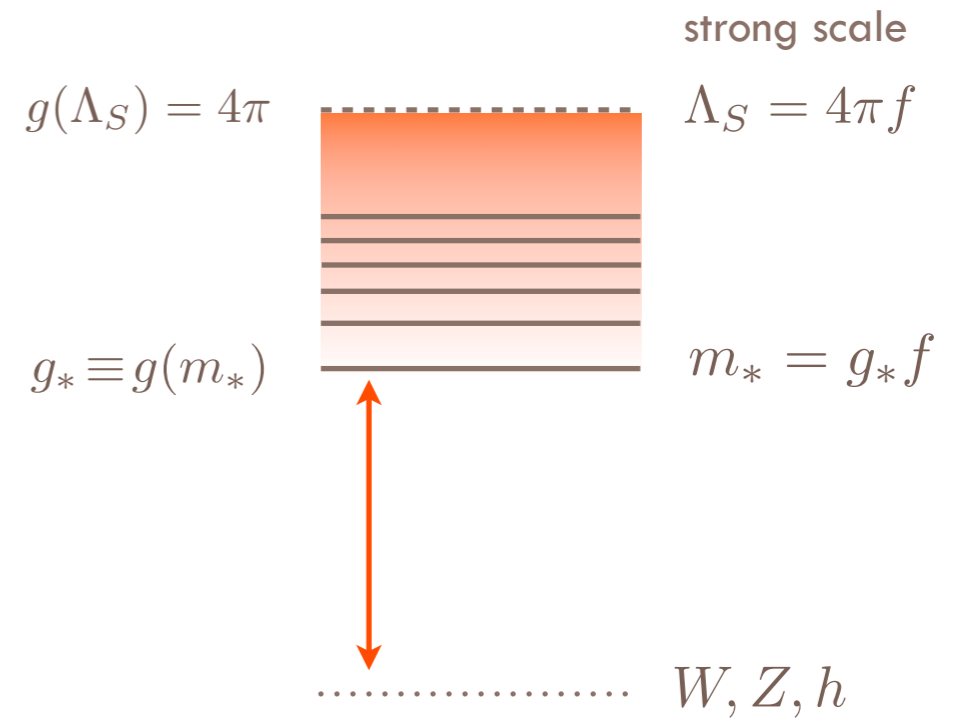
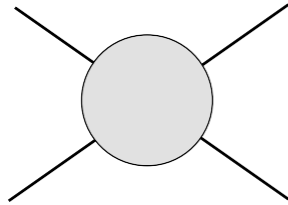
$$\frac{\delta A}{A_{SM}} \sim N_c N_F \left( \frac{g_*^2 v^2}{m_*^2} \right) \sim N_c N_F \frac{v^2}{f^2} \frac{\Delta m_*^2}{m_*^2}$$

multiplicity of  
composite states

# Tails in scattering amplitudes

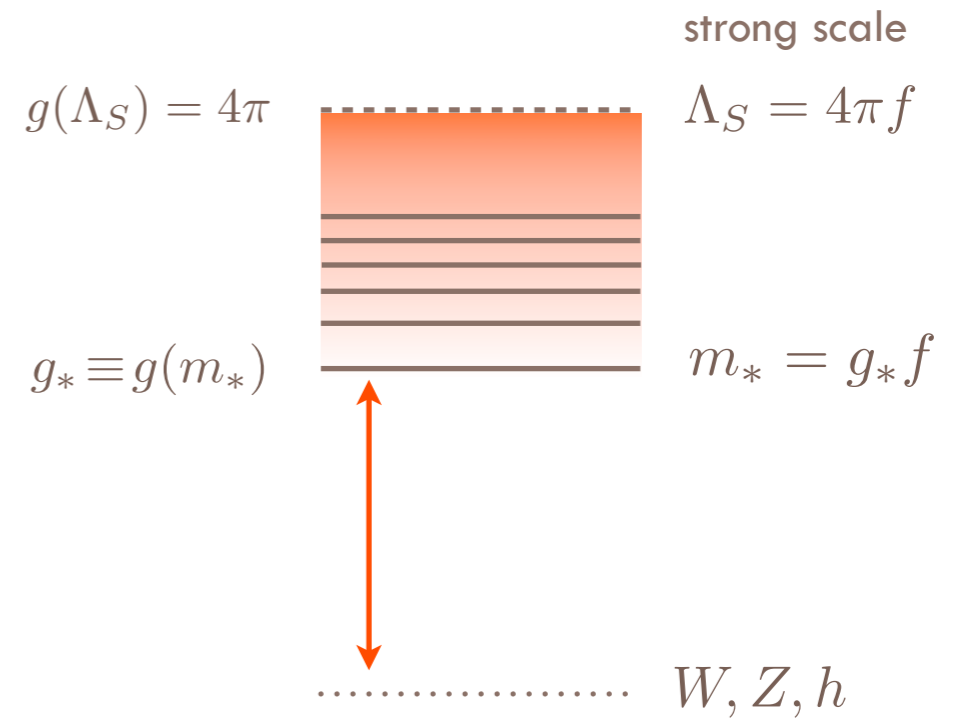
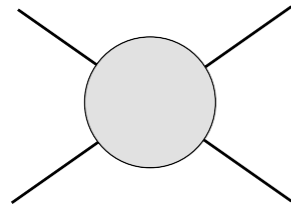


Precision measurement of scattering amplitudes can give an appraisal of the strength of the underlying interactions



$$\mathcal{A}(2 \rightarrow 2) = \delta_{hh} \frac{E^2}{v^2} \left( 1 + O\left(\frac{E^2}{m_*^2}\right) \right)$$

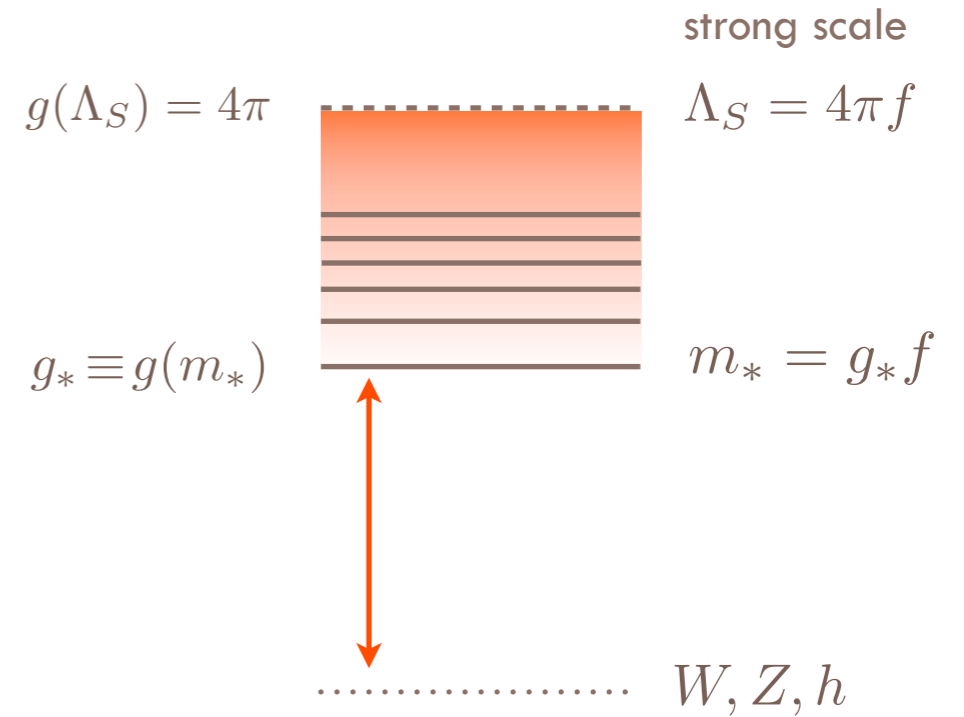
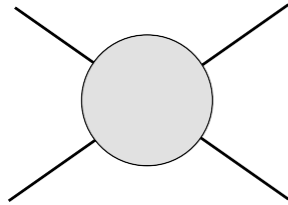
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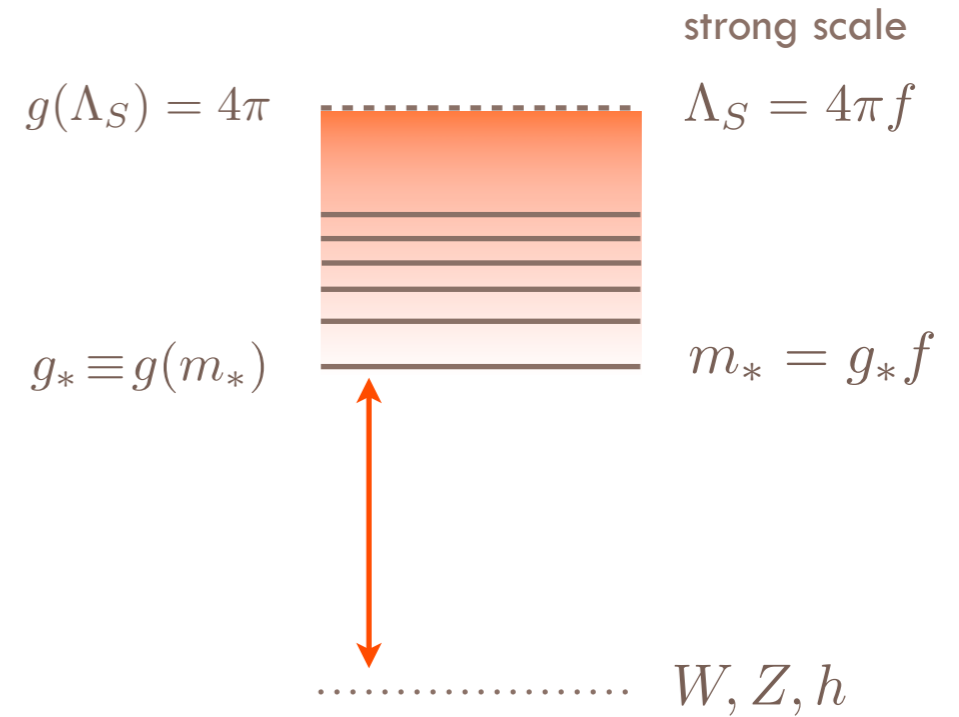
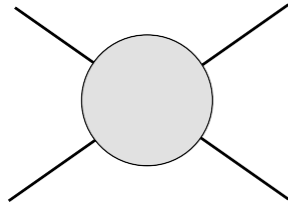
Suppose we find:

$$\delta_{hh}^{exp} \neq 0$$



$$g_* > g(E) = \sqrt{\delta_{hh}^{exp}} \frac{E}{v}$$

Precision measurement of scattering amplitudes can give an appraisal of the strength of the underlying interactions



Suppose we can bound  $\frac{E^2}{m_*^2} < \epsilon_{hh}$  hence  $m_* > \frac{E}{\sqrt{\epsilon_{hh}}} \equiv M$

