

Theories of Extra Dimensions

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March 2013

Motivation

- SM hierarchy problem: $M_{EW} \ll M_{Pl}$
- SM flavor problem: $m_e \ll m_t$
- Explained by new dynamics?
 - **Extra dimensions** (Warped (AdS), Flat)
 - Supersymmetry
 - Strong dynamics
 - Little Higgs



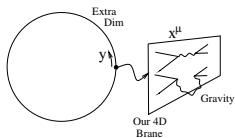
Talk Outline

- Aspects of Extra Dimensional Theories
 - Large Extra Dimensions (LED) (aka ADD)
 - Universal Extra Dimensions (UED)
 - Warped Extra Dimensions (WED) - **Main Focus**
- Kaluza-Klein (KK) expansion
- LHC Signatures



Large Extra Dimensions (LED, ADD)

- Usual picture
 - 3 space + 1 time Gravity scale $M_{pl} \sim 10^{19}$ GeV
- Large Extra Dimensions [Arkani-Hamed, Dimopoulos, Dvali (ADD)]
 - n (compact) space extra dims Radius R
 - Only fundamental scale $M_* \sim 10^3$ GeV
 - $M_{pl}^2 = M_*^{2+n} V_n$ $V_n \sim R^n$
 - Gravity in bulk, SM on brane
 - $S = \int d^4x d^n y \left[\mathcal{L}_{Bulk} + \delta(\underline{y}) \mathcal{L}_{Brane} \right]$



Universal Extra Dimensions (UED)

[Appelquist, Cheng, Dobrescu] [Cheng, Matchev, Schmaltz] [Datta, Kong, Matchev]

All SM fields propagate in Extra Dimension(s)

- No solution to the hierarchy problem
- KK number conserved
- Orbifolding implies KK parity conservation
 - Relaxed constraints since no tree level contribution to EW precision obs
 - $M_{KK} \gtrsim 400 \text{ GeV}$
- LKP stable!
 - Dark Matter
 - Missing energy at Colliders

[Servant, Tait]



Warped Extra Dimensions (WED, RS)

SM in background 5D warped AdS space

[Randall, Sundrum 99]

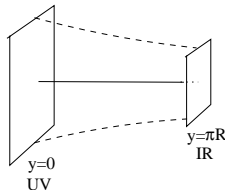
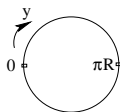
$$ds^2 = e^{-2k|y|}(\eta_{\mu\nu} dx^\mu dx^\nu) + dy^2$$

Z_2 orbifold fixed points:

- Planck (UV) Brane
- TeV (IR) Brane

R : radius of Ex. Dim.

k : AdS curvature scale ($k \lesssim M_{pl}$)



Hierarchy prob soln:

- IR localized Higgs : $M_{EW} \sim ke^{-k\pi R}$: Choose $k\pi R \sim 34$
 - CFT dual is a composite Higgs model

AdS/CFT Correspondence

AdS/CFT Correspondence

[Maldacena, 1997]

- A classical supergravity theory in $AdS_5 \times S_5$ at weak coupling is **dual** to a 4D large-N CFT at strong coupling
- The CFT is at the boundary of AdS [Witten 1998; Gubser, Klebanov, Polyakov 1998]

$$Z_{CFT}[\phi_0] = e^{-\Gamma_{AdS}[\phi_0]}$$

$\mathcal{L} \supset \int d^4x \mathcal{O}_{CFT}(x) \phi_0(x)$ Eg: $\langle \mathcal{O}(x_1) \mathcal{O}(x_2) \rangle = \frac{\delta^2 Z_{CFT}[\phi_0]}{\delta \phi_0(x_1) \delta(x_2)}$ with Z_{CFT} given by the RHS	$\Gamma_{AdS}[\phi]$ supergravity eff. action $\phi(y, x)$ is a solution of the EOM ($\delta\Gamma = 0$) for given bndry value $\phi_0(x) = \phi(y = y_0, x)$
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4D Duals of Warped Models

[Arkani-Hamed, Porrati, Randall, 2000; Rattazzi, Zaffaroni, 2001]

- Dual of Randall-Sundrum model **RS1 (SM on IR Brane)**
 - Planck brane \implies UV Cutoff; Dynamical gravity in the 4D CFT
 - TeV (IR) brane \implies IR Cutoff; Conformal invariance broken below a TeV
 - All SM fields are composites of the CFT
- Dual of Warped Models with **Bulk SM**
 - UV localized fields are elementary
 - IR localized fields (Higgs) are composite
 - 4D dual is Composite Higgs model [Georgi, Kaplan 1984]
 - Shares many features with Walking Extended Technicolor
 - Partial Compositeness
 - AdS dual is weakly coupled and hence calculable!
 - KK states are dual to composite resonances



Eg: 5-Dimensional Theory

Bulk fields $\Phi(x, y) = \{A_M, \phi, \Psi, \dots\}$

$$S^{(5)} = \int d^4x dy \mathcal{L}^{(5)} \quad ; \quad \mathcal{L}^{(5)} \supset \sqrt{|g|} M_*^3 \mathcal{R} + \mathcal{L}_A^{(5)} + \mathcal{L}_\Psi^{(5)} + \mathcal{L}_\phi^{(5)} + \mathcal{L}_{int}^{(5)}$$

$$\mathcal{L}_\Psi^{(5)} \supset \sqrt{|g|} \left\{ \bar{\Psi} i \Gamma^M \partial_M \Psi + c_\psi k \bar{\Psi} \Psi \right\}$$

$$\mathcal{L}_\phi^{(5)} \supset \sqrt{|g|} \left\{ \partial^M \phi^\dagger \partial_M \phi + m_\phi^2 \phi^\dagger \phi \right\};$$

$$\mathcal{L}_A^{(5)} \supset \sqrt{|g|} \left\{ -\frac{1}{4} F^{MN} F_{MN} \right\}$$

$$\mathcal{L}_{int}^{(5)} \supset \sqrt{|g|} \left\{ g_5 \bar{\Psi} \Gamma^M \Psi A_M + (\lambda_5 \phi \bar{\Psi}_L \Psi_R + h.c.) - \mathcal{V}(\phi^\dagger \phi) \right\}$$



Kaluza-Klein (KK) expansion

$\delta\mathcal{S}^{(5)} = 0 \implies$ Euler-Lagrange Equations of Motion (EOM)

- $\frac{\delta\mathcal{L}^{(5)}}{\delta\Phi} = \partial_M \frac{\delta\mathcal{L}^{(5)}}{\delta\partial_M\Phi}$

KK expansion: $\Phi(x, y) = \sum_{n=0}^{\infty} f_{(n)}^{\phi}(y) \phi^{(n)}(x)$ with $\int dy f_{(n)}^{\phi}(y) f_{(m)}^{\phi}(y) = \delta_{nm}$

Plug into EOM, y dependent piece is (for WED) [Gherghetta, Pomarol, 2000]

$$\left[-e^{sk|y|} \partial_5 (e^{-sk|y|} \partial_5) + \hat{M}_{\Phi}^2 \right] f_{(n)}(y) = e^{2k|y|} m_n^2 f_n(y)$$

$$s = \{2, 4, 1\}; \quad \hat{M}_{\Phi}^2 = \{0, ak^2, c(c \pm 1)k^2\}$$

The solution is

$$f_{(n)}(y) = \frac{1}{N_n} e^{sk|y|/2} \left[J_{\alpha} \left(\frac{m_n}{k} e^{k|y|} \right) + b_{\alpha} Y_{\alpha} \left(\frac{m_n}{k} e^{k|y|} \right) \right]$$



Equivalent 4D theory

Plug KK expansion into $\mathcal{S}^{(5)}$ & integrate over $y \rightarrow$ *equivalent 4D theory*

$$\mathcal{S}^{(4)} = \sum \int d^4x \, m_n^2 \phi^{(n)} \phi^{(n)} + g_{4D}^{(nml)} \psi^{(n)} \psi^{(m)} A^{(l)} + \lambda_{4D}^{(nm)} \psi_L^{(n)} \psi_R^{(m)} H$$

$\phi^{(n)} \rightarrow$ KK tower with mass m_n ; Denote $\phi^{(1)} \equiv \phi'$; $m_1 \equiv m_{KK} \sim \text{TeV}$

Some 4D couplings

- Yukawas: $\lambda_{4D}^{(00)} = \lambda_{5D} \int dy f_0^{\psi L} f_0^{\psi R} f^H$
- Gauge couplings: $g_{4D}^{(001)} = g_{5D} \int dy f_0^{\psi} f_0^{\psi} f_1^A$



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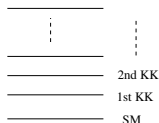
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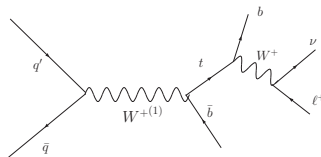
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In summary

- 5D (compact) field \leftrightarrow "Infinite" tower of 4D fields
- Look for this tower at the LHC

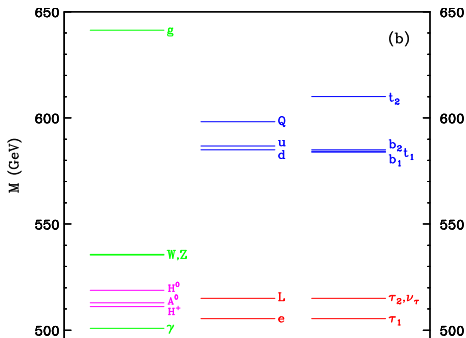


Example:



UED Spectrum

- All KK states degenerate at leading order
 - Loop corrections split this



[Cheng, Matchev, Schmaltz]

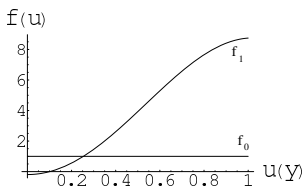
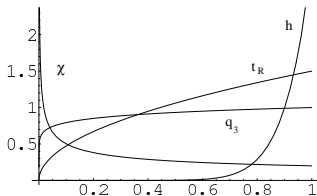
LHC SUSY ↔ UED confusion!

