



Review of Rare Kaon Decays (NA48/2 and NA62)

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on behalf of NA48/2 and NA62 collaborations

Outline:

- 1) Introduction to CERN kaon programme
- 2) Study of the rare decay $K^{\pm} \rightarrow \pi^{\pm} \gamma \gamma$
- 3) Precision measurements of $K^{\pm} \rightarrow \pi^+ \pi^- e^{\pm} \nu$ and $K^{\pm} \rightarrow \pi^0 \pi^0 e^{\pm} \nu$
- 4) Summary



Kaon physics facilities

BNL

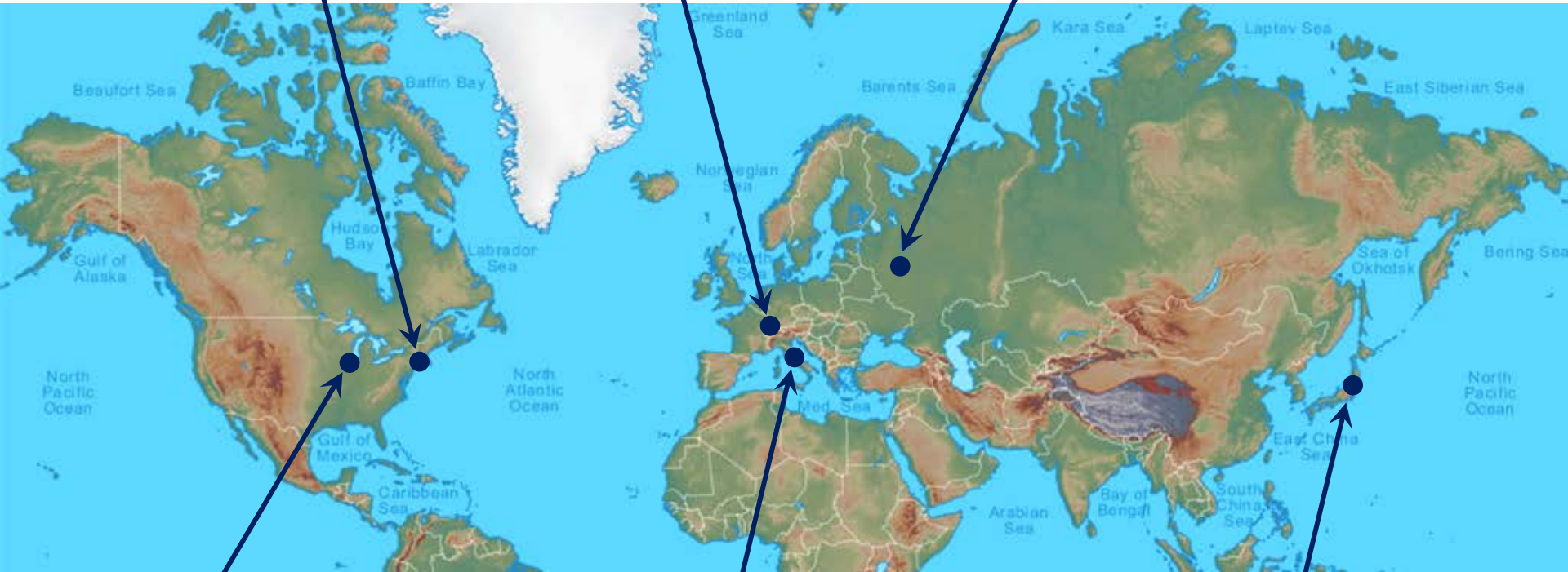
E865, E777, E787, E949

CERN

NA48, NA62

IHEP

ISTRA+, OKA



FNAL

KTeV, ORKA

LNF

KLOE, KLOE2

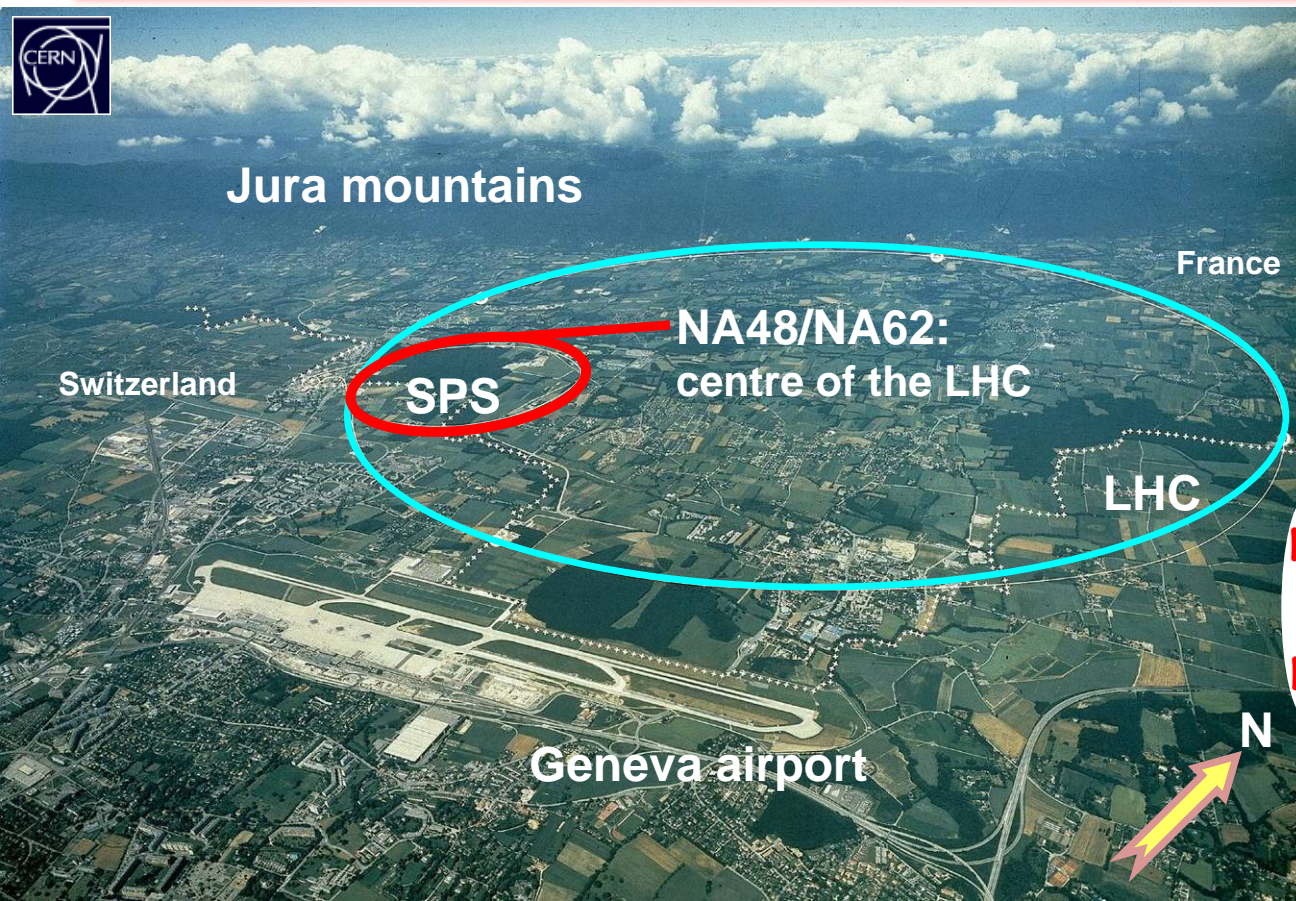
KEK/J-PARC

E391a, KOTO, TREK

A variety of experimental techniques:

K decay-in-flight (e.g. CERN), stopped **K**⁺ and a ϕ factory

CERN NA48/NA62 experiments



NA48/NA62 talks in Flavour Physics session:
 (semi)leptonic K^\pm decays by Riccardo Fantechi,
 future programme by Gianluca Lamanna.

