

Introduction to MAD-X

G. Sterbini, CERN
Thanks to W. Herr and B. Holzer

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`guido.sterbini@cern.ch`

Introduction

MAD-X syntax

Daily life

“Hello World!” example

DISCLAIMER. This material is intended to be an introduction to MAD-X: a large part of the code capabilities are not discussed in details or are not discussed at all!

A lot of material on the web...



- ▶ By googling “**madx**”, you get the MAD-X homepage.
- ▶ To wet your appetite, you can google “MAD-X primer”.
- ▶ To go in details, you can google “MAD-X manual”.

WHAT IS MAD-X?

- ▶ A general purpose beam optics and lattice program distributed for free by CERN.
- ▶ It is used at CERN since more than 20 years for machine design and simulation (PS, SPS, LHC, linacs...).
- ▶ MAD-X is written in C/C++/Fortran77/Fortran90 (source code is available under CERN copyright).

```

Terminal -- bash -- 66x19
cosmos:~ sterbini$ madx

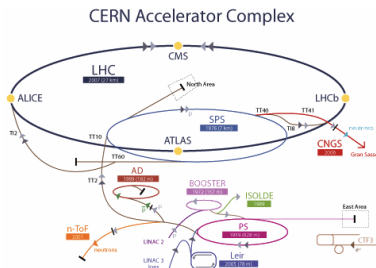
+++++
+ MAD-X 4.00.19 +
+ Production Version +
+ Code Modification Date: 04.05.2009 +
+ Execution Time Stamp: 06.01.10 11.50.55 +
+++++

X: ==>
quit;
quit;

Number of warnings: 0

+++++
+ MAD-X 4.00.19 Finished normally +
+++++
cosmos:~ sterbini$
  
```

A GENERAL PURPOSE BEAM OPTICS CODE



For circular machines, beam lines and linacs...

- ▶ **Describe/document** optics parameters from machine description.
- ▶ **Design** a lattice for getting the desired properties (**matching**).
- ▶ **Simulate** beam dynamics, machine imperfections and machine operation.

A GENERAL PURPOSE BEAM OPTICS CODE

MAD-X is

- ▶ **multiplatforms** (Linux/OSX/WIN...),
- ▶ very **flexible** and easy to extend,
- ▶ made for complicated applications, **powerful** and rather complete,
- ▶ mainly designed **for large projects** (LEP, LHC, CLIC...).

MAD-X is **NOT**

- ▶ a program for teaching,
- ▶ (very) easy to use for beginners,
- ▶ coming with a graphical user interface.

IN LARGE PROJECTS (E.G., LHC):

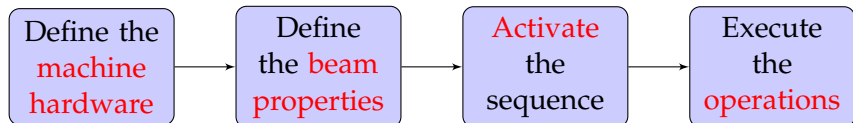


- ▶ Must be able to handle machines with $\geq 10^4$ elements,
- ▶ many simultaneous MAD-X users (LHC: more than 400 around the world): need consistent database,
- ▶ if you have many machines: ideally use only one design program.

DESCRIBE AN ACCELERATOR IN MAD-X

Goals...

- ▶ **Describe, optimize and simulate** a machine with several thousand elements eventually with magnetic elements shared by different beams, like in colliders.



MAD-X LANGUAGE

How does MAD-X get this info? Via text (**interpreter**).

- ▶ It accepts and executes statements, expressions...
- ▶ it can be used interactively (**input from command line**) or in batch (**input from file**),
- ▶ many features of a programming language (loops, if's, ...).

All input statements are analysed by a parser and checked.

- ▶ E.g. **assignments**: properties of machine elements, set up of the lattice, definition of beam properties, errors...
- ▶ E.g. **actions**: compute lattice functions, optimize and correct the machine...

