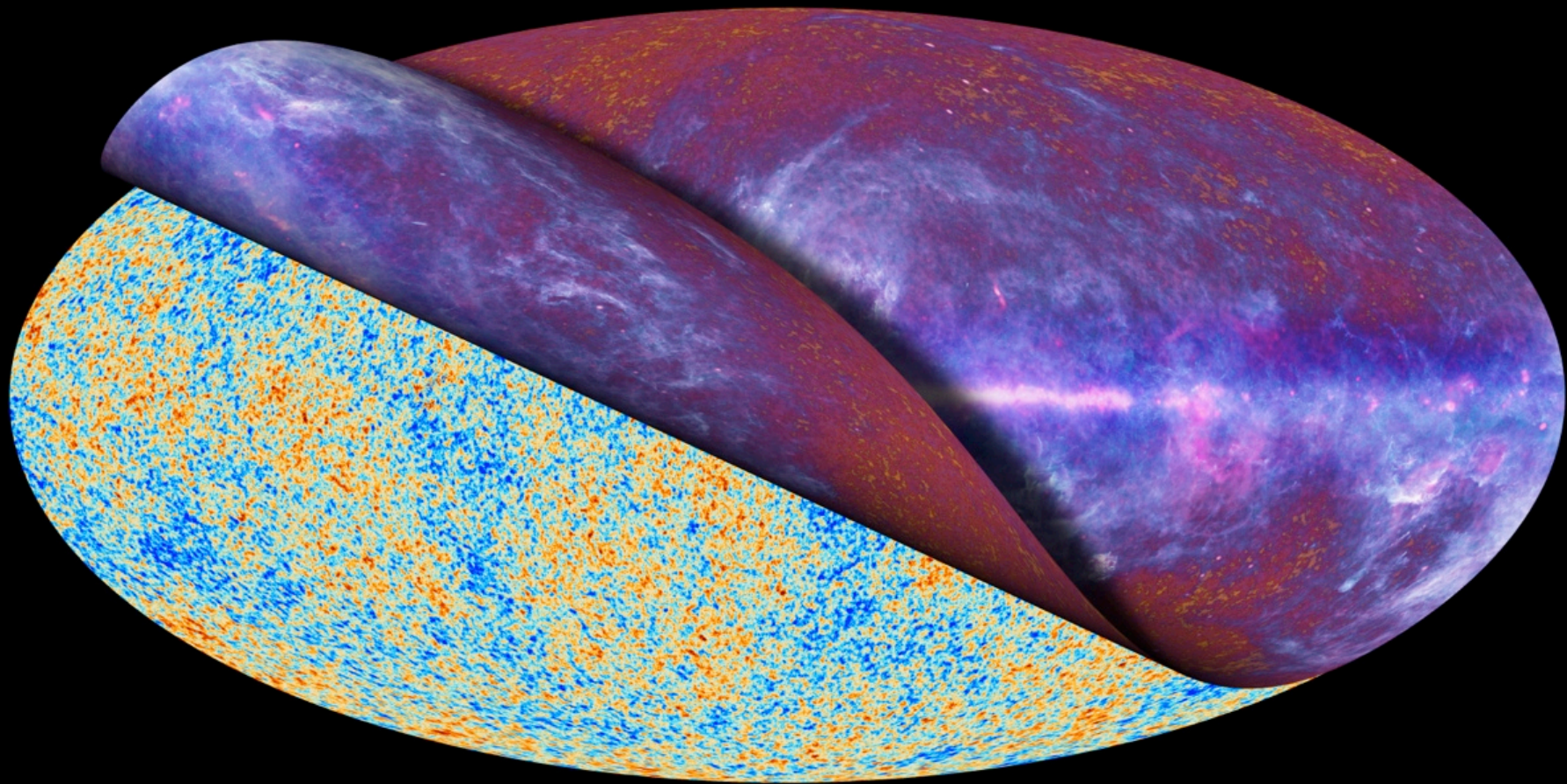




planck



**Planck unveils the Cosmic Microwave Background**

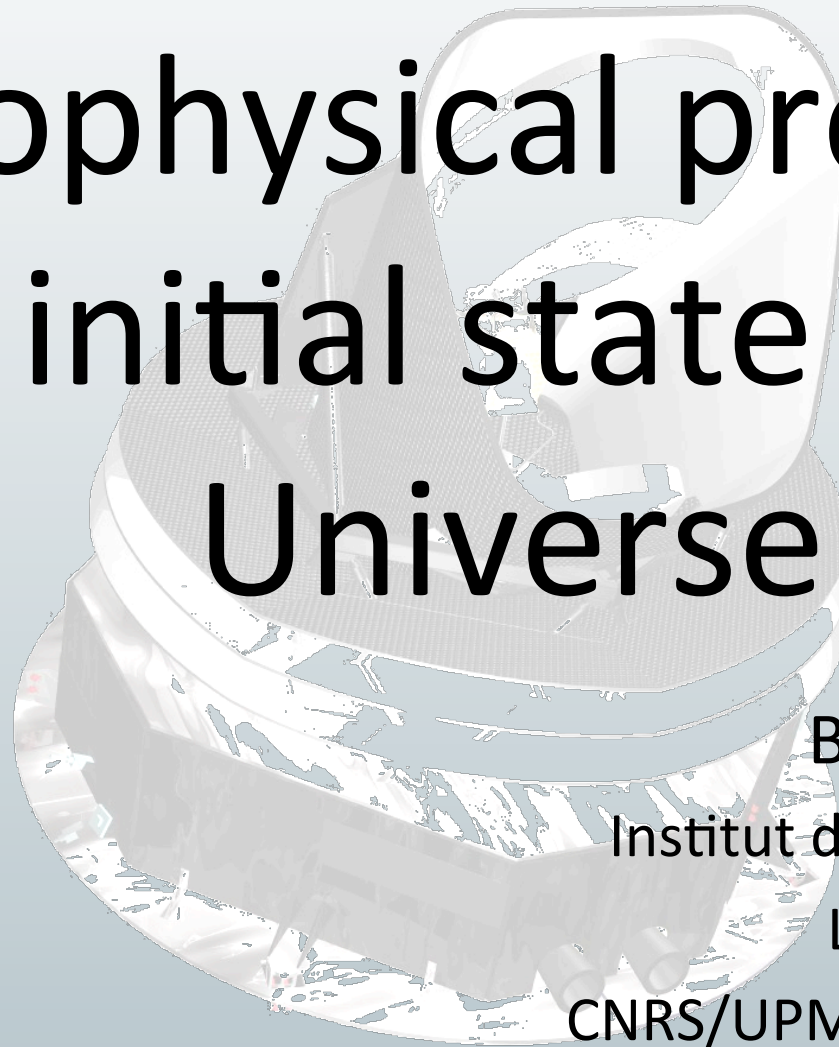
The scientific results from Planck are a product of the Planck Collaboration, including individuals from more than 100 scientific institutes in Europe, the USA and Canada



Planck is a project of the European Space Agency, with instruments provided by two scientific Consortia funded by ESA member states (in particular the lead countries: France and Italy) with contributions from NASA (USA), and telescope reflectors provided in a collaboration between ESA and a scientific Consortium led and funded by Denmark.



# Astrophysical probes of the initial state of the Universe



Benjamin D. Wandelt  
Institut d'Astrophysique de Paris  
Lagrange Institute, Paris  
CNRS/UPMC, Sorbonne University

On behalf of the Planck collaboration

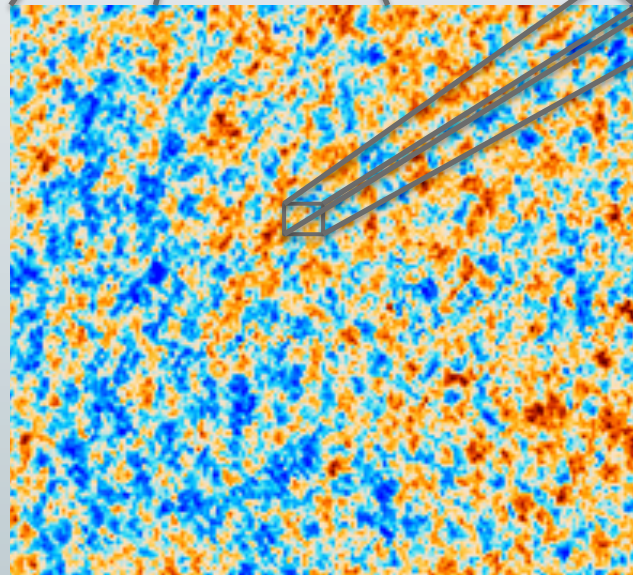
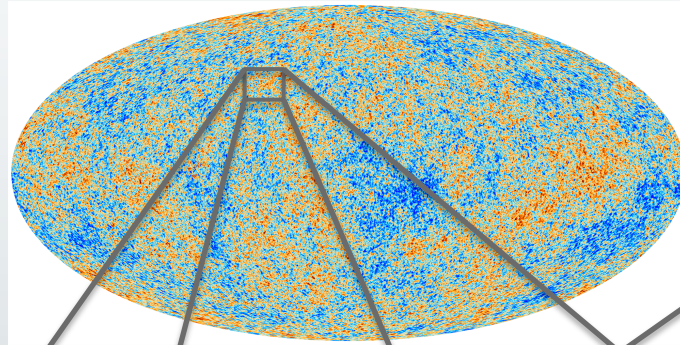




# The Big Picture

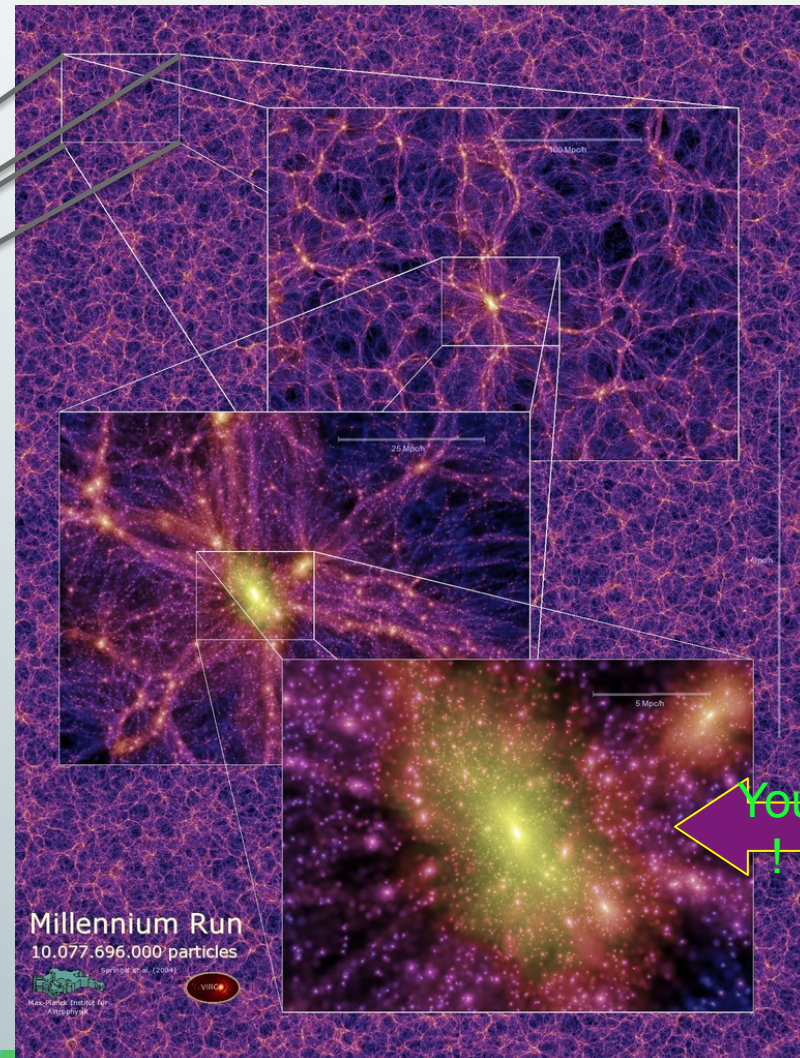


Planck



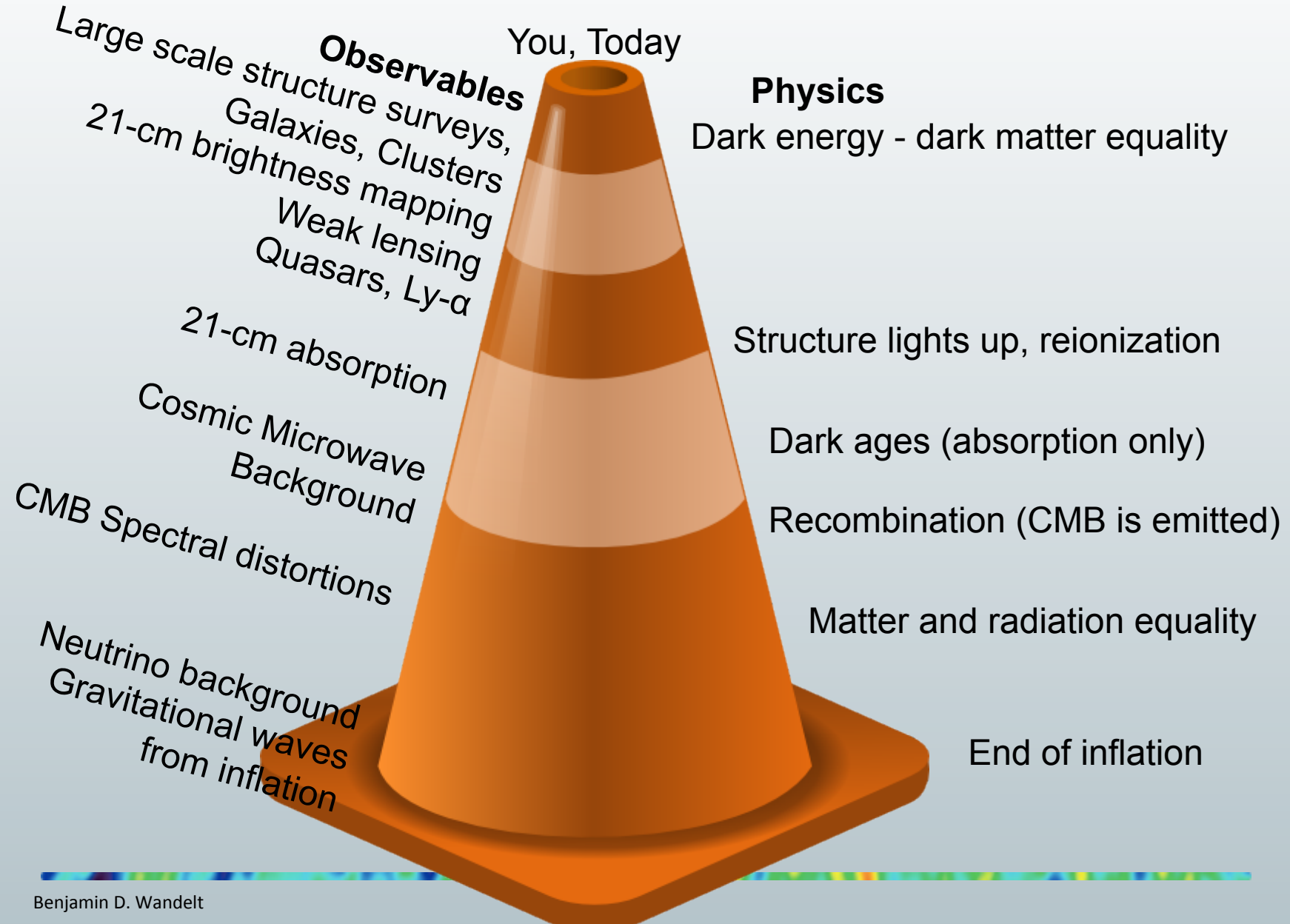
Primordial quantum perturbations as seen in the Cosmic Microwave Background

Dark matter distribution today (simulated)





# What is ultimately observable?





# Cosmology questions



**How did the Universe begin?**

**How did structure appear in the Universe?**

How did it evolve until today?

What is the Universe made of?

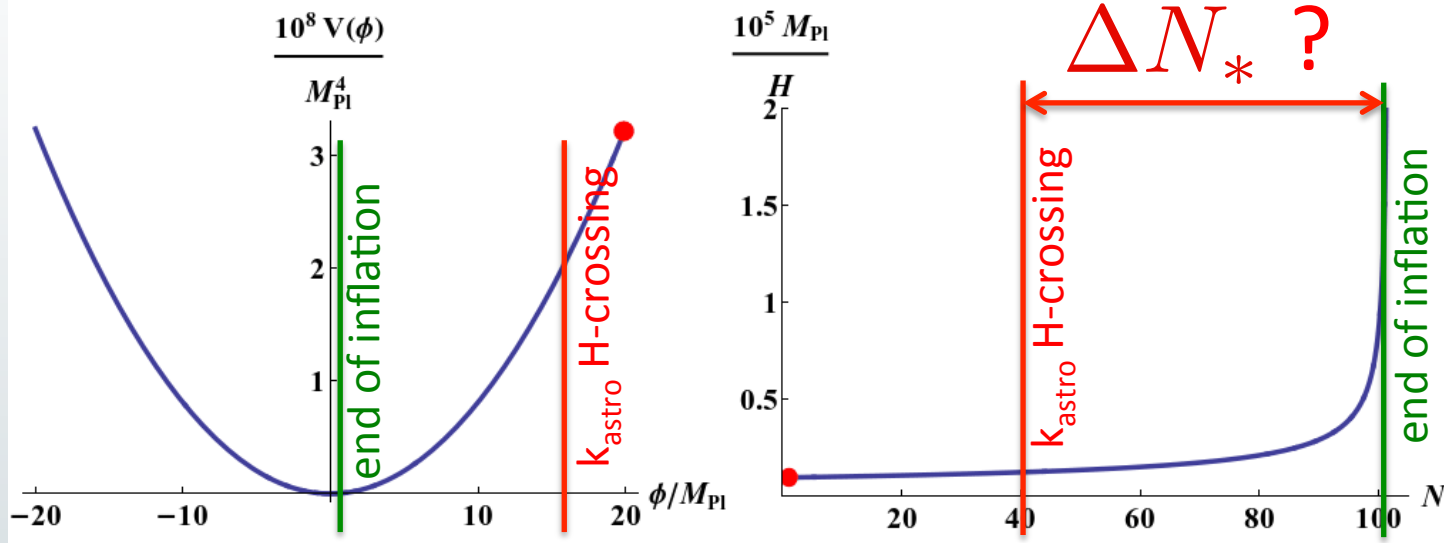
What are the properties of dark matter?

What are the properties of dark energy?

What is the geometry of the Universe?

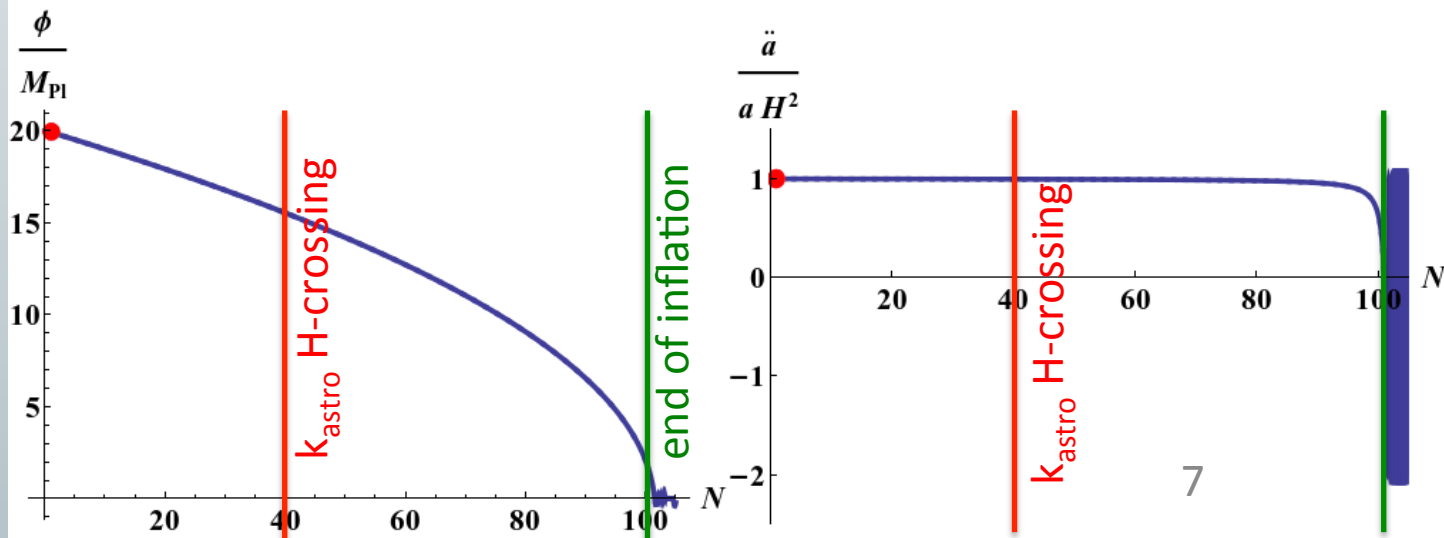
Is the Universe “symmetric?”

