



Prospects on MW measurements

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EPS 2013 conference

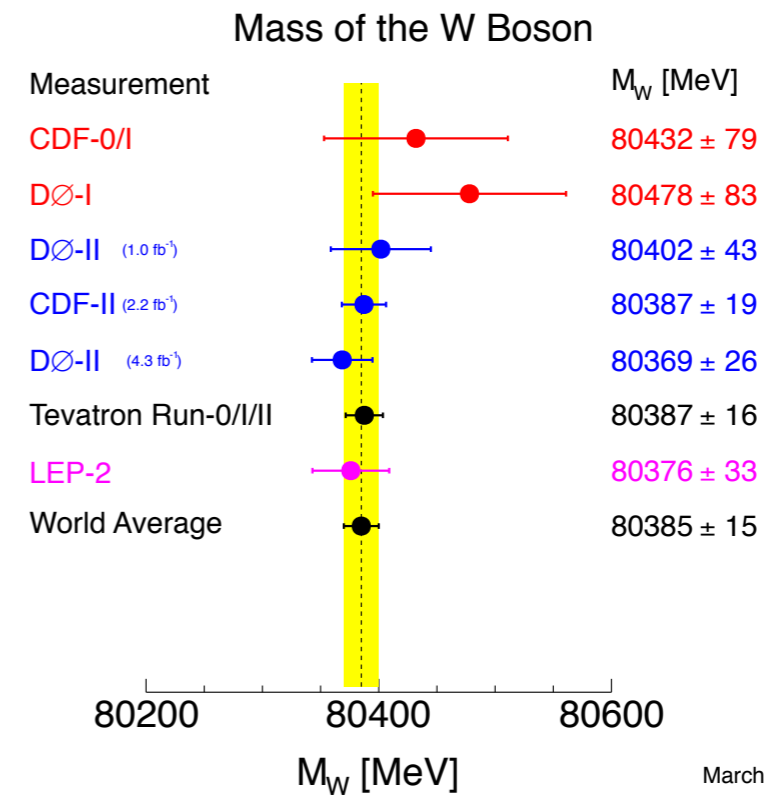
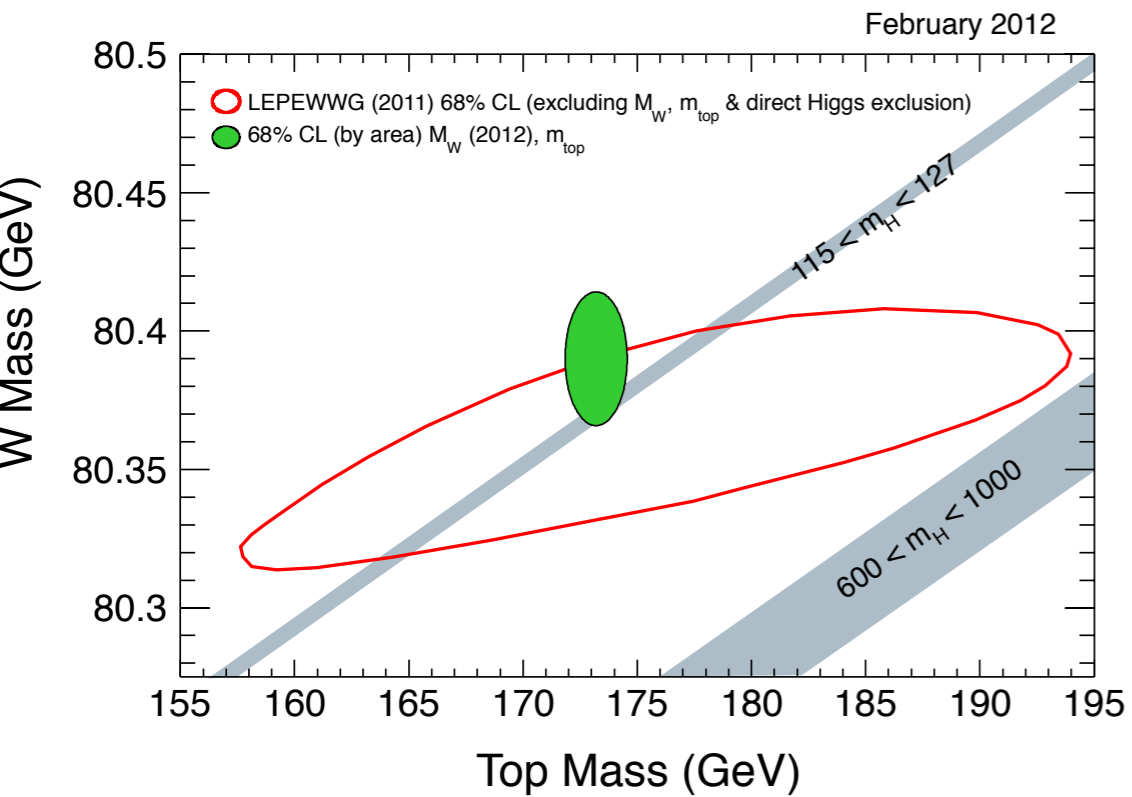
July 18th 2013

Plan of the talk

- observables relevant for the M_W measurement
- relevance of different classes of radiative corrections and their impact on the M_W measurement
- the POWHEG implementation of exact NLO-QCD and NLO-EW corrections to both charged current and neutral current Drell-Yan, matched with QCD and QED showers
- QCD and EW uncertainties
- PDF uncertainties

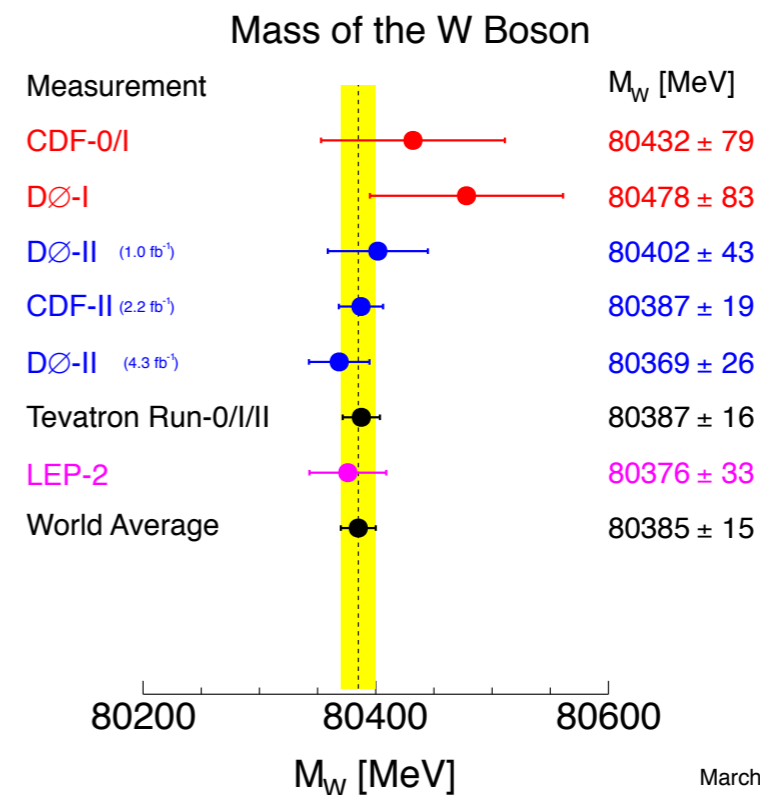
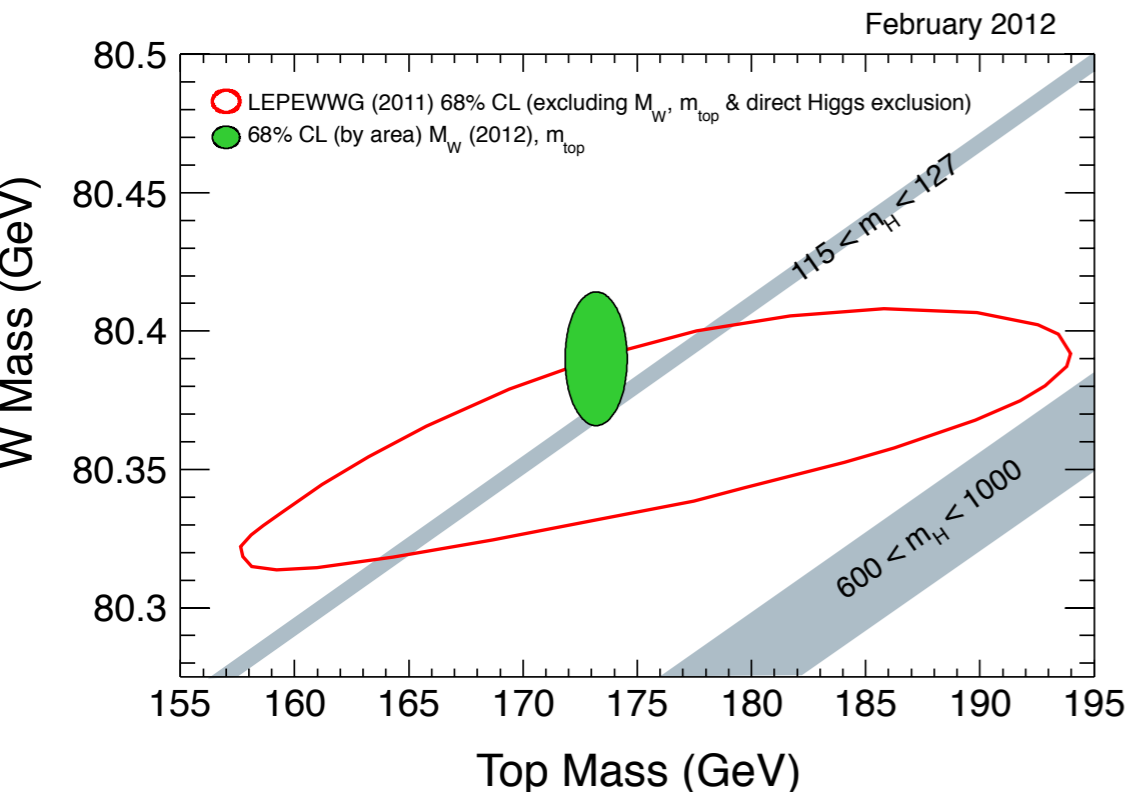
Motivations

A precise measurement of M_W provides a crucial test of the SM

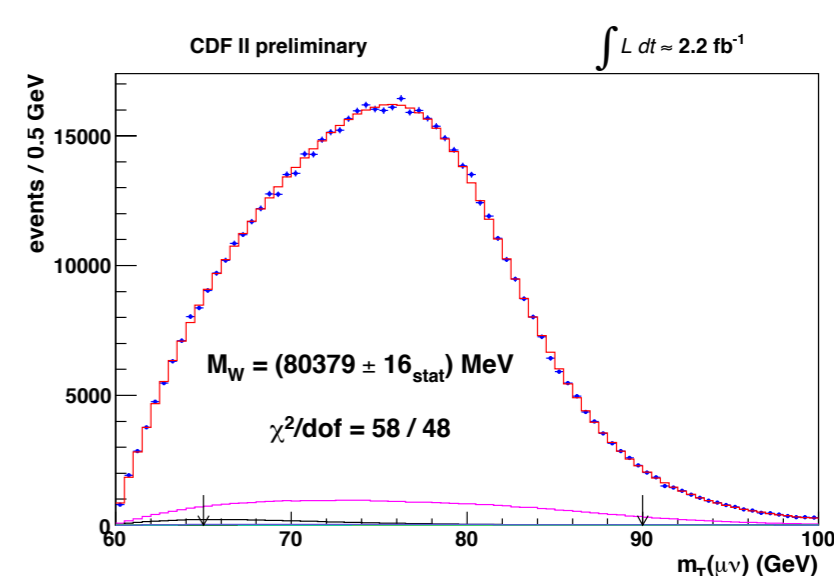
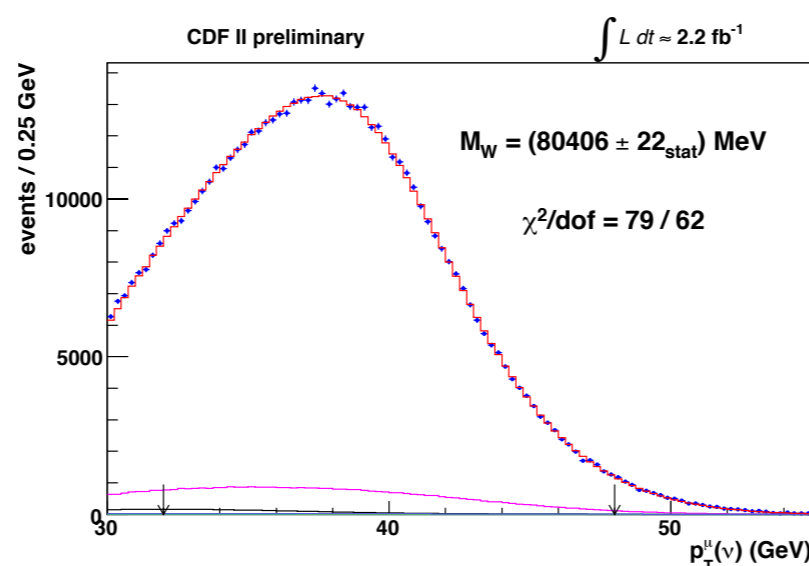
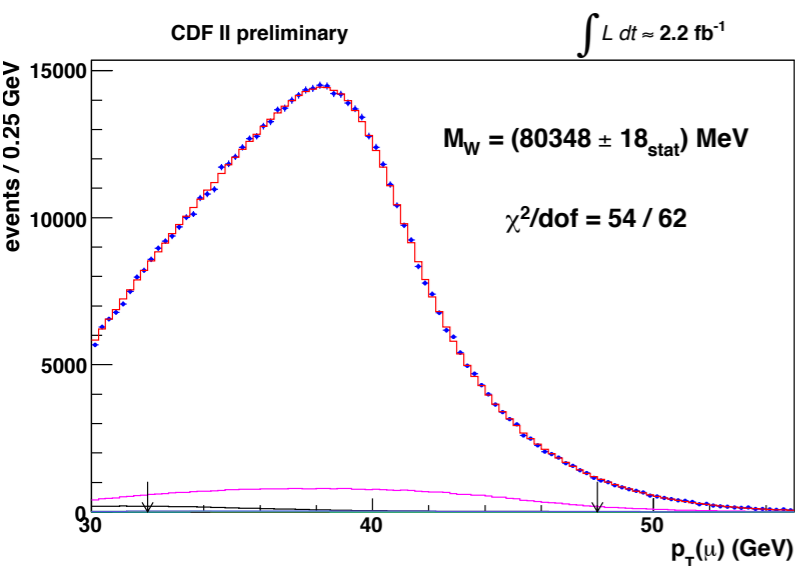


Motivations

A precise measurement of M_W provides a crucial test of the SM



M_W is extracted with a template fit technique of various distributions of CC-DY
 An event generator that includes the best available results in terms of radiative corrections is necessary to minimize the theoretical systematic error in the fit

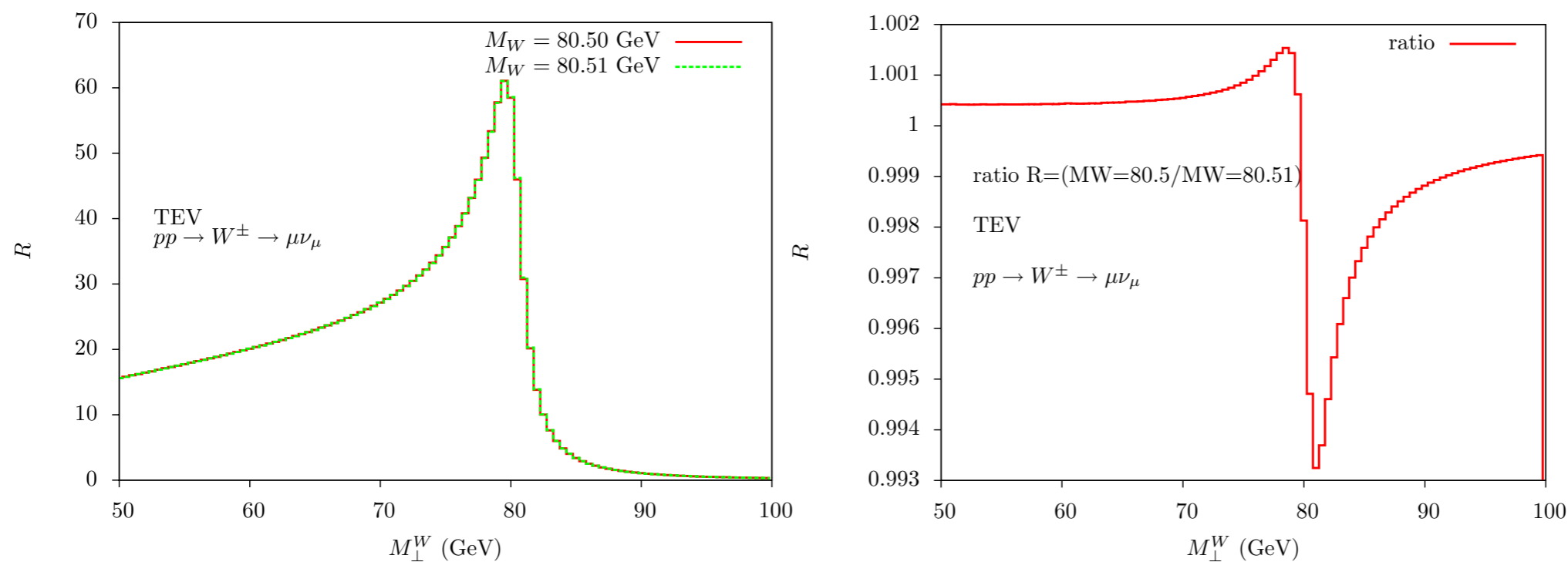


Template fit and theoretical accuracy

In a template fit approach

- the best theoretical prediction for a distribution is computed several times, with different values of M_W
- each template is compared to the data
- the measured M_W is the one of the template that maximizes the agreement with the data

Which level of accuracy do we need?