Explaining SM (gauge & mass) hierarchies (WED)

Bulk Fermions explain SM mass hierarchy [Gherghetta, Pomarol 00][Grossman, Neubert 00]

$$S^{(5)} \supset \int d^4x dy \left\{ c_\psi k \bar{\Psi}(x, y) \Psi(x, y) \right\}$$

Fermion bulk mass (c_ψ parameter) controls $f^\psi(y)$ localization



RS-GIM keeps FCNC under control



4-D KK couplings in WED

$$\xi \equiv \sqrt{k\pi R} \approx 5$$

Compare to SM couplings:

- ξ enhanced: $t_R t_R A'$, hhA' , $\phi\phi A'$
- $1/\xi$ suppressed: $\psi_{light} \psi_{light} A'_{++}$
- SM strength: $t_L t_L A'$

(Equivalence Theorem $\Rightarrow \phi \leftrightarrow A_L$)

Note: $\psi_{light} \psi_{light} A'_{-+} = 0$



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Effective coupling (Eg: Z'):

$$\mathcal{L}^{4D} \supset \bar{\psi}_{L,R} \gamma^\mu \left[eQ I A_{1\mu} + g_Z \left(T_L^3 - s_W^2 T_Q \right) I Z_{1\mu} + g_{Z'} \left(T_R^3 - s'^2 T_Y \right) I Z_{X1\mu} \right] \psi_{L,R}$$



Challenge I : Precision EW Constraints in WED



Precision Electroweak Constraints (S, T, $Zb\bar{b}$)

- Bulk gauge symm - $SU(2)_L \times U(1)$ (SM ψ , H on TeV Brane)
 - T parameter $\sim (\frac{v}{M_{KK}})^2 (k\pi R)$ [Csaki, Erlich, Terning 02]
 - S parameter also ($k\pi R$) enhanced

- AdS bulk gauge symm $SU(2)_R \Leftrightarrow$ CFT Custodial Symm [Agashe, Delgado, May, Sundrum 03]
 - T parameter - Protected
 - S parameter - $\frac{1}{k\pi R}$ for light bulk fermions
 - Problem: $Zb\bar{b}$ shifted

- 3rd gen quarks (2,2) [Agashe, Contino, DaRold, Pomarol 06]
 - $Zb\bar{b}$ coupling - Protected
 - Precision EW constraints $\Rightarrow M_{KK} \gtrsim 2 - 3$ TeV

[Carena, Ponton, Santiago, Wagner 06,07] [Bouchart, Moreau-08] [Djouadi, Moreau, Richard 06]



WED Bulk Gauge Group

[Agashe, Delgado, May, Sundrum 03]

Bulk gauge group : $SU(3)_{QCD} \otimes SU(2)_L \otimes SU(2)_R \otimes U(1)_X$

- 8 gluons
- 3 neutral EW (W_L^3, W_R^3, X)
- 2 charged EW (W_L^\pm, W_R^\pm)



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Gauge Symmetry breaking:

- By Boundary Condition (BC):
 - $SU(2)_R \times U(1)_X \rightarrow U(1)_Y$
- By VEV of TeV brane Higgs
 - $SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$

$$A_{-+}(x, y) \text{ BC: } A|_{y=0} = 0; \quad \partial_y A|_{y=\pi R} = 0$$

$$\text{Higgs } \Sigma = (2, 2)$$



Fermion representation : $Zb\bar{b}$ not protected

[Agashe, Delgado, May, Sundrum '03]

- Complete $SU(2)_R$ multiplet : Doublet t_R (DT) model

- $Q_L \equiv (\mathbf{2}, \mathbf{1})_{1/6} = (t_L, b_L)$

- $\psi_{t_R} \equiv (\mathbf{1}, \mathbf{2})_{1/6} = (t_R, b')$

- $\psi_{b_R} \equiv (\mathbf{1}, \mathbf{2})_{1/6} = (T, b_R)$

- "Project-out" b' , T zero-modes by $(-, +)$ B.C.

- New $\psi_{VL} : b', T$

- $b \leftrightarrow b'$ mixing

- $Zb\bar{b}$ coupling shifted

- So LEP constraint quite severe



Fermion representation : $Zb\bar{b}$ protected

- $Q_L = (2, 2)_{2/3} = \begin{pmatrix} t_L & \chi \\ b_L & T \end{pmatrix}$ [Agashe, Contino, DaRold, Pomarol '06]
- $Zb_L\bar{b}_L$ protected by custodial $SU(2)_{L+R} \otimes P_{LR}$ invariance
 $Wt_L b_L, Zt_L t_L$ not protected, so shifts



Fermion representation : $Zb\bar{b}$ protected

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Two t_R possibilities:

① Singlet t_R (ST) : $(1, 1)_{2/3} = t_R$ New $\psi_{VL} : \chi, T$

② Triplet t_R (TT) :

$$(1, 3)_{2/3} \oplus (3, 1)_{2/3} = \psi'_{tR} \oplus \psi''_{tR} = \begin{pmatrix} \frac{t_R}{\sqrt{2}} & \chi' \\ -\frac{t_R}{\sqrt{2}} & b' \end{pmatrix} \oplus \begin{pmatrix} \frac{t''}{\sqrt{2}} & \chi'' \\ b'' & -\frac{t''}{\sqrt{2}} \end{pmatrix}$$

New $\psi_{VL} : \chi, T, \chi', b', \chi'', t'', b''$



Flavor structure

[Agashe, Perez, Soni, 04]

$$\mathcal{L} \supset \bar{\Psi}^i i \Gamma^\mu D_\mu \Psi^i + M_{ij} \bar{\Psi}^i \Psi^j + y_{ij}^{5D} H \bar{\Psi}^i \Psi^j + h.c.$$

- Basis choice: M_{ij} diagonal $\equiv M_i$
 - All flavor violation from y_{ij}^{5D}
 - KK decompose and go to mass basis
 - $\implies g \bar{\Psi}_{(n)}^i W_\mu^{(k)} \Psi_{(m)}^j$ off-diagonal in flavor
(due to non-degenerate f^i i.e. M^i)
- 5D fermion Ψ is vector-like
 - M_{ij} is independent of $\langle H \rangle = v$
 - But zero-mode made chiral (SM)



FCNC couplings

- $h_{(0)}^{\mu\nu} \psi_{(0)} \psi_{(0)}$: diagonal
- $\{A_{(0)}, g_{(0)}\} \psi_{(0)} \psi_{(0)}$: diagonal (unbroken gauge symmetry)
- $\{Z_{(0)}, Z_{X(0)}\} \psi_{(0)} \psi_{(0)}$: almost diagonal (non-diagonal due to EWSB effect)
- $h \psi_{(0)} \psi_{(0)}$: diagonal (only source of mass is $\langle h \rangle = v$)

-
- $h_{(1)}^{\mu\nu} \psi_{(0)} \psi_{(0)}$: off-diagonal
 - $\{A_{(1)}, g_{(1)}\} \psi_{(0)} \psi_{(0)}$: off-diagonal (i=1,2 almost diagonal)
 - $\{Z_{(1)}, Z_{X(1)}\} \psi_{(0)} \psi_{(0)}$: off-diagonal

-
- $h_{(0)}^{\mu\nu} \psi_{(0)} \psi_{(1)}$: 0
 - $\{A_{(0)}, g_{(0)}\} \psi_{(0)} \psi_{(1)}$: 0 (unbroken gauge symmetry)
 - $\{Z_{(0)}, Z_{X(0)}\} \psi_{(0)} \psi_{(1)}$: off-diagonal (EWSB effect)
 - $h \psi_{(0)} \psi_{(1)}$: off-diagonal (since M_ψ is extra source of mass)

$\psi_{(0)} \leftrightarrow \psi_{(1)}$ mixing due to EWSB



FCCC couplings

- $W_{L(0)}^\pm \psi_{(0)}^i \psi_{(0)}^j : g V_{CKM}^{ij}$
- $\{W_{L(1)}^\pm, W_{R(1)}^\pm\} \psi_{(0)} \psi_{(0)} : g V_{100} [f_{W(1)} f_\psi f_\psi]$
 - [...] suppressed for $i = 1, 2$; (Not suppr for b_L, t_L, t_R)
- $W_{L(0)}^\pm \psi_{(0)} \psi_{(1)} : g V_{001} [f_{W(1)} f_\psi f_{\psi(1)}]$

Challenge II : Flavor Constraints in WED

- $K^0 \bar{K}^0$ mixing:

- Tree-level FCNC vertex $g_{(1)} d s \propto V_L^{d\dagger} \begin{pmatrix} [g_{(1)} d d] & 0 \\ 0 & [g_{(1)} s s] \end{pmatrix} V_L^d$

- $b \rightarrow s \gamma$:

- No tree-level contribution to helicity flip dipole operator
 - So 1-loop with $g_{(1)} b s_{(1)}$ OR $\phi^\pm b s_{(1)}$

- $b \rightarrow s \ell^+ \ell^-$, $b \rightarrow s s \bar{s}$, $K \rightarrow \pi \nu \bar{\nu}$:

- Tree level FCNC vertex $Z s d$

Bound : $m_{KK} \gtrsim \text{few TeV}$

[Agashe et al][Buras et al][Neubert et al][Csaki et al]

Relaxed with flavor alignment : MFV, NMFV, flavor symmetries, ...