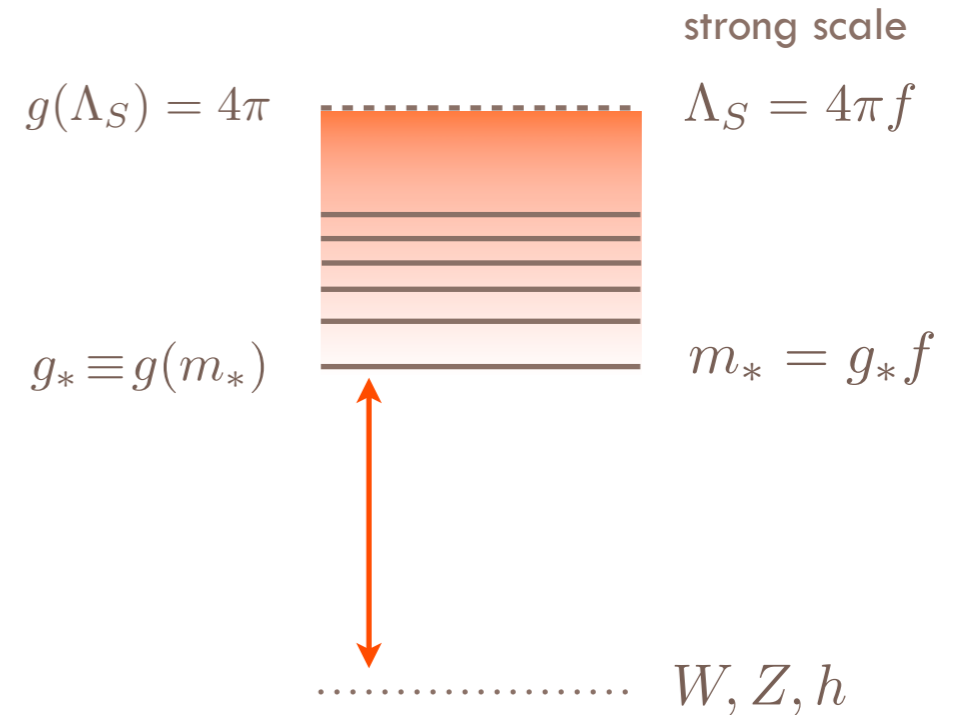
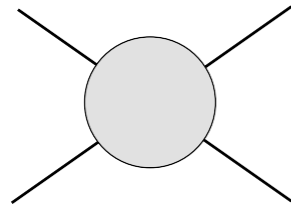
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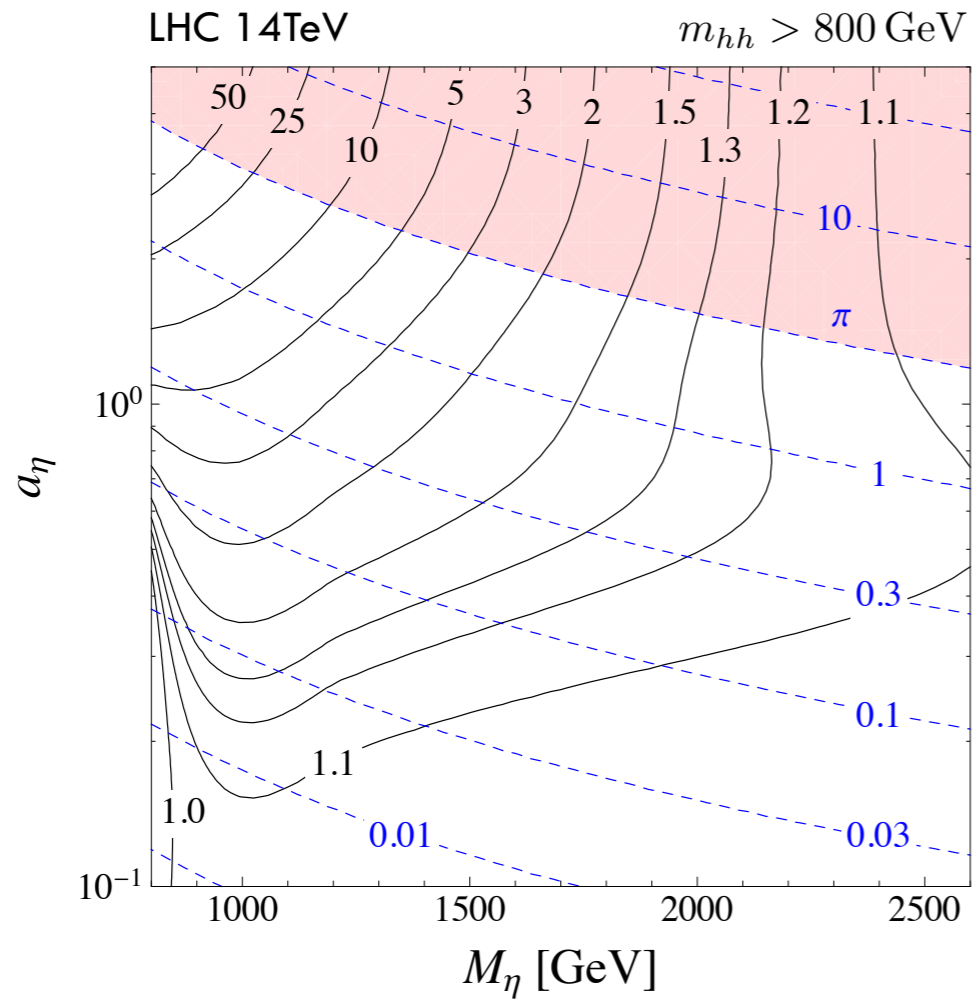
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$$g_* > g(E) = \sqrt{\delta_{hh}^{exp}} \frac{E}{v}$$

then we get the stronger limit

$$g_* > g(M) = \sqrt{\frac{\delta_{hh}^{exp}}{\epsilon_{hh}}} \frac{E}{v}$$



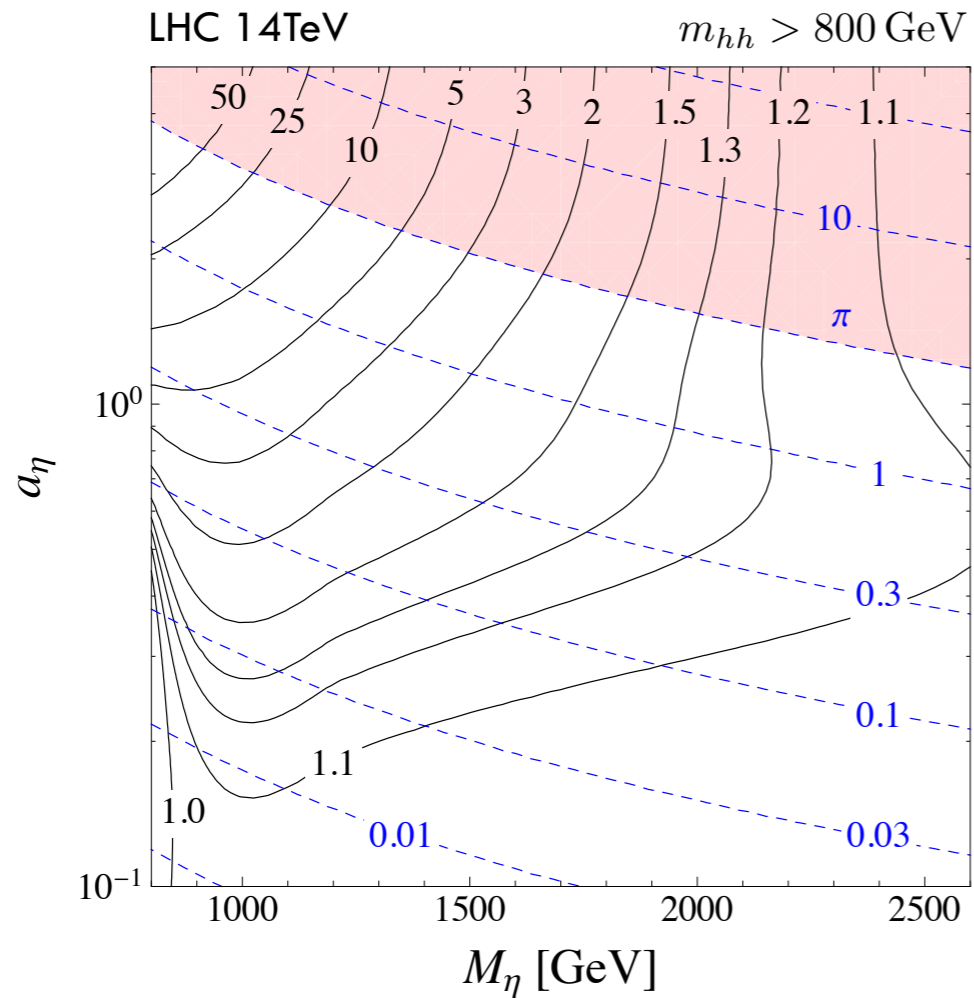
$$R = \frac{\sigma(pp \rightarrow hhjj)}{\sigma(pp \rightarrow hhjj)|_{LET}}$$

$$\mathcal{L} = \frac{a_\eta}{2f} \eta (\partial_\mu \pi)^2 + \dots$$

[ RC, Marzocca, Pappadopulo, Rattazzi, JHEP 1110(2011)081 ]

$$\mathcal{A}(2 \rightarrow 2) = \delta_{hh} \frac{E^2}{v^2} \left( 1 + O\left(\frac{E^2}{m_*^2}\right) \right)$$

measurement of resonance effects  
gives direct access to strong dynamics



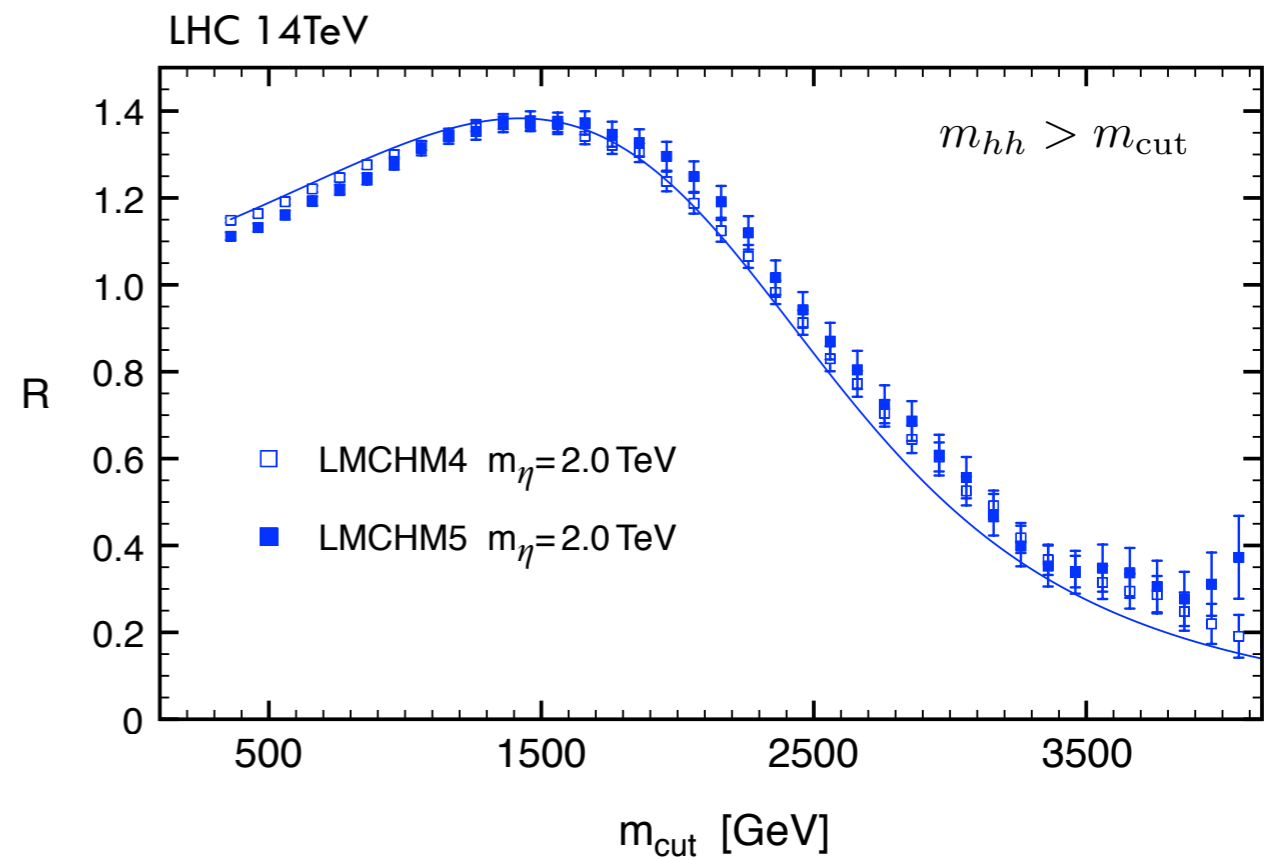
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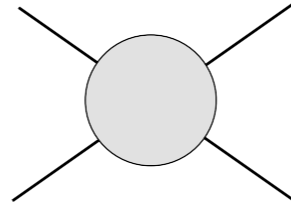
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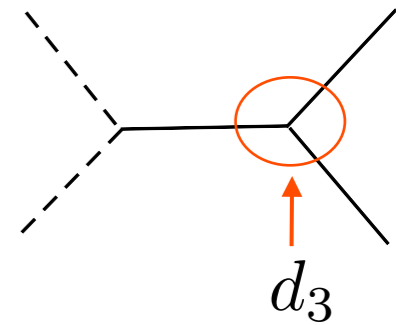
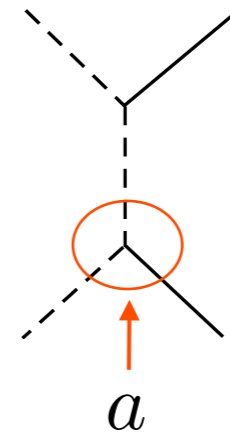
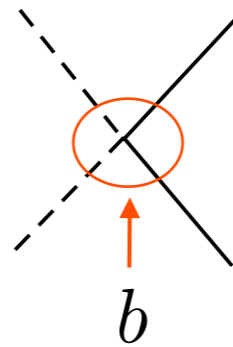
A high-energy  $e^+e^-$  collider  
(such as CLIC 3TeV) can  
provide a clean environment to  
make precision studies of  
scattering amplitudes