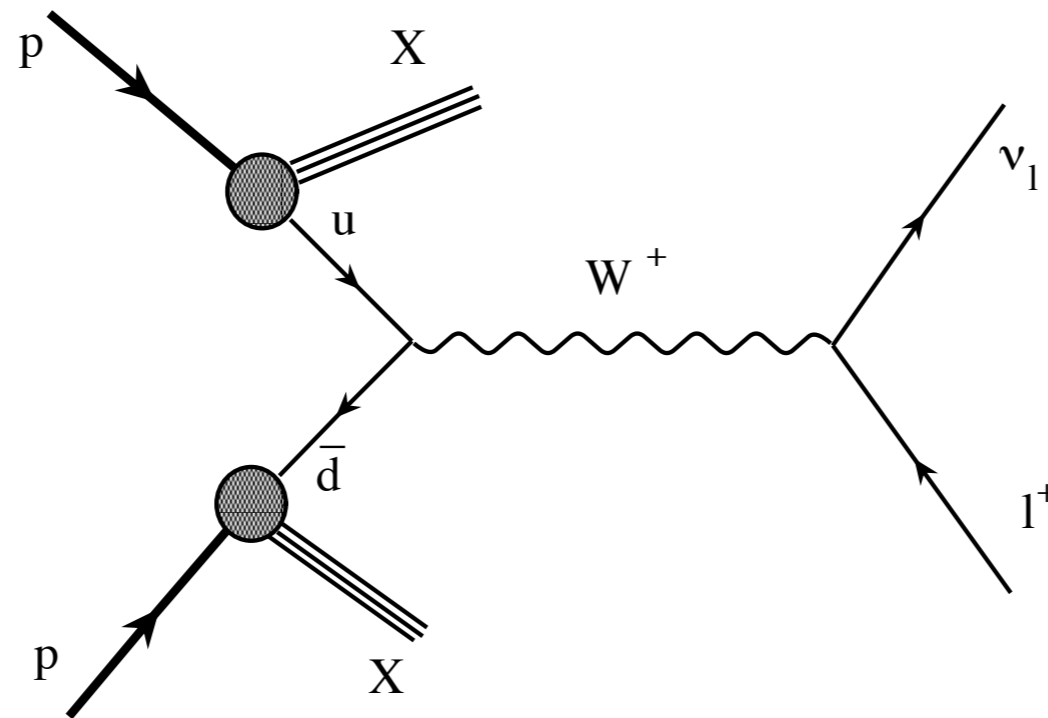


The measured M_W value does not depend on the normalization of the distributions but rather on their **shape**

If we aim at measuring M_W with 10-15 MeV of error, are we able to control the **shape** of the distributions and the theoretical uncertainties at the **few per mille level**?

Perturbative expansion of the Drell-Yan cross section

$$\begin{aligned}
 \sigma_{tot} = \sigma_0 &+ \boxed{\alpha_s \sigma_{\alpha_s} + \alpha_s^2 \sigma_{\alpha_s^2} + \dots} && \text{QCD} \\
 &+ \boxed{\alpha \sigma_{\alpha} + \alpha^2 \sigma_{\alpha^2} + \dots} && \text{EW} \\
 &+ \boxed{\alpha \alpha_s \sigma_{\alpha \alpha_s} + \alpha \alpha_s^2 \sigma_{\alpha \alpha_s^2} + \dots} && \text{mixed QCDxEW}
 \end{aligned}$$

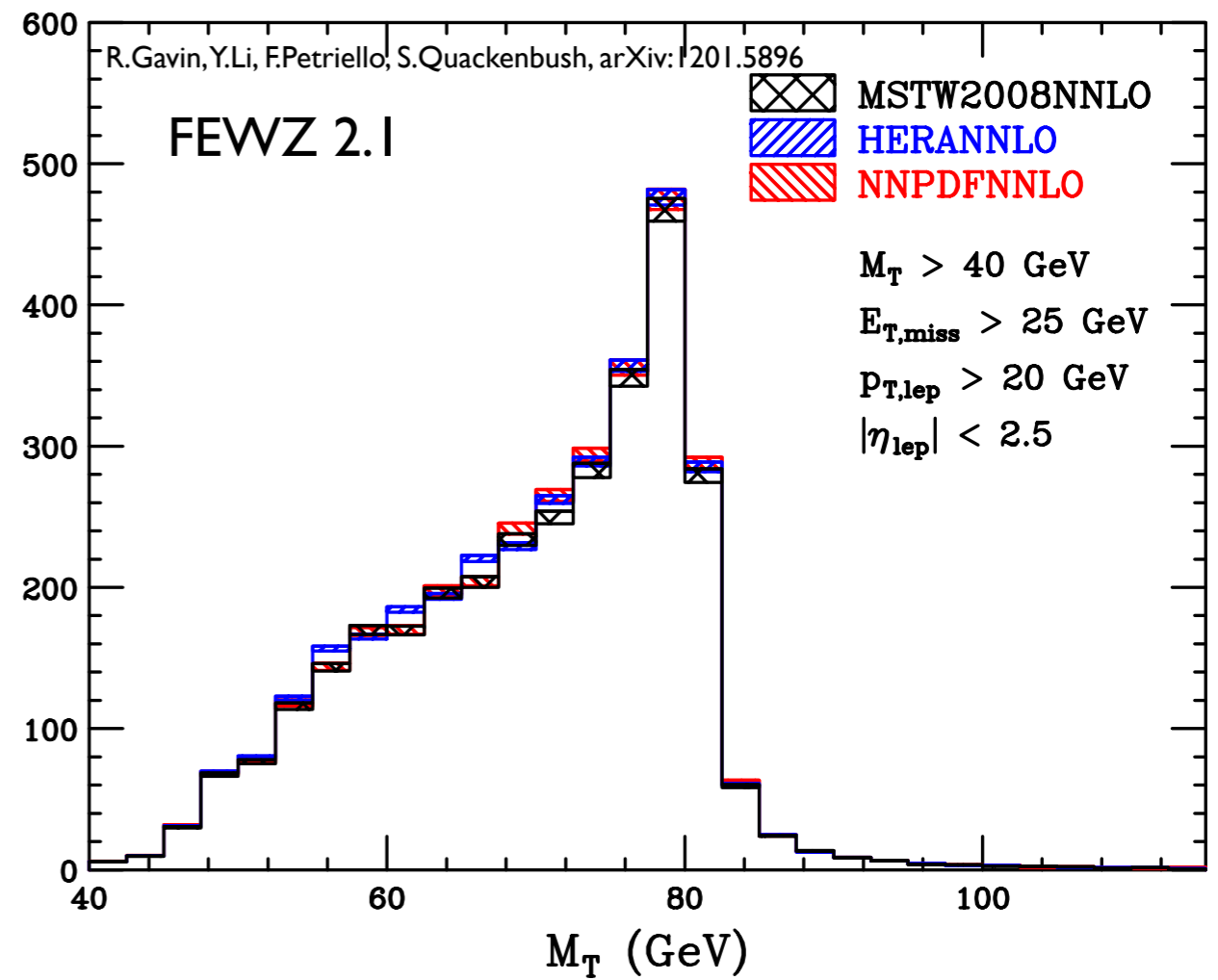
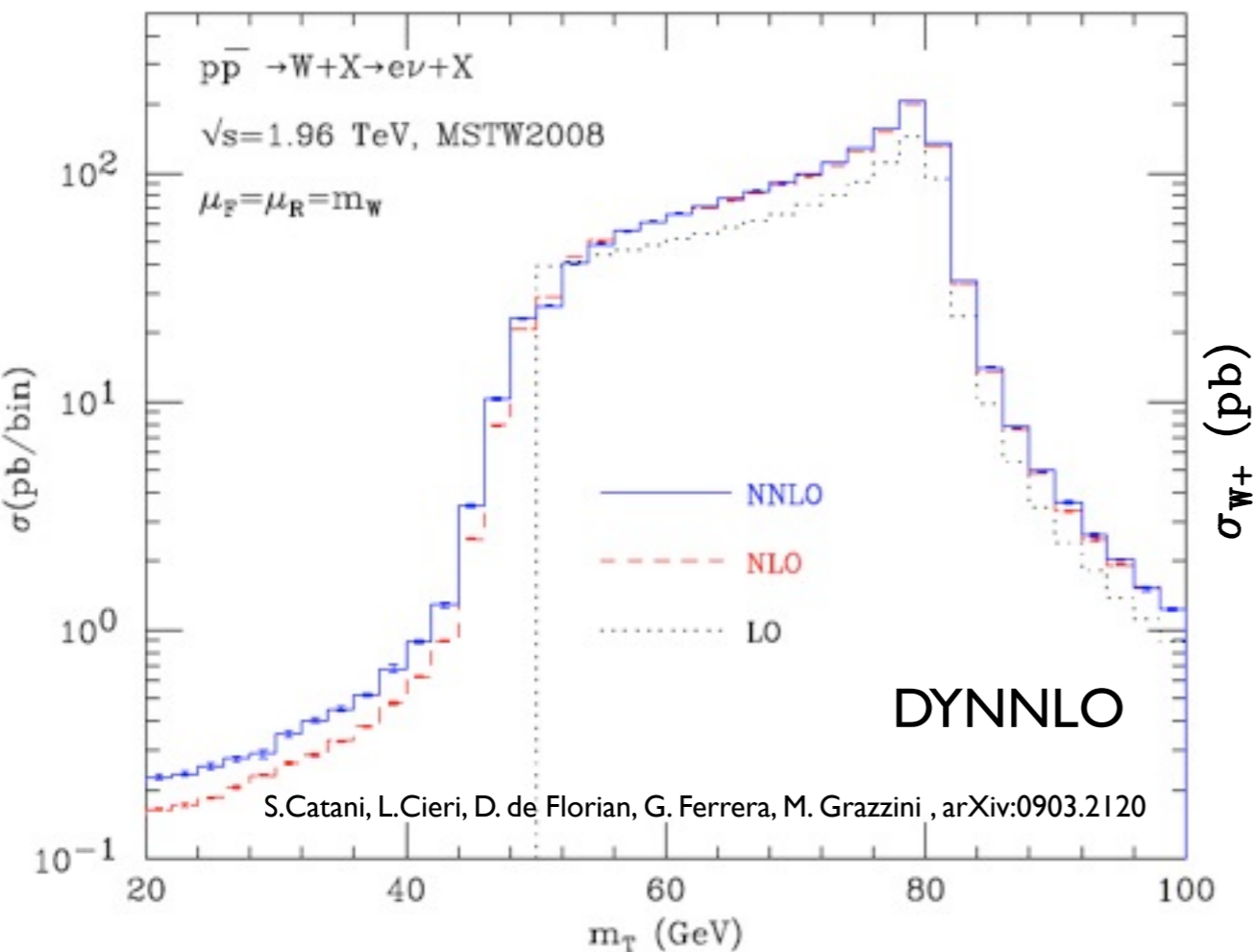


Which corrections modify the shape of the distributions?
affect the extraction of MW?

Perturbative expansion of the Drell-Yan cross section

$$\begin{aligned}
 \sigma_{tot} = & \sigma_0 + \boxed{\alpha_s \sigma_{\alpha_s} + \alpha_s^2 \sigma_{\alpha_s^2}} + \dots && \text{MCFM, FEWZ, DYNNLO} \\
 & + \boxed{\alpha \sigma_{\alpha}} + \alpha^2 \sigma_{\alpha^2} + \dots && \text{WGRAD, RADY, HORACE, SANC} \\
 & + \alpha \alpha_s \sigma_{\alpha \alpha_s} + \alpha \alpha_s^2 \sigma_{\alpha \alpha_s^2} + \dots
 \end{aligned}$$

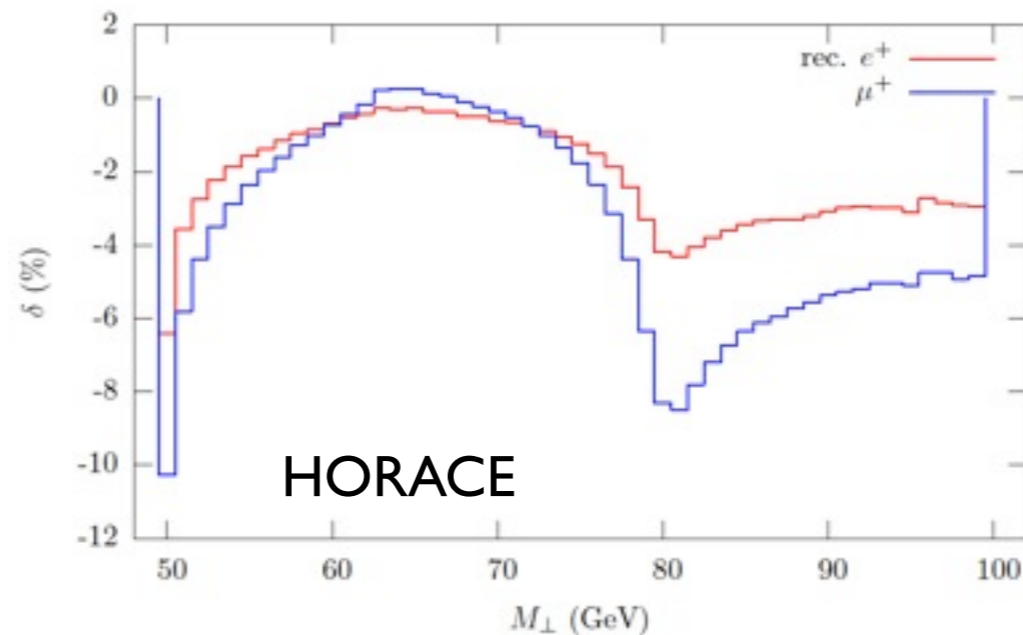
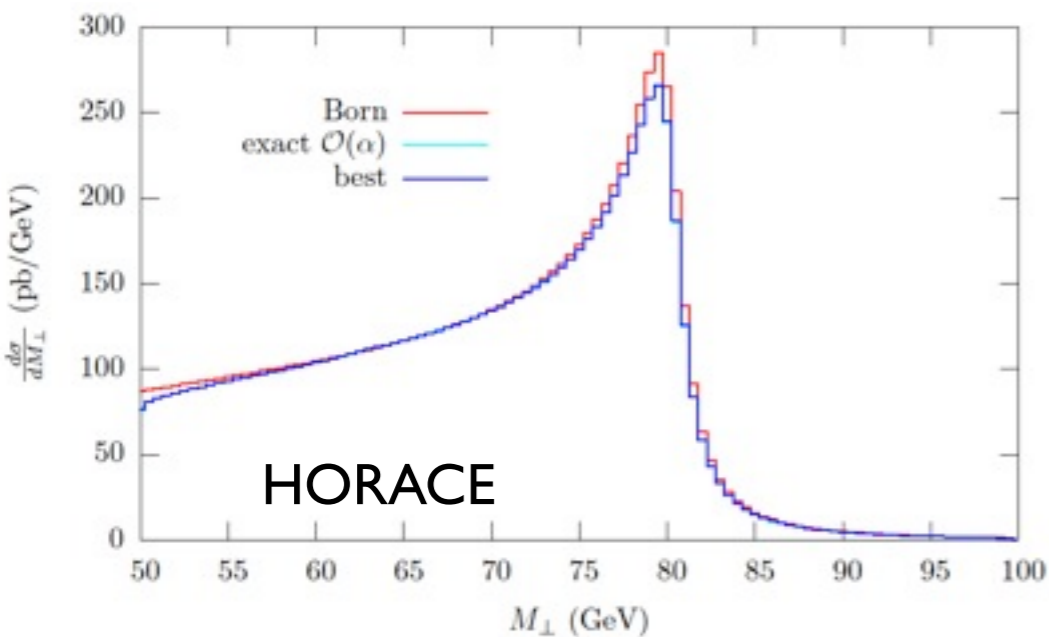
Fixed order corrections exactly evaluated and available in simulation codes



Perturbative expansion of the Drell-Yan cross section

$$\begin{aligned}
 \sigma_{tot} = \sigma_0 &+ \boxed{\alpha_s \sigma_{\alpha_s} + \alpha_s^2 \sigma_{\alpha_s^2}} + \dots && \text{MCFM, FEWZ, DYNNLO} \\
 &+ \boxed{\alpha \sigma_{\alpha}} + \alpha^2 \sigma_{\alpha^2} + \dots && \text{WGRAD, RADY, HORACE, SANC} \\
 &+ \alpha \alpha_s \sigma_{\alpha \alpha_s} + \alpha \alpha_s^2 \sigma_{\alpha \alpha_s^2} + \dots
 \end{aligned}$$

Fixed order corrections exactly evaluated and available in simulation codes



The change of the final state lepton distribution yields a huge shift in the extracted MW value

$$\Delta M_W^{\alpha} = 110 \text{ MeV}$$

Perturbative expansion of the Drell-Yan cross section

$$\begin{aligned}\sigma_{tot} = & \sigma_0 + \boxed{\alpha_s \sigma_{\alpha_s} + \alpha_s^2 \sigma_{\alpha_s^2}} + \dots \\ & + \boxed{\alpha \sigma_{\alpha}} + \boxed{\alpha^2 \sigma_{\alpha^2}} + \dots \\ & + \boxed{\alpha \alpha_s \sigma_{\alpha \alpha_s}} + \alpha \alpha_s^2 \sigma_{\alpha \alpha_s^2} + \dots\end{aligned}$$

Fixed order corrections exactly evaluated and available in simulation codes

Subsets of corrections partially evaluated or approximated

$\mathcal{O}(\alpha^2)$

EW Sudakov logs J.Kühn, A.Kulesza, S.Pozzorini, M.Schulze, Nucl.Phys.B797:27-77,2008, Phys.Lett.B651:160-165,2007, Nucl.Phys.B727:368-394,2005.

