



# 12<sup>th</sup> Zimányi Winter School on Heavy Ion Physics



## Kaon source imaging with the **STAR** experiment in 200 GeV Au+Au collisions at RHIC



Róbert Vértési  
(for the STAR collaboration)

Nuclear Physics Institute  
Czech Academy of Sciences

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MINISTERSTVO ŠKOLSTVÍ,  
MLÁDEŽE A TĚLOVÝCHOVY



OP Vzdělávání  
pro konkurenceschopnost

INVESTICE DO ROZVOJE VZDĚLÁVÁNÍ

# The RHIC facility



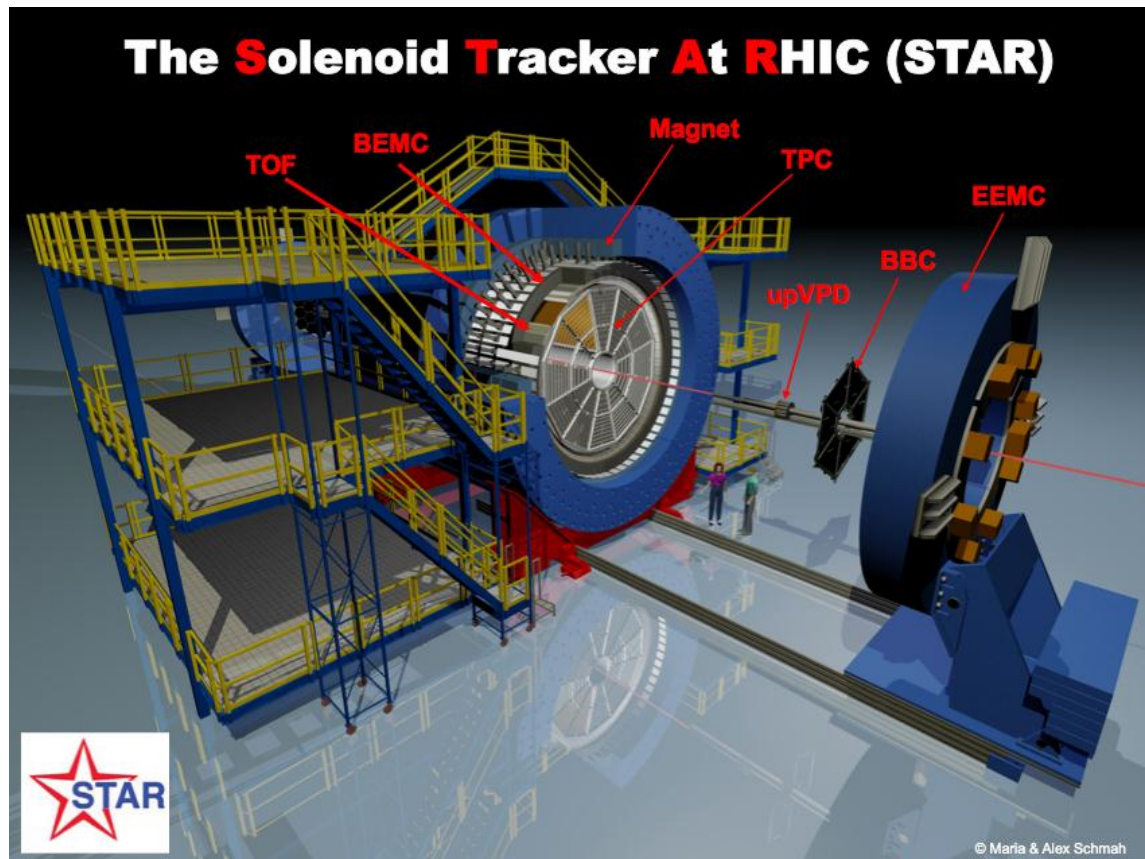
- Two independent rings
  - 3,9 km long each
- Collides heavy ions...
  - **Au+Au, Cu+Cu, U+U...**
  - $\sqrt{s_{NN}} = 7,7 - 200 \text{ GeV}$
- ...and protons
  - **p+p** up to  $\sqrt{s} = 500 \text{ GeV}$
  - Different polarization patterns
- Asymmetric setups
  - **d+Au, Cu+Au ...**
- 4 experiments
  - All different capabilities
  - PHENIX, STAR (the „large” ones)
  - PHOBOS, BRAHMS (completed)



# The STAR Experiment



## The Solenoid Tracker At RHIC (STAR)



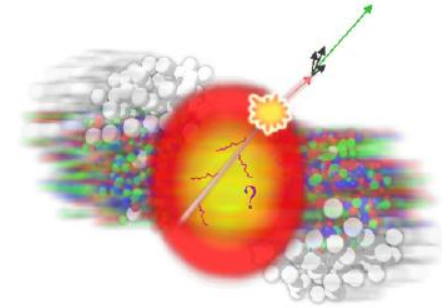
- Time Projection Chamber
  - $dE/dx$
  - Momentum
- Time of Flight detector
  - Velocity ( $1/\beta$ )
- Electromagnetic Calorimeter
  - $E/p$
  - trigger

# Hot nuclear matter

Nucl. Phys. A 757 (2005) p1 ; p28; p102 ; p184 [white papers]

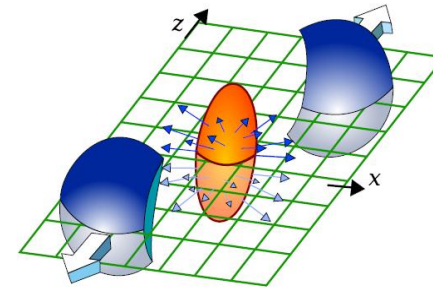
- Extremely dense

- Au+Au: jet suppression
  - No effect in d+Au
- Strongly interacting, new state of matter
- $\lambda \sim 3 \text{ fm}$  (5 GeV jet)



- Perfect fluid of quarks

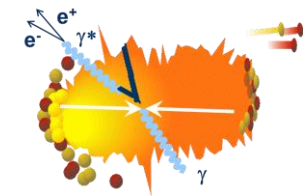
- Contradicts expectations
  - Degrees of freedom: quarks
  - Viscosity consistent with theoretical limit
- $\eta/s \sim \hbar/4\pi$ ,  $c_s = 0.35c$



- Quark Gluon Plasma (sQGP)

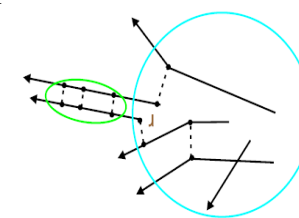
Phys.Rev.Lett. 104, 132301 (2010)

- Thermal radiation,  $T_{\text{init}} \sim 4 \times 10^{12} \text{ K}$
  - $T_{\text{init}} > 300 \text{ MeV} \gg T_{\text{Hagedorn}}$ ,  $\epsilon_{\text{init}} \sim 15 \text{ GeV/fm}^3$ ,  $p_{\text{init}} \geq 1.5 \text{ GeV/fm}^3$



- Evolution of the particle source?

- Dynamics, space-time extent ← correlations



# HBT source and correlation

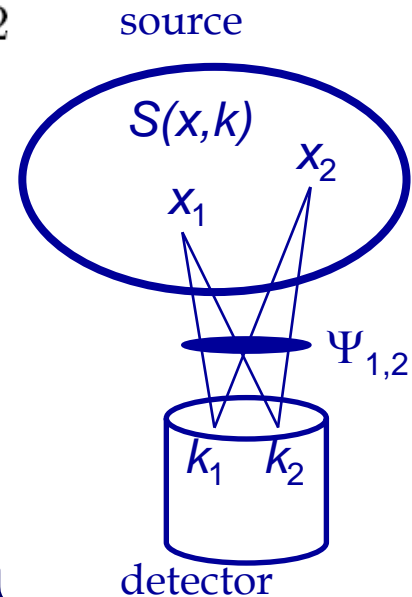


The invariant correlation function

$$C_2(k_1, k_2) = \frac{N_2(k_1, k_2)}{N_1(k_1)N_1(k_2)} \simeq 1 + \left| \frac{\tilde{S}(q, K)}{\tilde{S}(0, K)} \right|^2$$

$$N_1(k_1) = \int S(x_1, k_1) |\Psi_1|^2 dx_1$$

$$N_2(k_1, k_2) = \int S(x_1, k_1) S(x_2, k_2) |\Psi_{1,2}|^2 dx_1 dx_2$$



Depends on relative and average momenta

$$q = k_1 - k_2, K = 0.5(k_1 + k_2)$$

Includes Fourier-transformed form of the source

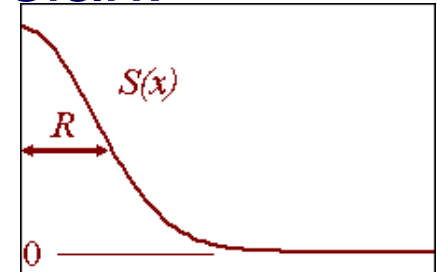
$$\tilde{S}(q, K) = \int dx S(x, k) e^{iqx}$$



