Lecture 2: Magnets & training, plus fine filaments

Magnets

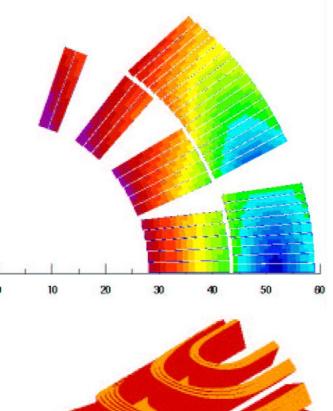
- magnetic fields above 2 Tesla
- coil shapes for solenoids, dipoles and quadrupoles
- engineering current density
- load lines

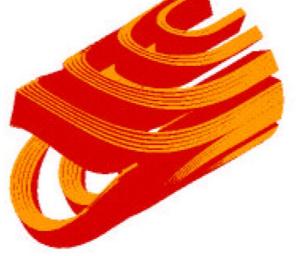
Degradation & Training

- causes of training release of energy within the magnet
- reducing training stability and minimum quench energy MQE

Fine filaments

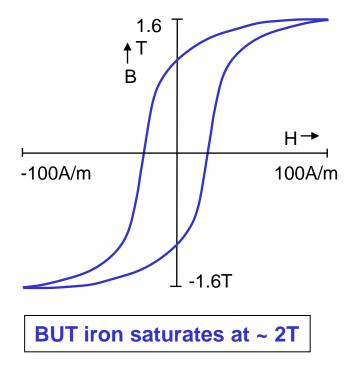
- the critical state model & screening currents
- flux jumping

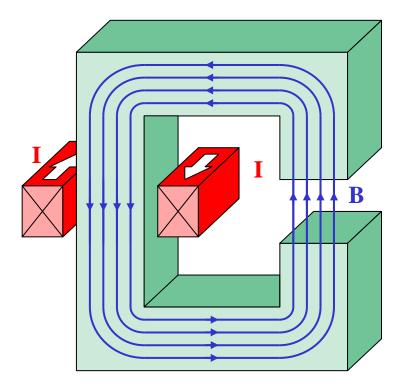




Fields and ways to create them: conventional

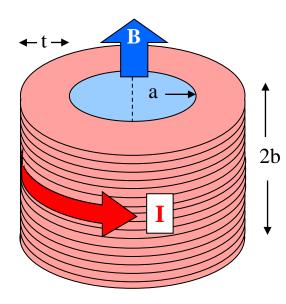
- conventional electromagnets have an iron yoke
 - reduces magnetic reluctance
 - reduces ampere turns required
 - reduces power consumption
- iron guides and shapes the field





Iron electromagnet – for accelerators, motors, transformers, generators etc

for higher fields we cannot rely on iron field must be created and shaped by the winding



Solenoids

- no iron field shape depends only on the winding
- azimuthal current flow, eg wire wound on bobbin, axial field
- the field produced by an infinitely long solenoid is

$$B = \mu_o NI = \mu_o J_e t$$

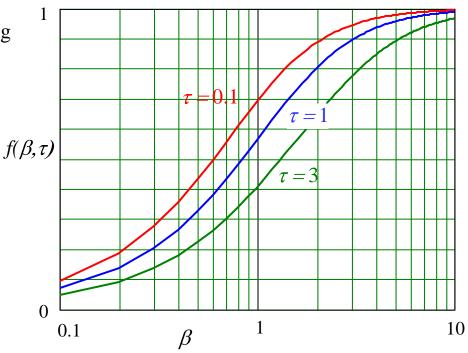
where N = number of turns/unit length, I = current , J_e = engineering current density

- so high $J_e \Rightarrow$ thin compact economical winding
- in solenoids of finite length the central field is

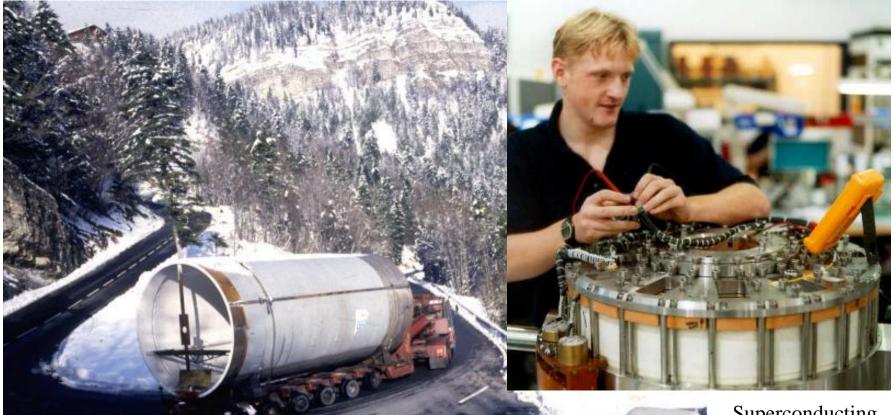
$$B = \mu_o J_e t f \mathbf{\Phi}, \tau$$

where $\beta = b/a$ $\tau = t/a$

• field uniformity and the ratio of peak field to central field get worse in short fat solenoids