MAD-X INPUT LANGUAGE

- ▶ **Strong resemblance to "C" language** (but NO need for declarations and NOT case sensitive apart in expressions in inverted commas),
- ▶ free format, all statements are terminated with **;** (do not forget!),
- ▶ comment lines start with: **//** or **!** or is between **/*...*/**,
- ▶ Arithmetic expressions, including basic functions (**exp**, **log**, **sin**, **cosh**...), built-in random number generators and predefined constants (speed of the light, e , π , m_p , m_e ...).

In particular it is possible to use deferred assignments

- ▶ regular assignment: **a = b**, if **b** changes **a** does not,
- ▶ deferred assignment: **a := b**, if **b** changes **a** is updated too.

EXAMPLE: DEFERRED ASSIGNMENTS

```
Terminal -- bash -- 87x33
+++++
+          MAD-X 4.00.19          +
+      Production Version      +
+ Code Modification Date: 04.05.2009 +
+ Execution Time Stamp: 06.01.10 11.10.52 +
+++++
a=1;

b=a;

c:=a;

a=2;

+++++ info: a redefined
value a;

a =          2 ;
value b;

b =          1 ;
value c;

c =          2 ;
quit;

Number of warnings: 0

+++++
+ MAD-X 4.00.19 Finished normally +
+++++
cosmos:examples sterbini$
```

We use the **value** command to print the variables content.

DEFINITIONS OF THE LATTICE ELEMENTS

Generic pattern to define an element:

label: *keyword*, *properties*...;

- ▶ For a dipole magnet:
MBL: **SBEND**, **L=10.0**;
- ▶ For a quadrupole magnet:
MQ: **QUADRUPOLE**, **L=3.3**;
- ▶ For a sextupole magnet:
MSF: **SEXTUPOLE**, **L=1.0**;

In the previous examples we considered only the **L** property, that is the length in meters of the element.

THE STRENGTH OF THE ELEMENTS

The name of the parameter that define the **normalized magnetic strength** of the element depends on the element type.

- ▶ For dipole (horizontal bending) magnet is k_0 :

$$k_0 = \frac{1}{B\rho} B_y \text{ [in m}^{-1}\text{]}$$

- ▶ For quadrupole magnet is k_1 :

$$k_1 = \frac{1}{B\rho} \frac{\partial B_y}{\partial x} \text{ [in m}^{-2}\text{]}$$

- ▶ For sextupole magnet is k_2 :

$$k_2 = \frac{1}{B\rho} \frac{\partial^2 B_y}{\partial x^2} \text{ [in m}^{-3}\text{]}$$

EXAMPLE: DEFINITIONS OF ELEMENTS

- ▶ Sextupole magnet:

`ksf = 0.00156;`

MSF: `SEXTUPOLE, K2 = ksf, L=1.0;`

- ▶ Multipole magnet "thin" element:

MMQ: `MULTIPOLE, KNL = {k0 · l, k1 · l, k2 · l, k3 · l, ... };`

- ▶ LHC dipole magnet as **thick** element:

`length = 14.3;`

`p = 7000;`

`angleLHC = 8.33 * clight * length/p;`

MBL: `SBEND, ANGLE = angleLHC;`

THE LATTICE SEQUENCE

A lattice sequence is an ordered collection of machine elements. Each element has a position in the sequence that can be defined wrt the CENTRE, EXIT or ENTRY of the element and wrt the sequence start or the position of an other element:

```
label: SEQUENCE, REFER=CENTRE, L=length;
...;
...;
...here specify position of all elements...;
...;
...;
ENDSEQUENCE;
```