QED LL

QED NLL (approximated)

additional light pairs (approximated)

$\mathcal{O}(\alpha \alpha_s)$

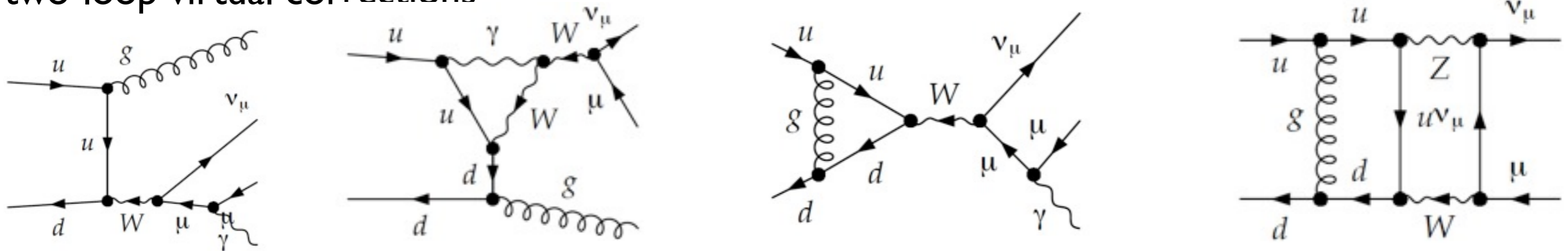
EW corrections to $f\bar{f}$ +jet production

QCD corrections to $f\bar{f}$ +gamma production

A.Denner, S.Dittmaier, T.Kasprzik, A.Mueck, arXiv:0909.3943, arXiv:1103.0914

Mixed QCDxEW corrections the Drell-Yan cross section $\sigma_{tot} = \sigma_0 + \alpha_s \sigma_{\alpha_s} + \alpha_s^2 \sigma_{\alpha_s^2} + \dots$ $+ \alpha \sigma_{\alpha} + \alpha^2 \sigma_{\alpha^2} + \dots$ $+ \alpha \alpha_s \sigma_{\alpha \alpha_s} + \alpha \alpha_s^2 \sigma_{\alpha \alpha_s^2} + \dots$

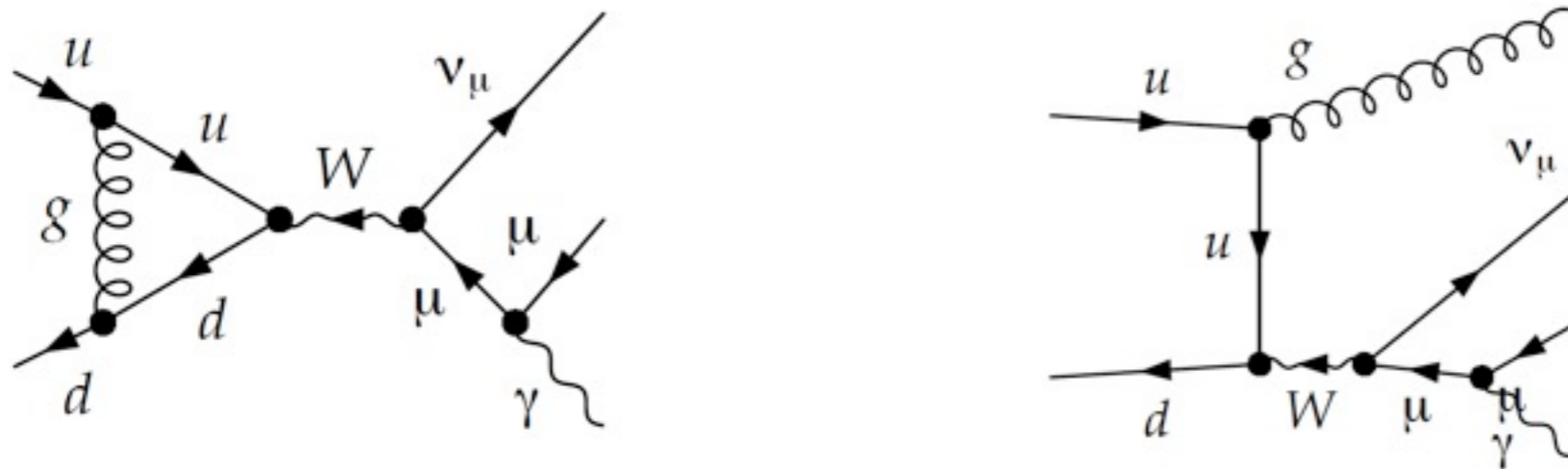
- The first mixed QCDxEW corrections include different contributions:
 - emission of two real additional partons (one photon + one gluon/quark)
 - emission of one real additional parton (one photon with QCD virtual corrections, one gluon/quark with EW virtual corrections)
 - two-loop virtual corrections



- an exact complete calculation is not yet available, neither for DY nor for single gauge boson production

W.B. Kilgore, C. Sturm, arXiv:1107.4798

- The bulk of the mixed QCDxEW corrections, relevant for a precision MW measurement, is factorized in QCD and EW contributions:
 (leading-log part of final state QED radiation) X (leading-log part of initial state QCD radiation || NLO-QCD contribution to the K-factor)



In any case, a fixed order description of the process is not sufficient...

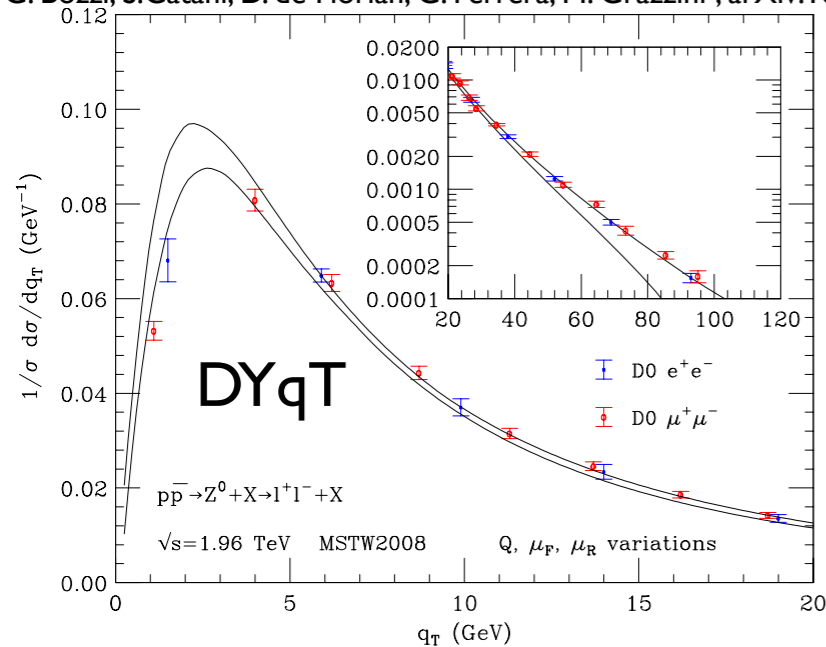
The relevance of multiple gluon/photon emission

numerical simulation of IS QCD multiple gluon emission via Parton Shower (Herwig, Pythia, Sherpa)

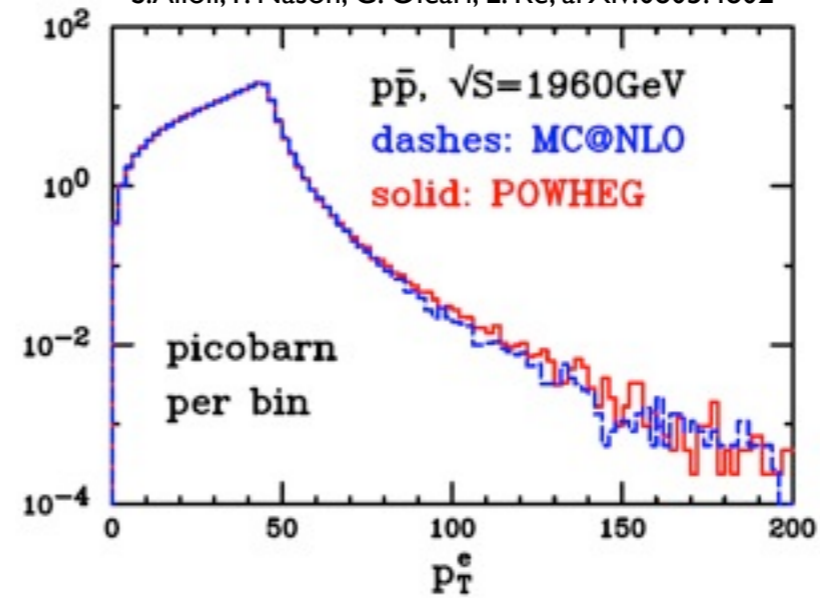
matching of NLO-QCD results with QCD Parton Shower (MC@NLO, POWHEG)

analytical resummation of initial state QCD multiple gluon emission (Resbos, DYqT)

G. Bozzi, S. Catani, D. de Florian, G. Ferrera, M. Grazzini, arXiv:1007.2351



S. Alioli, P. Nason, C. Oleari, E. Re, arXiv:0805.4802



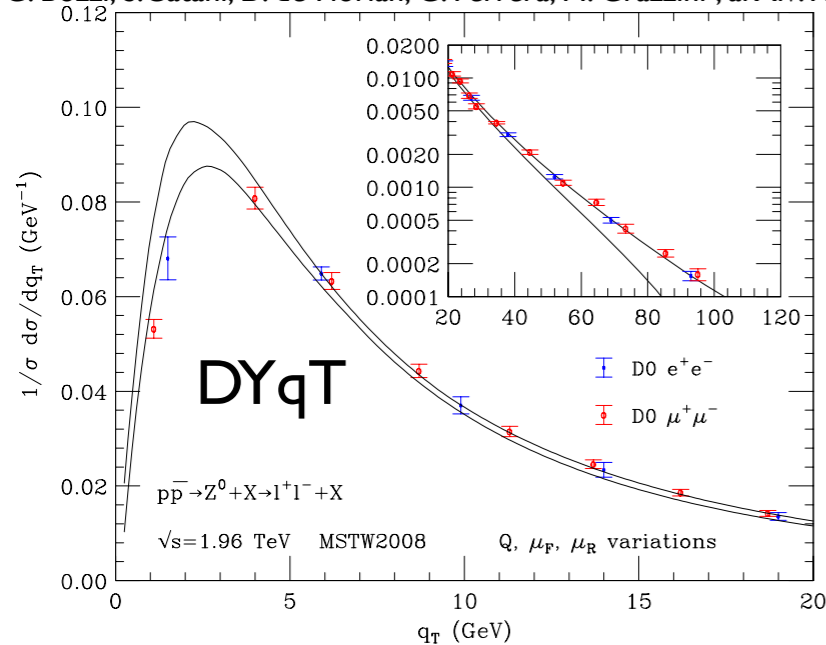
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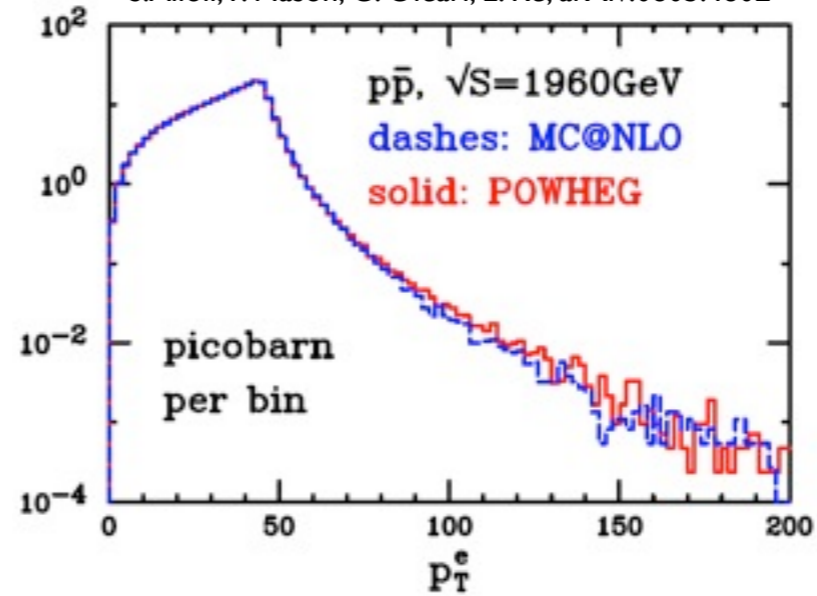
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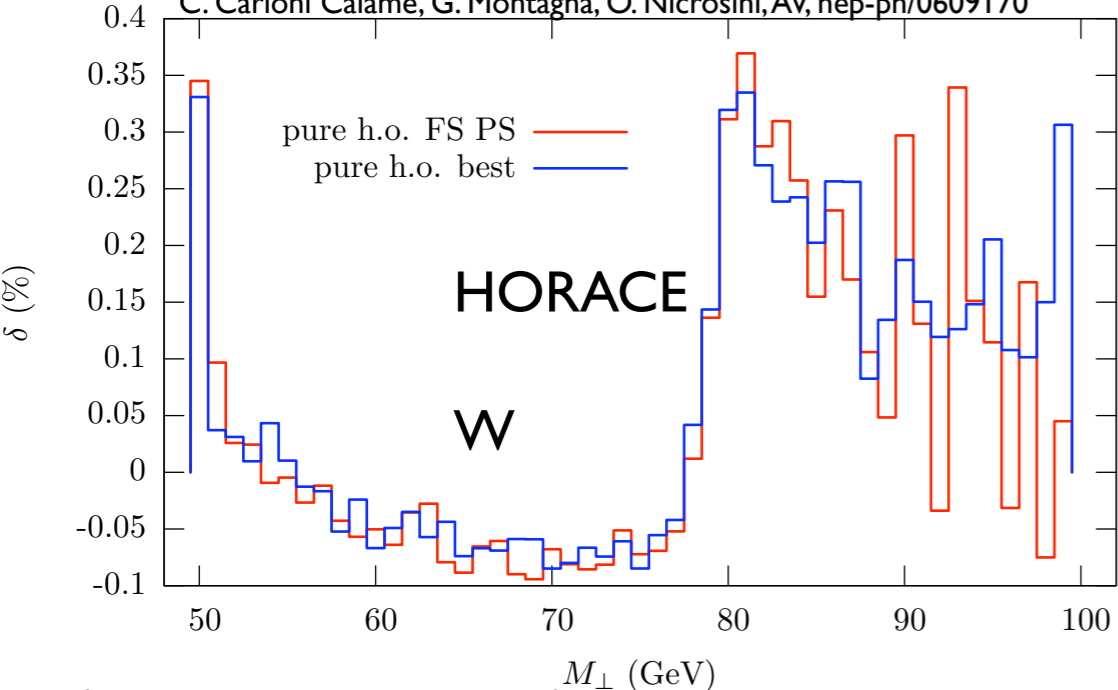
S. Alioli, P. Nason, C. Oleari, E. Re, arXiv:0805.4802



numerical simulation of final state QED multiple photon emission via Parton Shower (Photos, HORACE)

matching of NLO-EW results with complete QED Parton Shower (HORACE)

C. Carloni Calame, G. Montagna, O. Nicrosini, AV, hep-ph/0609170



Shift induced in the extraction of MW from higher order QED effects

$$\Delta M_W^\alpha = 110 \text{ MeV}$$

$$\Delta M_W^{exp} = -10 \text{ MeV}$$

Combining QCD + EW corrections: $\mathcal{O}(\alpha\alpha_s)$ ambiguities

G. Balossini, C.M. Carloni Calame, G. Montagna, M. Moretti, O. Nicrosini, F. Piccinini, M. Treccani, A. Vicini, JHEP 1001:013, 2010

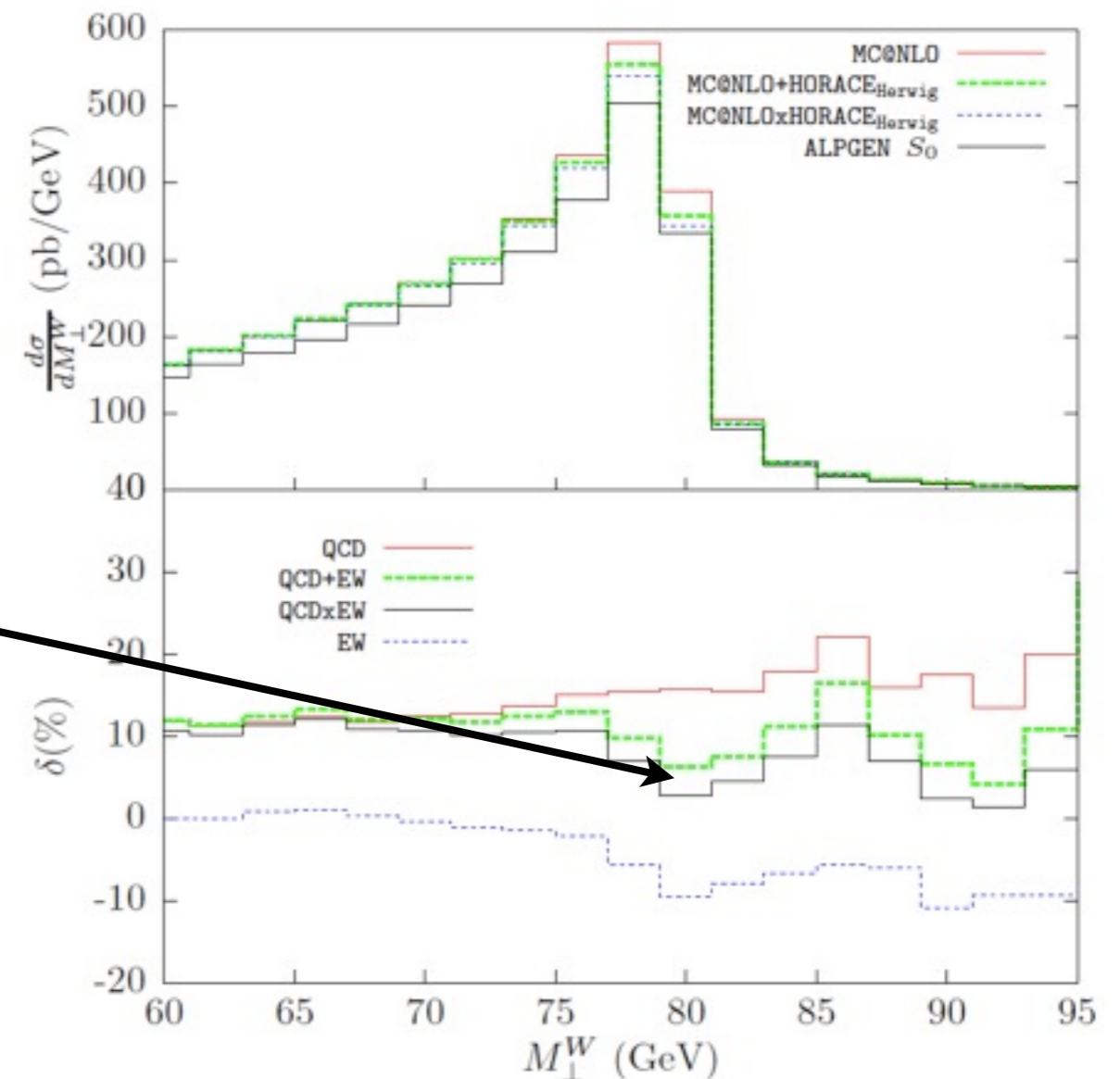
factorized prescription

$$\left[\frac{d\sigma}{d\mathcal{O}}\right]_{QCD \otimes EW} = \left(1 + \frac{\left[\frac{d\sigma}{d\mathcal{O}}\right]_{MC@NLO} - \left[\frac{d\sigma}{d\mathcal{O}}\right]_{HERWIG PS}}{\left[\frac{d\sigma}{d\mathcal{O}}\right]_{LO/NLO}}\right) \times \left\{ \left[\frac{d\sigma}{d\mathcal{O}}\right]_{EW} \right\}_{HERWIG PS}$$

additive prescription

$$\left[\frac{d\sigma}{d\mathcal{O}}\right]_{QCD \oplus EW} = \left\{ \frac{d\sigma}{d\mathcal{O}} \right\}_{QCD} + \left\{ \left[\frac{d\sigma}{d\mathcal{O}}\right]_{EW} - \left[\frac{d\sigma}{d\mathcal{O}}\right]_{Born} \right\}_{HERWIG PS}$$