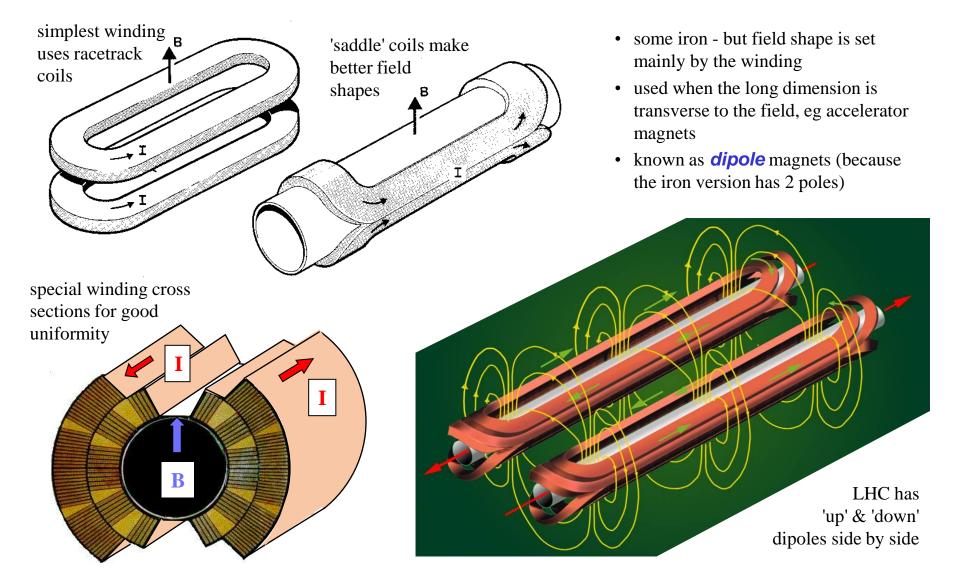
Superconducting solenoids



Superconducting solenoid for research

Delphi solenoid for HEP experiments at CERN 1.2T 5.5m dia 6.8m long 110MJ

Accelerators need transverse fields



Dipole field from overlapping cylinders

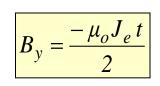
Ampere's law for the field inside a cylinder carrying uniform current density

$$\oint B.ds = 2\pi r B = \mu_o I = \mu_o \pi r^2 J \qquad B = \frac{\mu_o J r}{2}$$

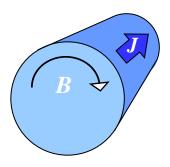
- two cylinders with opposite currents
- push them together
- currents cancel where they overlap \Rightarrow aperture
- fields in the aperture:

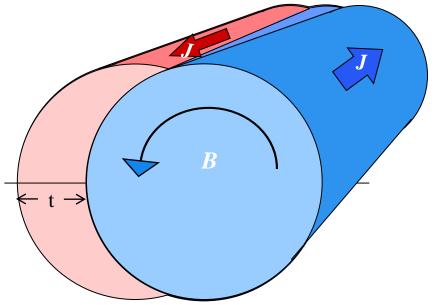
$$B_{y} = \frac{\mu_{o}J}{2} \blacktriangleleft r_{1}cos\theta_{1} + r_{2}cos\theta_{2} = \frac{-\mu_{o}Jt}{2}$$
$$B_{x} = \frac{\mu_{o}J}{2} \bigstar r_{1}sin\theta_{1} + r_{2}sin\theta_{2} = 0$$

• thus the overlapping cylinders give a perfect dipole field

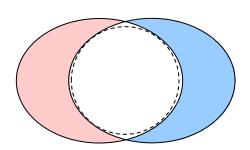


m current density $\frac{{}_{o}Jr}{2}$





- same trick with ellipses
- circular aperture



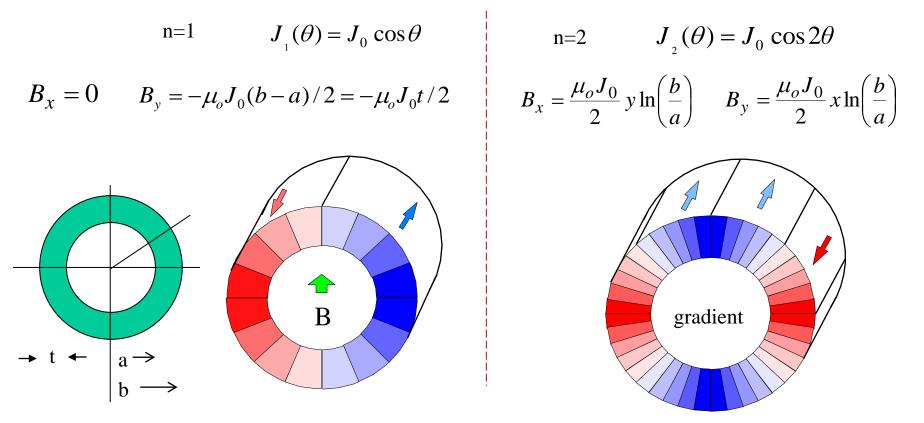
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Windings of distributed current density