EXAMPLE OF SEQUENCE: LHC (TOO TOUGH?)

```

Terminal - vim - 114x36
640 MSS : SEXTUPOLE, L := 1.MSS, Kmax := Kmax_MSS, Kmin := Kmin_MSS, Calib := Kmax_MSS / Imax_MSS;
641 //----- SOLENOID -----
642 MBAS2 : SOLENOID, L := 1.MBAS2;
643 MBCS2 : SOLENOID, L := 1.MBCS2;
644 MBLS2 : SOLENOID, L := 1.MBLS2;
645 //----- VCORRECTOR -----
646 MCBVC : VCORRECTOR, L := 1.MCBVC, Kmax := Kmax_MCBVC, Kmin := Kmin_MCBVC, Calib := Kmax_MCBVC / Imax_MCBVC;
647 MCBV : VCORRECTOR, L := 1.MCBV, Kmax := Kmax_MCBV, Kmin := Kmin_MCBV, Calib := Kmax_MCBV / Imax_MCBV;
648 MCBWV : VCORRECTOR, L := 1.MCBWV, Kmax := Kmax_MCBWV, Kmin := Kmin_MCBWV, Calib := Kmax_MCBWV / Imax_MCBWV;
649 MCBXV : VCORRECTOR, L := 1.MCBXV, Kmax := Kmax_MCBXV, Kmin := Kmin_MCBXV, Calib := Kmax_MCBXV / Imax_MCBXV;
650 MCBYV : VCORRECTOR, L := 1.MCBYV, Kmax := Kmax_MCBYV, Kmin := Kmin_MCBYV, Calib := Kmax_MCBYV / Imax_MCBYV;
651 //----- VKICKER -----
652 MBAW : VKICKER, L := 1.MBAW, Kmax := Kmax_MBAW, Kmin := Kmin_MBAW, Calib := Kmax_MBAW / Imax_MBAW;
653 MBWMD : VKICKER, L := 1.MBWMD, Kmax := Kmax_MBWMD, Kmin := Kmin_MBWMD, Calib := Kmax_MBWMD / Imax_MBWMD;
654 MBXWT : VKICKER, L := 1.MBXWT, Kmax := Kmax_MBXWT, Kmin := Kmin_MBXWT, Calib := Kmax_MBXWT / Imax_MBXWT;
655
656 //----- LHC SEQUENCE -----
657 LHCb1 : SEQUENCE, refer = CENTRE, L = LHLENGTH;
658 IP1:OMK,
659   at = pIP1+IP1OFS.B1*DS,
660   mech_sep = 0, slot_id = 2209454,
661   TAS.1R1:TAS,
662   at = 20.015+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 102103,
663   BPMSW.1R1:B1:BPMSW,
664   at = 21.475+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 104594,
665   MQXA.1R1:MQXA,
666   at = 26.15+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 282126, assembly_id = 102104,
667   MCBXH.1R1:MCBXH,
668   at = 29.842+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 282213, assembly_id = 102104,
669   MCBXV.1R1:MCBXV,
670   at = 29.842+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 282212, assembly_id = 102104,
671   BPMS.2R1:B1:BPMS,
672   at = 31.529+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 241889, assembly_id = 102105,
673   MQXB.A2R1:MQXB,
674   at = 34.8+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 241890, assembly_id = 102105,
675   MCBXH.2R1:MCBXH,
676   at = 38.019+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 249450, assembly_id = 102105,
677   MCBXV.2R1:MCBXV,
678   at = 38.019+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 249451, assembly_id = 102105,
679   MQXB.B2R1:MQXB,
680   at = 41.3+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 241892, assembly_id = 102105,
681   TASB.3R1:TASB,
682   at = 45.342+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 241893, assembly_id = 102106,
683   MQSX.3R1:MQSX,
684   at = 46.608+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 282127, assembly_id = 102106,
685   MQXA.3R1:MQXA,
686   at = 50.15+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 241895, assembly_id = 102106,
687   MCBXH.3R1:MCBXH,
688   at = 53.814+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 249456, assembly_id = 102106,
689   MCBXV.3R1:MCBXV,
690   at = 53.814+(0-IP1OFS.B1)*DS, mech_sep = 0, slot_id = 249457, assembly_id = 102106,

```


BEAM DEFINITION & SEQUENCE ACTIVATION

Generic pattern to define the beam:

label: **BEAM**, **PARTICLE**=x, **ENERGY**=y,...;

e.g., **BEAM**, **PARTICLE**=proton, **ENERGY**=7000;//in GeV

After a sequence has been read, it can be activated:

USE, **SEQUENCE**=sequence_label;

e.g., **USE**, **SEQUENCE**=lhc1;

The **USE** command expands the specified sequence, inserts the drift spaces and makes it active.