- the factorized and the additive formulae differ by few per cent
- different inclusion of higher orders $\mathcal{O}(\alpha_s^2)$ and $\mathcal{O}(\alpha\alpha_s)$
- the POWHEG formulation offers another recipe to combine the QCD and EW corrections



CC and NC Drell-Yan in POWHEG with exact NLO-(QCD+EW)

POWHEG, CC-DY: NLO-(QCD+EW) matched with QCD/QED Parton Shower

Bernaciak, Wackerth, arXiv:1201.4804

Barzè, Montagna, Nason, Nicrosini, Piccinini, arXiv:1202.0465

POWHEG, NC-DY: NLO-(QCD+EW) matched with QCD/QED Parton Shower

Barzè, Montagna, Nason, Nicrosini, Piccinini, Vicini, arXiv:1302.4606

<http://powhegbox.mib.infn.it/>

$$d\sigma = \sum_{f_b} \bar{B}^{f_b}(\Phi_n) d\Phi_n \left\{ \Delta^{f_b}(\Phi_n, p_T^{min}) + \sum_{\alpha_r \in \{\alpha_r | f_b\}} \frac{[d\Phi_{rad} \theta(k_T - p_T^{min}) \Delta^{f_b}(\Phi_n, k_T) R(\Phi_{n+1})]_{\bar{\Phi}_n^{\alpha_r} = \Phi_n}}{B^{f_b}(\Phi_n)} \right\}$$

(differential)
 overall normalization factor
 exact NLO QCD+EW accuracy
 (Born+virtual+integrated real)

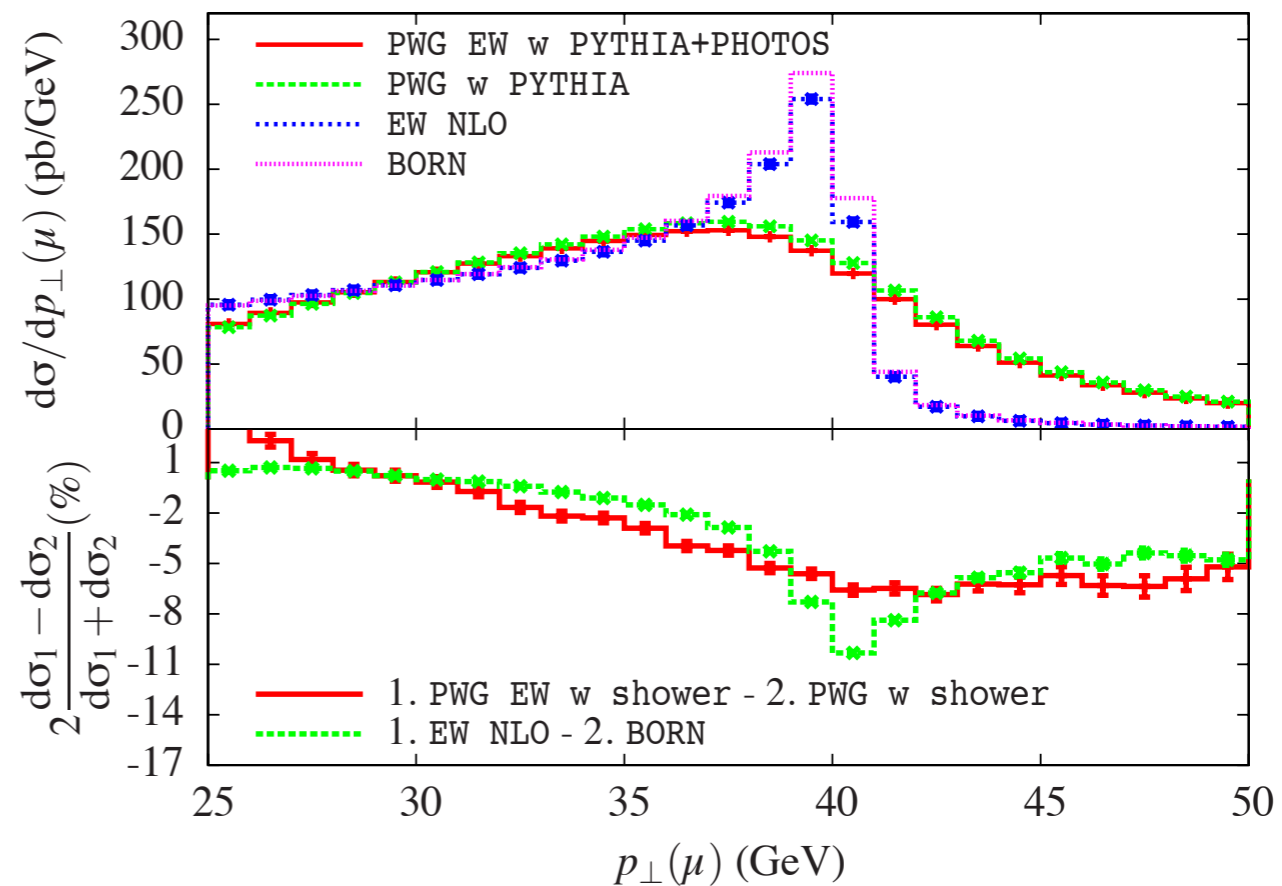
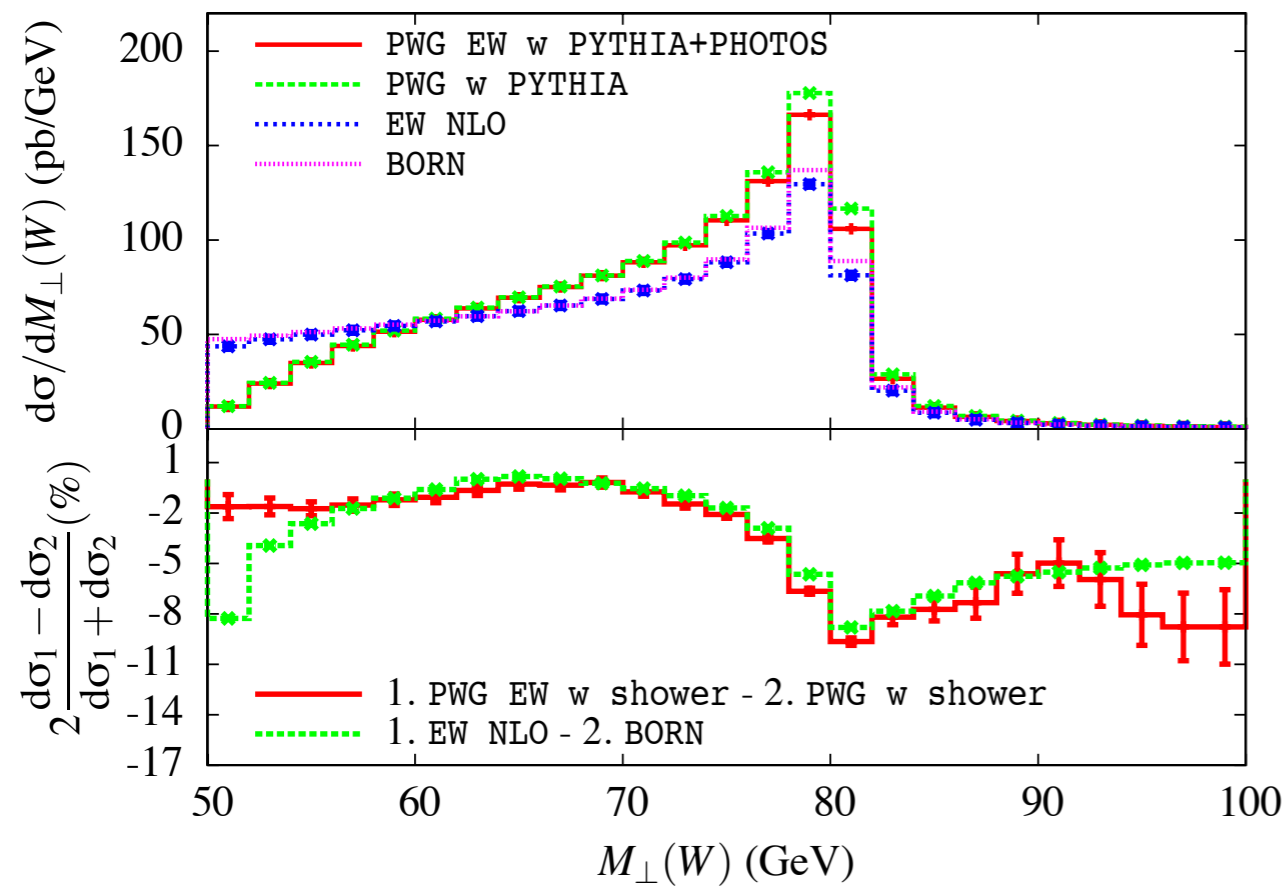
no emission probability
 (Sudakov form factor)

exact emission probability of one parton
 (either one photon or gluon or quark)
 requested to be the hardest emission
 (Sudakov form factor)

- the events generated in this way are then passed to PYTHIA/HERWIG for QCD and QED showering
- the effect of radiative corrections on the distributions is ruled by the (modified) Sudakov form factor and is factorized w.r.t. the lowest order kinematics \underline{B}

CC-DY: QCD+EW effects

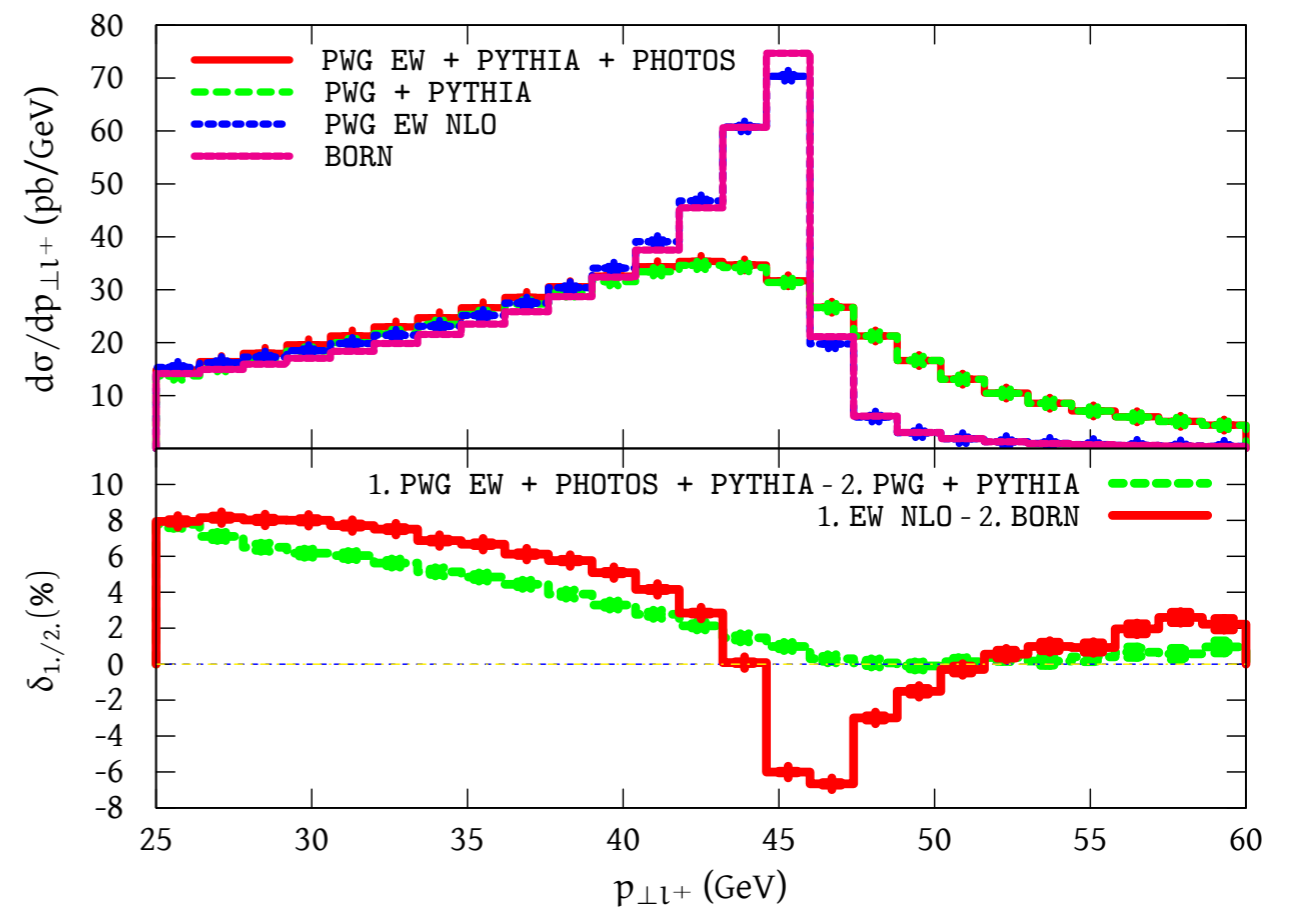
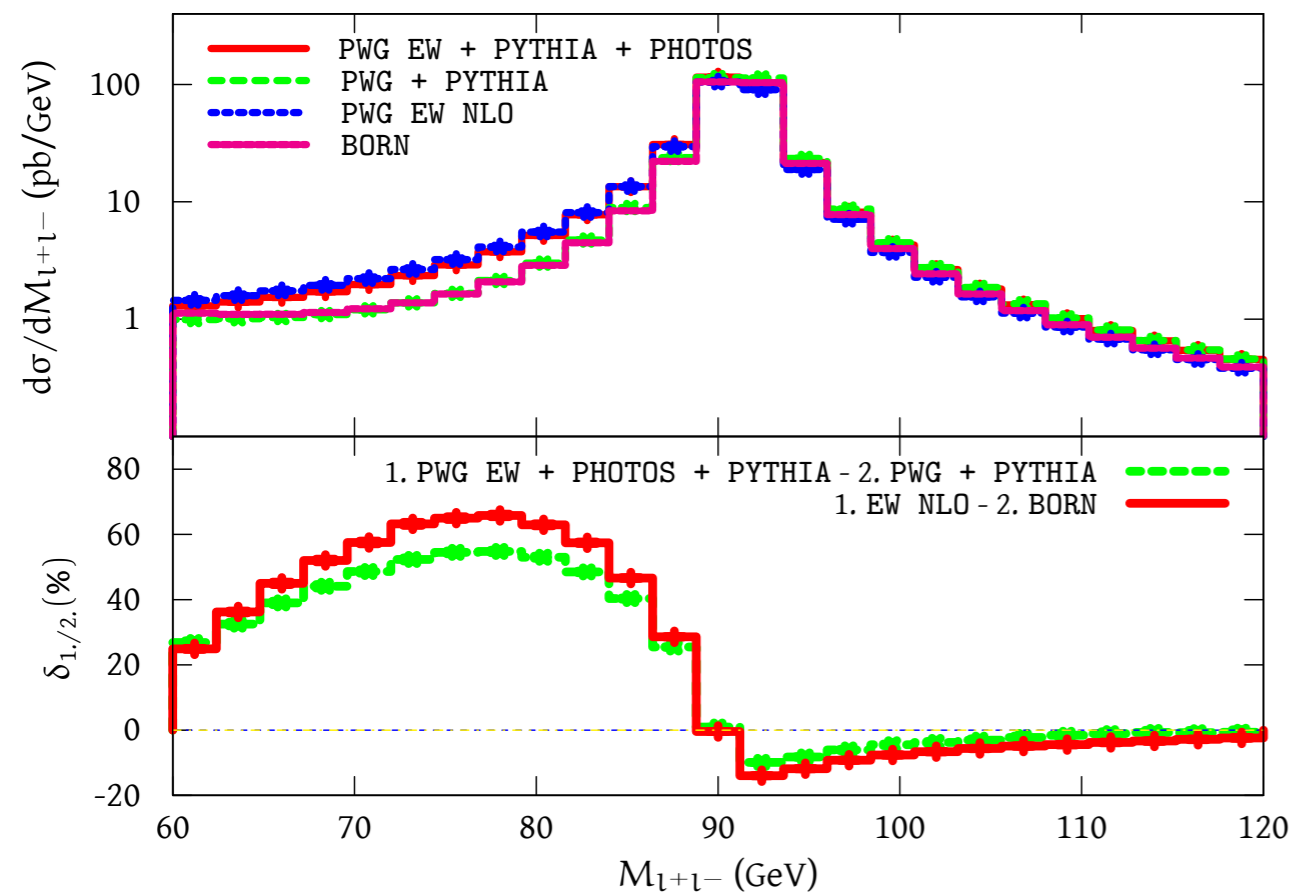
Barzè, Montagna, Nason, Nicrosini, Piccinini, arXiv:1202.0465



