



LHC optics estimation

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on behalf of the

TOTEM collaboration

<http://totem.web.cern.ch/Totem/>

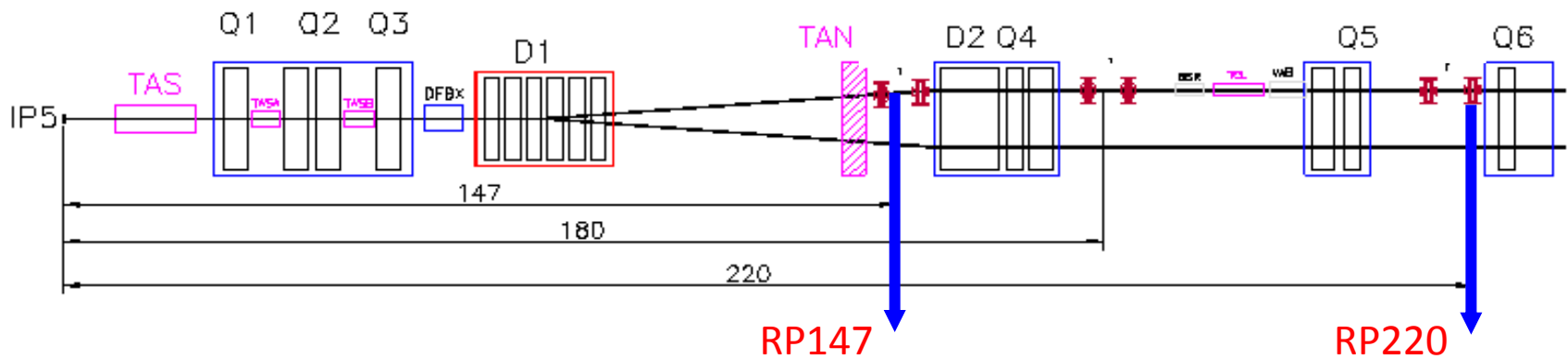
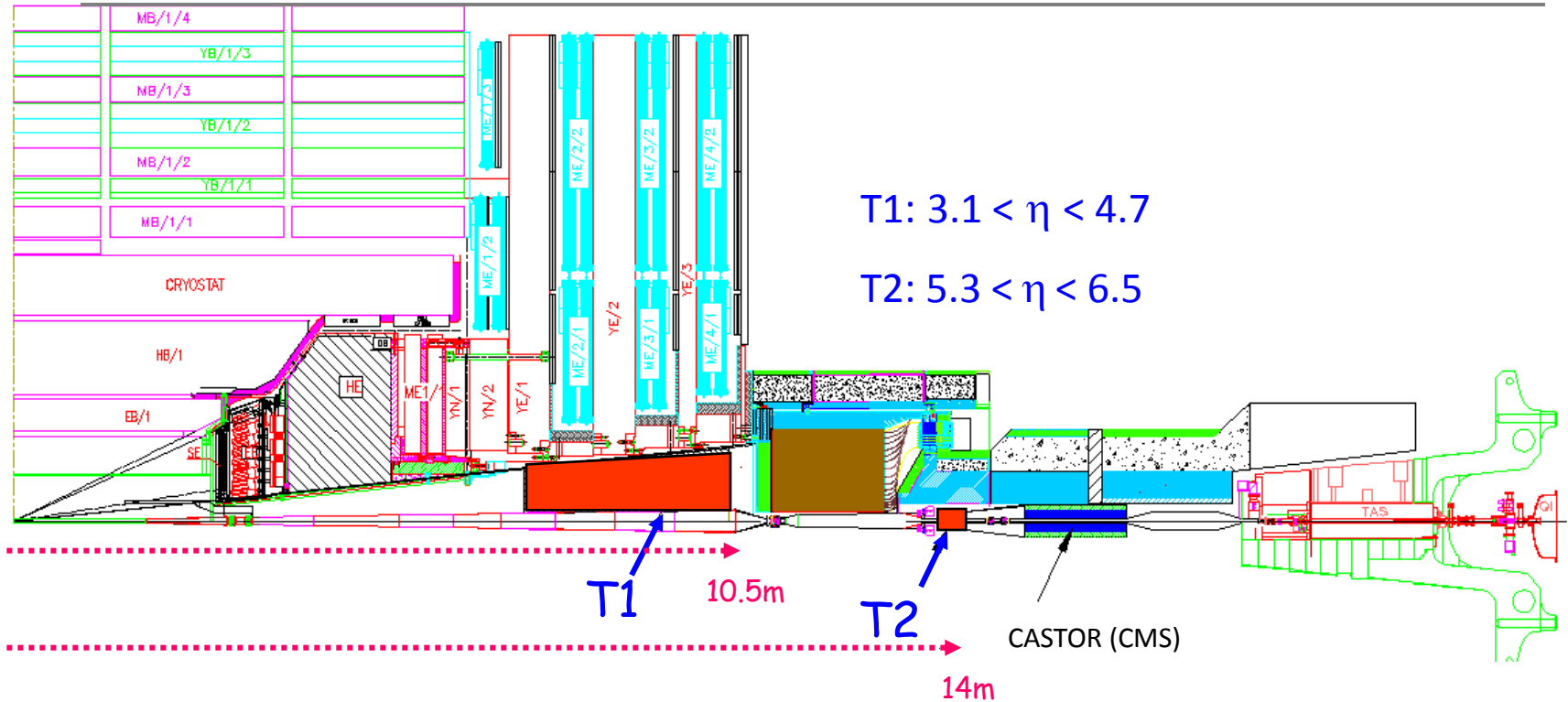
Zimányi Winter School