# Paradigm: Inflation



An example: « large field inflation »

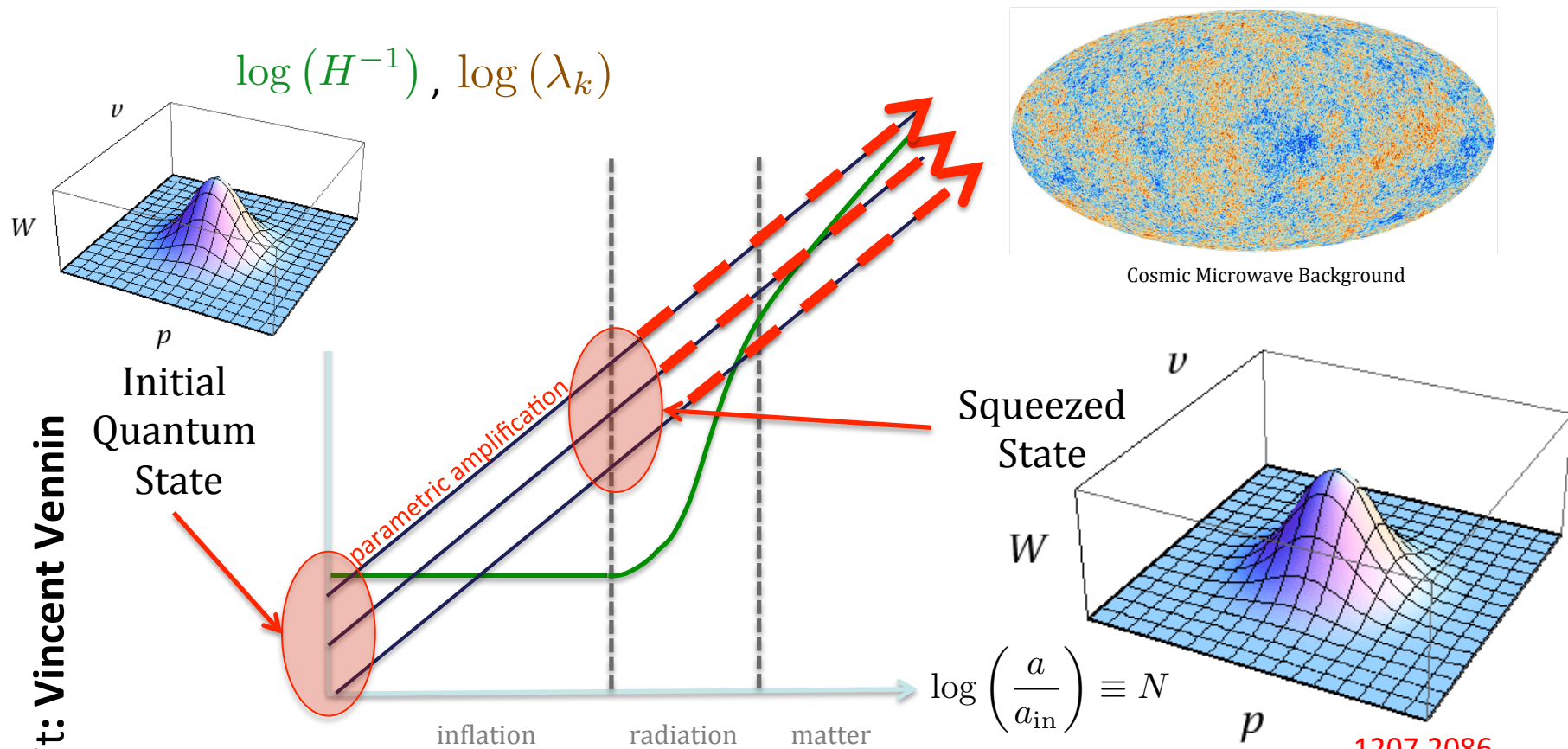
$$V(\phi) = \frac{m^2}{2} \phi^2$$



credit: Vincent Vennin

# Cosmological Inflation

Quantized fluctuations evolved over an expanding background



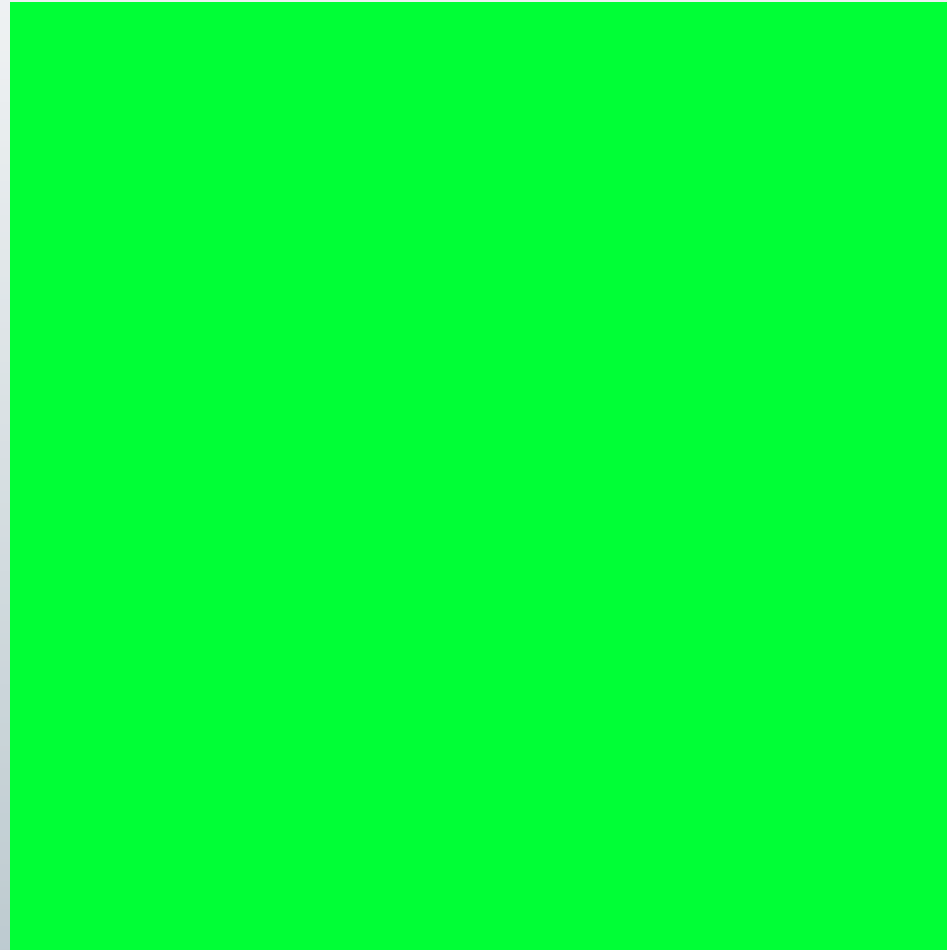
credit: Vincent Vennin

1207.2086  
J.Martin, Vincent  
Vennin & P.Peter

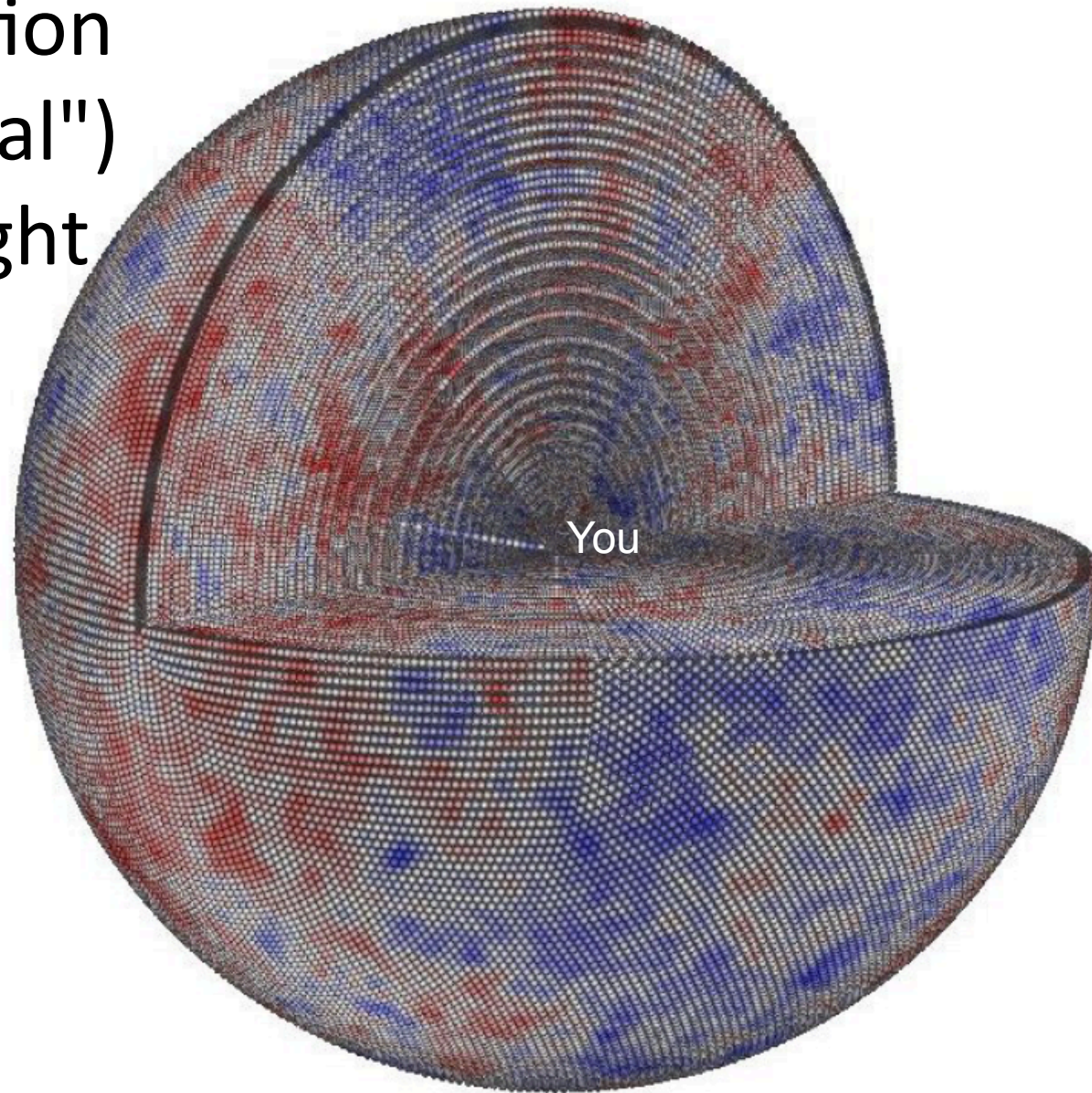




# Paradigm: perturbations arise from quantum fluctuations

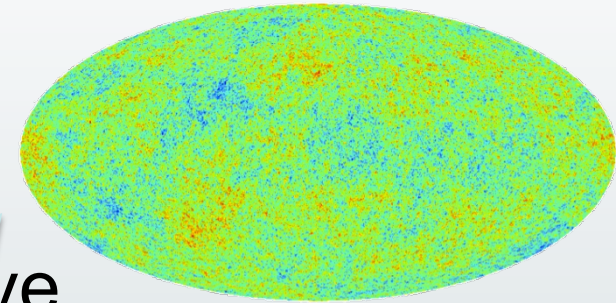
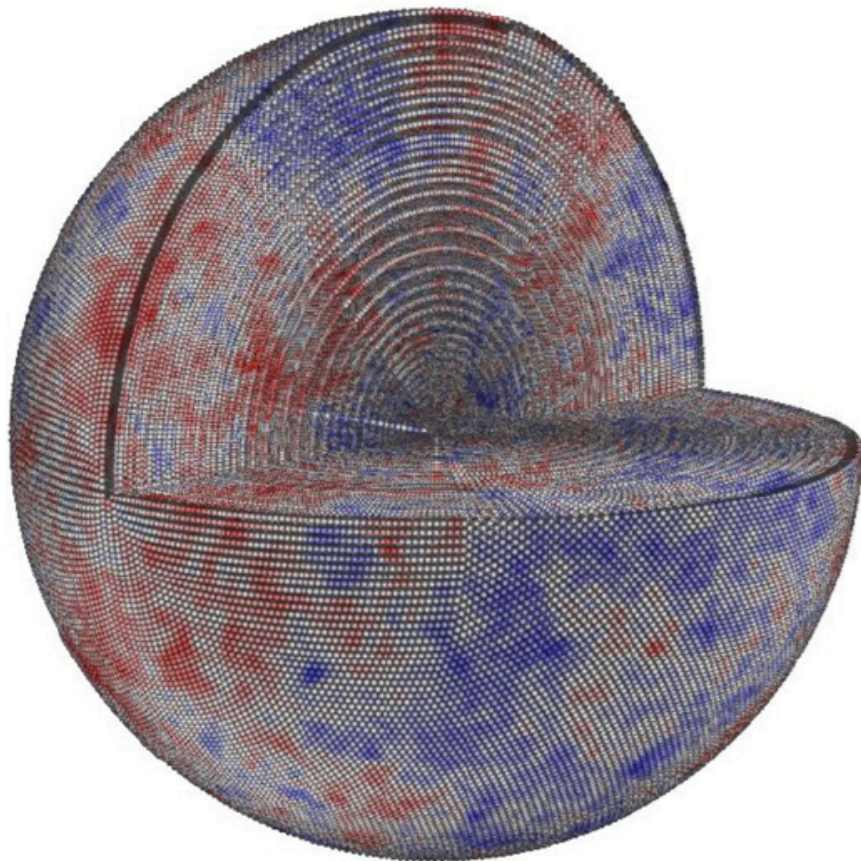


# Curvature perturbation ("potential") on the light cone





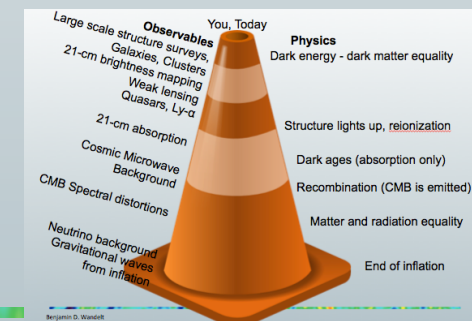
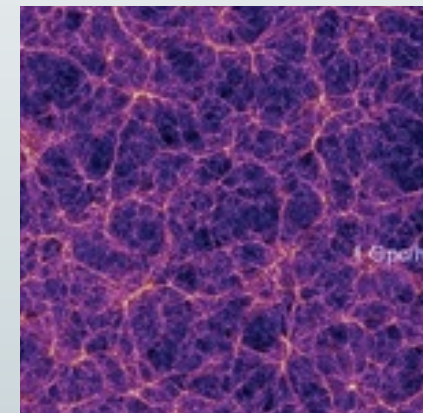
# Primordial perturbations give rise to observations



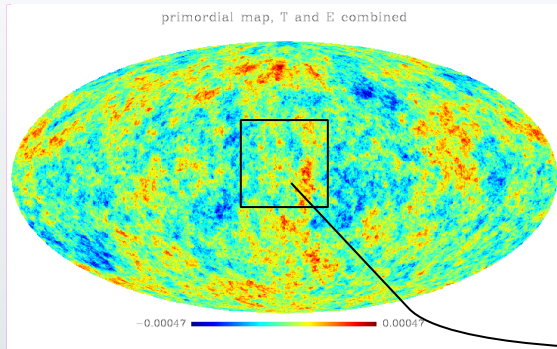
Radiative Transfer

Gravity

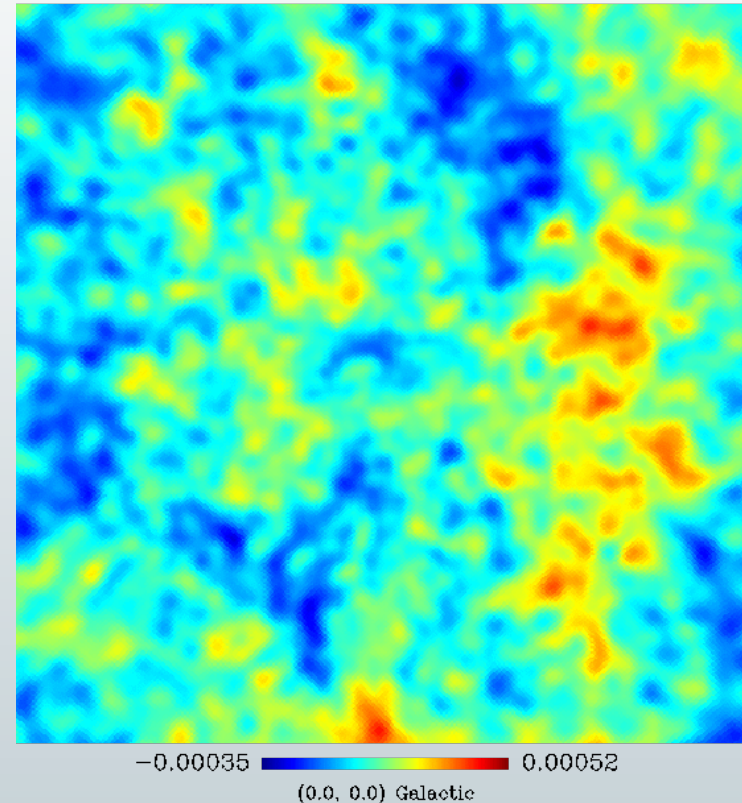
Astro-physics



# The linear physics CMB time machine



## Primordial curvature fluctuations

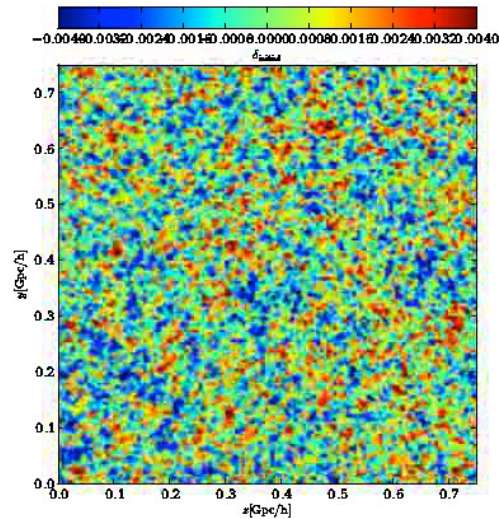


- The CMB T&E anisotropies map the Universe at  $t=380,000$
- By "inverting" linear physics we can infer primordial curvature perturbation and test model predictions for the power spectrum and beyond.

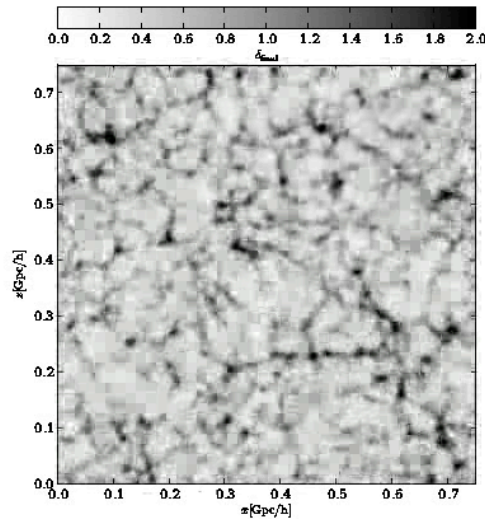
Komatsu, Spergel, Wandelt (2005)  
Yadav and Wandelt, PRD (2005)

# Now building non-linear time machines

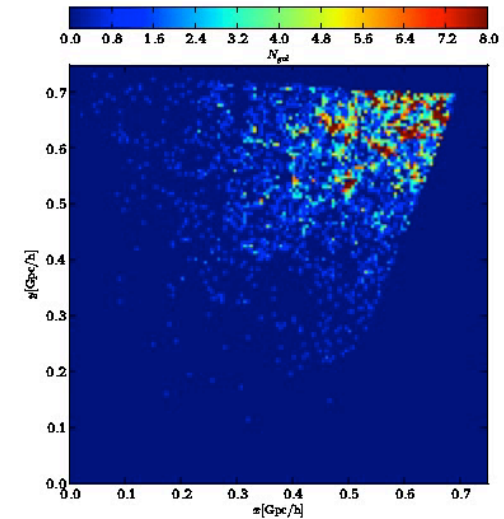
Reconstructed  
primordial density



Reconstructed non-linear  
density distribution today

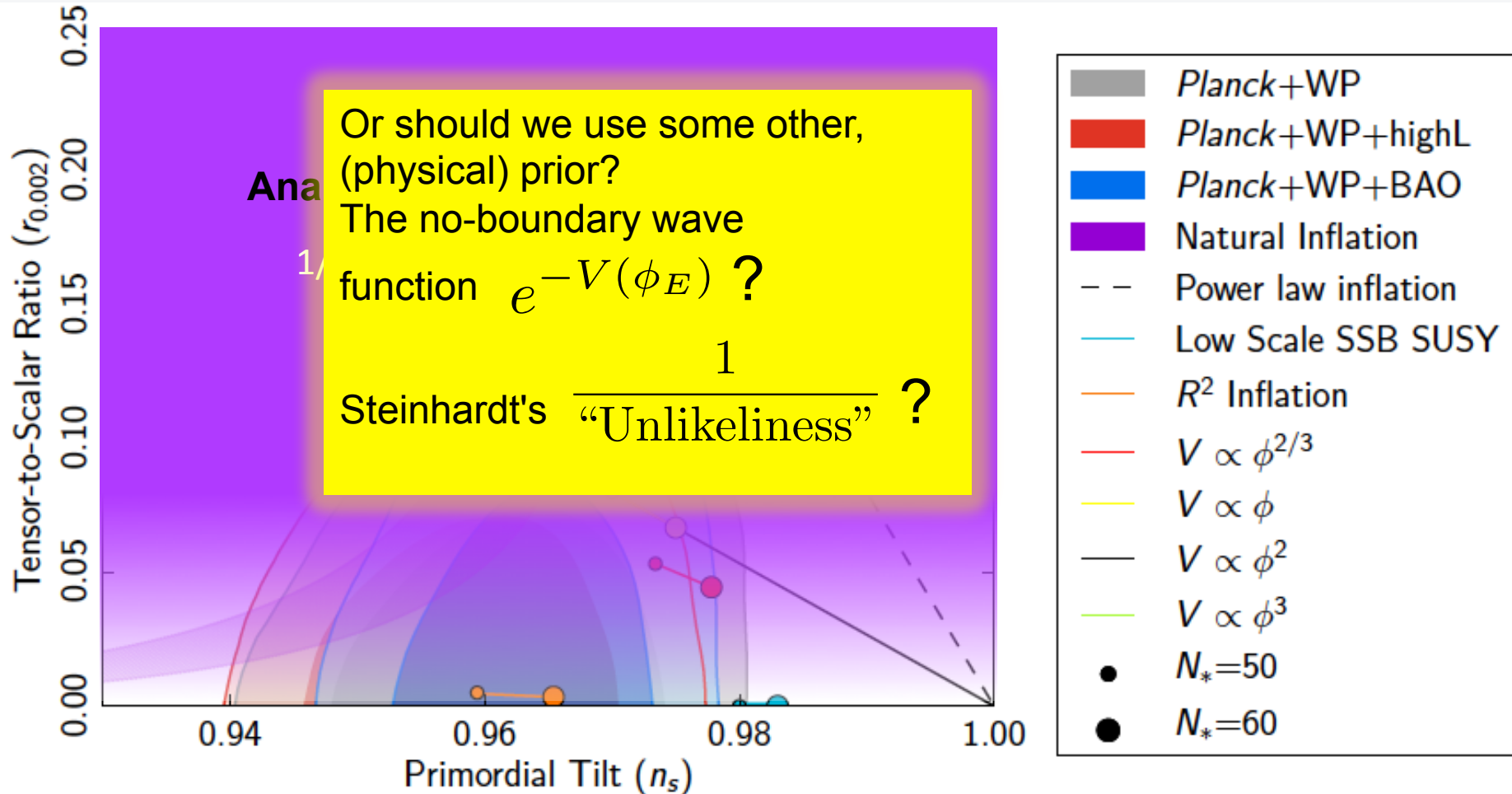


SDSS-like  
Galaxy mock



Animation shows uncertainties in Bayesian physical reconstruction of initial conditions from Large Scale Structure