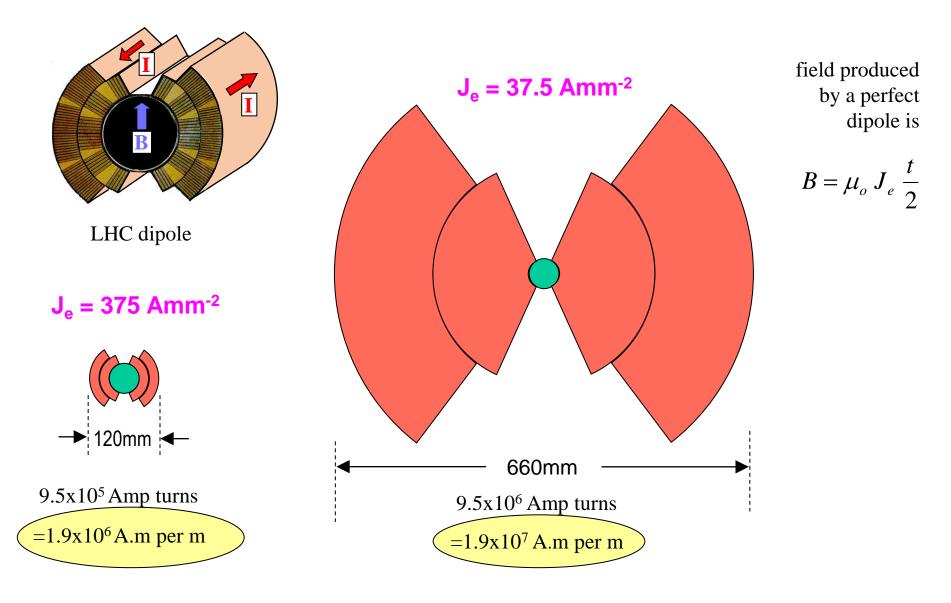
Analyse thin current sheets flowing on the surface of a cylinder using complex algebra. Let the *linear* current density (Amps per m of circumference) be $g_n = g_o cos(n\theta)$ (Am⁻¹)

For n = 1 we find a pure dipole field inside the cylinder, n = 2 gives a quadrupole etc.

Now superpose many cylinders of increasing radius to get a thick walled cylinder carrying an (area) current density $(Am^{-2}) J_n = J_o \cos(n\theta)$



Importance of (engineering) current density in dipoles

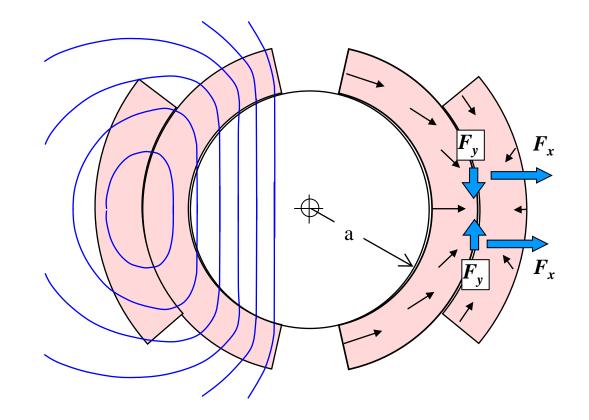


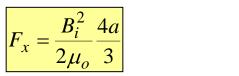
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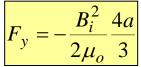


Electromagnetic forces in dipoles

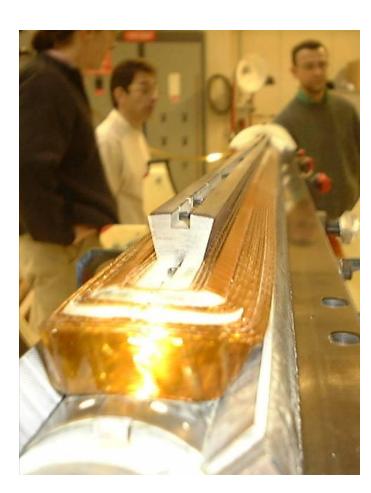
- forces in a dipole are horizontally outwards and vertically towards the median plane
- unlike a solenoid, the bursting forces cannot be supported by tension in the winding
- the outward force must be supported by an external structure
- both forces cause compressive stress and shear in the conductor and insulation
- apart from the ends, there is no tension in the conductor
- simple analysis for thin windings