# Gaussian approximation

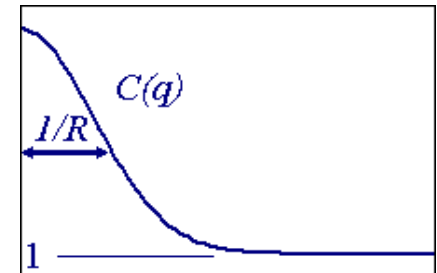
- If the source is approximated with Gaussian:

$$S(x) \sim \exp \left( -\frac{r_x^2}{2R_x^2} - \frac{r_y^2}{2R_y^2} - \frac{r_z^2}{2R_z^2} \right)$$



- Then the correlation function is also Gaussian:

$$C(q) - 1 \sim \exp \left( -q_x^2 R_x^2 - q_y^2 R_y^2 - q_z^2 R_z^2 \right)$$



- These radii are the so-called **HBT radii**
- Often specified in the LCMS system (not invariant)
  - Out:** direction of the mean transverse momentum of the pair
  - Side:** orthogonal to out

- Long:** beam direction

$$C(q) = 1 + \lambda \exp \left( -q_o^2 R_o^2 - q_s^2 R_s^2 - q_l^2 R_l^2 \right)$$

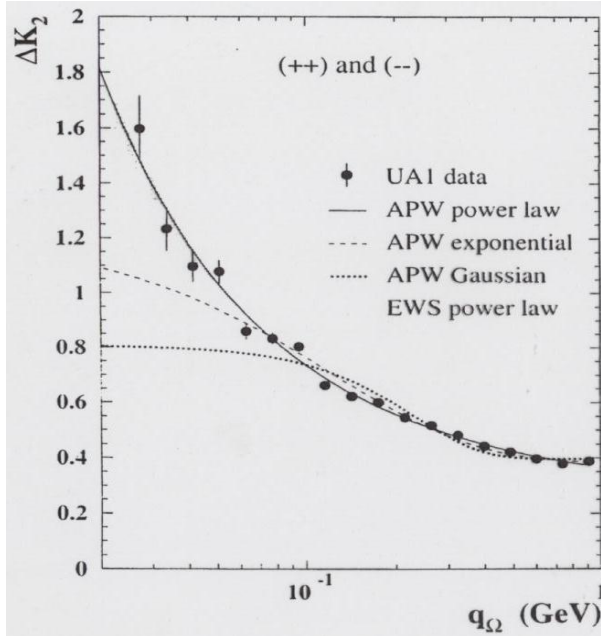
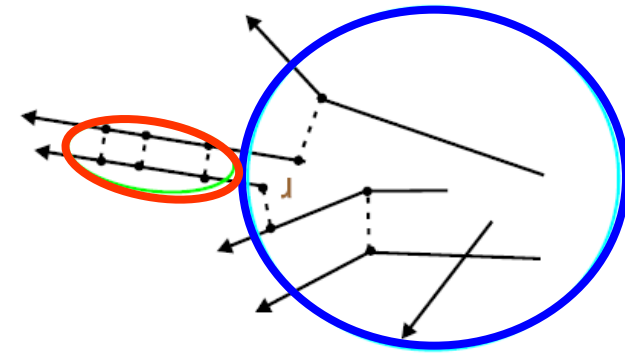
- Do not necessarily reflect the geometrical size

# Complications...

## Our source is not Gaussian

- Sometimes Gaussian assumption is meaningless
- Example: Lévy-function  

$$C_0 - 1 \sim \lambda \exp(-|qR|^\alpha)$$



## Final State Interactions

- Coulomb force  
(Have to correct for this)

$$C_0(q) = C_{\text{raw}}(q) K_{\text{coulomb}}^{-1}$$

1.  $K_{\text{coulomb}}$  is computed analytically
2.  $C_0$  is fitted,  $R, \lambda, \alpha$  determined

- Strong FSI ...

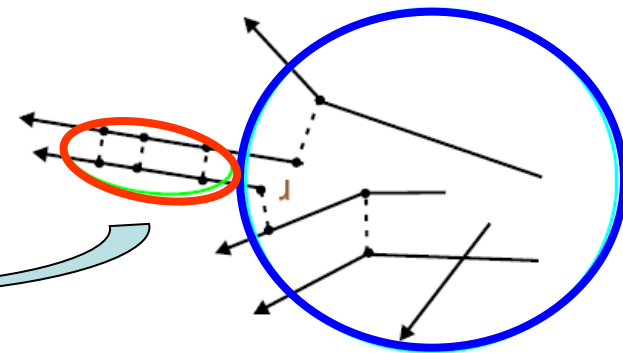
# Source Imaging – a general way



D. A. Brown, P. Danielewicz, nucl-th/9701010

- Instead of  $C_{\text{raw}}(q)$  we directly go for  $S(\mathbf{r})$

$$C(q) - 1 = 4\pi \int drr^2 K(q, r) S(r)$$



- 2-particle source function and relative position
- Evaluated in a specific transverse momentum range

- Numerically invert this equation

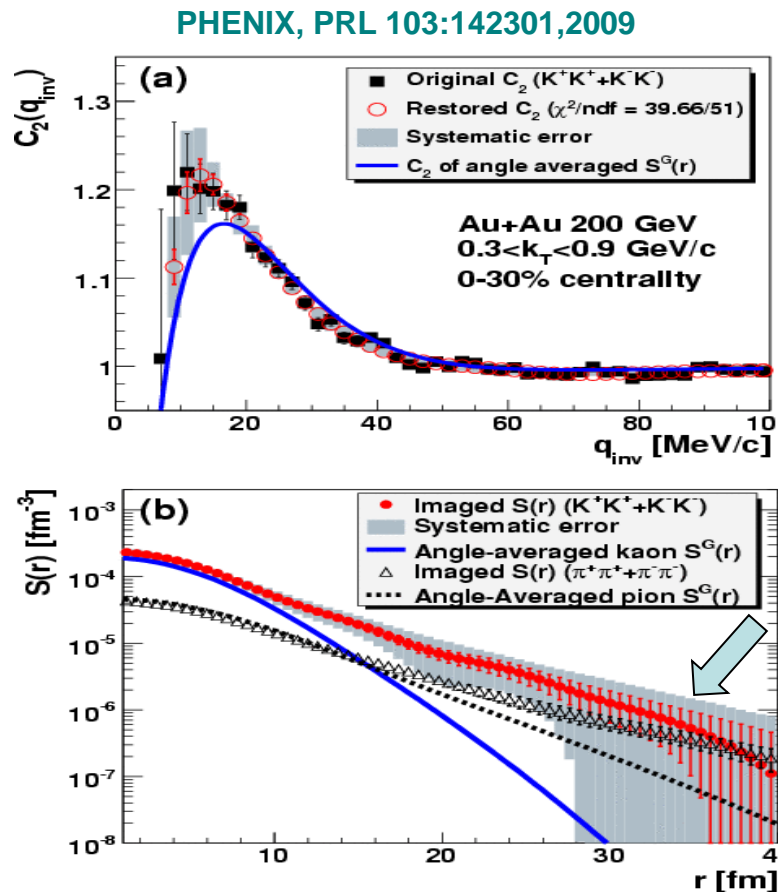
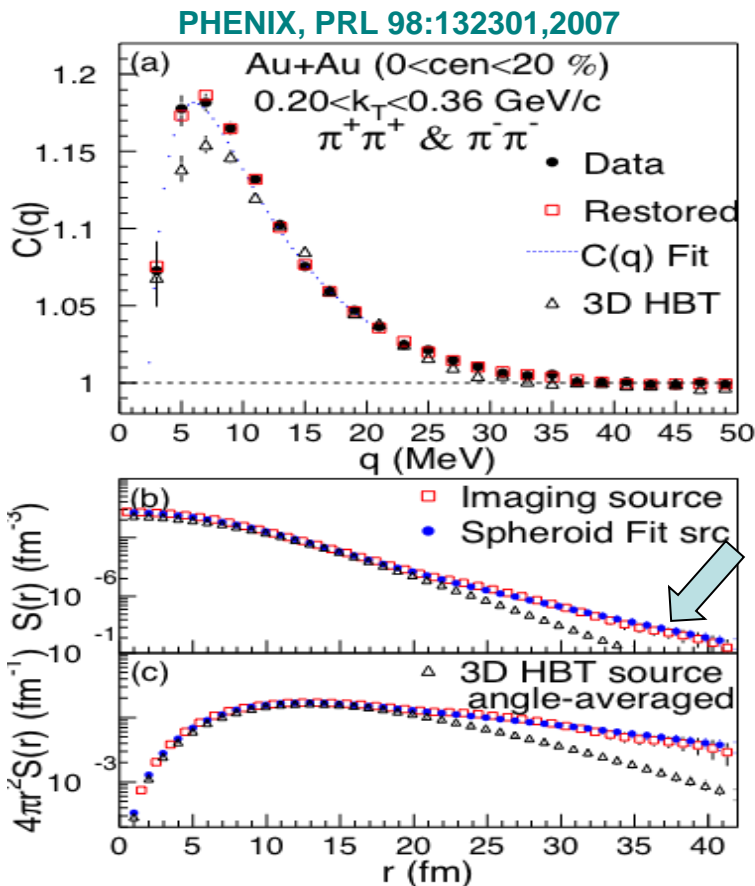
- No analytical solution, hence systematic errors
- But **no assumptions for the shape** of the source
- Final state interactions included as well as Coulomb interactions

- Approximations during FT  $\hat{S}(q)$

- Assumption of weak dependence in single particle sources
- Computation is numerical, ie. integration cut-off, though finite resolution in  $\mathbf{r}$
- Derived  $S(\mathbf{r})$  formula has further assumptions...