Jasche & Wandelt, arXiv: 1203.3639



$$V_* < (1.94 \times 10^{16} \text{ GeV})^4$$



# Detecting tilt!

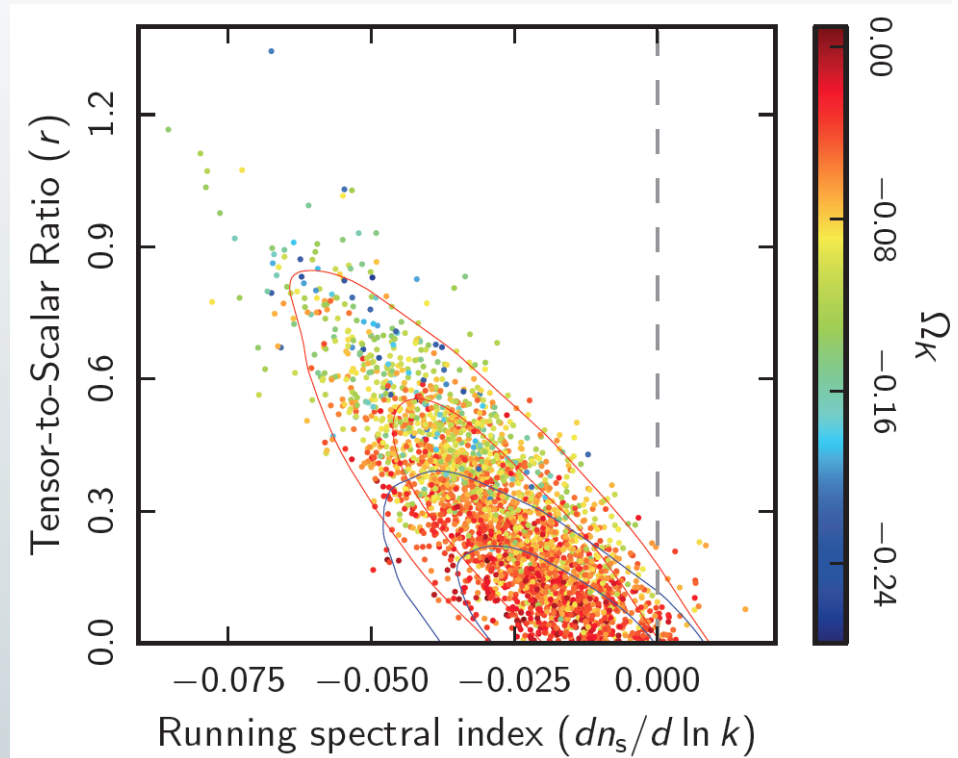


	HZ	HZ + $Y_p$	HZ + $N_{\text{eff}}$	$\Lambda$ CDM
$10^5 \Omega_b h^2$	$2296 \pm 24$	$2296 \pm 23$	$2285 \pm 23$	$2205 \pm 28$
$10^4 \Omega_c h^2$	$1088 \pm 13$	$1158 \pm 20$	$1298 \pm 43$	$1199 \pm 27$
$100 \theta_{\text{MC}}$	$1.04292 \pm 0.00054$	$1.04439 \pm 0.00063$	$1.04052 \pm 0.00067$	$1.04131 \pm 0.00063$
$\tau$	$0.125^{+0.016}_{-0.014}$	$0.109^{+0.013}_{-0.014}$	$0.105^{+0.014}_{-0.013}$	$0.089^{+0.012}_{-0.014}$
$\ln(10^{10} A_s)$	$3.133^{+0.032}_{-0.028}$	$3.137^{+0.027}_{-0.028}$	$3.143^{+0.027}_{-0.026}$	$3.089^{+0.024}_{-0.027}$
$n_s$	—	—	—	$0.9603 \pm 0.0073$
$N_{\text{eff}}$	—	—	$3.98 \pm 0.19$	—
$Y_p$	—	$0.3194 \pm 0.013$	—	—
$-2\Delta \ln(\mathcal{L}_{\text{max}})$	27.9	2.2	2.8	0

- Harrison-Zel'dovich spectrum ruled out robustly (w,  $\Sigma m_\nu$ , reionization)
- Allowing Helium abundance to float can rescue H-Z but at the cost of  $Y_p$  inconsistent with astrophysical constraints
- Main loophole is  $N_{\text{eff}}$

# The universe is (most likely) flat

- Inflation "predicts" flatness,  $|\Omega_k| \sim 10^{-5}$ , though open is possible. Closed is hard.
- Planck constraints are now at the  $10^{-3}$  level.
- With negative running *positive* curvature is possible. But large negative running is in conflict with 50 e-folds of inflation



$$\Omega_k = -0.0004 \pm 0.0036$$

(Planck+WP+BAO)

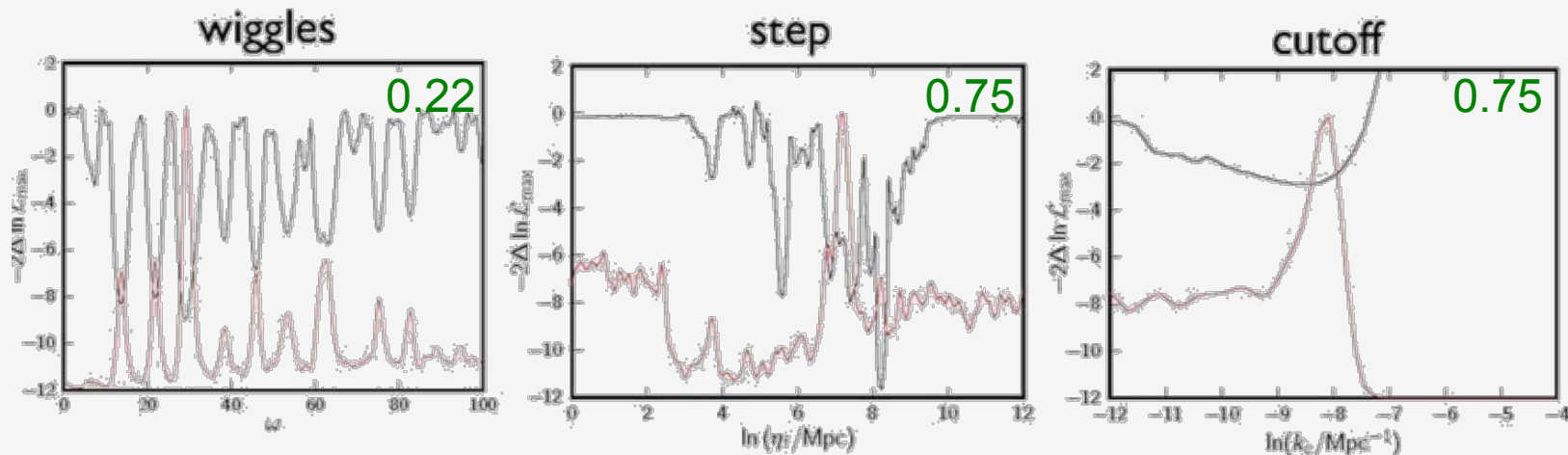


# Are there features in $P(k)$ ?

wiggles: 
$$\mathcal{P}_{\mathcal{R}}(k) = \mathcal{P}_0(k) \left\{ 1 + \alpha_w \sin \left[ \omega \ln \left( \frac{k}{k_*} \right) + \varphi \right] \right\}$$

step: 
$$\mathcal{P}_{\mathcal{R}}(k) = \exp \left[ \ln \mathcal{P}_0(k) + \frac{A_f}{3} \frac{k\eta_f/x_d}{\sinh(k\eta_f/x_d)} W'(k\eta_f) \right]$$

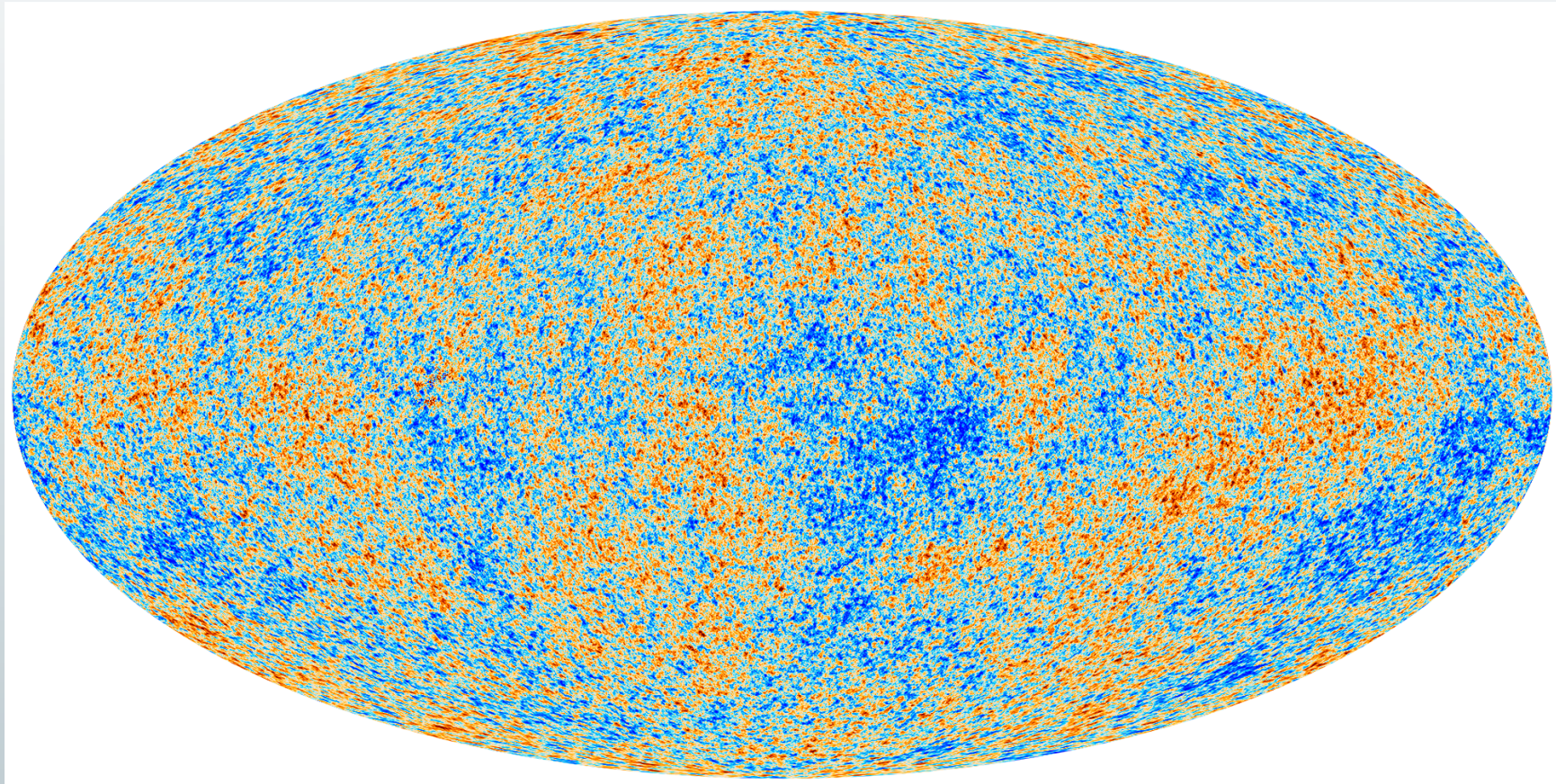
cutoff: 
$$\mathcal{P}_{\mathcal{R}}(k) = \mathcal{P}_0(k) \left\{ 1 - \exp \left[ - \left( \frac{k}{k_c} \right)^{\lambda_c} \right] \right\}$$



Bayesian evidence ratio compared to featureless model



# Back to the CMB map





# Why non-Gaussianity?



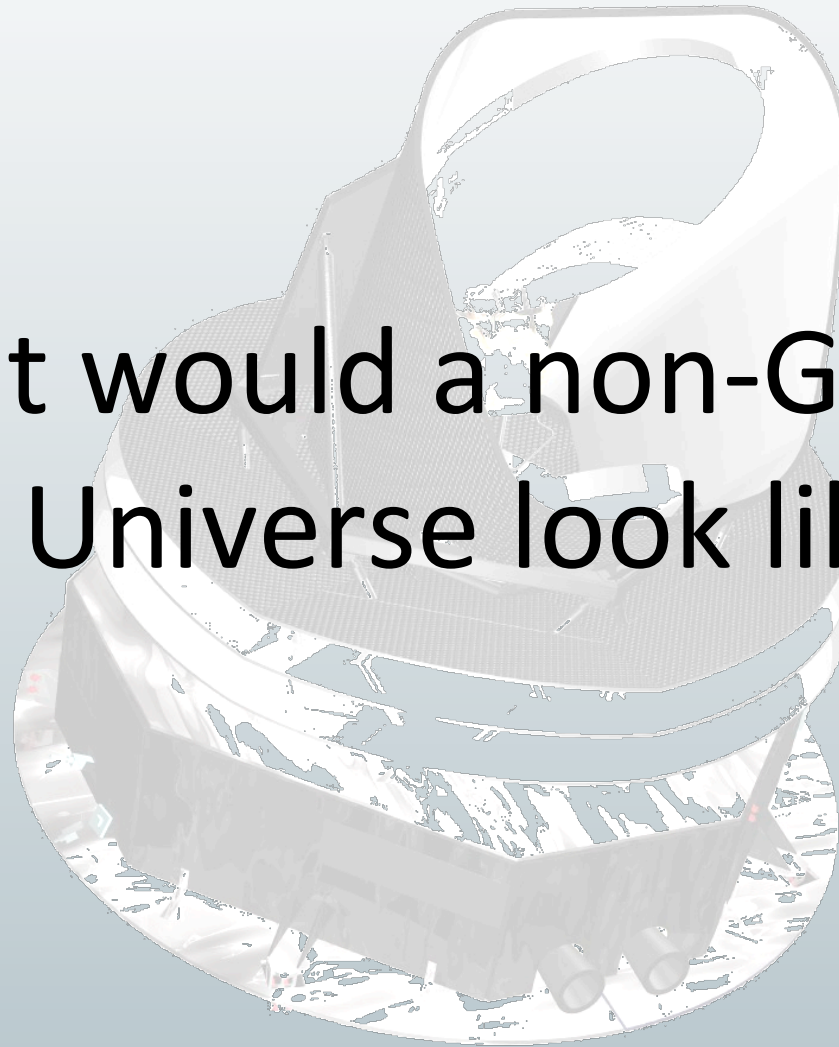
- There is more information in the map than the power spectrum alone.
- Non-Gaussianity currently is the highest precision test of standard inflation

*with Planck  $< \approx 0.01\%$*

*For comparison:*

- Flatness in second place with now  $\sim 0.1\%$
- Isocurvature constraints  $\sim 1\%$

What would a non-Gaussian  
Universe look like?



# An example: local $f_{NL}$

$$\Phi(x) = \Phi_G(x) + f_{NL} \Phi_G^2(x)$$

Characterizes the amplitude of non-Gaussianity

Salopek & Bond 1990  
Gangui et al 1994  
Verde et al 2000  
Komatsu & Spergel 2001

- This non-Gaussianity creates a bispectrum signature (as well as higher order moments)

$$\langle \Phi(k_1) \Phi(k_2) \Phi(k_3) \rangle = 2(2\pi)^3 f_{NL} \delta(k_1 + k_2 + k_3) P(k_1) P(k_2),$$

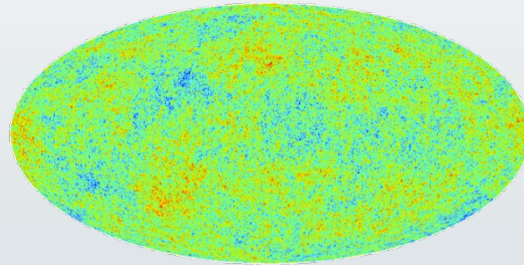
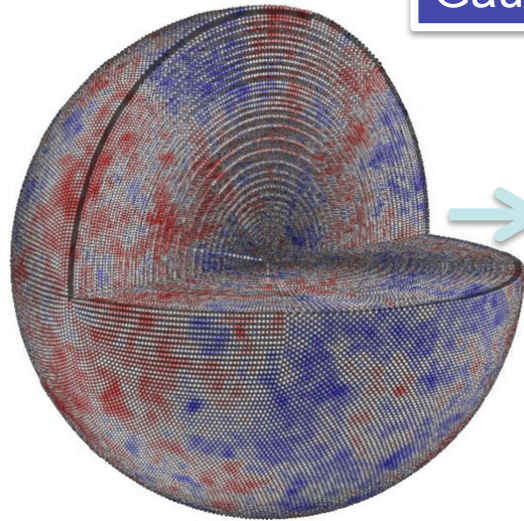
where  $(2\pi)^3 \delta(k_1 + k_2) P(k_1) = \langle \Phi(k_1) \Phi(k_2) \rangle$

- This translates into a bispectrum signature in the CMB through

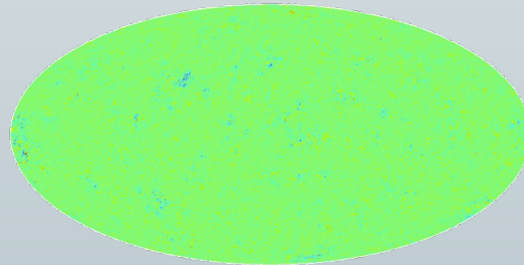
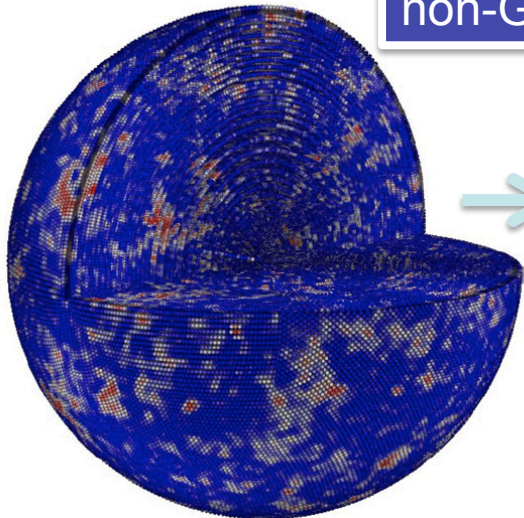
$$a_{lm} = 4\pi(-i)^l \int \frac{d^3\mathbf{k}}{(2\pi)^3} \Phi(\mathbf{k}) g_{Tl}(k) Y_{lm}^*(\hat{\mathbf{k}})$$