Budapest

2012, December 3.– 7.



Experimental layout of the TOTEM experiment

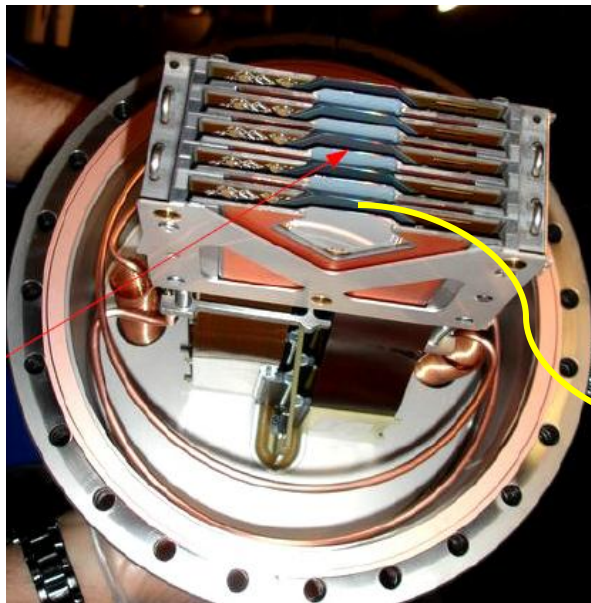
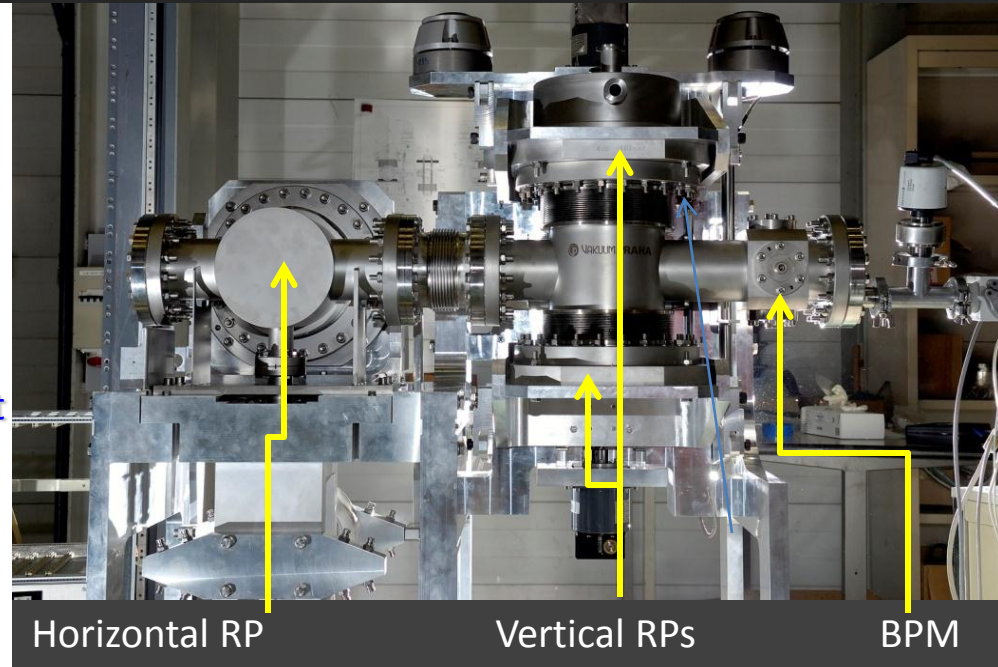