# PHENIX 1D pions and kaons



- Observed **long tail** in 1D pion correlation
- Attributed to resonance decays and non-zero emission duration
- Former contradicted by even **more pronounced tail** in kaon C

# 3D source shape analysis



## Expansion of $R(\mathbf{q})$ and $S(\mathbf{r})$ in Cartesian Harmonic basis

Danielewicz and Pratt, Phys.Lett. B618:60, 2005

$$R(\mathbf{q}) = \sum_l \sum_{\alpha_1 \dots \alpha_l} R_{\alpha_1 \dots \alpha_l}^l(q) A_{\alpha_1 \dots \alpha_l}^l(\Omega_q) \quad (1)$$

$$S(\mathbf{r}) = \sum_l \sum_{\alpha_1 \dots \alpha_l} S_{\alpha_1 \dots \alpha_l}^l(r) A_{\alpha_1 \dots \alpha_l}^l(\Omega_q) \quad (2)$$

$\alpha_i = \mathbf{x}, \mathbf{y}$  or  $\mathbf{z}$

$\mathbf{x} = \text{out-direction}$

$\mathbf{y} = \text{side-direction}$

$\mathbf{z} = \text{long-direction}$

### 3D Koonin-Pratt:

$$R(\mathbf{q}) = C(\mathbf{q}) - 1 = 4\pi \int dr^3 K(\mathbf{q}, \mathbf{r}) S(\mathbf{r}) \quad (3)$$

$$\text{Plug (1) and (2) into (3)} \Rightarrow R_{\alpha_1 \dots \alpha_l}^l(q) = 4\pi \int dr^3 K_l(q, r) S_{\alpha_1 \dots \alpha_l}^l(r) \quad (4)$$

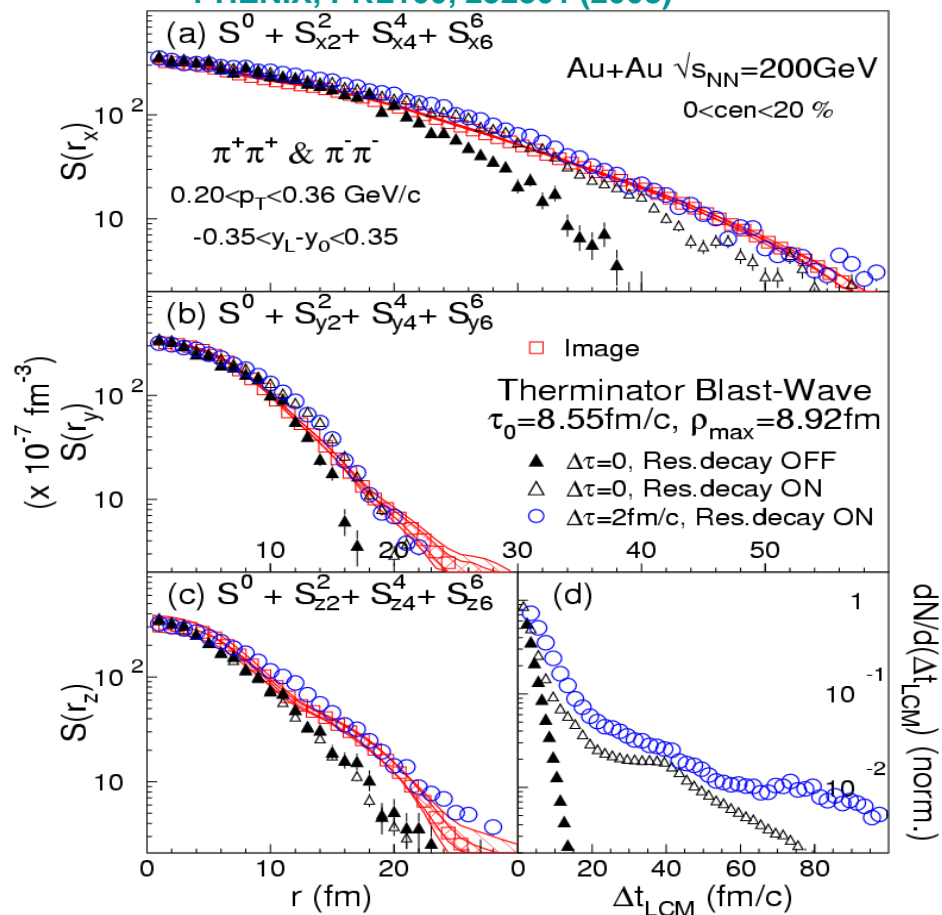
$$\text{Invert (1)} \Rightarrow R_{\alpha_1 \dots \alpha_l}^l(q) = \frac{(2l+1)!!}{l!} \int \frac{d\Omega_q}{4\pi} A_{\alpha_1 \dots \alpha_l}^l(\Omega_q) R(\mathbf{q})$$

$$\text{Invert (2)} \Rightarrow S_{\alpha_1 \dots \alpha_l}^l = \frac{(2l+1)!!}{l!} \int \frac{d\Omega_q}{4\pi} A_{\alpha_1 \dots \alpha_l}^l(\Omega_q) S(\mathbf{q})$$

# 3D pions, PHENIX vs. STAR



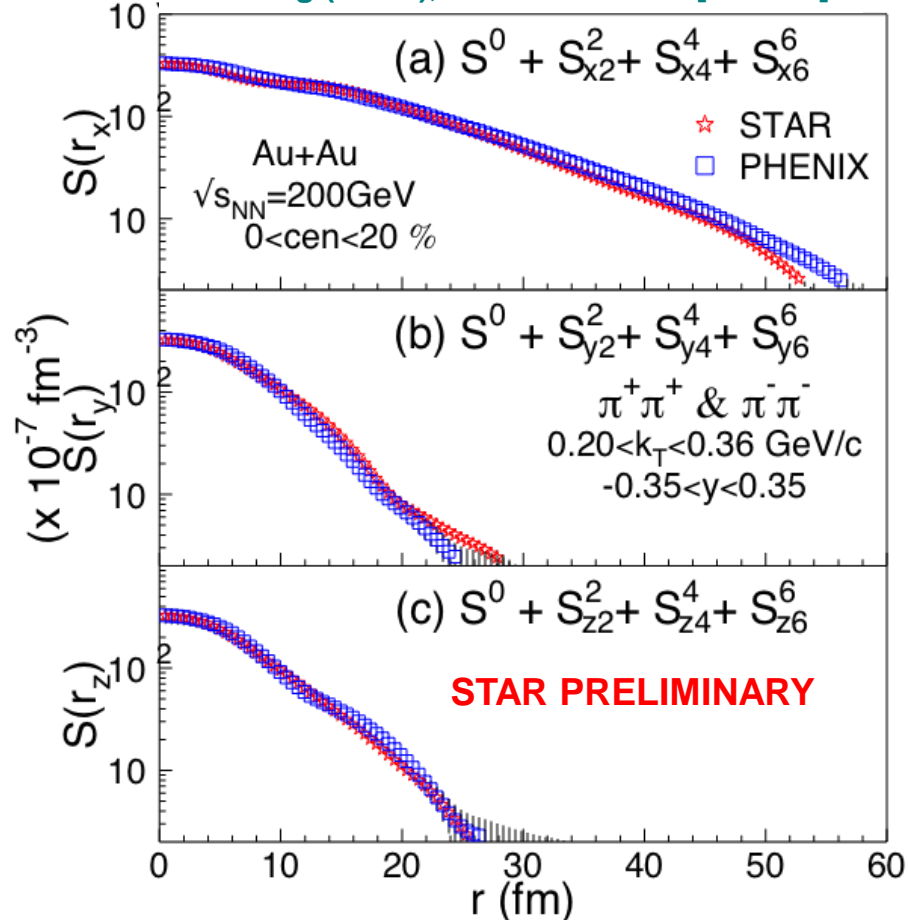
PHENIX, PRL100, 232301 (2008)