# From curvature to CMB sky

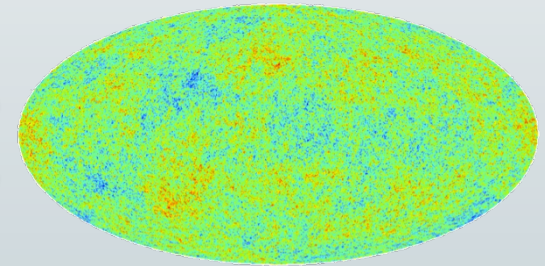
Gaussian



non-Gaussian



signal

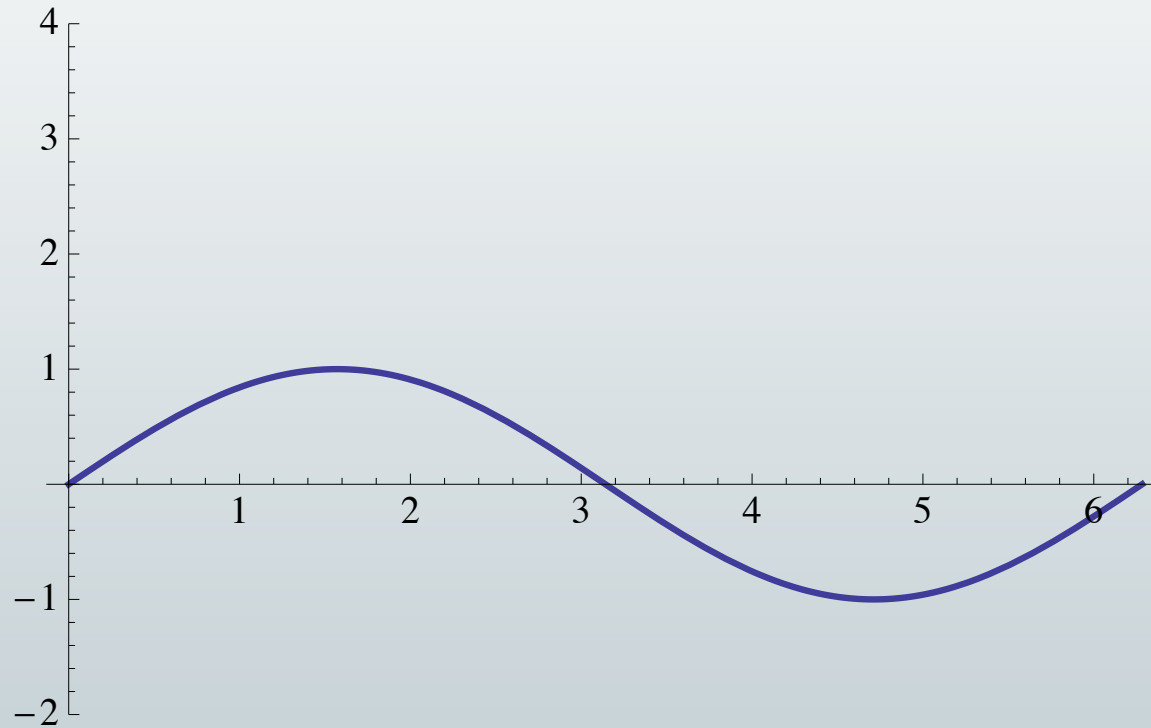




# Local non-Gaussianity illustrated

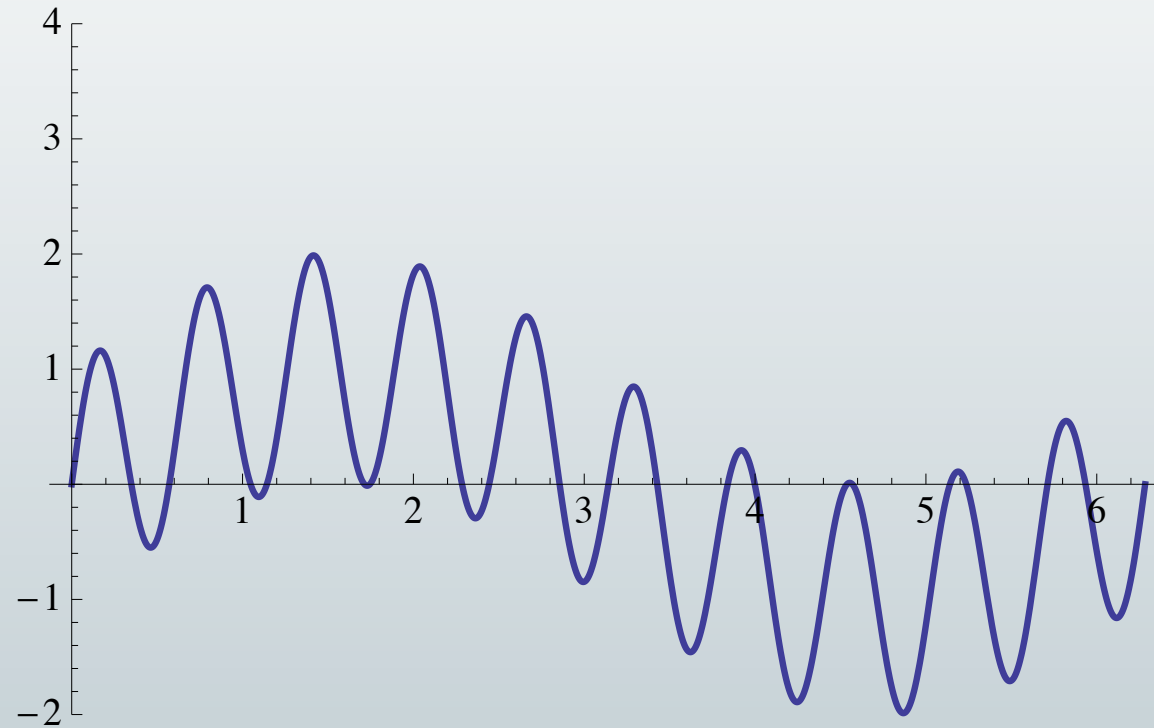


$$\Phi_{\text{long}}$$



# Local non-Gaussianity illustrated

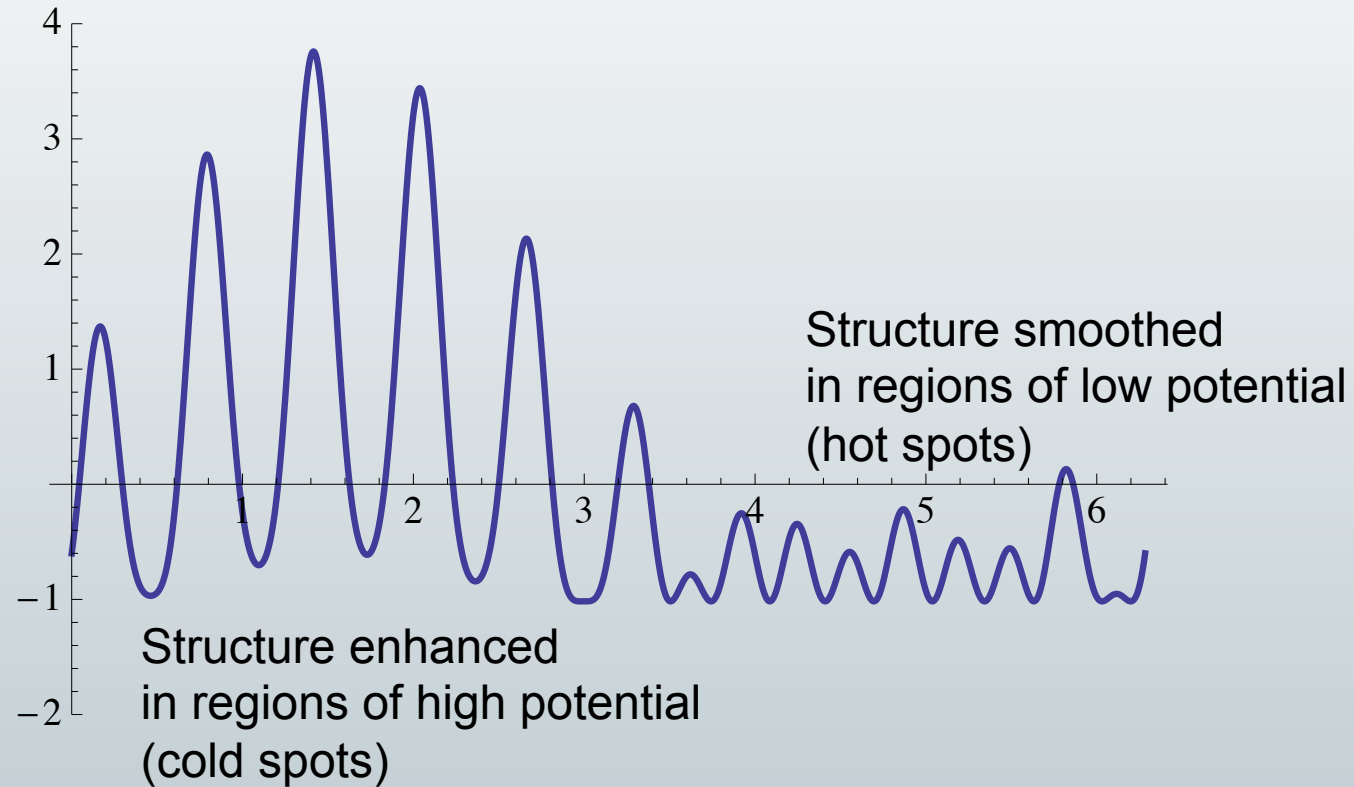
$$\Phi = \Phi_{\text{long}} + \Phi_{\text{short}}$$





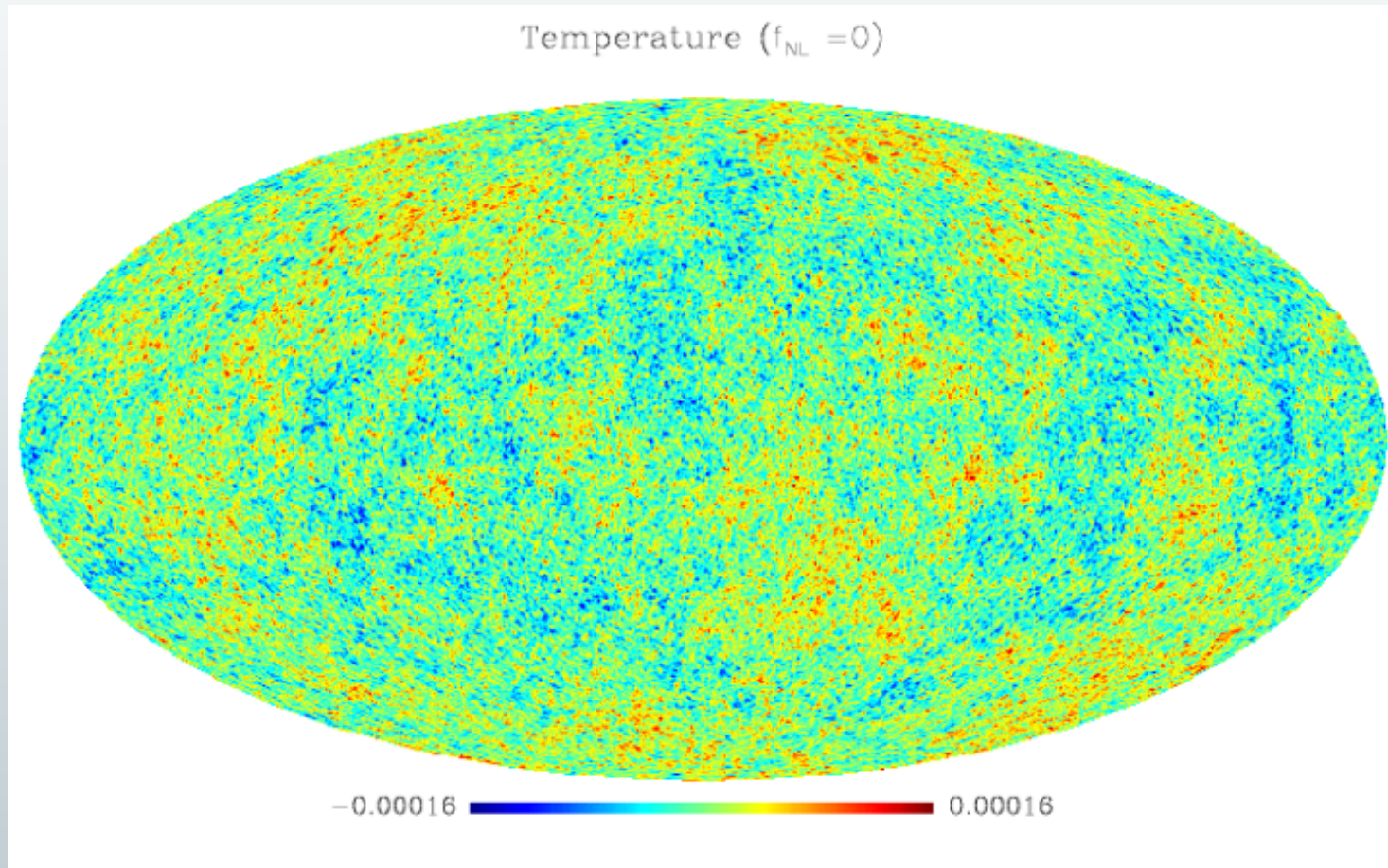
# Local non-Gaussianity illustrated

$$\Phi_{NL} = \Phi + f_{NL}(\Phi^2 - \langle \Phi^2 \rangle)$$



Note that this gives rise to both bispectrum and trispectrum signatures:  $f_{NL}$  and  $\tau_{NL}$