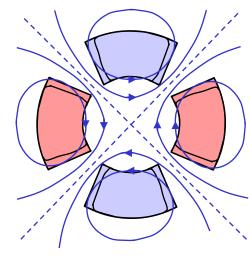


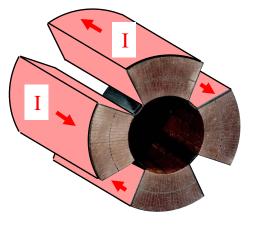




Quadrupole windings



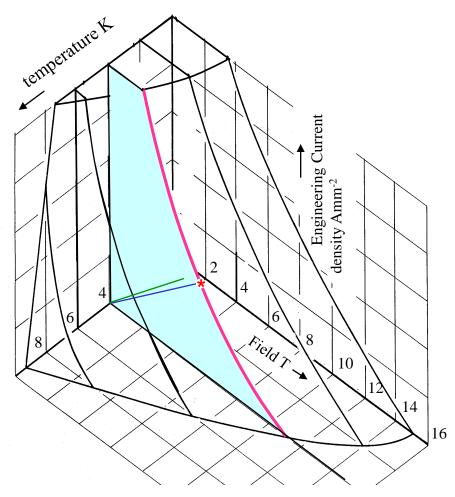


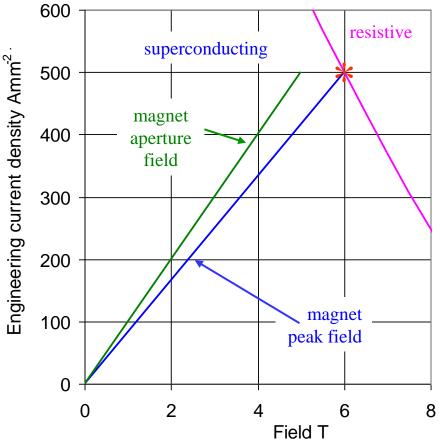


 $B_x = ky$ $B_y = kx$



Critical surface and magnet load lines

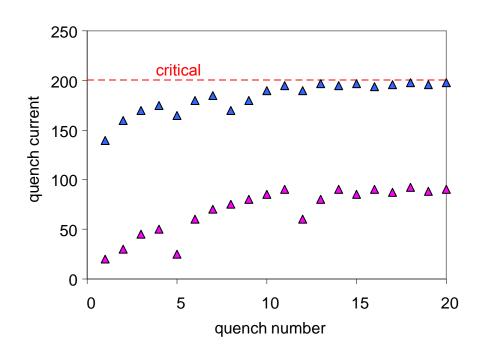


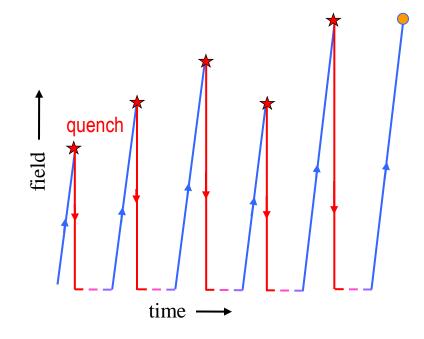


- load line relates magnet field to current
- peak field > aperture (useful) field
- we expect the magnet to go resistive
 'quench' where the peak field load line
 crosses the critical current line *

Degraded performance and 'training' of magnets

- early disappointment for magnet makers when they ramped up the magnet current for the first time
- instead of going up to the critical line, it 'quenched' (went resistive) at less than the expected current
- at the next try it did better
- known as *training*

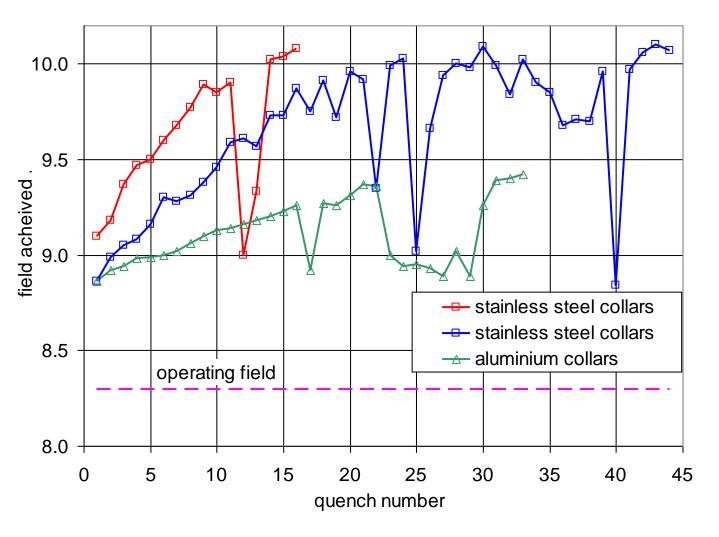




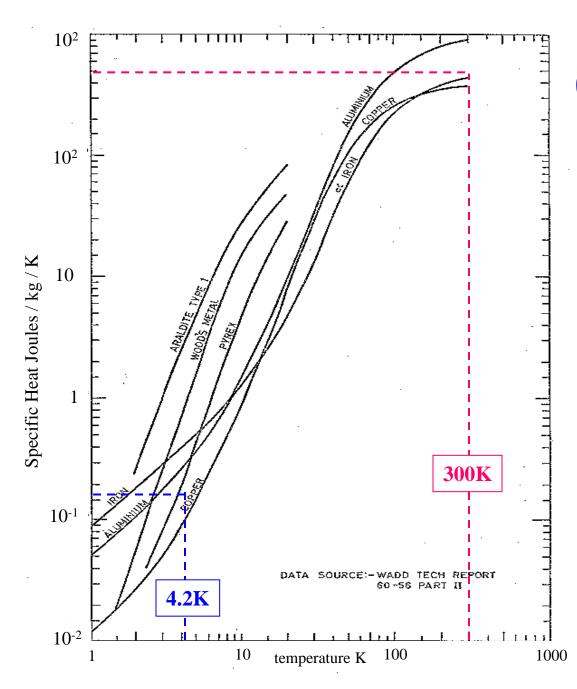
- after a *quench*, the stored energy of the magnet is dissipated in the magnet, raising its temperature way above critical
- you must wait for it to cool down and then try again
- well made magnets ▲ are better than poorly made ▲

'Training' of magnets

- it's better than the old days, but training is still with us
- it seems to be affected by the construction technique of the magnet
- it can be wiped out if the magnet is warmed to room temperature
- 'de-training is the most worrysome feature