Elongated source in “out” direction

Therminator Blast Wave model suggests non-zero emission duration

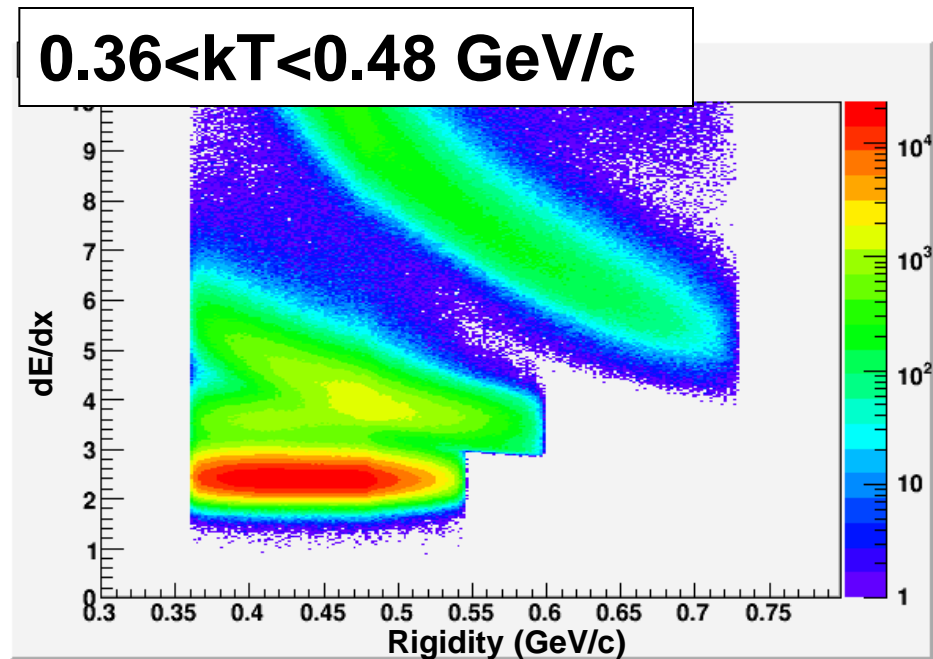
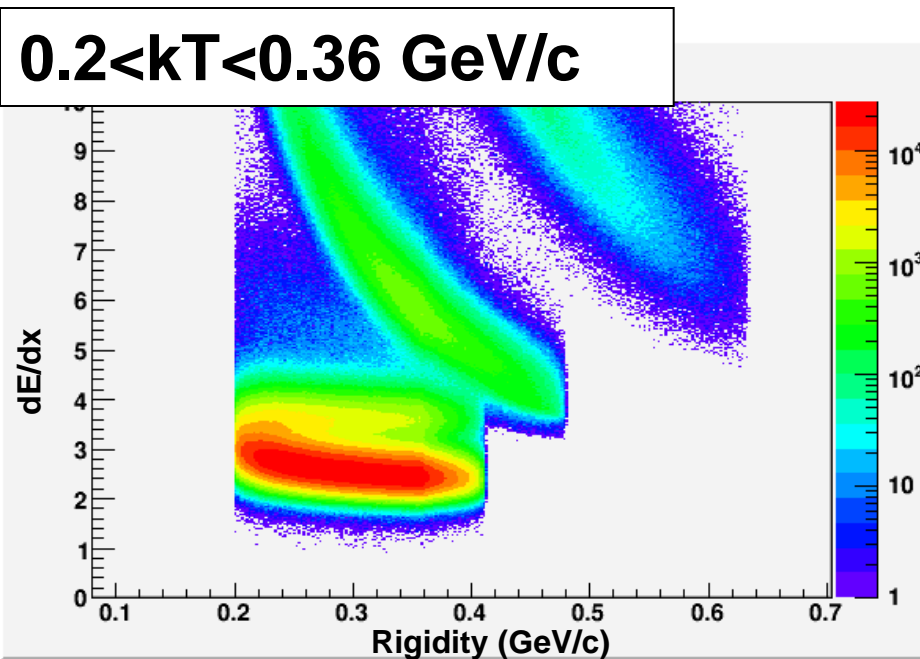
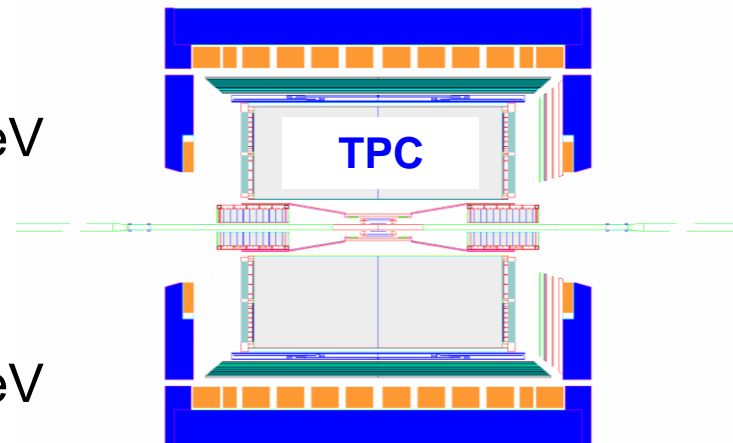
P. Chung (STAR), arXiv:1012.5674 [nucl-ex]



Very good agreement of PHENIX and STAR 3D pion source images

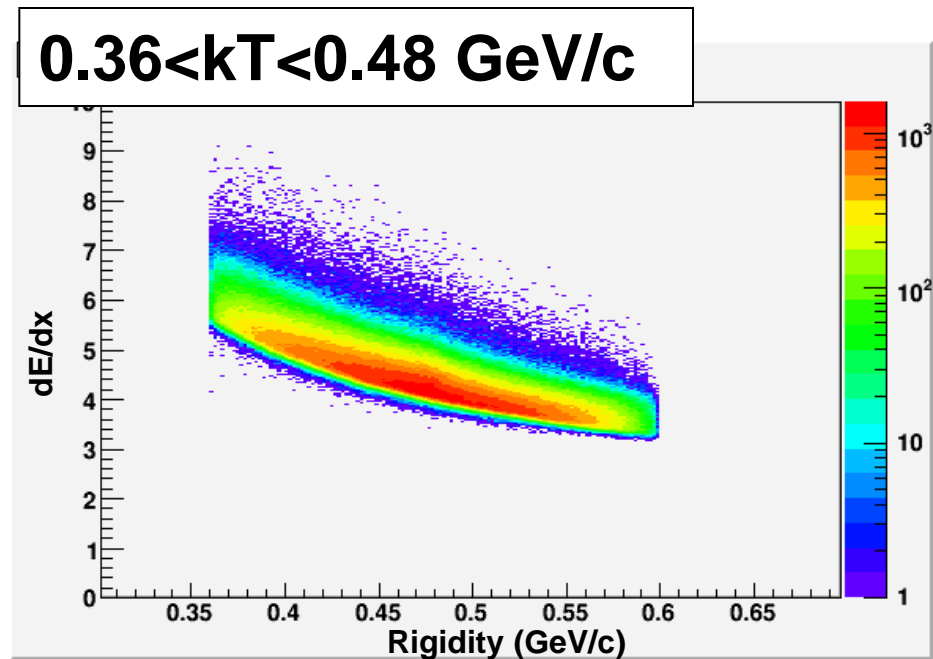
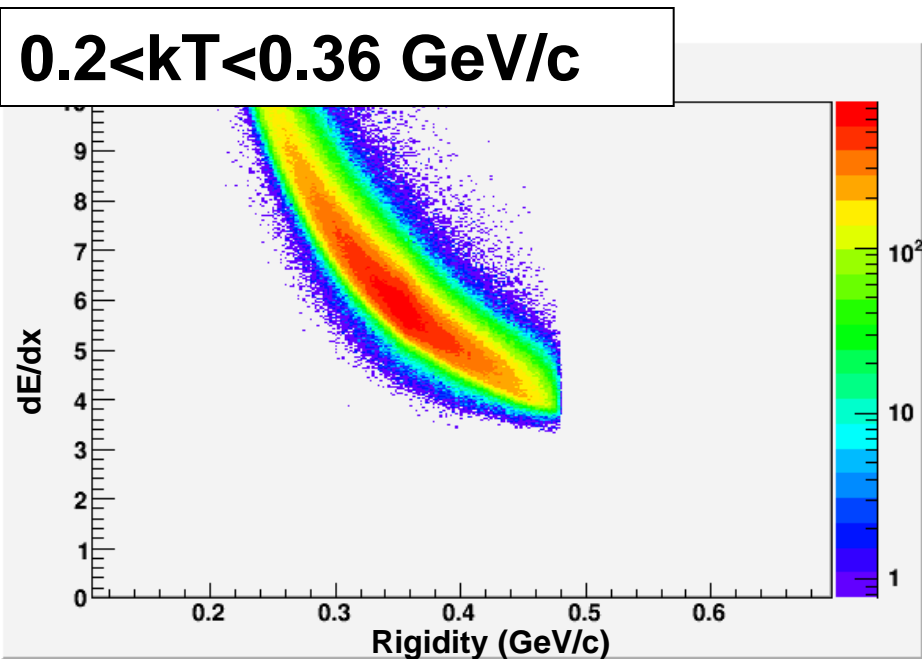
# Kaon analyses

- Dataset #1 (Source shape analysis)
  - 20% most central Au+Au @  $\sqrt{s_{NN}}=200$  GeV
  - Run 4: 4.6 Mevts, Run 7: 16 Mevts
- Dataset #2 (mT-dependent analysis)
  - 30% most central Au+Au @  $\sqrt{s_{NN}}=200$  GeV
  - Run 4: 6.6 Mevts