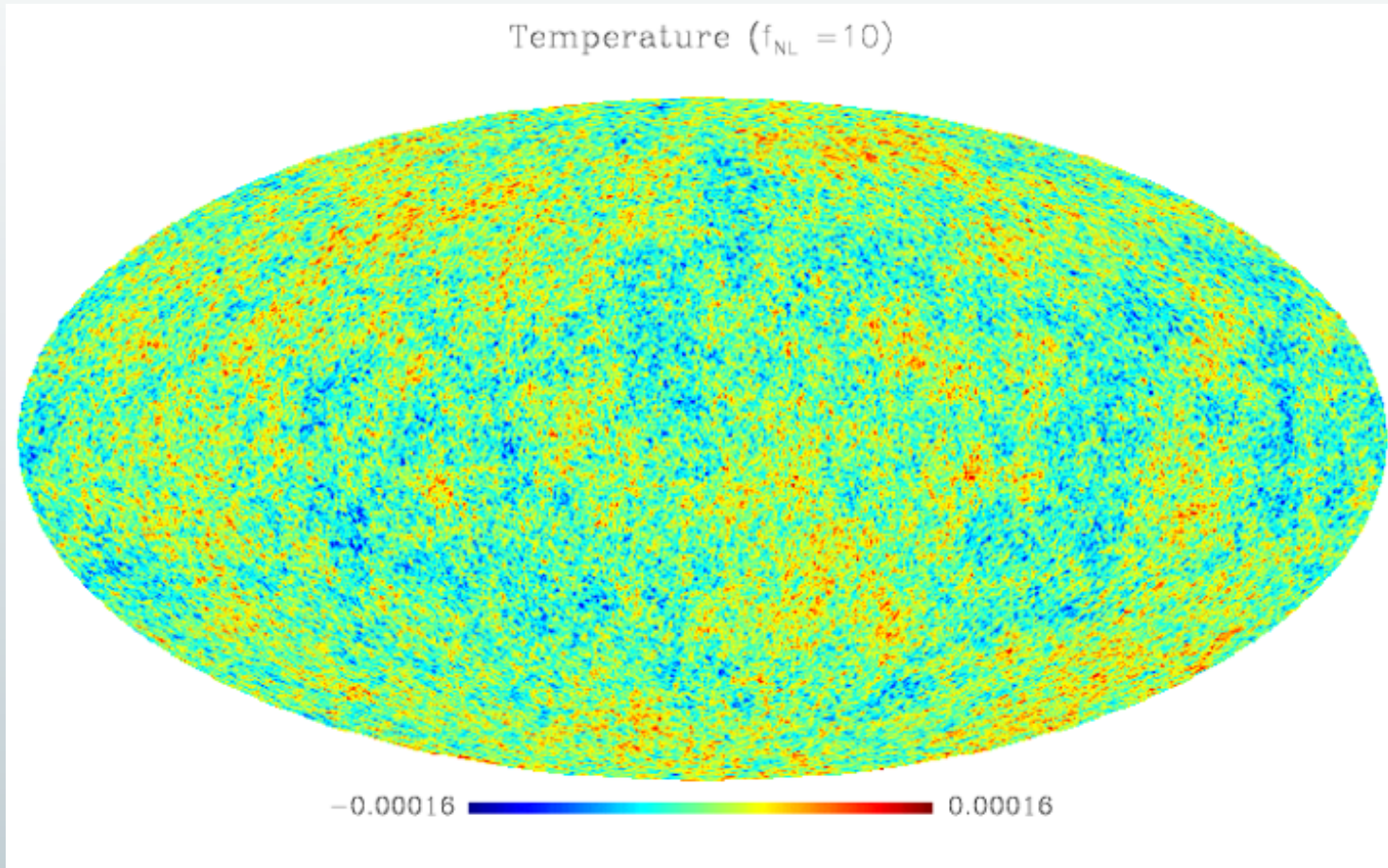
$$f_{\text{NL}} = 0$$



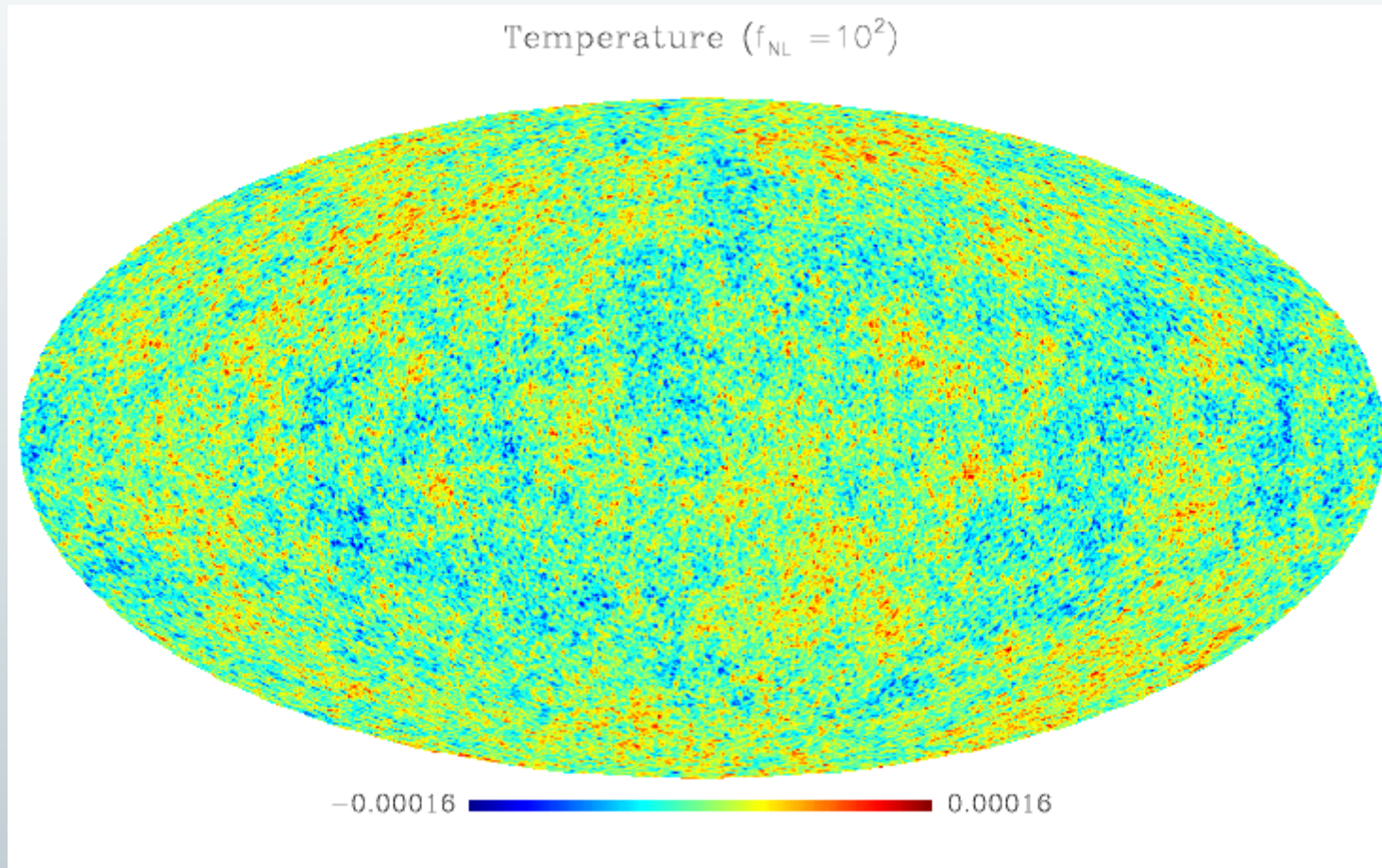


planck

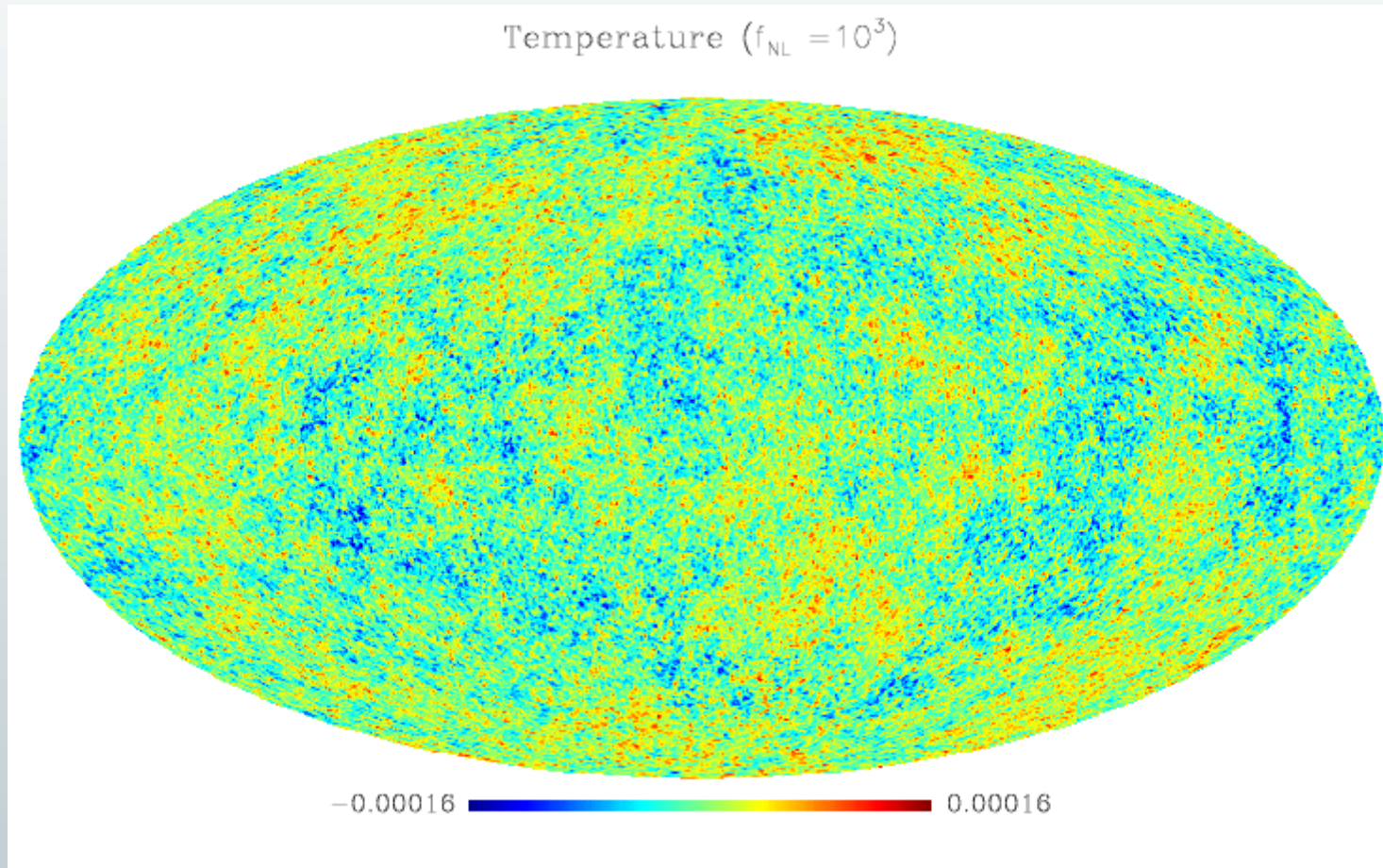
$$f_{NL} = 10$$



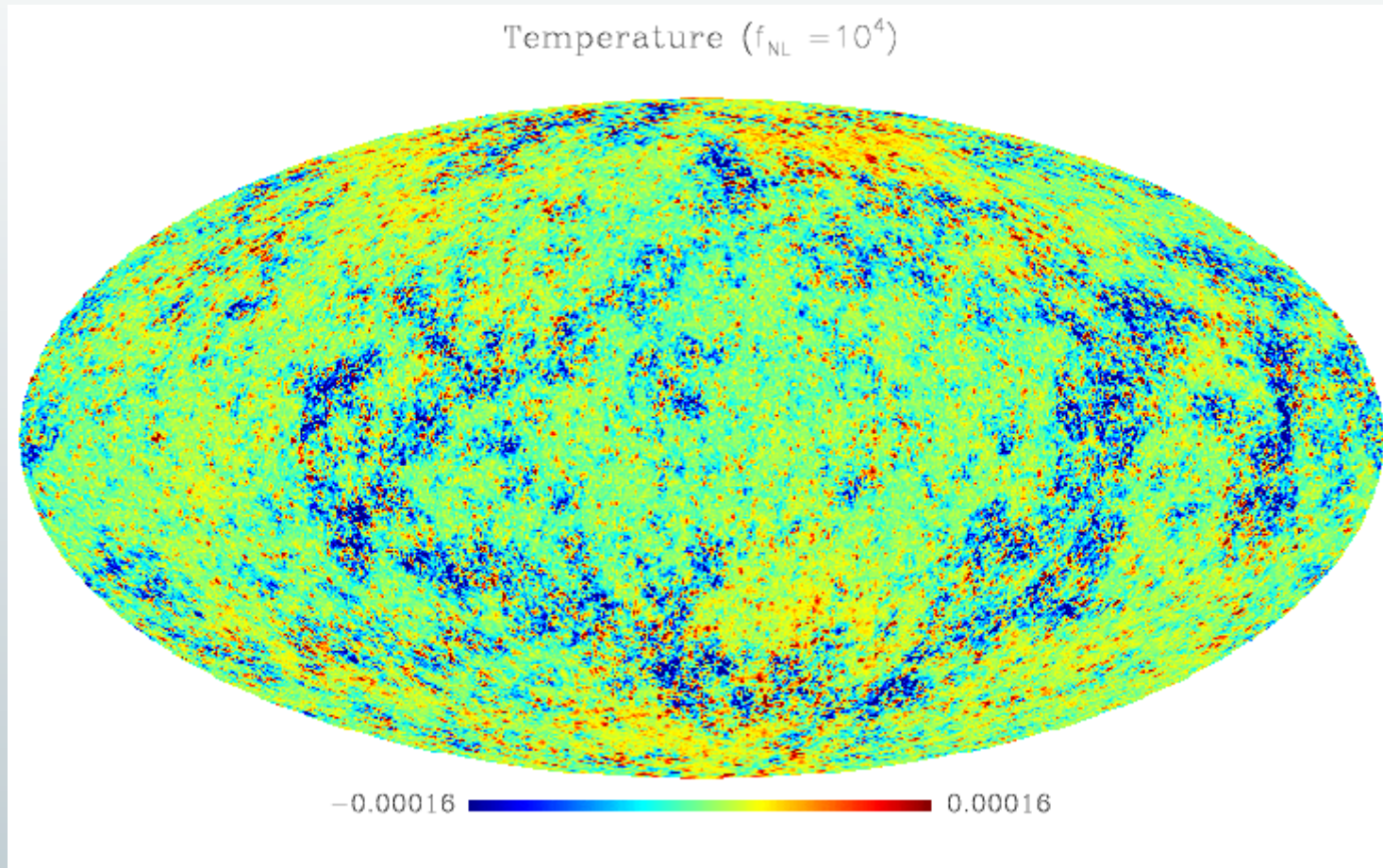
$$f_{\text{NL}} = 100$$



$$f_{\text{NL}} = 10^3$$

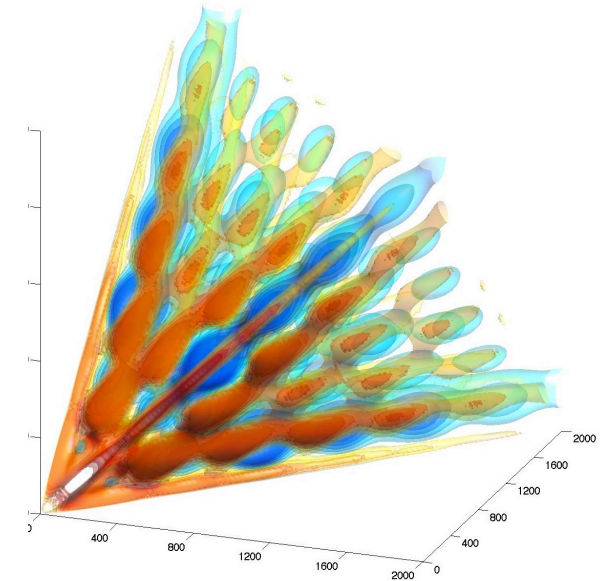
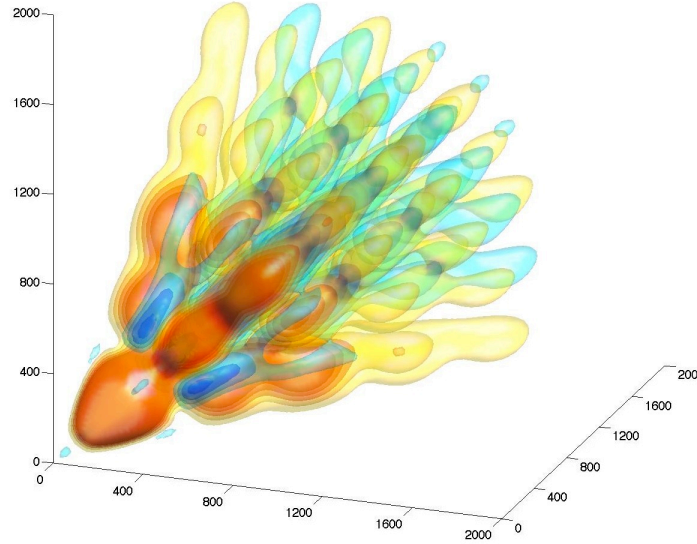
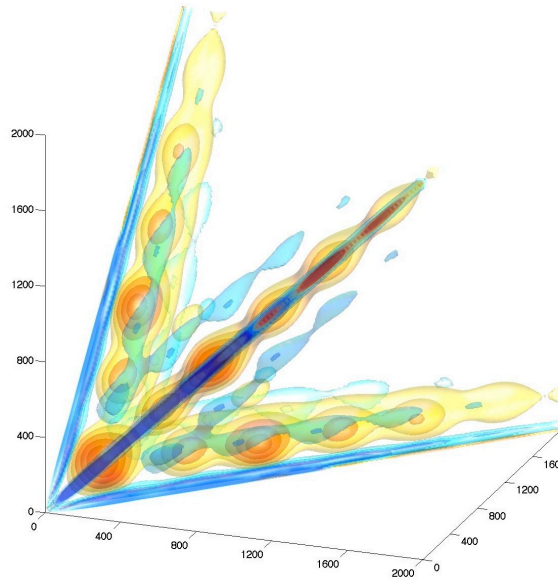


$$f_{\text{NL}} = 10^4$$





# CMB bispectrum fingerprinting with Planck



## NG of *local* type:

- Multi-field models
- Curvaton
- Ekpyrotic/cyclic models

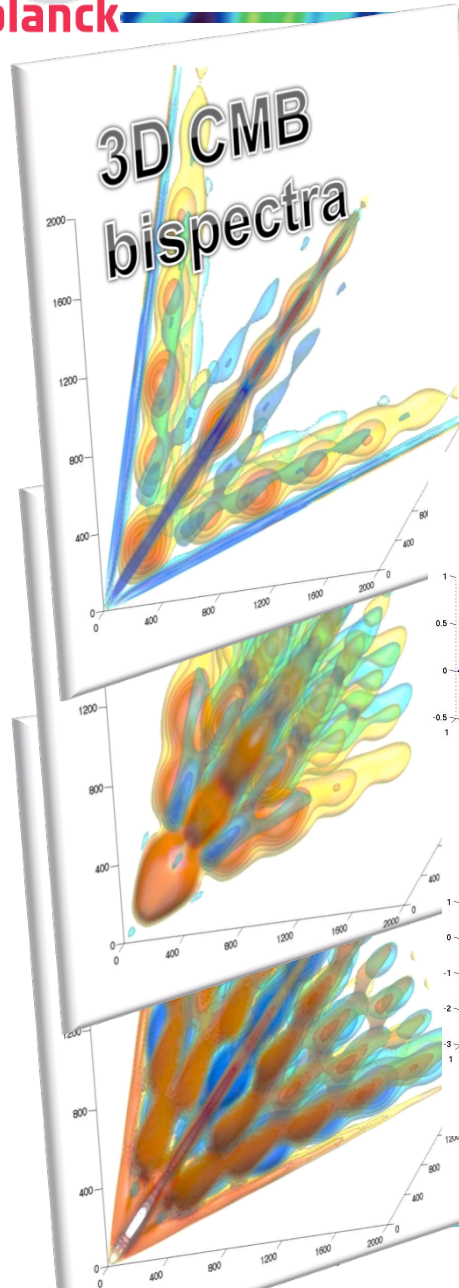
## NG of *equilateral* type

- Non-canonical kinetic term
  - K-inflation
  - DBI inflation
- Higher-derivate terms in Lagrangian
  - Ghost inflation
- Effective field theory

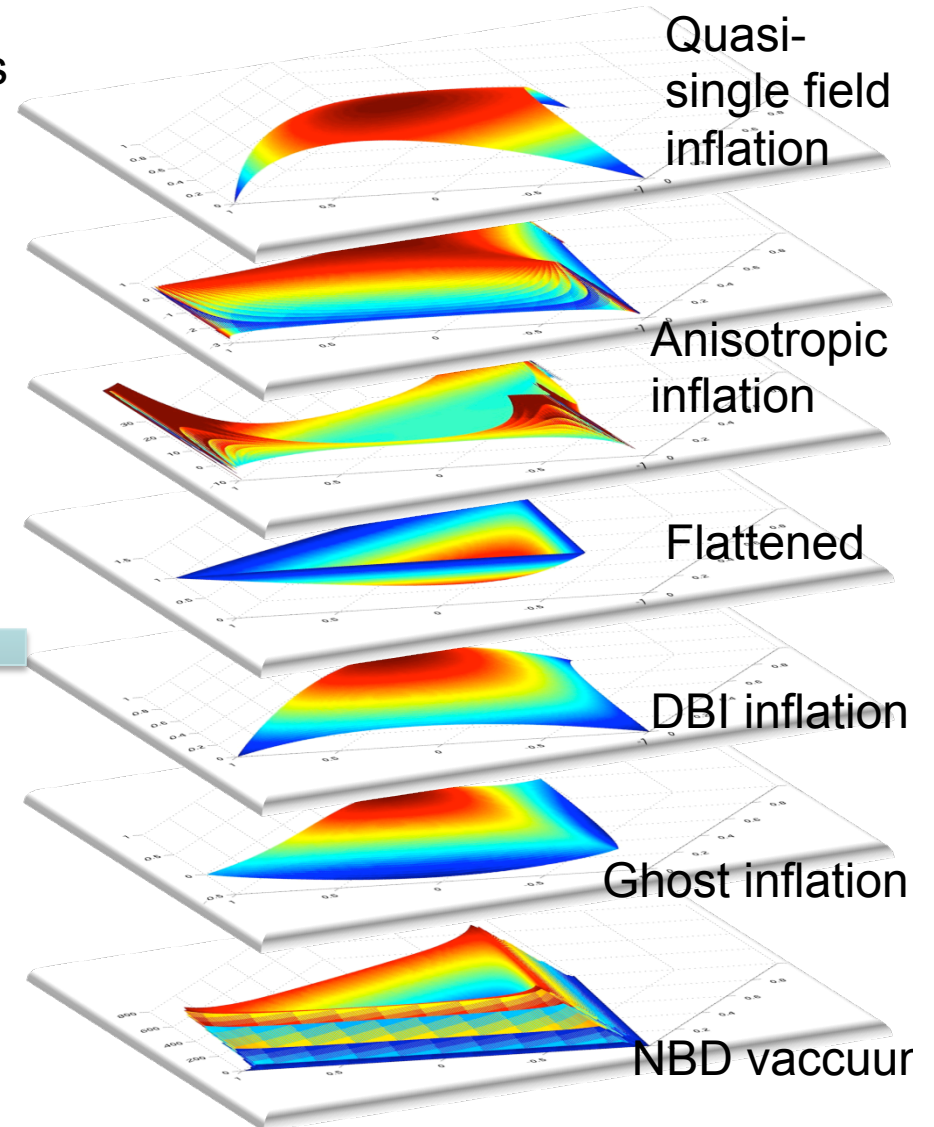
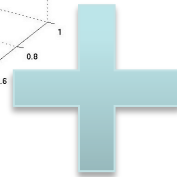
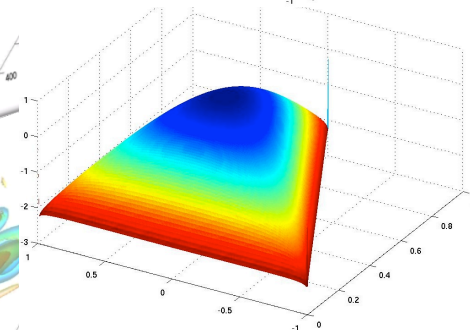
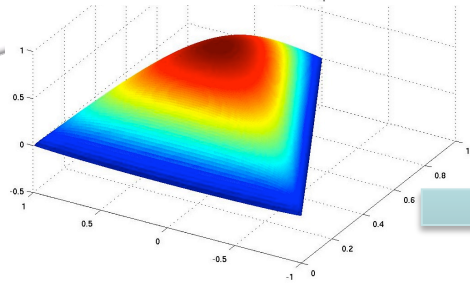
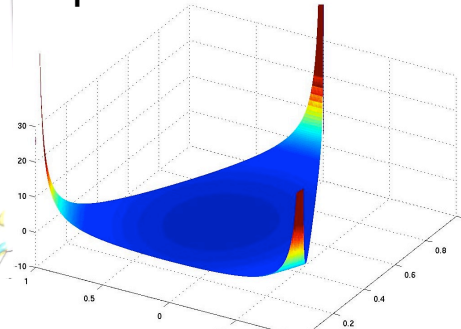
## NG of *orthogonal* type

- Distinguishes between different variants of
  - Non-canonical kinetic term
  - Higher derivative interactions
- Galileon inflation

# Bispectrum fingerprinting



Slices through bispectra of primordial fluctuations





Isotropic m-dependence

Theoretical template

$$\hat{f}_{\text{NL}} = \frac{1}{N} \sum_{\ell_i, m_i} \mathcal{G}_{m_1 m_2 m_3}^{\ell_1 \ell_2 \ell_3} b_{\ell_1 \ell_2 \ell_3}^{\text{th}}$$

$$\times \left[ C_{\ell_1 m_1, \ell'_1 m'_1}^{-1} a_{\ell'_1 m'_1} C_{\ell_2 m_2, \ell'_2 m'_2}^{-1} a_{\ell'_2 m'_2} C_{\ell_3 m_3, \ell'_3 m'_3}^{-1} a_{\ell'_3 m'_3} - 3 C_{\ell_1 m_1, \ell_2 m_2}^{-1} C_{\ell_3 m_3, \ell'_3 m'_3}^{-1} a_{\ell'_3 m'_3} \right],$$

Variance-reducing linear term

Weighted data bispectrum

$$\hat{f}_{\text{NL}} = \frac{1}{N} \sum_{\ell_i, m_i} \mathcal{G}_{m_1 m_2 m_3}^{\ell_1 \ell_2 \ell_3} b_{\ell_1 \ell_2 \ell_3}^{\text{th}} \\ \times [C_{\ell_1 m_1, \ell'_1 m'_1}^{-1} a_{\ell'_1 m'_1} C_{\ell_2 m_2, \ell'_2 m'_2}^{-1} a_{\ell'_2 m'_2} C_{\ell_3 m_3, \ell'_3 m'_3}^{-1} a_{\ell'_3 m'_3} \\ - 3 C_{\ell_1 m_1, \ell_2 m_2}^{-1} C_{\ell_3 m_3, \ell'_3 m'_3}^{-1} a_{\ell'_3 m'_3}],$$

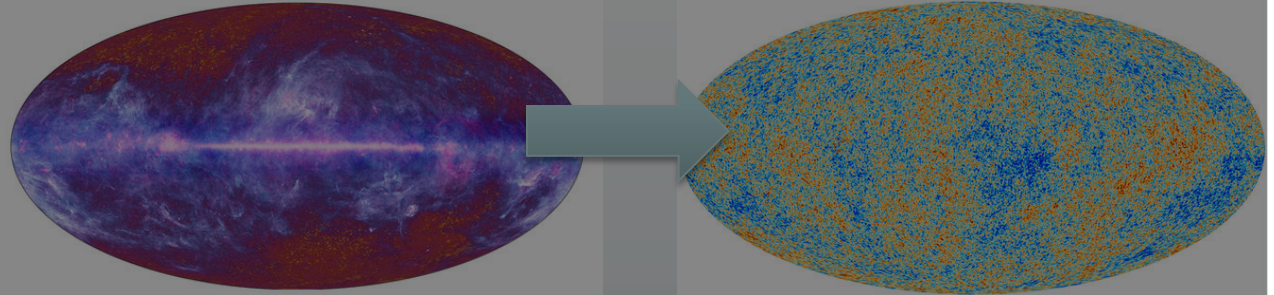
Scales as  $O(L_{\text{max}}^5)$

- Brute force implementation unfeasible for Planck data.
- Key idea: KSW - factorization

$$b_{\ell_1 \ell_2 \ell_3} = \sum_{ijk} X_{\ell_1}^i Y_{\ell_2}^j Z_{\ell_3}^k \Rightarrow B_{\ell_1 \ell_2 \ell_3}^{m_1 m_2 m_3} = b_{\ell_1 \ell_2 \ell_3} \int Y_{\ell_1}^{m_1}(\Omega) Y_{\ell_2}^{m_2}(\Omega) Y_{\ell_3}^{m_3}(\Omega)$$

- Gives  $L_{\text{max}}^2$  speed-up:  $\sim 10^6$  for Planck

➤ Foregrounds



➤ Systematics

**4<sup>th</sup> challenge: confirmation bias**



➤ Computation



# What is confirmation bias?

- "The wolf and the 7 little kids" is a story of confirmation bias
- The kids are waiting for their mom to come home – **they want to "detect" their mom.**
- At first the wolf's voice does not match mother sheep's a first-look analysis fails and the kids are safe.
- Then the wolf changes his voice but the kids require a systematics test: "show us your paw!" The test fails and the kids are safe.
- When the wolf paints his paw white, the test passes.
- But instead of doing further tests (*show us your face! show us your tail!*) they let the wolf in – and he eats them all up.





# Confirmation bias



We have a strong prior – the canonical expectation is Gaussian Lambda CDM and red flags rise in the analysis if we depart from this model.

**How we avoid being eaten:**

Treat the measurement on an equal footing – whether it is a detection or a constraint.