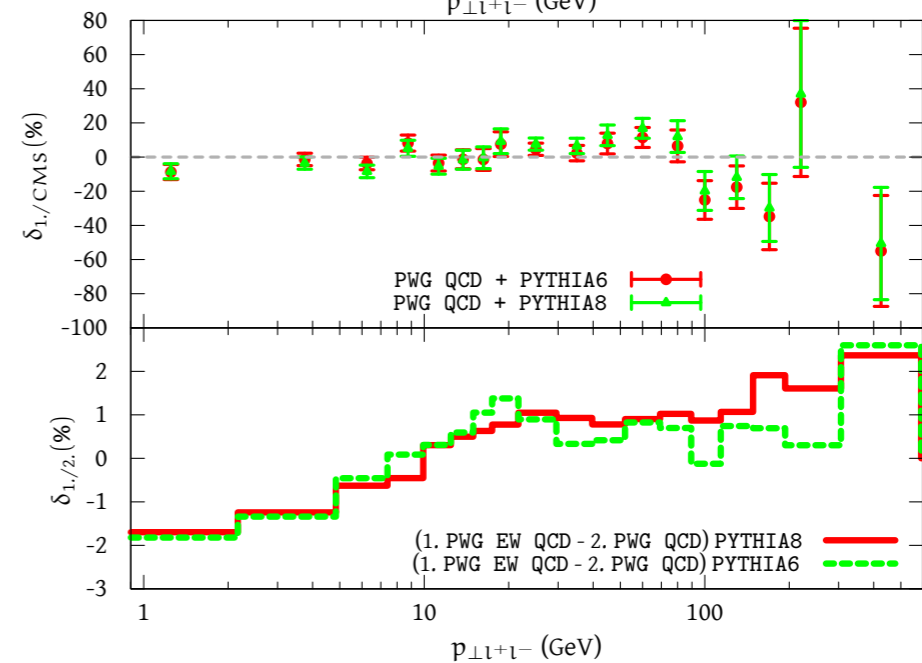
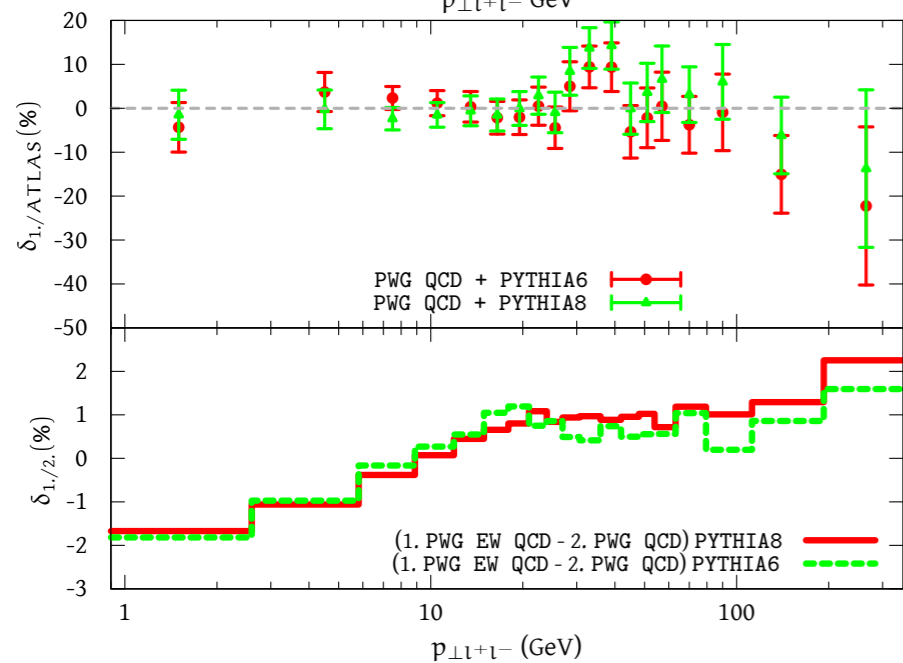
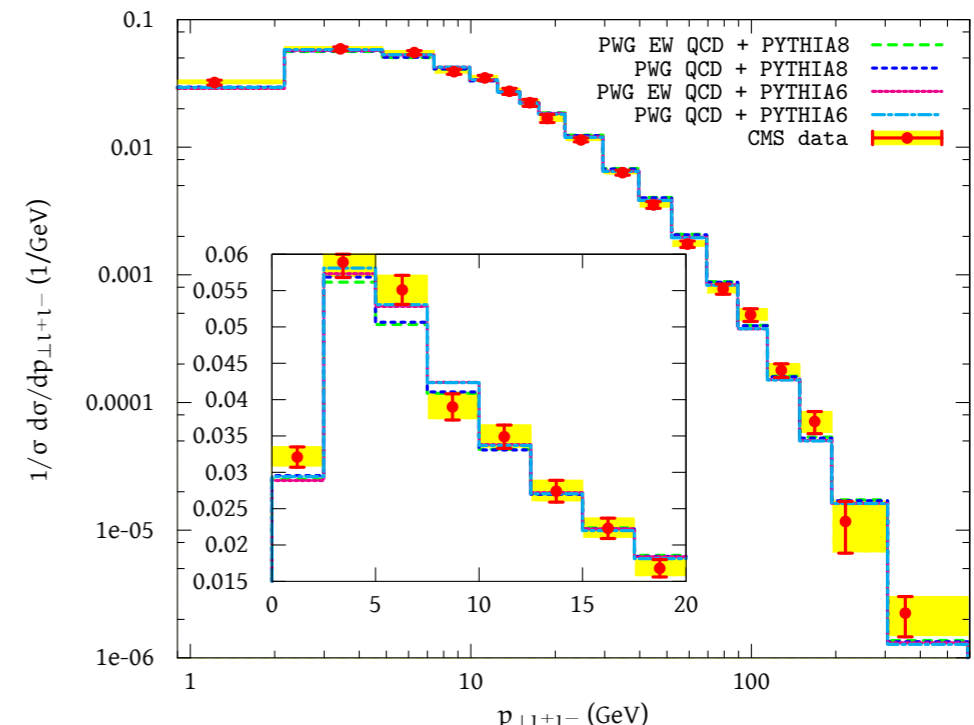
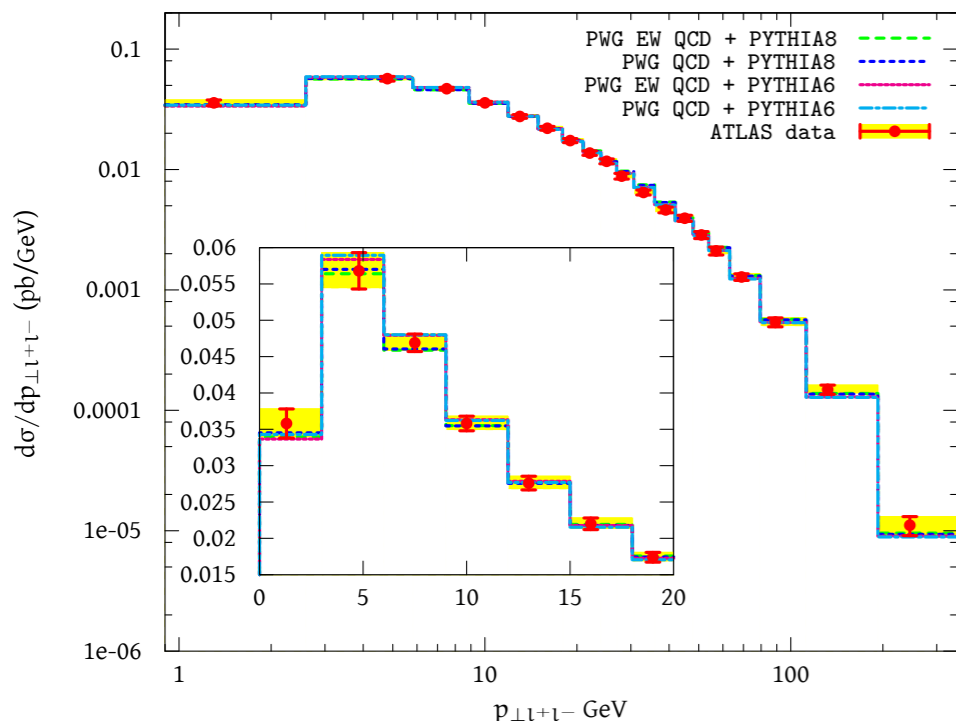
- FSR multiple photon radiation included with PHOTOS
- transverse mass stable against QCD corrections \rightarrow NLO-EW effects are preserved after showering
- the lepton transverse momentum is more sensitive to multiple gluon radiation
the sharp peak due to EW corrections is reduced by the QCD-Parton Shower
- the interplay between QCD and EW corrections yields effects at the per cent level
- leading higher-order mixed $O(\alpha\alpha_s)$ corrections are taken into account
together with the proper matching of NLO-(QCD+EW) matrix elements and (QCD+QED) Parton Shower

NC-DY: QCD+EW effects

Barzè, Montagna, Nason, Nicrosini, Piccinini, Vicini, arXiv:1302.4606

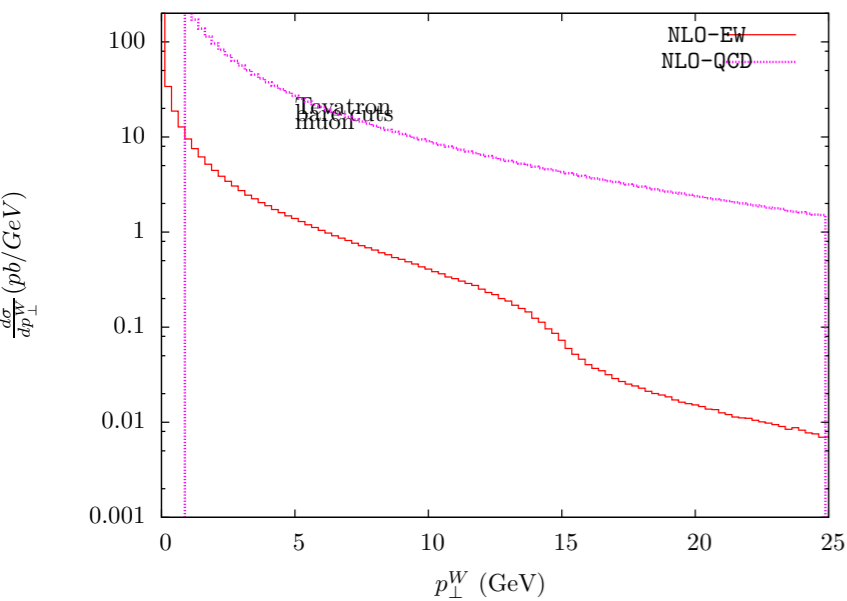


- the lepton transverse momentum is very sensitive to multiple gluon radiation
 - the sharp peak due to EW corrections is reduced by the interplay with the QCD-Parton Shower; factorizable $O(\alpha\alpha_s)$ corrections are at the level of 7%
 - an additive prescription to combine QCD+EW effects instead preserves the peak
- the fixed-order QCD description of the lepton transverse momentum distribution is poor, a resummation is needed
- the combination of NLO-EW effects with multiple gluon emission strongly smears both the NLO-QCD fixed order spectrum and the peaked NLO-EW correction



- the description of the lepton-pair transverse momentum distribution data is in general good
- default values for the non-perturbative parameters in PYTHIA6 and PYTHIA8 have been used (further tuning possible)
- full NLO-EW matrix element → bulk of the QED effects on p_{tZ} ; multiple photon radiation has negligible impact
- QED radiation affects differently p_{tW} and p_{tZ} , both in its FSR and in its ISR components

QED induced $W(Z)$ transverse momentum

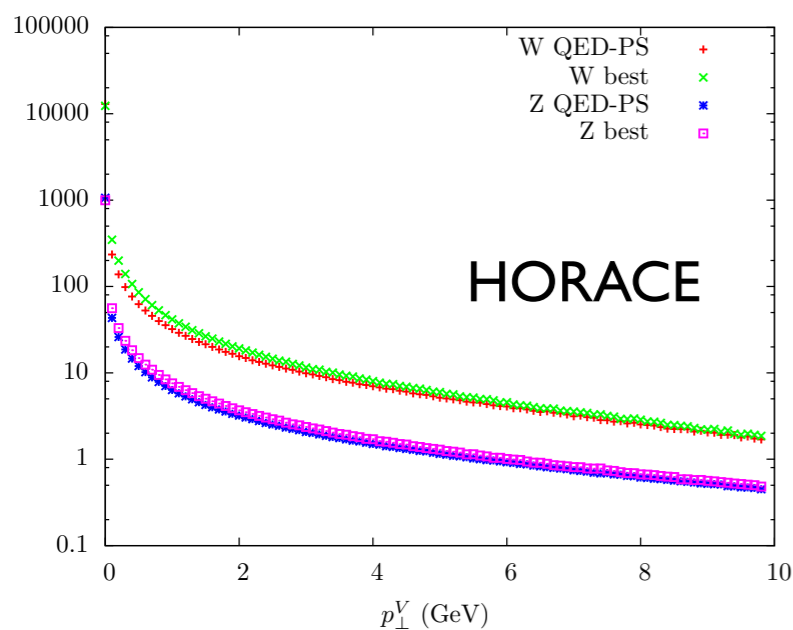


Uncertainty on p_{\perp}^W directly translates into an uncertainty on M_W .

Photon radiation yields a tiny gauge boson transverse momentum.

The gauge boson transverse momentum is different in the CC and NC channels because of the different flavor structure.

A possible estimate of the “non-final state” component differs in the 2 cases by $54 (Z) - 33 (W) = 21 \text{ MeV}$



$\langle p_{\perp}^V \rangle =$	Z FSR-PS	0.409	GeV
	Z best	0.463	GeV
	W FSR-PS	0.174	GeV
	W best	0.207	GeV

The fit of the non-perturbative PYTHIA parameters from the Z transverse momentum should be done using POWHEG (QCD+EW) + PYTHIA, in order to remove completely the EW corrections to the NC channel from the tuning → the PYTHIA parameters will encode only non-perturbative QCD information

In the simulation of the CC channel, the use of POWHEG (QCD+EW), with the above PYTHIA parameters, will yield the proper combination of QCD and EW effects

Ambiguities affecting the shape of the pt_V distribution

The prediction of the pt_V distribution depends on the:

- logarithmic accuracy of the resummation
uncertainty parametrized by the resummation scale Q (analytical approach)
- prescription to match fixed-order results and Parton Shower
variation of $hfact$ in the general formulation of NLO-matched Shower MC
- QED and mixed QCDxQED effects

Any choice of the scale Q or of the factor $hfact$, for a given PDF set,
will then require a corresponding tuning of the model dependent part of the simulation;

We should not discard the QCD theoretical uncertainties!

- non-perturbative “intrinsic” transverse momentum component
measured from pt_Z ; validity of the extrapolation to a different phase-space?
- PDF set choice: partial correlation between pt_Z and pt_W , in particular via the gluon density

Classification of EW radiative corrections

Barzè, Bizjak, Montagna, Nicosini, Piccinini, Vicini, in preparation

- each set of radiative corrections induces a distortion of the shape of the observables
- with a template-fit approach, the distortion of the shape is translated into a MW shift
- study performed in the Tevatron setup (energy and acceptance cuts)
- the available subsets of corrections MUST be included in the analysis

		m_T		p_T^l		E_T		
line	approximation 1	approximation 2	e	μ	e	μ	e	μ
1	BORN	LL1 γ	-143 ± 3.1	-148 ± 2.1	-167 ± 3.7	-198 ± 3.1	-104 ± 4.0	-89 ± 2.5
2	BORN	LLn γ	-138 ± 3.1	-138 ± 2.1	-162 ± 3.7	-184 ± 3.1	-104 ± 4.0	-85 ± 2.5
3	LL1 γ	LLn γ	5 ± 3.5	10 ± 2.3	5 ± 4.4	15 ± 3.3	1 ± 4.5	5 ± 2.5
4	BORN	$\mathcal{O}(\alpha)$	-147 ± 2.8	-153 ± 2.5	-174 ± 3.5	-208 ± 3.5	-105 ± 3.7	-91 ± 2.8
5	BORN	MATCH	-137 ± 3.0	-138 ± 3.4	-163 ± 3.7	-190 ± 3.4	-96 ± 4.0	-78 ± 2.7
6	$\mathcal{O}(\alpha)$	MATCH	11 ± 3.0	12 ± 3.0	11 ± 3.5	16 ± 3.3	12 ± 4.0	13 ± 3.8
7	LL1 γ	$\mathcal{O}(\alpha)$	-1 ± 3.4	-3 ± 2.5	-3 ± 4.1	-5 ± 3.7	-1 ± 4.4	-1 ± 3.0
8	LLn γ	MATCH	4 ± 3.5	5 ± 2.4	4 ± 4.2	2 ± 3.5	10 ± 4.5	10 ± 2.8

		m_T	
line	approximation 1	approximation 2	e μ
1	exp-LL	exp-LL + e^+e^-	-2 -3
2	exp-LL	exp-LL + $e^+e^- + \mu^+\mu^-$	-3 -3