[Fitzpatrick et al][Agashe et al]

[SG, A.Iyer, S.Vempati Ongoing]



LHC Phenomenology

LED KK Graviton @ LHC

Look for KK Gravitons ($h_{\mu\nu}^{(n)}$) : Missing energy (MET)

[Giudice, Rattazzi, Wells 1998][Hewett 1998] [Han, Lykken, Zhang 1998]

- Small KK spacing : sum over huge number of states
 - Cutoff dependence
- Final state Gravitons : $pp \rightarrow \gamma h^{(n)}, j G^{(n)}$
- Virtual Gravitons : $pp \rightarrow h^{(n)} \rightarrow \ell^+ \ell^-, \dots$



LED LHC Limit $pp \rightarrow h_{\mu\nu}^{(n)} \rightarrow \ell^+ \ell^-$

TABLE VIII. Observed 95% C.L. lower limits on M_S (in units of TeV), including systematic uncertainties, for ADD signal in the GRW, Hewett and HLZ formalisms with K factors of 1.6 and 1.7 applied to the signal for the dilepton and diphoton channels, respectively. Separate results are provided for the different choices of flat priors: $1/M_S^4$ and $1/M_S^8$.

Channel	Prior	GRW	Hewett	HLZ				
				$n=3$	$n=4$	$n=5$	$n=6$	$n=7$
ee	$1/M_S^4$	2.95	2.63	3.51	2.95	2.66	2.48	2.34
	$1/M_S^8$	2.82	2.67	3.08	2.82	2.68	2.59	2.52
$\mu\mu$	$1/M_S^4$	3.07	2.74	3.65	3.07	2.77	2.58	2.44
	$1/M_S^8$	2.82	2.67	3.08	2.82	2.68	2.59	2.52
$ee + \mu\mu$	$1/M_S^4$	3.27	2.92	3.88	3.27	2.95	2.75	2.60
	$1/M_S^8$	3.09	2.92	3.37	3.09	2.94	2.84	2.76
$ee + \mu\mu + \gamma\gamma$	$1/M_S^4$	3.51	3.14	4.18	3.51	3.17	2.95	2.79
	$1/M_S^8$	3.39	3.20	3.69	3.39	3.22	3.11	3.02

ATLAS : 1211.1150 : 7TeV, 5 fb^{-1}

WED KK Graviton

[Agashe et al, 07] [Fitzpatrick et al, 07]

$$m_n = x_n k e^{-k\pi r} \quad x_n = 3.83, 7.02, \dots$$

$$\mathcal{L} \supset -\frac{C^{ffG}}{\Lambda} T^{\alpha\beta} h_{\alpha\beta}^{(n)} \quad \Lambda = \bar{M}_P e^{-k\pi r}$$

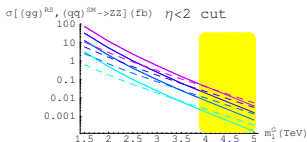
- SM on IR brane

- CDF & D0 bounds : $m_1 > 300 - 900$ GeV for $\frac{k}{M_p} = 0.01-0.1$
- ATLAS & CMS reach : 3.5 TeV with $100 fb^{-1}$

$$gg \rightarrow h^{(1)} \rightarrow ZZ \rightarrow 4\ell$$

- SM in Bulk (flavor)

- light fermion couplings highly suppressed
- gauge field couplings $\frac{1}{k\pi r}$ suppressed
- Decays dominantly to t, h, V_{Long}



various $\frac{k}{M_p}$; SM dashed

[Agashe, Davoudiasl, Perez, Soni, 2007]



KK Gluon

[Agashe et al, 06] [Lillie et al, 07]

$$m_n = x_n k e^{-k\pi r} \quad x_n \approx 2.45, 5.57, \dots \quad \text{Width } \Gamma \approx \frac{M}{6}$$

$g^{(1)} t\bar{t}$: parity violating couplings!

$$\text{LHC: } q\bar{q} \rightarrow g^{(1)} \rightarrow t\bar{t}$$



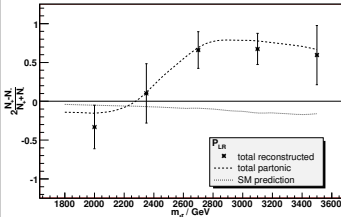
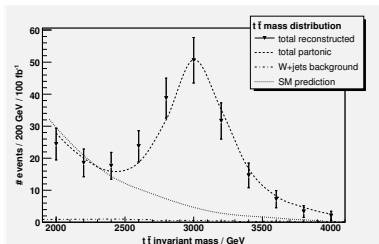
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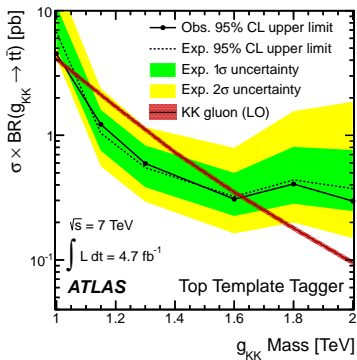
$$\text{LHC: } q\bar{q} \rightarrow g^{(1)} \rightarrow t\bar{t}$$



$$P_{LR} = 2 \frac{N_+ - N_-}{N_+ + N_-} \quad N_+ \text{ forward going } \ell \text{ wrt } k_t$$

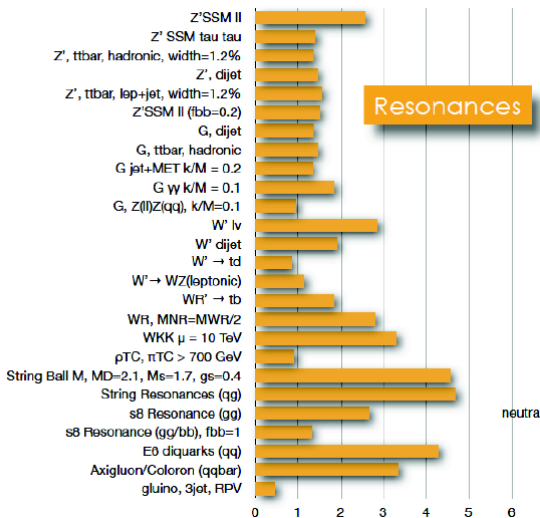
LHC reach: About 4 TeV with 100 fb⁻¹

LHC KK-gluon search



ATLAS JHEP01(2013) 116 : Limit (7 TeV, 4.7 fb^{-1}): $M_{KK} > 1.6 \text{ TeV} @ 95\% \text{ CL}$

CMS Resonances Limits (Moriond 2013)



ATLAS Extra Dimensions Limits (Moriond 2013)

ATLAS Exotics Searches* - 95% CL Lower Limits (Status: HCP 2012)

Large ED (ADD) : microjet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}$, 7 TeV [1210.4491]	4.37 TeV	$M_D (\delta=2)$
Large ED (ADD) : monophoton + $E_{T,miss}$	$L=4.6 \text{ fb}^{-1}$, 7 TeV [1209.4525]	1.93 TeV	$M_D (\delta=2)$
Large ED (ADD) : diphoton & dilepton, $m_{\gamma\gamma}$	$L=4.7 \text{ fb}^{-1}$, 7 TeV [1211.1190]	4.10 TeV	M_S (HLZ $\delta=3$, NLO)
UED : diphoton + $E_{T,miss}$	$L=4.8 \text{ fb}^{-1}$, 7 TeV [ATLAS-CONF-2012-072]	1.41 TeV	Compact scale R^{-1}
S^1/Z_2 ED : dilepton, m_{ll}	$L=4.9-5.3 \text{ fb}^{-1}$, 7 TeV [1209.2535]	4.71 TeV	$M_{KK} \sim R^{-1}$
RS1 : diphoton & dilepton, $m_{\gamma\gamma}$	$L=4.7-5.3 \text{ fb}^{-1}$, 7 TeV [1210.5359]	2.23 TeV	Graviton mass ($k/M_{Pl} = 0.1$)
RS1 : ZZ resonance, m_{ll}	$L=1.0 \text{ fb}^{-1}$, 7 TeV [1203.0718]	345 GeV	Graviton mass ($k/M_{Pl} = 0.1$)
RS1 : WW resonance, $m_{\gamma\gamma}$	$L=4.7 \text{ fb}^{-1}$, 7 TeV [1208.2583]	1.23 TeV	Graviton mass ($k/M_{Pl} = 0.1$)
$S^1 g_{KK} \rightarrow tt$ (BR=0.925) : $tt \rightarrow l+jets$, m_{jj}	$L=4.7 \text{ fb}^{-1}$, 7 TeV [ATLAS-CONF-2012-136]	1.9 TeV	g_{KK} mass
ADD BH ($M_{Pl}/M_D=3$) : SS dimuon, $N_{col,part}$	$L=1.3 \text{ fb}^{-1}$, 7 TeV [1111.0686]	1.25 TeV	$M_D (\delta=6)$
ADD BH ($M_{Pl}/M_D=3$) : leptons + jets, $2p_T$	$L=1.0 \text{ fb}^{-1}$, 7 TeV [1204.4545]	1.5 TeV	$M_D (\delta=6)$
Quantum black hole : dijet, $F(m_{jj})$	$L=4.7 \text{ fb}^{-1}$, 7 TeV [1210.1715]	4.11 TeV	$M_D (\delta=6)$