DEFINITION OF OPERATIONS

Once the sequence is activated we can perform operations on it.

- ▶ Calculation of Twiss parameters around the machine (**very important**) in order to know, for stable sequences, their main optical parameters.

TWISS, **SEQUENCE**=sequence_label;

- ▶ Production of graphical output of the main optical function (e.g., β -functions):

PLOT, **HAXIS**=s, **VAXIS**=betx,bety;

Example

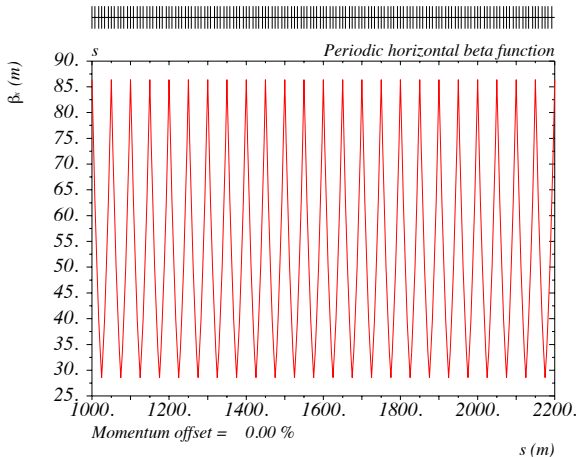
TWISS, **SEQUENCE**=juaseq, **FILE**=twiss.out;

PLOT, **HAXIS**=s, **VAXIS**=betx, bety, **COLOUR**=100;

EXAMPLE OF THE TWISS FILE

```
* NAME                S                BETX                BETY
$ %s                 %le                 %le                 %le
"QF"                 1.5425             107.5443191         19.4745051
"QD"                 33.5425            19.5134888          107.4973054
"QF"                 65.5425            107.5443191         19.4745051
"QD"                 97.5425            19.5134888          107.4973054
"QF"                 129.5425           107.5443191         19.4745051
"QD"                 161.5425           19.5134888          107.4973054
"QF"                 193.5425           107.5443191         19.4745051
"QD"                 225.5425           19.5134888          107.4973054
"QF"                 257.5425           107.5443191         19.4745051
"QD"                 289.5425           19.5134888          107.4973054
"QF"                 321.5425           107.5443191         19.4745051
"QD"                 353.5425           19.5134888          107.4973054
"QF"                 385.5425           107.5443191         19.4745051
"QD"                 417.5425           19.5134888          107.4973054
"QF"                 449.5425           107.5443191         19.4745051
"QD"                 481.5425           19.5134888          107.4973054
"QF"                 513.5425           107.5443191         19.4745051
"QD"                 545.5425           19.5134888          107.4973054
"QF"                 577.5425           107.5443191         19.4745051
"QD"                 609.5425           19.5134888          107.4973054
....
....
```

EXAMPLE OF THE GRAPHICAL OUTPUT (PS FORMAT)



MATCHING GLOBAL PARAMETERS

It is possible to modify the optical parameters of the machine using the MATCHING module of MAD-X.

- ▶ Adjust magnetic strengths to get desired properties (e.g., tune Q, chromaticity dQ),
- ▶ Define the **properties** to match and the **parameters** to vary.

Example:

```
MATCH, SEQUENCE=sequence_name;  
  GLOBAL, Q1=26.58; // H-tune  
  GLOBAL, Q2=26.62; // V-tune  
  VARY, NAME= kqf, STEP=0.00001;  
  VARY, NAME = kqd, STEP=0.00001;  
  LMDIF, CALLS=50, TOLERANCE=1e-6; // method adopted  
ENDMATCH;
```


GENERAL CONSIDERATIONS ON MAD-X SYNTAX

Input language seems heavy, but:

- ▶ can be interfaced to data base and to other programs (e.g., MathematicaTM, MatlabTM...),
- ▶ programs exist to generate the input interactively,
- ▶ allows web based applications,
- ▶ allows interface to operating system.