# Different Estimators



- KSW (Komatsu, Spergel, Wandelt 2003)
  - *Gives exact fit to separable bispectrum*
  - *Limited to factorizable templates*
- Modal (Fergusson, Liguori, Shellard 2009)
  - *Sum of KSW-like smooth templates to fit arbitrary templates*
  - *General up to resolution limit*
  - *Freedom to choose basis set*
  - *Fit global variations across entire L-range*
- Binned (Bucher, v. Tent, Carvalho 2009)
  - *Block-shaped templates, binning L-ranges*
  - *Compact basis in L*



# Simulation tests



- To participate in the analysis all estimators have to pass a suite of simulation challenges for Gaussian and non-Gaussian simulations
  
- These simulations test
  - *Map-by-map agreement of estimators*
  - *Robustness to foreground residuals*
  - *Ability to find and accurately measure unknown non-Gaussianity from a simulated data set (FFP6, including foregrounds, correlated noise, flagging, realistic band-passes, asymmetric main beams)*

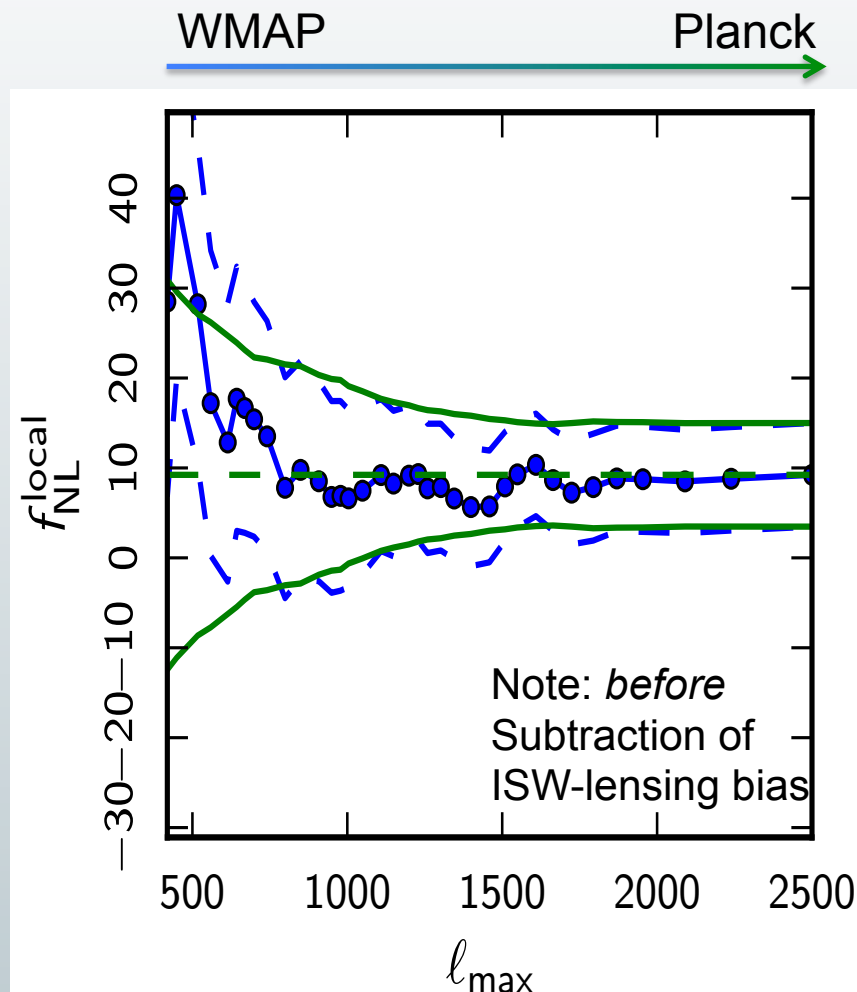


# The Planck NG analysis passed an extensive validation campaign



- Estimators agree
  - *KSW (Komatsu, Spergel, Wandelt 2003)*
  - *Modal (Fergusson, Liguori, Shellard, 2009)*
  - *Binned (Bucher, v. Tent, Carvalho 2009)*
  - *Skew- $C_l$  (Munshi, Heavens 2010)*
  - *Minkowski Functionals (Ducout et al. 2012)*
- Multiple foreground cleaning methods agree
  - *SMICA*
  - *NILC*
  - *SEVEM*
  - *(C-R)*
- Negligible impact of foreground residuals
- Null tests pass
- Consistent...
  - *Resolution dependence*
  - *Frequency dependence*
  - *Mask dependence*

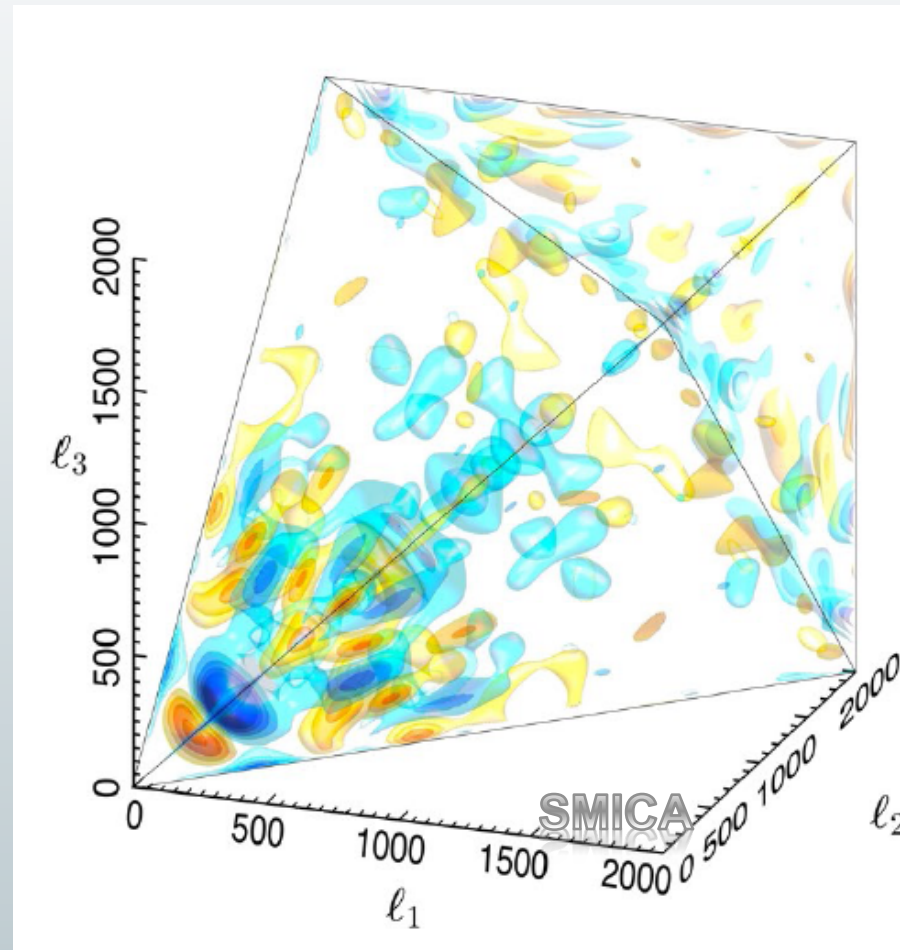




- Limiting the analysis to large scales (low  $l$ ), we make contact with WMAP9 ( $f_{NL}^{local} = 40 \pm 20$ )
- Planck allows using 10 times more modes and now rules out the WMAP central value by  $\sim 6$  sigma.

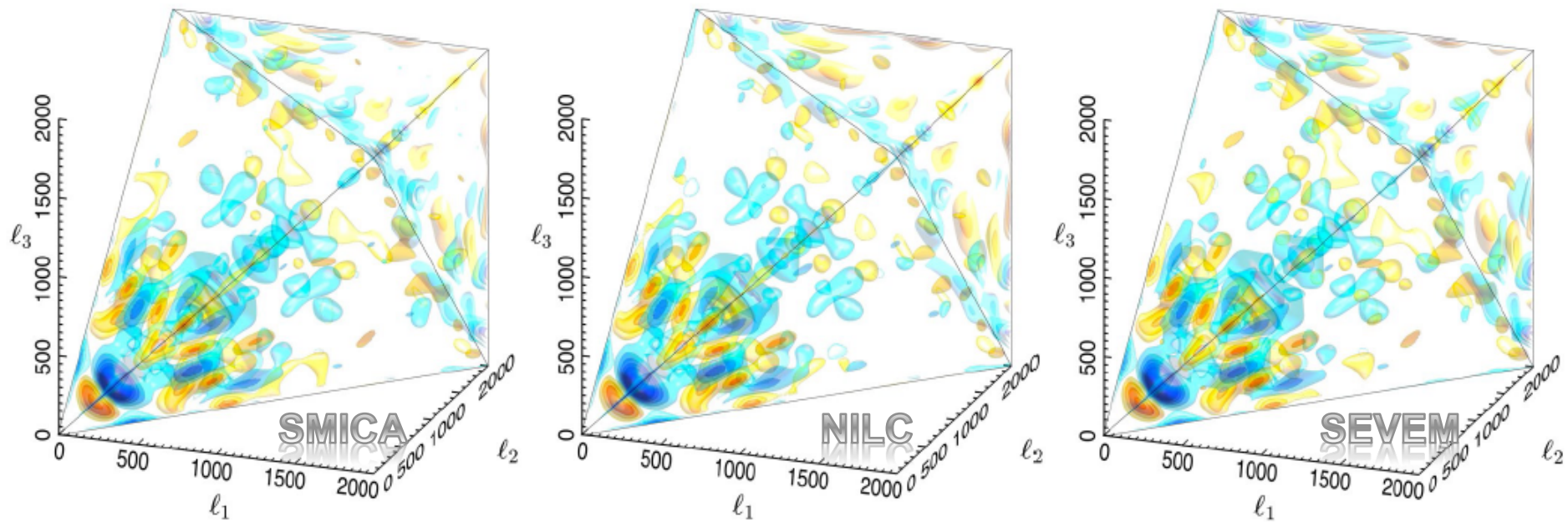


# The Planck bispectrum (modal decomposition)



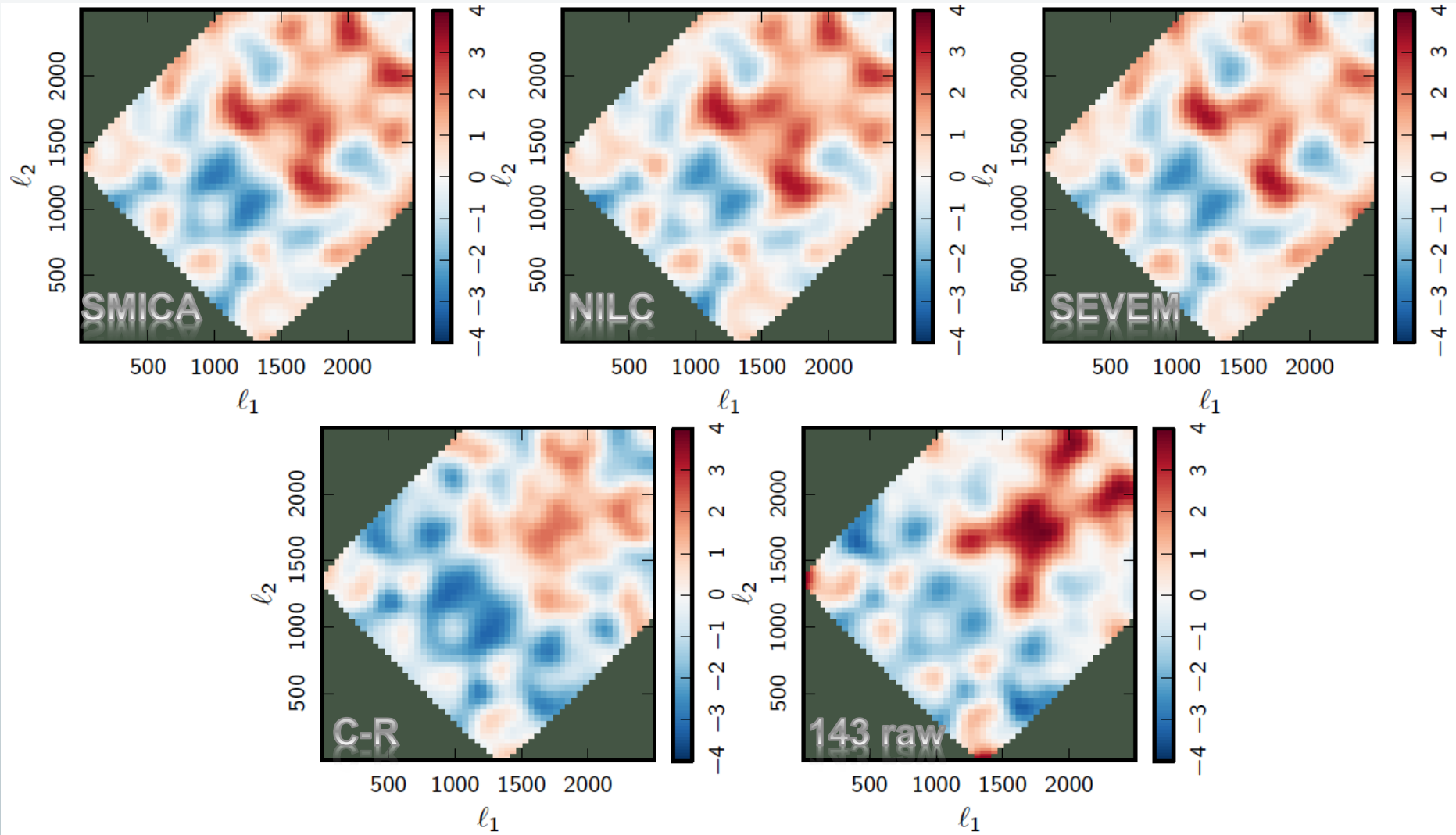


# Robust to foreground cleaning: the Planck modal bispectrum



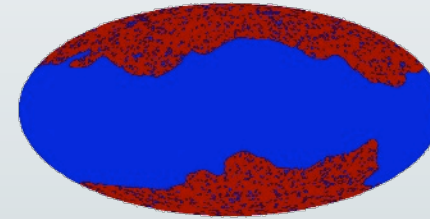
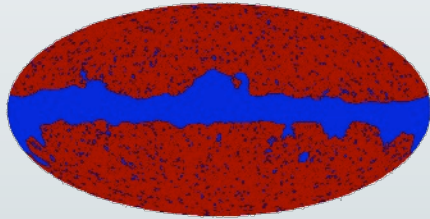


# Robust to foreground cleaning: (binned bispectrum)





# Masked raw frequency maps are consistent with zero $f_{NL}$



	SMICA $f_{\text{sky}} = 0.73$	70 GHz	100 GHz $f_{\text{sky}} = 0.32$	143 GHz	217 GHz
Local	$9.2 \pm 5.9$	$19.7 \pm 26.0$	$-2.5 \pm 13.2$	$10.4 \pm 9.8$	$-4.7 \pm 9.6$
Equilateral	$-20 \pm 73$	$159 \pm 188$	$70 \pm 132$	$48 \pm 114$	$-9 \pm 114$
Orthogonal	$-39 \pm 39$	$-78 \pm 139$	$-106 \pm 81$	$-101 \pm 64$	$-84 \pm 63$



# Planck results: the highest precision test of origin of cosmic structure

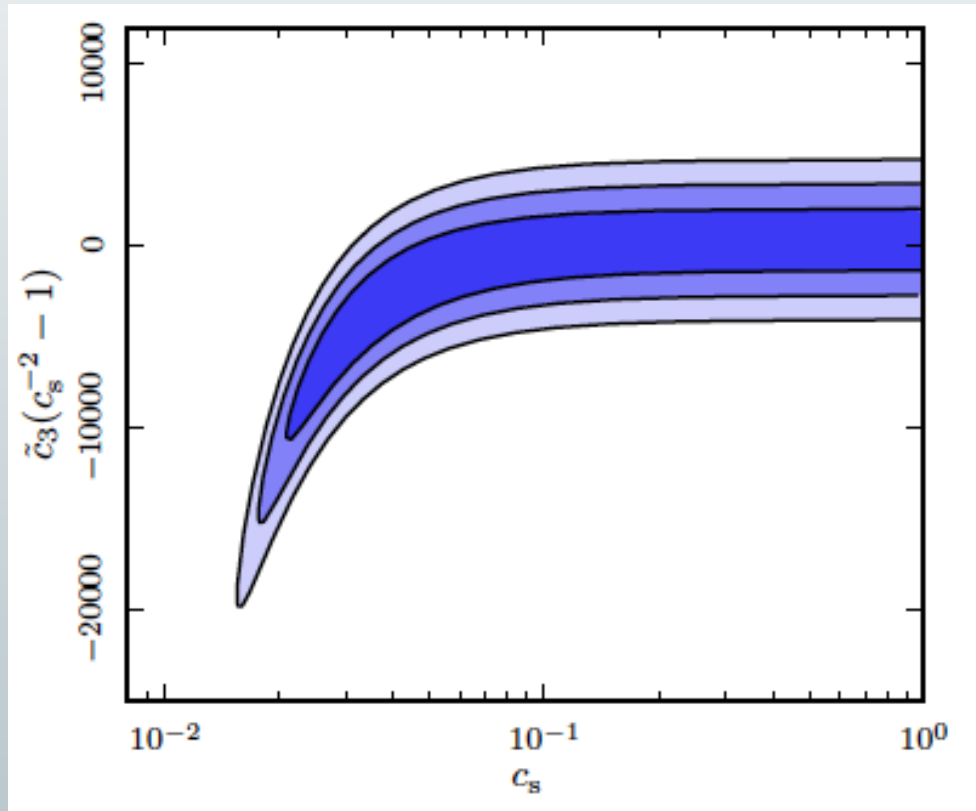


	KSW	Independent			ISW-lensing subtracted		
		Binned	Modal		KSW	Binned	Modal
<b>SMICA</b>							
Local .....	$9.8 \pm 5.8$	$9.2 \pm 5.9$	$8.3 \pm 5.9$	.....	$2.7 \pm 5.8$	$2.2 \pm 5.9$	$1.6 \pm 6.0$
Equilateral .....	$-37 \pm 75$	$-20 \pm 73$	$-20 \pm 77$	.....	$-42 \pm 75$	$-25 \pm 73$	$-20 \pm 77$
Orthogonal .....	$-46 \pm 39$	$-39 \pm 41$	$-36 \pm 41$	.....	$-25 \pm 39$	$-17 \pm 41$	$-14 \pm 42$
<b>NILC</b>							
Local .....	$11.6 \pm 5.8$	$10.5 \pm 5.8$	$9.4 \pm 5.9$	.....	$4.5 \pm 5.8$	$3.6 \pm 5.8$	$2.7 \pm 6.0$
Equilateral .....	$-41 \pm 76$	$-31 \pm 73$	$-20 \pm 76$	.....	$-48 \pm 76$	$-38 \pm 73$	$-20 \pm 78$
Orthogonal .....	$-74 \pm 40$	$-62 \pm 41$	$-60 \pm 40$	.....	$-53 \pm 40$	$-41 \pm 41$	$-37 \pm 43$
<b>SEVEM</b>							
Local .....	$10.5 \pm 5.9$	$10.1 \pm 6.2$	$9.4 \pm 6.0$	.....	$3.4 \pm 5.9$	$3.2 \pm 6.2$	$2.6 \pm 6.0$
Equilateral .....	$-32 \pm 76$	$-21 \pm 73$	$-13 \pm 77$	.....	$-36 \pm 76$	$-25 \pm 73$	$-13 \pm 78$
Orthogonal .....	$-34 \pm 40$	$-30 \pm 42$	$-24 \pm 42$	.....	$-14 \pm 40$	$-9 \pm 42$	$-2 \pm 42$
<b>C-R</b>							
Local .....	$12.4 \pm 6.0$	$11.3 \pm 5.9$	$10.9 \pm 5.9$	.....	$6.4 \pm 6.0$	$5.5 \pm 5.9$	$5.1 \pm 5.9$
Equilateral .....	$-60 \pm 79$	$-52 \pm 74$	$-33 \pm 78$	.....	$-62 \pm 79$	$-55 \pm 74$	$-32 \pm 78$
Orthogonal .....	$-76 \pm 42$	$-60 \pm 42$	$-63 \pm 42$	.....	$-57 \pm 42$	$-41 \pm 42$	$-42 \pm 42$

68% confidence intervals

$$S = \int d^4x \sqrt{-g} \left[ -\frac{M_{\text{Pl}}^2 \dot{H}}{c_s^2} \left( \dot{\pi}^2 - c_s^2 \frac{(\partial_i \pi)^2}{a^2} \right) - M_{\text{Pl}}^2 \dot{H} (1 - c_s^{-2}) \dot{\pi} \frac{(\partial_i \pi)^2}{a^2} + \left( M_{\text{Pl}}^2 \dot{H} (1 - c_s^{-2}) - \frac{4}{3} M_3^4 \right) \dot{\pi}^3 \right]$$

Senatore et al 2010  
Chen et al. 2007, 2010

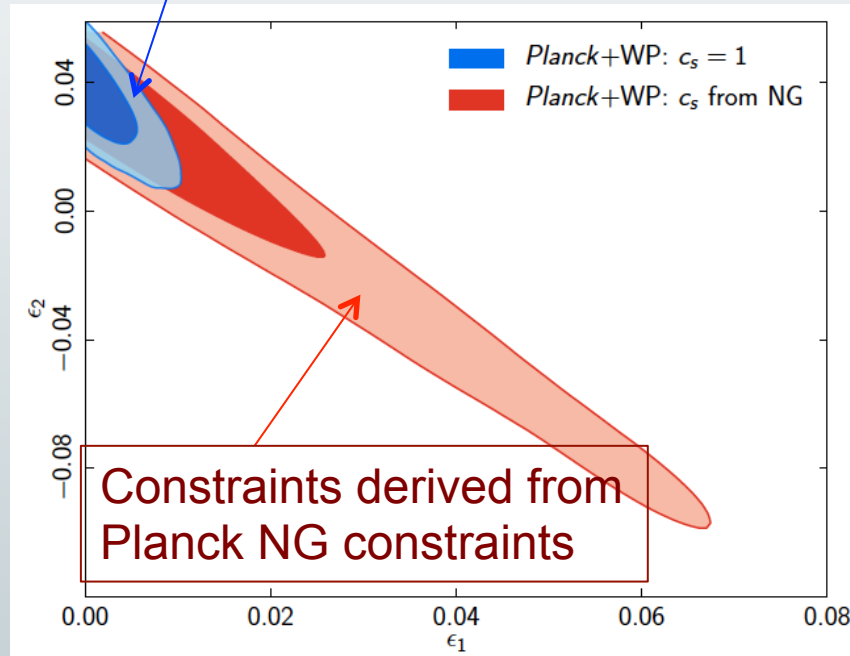


Specific bispectrum shapes correspond to cubic interaction terms in the Lagrangian