ATLAS
Preliminary

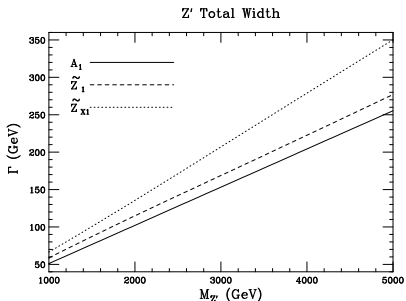
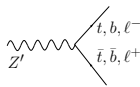
$$\int L dt = (1.0 - 13.0) \text{ fb}^{-1}$$

$$\sqrt{s} = 7, 8 \text{ TeV}$$



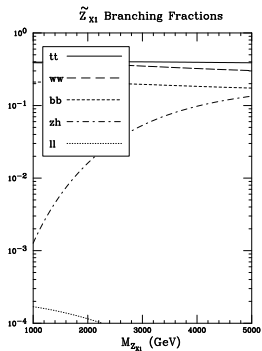
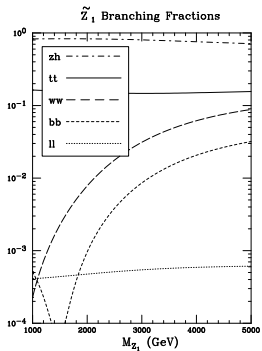
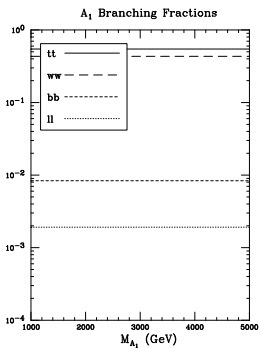
Z' decays in WED

[Agashe, Davoudiasl, SG, Han, Huang, Perez, Si, Soni - arXiv:0709.0007 [hep-ph]]

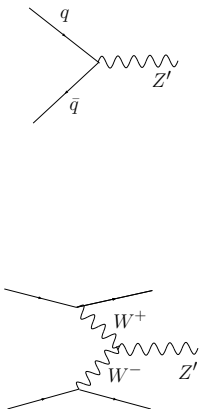


$M_{Z'} = 2\text{TeV}$	A_1	Z_1	Z_{X1}
Γ (GeV)	103.3	114.6	135.6

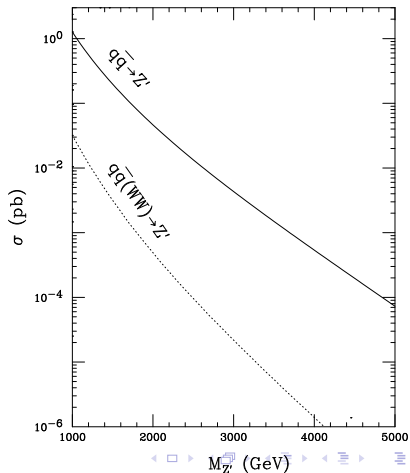
Z' Branching Ratios in WED



WED Z' production at the LHC



Total Z' Cross Section at LHC



WED Z' channels summary

($\mathcal{L}_{2\text{ TeV}}$; $\mathcal{L}_{3\text{ TeV}}$) in fb^{-1}

- $pp \rightarrow Z' \rightarrow W^+ W^-$
 - Fully leptonic : $W \rightarrow \ell\nu$; $W \rightarrow \ell\nu$ $\mathcal{L} : (100; 1000) \text{ fb}^{-1}$
 - Semi leptonic : $W \rightarrow \ell\nu$; $W \rightarrow (jj)$ $\mathcal{L} : (100; 1000) \text{ fb}^{-1}$

- $pp \rightarrow Z' \rightarrow Z h$
 - $m_h = 120\text{GeV}$: $Z \rightarrow \ell^+\ell^-$; $h \rightarrow b\bar{b}$ $\mathcal{L} : (200; 1000) \text{ fb}^{-1}$
 - $m_h = 150\text{GeV}$: $Z \rightarrow (jj)$; $h \rightarrow W^+ W^- \rightarrow (jj) \ell\nu$ $\mathcal{L} : (75; 300) \text{ fb}^{-1}$

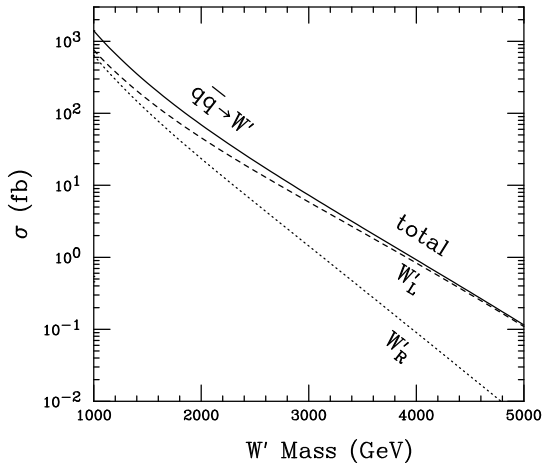
- $pp \rightarrow Z' \rightarrow \ell^+\ell^-$ $\mathcal{L} : (1000; -) \text{ fb}^{-1}$
 - $BR_{\ell\ell} \sim 10^{-3}$ Tiny!

- $pp \rightarrow Z' \rightarrow t\bar{t}, b\bar{b}$
 - KK gluon “pollution” [Djouadi, Moreau, Singh 07]



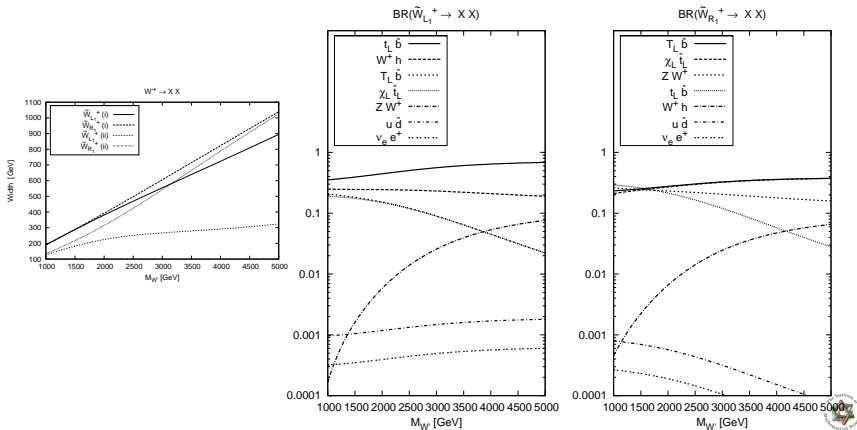
W' cross section

[Agashe, SG, Han, Huang, Soni, 08: arXiv:0810.1497]

Total W' Cross Section at LHC

W' @ LHC

W'^{\pm} Width and BR



W'[±] Channels summary

($\mathcal{L}_{2\text{TeV}}$; $\mathcal{L}_{3\text{TeV}}$) in fb^{-1}

- $W'^{\pm} \rightarrow t b$:
 - Leptonic $\mathcal{L} : (100; 1000) \text{ fb}^{-1}$
 - $t \bar{t}$ becomes (reducible) bkgnd since collimated t can fake a b-jet
Jet-mass cut : cone size 1.0 and $0 < j_M < 75 \Rightarrow 0.4\%$ of $t\text{ops}$ fake b
- $W'^{\pm} \rightarrow Z W$:
 - Fully leptonic $\mathcal{L} : (100; 1000) \text{ fb}^{-1}$
 - Semi leptonic $\mathcal{L} : (300; -) \text{ fb}^{-1}$
- $W'^{\pm} \rightarrow W h$: $\mathcal{L} : (100; 300) \text{ fb}^{-1}$
 - $m_h \approx 120 : h \rightarrow b b$
 - What is b-tagging eff at large p_{T_b} ?
 - $m_h \approx 150 : h \rightarrow W W$
 - Use W jet-mass to reject light jet



Measuring W' Chirality in $(pp) u\bar{d} \rightarrow W'^+ \rightarrow t\bar{b} \rightarrow \ell^+ \nu b\bar{b}$ (WED)

A Model Independent Study

[SG, Han, Lewis, Si, Zhou, 2010: arXiv:1008.3508]

$$L \supset \bar{\psi}_u (g_L P_L + g_R P_R) \psi_d W'$$

- Can we measure $g_{L,R}^{ud}$, $g_{L,R}^{tb}$?
- Yes, encoded in **top polarization!**



Measuring W' Chirality in $(pp) u\bar{d} \rightarrow W'^+ \rightarrow t\bar{b} \rightarrow \ell^+ \nu b\bar{b}$ (WED)

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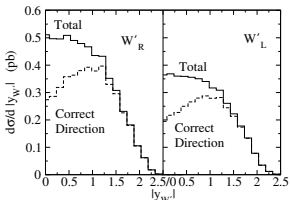
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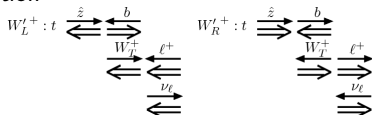
Need to fix u direction:

Statistical only: On avg u carries higher momentum fraction than \bar{d}



\therefore direction of $y_{W'} > 0.8$ is u direction

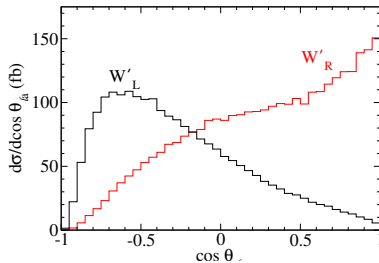
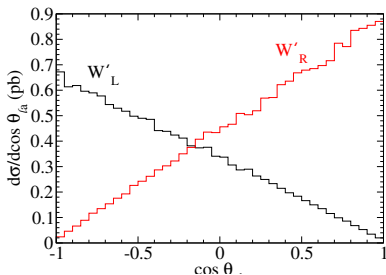
θ_ℓ distribution analyzes top polarization