Earlier: NA31

NA48 discovery of direct CPV	1997: $\epsilon'/\epsilon: K_L+K_S$
	1998: K_L+K_S
	1999: K_L+K_S K_S HI
	2000: K_L only K_S HI
	2001: K_L+K_S K_S HI
NA48/1	2002: K_S /hyperons
NA48/2	2003: K^+/K^-
	2004: K^+/K^-
NA62 R_K phase	2007: $K_{e2}^\pm/K_{\mu2}^\pm$ tests
	2008: $K_{e2}^\pm/K_{\mu2}^\pm$ tests
NA62	2012: technical run
	2014: 1 st $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ run

Detector: NA48/2 and NA62-R_K

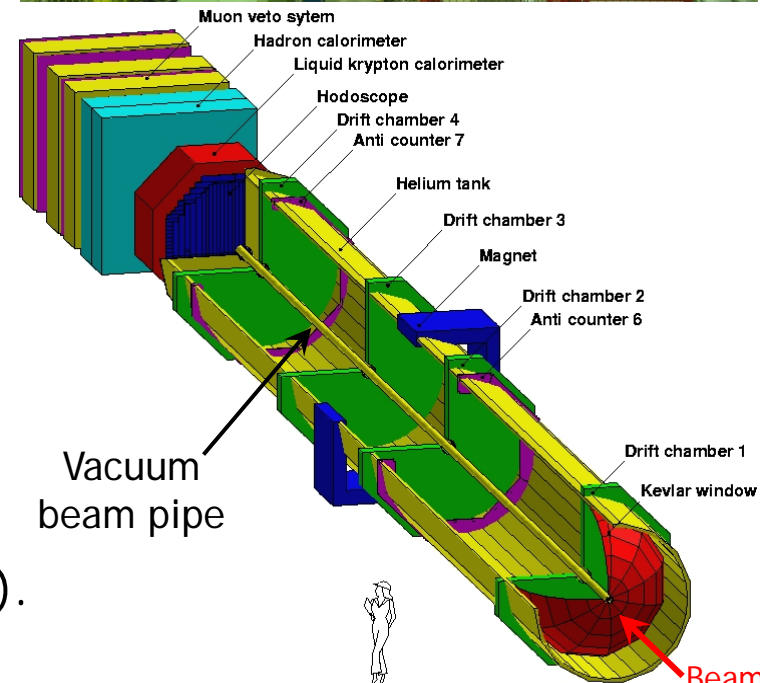
2003–2008: charged kaon beams,
the NA48 detector

Narrow momentum band K^\pm beams:
 $P_K = 60$ (74) GeV/c, $\delta P_K/P_K = 1\text{...}4\%$ (rms).

- ❖ **NA48/2**: six months in 2003–04;
- ❖ **NA62-R_K**: four months in 2007.

Principal subdetectors:

- ❖ **Magnetic spectrometer (4 DCHs)**
4 views/DCH: redundancy \Rightarrow efficiency;
 $\delta p/p = 0.48\% + 0.009\%p$ [GeV/c] (in 2007)
- ❖ **Scintillator hodoscope**
Fast trigger, time measurement (150ps).
- ❖ **Liquid Krypton EM calorimeter (LKr)**
High granularity, quasi-homogeneous;
 $\sigma_E/E = 3.2\%/E^{1/2} + 9\%/E + 0.42\%$ [GeV];
 $\sigma_x = \sigma_y = 4.2\text{mm}/E^{1/2} + 0.6\text{mm}$ (1.5mm@10GeV).



Recent K^\pm data samples

Experiment	NA48/2 (K^\pm)	NA62-R _K (K^\pm)	NA62 (K^+ ; <i>planned</i>)
Data taking period	2003–2004	2007–2008	2014–2017
Beam momentum, GeV/c	60	74	75
RMS momentum bite, GeV/c	2.2	1.4	0.8
Spectrometer thickness, X_0	2.8%	2.8%	1.8%
Spectrometer P_T kick, MeV/c	120	265	270
$M(K^+ \rightarrow \pi^+ \pi^+ \pi^-)$ resolution, MeV/c ²	1.7	1.2	0.8
K decays in fiducial volume	1.9×10^{11}	2.5×10^{10}	1.2×10^{13}
Main trigger	multi-track; $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$	e^\pm	$K_{\pi\nu\nu} + \dots$

Same detector (NA48)

$K^\pm \rightarrow \pi^\pm \gamma\gamma$: introduction

ChPT: spectrum determined by \hat{c} parameter.
 Dominated by pion loop: cusp at $2\pi^\pm$ threshold
 [Ecker, Pich, de Rafael, NPB303 (1988) 665]