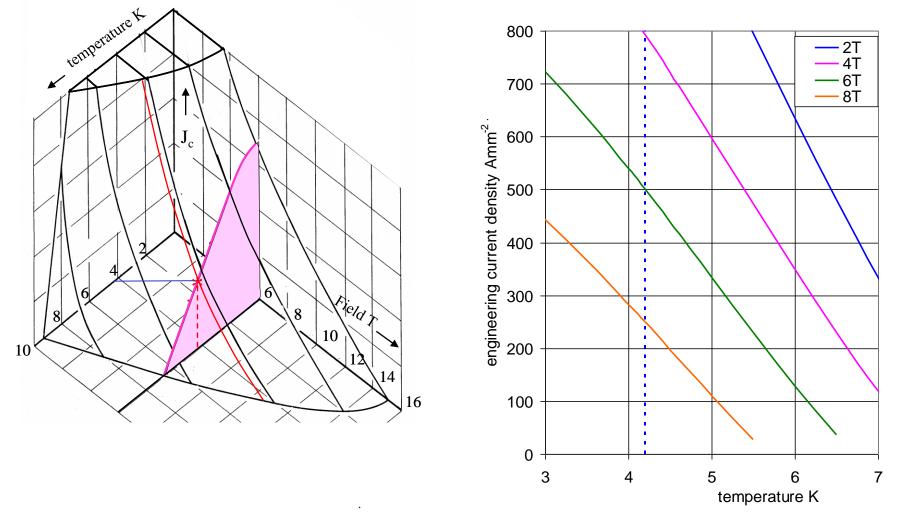
Training of LHC short prototype dipoles (from A. Siemko)



Causes of training: (1) low specific heat

- the specific heat of all substances falls with temperature
- at 4.2K, it is ~2,000 times less than at room temperature
- a given release of energy within the winding thus produce a temperature rise 2,000 times greater than at room temperature
- the smallest energy release can therefore produce catastrophic effects

Causes of training: (2) J_c decreases with temperature



at any field, J_c of NbTi falls ~ linearly with temperature

- so any temperature rise drives the conductor towards the resistive state

Causes of training: (3) conductor motion

Conductors in a magnet are pushed by the electromagnetic forces. Sometimes they move suddenly under this force - the magnet 'creaks' as the stress comes on. A large fraction of the work done by the magnetic field in pushing the conductor is released as frictional heating

work done per unit length of conductor if it is pushed a distance δz

 $W = F.\delta z = B.I.\delta z$

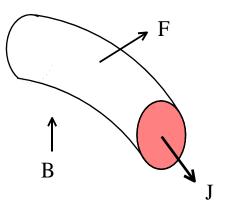
frictional heating per unit volume

 $Q = B.J.\delta z$

typical numbers for NbTi:

 $B = 5T \quad J_{eng} = 5 \times 10^8 \text{ A.m}^{-2}$ so if $\delta = 10 \ \mu\text{m}$ then Q = 2.5 x 10⁴ J.m⁻³ Starting from 4.2K $\theta_{final} = 7.5$ K

can <u>you</u> engineer a winding to better than **10 µm**?





Causes of training: (4) resin cracking

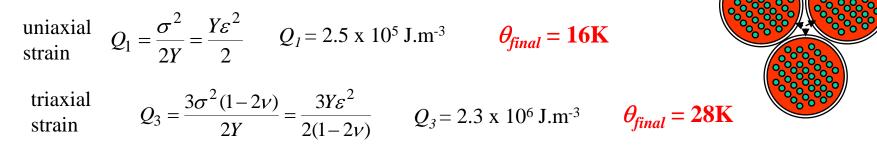
Try to stop wire movement by impregnating the winding with epoxy resin. But resin contracts more than metal, so it goes into tension. Almost all organic materials become brittle at low temperature.

brittleness + *tension* \Rightarrow *cracking* \Rightarrow *energy release*

Calculate strain energy in resin caused by differential thermal contraction

 σ = tensile stress Y = Young's modulus v = Poisson's ratio ε = differential strain due to cooling = contraction (resin - metal)

typically: $\varepsilon = (11.5 - 3) \times 10^{-3}$ $Y = 7 \times 10^9 \text{ Pa}$ $v = \frac{1}{3}$



cracking releases most of this stored energy as heat

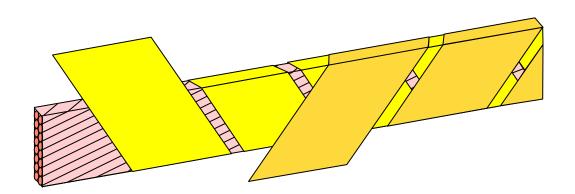
Interesting fact: magnets impregnated with paraffin wax show almost no training although the wax is full of cracks after cooldown.
 Presumably the wax breaks at low σ before it has had chance to store up any strain energy

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How to reduce training?

1) Reduce the disturbances occurring in the magnet winding

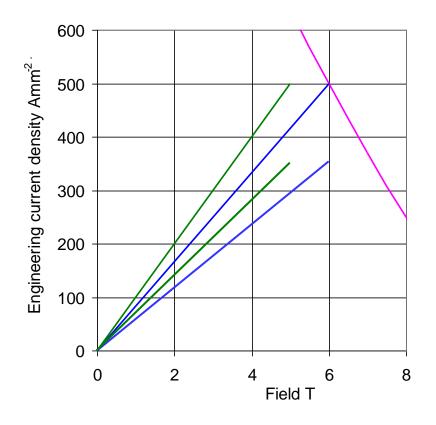
- make the winding fit together exactly to reduce movement of conductors under field forces
- pre-compress the winding to reduce movement under field forces
- if using resin, minimize the volume and choose a crack resistant type
- match thermal contractions, eg fill epoxy with mineral or glass fibre
- impregnate with wax but poor mechanical properties
- most accelerator magnets are insulated using a Kapton film with a very thin adhesive coating on the outer face
 away from the superconductor
- allows liquid helium to penetrate the cable