[ RC , Grojean, Pappadopulo,  
Rattazzi, Thamm, to appear ]

Example:  $WW \rightarrow hh$

$$A(WW \rightarrow hh) \sim \frac{s}{v^2}(a^2 - b)$$



dim 6:  $O_H = \frac{c_H}{2f^2} \partial_\mu |H|^2 \partial^\mu |H|^2$

$$a = 1 - \frac{c_H}{2} \frac{v^2}{f^2} + \left( \frac{3c_H^2}{8} - \frac{c'_H}{4} \right) \frac{v^4}{f^4}$$

dim 8:  $O'_H = \frac{c'_H}{2f^4} |H|^2 \partial_\mu |H|^2 \partial^\mu |H|^2$

$$b = 1 - 2c_H \frac{v^2}{f^2} + \left( 3c_H^2 - \frac{3c'_H}{2} \right) \frac{v^4}{f^4}$$



Ex:  $SO(5)/SO(4)$

In PNGB Higgs theories the whole series in  $H/f$  can be resummed:

$$a = \sqrt{1 - \xi}$$

$$\xi = \frac{v^2}{f^2}$$

$$b = 1 - 2\xi$$

At dimension-6 level:

$$\Delta b = 2\Delta a^2 (1 + O(\Delta a^2))$$

$$\Delta b \equiv 1 - b$$
$$\Delta a^2 \equiv 1 - a^2$$

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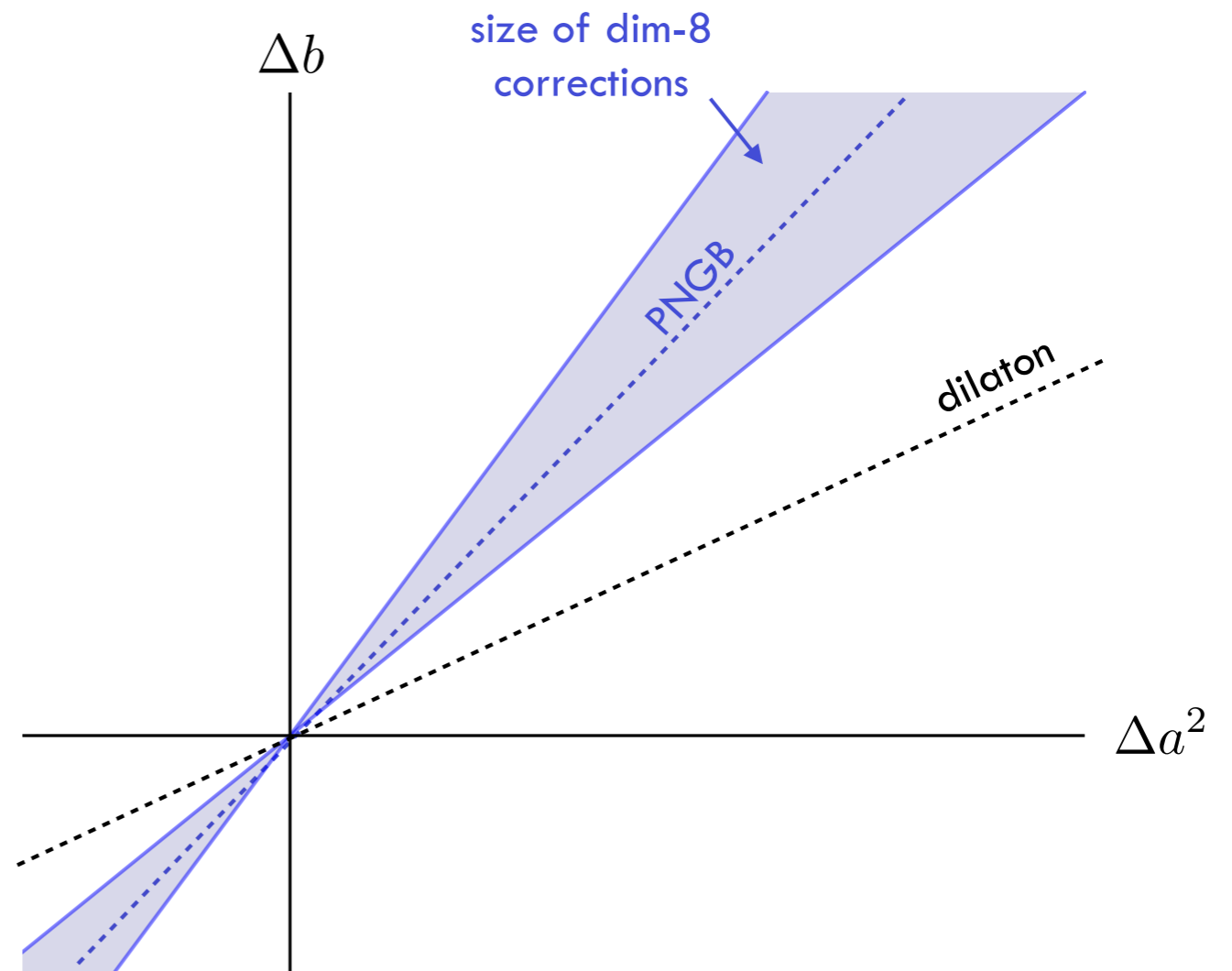
Scenario 1:

$$\Delta a^2 \sim \Delta b \sim 10\%$$

Exp. precision  $\sim 1\%$



Test dim-8 operators



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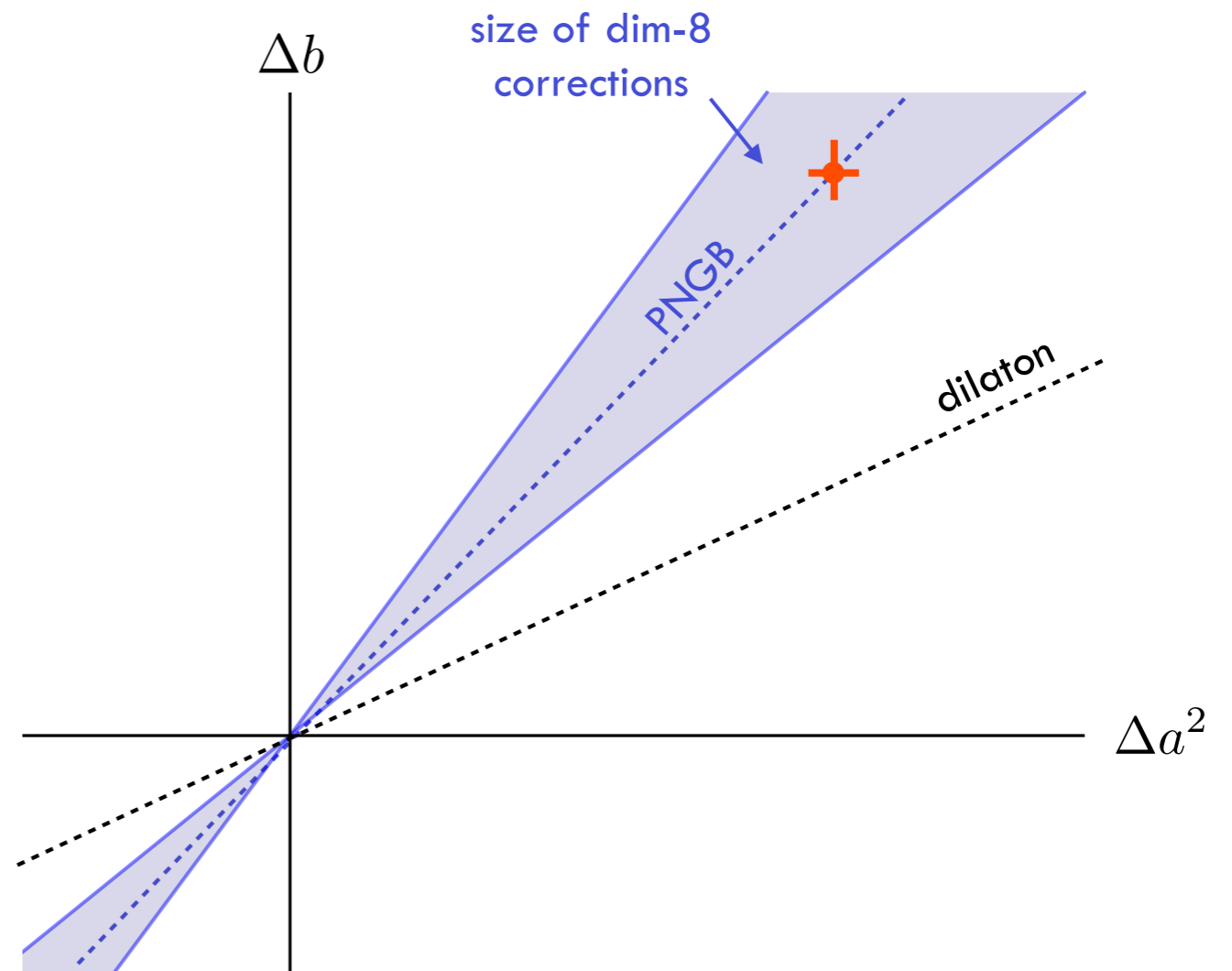
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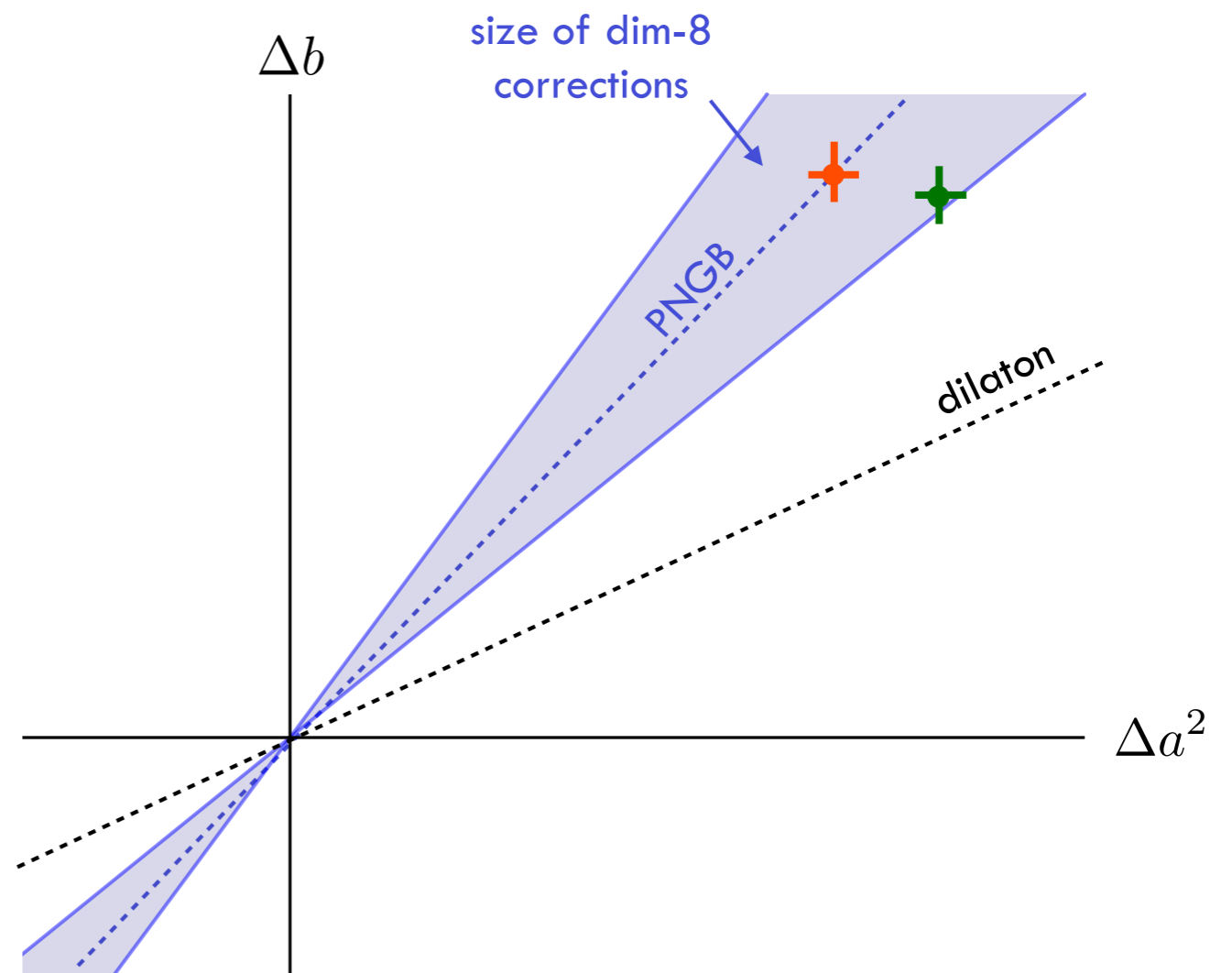
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2. SILH proved, PNGB disproved