MAD-X can estimate the machine performance by:

- ▶ studying of long term stability with multipolar component,
- ▶ taking into account the tolerances for machine elements,
- ▶ simulating operation of the machine (imperfections,...).

DO WE USE MAD-X FOR EVERYTHING? **NO!**

MAD-X is an **optics** program (**single particle dynamics**).

MAD-X has limitations where

- ▶ **multi particle and multi bunch** simulations are required,
- ▶ **machine is not static**, i.e., beam changes its own environment (space charge, instabilities, beam-beam effects...),
- ▶ requires self-consistent treatment, **computation of fields and forces**,
- ▶ execution **speed** is an issue,
- ▶ for detailed studies dedicated programs are needed, **but often with I/O interface to MAD-X**.

SOME USEFUL TIPS FOR THE TUTORIALS (WIN)

Additional software needed...

- ▶ Most of the input/output of MADX is in ASCII files: you can read/write/edit them using **Notepad++**. The graphical output of MAD is on PS format: you can use **Evince** to open it.

Tricks for beginners:

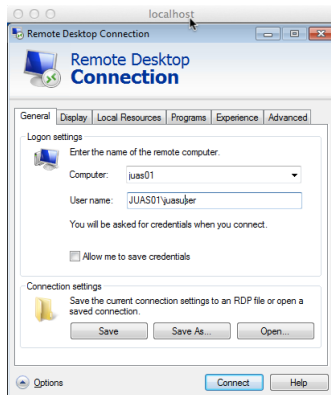
- ▶ a working MAD-X environment has been set up for you
- ▶ to make all happy, we will use a unix-like shell (**Cygwin**) in a WIN OS.
- ▶ once you have the input (e.g., **whatever.inp**), execute it by:
 - ▶ 1. "CALL, FILE=**whatever.inp**;" at the **MADX prompt**,
 - ▶ 2. **madx<whatever.inp**" at the **shell (preferred)**.

REMOTE CERN MACHINES (SOMEONE MISSING?)

Family name	Name	Remote machine
ABREU FERNANDES	Miguel Filipe	JUAS01
AZIZI	Roxana	JUAS02
BANFI	Damilo	JUAS03
BARTOZIK	Marcin	JUAS04
BATTAGLIA	Giorgio	JUAS05
BEN ZID	Oussema	JUAS06
BRACCALENTI	Edoardo	JUAS07
CIAMBRELLA	Massimo	JUAS08
CRUZ ALANIZ	Emilia	JUAS09
DAYYANI KELISANI	Mohsen	JUAS10
EL MHARI	Charaf	JUAS11
ESTEBAN MARTI	Sergi	JUAS12
FRASCIELLO	Oscar	JUAS13
GINER NAVARRO	Jorge	JUAS14
HAJ TAHAR	Malek	JUAS15
HOFMANN	Thomas	JUAS16
HUSCHAUER	Alexander	JUAS17
KALAMAİKO	Anatolli	JUAS18
KRAMMER	Jakob	JUAS19
KRAUS	Ingrid	JUAS20
KURICHIYANIL	Neeraj	JUAS21
LA FERLA	Marco	JUAS22
LABUSSIERE	Etienne	JUAS23
LAGIER	Stphane	JUAS24
LEDERER	Stephan	JUAS25
LEO	Stefano	JUAS26
LIEBERWIRTH	Alice	JUAS27
MEREGHETTI	Alessio	JUAS28
NAVARRO QUIRANTE	Jose Luis	JUAS29
NAVEED	Sehar	JUAS30
NUEL GAVALDA	Xavier	JUAS31
PAPADOPOULOU	Stefania	JUAS32
PATECKI	Marcin	JUAS33
PATEL	Vivek	JUAS34
RAJABI	Ali	JUAS35
RAUCY	Christopher	JUAS36
REY	Solenne	JUAS37
SANAYE HAJARI	Shahin	JUAS38
SOFANAC	Martina	JUAS39
STEINMANN	Johannes	JUAS40
TAKABATAKE	Mao	JUAS41
UNGETHM	Carina	JUAS42
ZHENG	Dawei	JUAS43
ZWICKER	Benjamin	JUAS44

ACCESS REMOTE MACHINE JUASXX

- ▶ Computer: JUASXX
- ▶ User: JUASXX\juasuser
- ▶ PWD: Juas12User
- ▶ Cygwin (UNIX shell in WIN). From the shell with the command "open" you open the Win Explorer (edit inp, read out)
- ▶ Use your assigned PC!