Roman Pot stations

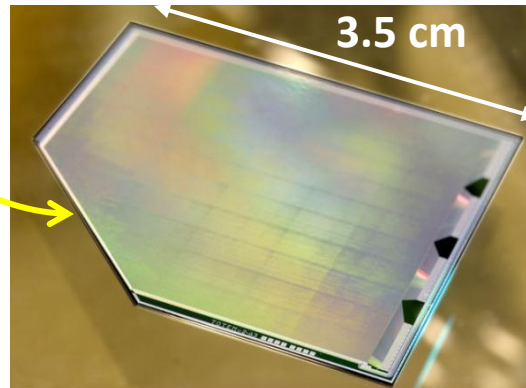
RP stations

- ◆ 2 units at about 5 m distance
- ◆ Measurement of very small proton scattering angles (few μrad)
- ◆ Vertical and horizontal pots mounted as close as possible to the beam
- ◆ BPM fixed to the structure gives precise position relative to the beam
- ◆ Overlapping detectors: relative alignment (10 μm inside unit between 3 RPs)

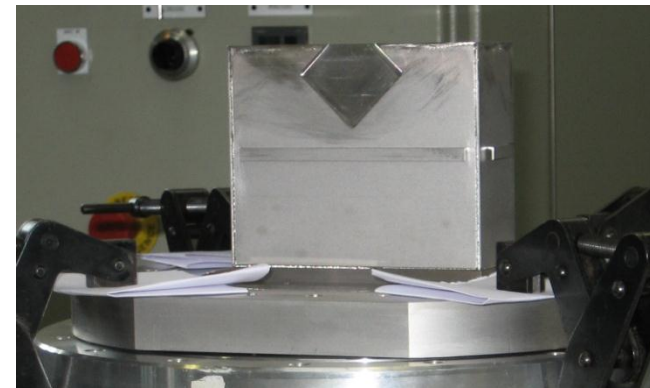
RP unit: 2 vertical, 1 horizontal pot + BPM



10 planes of edgeless detectors



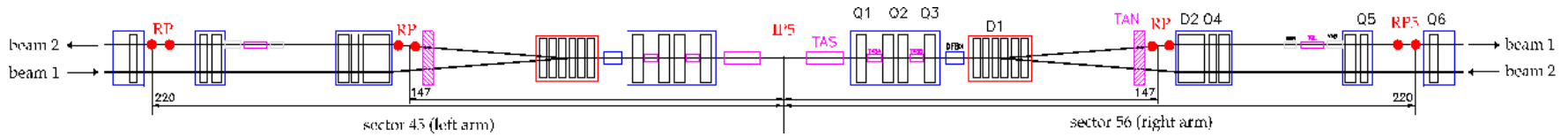
Si edgeless detector



1 Roman Pot



LHC optics in brief



Proton position at a given RP (x, y) is a function of position (x^*, y^*) and angle (Θ_x^*, Θ_y^*) at IP5:

$$\left. \begin{matrix} \text{measured} \\ \left(\begin{matrix} x \\ \Theta_x \\ y \\ \Theta_y \\ \Delta p/p \end{matrix} \right)_{\text{RP}} \end{matrix} \right\} = \begin{pmatrix} v_x & L_x & 0 & 0 & D_x \\ v'_x & L'_x & 0 & 0 & D'_x \\ 0 & 0 & v_y & L_y & 0 \\ 0 & 0 & v'_y & L'_y & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} \left. \begin{matrix} \left(\begin{matrix} x^* \\ \Theta_x^* \\ y^* \\ \Theta_y^* \\ \Delta p/p \end{matrix} \right)_{\text{IP5}} \\ \text{reconstructed} \end{matrix} \right\}$$

The *effective length* and *magnification* expressed with the phase advance

$$L(s) = \sqrt{\beta(s)\beta^*} \sin \Delta\mu(s) \quad v(s) = \sqrt{\beta(s)\beta^{*-1}} \cos \Delta\mu(s) \quad \Delta\mu(s) = \int_0^s \beta^{-1}(s') ds'$$

Beam size and divergence at IP5 and RP

$$\sigma(x) = \sqrt{\varepsilon\beta_x} \quad \text{describes the spread of primary vertex and beam size at RP}$$

$$\sigma(\Theta) = \sqrt{\varepsilon/\beta_x} \quad \text{beam divergence @IP5 limits the angle measurement precision}$$