Analyze in top rest frame



Measuring W' Chirality (Results)



WED KK Fermions @ LHC

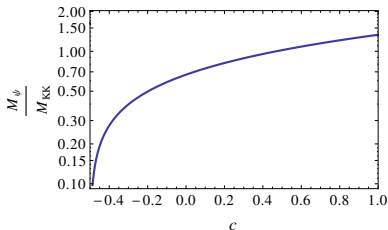
- SM fermions : $(+, +)$ BC \rightarrow zero-mode
- “Exotic” fermions : $(-, +)$ BC \rightarrow No zero-mode
 - 1^{st} KK vectorlike fermion

- Typical c_{tR}, c_{tL} : $(-, +)$ top-partners “light”

c : Fermion bulk mass parameter

[Choi, Kim, 2002] [Agashe, Delgado, May, Sundrum, 03]
[Agashe, Perez, Soni, 04] [Agashe, Servant 04]

- Look for it at the LHC



[Dennis et al, '07] [Carena et al, '07] [Contino, Servant, '08]
[Atre et al, '09, '11] [Aguilar-Saavedra, '09] [Mrazek, Wulzer, '09]

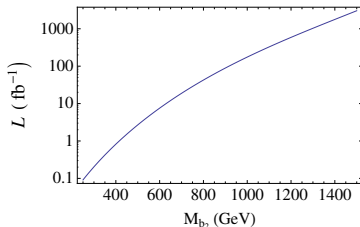
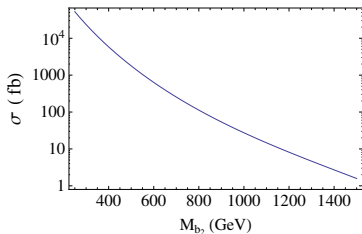
[SG, Moreau, Singh, '10] [SG, Mandal, Mitra, Tibrewala, '11] [SG, Mandal, Mitra, Moreau : Work In Progress]



b' Pair Production

[SG, T.Mandal, S.Mitra, R.Tibrewala, arXiv:1107.4306]

Pair Production : $pp \rightarrow b'\bar{b}' \rightarrow bZ\bar{b}Z \rightarrow bj\bar{j}b\bar{b}ll$



Cuts:
Rapidity: $-2.5 < y_{b,j,Z} < 2.5$,
Transverse momentum: $p_{T,b,j,Z} > 25$ GeV,
Invariant mass cuts:
 $M_Z - 10$ GeV $< M_{jj} < M_Z + 10$ GeV,
 $0.95M_{b_2} < M_{(bZ)} < 1.05M_{b_2}$.



KK states at the LHC

- $h_{\mu\nu}^{(1)}$ (KK Graviton)

$$gg \rightarrow h^{(1)} \rightarrow t\bar{t}$$

$L = 300 \text{ fb}^{-1}$ LHC reach is about 2 TeV

[Agashe, Davoudiasl, Perez, Soni 07]
[Fitzpatrick, Kaplan, Randall, Wang 07]

- $g_{\mu}^{(1)}$ (KK Gluon)

$$q\bar{q} \rightarrow g^{(1)} \rightarrow t\bar{t}$$

$L = 100 \text{ fb}^{-1}$ LHC reach is 4 TeV

[Agashe, Belyaev, Krupovnickas, Perez, Virzi 06]
[Lillie, Randall, Wang, 07] [Lillie, Shu, Tait 07]

- $Z_{\mu}^{(1)}, W_{\mu}^{(1)\pm}$ ($Z_{KK} \equiv Z'$, $W_{KK}^{\pm} \equiv W'$)

$$q\bar{q} \rightarrow Z', W' \rightarrow XX$$

[Agashe, Davoudiasl, SG, Han, Huang, Perez, Si, Soni 0709.0007 & 0810.1497]

- b', t', χ (KK Fermions)

[Agashe, Servant 04][Dennis et al 07][Contino, Servant 08][SG, Mandal, Mitra, Moreau ongoing]

- Radion



Little RS (LRS) ($Z' \rightarrow l^+ l^-$)

$$M_{EW} \sim k e^{-k\pi R} ; \text{ Vary } k, k\pi R ; (k\pi R)_{LRS} < (k\pi R)_{RS} = 35$$

- RS: $k \lesssim M_{pl}$
- **LRS:** $k \ll M_{pl}$; $k\pi R = 7 \implies k \approx 1000 \text{ TeV}$ [Davoudiasl, Perez, Soni 08]
- RS as a theory of flavor! (*give-up solution to hierarchy problem*)

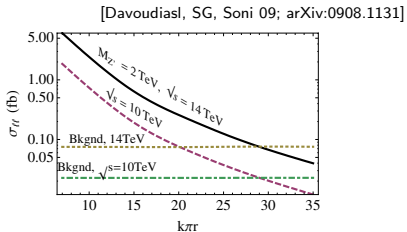
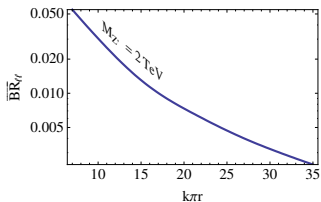


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$$pp \rightarrow Z'_{LRS} \rightarrow l^+l^-$$



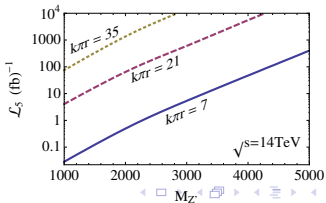
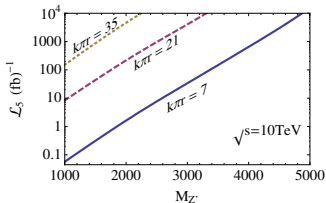
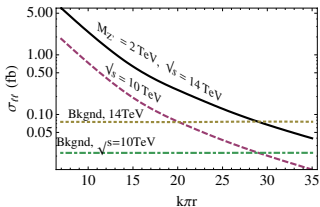
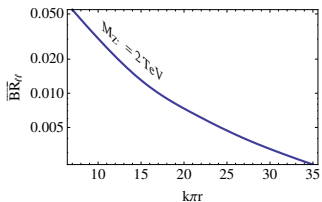
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$$pp \rightarrow Z'_{LRS} \rightarrow l^+ l^-$$

[Davoudiasl, SG, Soni 09; arXiv:0908.1131]



LED Bulk ν_R

[Dienes, Dudas, Gherghetta]
 [Davoudiasl, Langacker, Perelstein]
 [Cao, SG, Yuan 2003, 2004]

- Introduce Bulk ν_R propagating in δ dimensions

- $\Psi^\alpha(x^\mu, y) = \begin{pmatrix} \psi_L^\alpha(x^\mu, y) \\ \psi_R^\alpha(x^\mu, y) \end{pmatrix} \quad (\delta = 1) \quad \alpha \rightarrow \text{Generation}$

- $\mathcal{L}_{\text{Bulk}} \supset \bar{\Psi}^\alpha i \Gamma^M D_M \Psi^\alpha$

$$\mathcal{L}_{\text{Brane}} \supset \mathcal{L}_{\text{SM}} - \left(\frac{\Lambda_{\alpha\beta}^\nu}{\sqrt{M_*^\delta}} h \psi_R^\beta \nu_L^\alpha + h.c. \right)$$

- $\nu_L \rightarrow$ Usual SM left-handed neutrino
- $\psi_R \rightarrow$ Bulk right-handed neutrino $\equiv \nu_R$
- $\psi_L \rightarrow$ No direct coupling to SM



LED Bulk ν_R at colliders

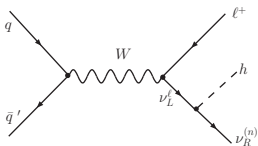
- ν_R couples only to ν_L and h (Yukawa)

$$\bullet \mathcal{L}^{(4)} \supset - \left[\frac{\bar{m}_\nu^{i\beta}}{v} \left(h \nu_R^i \nu_L^\beta + \sum_{\hat{n}} \sqrt{2} h \nu_R^{i(\hat{n})} \nu_L^\beta \right) + h.c. \right] \quad \bar{m}_\nu \equiv m_0 l^\dagger$$

- New Higgs production mechanism (Signal)

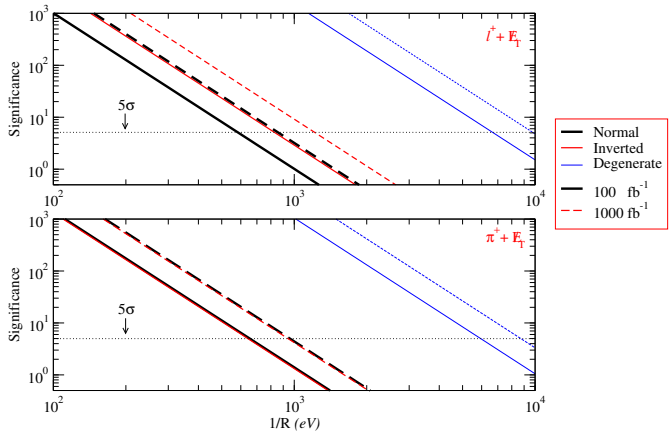
$$q \bar{q}' \rightarrow W^* \rightarrow \ell^+ h \nu_R^{(n)} \quad (\ell = e, \mu, \tau)$$