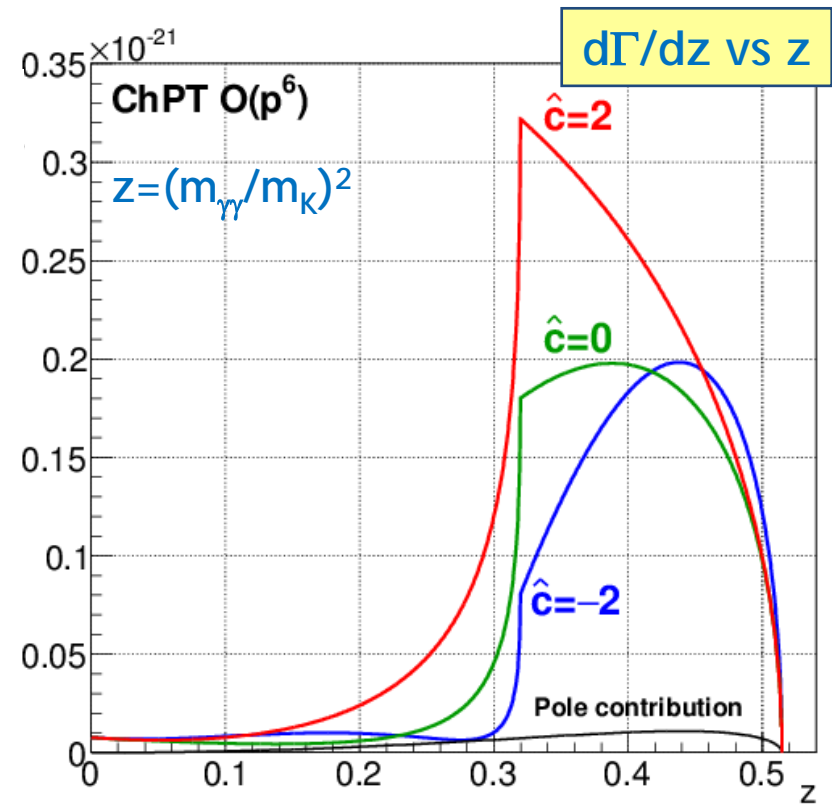
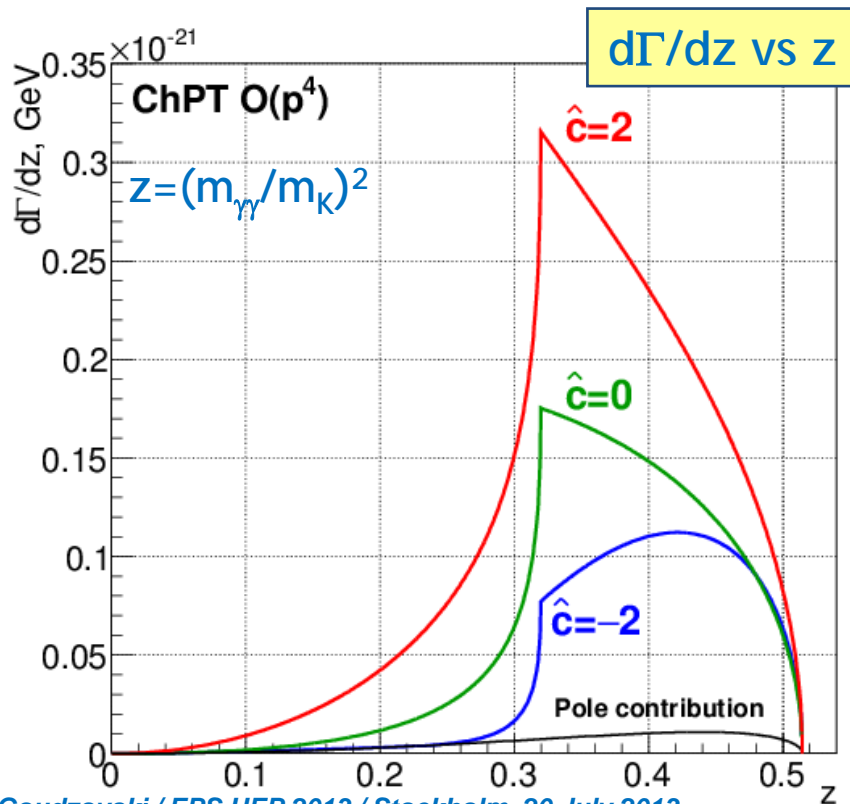
$O(p^6)$: significant correction;
 non-zero rate at $m_{\gamma\gamma}=0$.

[D'Ambrosio, Portolés, PLB386 (1996) 403]
 [Gérard, Smith, Trine, NPB730 (2005) 1]

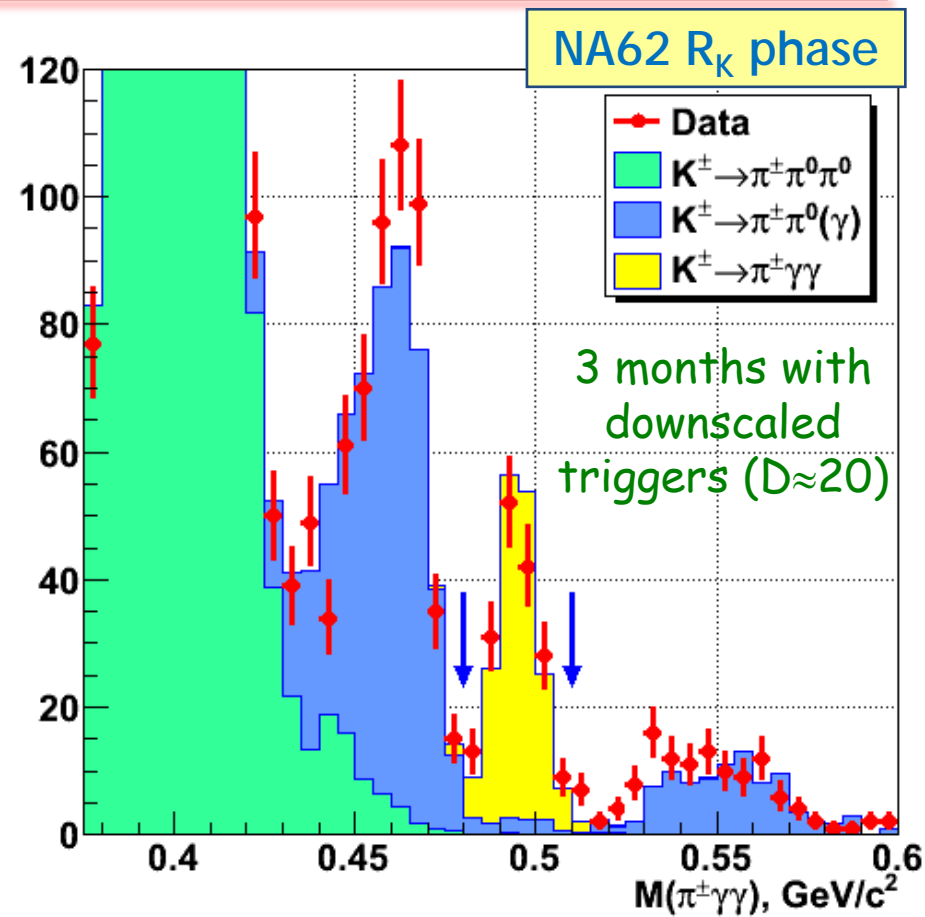
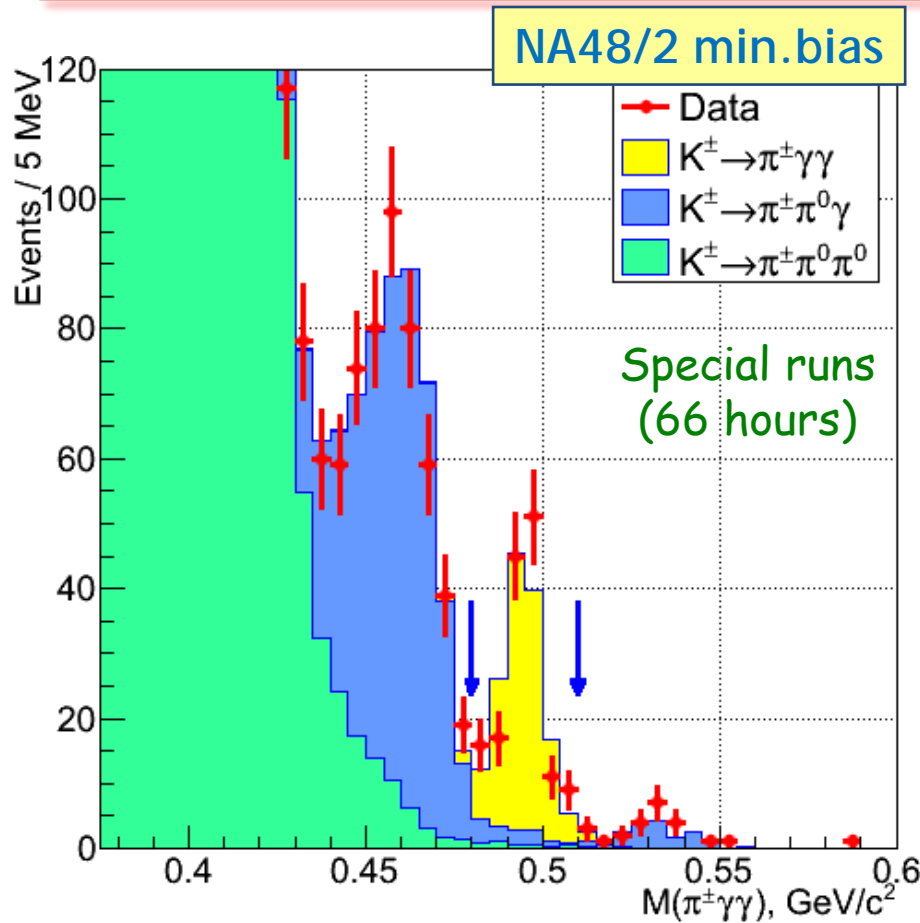
Experimental status:

❖ BNL E787: 31 candidates,
 $BR = (1.10 \pm 0.32) \times 10^{-6}$.
 [PRL79 (1997) 4079]

❖ NA48/2, NA62: using low beam
 intensity minimum bias samples



Minimum bias data samples



$K_{\pi\gamma\gamma}$ candidates	149
$K_{2\pi(\gamma)}$ background	11.4 ± 0.6
$K_{3\pi}$ background	4.1 ± 0.4
$K_{\pi\gamma\gamma}$ signal	134 ± 12

$K_{\pi\gamma\gamma}$ candidates	175
$K_{2\pi(\gamma)}$ background	11.1 ± 1.0
$K_{3\pi}$ background	1.3 ± 0.3
$K_{\pi\gamma\gamma}$ signal	163 ± 13

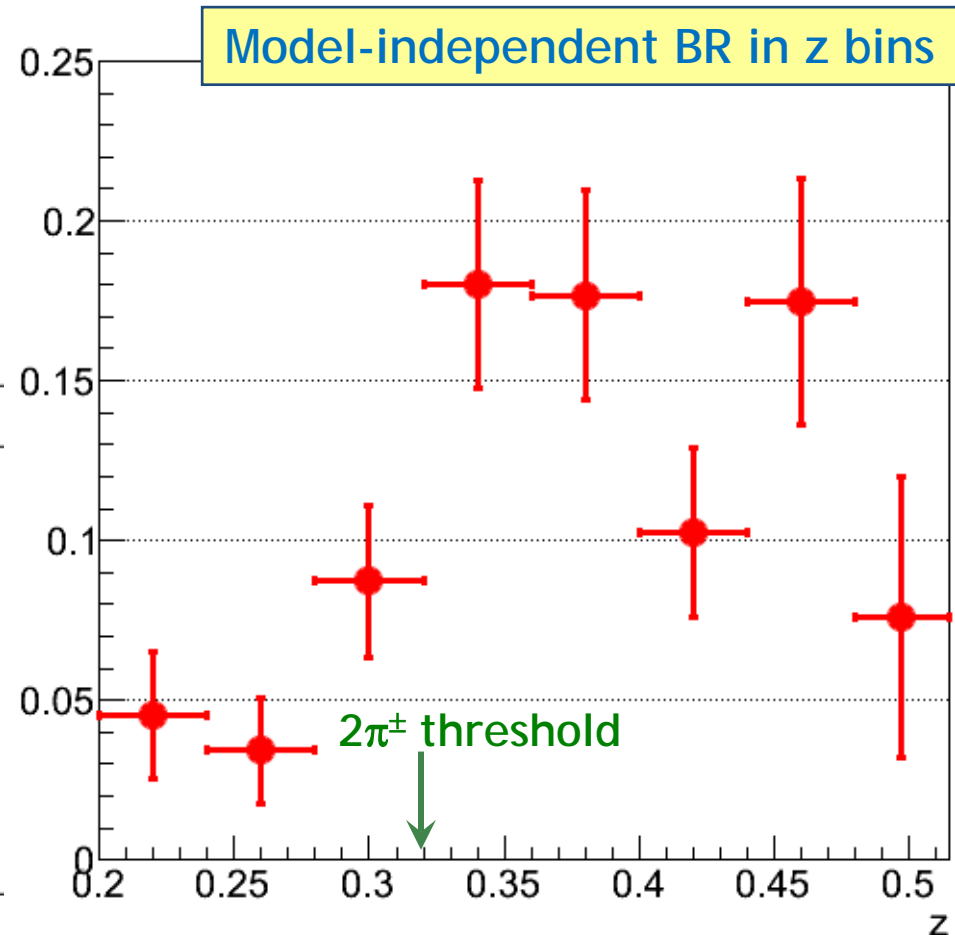
NA48/2: model-independent BR

THE FINAL NA48/2 RESULT

NEW: July 2013

Sufficiently small z bins:
acceptance almost independent
of kinematical distribution

z range	N_j	N_j^B	A_j	$B_j \times 10^6$
0.20–0.24	13	4.89	0.194	0.045 ± 0.020
0.24–0.28	9	2.73	0.198	0.034 ± 0.016
0.28–0.32	18	2.33	0.194	0.087 ± 0.024
0.32–0.36	33	1.30	0.190	0.180 ± 0.033
0.36–0.40	31	0.98	0.184	0.177 ± 0.033
0.40–0.44	18	1.61	0.173	0.103 ± 0.027
0.44–0.48	23	1.21	0.135	0.175 ± 0.038
$z > 0.48$	4	0.52	0.049	0.076 ± 0.044