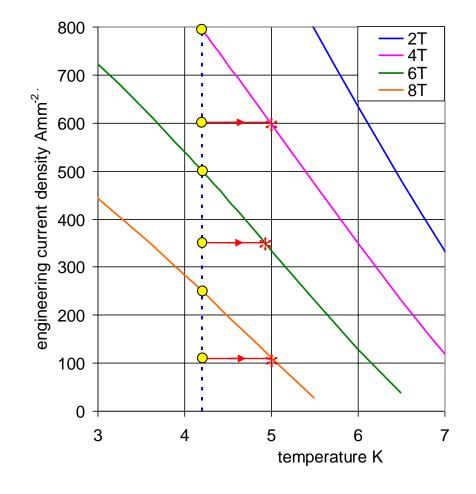


How to reduce training?

2) Make the conductor able to withstand disturbances without quenching

- increase the temperature margin
- operate at lower current
- but need more winding to make same field





- harder at high fields than at low fields
- higher critical temperature HTS?

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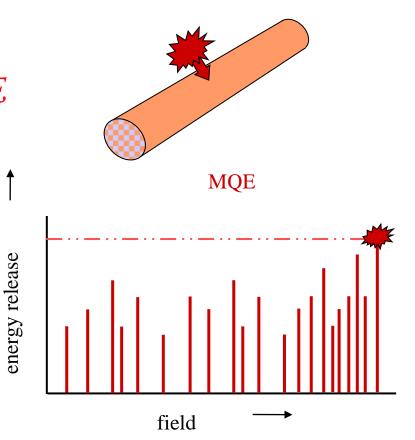
How to reduce training?

2) Make the conductor able to withstand disturbances without quenching

- increase the temperature margin
- increase the cooling more cooled surface better heat transfer superfluid helium
- increase the specific heat experiments with Gd_2O_2S HoCu₂ etc
- most of this may be characterized by a single number

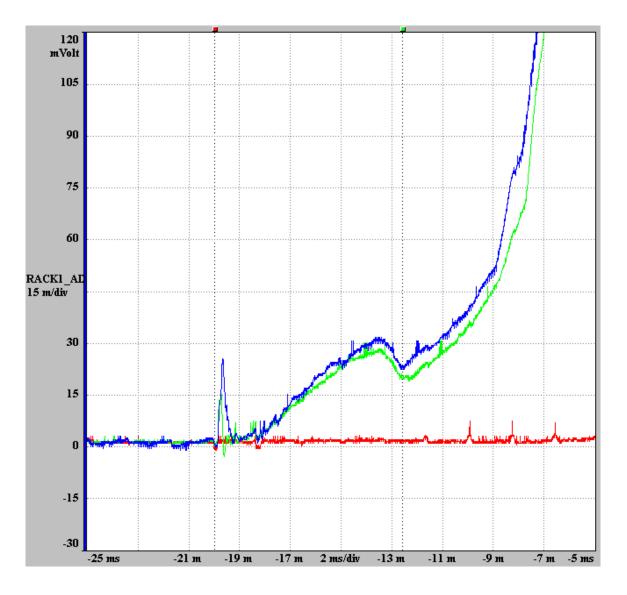
Minimum Quench Energy MQE

- defined as the energy input at a point in very short time which is just enough to trigger a quench.
- energy input > MQE \Rightarrow quench
- energy input < MQE \Rightarrow recovery
- energy disturbances occur at random as a magnet is ramped up to field
- for good magnet performance we want a high MQE



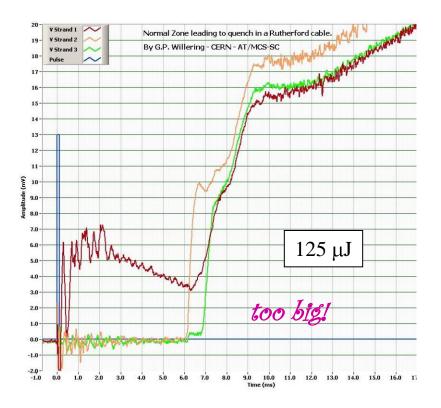
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Quench initiation by a disturbance

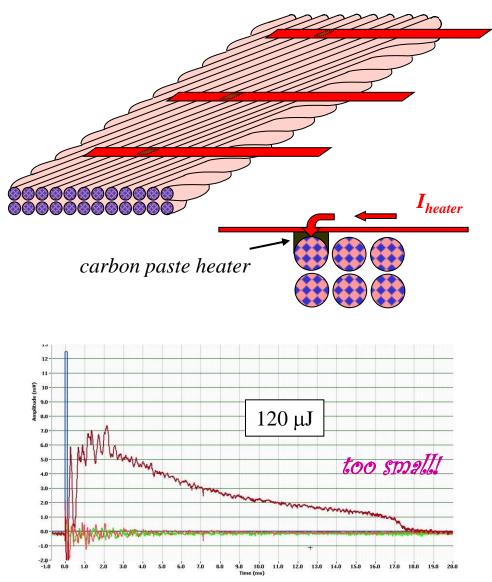


- CERN picture of the internal voltage in an LHC dipole just before a quench
- note the initiating spike conductor motion?
- after the spike, conductor goes resistive, then it almost recovers
- but then goes on to a full quench
- this disturbance was more than the MQE