← additional lepton-pair emission simulated in HORACE

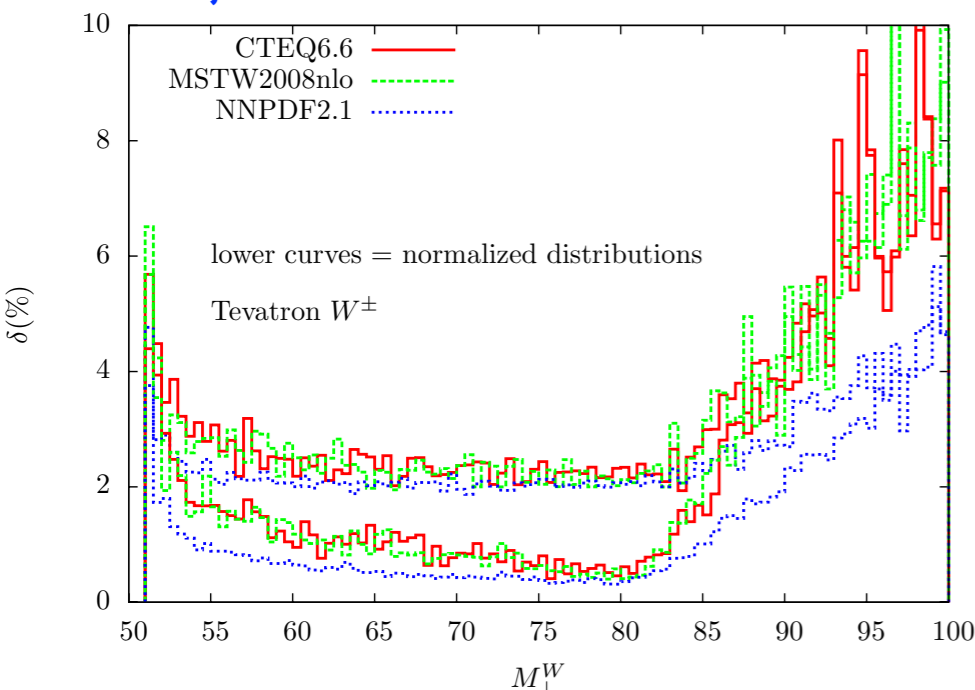
- an estimate of remaining sources of uncertainty can enter in the theoretical systematic error

		m_T		p_T^l		E_T		
line	approx.1	approx.2	e	μ	e	μ	e	μ
1	exp-LL $\kappa = 1.5$	exp-LL $\kappa = 1$	4.0	5.9	4.0	7.7	2.4	3.8
2	$\mathcal{O}(\alpha)$ LL $\kappa = 1.5$	$\mathcal{O}(\alpha)$ LL $\kappa = 1$	1.9	4.8	1.8	5.9	1.5	2.3
$\Delta M_W^{\alpha^2}$ according to Eq. (25)			2.1	1.1	2.2	1.8	0.9	1.5

		m_T		p_T^l		E_T		
line	approx. 1	approx. 2	e	μ	e	μ	e	μ
1	$\mathcal{O}(\alpha)$ α_0	$\mathcal{O}(\alpha)$ $G_\mu - I$	-9.0	-11.6	-10.8	-11.8	-2.8	-7.4
2	$\mathcal{O}(\alpha)$ α_0	$\mathcal{O}(\alpha)$ $G_\mu - II$	1.2	-0.3	-0.2	0.2	1.7	-0.7
3	$\mathcal{O}(\alpha)$ $G_\mu - I$	$\mathcal{O}(\alpha)$ $G_\mu - II$	10.1	11.2	10.6	12.0	4.4	6.6
4	matched α_0	matched $G_\mu - I$	-0.1	-0.1	0.0	-1.1	2.0	1.8
5	matched α_0	matched $G_\mu - II$	1.7	1.1	1.3	-0.3	4.0	2.6
6	matched $G_\mu - I$	matched $G_\mu - II$	1.8	1.2	1.0	0.8	2.0	0.9

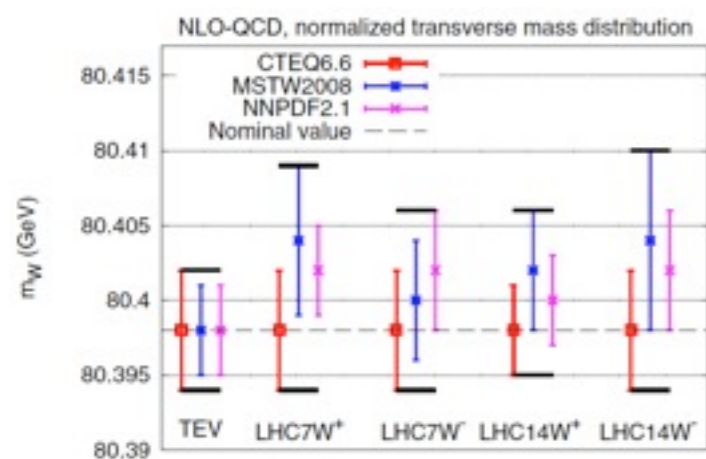
PDF error on MW from transverse mass distribution

Bozzi, Rojo, Vicini, arXiv:1104.2056



- the PDF effect on MW is obtained by studying the transverse mass normalized distributions: different **PDF normalization** should **NOT** be accounted for by a MW shift
- templates and pseudodata computed with the same generator in the same experimental setup: in first approximation the PDF effects factorize w.r.t. all the other theoretical and experimental factors

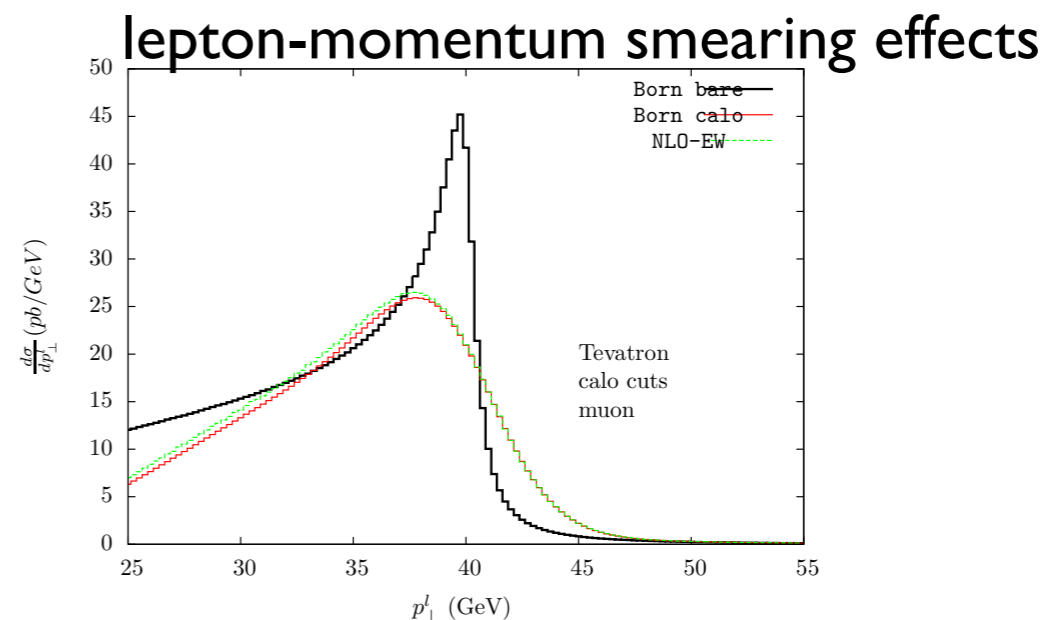
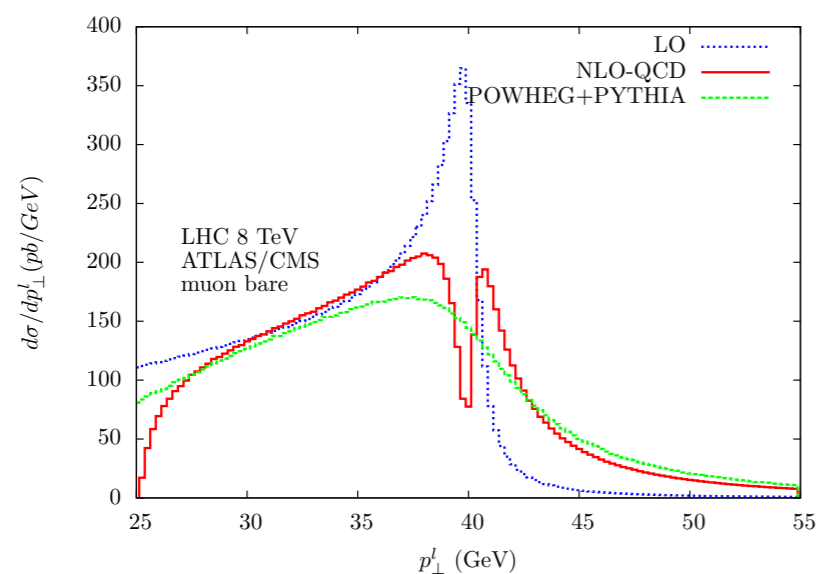
	CTEQ6.6		MSTW2008		NNPDF2.1		δ_{pdf}^{tot}
	$m_W \pm \delta_{pdf}$	$\langle \chi^2 \rangle$	$m_W \pm \delta_{pdf}$	$\langle \chi^2 \rangle$	$m_W \pm \delta_{pdf}$	$\langle \chi^2 \rangle$	
Tevatron, W^\pm	80.398 ± 0.004	1.42	80.398 ± 0.003	1.42	80.398 ± 0.003	1.30	4
LHC 7 TeV W^+	80.398 ± 0.004	1.22	80.404 ± 0.005	1.55	80.402 ± 0.003	1.35	8
LHC 7 TeV W^-	80.398 ± 0.004	1.22	80.400 ± 0.004	1.19	80.402 ± 0.004	1.78	6
LHC 14 TeV W^+	80.398 ± 0.003	1.34	80.402 ± 0.004	1.48	80.400 ± 0.003	1.41	6
LHC 14 TeV W^-	80.398 ± 0.004	1.44	80.404 ± 0.006	1.38	80.402 ± 0.004	1.57	8



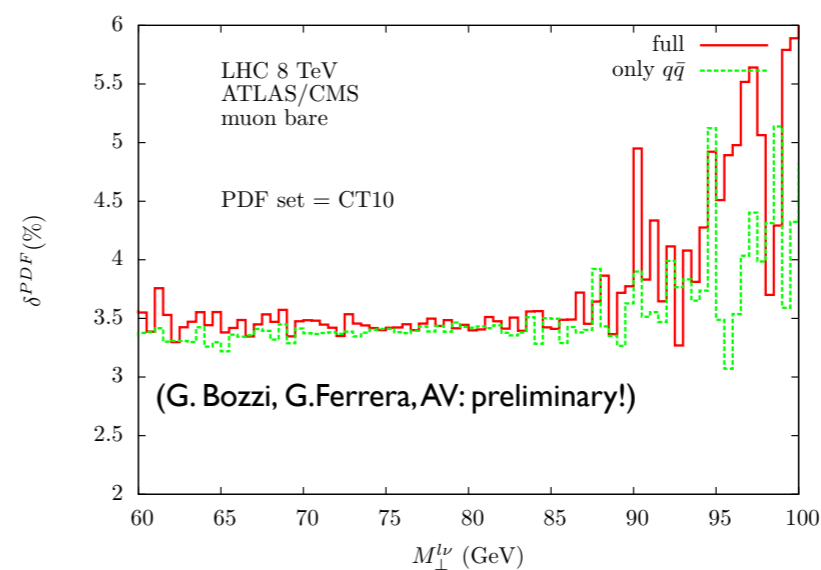
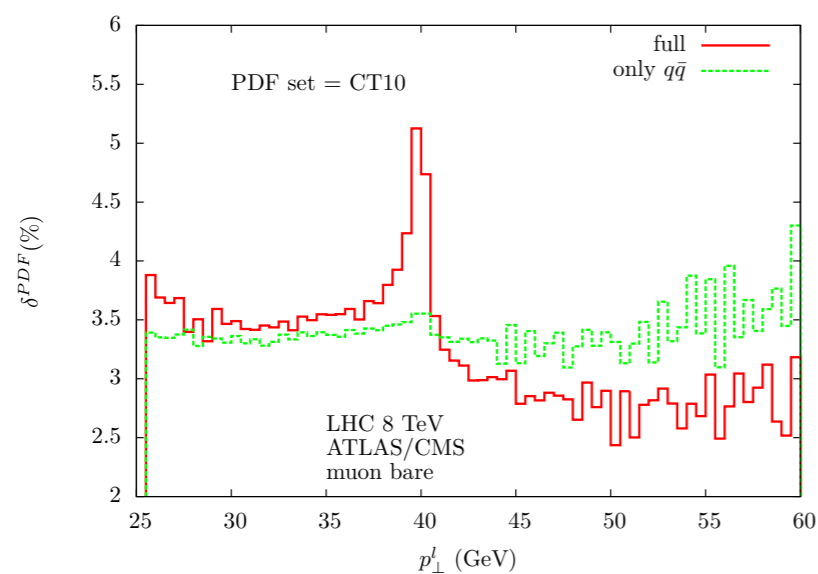
- the accuracy of the templates, to avoid spurious fluctuations, is very important because many effects are of $O(5 \text{ MeV})$: it is a highly demanding task from the computational point of view, already at NLO-QCD
- for the transverse mass distribution, a fixed order NLO-QCD analysis is sufficient to assess this uncertainty
- if confirmed, the PDF error is moderate at the Tevatron, but also at the LHC, even before the use of the LHC data

PDF error on MW from lepton transverse momentum distribution

- lepton transverse momentum distribution sensitive to the details of QCD radiation



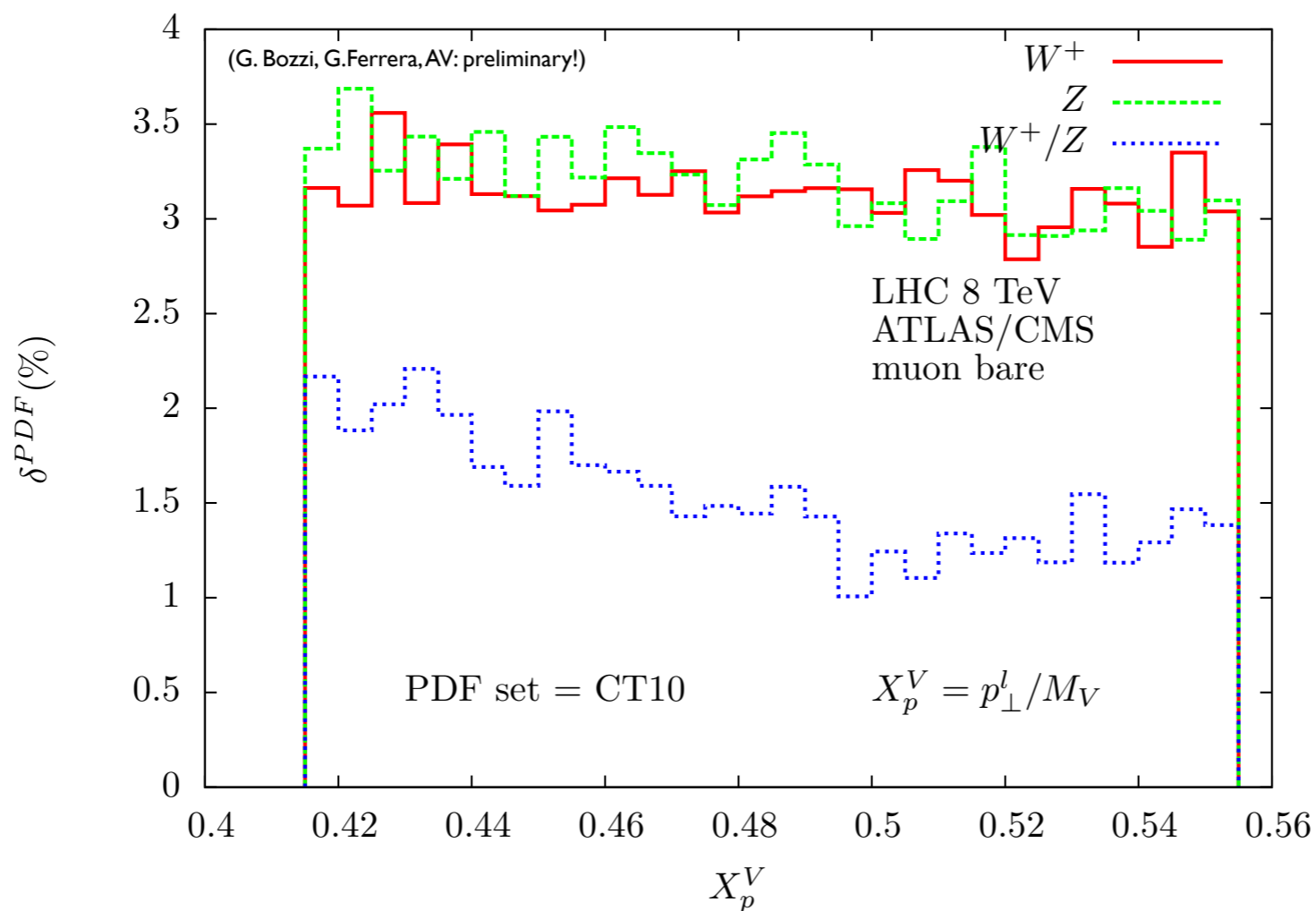
- at NLO-QCD gluon-quark subprocesses yield an important contribution
→ the gluon PDF uncertainty is more pronounced than in the transverse mass case
- the PDF uncertainty due to quarks is rather flat over the entire range of the distribution
- the effect of the momentum smearing has to be included in the templates used in the MW fit, to isolate the pure PDF contribution to the uncertainty



- caveat: 1) the above uncertainties have been computed with DYNNLO at NLO-QCD
2) only the full process has a well defined physical meaning
take these plots only as motivation for a complete study

PDF error on MW from lepton transverse momentum distribution

a **preliminary** study with DYqT shows that it is possible to partially get rid of the PDF uncertainty (e.g. of the quark-gluon luminosity) by studying appropriate ratios of observables which should preserve the sensitivity to MW (in progress)



$$\frac{d\sigma}{dX_p^V}$$

these results are obtained with DYqT including the resummation with (LO+NLL)-QCD accuracy of $\log(pt_V/M_V)$ including the gluon-induced subprocesses

the W^+ distribution is sensitive to MW (jacobian peak corresponding to $X_p=0.5$)

the Z distribution is weakly sensitive to MW (couplings), but probes similar x PDF ranges

It is crucial to have a precise assessment of the PDF uncertainty affecting MW in the lepton-pt case to understand if this is a potential bottleneck of the analysis