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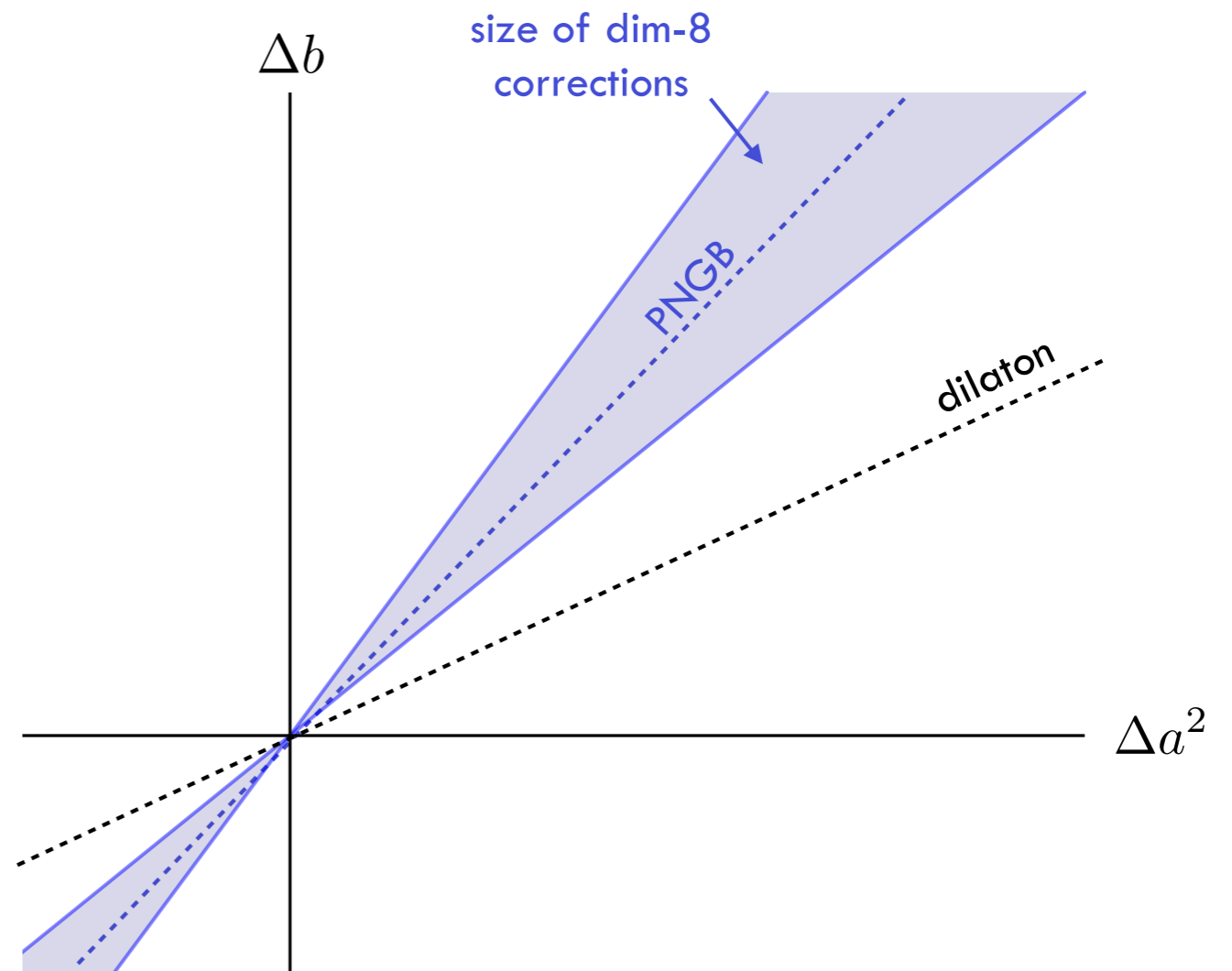
$$\Delta b \equiv 1 - b$$

$$\Delta a^2 \equiv 1 - a^2$$

Scenario 2:

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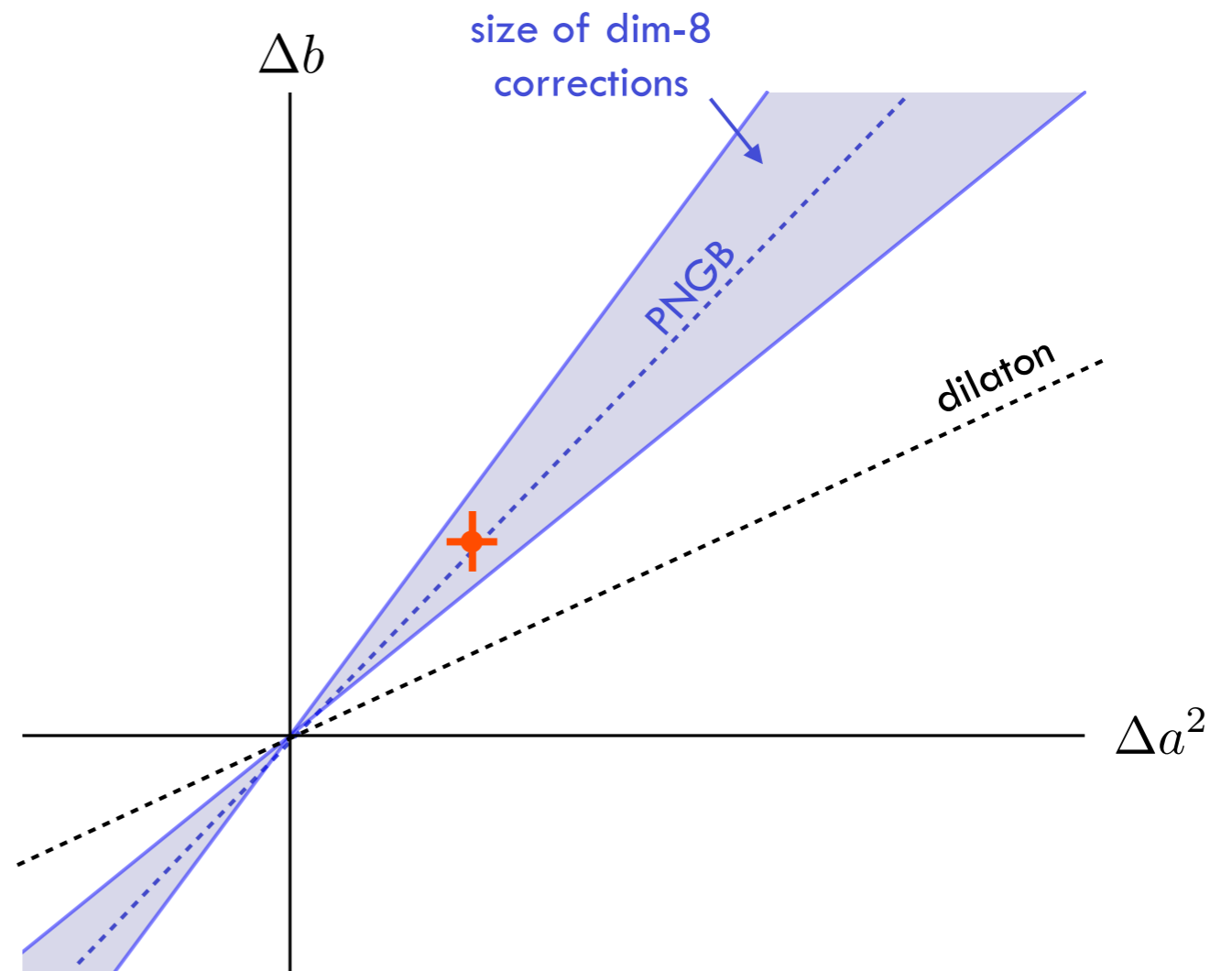
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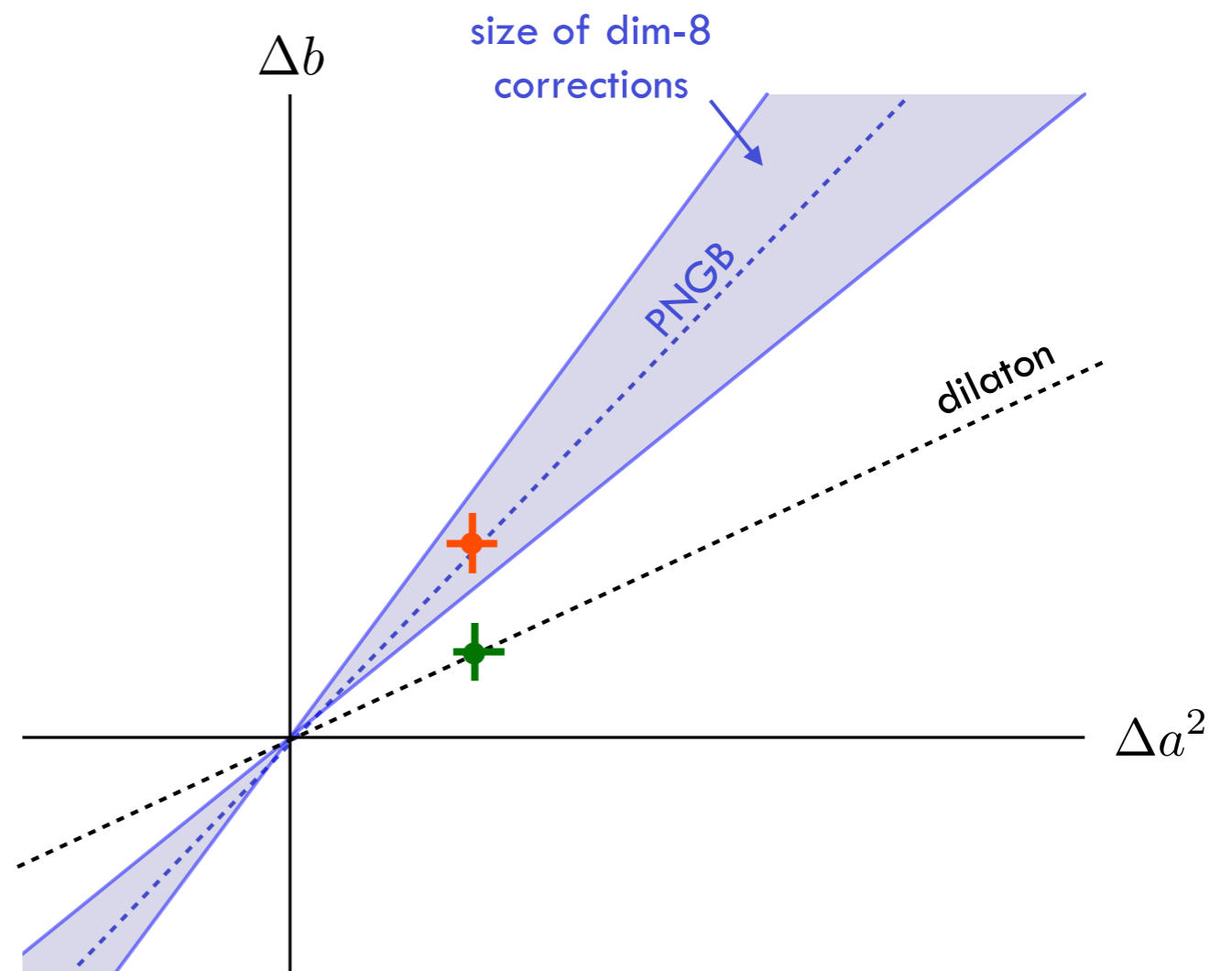
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Exp. precision  $\sim 1\%$

1. SILH proved
2. SILH (i.e. Higgs doublet) disproved



An  $e^+e^-$  collider with  $\sqrt{s} = 3 \text{ TeV}$  can reach a precision of a few % on the coupling  $b$  through the process  $e^+e^- \rightarrow \nu\bar{\nu} hh \rightarrow \nu\bar{\nu} b\bar{b}b\bar{b}$

