AdS/CFT and applications

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Outline

Why use AdS/CFT?

The AdS/CFT description of a plasma system

A heavy-ion collision

Five AdS/CFT studies

Summary

- ▶ New ways of looking at nonperturbative gauge theory physics...
- ▶ Intricate links with General Relativity...
- ► Has been extended to many other cases

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Many other applications...

c.f. plenary talk by Zvi Berr

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- Deconfined phase
- Strongly coupled
- ▶ No supersymmetry!

Differences

- No running coupling → Even at very high energy densities the coupling remains strong
- (Exactly) conformal equation of state \longrightarrow Perhaps not so bad around $T \sim 1.5 2.5 T_c$
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- ▶ Use it as a theoretical laboratory where we may compute from 'first principles' nonequilibrium nonperturbative dynamics
- ► Gain qualitative insight into the physics which is very difficult to access using other methods
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Describe it in terms of lightest degrees of freedom on the AdS side which are relevant at strong coupling

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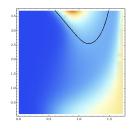
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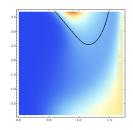
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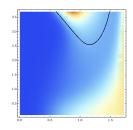
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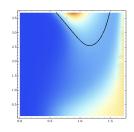
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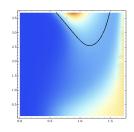
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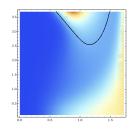
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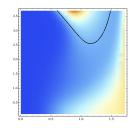
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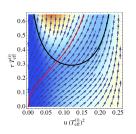
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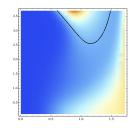
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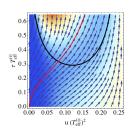




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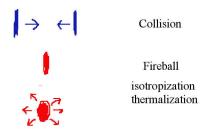


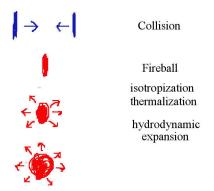
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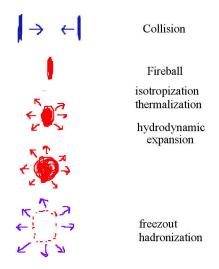
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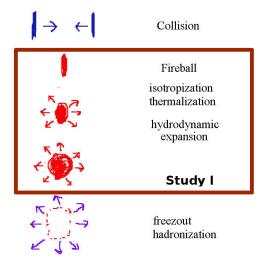


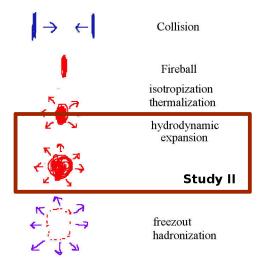


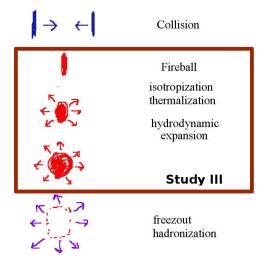


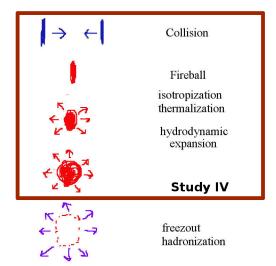


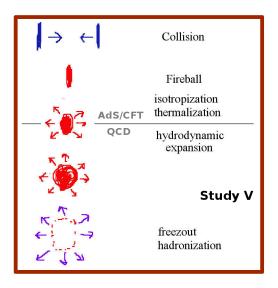












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Understand the features of the farfrom equilibrium stage of the dynamics of the strongly coupled plasma system

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M. Heller, RJ, P. Witaszczyk, 1103.3452 [PRL 108, 201602 (2012) (physics)

M. Heller, RJ, P. Witaszczyk, 1203.0755 [PRD 85, 126002 (2012)] (technical details)

Bjorken '83

Assume a flow that is invariant under longitudinal boosts and does not depend on the transverse coordinates.

- 1. When does hydrodynamics become applicable?
- **2.** Is $T_{\mu\nu}$ there approximately isotropic?
- **3.** What characterization of the initial state determines its transition to hydrodynamics?

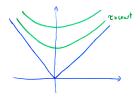
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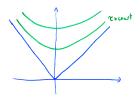
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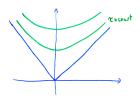
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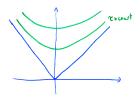
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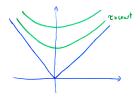
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- 1. As a measure of energy density introduce the effective temperature (≡ temperature of a thermal system with the same energy density)
- **2.** Form the dimensionless product $w \equiv T_{eff} \cdot \tau$
- 3. For all initial conditions considered, *viscous* hydrodynamics works very well for $w \equiv T_{eff} \cdot \tau > 0.7$

(natural values for RHIC: ($\tau_0 = 0.25 \, fm, T_0 = 500 \, MeV$) assumed in [Broniowski, Chojnacki, Florkowski, Kisiel] correspond to w = 0.63)

4. The plasma system is described by viscous hydrodynamics even though it is not in true thermal equilibrium — there is still a sizable pressure anisotropy

$$\Delta p_L \equiv 1 - \frac{p_L}{\varepsilon/3} \sim 0.7$$

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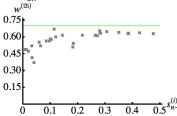
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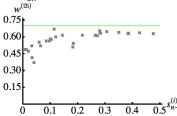
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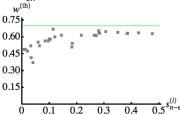
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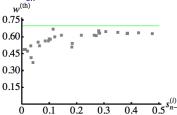
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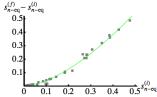


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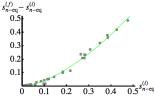
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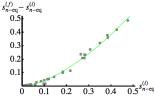
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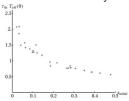


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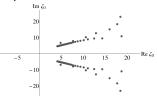
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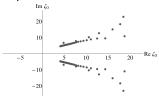


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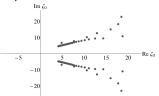


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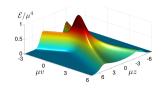
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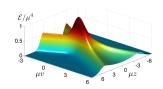
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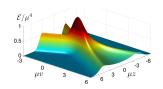
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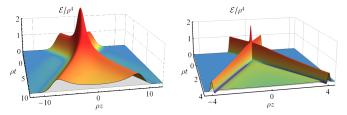
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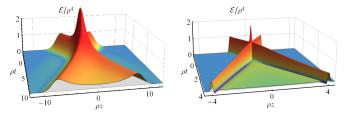
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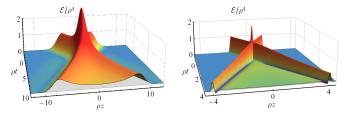
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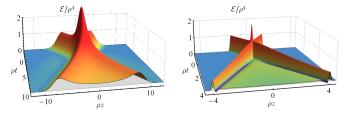
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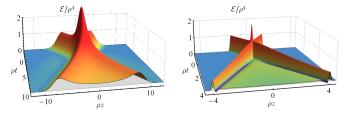
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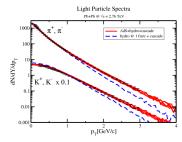
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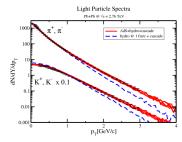
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