Measuring the MQE for a cable

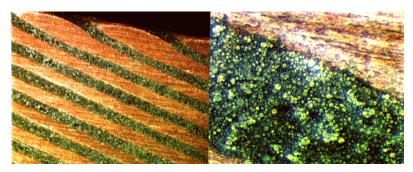


- pass a small pulse of current from the copper foil to the superconducting wire
- generates heat in the carbon paste contact
- how much to quench the cable?
- find the Minimum Quench Energy MQE

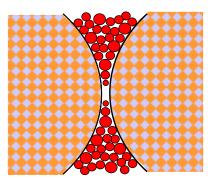


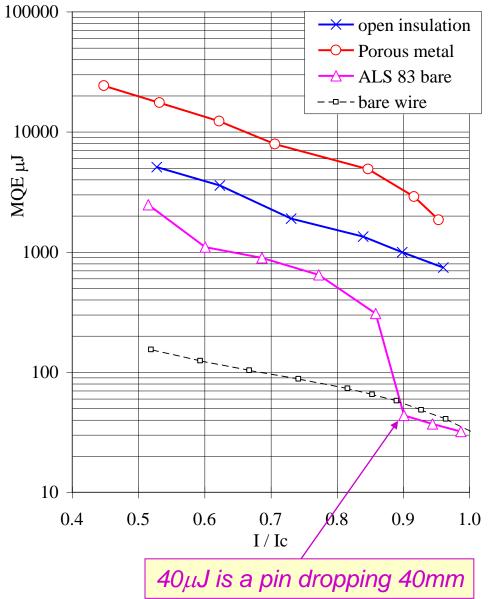
Different cables have different MQEs

- similar cables with different cooling
- better cooling gives higher MQE
- high MQE is best because it is harder to quench the magnet



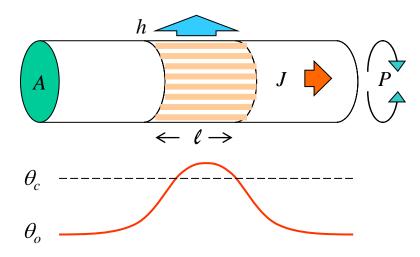
- experimental cable with porous metal heat exchanger
- excellent heat transfer to the liquid helium coolant





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Factors affecting the Minimum Quench Energy



 $\frac{2kA(\theta_c - \theta_o)}{I} + hPl(\theta_c - \theta_o) = J_c^2 \rho Al$

Very approximate heat balance

- heat a short zone of conductor \Rightarrow resistive
- heat conducted out > generation \Rightarrow zone shrinks
- heat conducted out < generation \Rightarrow zone grows
- boundary between the two conditions is the *minimum propagating zone MPZ*
- large MPZ \Rightarrow stability against disturbances

so length
of MPZ
$$l = \left\{ \frac{2k(\theta_c - \theta_o)}{J_c^2 \rho - \frac{hP}{A}(\theta_c - \theta_o)} \right\}^{\frac{1}{2}}$$

where: k = thermal conductivity $\rho =$ resistivity A = cross sectional area of conductor h = heat transfer coefficient to coolant – if there is any in contact P = cooled perimeter of conductor

Energy to set up MPZ is the Minimum Quench Energy

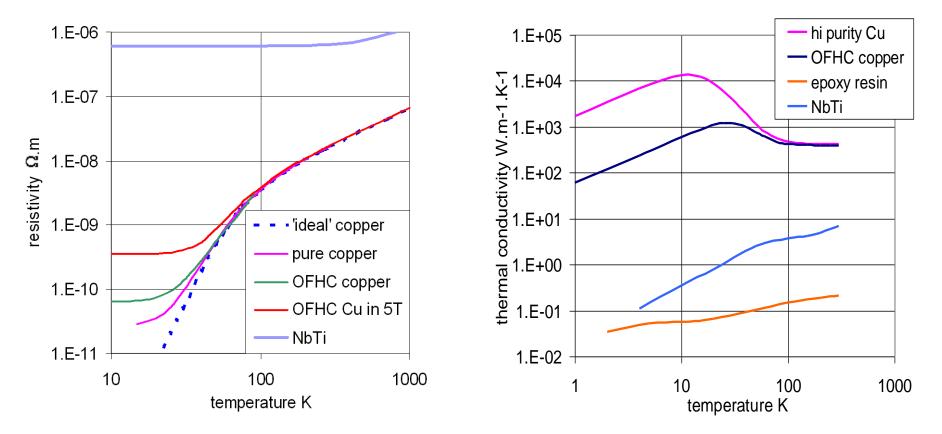
long $MPZ \Rightarrow$ large MQE

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How to make a long $MPZ \Rightarrow large MQE$

$$l = \left\{ \frac{2k(\theta_c - \theta_o)}{J_c^2 \rho - \frac{hP}{A}(\theta_c - \theta_o)} \right\}^{\frac{1}{2}}$$

- make thermal conductivity k large
- make resistivity ρ small
- make heat transfer hP/A large (but $\Rightarrow \log J_{eng}$)