"HELLO WORLD!" INPUT FILE

```
Terminal - vim -- 105x36
1 /****Definition of elements****/
2 qfType:QUADRUPOLE, L=1.5, K1:=kf;
3 qdType:QUADRUPOLE, L=1.5, K1:=kd;
4
5 /****Definition of the sequence****/
6 fodo:SEQUENCE, REFER=exit, L=10;
7 qf: qfType, at=5;
8 qd: qdType, at=10;
9 ENDSEQUENCE;
10
11 /****Definition of the strength****/
12 kf=+0.2985;
13 kd=-0.2985;
14
15 /****Definition of the beam****/
16 beam, particle=proton, energy=7001;
17
18 /****Activation of the sequence****/
19 use, sequence=fodo;
20
21 /****Operations****/
22 twiss;
23 plot, HAXIS=s, VAXIS=betx, bety;
24
25 /****Matching****/
26 MATCH, sequence=fodo;
27   GLOBAL, Q1=.25;
28   GLOBAL, Q2=.25;
29   VARY, NAME=kf, STEP=0.00001;
30   VARY, NAME=kd, STEP=0.00001;
31   LMDIF, CALLS=50, TOLERANCE=1e-8;
32 ENDMATCH;
33
34 /****Best Regards****/
35 QUIT
"fodo.mad" 35L, 689C
```

“HELLO WORLD!” OUTPUT (1)

```
Terminal — bash — 105x36
cosmos:examples sterbini$ madx<fodo.mad

+++++
+          MAD-X 4.00.19          +
+      Production Version      +
+ Code Modification Date: 04.05.2009  +
+ Execution Time Stamp: 07.01.10 12.04.00 +
+++++
/****Definition of elements****/

qfType:QUADRUPOLE, L=1.5, K1:=kf;

qdType:QUADRUPOLE, L=1.5, K1:=kd;

/****Definition of the sequence****/

fodo:SEQUENCE, REFER=exit, L=10;

qf: qfType, at=5;

qd: qdType, at=10;

ENDSEQUENCE;

/****Definition of the strength****/

kf=+0.2985;

kd=-0.2985;
```

"HELLO WORLD!" OUTPUT (2)

```

Terminal — bash — 105x36
/****Definition of the beam****/
beam, particle=proton, energy=7001;

/****Activation of the sequence****/
use, sequence=fodo;

/****Operations****/
twiss;

enter Twiss module
+++++ info: Zero value of SIGT replaced by 1.
+++++ info: Zero value of SIGE replaced by 1/1000.

iteration: 1 error: 0.000000E+00 deltap: 0.000000E+00
orbit: 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00

+++++ table: summ

      length      orbit5      alfa      gammatr
      10          -0      -3.30872245e-24  -5.497558139e+11

      q1          dq1          betxmax      dxmax
0.4877944671    -8.265035446      208.1244543      0

      dxrms      xcomax      xcorms      q2
      0          0          0          0.4877944671

      dq2          betymax      dymax      dyrms
-8.265035446    208.1244543      0          0