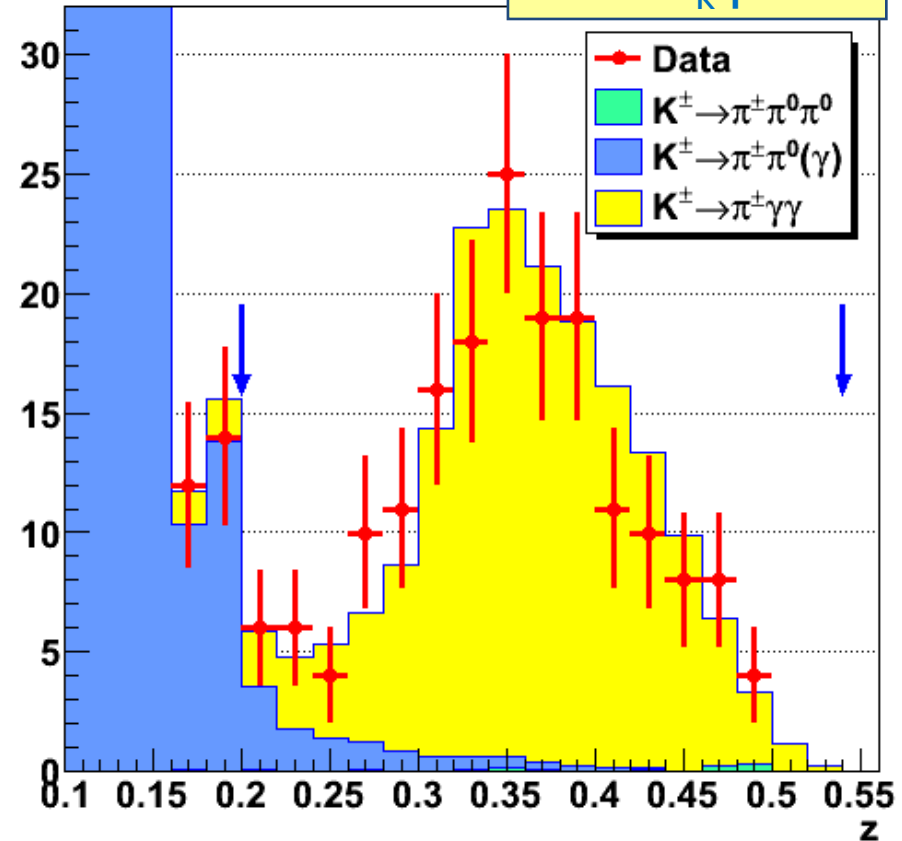
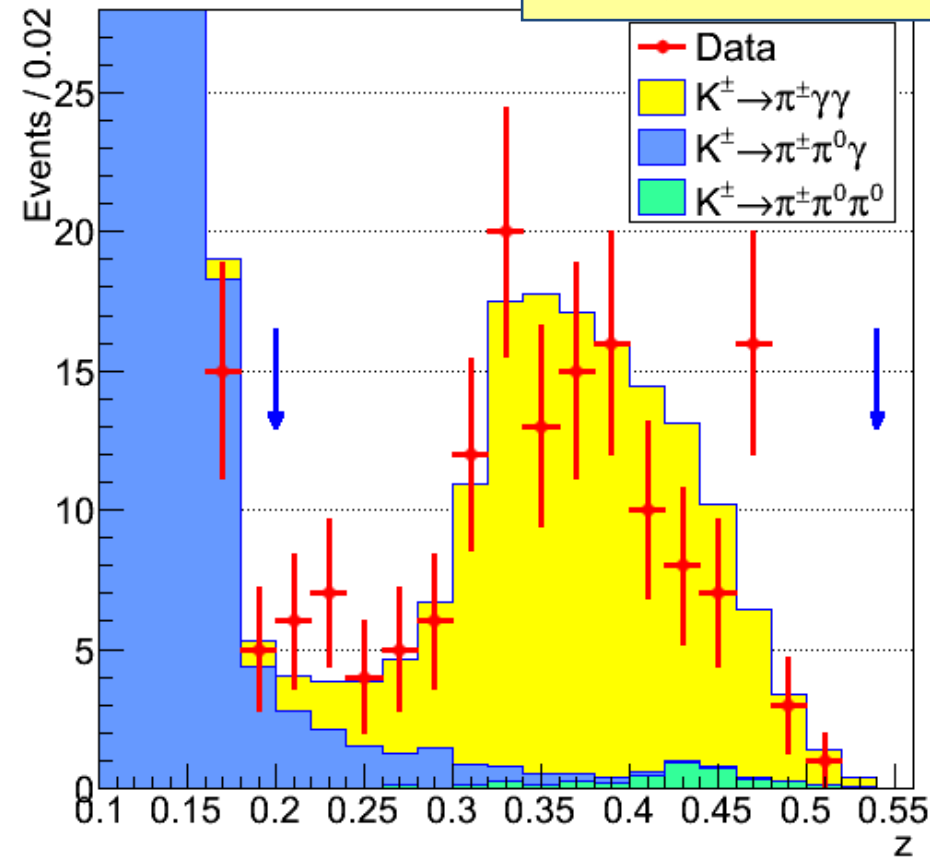
$$BR_{MI}(z>0.2) = (0.877 \pm 0.087_{\text{stat}} \pm 0.017_{\text{syst}}) \times 10^{-6}$$

Main systematic effect: background estimate (LKr cluster merging)

Fits to ChPT description

NA48/2 min.bias

NA62 R_K phase



External parameters of the $O(p^6)$ fit:

$K_{3\pi}$ amplitude parameters: from fit to experimental data [NPB648 (2003) 317];

polynomial contributions: $\eta_1=2.06$, $\eta_2=0.24$, $\eta_3=-0.26$ [PLB386 (1996) 403].

→ Data support the ChPT prediction of a cusp at the di-pion threshold

Fits to ChPT: results

ChPT formulation: D'Ambrosio, Portolés, PLB386 (1996) 403

PRELIMINARY

NA48/2 (minimum bias)

ChPT $O(p^4)$:

$$\hat{c} = 1.36 \pm 0.33_{\text{stat}} \pm 0.07_{\text{syst}} = 1.36 \pm 0.34$$

ChPT $O(p^6)$:

$$\hat{c} = 1.67 \pm 0.39_{\text{stat}} \pm 0.09_{\text{syst}} = 1.67 \pm 0.40$$

NA62 (2007)

ChPT $O(p^4)$:

$$\hat{c} = 1.71 \pm 0.29_{\text{stat}} \pm 0.06_{\text{syst}} = 1.71 \pm 0.30$$

ChPT $O(p^6)$:

$$\hat{c} = 2.21 \pm 0.31_{\text{stat}} \pm 0.08_{\text{syst}} = 2.21 \pm 0.32$$



Combined

ChPT $O(p^4)$ fit: (correlated systematic uncertainties)

$$\hat{c} = 1.56 \pm 0.22_{\text{stat}} \pm 0.07_{\text{syst}} = 1.56 \pm 0.23$$

ChPT $O(p^6)$ fit:

$$\hat{c} = 2.00 \pm 0.24_{\text{stat}} \pm 0.09_{\text{syst}} = 2.00 \pm 0.26$$

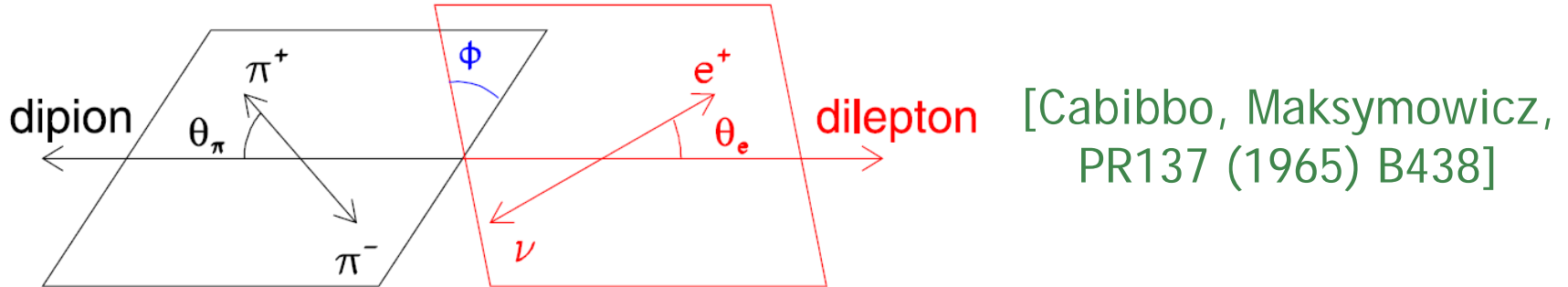
$$BR_6 = (1.01 \pm 0.06) \times 10^{-6}$$

(model-dependent BR
in full phase space)