- Signal can be enhanced due to large number of final state $\nu_R^{(n)}$
- New Higgs decay mode
 - Invisible mode: ($h \rightarrow \nu_L \nu_R^{(n)}$)
 - (SM: $h \rightarrow b \bar{b}$)



LED Bulk ν_R @ LHC

$$\delta = 3, \sqrt{S} = 14 \text{ TeV}$$



Conclusions

- LED recasts Heirarchy Problem statement
 - LHC Limits strong
- UED provides Dark Matter candidate
- Warped Models
 - Bulk fields limits weaker
 - **LHC14 high luminosity run crucial**
 - Possibly dual to 4D strongly coupled theory



BACKUP SLIDES

BACKUP SLIDES



Yukawa Couplings

Yukawa Couplings

- No $Zb\bar{b}$ protection

- DT $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \bar{Q}_L \Sigma \psi_{t_R} + \lambda_b \bar{Q}_L \Sigma \psi_{b_R} + h.c.$

- With $Zb\bar{b}$ protection

- ST $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \text{Tr}[\bar{Q}_L \Sigma] t_R + h.c.$

- TT $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \text{Tr}[\bar{Q}_L \Sigma \psi'_{t_R}] + \lambda'_t \text{Tr}[\bar{Q}_L \Sigma \psi''_{t_R}] + h.c.$

- b Yukawa requires triplet b_R

$$(1, 3)_{2/3} \oplus (3, 1)_{2/3} = \psi'_{b_R} \oplus \psi''_{b_R} = \begin{pmatrix} \frac{t'_b}{\sqrt{2}} & \chi'_b \\ b_R & -\frac{t'_b}{\sqrt{2}} \end{pmatrix} \oplus \begin{pmatrix} \frac{t''_b}{\sqrt{2}} & \chi''_b \\ b''_b & -\frac{t''_b}{\sqrt{2}} \end{pmatrix}$$

$$\mathcal{L}_{\text{Yuk}} \supset \lambda_b \text{Tr}[\bar{Q}_L \Sigma \psi'_{b_R}] + \lambda'_b \text{Tr}[\bar{Q}_L \Sigma \psi''_{b_R}] + h.c.$$

c_{b_R} such that new $\psi'_b, \psi''_b \gtrsim 3$ TeV, so ignore them



WED $pp \rightarrow g^{(1)} \rightarrow t\bar{t}$ (semi-leptonic)

!!!Warning!!! Very rough estimates!

- $\sigma(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 14\text{TeV}, k\pi R = 35) \approx 600\text{fb}$
 - $\mathcal{L}^{5\sigma}(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 14\text{TeV}, k\pi R = 35) = 1.2\text{fb}^{-1}$
- $14\text{TeV} \rightarrow 7\text{TeV}$: $\sigma(g^{(1)} = 2\text{TeV})$ falls by a factor of 25
 - $\mathcal{L}^{5\sigma}(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 7\text{TeV}, k\pi R = 35) = 30\text{fb}^{-1}$
(Assumed : Bkgnd falls with same factor)
- $\mathcal{L}^{5\sigma}(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 7\text{TeV}, k\pi R = 7) = 1\text{fb}^{-1}$



Bulk EW Gauge Sector

Bulk EW Gauge group : $SU(2)_L \times SU(2)_R \times U(1)_X$

- Three neutral gauge bosons: (W_L^3, W_R^3, X)
- Two charged gauge bosons: (W_L^\pm, W_R^\pm)

Symmetry Breaking:

- By Boundary Condition (BC):

$$Z_X(-, +) \text{ means } Z_X|_{y=0} = 0; \partial_y Z_X|_{y=\pi R} = 0$$

- $SU(2)_R \times U(1)_X \rightarrow U(1)_Y$: $(W_R^3, W_L^3, X) \rightarrow (W_L^3, B, Z_X)$
 $A \rightarrow (+, +)$; $Z \rightarrow (+, +)$; $Z_X \rightarrow (-, +)$
- $Z_X \equiv \frac{1}{\sqrt{g_X^2 + g_R^2}}(g_R W_R^3 - g_X X) \rightarrow (-, +)$; $W_R^\pm \rightarrow (-, +)$
- $B \equiv \frac{1}{\sqrt{g_X^2 + g_R^2}}(g_X W_R^3 + g_R X) \rightarrow (+, +)$; $W_L^\pm \rightarrow (+, +)$



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- $B \equiv \frac{1}{\sqrt{g_X^2 + g_R^2}}(g_X W_R^3 + g_R X) \rightarrow (+, +)$; $W_L^\pm \rightarrow (+, +)$

- By VEV of TeV brane Higgs

- $SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$: $(W_L^3, B, Z_X) \rightarrow (A, Z, Z_X)$



Gauge EW KK States

Gauge Boson

- “Zero” modes: $A^{(0)}, Z^{(0)}$; $W_L^{(0)}$
- First KK modes: $A^{(1)}, Z^{(1)}, Z_X^{(1)} \rightarrow Z'$; $W_L^{(1)}, W_R^{(1)}$

EWSB mixes : $Z^{(0)} \leftrightarrow Z^{(1)}$; $Z^{(0)} \leftrightarrow Z_X^{(1)}$; $Z^{(1)} \leftrightarrow Z_X^{(1)}$
 $W_L^{(0)} \leftrightarrow W_L^{(1)}$; $W_L^{(0)} \leftrightarrow W_R^{(1)}$; $W_L^{(1)} \leftrightarrow W_R^{(1)}$

Mass eigenstates :

- “Zero” modes: A, Z ; W^\pm
- First KK modes: $A_1, \tilde{Z}_1, \tilde{Z}_{X_1} \rightarrow Z'$; $\tilde{W}_{L_1}, \tilde{W}_{R_1} \rightarrow W'^\pm$



Z' Overlap Integrals

Define: $\xi \equiv \sqrt{k\pi R} = 5.83$

Z' overlap with Higgs $\rightarrow \xi$

Z' overlap with fermions:

	Q_L^3	t_R	other fermions
\mathcal{I}^+	$-\frac{1.13}{\xi} + 0.2\xi \approx 1$	$-\frac{1.13}{\xi} + 0.7\xi \approx 3.9$	$-\frac{1.13}{\xi} \approx -0.2$
\mathcal{I}^-	$0.2\xi \approx 1.2$	$0.7\xi \approx 4.1$	0

Compared to SM

- Z' couplings to h enhanced (also V_L - Equivalence Theorem!)
- Z' couplings to t_R enhanced
- Z' couplings to χ suppressed

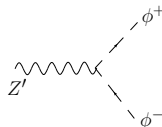
$$\bar{\psi}_{L,R} \gamma^\mu \left[eQ\mathcal{I}A_{1\mu} + g_Z (T_L^3 - s_W^2 T_Q) \mathcal{I}Z_{1\mu} + g_{Z'} (T_R^3 - s'^2 T_Y) \mathcal{I}Z_{X1\mu} \right] \psi_{L,R}$$



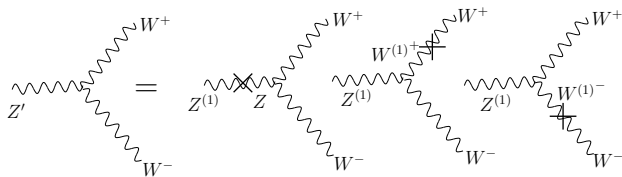
EWSB induced $Z'W^+W^-$ coupling

$Z^{(1)}V^{(0)}V^{(0)}$ is zero by orthogonality ...
 ... but induced after EWSB

Using Goldstone equivalence:



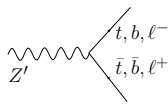
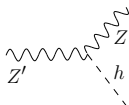
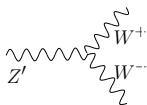
In Unitary Gauge:



Even though $\xi \cdot \left(\frac{v}{M_{KK}}\right)^2$ suppressed ...

Z' decays

[Agashe, Davoudiasl, SG, Han, Huang, Perez, Si, Soni - arXiv:0709.0007 [hep-ph]]



$$\Gamma(A_1 \rightarrow W_L W_L) = \frac{e^2 \kappa^2}{192\pi} \frac{M_{Z'}^5}{m_W^4}; \quad \kappa \propto \sqrt{k\pi r_c} \left(\frac{m_W}{M_{W_1^\pm}} \right)^2,$$

$$\Gamma(\tilde{Z}_1, \tilde{Z}_{X1} \rightarrow W_L W_L) = \frac{g_L^2 c_W^2 \kappa^2}{192\pi} \frac{M_{Z'}^5}{m_W^4}; \quad \kappa \propto \sqrt{k\pi r_c} \left(\frac{m_Z}{(M_{Z_1}, M_{Z_{X1}})} \right)^2,$$

$$\Gamma(\tilde{Z}_1, \tilde{Z}_{X1} \rightarrow Z_L h) = \frac{g_Z^2 \kappa^2}{192\pi} M_{Z'}; \quad \kappa \propto \sqrt{k\pi r_c},$$

$$\Gamma(Z' \rightarrow f\bar{f}) = \frac{(e^2, g_Z^2)}{12\pi} (\kappa_V^2 + \kappa_A^2) M_{Z'}.$$