```

"HELLO WORLD!" OUTPUT (3)

```

Terminal — bash — 105x36
twiss;

enter Twiss module
+++++ info: Zero value of SIGT replaced by 1.
+++++ info: Zero value of SIGE replaced by 1/1000.

iteration: 1 error: 0.000000E+00 deltap: 0.000000E+00
orbit: 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00

+++++ table: summ

      length      orbit5      alfa      gammatr
      10          -0      -3.30872245e-24      -5.497558139e+11

      q1          dq1          betxmax          dxmax
0.4877944671      -8.265035446      208.1244543          0

      dxrms          xcomax          xcorms          q2
0          0          0          0.4877944671

      dq2          betymax          dymax          dyrms
-8.265035446      208.1244543          0          0

      ycomax          ycorms          deltap          synch_1
0          0          0          0

      synch_2          synch_3          synch_4          synch_5
0          0          0          0

plot, HAXIS=s, VAXIS=betx, bety;

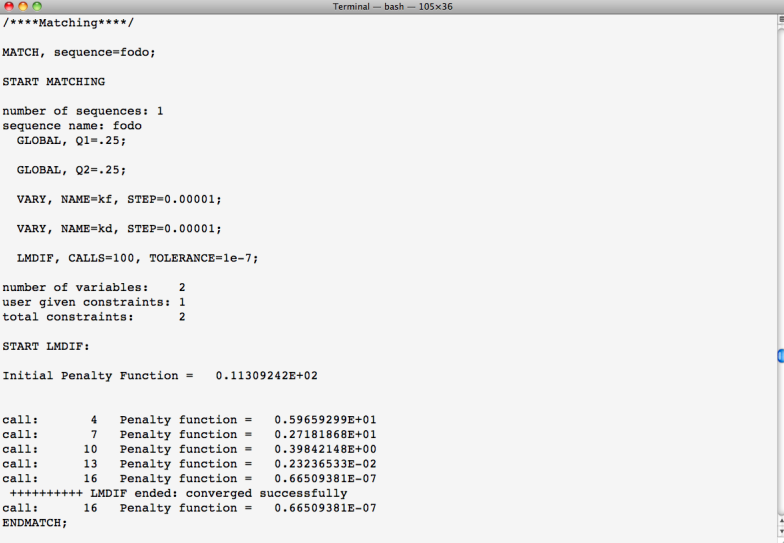
+++++ info: Zero value of SIGT replaced by 1.
+++++ info: Zero value of SIGE replaced by 1/1000.

GX PLOT-X11 1.50 initialized

plot number = 1

```

"HELLO WORLD!" OUTPUT (4)



```
Terminal — bash — 105x36
/****Matching****/

MATCH, sequence=fodo;

START MATCHING

number of sequences: 1
sequence name: fodo
  GLOBAL, Q1=.25;

  GLOBAL, Q2=.25;

  VARY, NAME=kf, STEP=0.00001;

  VARY, NAME=kd, STEP=0.00001;

  LMDIF, CALLS=100, TOLERANCE=1e-7;

number of variables: 2
user given constraints: 1
total constraints: 2

START LMDIF:

Initial Penalty Function = 0.11309242E+02

call:      4  Penalty function = 0.59659299E+01
call:      7  Penalty function = 0.27181868E+01
call:     10  Penalty function = 0.39842148E+00
call:     13  Penalty function = 0.23236533E-02
call:     16  Penalty function = 0.66509381E-07
+++++++ LMDIF ended: converged successfully
call:     16  Penalty function = 0.66509381E-07
ENDMATCH;
```


"HELLO WORLD!" OUTPUT (5)

```

Terminal — bash — 105x36

MATCH SUMMARY

Node_Name           Constraint  Type  Target Value      Final Value      Penalty
-----
Global constraint:  q1         4     2.50000000E-01    2.50018141E-01    3.29107276E-08
Global constraint:  q2         4     2.50000000E-01    2.50018330E-01    3.35986532E-08

Final Penalty Function = 6.65093808e-08

Variable           Final Value  Initial Value  Lower Limit  Upper Limit
-----
kf                 2.11034e-01  2.98500e-01  -1.00000e+20  1.00000e+20
kd                -2.11034e-01 -2.98500e-01 -1.00000e+20  1.00000e+20

END MATCH SUMMARY

VARIABLE "TAR" SET TO 6.65093808e-08

/****Best Regards****/

QUIT;

Number of warnings: 0

+++++
+ MAD-X 4.00.19 Finished normally +
+++++

```