Barger et al. PRD 67 (2003) 115001

RC , Grojean, Pappadopulo, Rattazzi, Thamm, to appear

Expected precision on  $\delta_b$  with  $L = 1 \text{ ab}^{-1}/a^4$

measured $\delta_b$	$\bar{\delta}_{d_3}$						
	-0.5	-0.3	-0.1	0	0.1	0.3	0.5
0	$-0.01^{+0.03}_{-0.09}$	$0.01^{+0.03}_{-0.10}$	$0.01^{+0.03}_{-0.04}$	$0.01^{+0.04}_{-0.04}$	$0.01^{+0.04}_{-0.04}$	$0.0^{+0.03}_{-0.03}$	$0.0^{+0.02}_{-0.03}$
0.01	$0.01^{+0.03}_{-0.10}$	$0.02^{+0.03}_{-0.04}$	$0.02^{+0.03}_{-0.04}$	$0.02^{+0.04}_{-0.04}$	$0.02^{+0.04}_{-0.03}$	$0.01^{+0.03}_{-0.03}$	$0.01^{+0.02}_{-0.03}$
0.02	$0.02^{+0.03}_{-0.04}$	$0.03^{+0.03}_{-0.04}$	$0.03^{+0.04}_{-0.04}$	$0.03^{+0.05}_{-0.03}$	$0.02^{+0.05}_{-0.03}$	$0.02^{+0.02}_{-0.03}$	$0.02^{+0.02}_{-0.03}$
0.03	$0.03^{+0.02}_{-0.04}$	$0.04^{+0.03}_{-0.03}$	$0.04^{+0.04}_{-0.03}$	$0.04^{+0.05}_{-0.03}$	$0.03^{+0.06}_{-0.03}$	$0.03^{+0.08}_{-0.03}$	$0.03^{+0.02}_{-0.03}$
0.05	$0.05^{+0.02}_{-0.03}$	$0.06^{+0.03}_{-0.03}$	$0.07^{+0.05}_{-0.03}$	$0.06^{+0.06}_{-0.03}$	$0.05^{+0.03}_{-0.03}$	$0.05^{+0.09}_{-0.02}$	$0.05^{+0.10}_{-0.02}$
0.1	$0.11^{+0.02}_{-0.03}$	$0.13^{+0.03}_{-0.04}$	$0.11^{+0.07}_{-0.02}$	$0.1^{+0.03}_{-0.02}$	$0.1^{+0.06}_{-0.02}$	$0.1^{+0.02}_{-0.02}$	$0.1^{+0.02}_{-0.02}$
0.3	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$
0.5	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$

$$\delta_b = 1 - b/a^2$$

$$\delta_{d_3} = 1 - d_3/a$$



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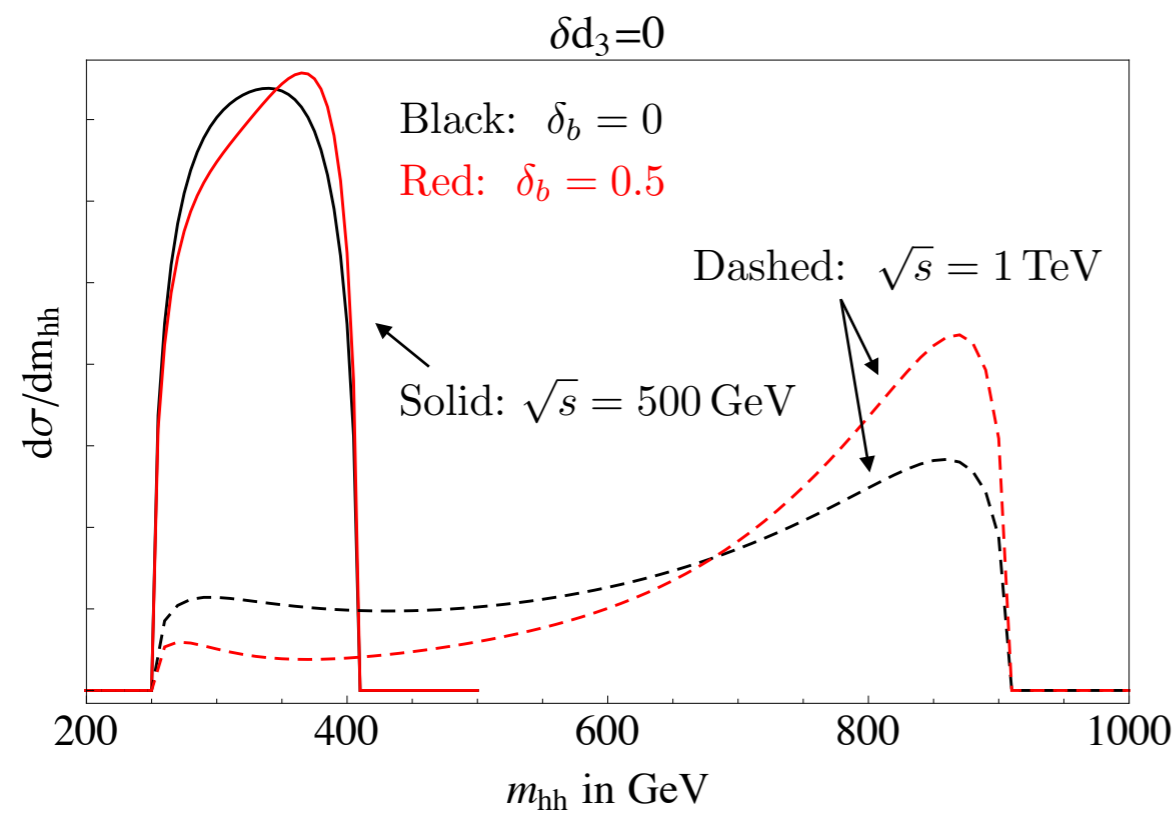
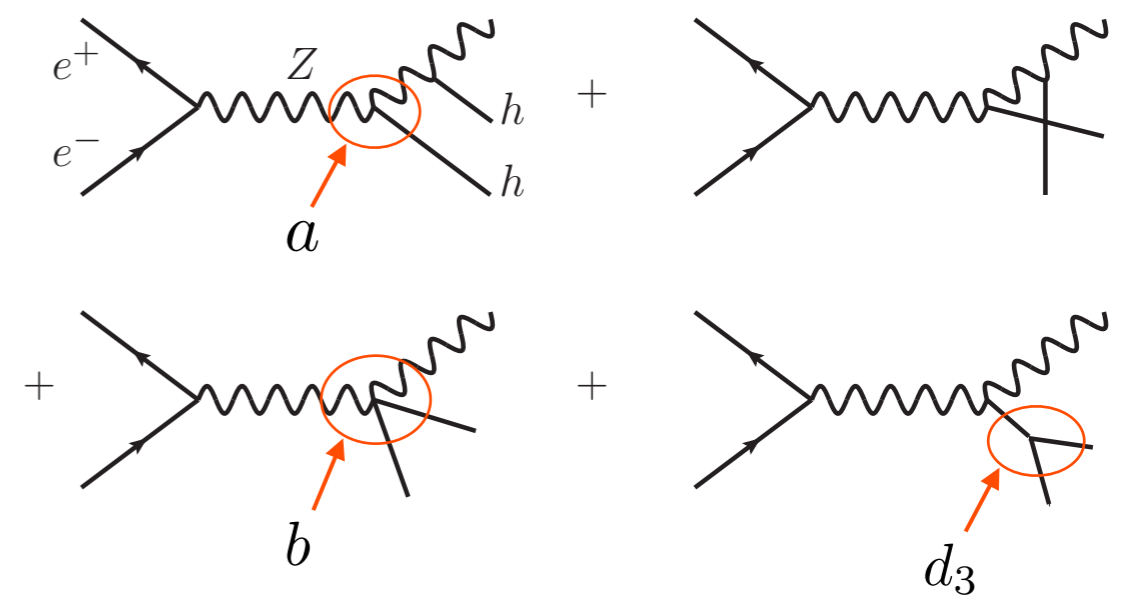
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	-0.5	-0.3	-0.1	0	0.1	0.3	0.5
0	$-0.01^{+0.03}_{-0.09}$	$0.01^{+0.03}_{-0.10}$	$0.01^{+0.03}_{-0.04}$	$0.01^{+0.04}_{-0.04}$	$0.01^{+0.04}_{-0.04}$	$0.0^{+0.03}_{-0.03}$	$0.0^{+0.02}_{-0.03}$
0.01	$0.01^{+0.03}_{-0.10}$	$0.02^{+0.03}_{-0.04}$	$0.02^{+0.03}_{-0.04}$	$0.02^{+0.04}_{-0.04}$	$0.02^{+0.04}_{-0.03}$	$0.01^{+0.03}_{-0.03}$	$0.01^{+0.02}_{-0.03}$
0.02	$0.02^{+0.03}_{-0.04}$	$0.03^{+0.03}_{-0.04}$	$0.03^{+0.04}_{-0.04}$	$0.03^{+0.05}_{-0.03}$	$0.02^{+0.05}_{-0.03}$	$0.02^{+0.02}_{-0.03}$	$0.02^{+0.02}_{-0.03}$
0.03	$0.03^{+0.02}_{-0.04}$	$0.04^{+0.03}_{-0.03}$	$0.04^{+0.04}_{-0.03}$	$0.04^{+0.05}_{-0.03}$	$0.03^{+0.06}_{-0.03}$	$0.03^{+0.08}_{-0.03}$	$0.03^{+0.02}_{-0.03}$
0.05	$0.05^{+0.02}_{-0.03}$	$0.06^{+0.03}_{-0.03}$	$0.07^{+0.05}_{-0.03}$	$0.06^{+0.06}_{-0.03}$	$0.05^{+0.03}_{-0.03}$	$0.05^{+0.09}_{-0.02}$	$0.05^{+0.10}_{-0.02}$
0.1	$0.11^{+0.02}_{-0.03}$	$0.13^{+0.03}_{-0.04}$	$0.11^{+0.07}_{-0.02}$	$0.1^{+0.03}_{-0.02}$	$0.1^{+0.06}_{-0.02}$	$0.1^{+0.02}_{-0.02}$	$0.1^{+0.02}_{-0.02}$
0.3	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$	$0.3^{+0.02}_{-0.02}$
0.5	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$	$0.5^{+0.02}_{-0.02}$