Cf. PDG (=BNL E787): $BR_6 = (1.10 \pm 0.32) \times 10^{-6}$

K_{e4} decays: introduction

Five kinematic variables: S_π , S_e , $\cos\theta_\pi$, $\cos\theta_e$, Φ



Partial wave expansion and form factors [Pais, Treiman, PR168 (1968) 1858]

$$K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu \quad (K_{e4}^{+-})$$

$$K^\pm \rightarrow \pi^0 \pi^0 e^\pm \nu \quad (K_{e4}^{00})$$

$$F = F_s e^{i\delta_s} + F_p e^{i\delta_p} \cos \theta_\pi + \dots$$

$$F = F_s e^{i\delta_s}$$

$$G = G_p e^{i\delta_g} + \dots; \quad H = H_p e^{i\delta_h} + \dots$$

$$\left\{ \begin{array}{l} F_s = f_s + f'_s q^2 + f''_s q^4 + f'_e S_e / 4m_\pi^2 + \dots \\ F_p = f_p + f'_p q^2 + \dots \\ G_p = g_p + g'_p q^2 + \dots \end{array} \right.$$

$$H_p = h_p + h'_p q^2 + \dots \quad \text{vector}$$

$$\delta(q^2) = \delta_s - \delta_p.$$

$\pi\pi$ s-wave scattering lengths
can be extracted

from variation of δ with S_π

[Ananthanarayan et al.,

Phys.Rep. 353 (2001) 207;

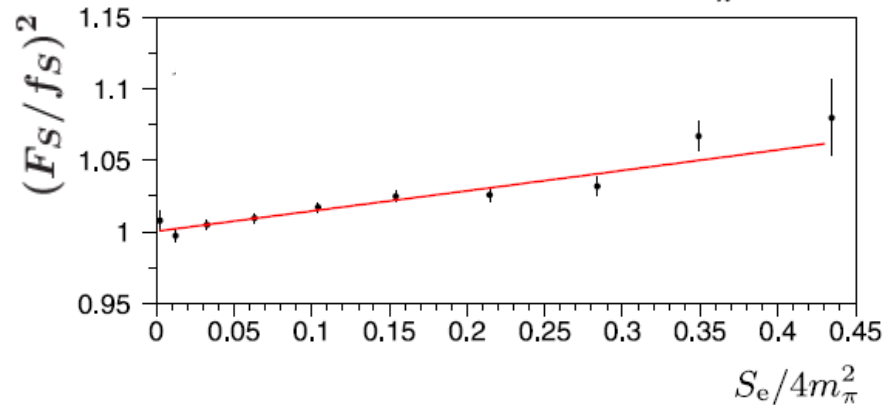
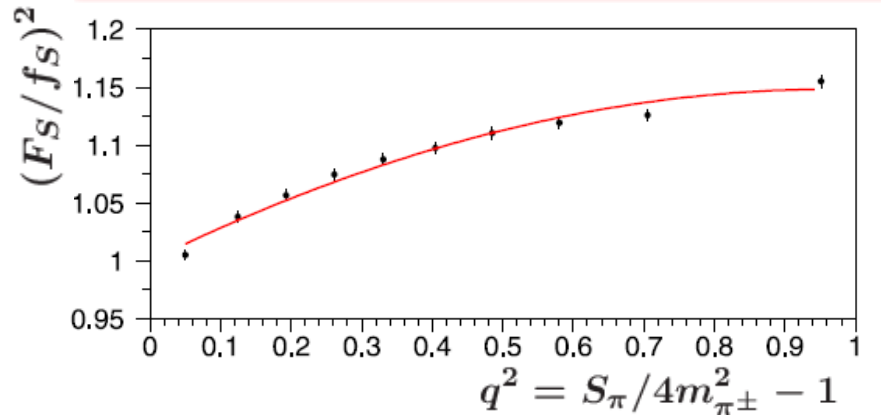
Colangelo, Gasser, Rusetsky,

EPJC59 (2009) 777]

NA48/2: $K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu$ form factors

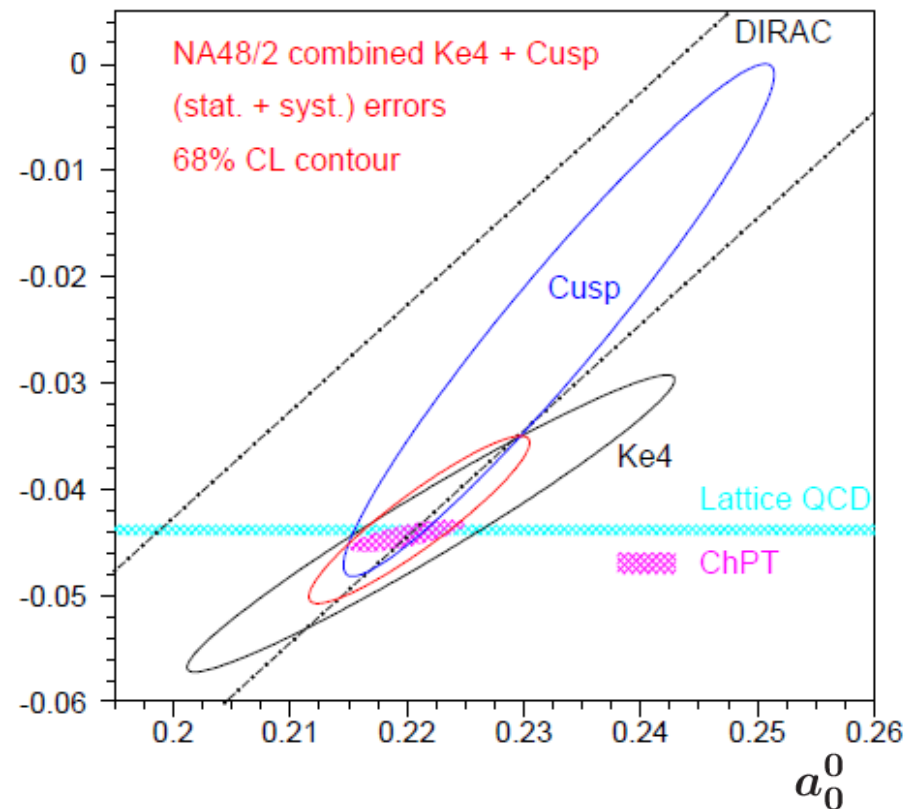
Final NA48/2 results [EPJC70 (2010) 635]

1.13M candidates, 0.6% background
(from $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$, $K^\pm \rightarrow \pi^\pm \pi^0_D$ (π^0))



a_0^2

s-wave pion scattering lengths



f'_s/f_s	=	0.152	$\pm 0.007_{\text{stat}}$	$\pm 0.005_{\text{syst}}$
f''_s/f_s	=	-0.073	$\pm 0.007_{\text{stat}}$	$\pm 0.006_{\text{syst}}$
f'_e/f_s	=	0.068	$\pm 0.006_{\text{stat}}$	$\pm 0.007_{\text{syst}}$
f_p/f_s	=	-0.048	$\pm 0.003_{\text{stat}}$	$\pm 0.004_{\text{syst}}$
g_p/f_s	=	0.868	$\pm 0.010_{\text{stat}}$	$\pm 0.010_{\text{syst}}$
g'_p/f_s	=	0.089	$\pm 0.017_{\text{stat}}$	$\pm 0.013_{\text{syst}}$
h_p/f_s	=	-0.398	$\pm 0.015_{\text{stat}}$	$\pm 0.008_{\text{syst}}$