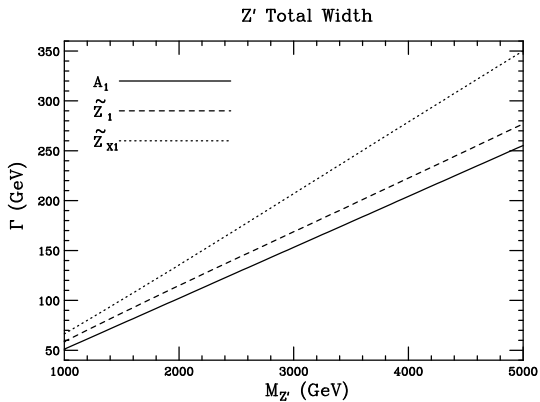


Widths & BR's (For $M_{Z'} = 2\text{TeV}$)

	A_1		\tilde{Z}_1		\tilde{Z}_{X1}	
	$\Gamma(\text{GeV})$	BR	$\Gamma(\text{GeV})$	BR	$\Gamma(\text{GeV})$	BR
$\bar{t}t$	55.8	0.54	18.3	0.16	55.6	0.41
$\bar{b}b$	0.9	8.7×10^{-3}	0.12	10^{-3}	28.5	0.21
$\bar{u}u$	0.28	2.7×10^{-3}	0.2	1.7×10^{-3}	0.05	4×10^{-4}
$\bar{d}d$	0.07	6.7×10^{-4}	0.25	2.2×10^{-3}	0.07	5.2×10^{-4}
$\ell^+\ell^-$	0.21	2×10^{-3}	0.06	5×10^{-4}	0.02	1.2×10^{-4}
$W_L^+ W_L^-$	45.5	0.44	0.88	7.7×10^{-3}	50.2	0.37
$Z_L h$	-	-	94	0.82	2.7	0.02
Total	103.3		114.6		135.6	



Total Widths

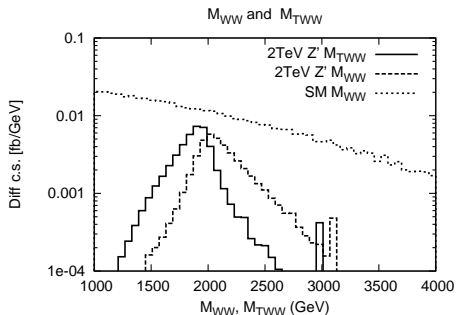


$M_{Z'} = 2\text{TeV}$	A_1	Z_1	Z_{X1}
Γ (GeV)	103.3	114.6	135.6

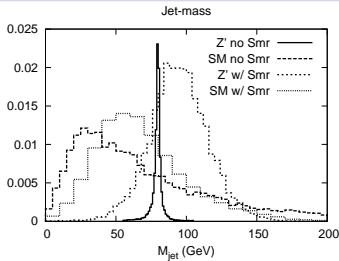
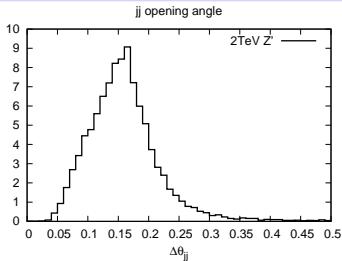


$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell \nu jj$

$$M_{eff} \equiv p_{T_{jj}} + p_{T_\ell} + \cancel{p}_T \quad M_{T_{WW}} \equiv 2\sqrt{p_{T_{jj}}^2 + m_W^2}$$



$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell \nu jj$ (Boosted $W \rightarrow (jj)$)



jj Collimation implies forming m_W nontrivial : use jet-mass

In our study: Jet-mass after Parton shower in Pythia

[Thanks to Frank Paige for discussions]

To account for (HCal) expt. uncert.

Smearing by $\delta E = 80\%/\sqrt{E}$; $\delta\eta, \delta\phi = 0.05$

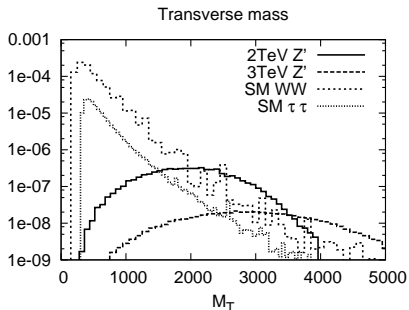
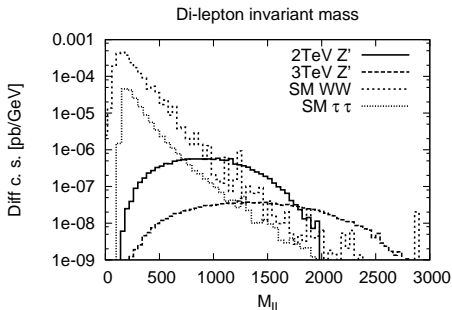
Tracker + ECal (2 cores?) have better resolutions

[F. Paige; M. Strassler]



$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell\nu\ell\nu$

2 ν 's \Rightarrow cannot reconstruct event



$$M_{eff} \equiv p_{T_{\ell_1}} + p_{T_{\ell_2}} + \cancel{p}_T \quad M_{T_{WW}} \equiv 2\sqrt{p_{T_{\ell\ell}}^2 + M_{\ell\ell}^2}$$

\mathcal{L} needed: 100 fb^{-1} (2 TeV) ; 1000 fb^{-1} (3 TeV)



$$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell\nu\ell\nu$$

Cross-section (in fb) after cuts:

2 TeV	Basic cuts	$ \eta_\ell < 2$	$M_{eff} > 1$ TeV	$M_T > 1.75$ TeV	# Evts	S/B	S/\sqrt{B}
Signal	0.48	0.44	0.31	0.26	26	0.9	4.9
WW	82	52	0.4	0.26	26		
$\tau\tau$	7.7	5.6	0.045	0.026	2.6		
3 TeV	Basic cuts	$ \eta_\ell < 2$	$1.5 < M_{eff} < 2.75$	$2.5 < M_T < 5$	# Evts	S/B	S/\sqrt{B}
Signal	0.05	0.05	0.03	0.025	25		
WW	82	52	0.08	0.04	40	0.6	3.8
$\tau\tau$	7.7	5.6	0.015	0.003	3		

events above is for

- 2 TeV : 100 fb^{-1}
- 3 TeV : 1000 fb^{-1}



$$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell \nu jj$$

Cross-section (in fb) after cuts:

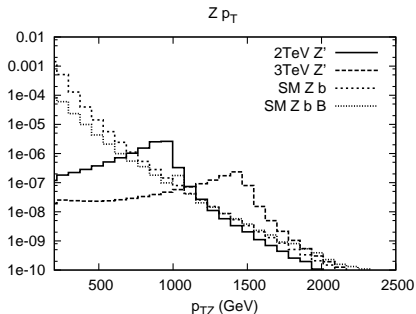
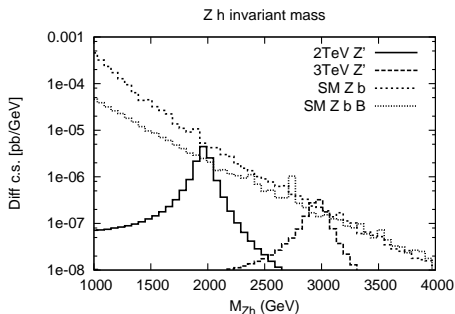
$M_{Z'} = 2 \text{ TeV}$	p_T	$\eta_{\ell,j}$	M_{eff}	$M_{T_{WW}}$	M_{jet}	# Evts	S/B	S/\sqrt{B}
Signal	4.5	2.40	2.37	1.6	1.25	125	0.39	6.9
W+1j	1.5×10^5	3.1×10^4	223.6	10.5	3.15	315		
WW	1.2×10^3	226	2.9	0.13	0.1	10		
$M_{Z'} = 3 \text{ TeV}$								
Signal	0.37	0.24	0.24	0.12	-	120	0.17	4.6
W+1j	1.5×10^5	3.1×10^4	88.5	0.68	-	680		
WW	1.2×10^3	226	1.3	0.01	-	10		

events above is for

- 2 TeV : 100 fb^{-1}
- 3 TeV : 1000 fb^{-1}



$pp \rightarrow Z' \rightarrow Zh \rightarrow \ell^+ \ell^- b \bar{b}$ ($m_h = 120$ GeV)



How well can we tag high p_T b's ?