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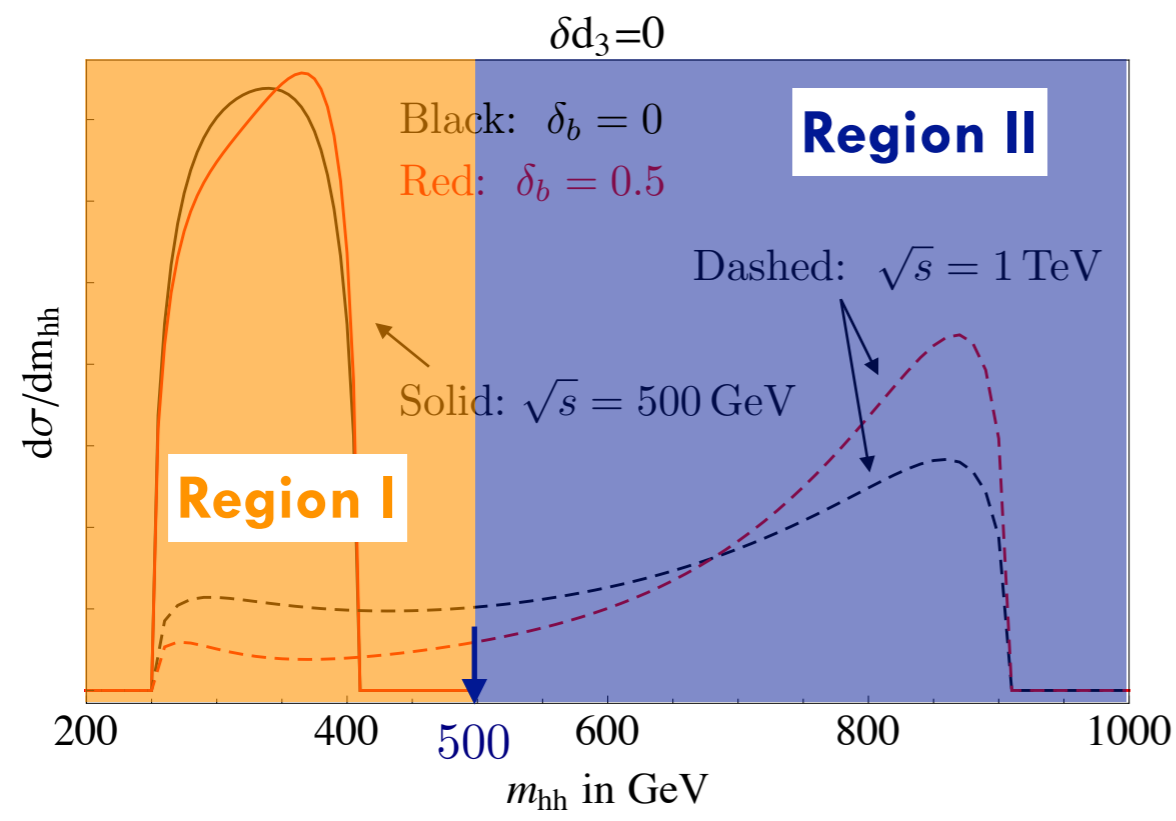
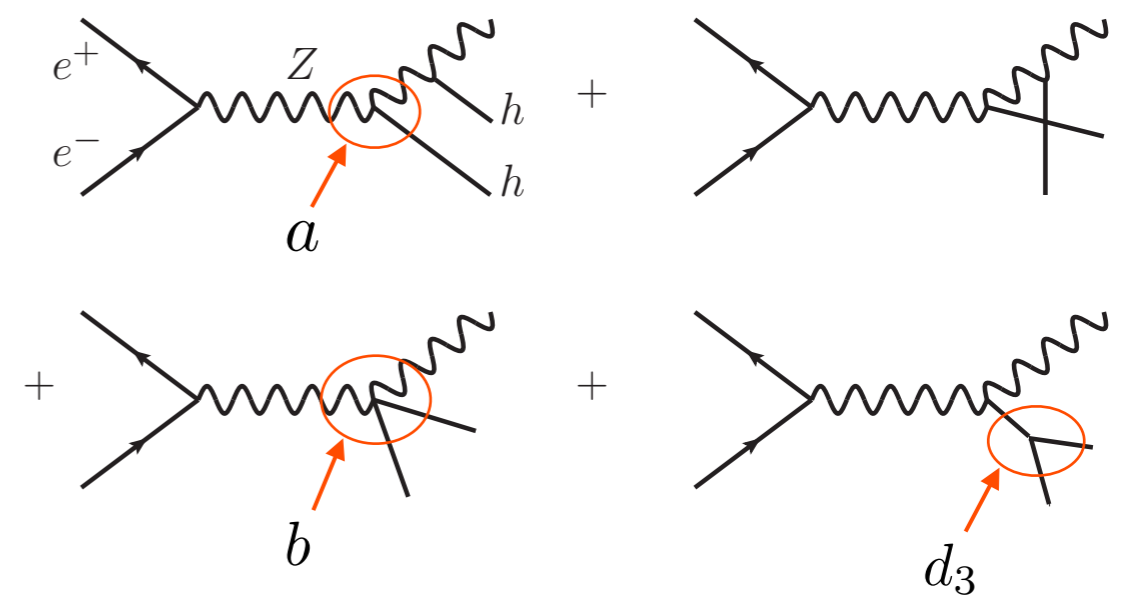
An  $e^+e^-$  collider with  $\sqrt{s} = 500 \text{ GeV} - 1 \text{ TeV}$  can reach a precision of  $\sim 20\%$  on  $b$  through the double Higgsstrahlung process

RC , Grojean, Pappadopulo, Rattazzi, Thamm, to appear



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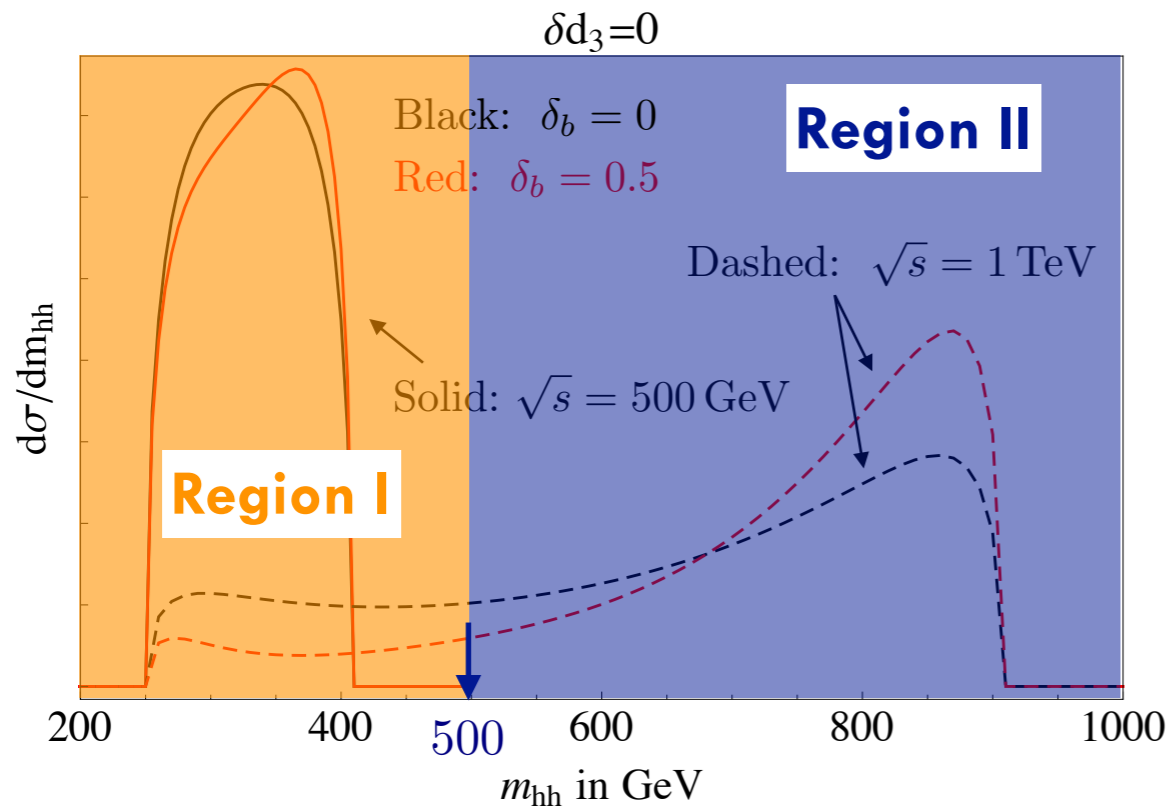
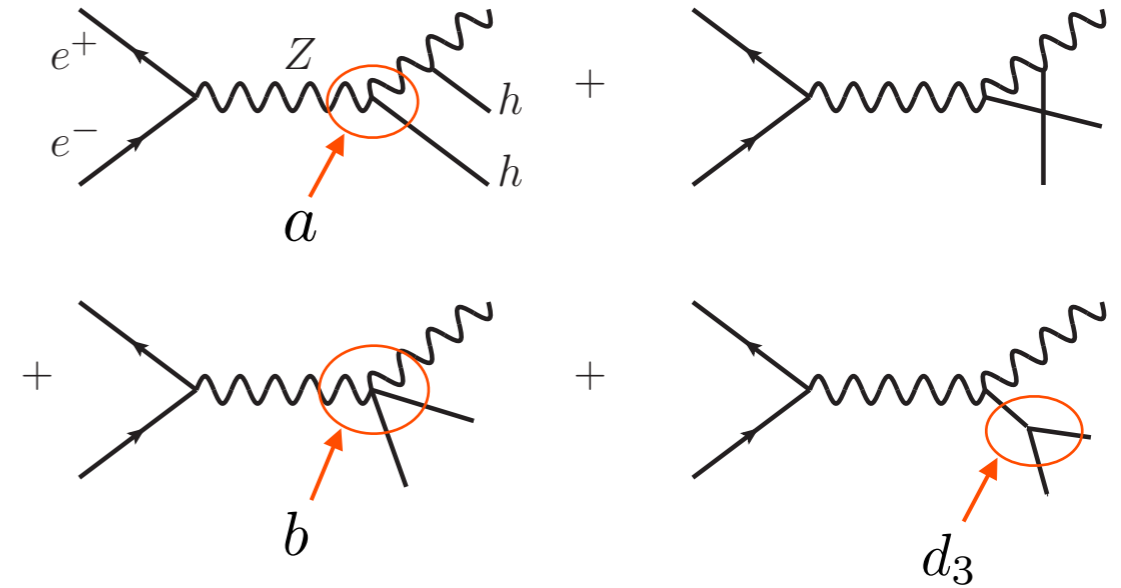
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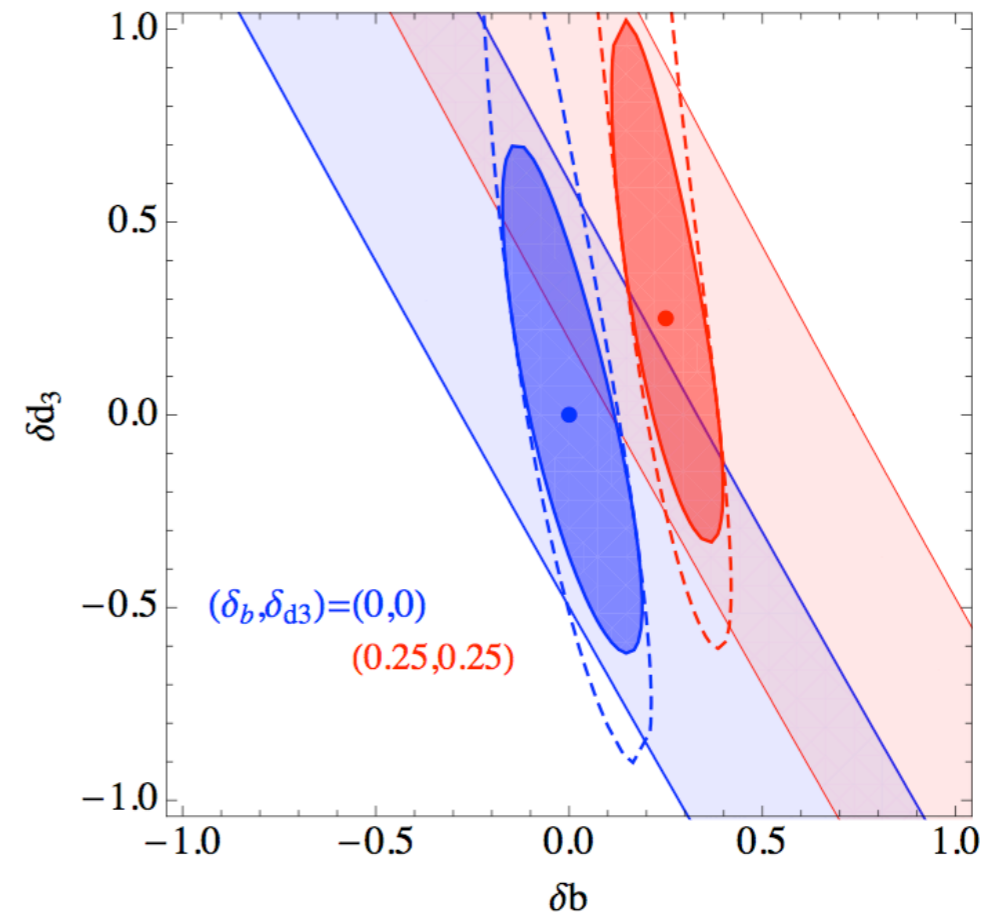
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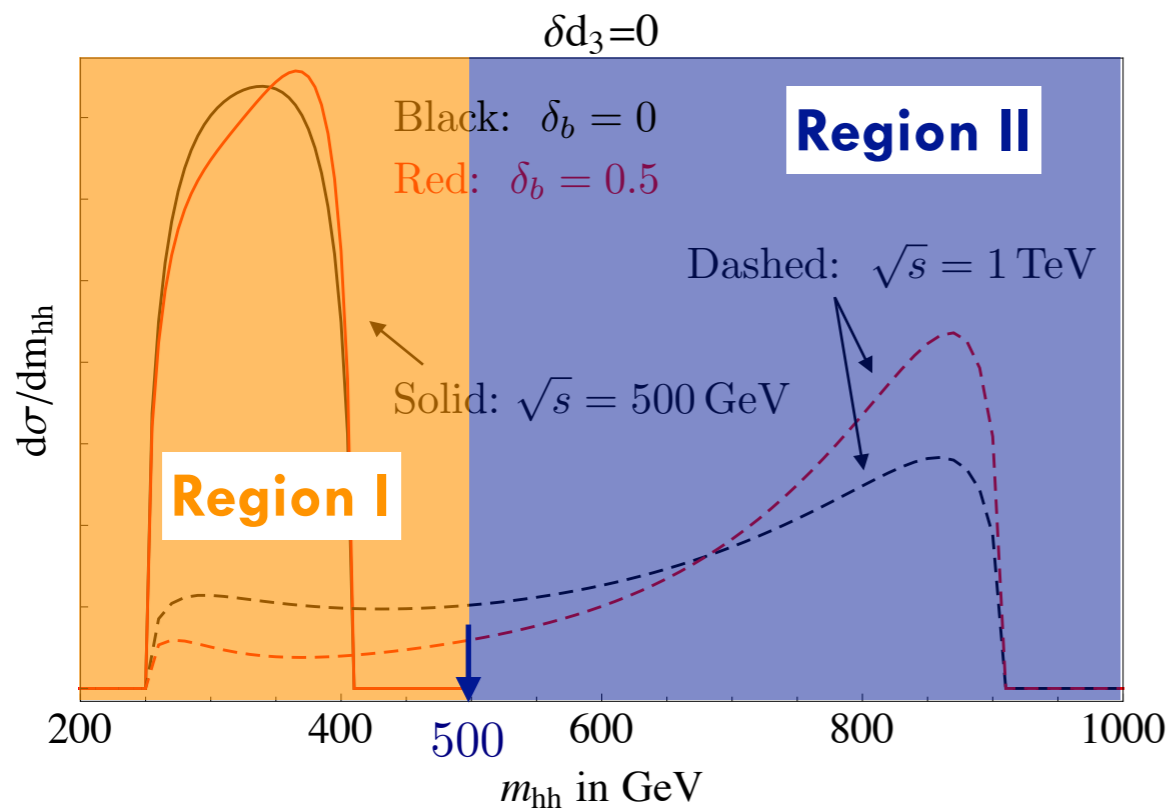
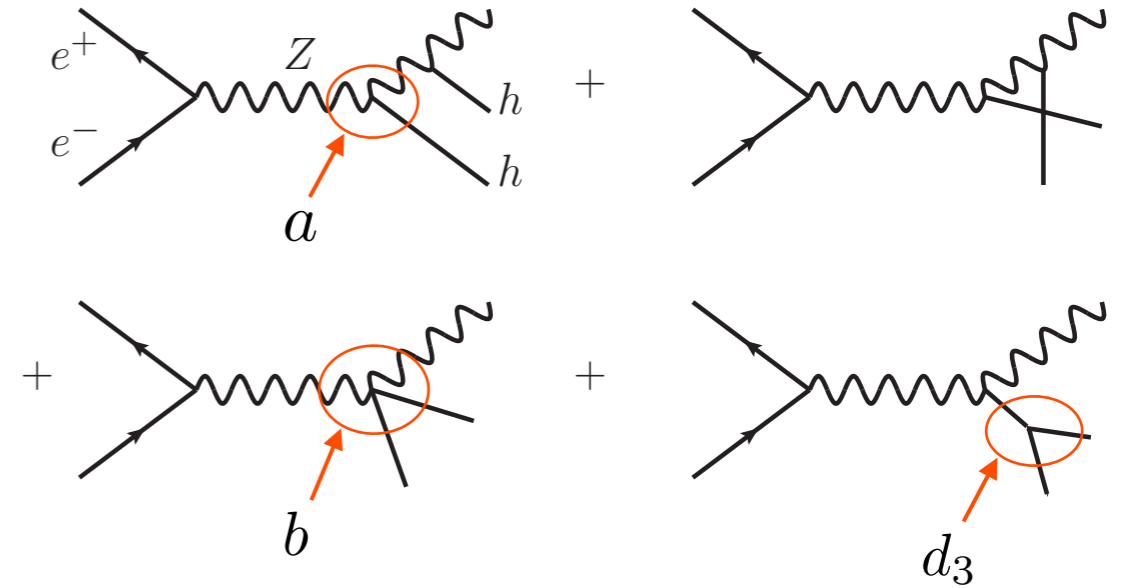