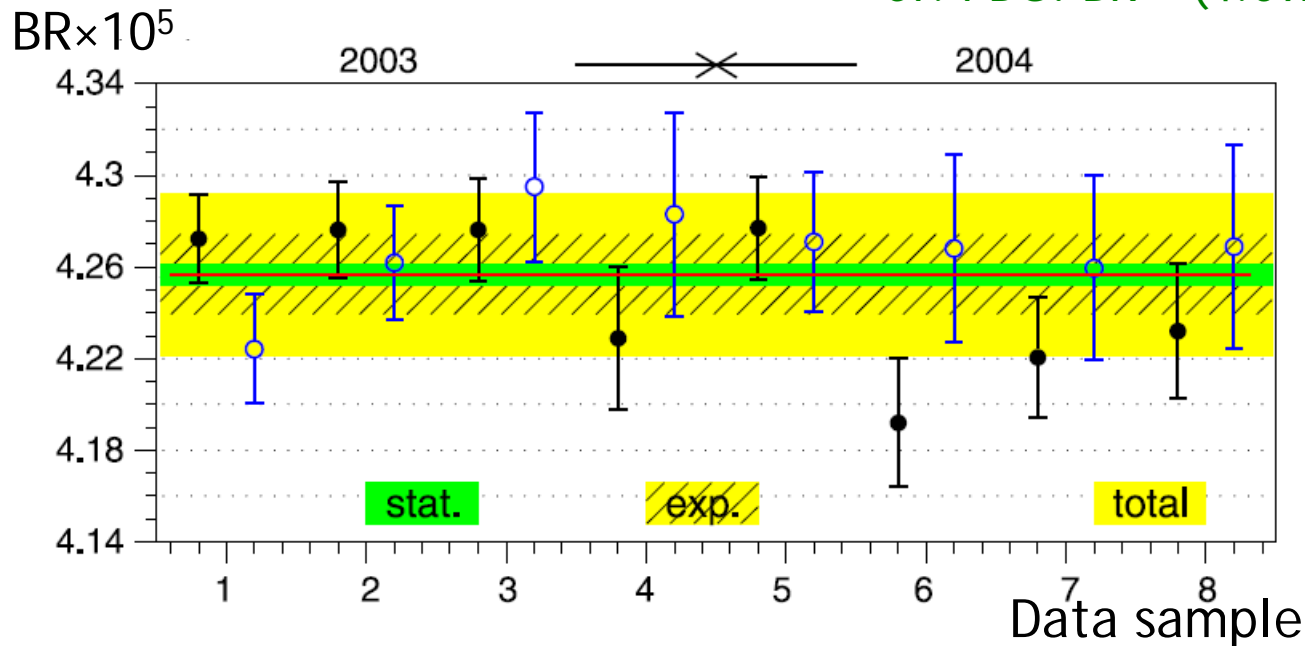
NA48/2: $\text{BR}(\text{K}^\pm \rightarrow \pi^+ \pi^- e^\pm \nu)$ and f_s

BR measured with respect to normalisation mode: $\text{K}^\pm \rightarrow \pi^+ \pi^- \pi^\pm$.

Final result: [PLB715 (2012) 105]

$$\text{BR}(\text{K}^\pm \rightarrow \pi^+ \pi^- e^\pm \nu) = (4.257 \pm 0.004_{\text{stat}} \pm 0.016_{\text{syst}} \pm 0.031_{\text{ext}}) \times 10^{-5}$$

Cf. PDG: $\text{BR} = (4.09 \pm 0.10) \times 10^{-5}$



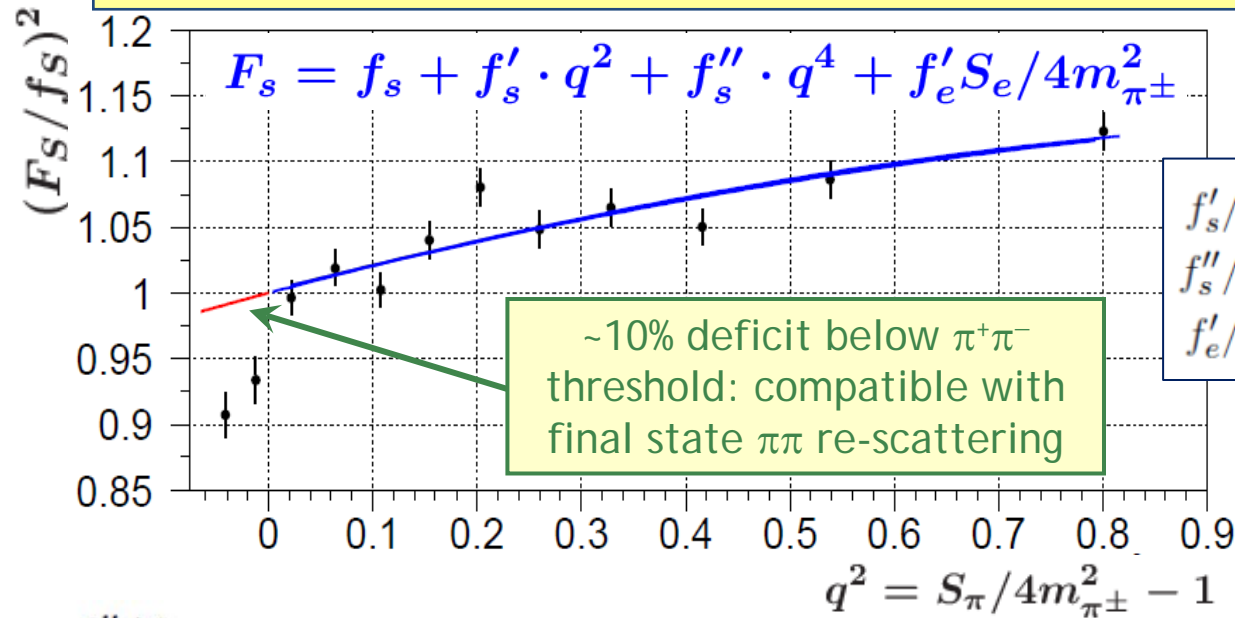
$\text{BR}(\text{K}^\pm \rightarrow \pi^+ \pi^- e^\pm \nu) = \tau_K (|V_{us}| f_s)^2 \times \mathfrak{F} \rightarrow$ absolute f_s measurement.

$$\begin{aligned} \text{Results: } |V_{us}| f_s &= 1.285 \pm 0.001_{\text{stat}} \pm 0.004_{\text{syst}} \pm 0.005_{\text{ext}} \\ f_s &= 5.705 \pm 0.003_{\text{stat}} \pm 0.017_{\text{syst}} \pm 0.031_{\text{ext}} \end{aligned}$$

NA48/2: $K^\pm \rightarrow \pi^0 \pi^0 e^\pm \nu$ form factor

66K candidates, 1.07% background ($K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$; accidentals)