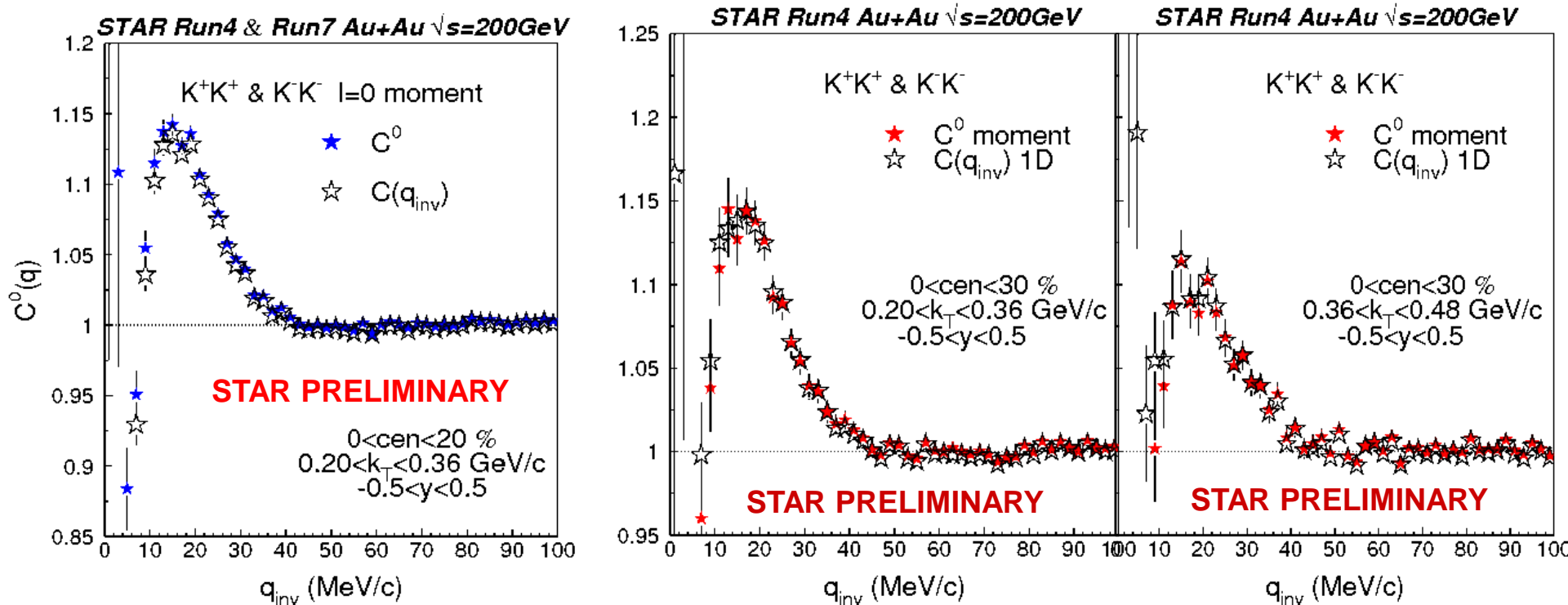


# PID cut applied

- Dataset #1 (Source shape analysis)
  - $dE/dx$ :  $\sigma(\text{Kaon}) < 2.0$  and  $\sigma(\text{Pion}) > 3.0$  and  $\sigma(\text{electron}) > 2.0$
  - $|y| < 0.5$
  - $0.2 < p_T < 0.4 \text{ GeV}/c$
- Dataset #2 (mT-dependent analysis)
  - $-1.5 < \sigma(\text{Kaon}) < 2.0$
  - $-0.5 < \sigma(\text{Kaon}) < 2.0$



# Kaon $C_0(q_{inv})$ vs. $C(q_{inv})$



**$l=0$  moment in agreement with 1D  $C(q)$**



# Fit to correlation moments #1

- Trial functional form for  $S(r)$ :  
4-parameter ellipsoid (3D Gauss)

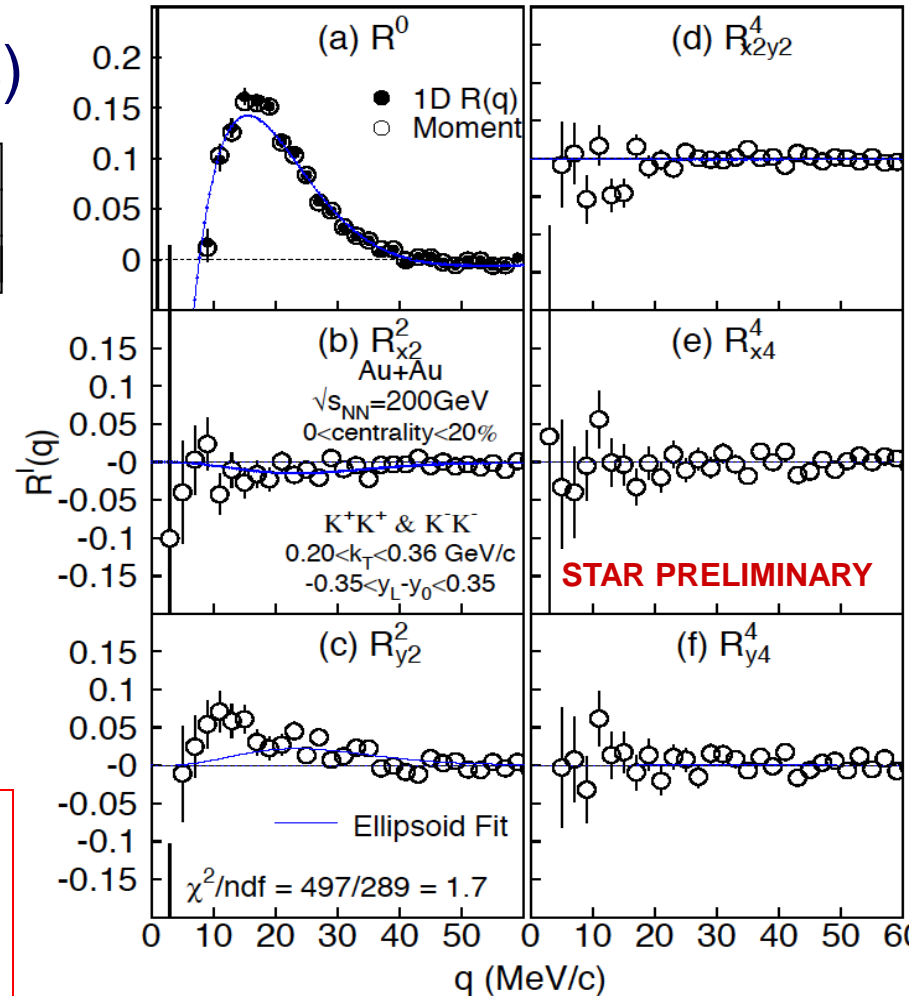
$$S^G(x, y, z) \equiv \frac{l}{(2p)^3 r_x r_y r_z} \exp \left[ - \left( \frac{x^2}{4r_x^2} + \frac{y^2}{4r_y^2} + \frac{z^2}{4r_z^2} \right) \right]$$

- Fit to  $C(q)$ : technically a simultaneous fit on 6 independent moments

$$R^l_{\alpha_1 \dots \alpha_l}, \quad 0 \leq l \leq 4$$

- Result: statistically good fit

<b>Dataset #1</b>	$\lambda = 0.48 \pm 0.01$
<b>Run4+Run7</b>	$r_x = (4.8 \pm 0.1) \text{ fm}$
<b>Cent&lt;20%</b>	$r_y = (4.3 \pm 0.1) \text{ fm}$
<b>0.2&lt;kT&lt;0.36 GeV/c</b>	$r_z = (4.7 \pm 0.1) \text{ fm}$