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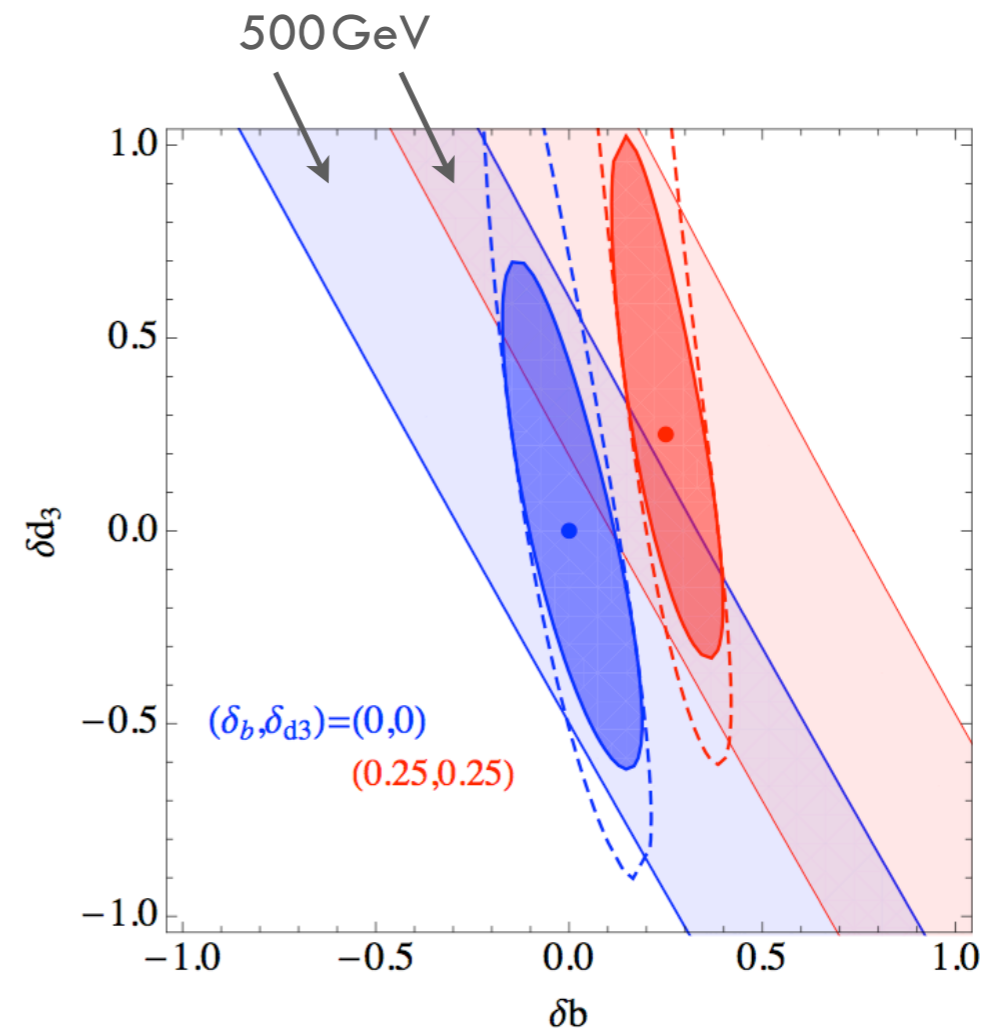


An  $e^+e^-$  collider with  $\sqrt{s} = 500 \text{ GeV} - 1 \text{ TeV}$  can reach a precision of  $\sim 20\%$  on  $b$  through the double Higgsstrahlung process

RC, Grojean, Pappadopulo, Rattazzi, Thamm, to appear

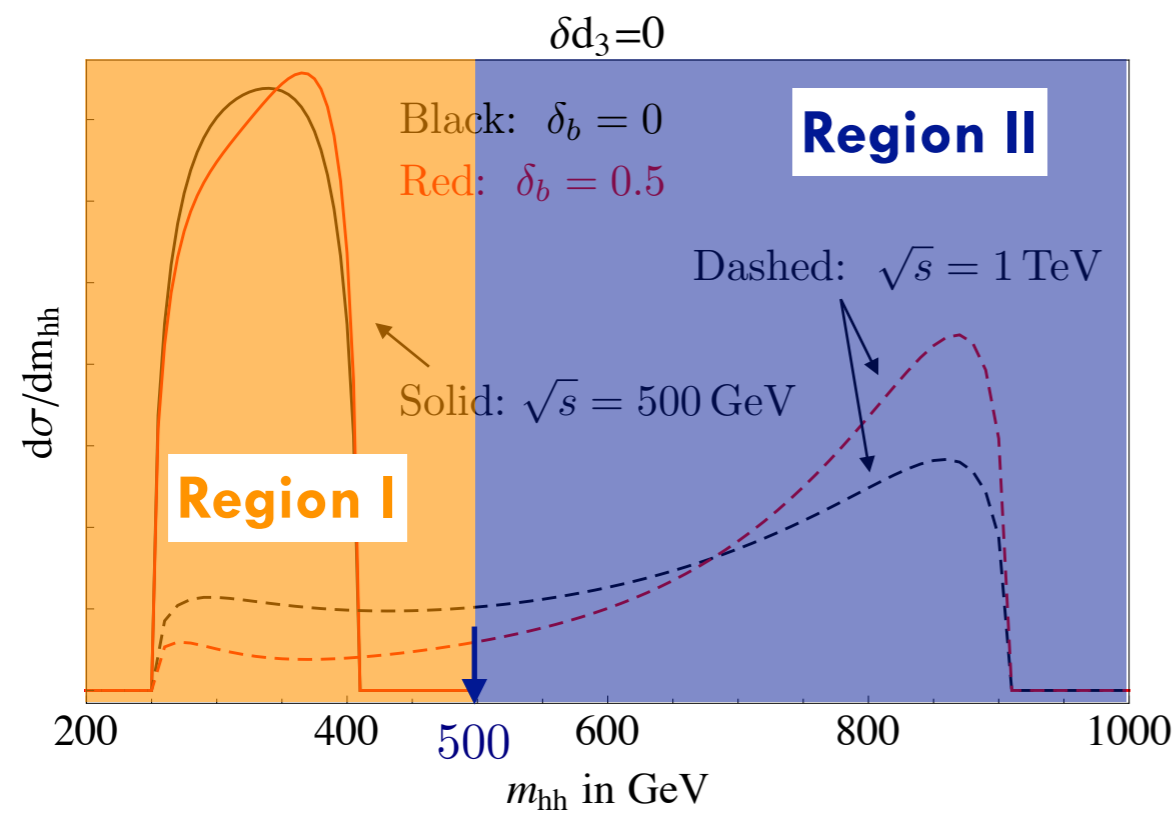
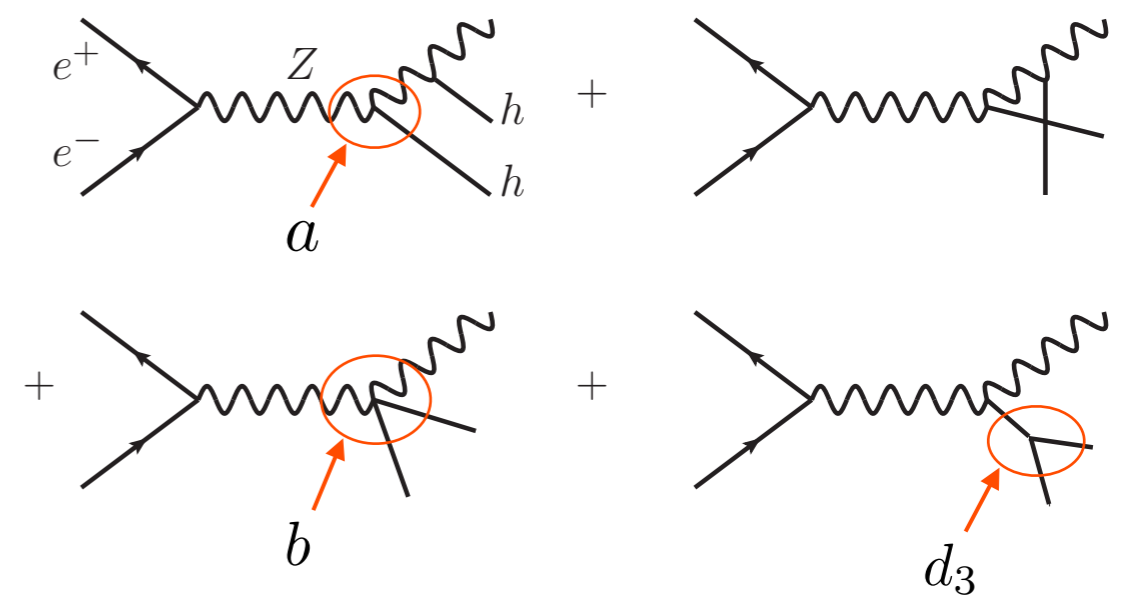