For $\epsilon_b = 0.4$, expect $R_j \approx 20 - 50$; $R_c = 5$

Two b's close : $\Delta R_{bb} \sim 0.16$

\mathcal{L} needed: 200 fb^{-1} (2 TeV) ; 1000 fb^{-1} (3 TeV)



$pp \rightarrow Z' \rightarrow Zh \rightarrow \ell^+ \ell^- b \bar{b}$ ($m_h = 120$ GeV)

Cross-section (in fb) after cuts:

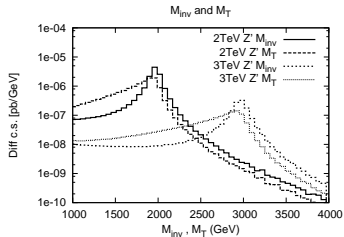
$M_{Z'} = 2$ TeV	Basic	$p_{T, \eta}$	$\cos \theta_{Zh}$	M_{inv}	b-tag	# Evts	S/B	S/\sqrt{B}
$Z' \rightarrow hZ \rightarrow b\bar{b}\ell\ell$	0.81	0.73	0.43	0.34	0.14	27	1.1	5.3
SM $Z + b$	157	1.6	0.9	0.04	0.016	3		
SM $Z + b\bar{b}$	13.5	0.15	0.05	0.01	0.004	0.8		
SM $Z + q_l$	2720	48	22.4	1.5	0.08	15		
SM $Z + g$	505.4	11.2	5.8	0.5	0.025	5		
SM $Z + c$	184	1.9	1.1	0.05	0.01	2		
$M_{Z'} = 3$ TeV								
$Z' \rightarrow hZ \rightarrow b\bar{b}\ell\ell$	0.81	0.12	0.05	0.04	0.016	16	2	5.7
SM $Z + b$	157	0.002	0.001	3×10^{-4}	1.2×10^{-4}	0.12		
SM $Z + b\bar{b}$	13.5	0.018	0.014	0.002	0.001	1		
SM $Z + q_l$	2720	1.1	0.7	0.1	0.005	5		
SM $Z + g$	505.4	0.3	0.2	0.03	0.0015	1.5		
SM $Z + c$	183.5	0.03	0.02	0.002	4×10^{-4}	0.4		

events above is for

- 2 TeV : 200 fb⁻¹
- 3 TeV : 1000 fb⁻¹



$pp \rightarrow Z' \rightarrow Z h : Z \rightarrow jj ; h \rightarrow W^+ W^- \rightarrow jj \ell \nu$
 ($m_h = 150$ GeV)



$$M_{T_{Zh}} \equiv \sqrt{p_{TZ}^2 + m_Z^2} + \sqrt{p_{Th}^2 + m_h^2}$$

$M_{Z'} = 2$ TeV $m_h = 150$ GeV	Basic	p_T, η	$\cos \theta$	M_T	M_{jet}	# Evts	S/B	S/\sqrt{B}
$Z' \rightarrow hZ \rightarrow \ell \cancel{E}_T (jj) (jj)$	2.4	1.6	0.88	0.7	0.54	54	2.5	11.5
SM $W jj$	3×10^4	35.5	12.7	0.62	0.19	19		
SM $W Z j$	184	0.45	0.15	0.02	0.02	2		
SM $W W j$	712	0.54	0.2	0.02	0.01	1		
$M_{Z'} = 3$ TeV $m_h = 150$ GeV								
$Z' \rightarrow hZ \rightarrow \ell \cancel{E}_T (jj) (jj)$	0.26	0.2	0.14	0.06	—	18	1.2	4.7
SM $W jj$	3×10^4	4.1	0.05	—	—	15		

events above is for

- 2 TeV : 100 fb⁻¹
- 3 TeV : 300 fb⁻¹



$$pp \rightarrow Z' \rightarrow \ell^+ \ell^-$$

$M_{Z'} = 2 \text{ TeV}$	Basic	$p_{T\ell}$	$M_{\ell\ell}$	# Evts	S/B	S/\sqrt{B}
Signal	0.1	0.09	0.06	60	0.3	4.2
SM $\ell\ell$	3×10^4	5.4	0.2	200		
SM WW	295	0.03	0.002	2		

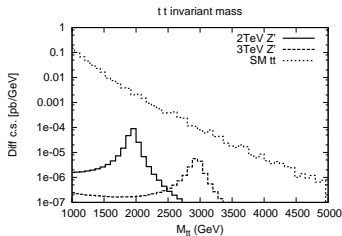
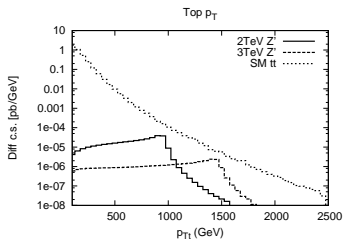
events above is for

- 2 TeV : 1000 fb⁻¹

Experimentally clean, but needs a LOT of luminosity



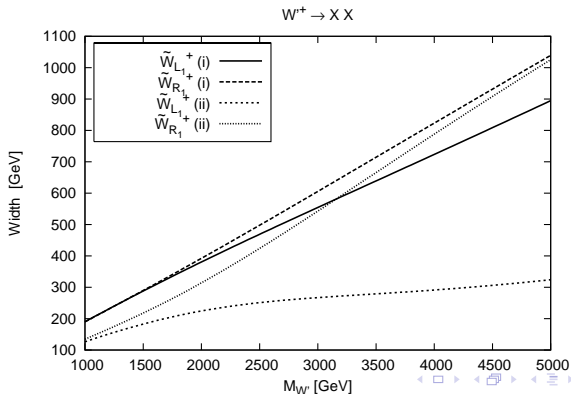
$pp \rightarrow Z' \rightarrow t\bar{t}$



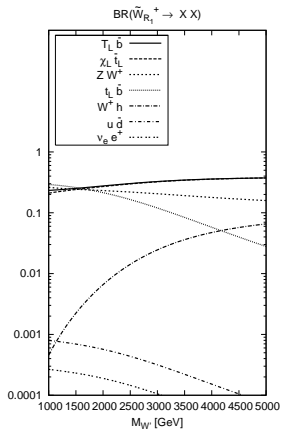
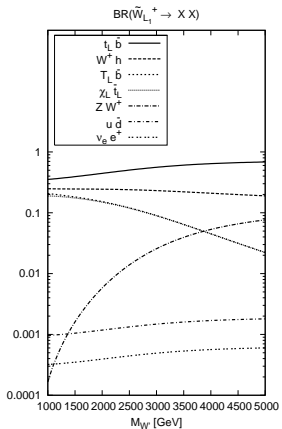
$M_{Z'} = 2 \text{ TeV}$	Basic	$p_T > 800$	$1900 < M_{t\bar{t}} < 2100$
Signal	17	7.2	5.6
SM $t\bar{t}$	1.9×10^5	31.1	19.1
$M_{Z'} = 3 \text{ TeV}$	Basic	$p_T > 1250$	$2850 < M_{t\bar{t}} < 3100$
Signal	1.7	0.56	0.45
SM $t\bar{t}$	1.9×10^5	4.1	1.1



W'^{\pm} width



$W'^{\pm} BR$

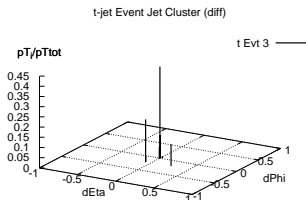
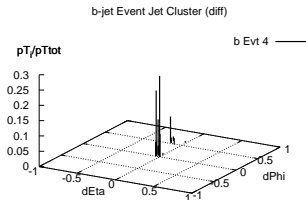
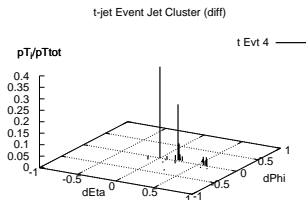
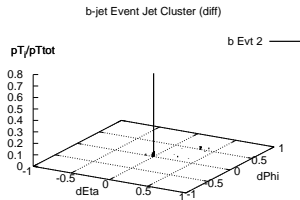


$W'^{\pm} \rightarrow t b \rightarrow l \nu b b$

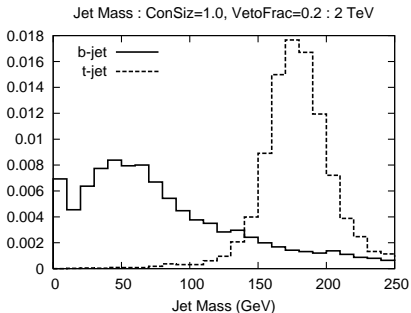
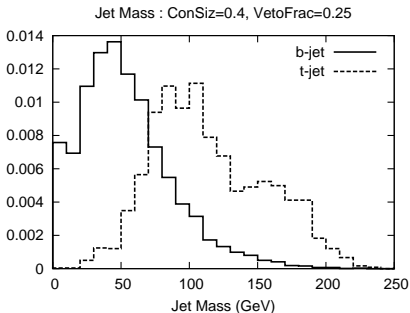
Signal c.s. $\sim 1fb$

Bkgnd is single top + QCD W b b AND ...

$t\bar{t}$: hadronically decaying top can fake a b



$$W'^{\pm} \rightarrow t b \rightarrow \ell \nu b b$$



Jet-mass cut: cone size 1.0 and $0 < j_M < 75 \Rightarrow 0.4\%$ of *top fakes b*
 \mathcal{L} needed: 100 fb^{-1} (2 TeV)



$W'^{\pm} \rightarrow Z W$ and $W h$

$W'^{\pm} \rightarrow Z W$:

- Fully leptonic $\rightarrow \mathcal{L} : 100 \text{ fb}^{-1}$ (2 TeV) ; 1000 fb^{-1} (3 TeV)
- Semi leptonic $\rightarrow \mathcal{L} : 300 \text{ fb}^{-1}$ (2 TeV) (SM $W/Z + 1j$ large)



$W'^{\pm} \rightarrow Z W$ and $W h$

$W'^{\pm} \rightarrow Z W$:

- Fully leptonic $\rightarrow \mathcal{L} : 100 \text{ fb}^{-1}$ (2 TeV) ; 1000 fb^{-1} (3 TeV)
- Semi leptonic $\rightarrow \mathcal{L} : 300 \text{ fb}^{-1}$ (2 TeV) (SM $W/Z + 1j$ large)

$W'^{\pm} \rightarrow W h$:

- $m_h \approx 120 : h \rightarrow b b$
 - What is b-tagging eff?
- $m_h \approx 150 : h \rightarrow W W$
 - Use W jet-mass to reject light jet

\mathcal{L} needed: 100 fb^{-1} (2TeV) ; 300 fb^{-1} (3TeV)



- Warped (RS) model
- Heavy EW gauge bosons : 3 neutral (Z') & 2 charged (W'^{\pm})
 - Precision electroweak observables require $M_{Z'}$, $M_{W_1^{\pm}} \gtrsim 2$ TeV
 - Makes discovery challenging at the LHC