Conclusions

The MW measurement with 10 (or even 5) MeV of final error is a very ambitious task which requires a thorough discussion of several sources of theoretical systematic error

- different behaviour of observables inclusive vs more exclusive w.r.t. QCD radiation
relevance of QED radiation beyond LL-accuracy, including matching with exact NLO-EW results
- full NLO-(QCD+EW) matrix elements, matched with QCD+QED showers, are available in POWHEG both in CC and in NC
- matching resummation/Parton Shower with fixed order results introduces some ambiguities which affect the shape of pt_V distribution (and in turn of pt_l or MT_W and in turn of MW)
- the merging procedure to combine QCD and EW corrections may follow different prescriptions yielding different results → need for a full $O(\alpha\alpha_s)$ calculation
POWHEG QCD+EW provides a motivated Ansatz that includes systematically several higher-order mixed contributions
- PDF uncertainties are quite under control in the transverse mass case
require a better understanding of the gluon density in the lepton transverse momentum distribution
- purely EW corrections, including several $O(\alpha^2)$ subsets of corrections, are quite under control, with a residual uncertainty at the level of 5 MeV
- a detailed tune of PYTHIA parameters must be performed with POWHEG QCD+EW NC and the result consistently applied to the CC process
- the fitting procedure introduces its own systematic error in the MW determination

back-up slides

Inclusion in POWHEG of the exact $O(\alpha)$ corrections (NLO-EW)

$$d\sigma = \sum_{f_b} \bar{B}^{f_b}(\Phi_n) d\Phi_n \left\{ \Delta^{f_b}(\Phi_n, p_T^{min}) + \sum_{\alpha_r \in \{\alpha_r | f_b\}} \frac{[d\Phi_{rad} \theta(k_T - p_T^{min}) \Delta^{f_b}(\Phi_n, k_T) R(\Phi_{n+1})]_{\alpha_r}^{\bar{\Phi}_n^{\alpha_r} = \Phi_n}}{B^{f_b}(\Phi_n)} \right\}$$

- the POWHEG basic formula
 - is additive in the overall normalization,
 - it describes exactly one parton emission (photon/gluon/quark) (but NOT two partons)
 - includes in a factorized form mixed and higher order corrections relevant in the distributions in particular the bulk of the $O(\alpha\alpha_s)$ corrections (but it has NOT $O(\alpha\alpha_s)$ accuracy)

- difference with respect to

$$\mathcal{O} = \mathcal{O}_{LO} \left(1 + \delta_{QCD}^{NLO+NNLO} + \delta_{EW}^{NLO} \right)$$

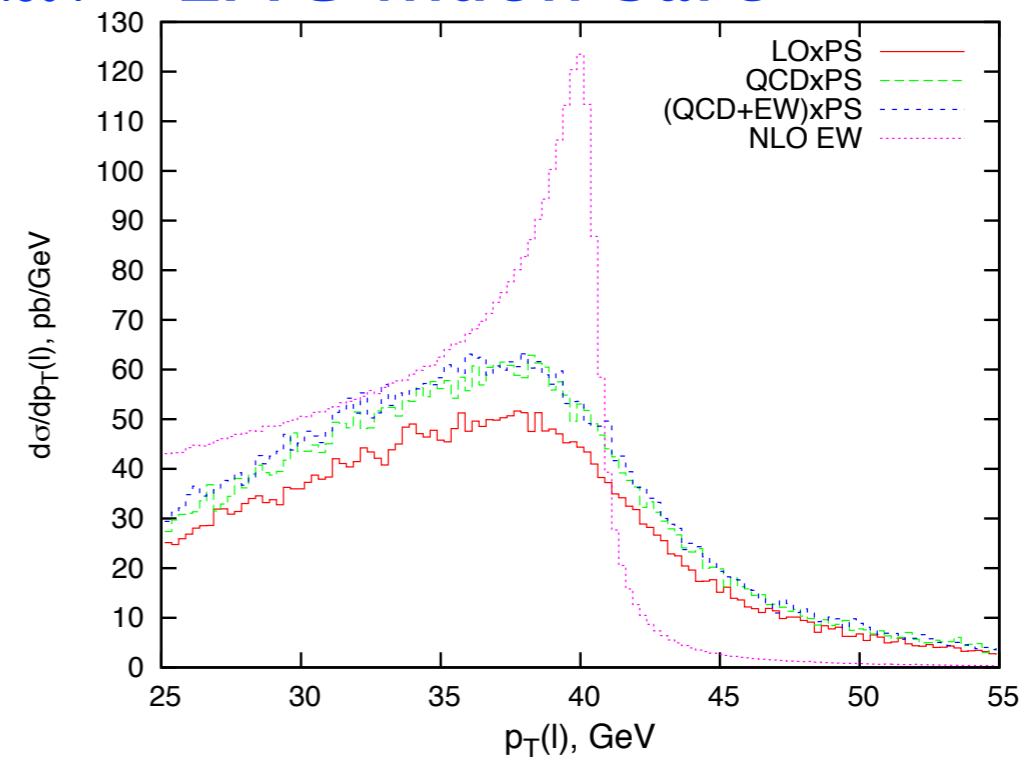
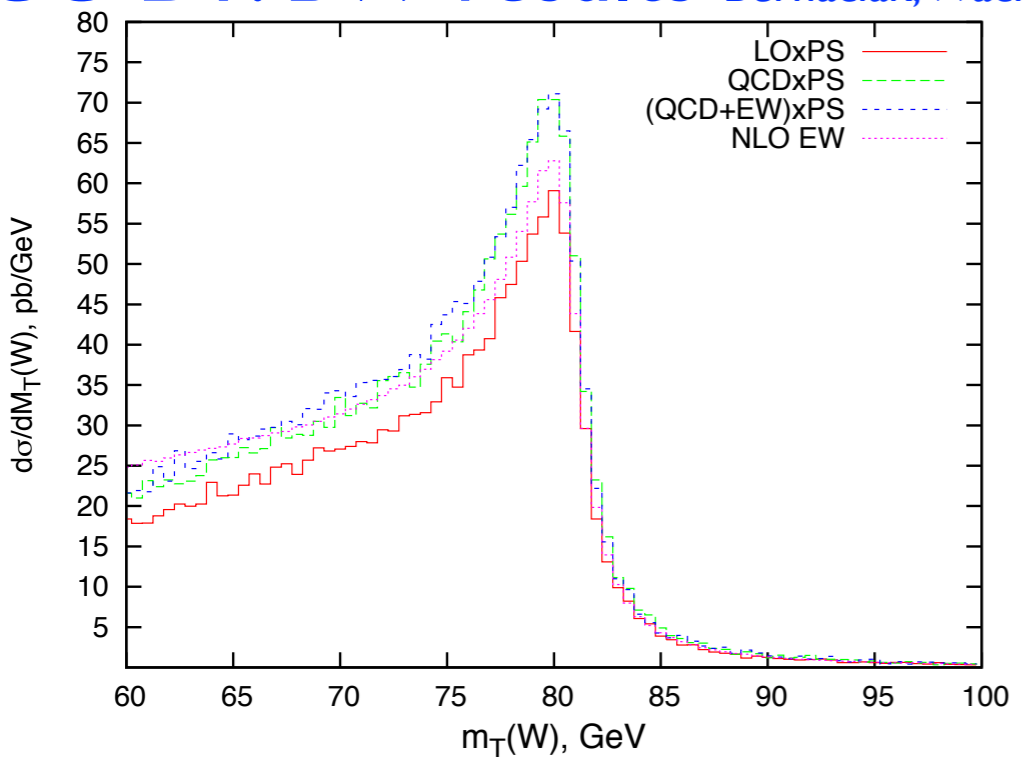
1) purely additive prescription

$$\mathcal{O} = \mathcal{O}_{LO} \left(1 + \delta_{QCD}^{NLO+NNLO} \right) \left(1 + \delta_{EW}^{NLO} \right)$$

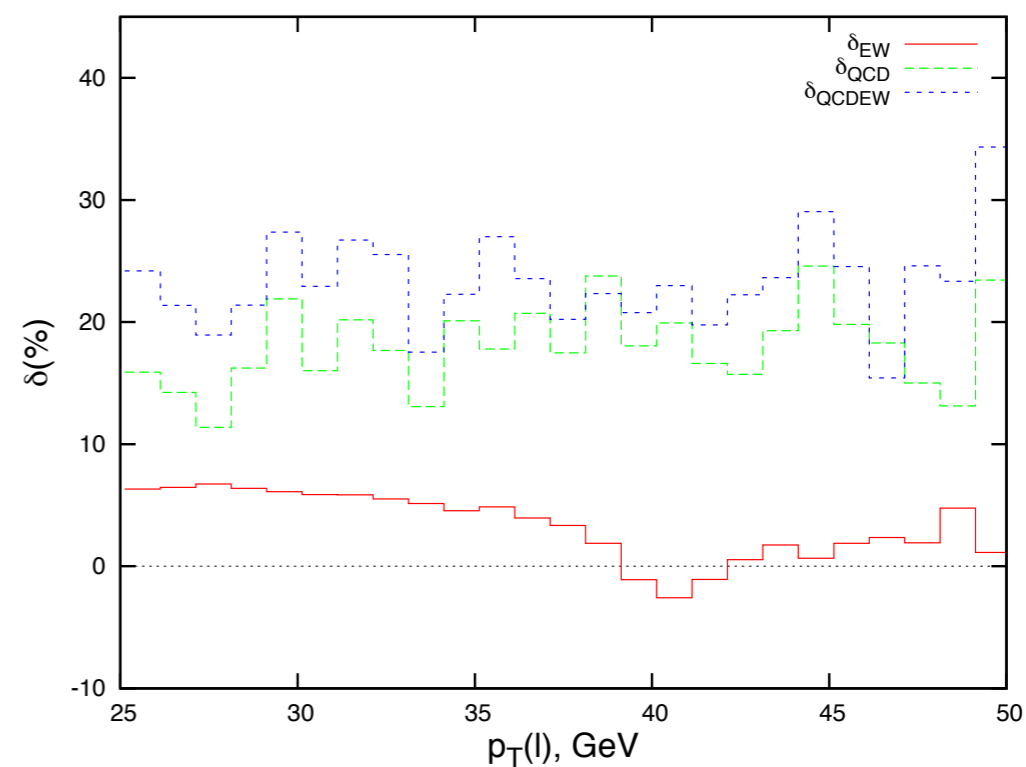
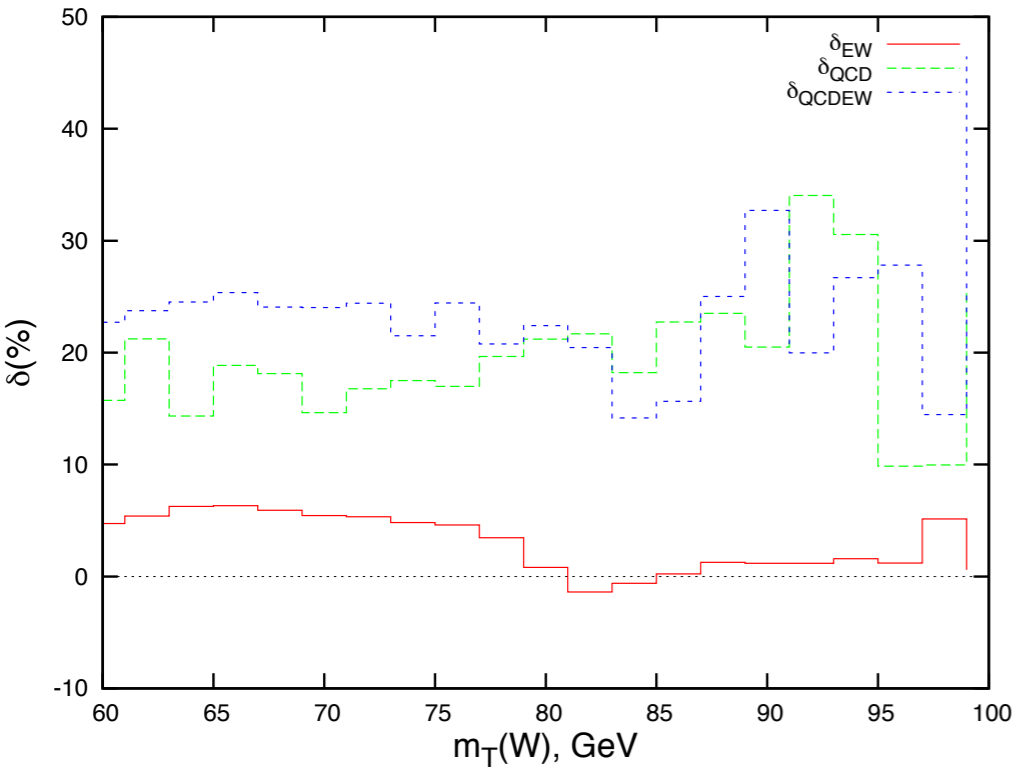
2) factorized use of (differential) K-factors

- POWHEG accounts for multiple emission effects
- the kinematics of multiple emissions is exact (fully differential)

- the subtraction of IS QED collinear singularities is consistent only with MRST2004QED, where the evolution kernel of the parton densities includes also a QED term; updated PDF set including QED effects will be welcome!

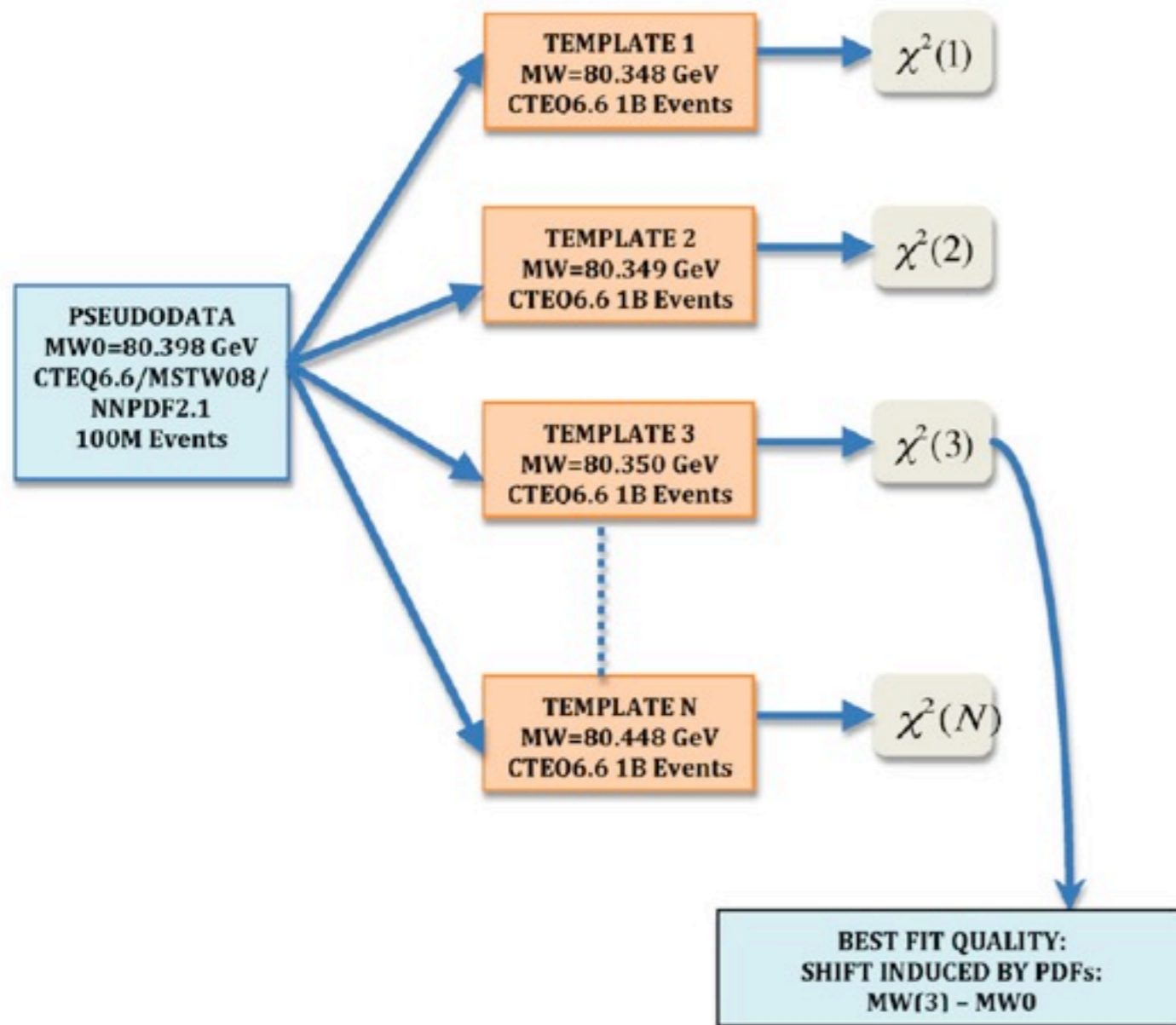


- all the results in the α_0 input scheme
- the pure NLO-EW curves do NOT include the QCD Parton Shower (δ is relative to pure LO)
- the (QCD+EW)xPS results include only the QCD Parton Shower
- QCD corrections tend to be flat over the whole M_T range
- the sharp peak of lepton p_T distribution due to EW corrections is reduced by the QCD-Parton Shower



Estimate of the error on MW induced by the PDFs (G. Bozzi et al, arXiv:1104.2056)

- each PDF replica is used to generate a set of pseudodata, with a fixed value MW_0
- a very accurate set of template distributions has been prepared, varying only MW, with a reference(CTEQ6.6) PDF replica
- when pseudodata generated with the reference replica are fitted, the nominal value MW_0 is found (sanity check)
- the same code, DYNNLO, has been used to generate both, pseudodata and templates \rightarrow only effect probed is the PDF one



- the MW shift expresses the distance between the PDF replica under study and the reference replica
- the PDF error is obtained combining the different MW results from each replica, according to the formulae recommended by the PDF collaborations