Use these to directly constrain parameters in the Lagrangian

# NG impact on general single field models

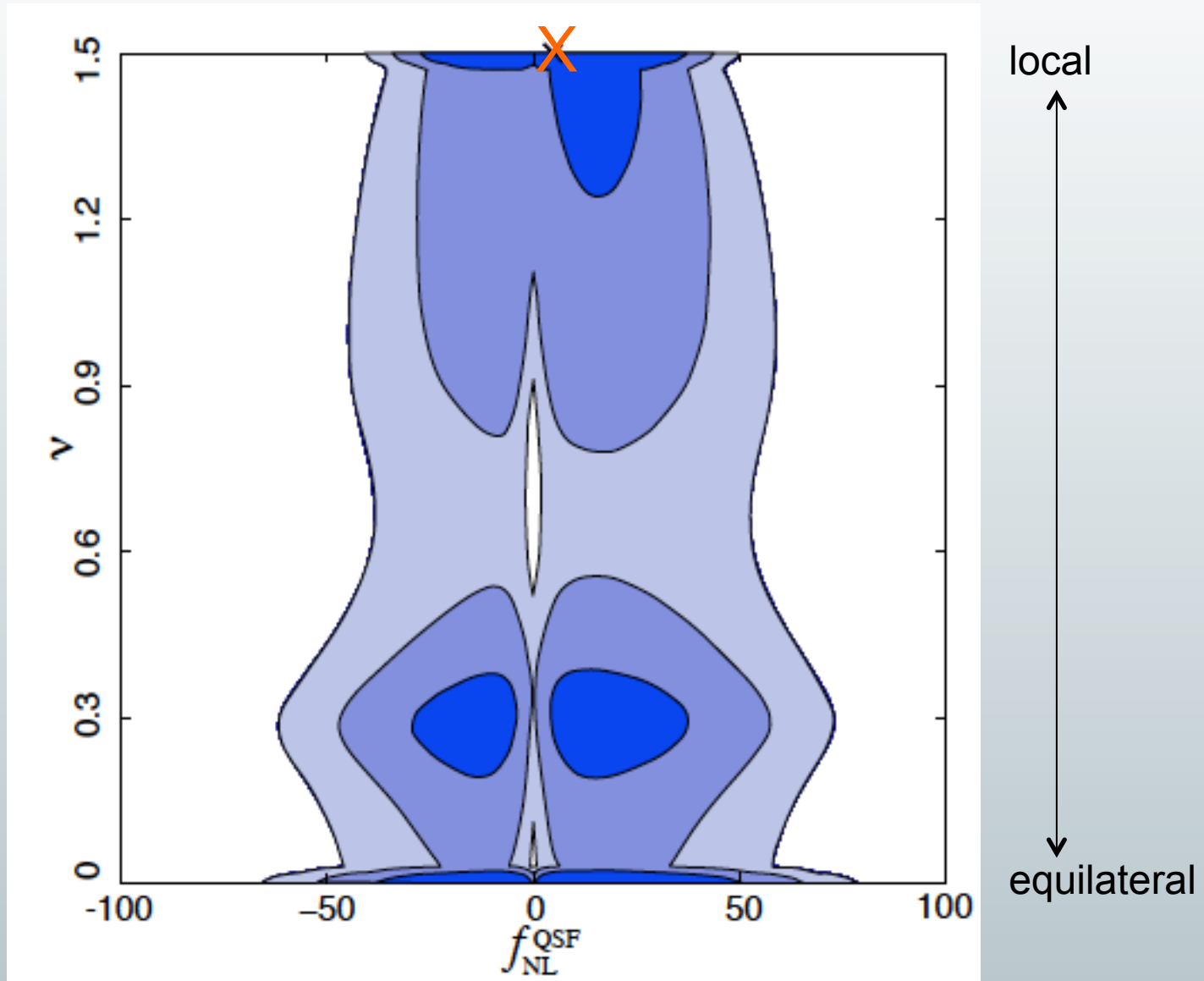
Sound speed fixed to 1



- Allowing varying sound speed through a non-standard kinetic term during inflation opens a parameter degeneracy
- But the kinetic term also produces an equilateral bispectrum. The NG constraints break the degeneracy.



# Quasi-single field model

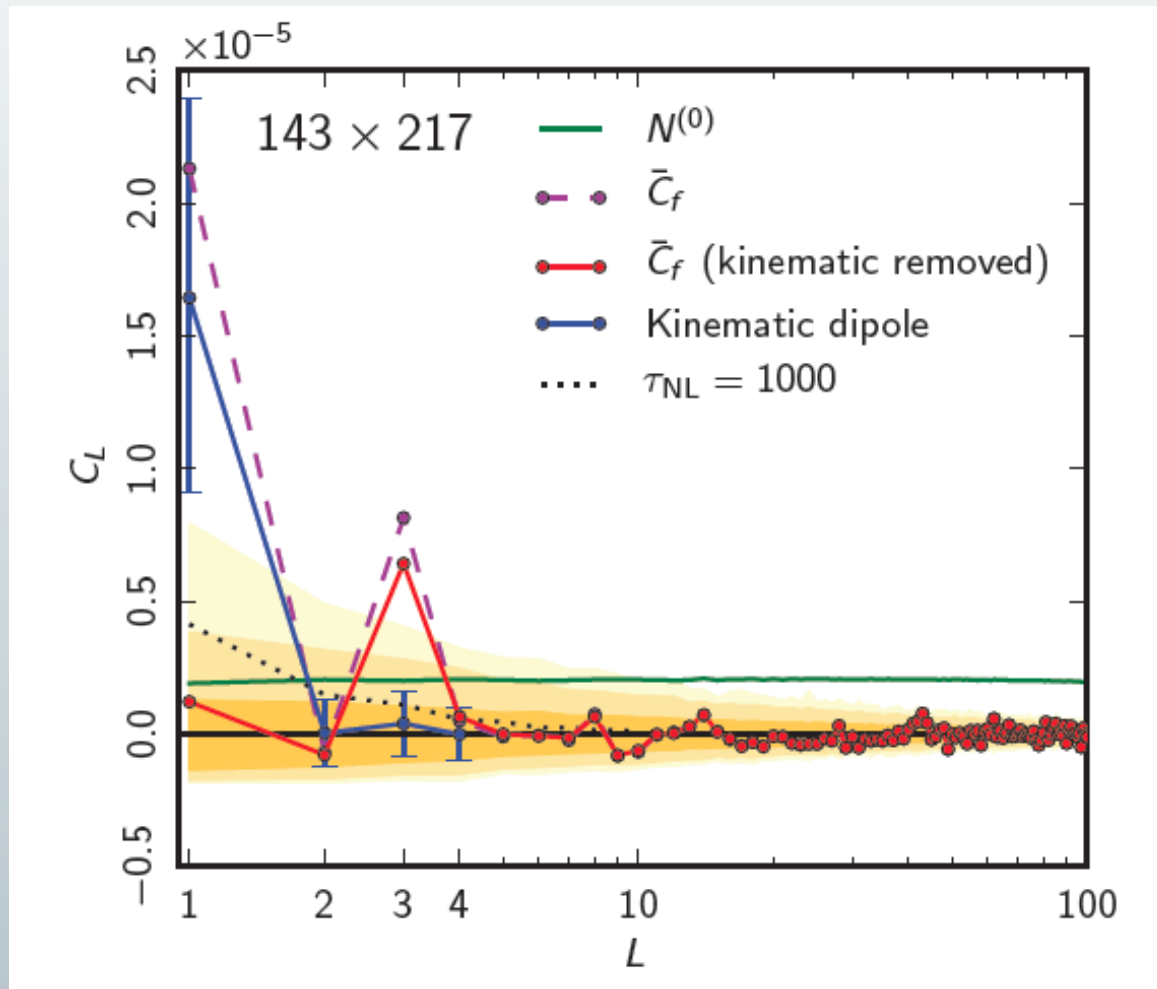




# Constraint on 4-point function from local non-Gaussianity:



$$\tau_{\text{NL}} < 2800$$





# Planck primordial non-Gaussianity results

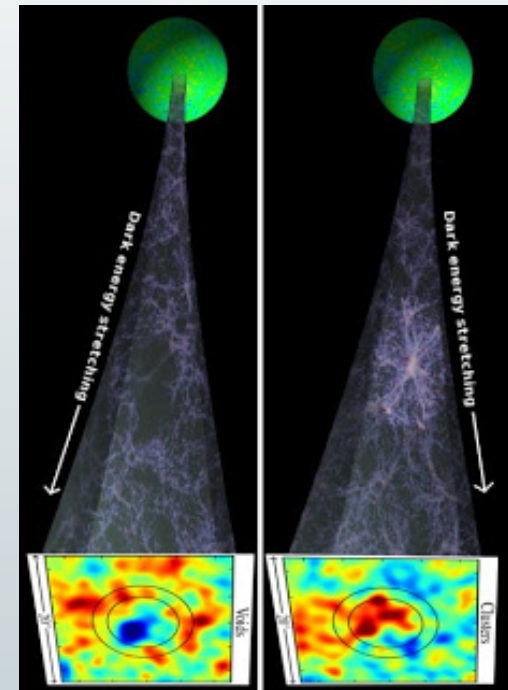


- Slowly rolling, single scalar-field inflation models are favoured by the Planck data
- Multi-field models are not ruled out but also not detected. The curvaton decay fraction  $r_D > 15\%$  (95% C.L.)
- Planck map rules out small speed of sound during inflation  $c_s > 0.02$  (95% C.L.)
- Planck map is consistent with standard BD vacuum.
- Planck strongly constrains a class of ekpyrotic/cyclic models (those with exponential potential, entropic generation of perturbations and conversion during ekpyrotic smoothing phase).

# The late-time bispectrum

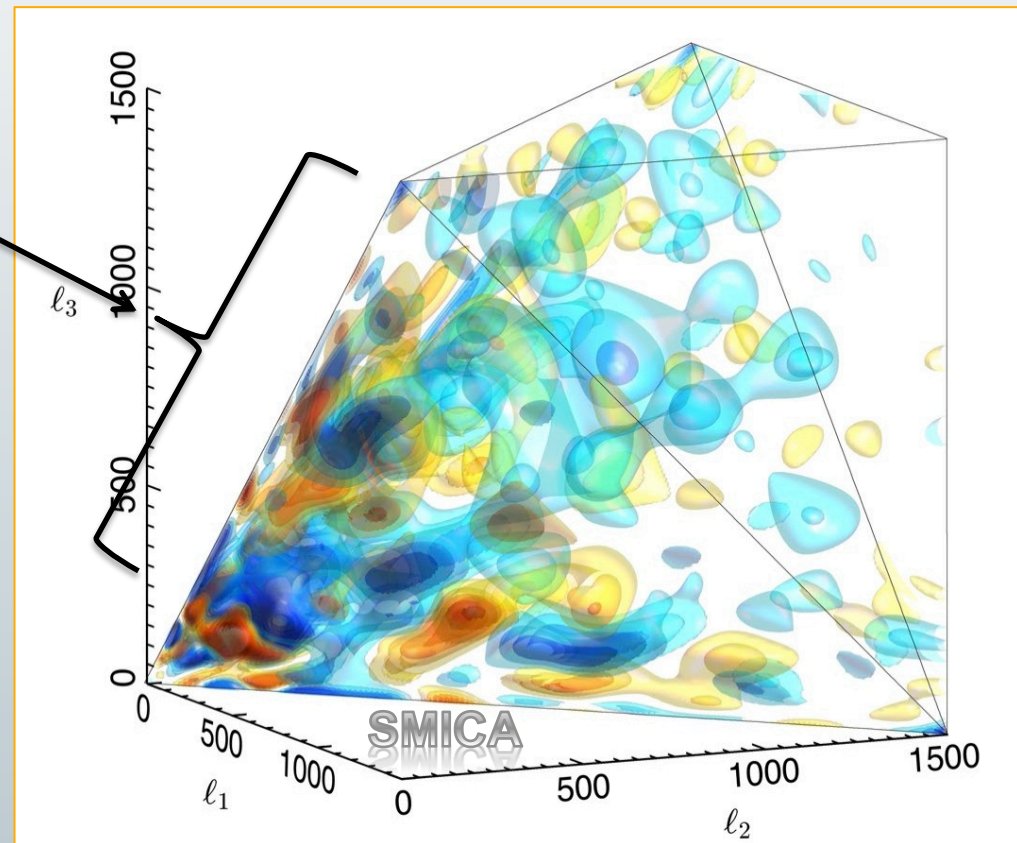
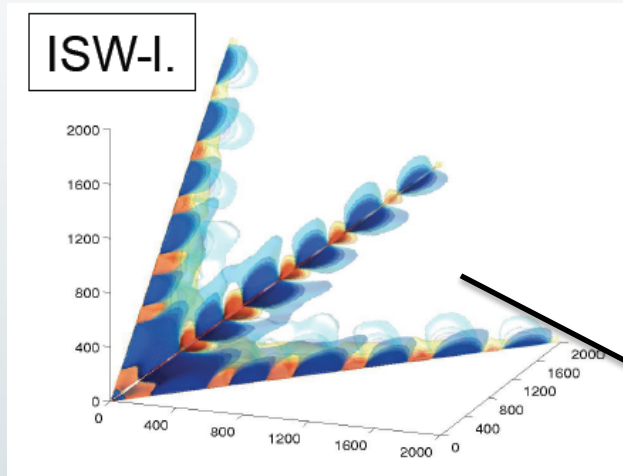


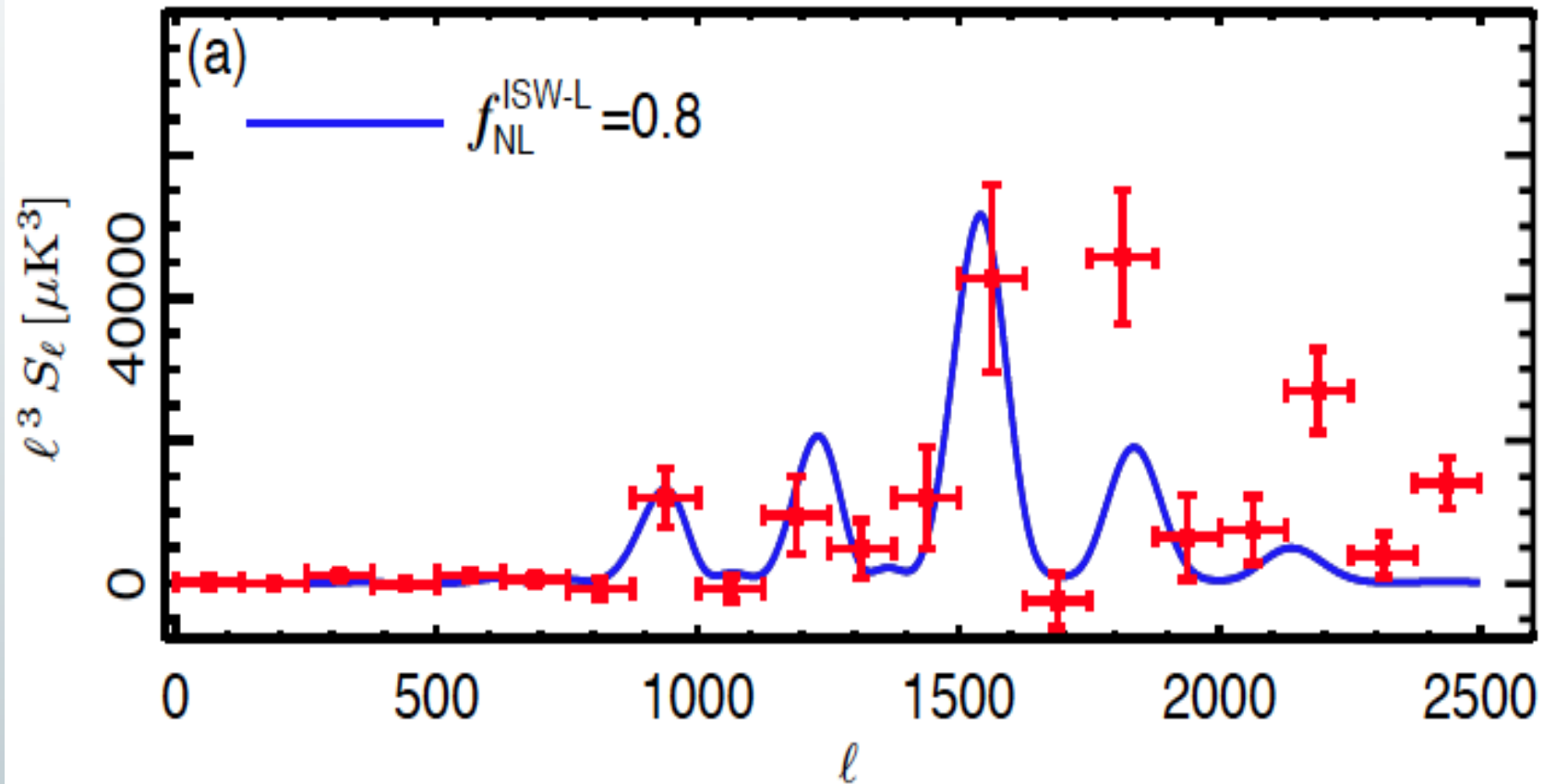
- The *erasure of structure caused by dark energy (late-time inflation)* creates a non-Gaussian signal in the CMB
- This effect manifests as the “ISW-Lensing” bispectrum
- Planck see this effect at the expected level with **2.6 sigma** significance.





# The 2.6- $\sigma$ ISW lensing effect – visible by eye in the Planck bispectrum







# Can TOD processing remove Non-Gaussianity?



- $l \sim 500$  consistent with WMAP -> Any removal would have had to occur exclusively at high  $l$
- Yet, TOD processing clearly preserved
  - *Lensing signal*
  - *Infrared-background lensing correlation*both seen with high significance in Planck data – and at the expected level.
- ISW-lensing bispectrum estimate consistent with expected level at 0.6 sigma and non-zero by 2.6 sigma. This is also a squeezed bispectrum shape.

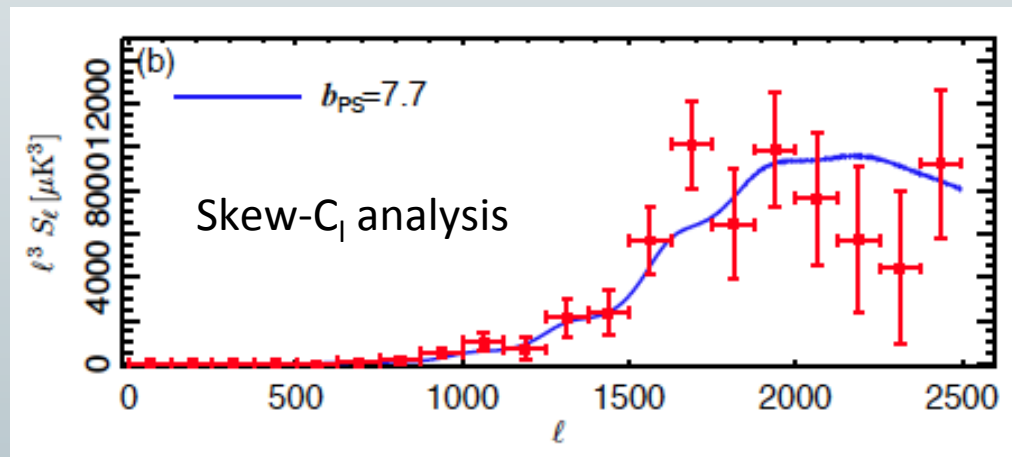
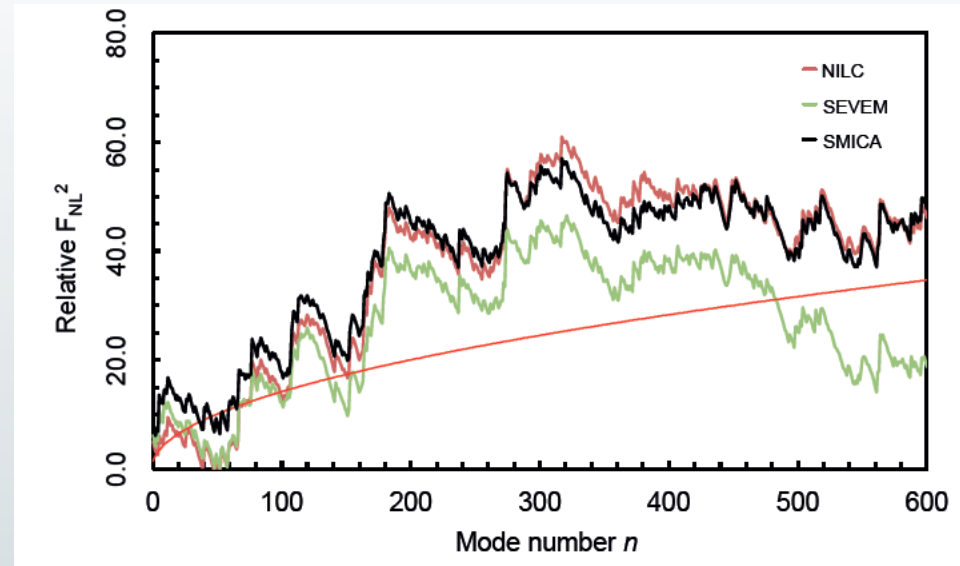




# Lots of information – large discovery potential



Blind search for excess variance looks consistent with random Gaussian bispectrum.