Form-factor measurement above $2m(\pi^\pm)$ threshold



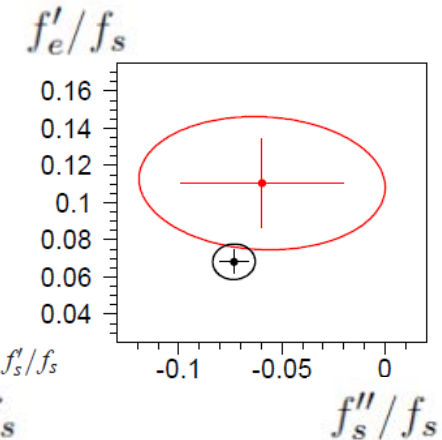
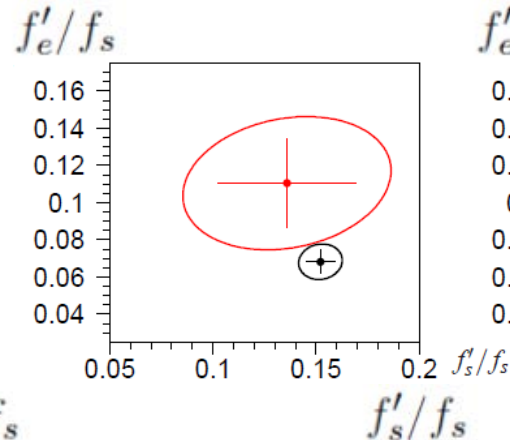
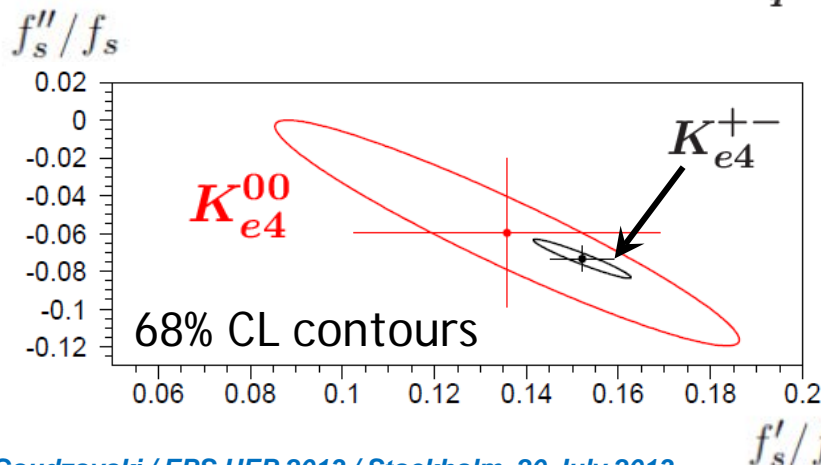
Preliminary results:

$$f'_s/f_s = 0.136 \pm 0.033_{stat} \pm 0.015_{syst}$$

$$f''_s/f_s = -0.060 \pm 0.039_{stat} \pm 0.015_{syst}$$

$$f'_e/f_s = 0.110 \pm 0.024_{stat} \pm 0.022_{syst}$$

Evidence for S_e -dependence of F_s



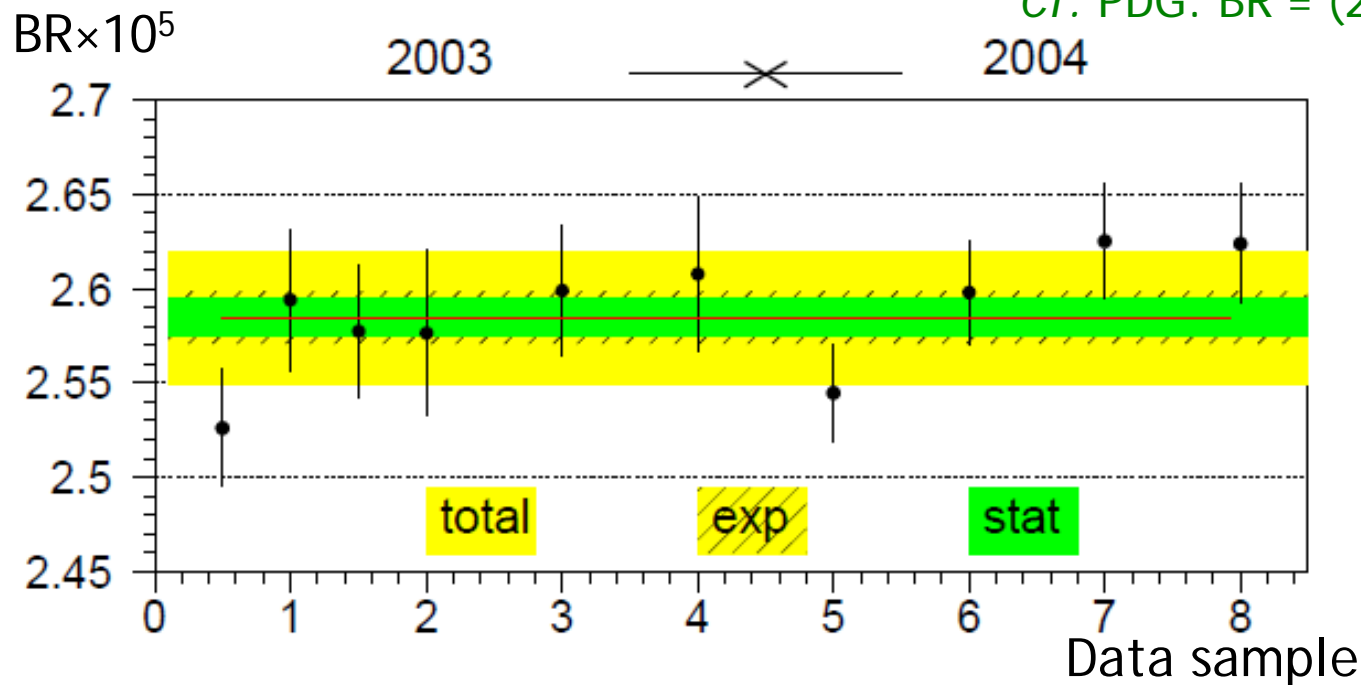
NA48/2: $\text{BR}(\text{K}^\pm \rightarrow \pi^0 \pi^0 e^\pm \nu)$ and f_s

BR measured with respect to normalisation mode: $\text{K}^\pm \rightarrow \pi^\pm \pi^0 \pi^0$.

Preliminary result:

$$\text{BR}(\text{K}^\pm \rightarrow \pi^0 \pi^0 e^\pm \nu) = (2.585 \pm 0.010_{\text{stat}} \pm 0.010_{\text{syst}} \pm 0.032_{\text{ext}}) \times 10^{-5}$$

Cf. PDG: $\text{BR} = (2.2 \pm 0.4) \times 10^{-5}$



$\text{BR}(\text{K}^\pm \rightarrow \pi^0 \pi^0 e^\pm \nu) = \tau_K (|V_{us}| f_s)^2 \times \mathfrak{F} \rightarrow$ absolute f_s measurement.

Results: $|V_{us}| f_s = 1.372 \pm 0.003_{\text{stat}} \pm 0.004_{\text{syst}} \pm 0.008_{\text{ext}}$
 $f_s = 6.092 \pm 0.012_{\text{stat}} \pm 0.017_{\text{syst}} \pm 0.045_{\text{ext}}$

New precision inputs to low energy QCD

- ❖ Rare decay $K^\pm \rightarrow \pi^\pm \gamma \gamma$ with NA48/2 and NA62 minimum bias samples:
 - ✓ a new result: model-independent $BR(z > 0.2)$;
 - ✓ data agree with ChPT description (dominated by pion loop);
 - ✓ final results and publications are **in preparation**.
- ❖ $K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu$ decay with main NA48/2 sample (**complete**):
 - ✓ precision measurements of form factors, pion scattering lengths and BR.
- ❖ $K^\pm \rightarrow \pi^0 \pi^0 e^\pm \nu$ decay with main NA48/2 sample (**work in progress**):
 - ✓ preliminary measurements of the form factor and BR;
 - ✓ cusp-like structure due to final state re-scattering observed in S_π spectrum.