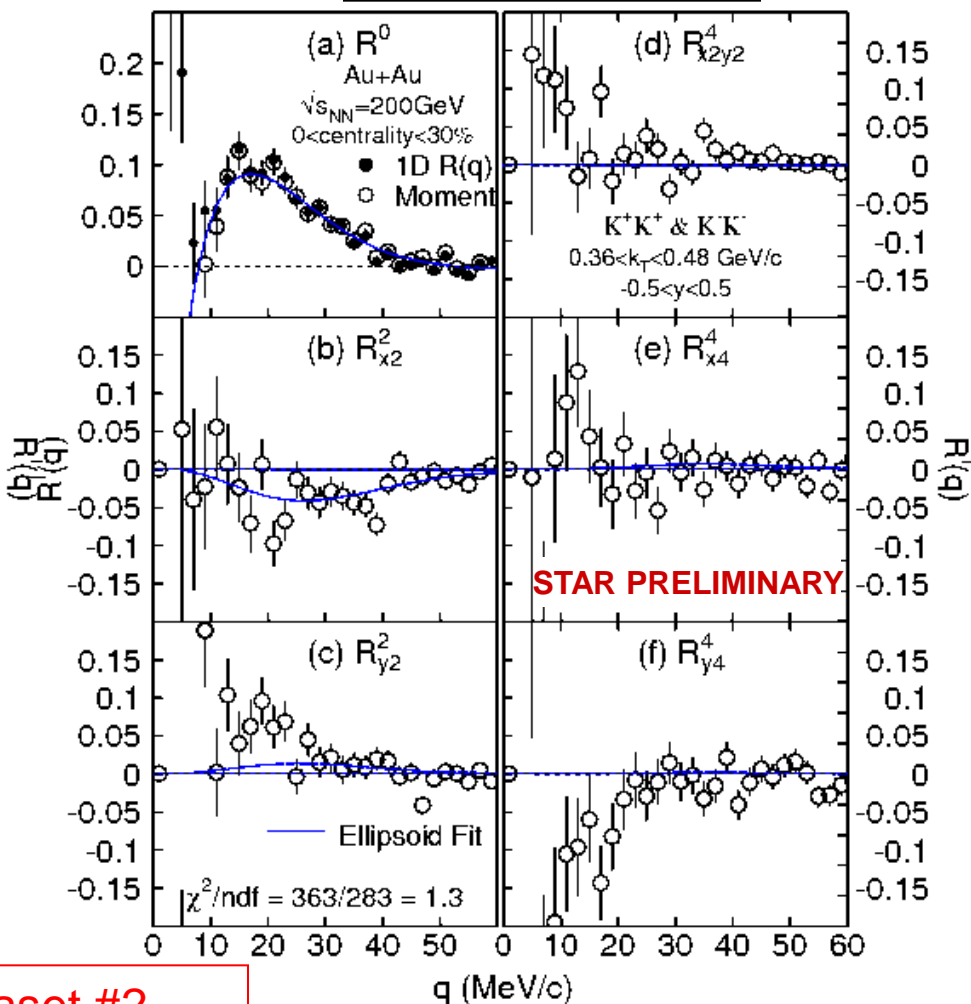
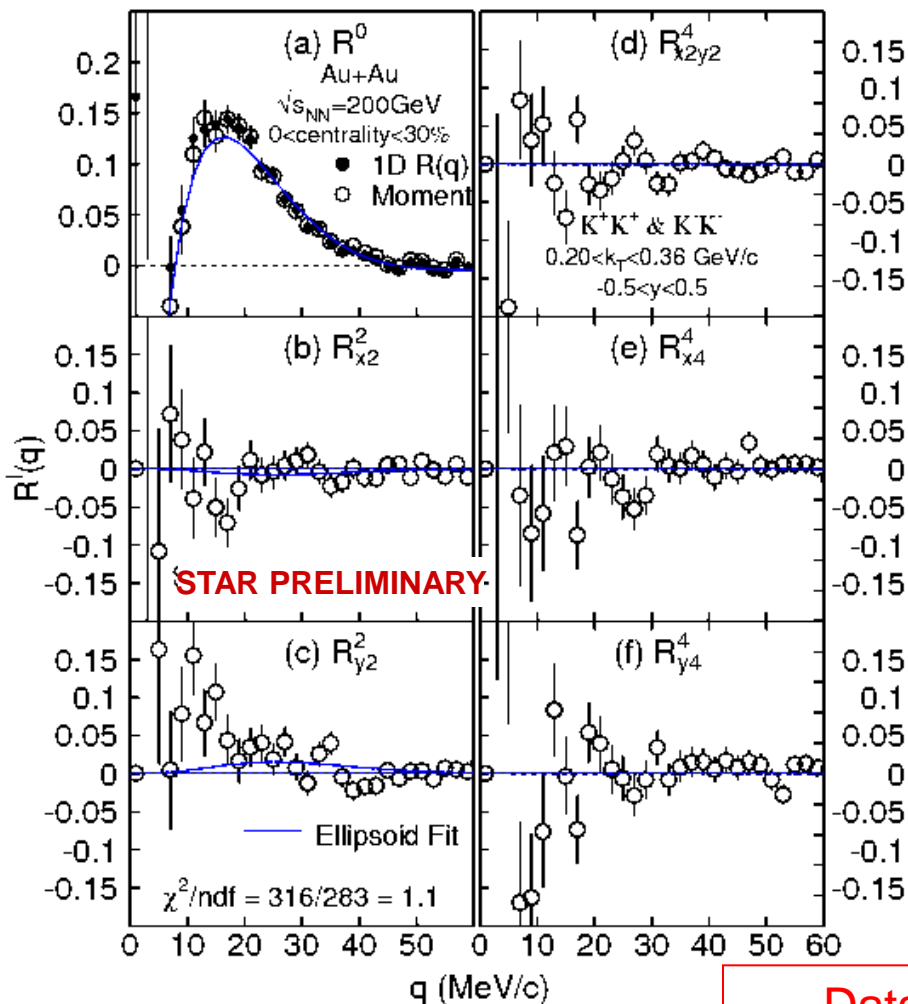