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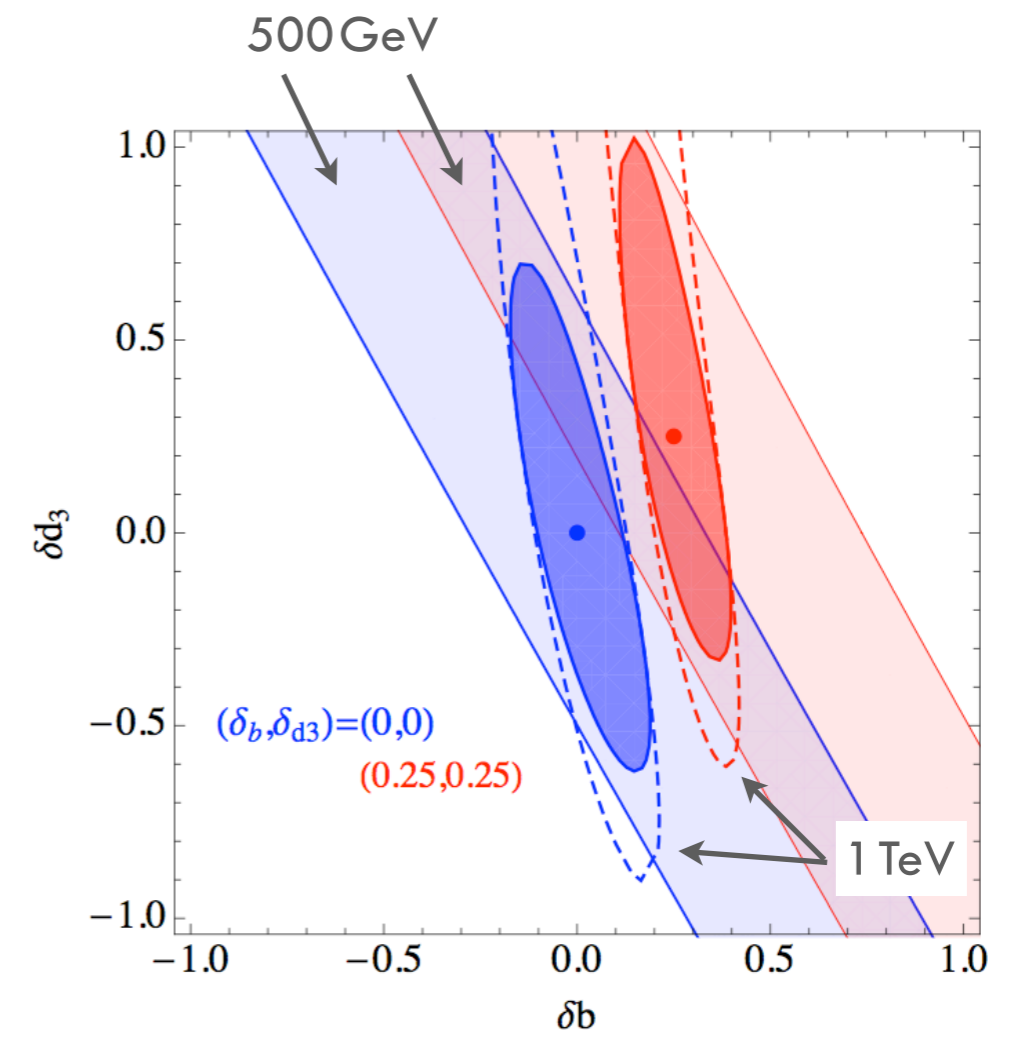


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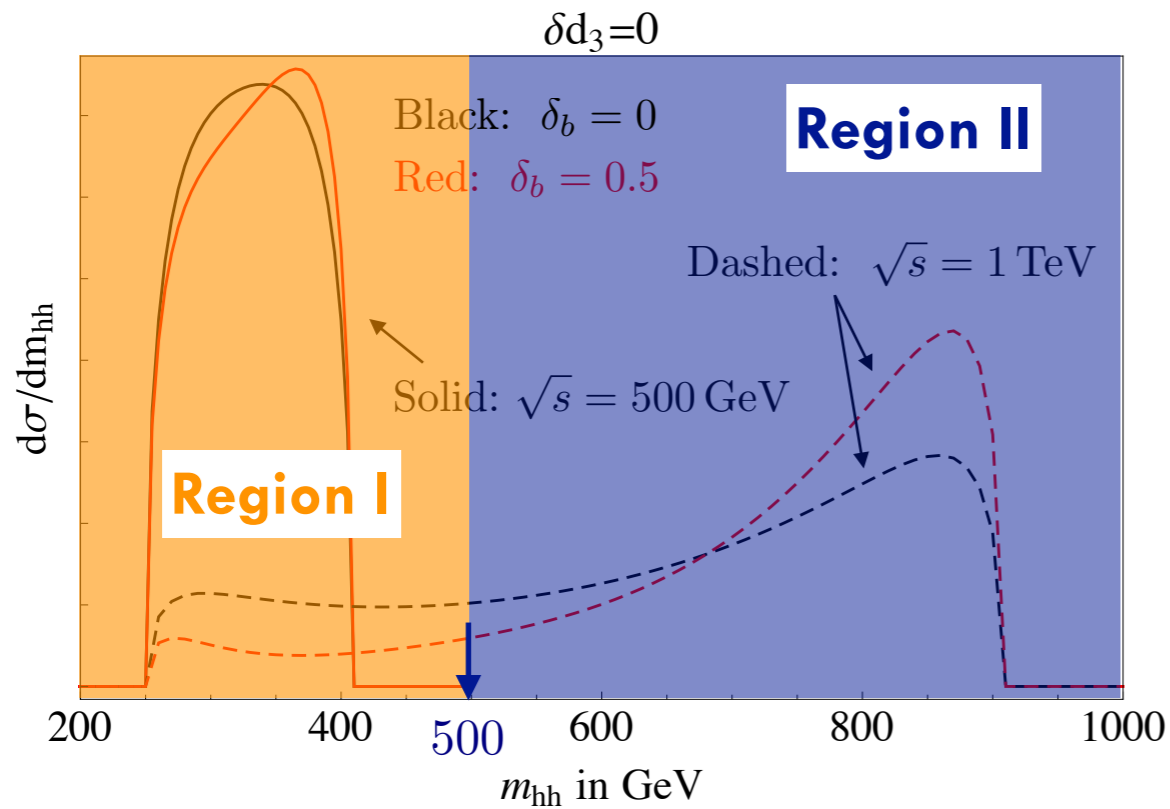
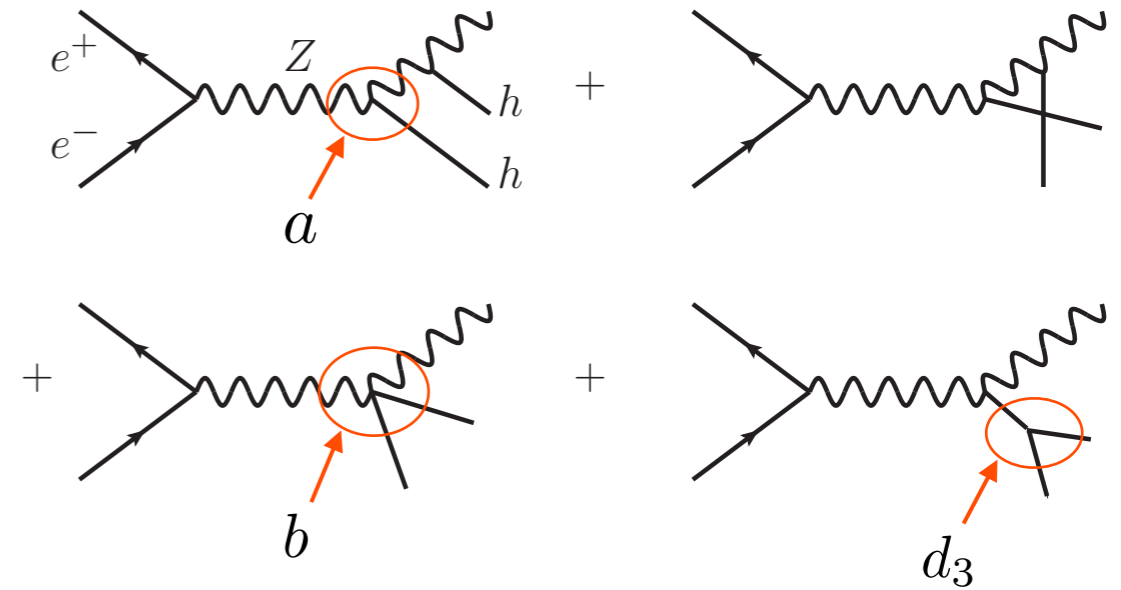


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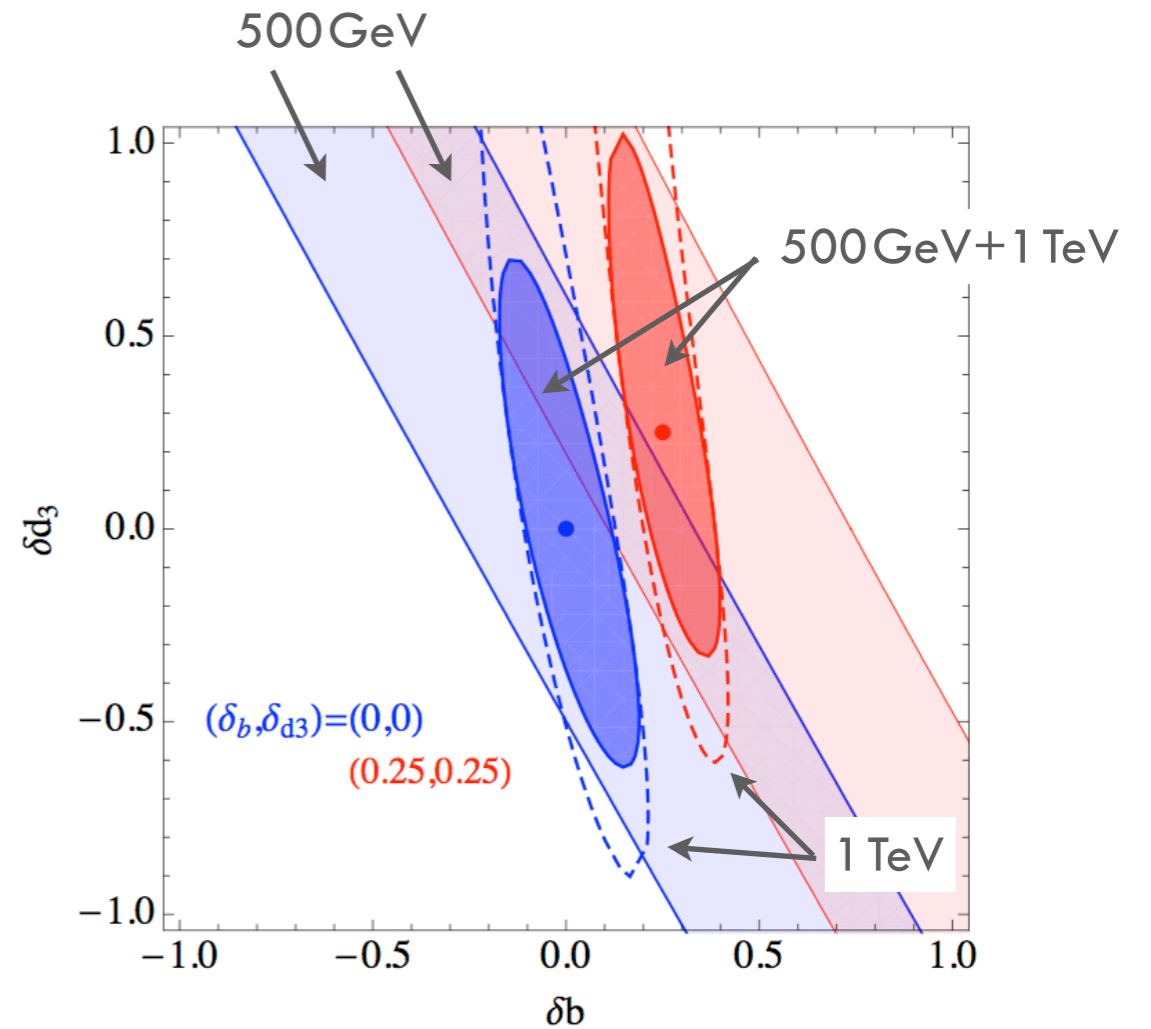


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  - coupling  $hhVV$  at  $\sim 20\%$  ( $e^+e^-$  with  $\sqrt{s} = 500 \text{ GeV} + 1 \text{ TeV}$  )