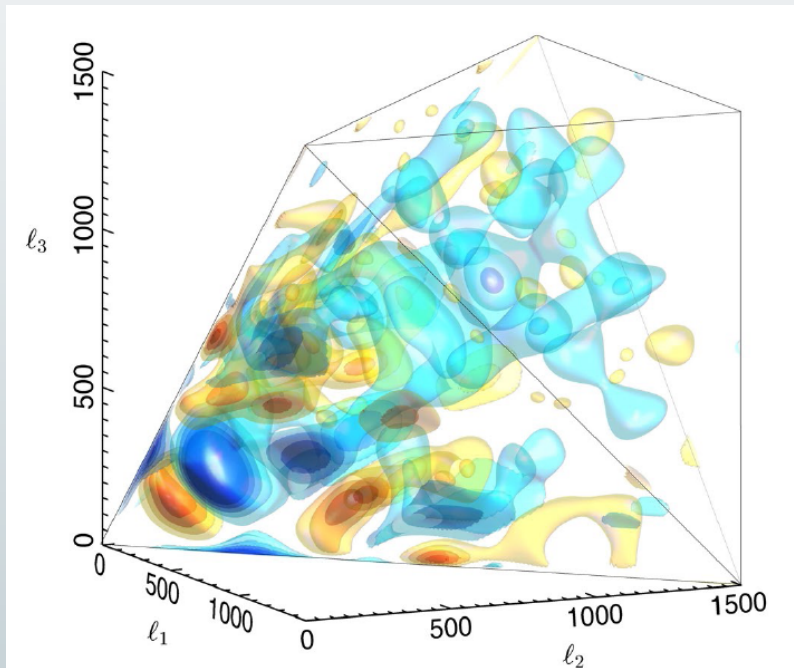


But a given template shape can have high significance.

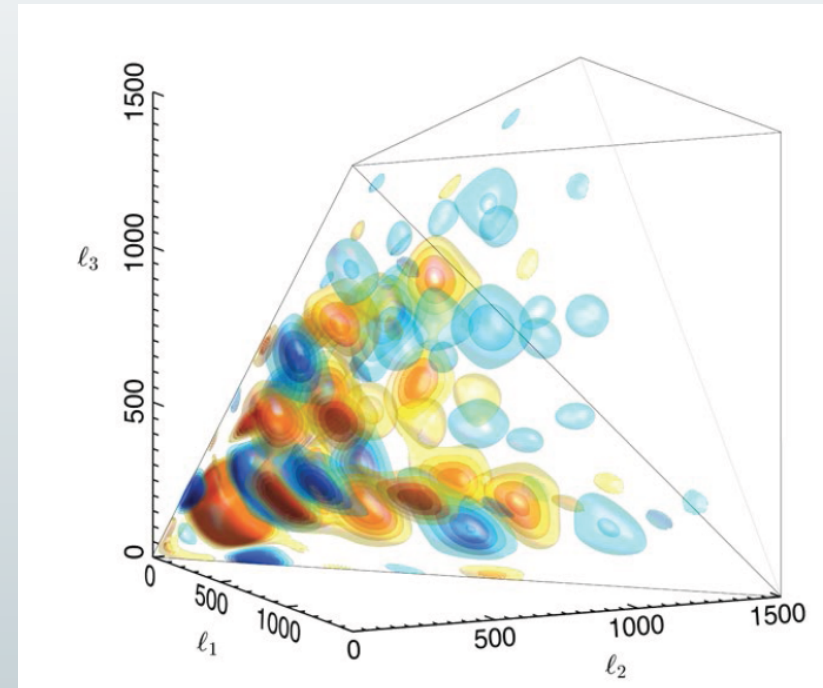
Residual point source bispectrum detected at 5 sigma in SMICA map.

# 3-sigma hint of oscillatory feature?

Data



Best fit feature model bispectrum



Not (yet?) highly significant if “look-elsewhere” effect is taken into account.  
Warrants further analysis.



# Beyond the power spectrum



- Features in the  $P(k)$  should also be visible in the bispectrum (and vice versa). Power spectrum and non-Gaussianity analyses not yet done in fully overlapping parameter range.

Example:

- k-inflation (Armendariz-Picon et al. 1999) fits the Planck power spectrum and NG separately but not both:

NG (equil):  $\gamma \geq 0.05$  at 95% CL.

$n_s$ :  $0.01 \leq \gamma \leq 0.02$  at 95% CL.



# The view of the initial state of the Universe after Planck



- Slowly rolling, single scalar-field inflation models are favoured by the Planck data. Questions of prior choice remain
- New constraint volume for three main NG shapes **20 times** smaller than pre-Planck.
- We do see non-primordial non-Gaussianity at levels consistent with expectations
- Planck non-Gaussianity is the highest precision test to date of the physical mechanism at the origin of cosmic structure



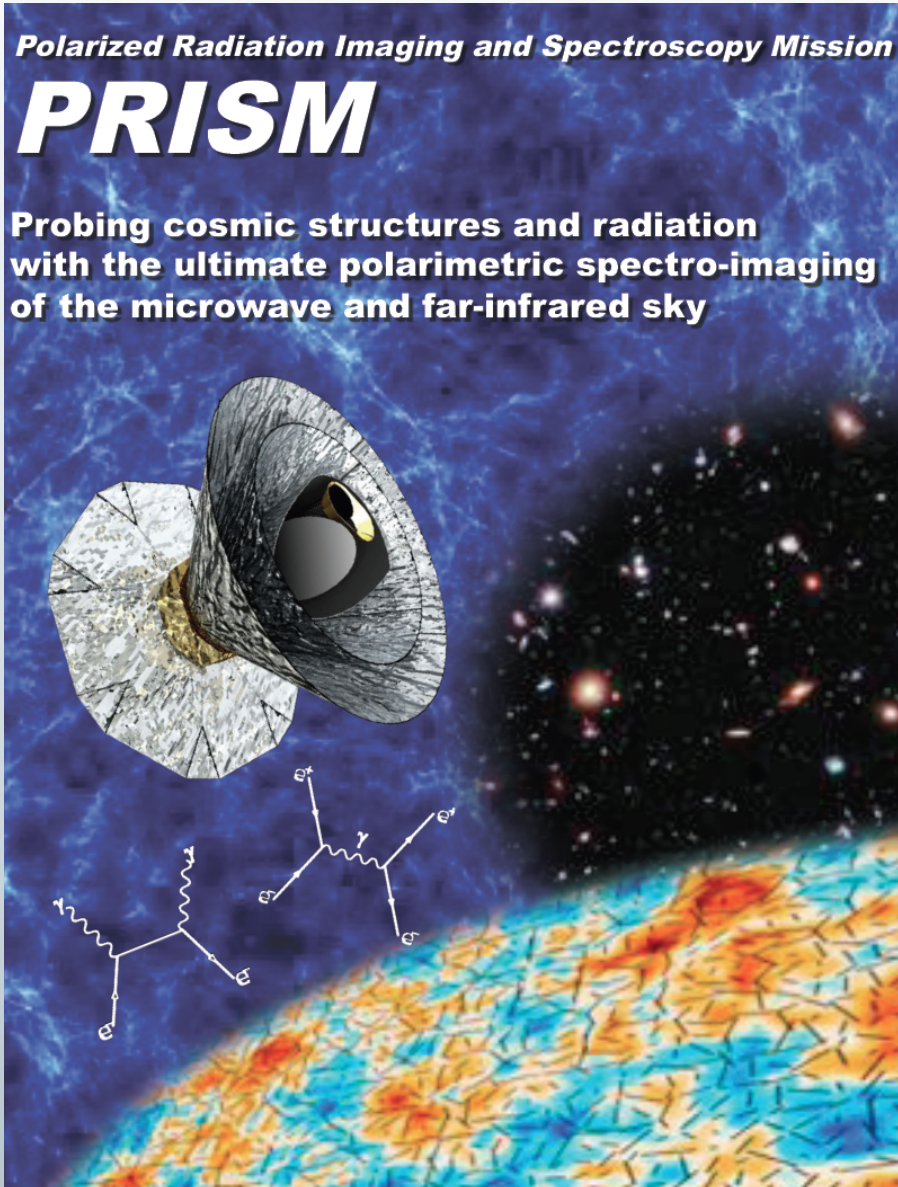
# Beyond Planck



*Polarized Radiation Imaging and Spectroscopy Mission*

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**Probing cosmic structures and radiation with the ultimate polarimetric spectro-imaging of the microwave and far-infrared sky**



Benjamin D. Wandelt

- Inflationary B-modes
- Probing new physics through CMB spectral distortions
- Full view of primordial perturbations in polarization
- The ultimate survey of clusters of galaxies
- Neutrino masses 0.04 eV from CMB alone

**Please register your support at**  
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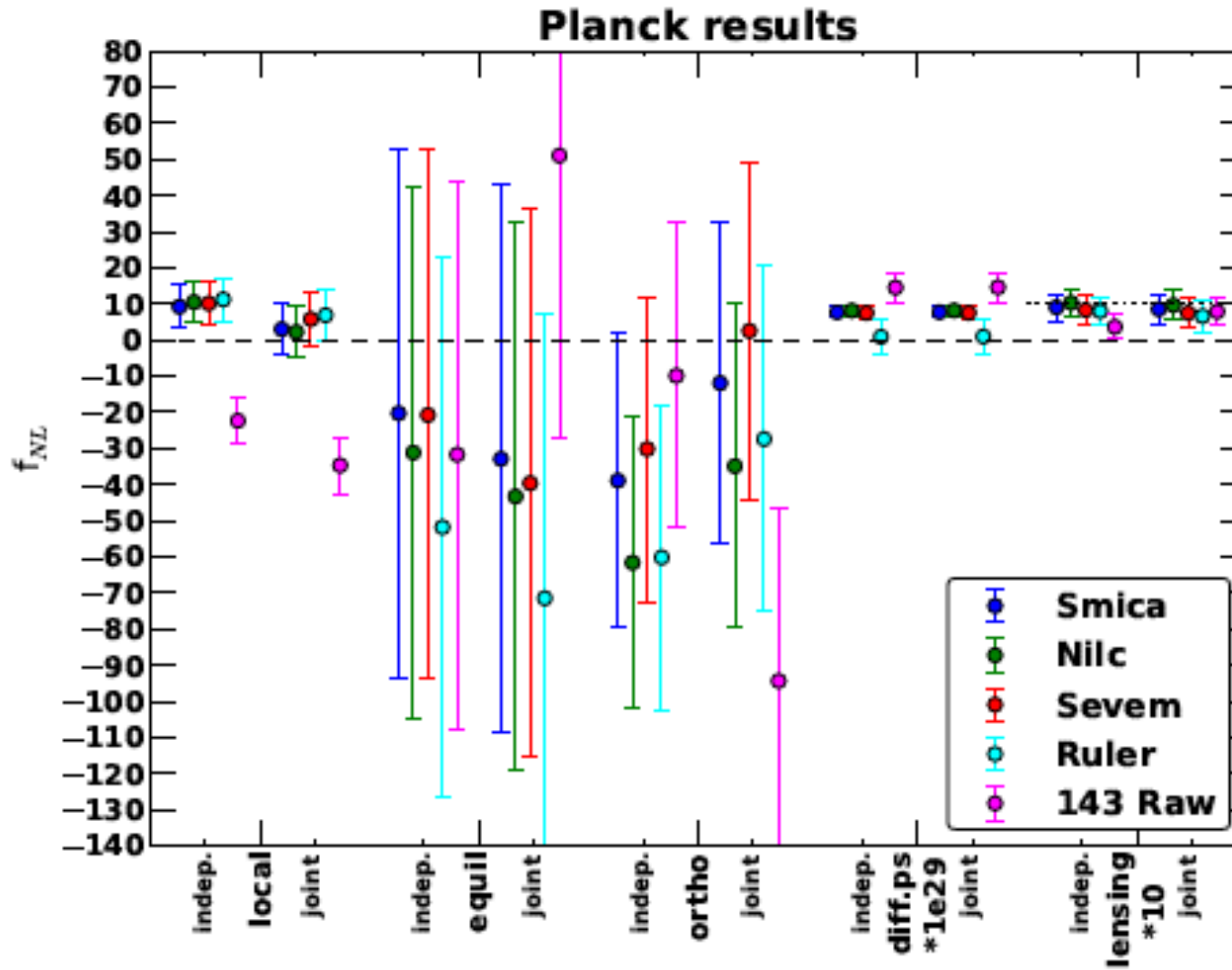
planck





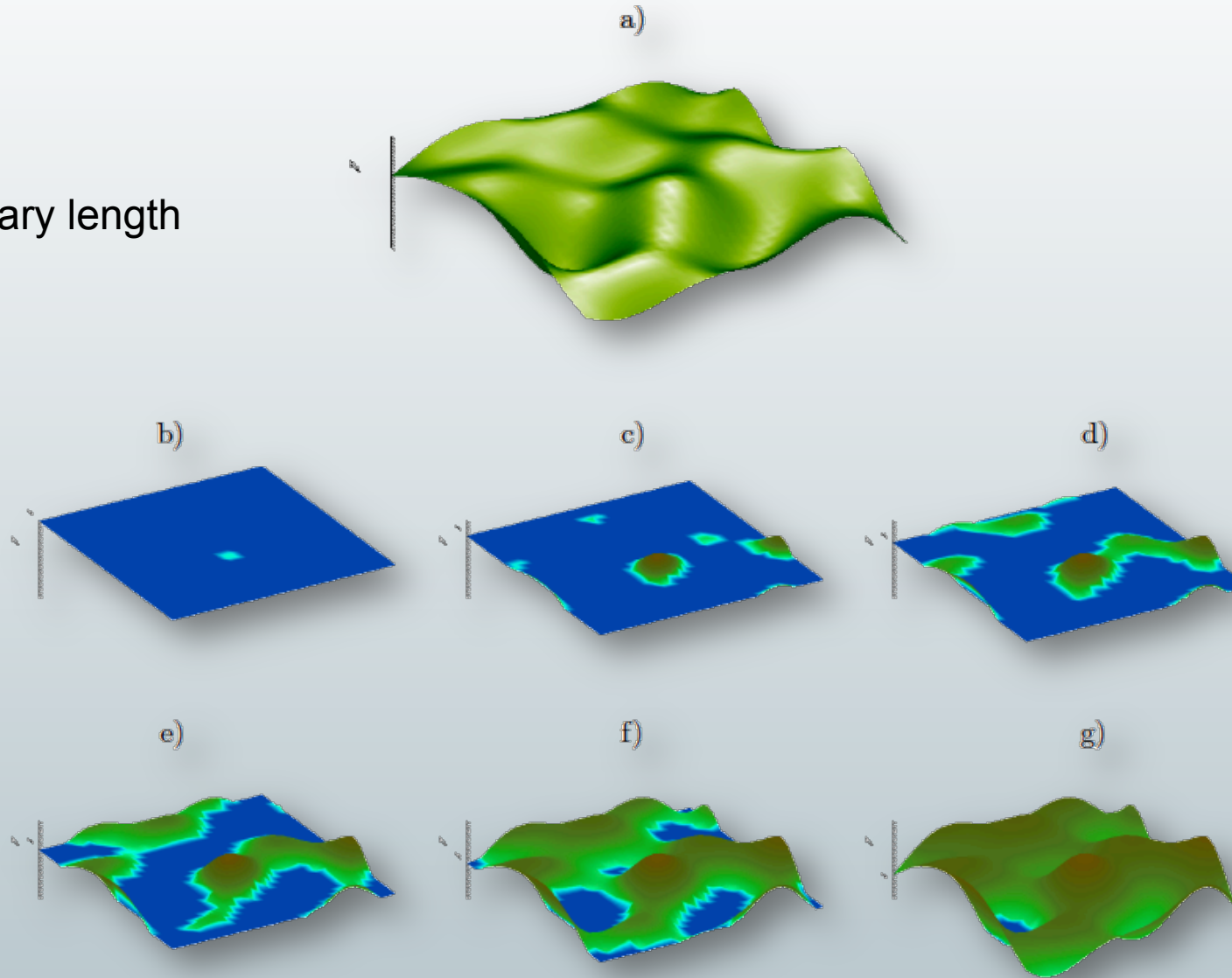
# Appendices

# Independent and joint analyses



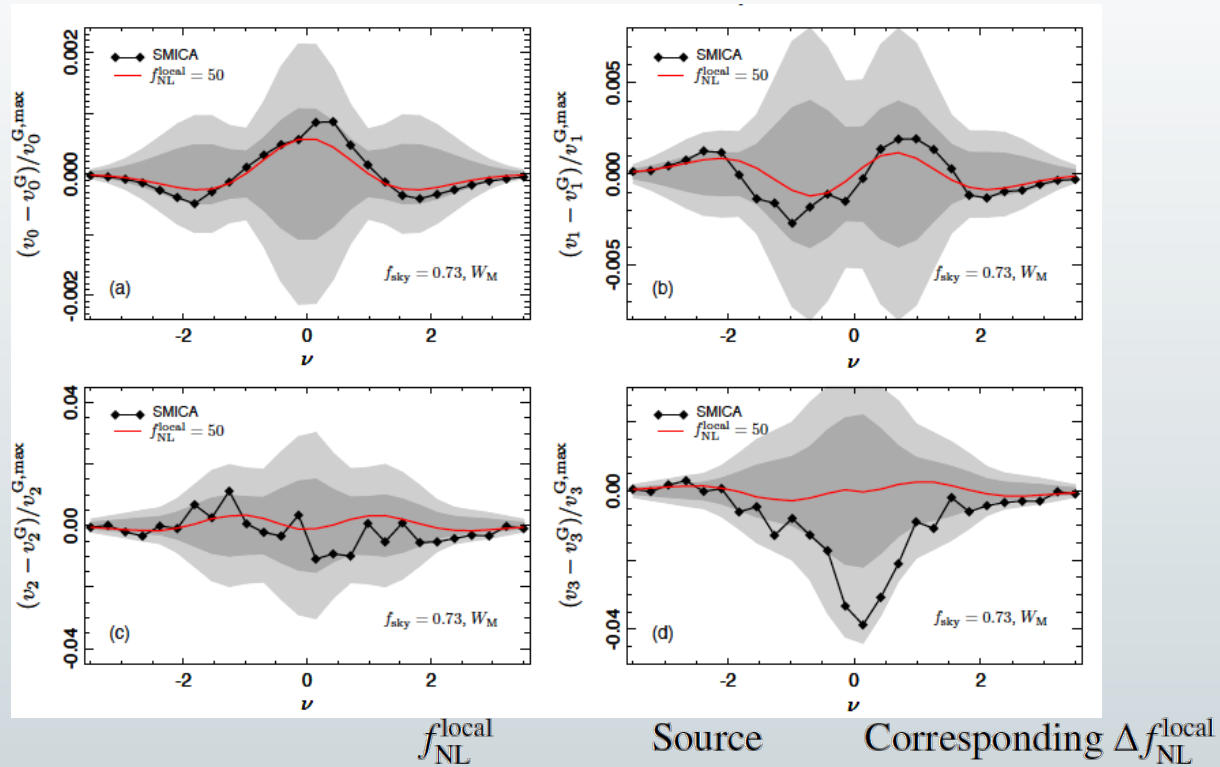


Area  
Boundary length  
Genus



Ducout 2012

# Minkowski functionals



	$f_{NL}^{\text{local}}$	Source	Corresponding $\Delta f_{NL}^{\text{local}}$
Raw map	$19.1 \pm 19.3$		—
Lensing subtracted	$8.5 \pm 20.5$	Lensing	+10.6
Lensing+PS subtracted	$7.7 \pm 20.3$	Point sources	+0.8
Lensing+CIB subtracted	$7.5 \pm 20.5$	CIB	+1.0
Lensing+SZ subtracted	$6.0 \pm 20.4$	SZ	+2.5
<b>All subtracted</b>	<b><math>4.2 \pm 20.5</math></b>	All	+14.9



# Planck TOI processing did not destroy non-Gaussian signals



1. ISW-lensing (3-pt, squeezed): weak  $2.6\text{-}\sigma$  signal at a level consistent with expectations from LCDM
2. CIB-lensing (3-pt, squeezed): very strong detection ( $\sim 40\text{-}\sigma$ ), consistent with observed CIB and lensing auto-spectra
3. Lensing (4-pt): strong detection consistent with LCDM
4. Modulation due to peculiar motion (4-pt) seen at a sensible level and in a plausible direction
5. Residual point sources (3-pt)  $5\text{-}\sigma$
6. Detailed agreement with the WMAP-9 findings in the scale range where WMAP is signal dominated ( $l < 600$ )

# Scalar Power Spectrum

Cosmological Fluctuations:

- are combined gauge invariant perturbations of the metric and of the inflaton field  $v$
- are the seeds of temperature anisotropies in the CMB  $v \propto \frac{\delta T}{T}$
- Follow a parametric amplifying equation of motion

$$v''_{\mathbf{k}} + \left[ k^2 - \frac{(a\sqrt{\epsilon_1})''}{a\sqrt{\epsilon_1}} \right] v_{\mathbf{k}} = 0$$

Power Spectrum:

$$P_v(k) = \frac{k^3}{2\pi^2} \langle \hat{v}_k^2 \rangle$$

$$= \frac{a^2 H^2}{8\pi^2 M_{\text{Pl}}^2 \epsilon_{1\diamond}} \left[ 1 - (2\epsilon_{1\diamond} + \epsilon_{2\diamond} + \dots) \ln \frac{k}{k_\diamond} + \left( 2\epsilon_{1\diamond}^2 + \epsilon_{1\diamond}\epsilon_{2\diamond} + \frac{\epsilon_{2\diamond}^2}{2} - \frac{\epsilon_{2\diamond}\epsilon_{3\diamond}}{2} + \dots \right) \ln^2 \frac{k}{k_\diamond} + \dots \right]$$

Spectral index  $n_S = \left. \frac{d \ln P}{d \ln k} \right|_{k_*}$

$$n_S^{\text{Planck}} \sim 0.96$$

Gravity waves:

$$r = \frac{P_h(k_*)}{P_v(k_*)} = 16\epsilon_{1*} + \dots$$



# The ekpyrotic prediction



Print Sidebar Steinhardt.F4v

the big bang is a big bounce

- no flatness or causal connectedness problem
- new mechanism for smoothing the universe prior to the bang
- new mechanism for generating scale-invariant density perturbations
- no transplanckian problem

**predictions:**

- no observable tensor modes in CMB

**non-gaussianity  $|f_{NL}(\text{local})| = 20-50$  correlated with tilt**

-----

cyclic universe

- may compete successfully with inflation (see J-L Lehners 2012)
- may explain what we have learned about the state of the vacuum

Applications Creminelli3.hi.mp4 -26:20

March, 6  
2013  
Perimeter