# Fit to correlation moments #2



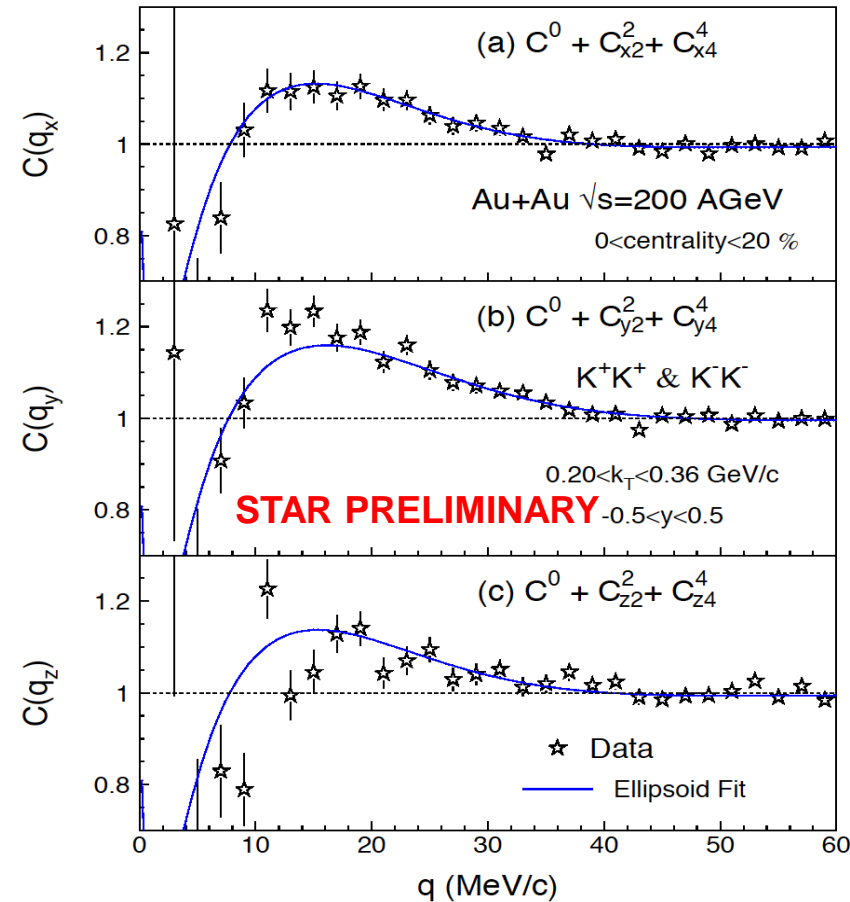
0.2 < kT < 0.36 GeV/c

0.36 < kT < 0.48 GeV/c



Dataset #2  
Run4 Cent < 30%

# 3D Kaon source vs. Model

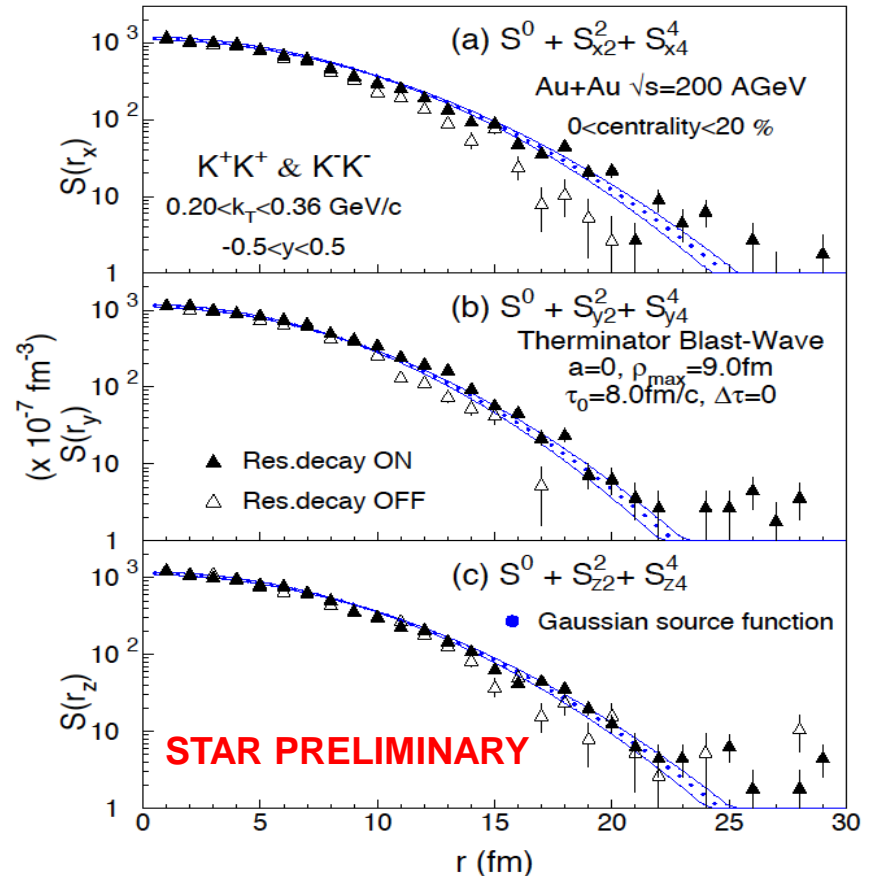


## Correlation profiles

$$C(q_x) \equiv C(q_x, 0, 0)$$

$$C(q_y) \equiv C(0, q_y, 0)$$

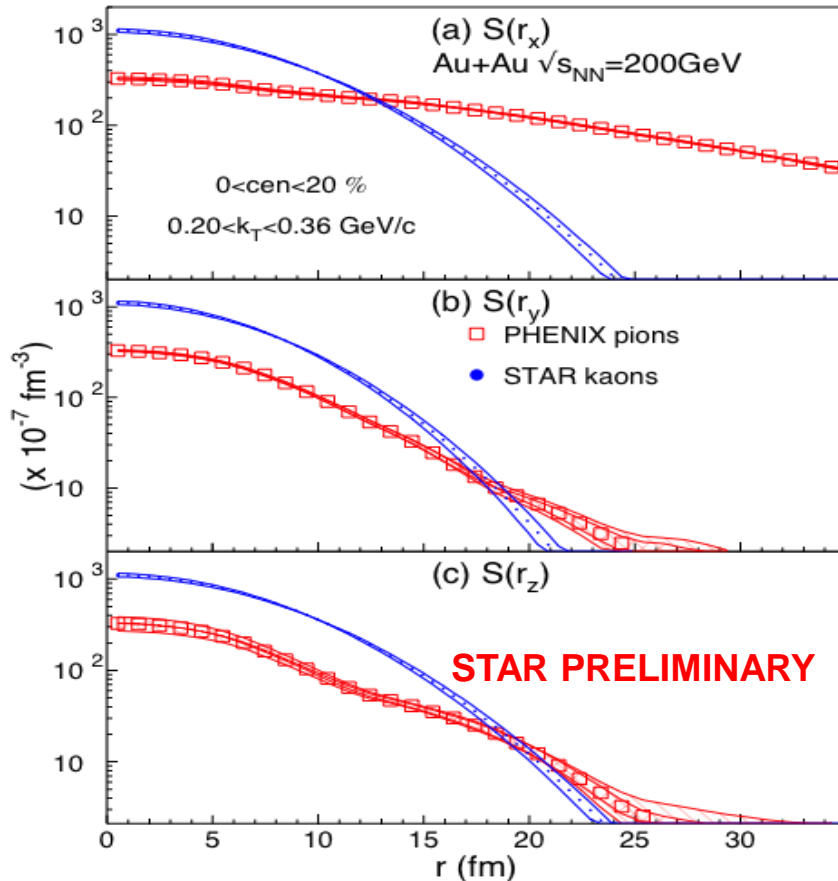
$$C(q_z) \equiv C(0, 0, q_z)$$



Source consistent with Therminator Blast Wave model w/ resonances

- Instant freeze-out at  $\tau_0 = 0.8$  fm/c
- Zero emission duration

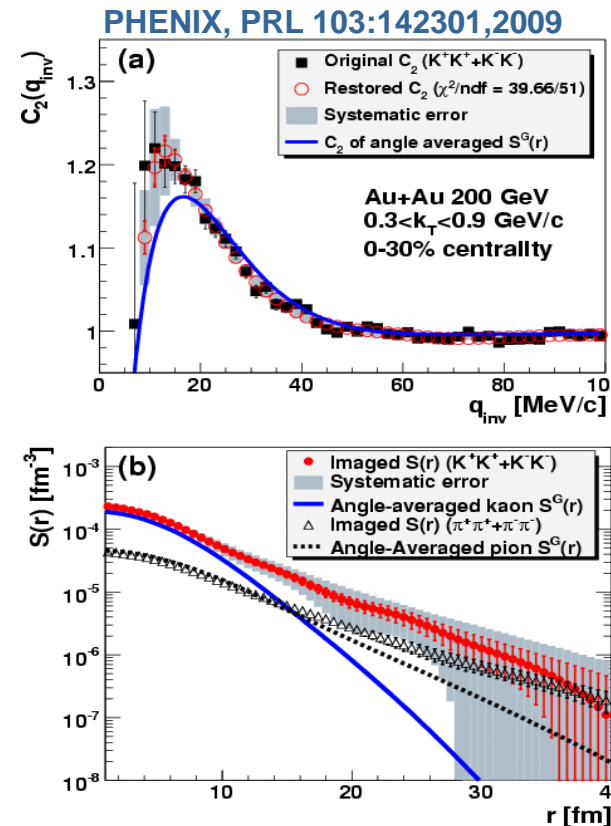
# Data comparison



Kaon vs. Pion: different shape

- Gaussian, no long tail present
- Sign of different freeze-out dynamics?

Note: systematic errors for kaons are not represented



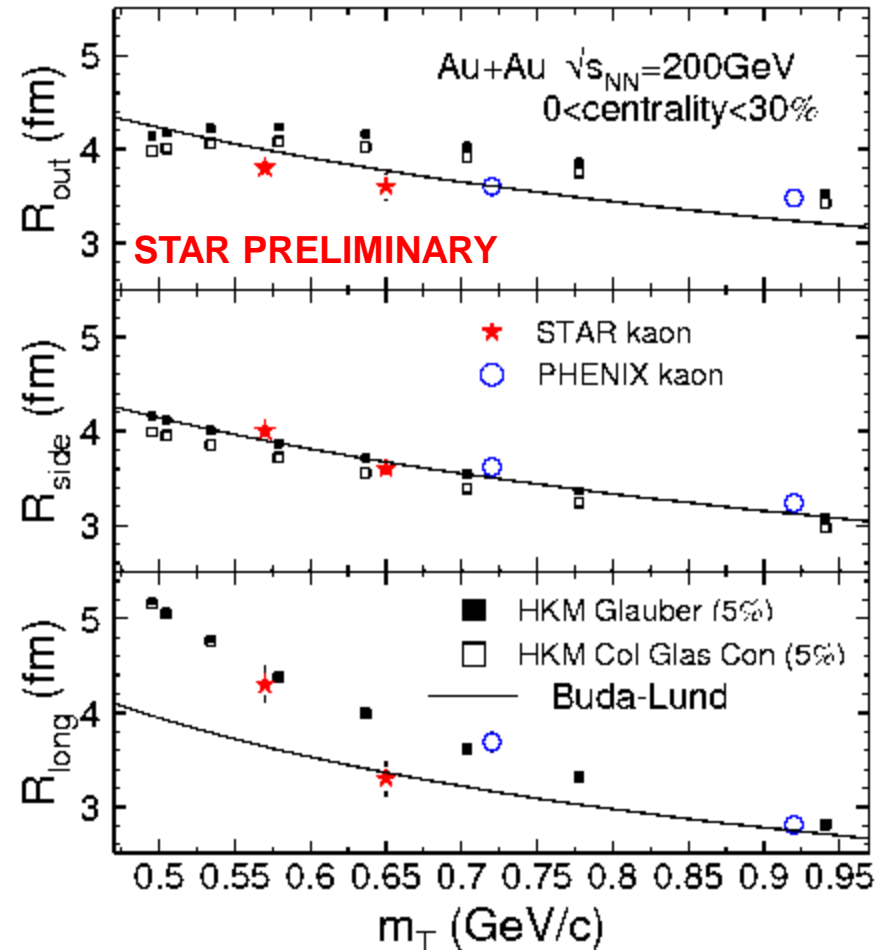
1D PHENIX kaon:

- Observed long tail due to wide  $k_T$  bin?  
 $0.3 < k_T < 0.9 \text{ GeV}$

# Transverse mass dependence

P. Chung (STAR), PoS WPCF2011 (2011) 036

- Rising trend at low  $m_T$
- Buda-Lund model
  - Inherent  $m_T$ -scaling
  - Works perfectly for pions
  - Deviates from kaons in the “long” direction in the lowest  $m_T$  bin
- HKM (Hidro-kinetic model)
  - Describes all trends
  - Some deviation in the “out” direction
  - Note the different centrality definition



Note: systematic errors are not represented here

Buda-Lund: arXiv:0801.4434v2

HKM: PRC81, 054903 (2010)

# Summary

- First model-independent extraction of kaon 3D source shape presented
- No significant non-Gaussian tail is observed in  $\sqrt{s_{NN}}=200$  GeV central RHIC data
- Comparison with Therminator model indicates that kaons and pions may be subject to different dynamics
- The  $m_T$ -dependence of the Gaussian radii indicates that  $m_T$ -scaling is broken in the “long” direction



# The End

A large, pixelated sun with a bright yellow center and a blue and white outer ring, set against a white background.