Matching NLO calculations with resummation: DY_{qT}

Bozzi, Catani, De Florian, Ferrera, Grazzini

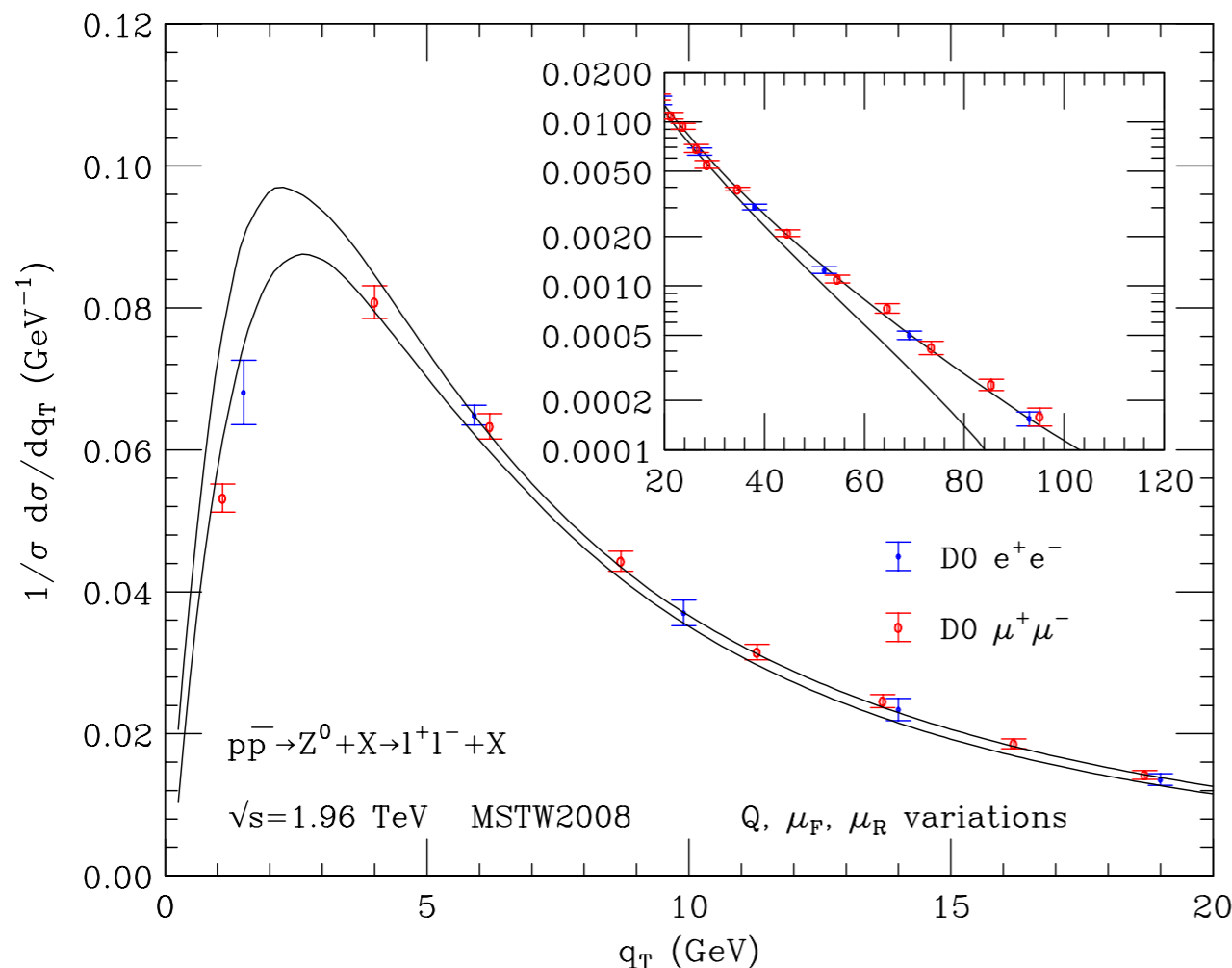
$$\frac{d\hat{\sigma}_{Vab}^{(\text{res.})}}{dq_T^2}(q_T, M, \hat{s}; \alpha_S(\mu_R^2), \mu_R^2, \mu_F^2) = \frac{M^2}{\hat{s}} \int_0^\infty db \frac{b}{2} J_0(bq_T) \mathcal{W}_{ab}^V(b, M, \hat{s}; \alpha_S(\mu_R^2), \mu_R^2, \mu_F^2) ,$$

process dependent

$$\mathcal{W}_N^V(b, M; \alpha_S(\mu_R^2), \mu_R^2, \mu_F^2) = \mathcal{H}_N^V(M, \alpha_S(\mu_R^2); M^2/\mu_R^2, M^2/\mu_F^2, M^2/Q^2) \times \exp\{\mathcal{G}_N(\alpha_S(\mu_R^2), L; M^2/\mu_R^2, M^2/Q^2)\} ,$$

universal

G. Bozzi, S. Catani, D. de Florian, G. Ferrera, M. Grazzini, arXiv:1007.2351



Q is the resummation scale

the fixed order total cross section is by construction reproduced

a non-perturbative smearing factor can be applied on top of the pQCD result

Comparison between POWHEG and MC@NLO

$$d\sigma^{\text{NLO+PS}} = d\Phi_B \bar{B}^s(\Phi_B) \left[\Delta^s(p_{\perp}^{\min}) + d\Phi_{R|B} \frac{R^s(\Phi_R)}{B(\Phi_B)} \Delta^s(p_T(\Phi)) \right] + d\Phi_R R^f(\Phi_R)$$

$$\bar{B}^s = B(\Phi_B) + \left[V(\Phi_B) + \int d\Phi_{R|B} R^s(\Phi_{R|B}) \right]$$

R^s enters in the Sudakov form factor $\Delta^s(p_T(\Phi))$

the virtuality of the first, hardest emission is analogous to the resummation scale in DYqT, different event by event

MC@NLO

$$R^s \propto \frac{\alpha_s}{t} P_{ij}(z) B(\Phi_B)$$

$$R^f = R - R^s$$

the universal collinear splitting function is used in the Sudakov

the full matrix element R is used only in the regular part

POWHEG

$$R^s = \frac{h^2}{h^2 + p_T^2} R, \quad R^f = \frac{p_T^2}{h^2 + p_T^2} R$$

the scale h (introduced in the Higgs gluon fusion code) divides low from large p_T values

at low p_T , R tends to its collinear approximation

at large p_T the damping factor suppresses R in the Sudakov

- the two approaches exactly agree at NLO-QCD, they differ by higher order corrections

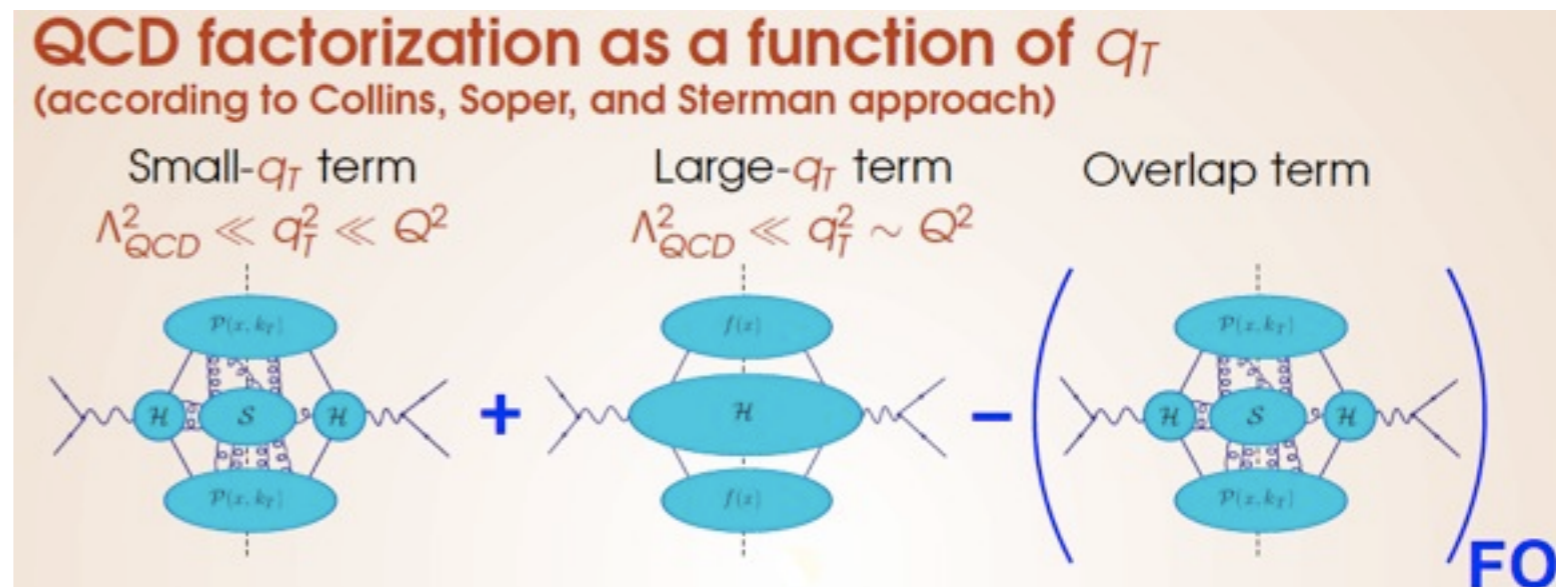
a choice of h that mimics a NLO+NNLL shape must be supplemented by a study on the systematics obtained by varying h

different choices for R^f , combined with the cross section unitarity constraint, may lead to an uncertainty band on $p_T H$

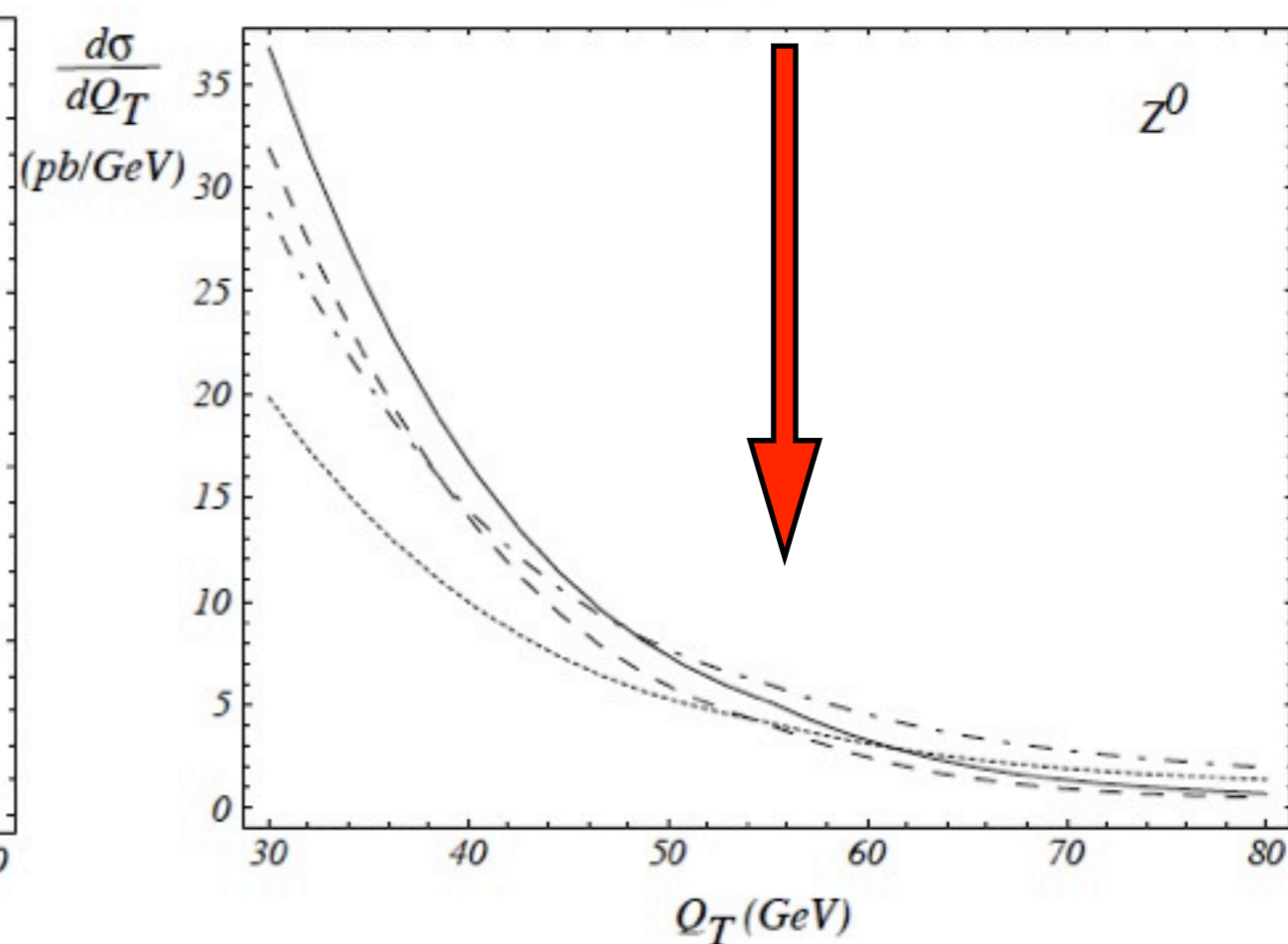
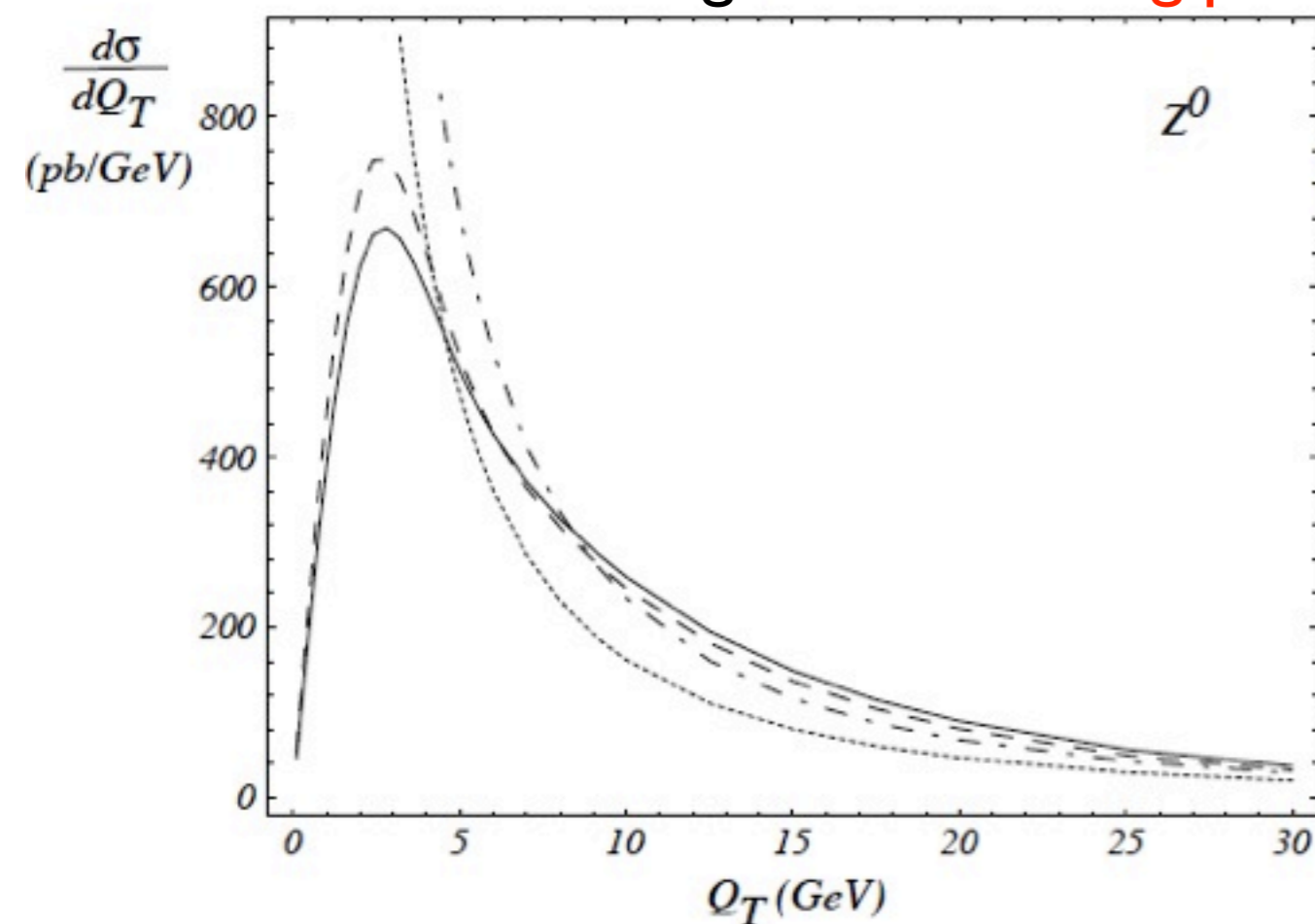
Matching NLO calculations with resummation: ResBos

Landry, Brock, Nadolski, Yuan, Balazs

- Finite order: part of the NNLO results
lepton spin correlation at NLO
- Resummed term W at NNLL
for Sudakov factor and non-collinear $pdfs$
- Two representations of the
hard-vertex function H



matching at the **crossing point** between resummed and fixed order results



On-going benchmarking study within the LHC-EWWG

see <http://lpsc.web.cern.ch/lpsc/>

- the authors of the following codes are actively participating to this study
 - HORACE, RADY, SANC, WZGRAD
 - PHOTOS, WINHAC
 - DYNNLO, FEWZ
 - POWHEG (only QCD and QCD+EW)
- in a first phase, technical agreement (same inputs \Rightarrow same outputs)
at LO, NLO-QCD, NLO-EW has been reached on differential distributions at better than 0.5% level
- given this common starting point with NLO accuracy,
we are now exploring the impact of higher order corrections (pure QCD, pure EW, mixed QCDxEW)
 - corrections available only in some codes (e.g. NNLO-QCD vs QCD-PS)
 - ambiguities which can not be fixed without an explicit full next-order calculation (e.g. EW inputs)