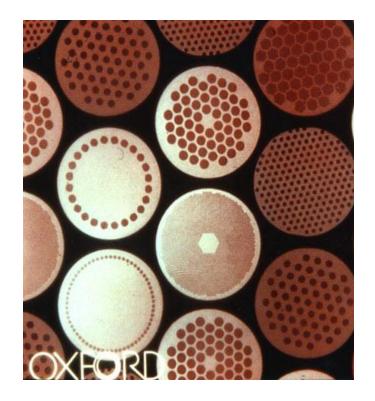


Large MPZ \Rightarrow large MQE \Rightarrow less training

$$l = \left\{ \frac{2k(\theta_c - \theta_o)}{J_c^2 \rho - \frac{hP}{A}(\theta_c - \theta_o)} \right\}^{\frac{1}{2}}$$

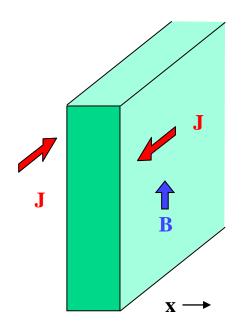
- make thermal conductivity *k* large
- make resistivity ρ small
- make heat transfer term hP/A large

- NbTi has high ρ and low k
- copper has low ρ and high k
- mix copper and NbTi in a filamentary composite wire
- make NbTi in *fine filaments* for intimate mixing
- maximum diameter of filaments ~ 50μ m
- make the windings porous to liquid helium
 superfluid is best
- fine filaments also eliminate flux jumping (see later slides)



Another cause of training: flux jumping

- changing magnetic fields induce screening currents in superconductors
- screening currents are in addition to transport currents, which come from the power supply
- like eddy currents but don't decay because no resistance,



- usual model is a superconducting slab in a changing magnetic field B_v
- assume it's infinitely long in the *z* and *y* directions simplifies to a 1 dim problem
- *dB/dt* induces an electric field *E* which causes screening currents to flow at critical current density *J_c*
- known as the critical state model or Bean model
- in the 1 dim infinite slab geometry, Maxwell's equation says

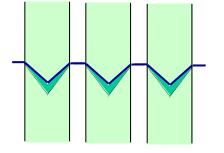
$$\frac{\partial B_y}{\partial x} = -\mu_o J_z = \mu_o J_c$$

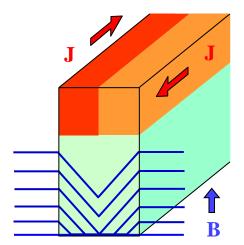
• so uniform J_c means a constant field gradient inside the superconductor

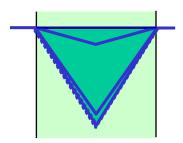
Flux Jumping

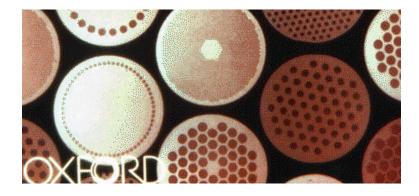
a magnetic thermal feedback instability

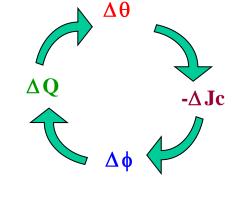
- screening currents
- temperature rise
 - reduced critical current density
 - flux motion
 - energy dissipation
- • temperature rise
 - cure flux jumping by weakening a link in the feedback loop
 - fine filaments reduce $\Delta \phi$ for a given $-\Delta Jc$
 - for NbTi the stable diameter is ~ 50μm





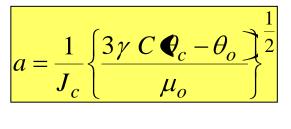






Flux jumping: the numbers for NbTi

criterion for stability against flux jumping a = half width of filament

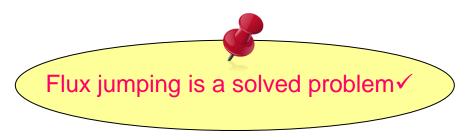


typical figures for NbTi at 4.2K and 1T J_c critical current density = 7.5 x 10⁹ Am⁻² γ density = 6.2 x 10³ kg.m³ C specific heat = 0.89 J.kg⁻¹K⁻¹ θ_c critical temperature = 9.0K

so $a = 33 \mu m$, ie 66 μm diameter filaments

Notes:

- least stable at low field because J_c is highest
- instability gets worse with decreasing temperature because J_c increases and C decreases
- criterion gives the size at which filament is just stable against infinitely small disturbances
 still sensitive to moderate disturbances, eg mechanical movement
- better to go somewhat smaller than the limiting size
- in practice 50µm diameter seems to work OK



Concluding remarks

- superconducting magnets can make higher fields than conventional because they don't need iron which saturates at 2T although iron is often used for shielding
- to get different field shapes you have to shape the <u>winding</u> (not the iron)
- practical winding shapes are derived from the ideal overlapping ellipses or $J = J_o Cos \theta$
- engineering current density is important for a compact economic magnet design
- expected magnet performance is given by the intersection of the load line and critical surface
- degraded performance and training are still a problem for magnets and de-training is worse
- improve training by good winding construction
 ⇒ no movement, low thermal contraction, no cracking
- improve training by making the conductor have a high MQE

 temperature margin, high conductivity, good cooling
 NbTi in good contact with copper ⇒ fine filaments
- changing fields induce screening currents in all superconductors \Rightarrow flux jumping
- flux jumping did cause degraded magnet performance but fine filaments have now cured it