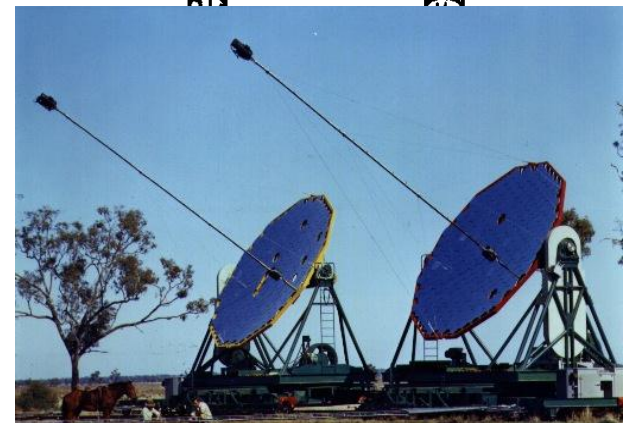
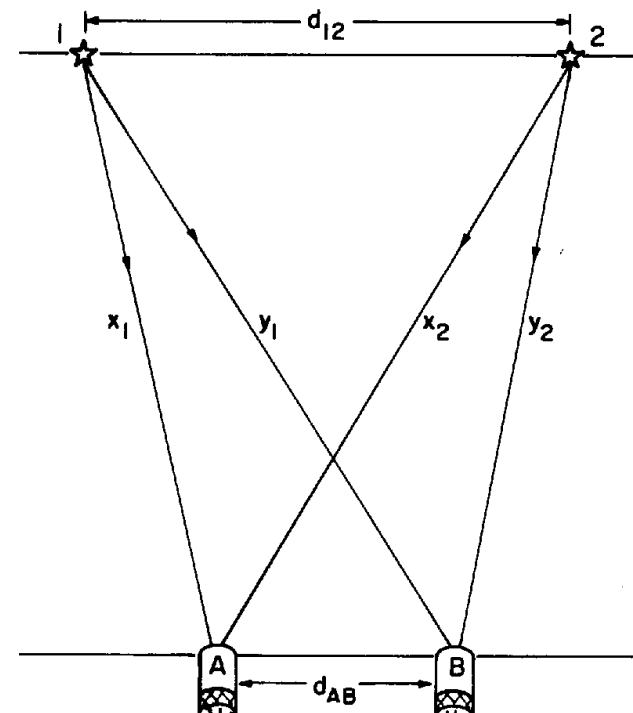
**Thank You**  
for your attention

backup slides follow...

# The HBT effect

## History

- „Interference between two different photons can never occur.”  
P. A. M. Dirac, The Principles of Quantum Mechanics, Oxford, 1930
- Robert **Hanbury Brown** and Richard Q. **Twiss**, (engineers, worked in radio astronomy) found **correlation between photons from different sources**.
- „In fact to a surprising number of people the idea that the arrival of photons at two separated detectors can ever be correlated was not only heretical but patently absurd, and they told us so in no uncertain terms, in person, by letter, in print, and by publishing the results of laboratory experiments, which **claimed to show that we were wrong ...**”

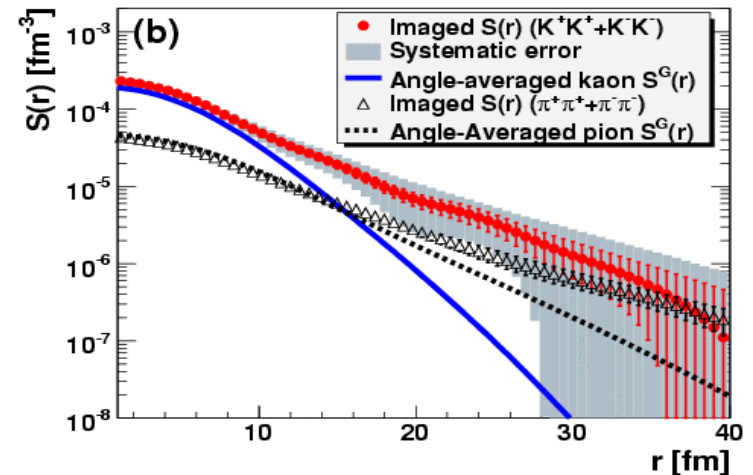
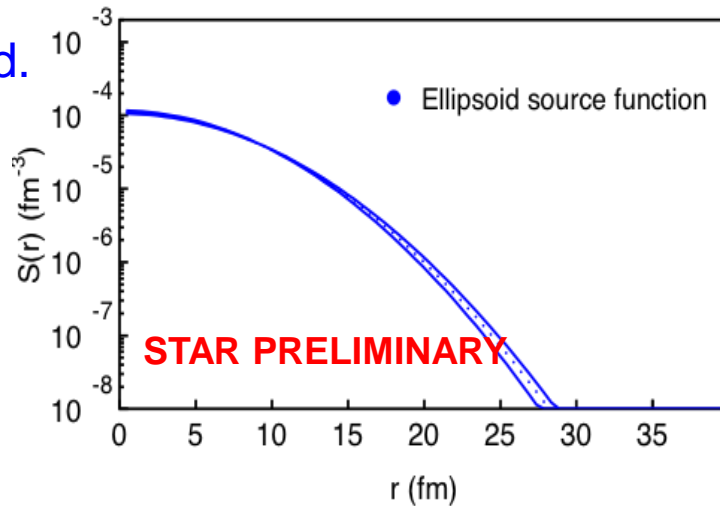
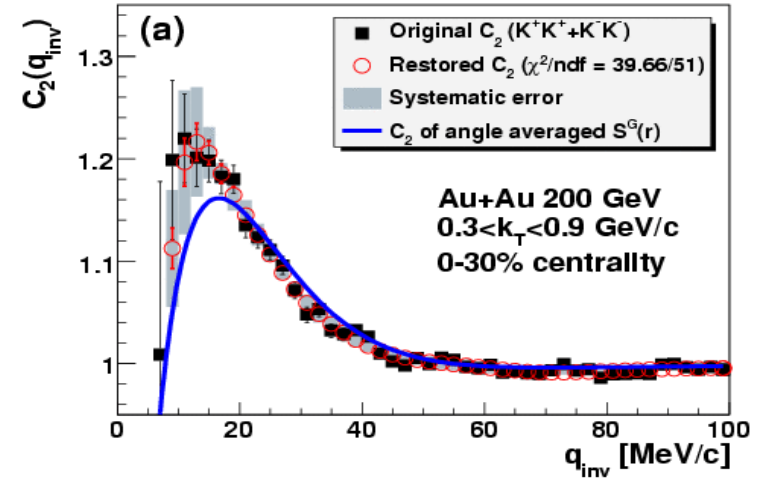
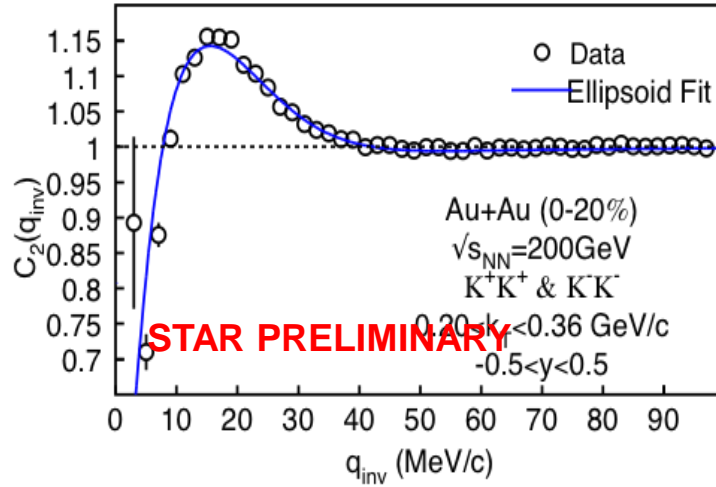


# STAR 1D kaons

34M+83M=117M  
K<sup>+</sup>K<sup>+</sup> & K<sup>-</sup>K<sup>-</sup> pairs

STAR data are well described by Gaussian, contrary to PHENIX no non-gaussian tails are observed.

May be due to a different  $k_T$ -range: STAR bin is 4x narrower.



# Model comparison: thermal BW

## Therminator

(A Thermal Heavy Ion Generator)

A. Kisiel et al., Phys. Rev. C 73:064902 2006

- Longitudinal boost invariance
- **Blast-wave** expansion: transverse velocity profile semi-linear in transverse radius  $\rho$ :  
 $v_t(\rho) = (\rho/\rho_{\max}) / (\rho/\rho_{\max} + v_t)$  ;  $v_t = 0.445$   
 from BW fits to particle spectra
- Thermal emission at proper time  $\tau$ , from an infinite cylinder radius  $\rho_{\max}$
- Freeze-out occurs at  $\tau = \tau_0 + a\rho$ .
- Particles which are emitted at  $(z, \rho)$  have LAB emission time  $\tau^2 = (\tau_0 + a\rho)^2 + z^2$ .
- Finite emission duration  $\Delta\tau$

## Source consistent with BW and resonances

- Instant freeze-out at  $\tau_0 = 0.8$  fm/c
- Zero emission duration