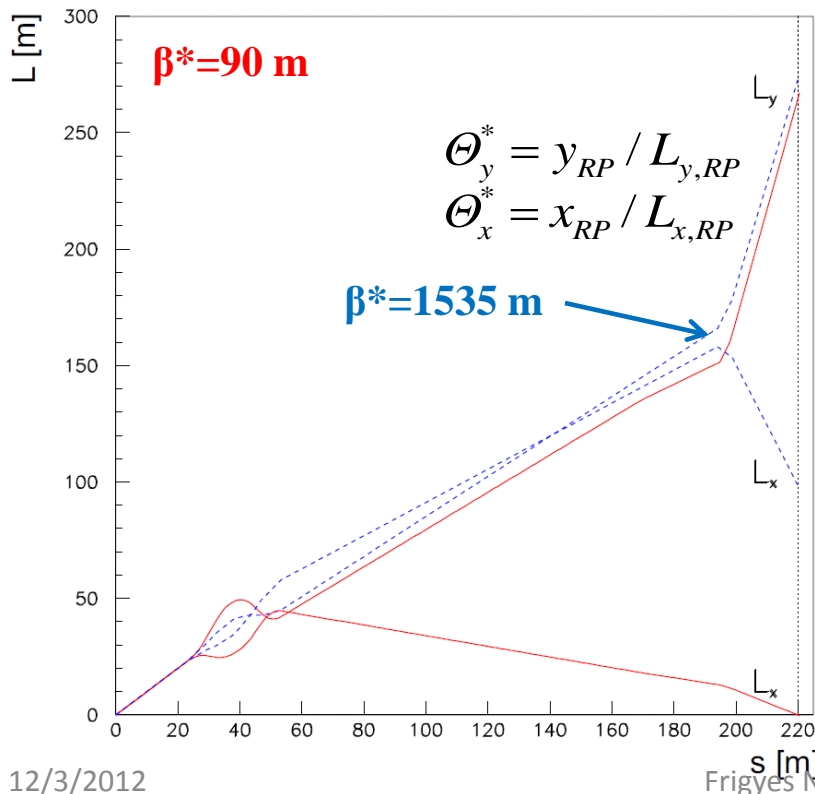


High $\beta^*=1535$ m target optics

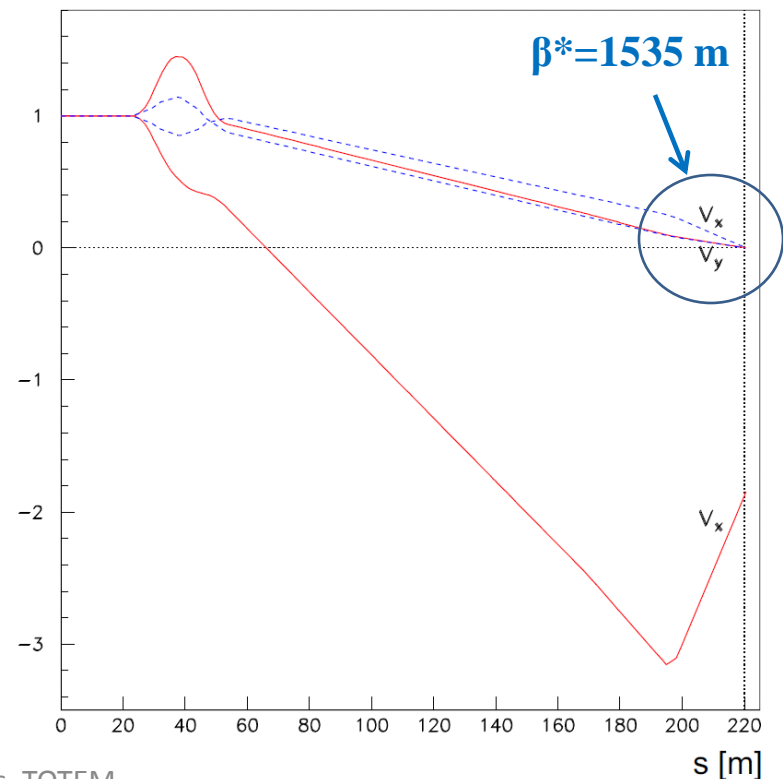
$\beta^* = 1535$ m is the *target* optics. Requires different injection optics. Properties:

- beam divergence $\sigma_{\theta^*} \approx 0.3 \mu\text{rad}$, vertex size $\sigma_{\text{IP}} \approx 450 \mu\text{m}$
- $\Delta\mu_{x,y} = \pi/2 \rightarrow v_{x,y} = 0$. Parallel-to-point focusing **eliminates** the large vertex contribution
- the large (270 m) vertical effective length L_y pushes protons vertically into RP acceptance
- acceptance in momentum transfer, $|t| > 2 \cdot 10^{-3} \text{ GeV}^2$, with $10 \sigma_{\text{beam size@RP}}$

Effective lengths from IP5 to RP @220 m



Magnification from IP5 to RP @220 m



LOW $\beta^*=3.5$ m OPTICS

Low $\beta^*=3.5\text{m}$ optics

Objective:

- to measure elastic scattering at high $|t|$

Properties of the optics:

- $\sigma_{IP} \approx 37 \mu\text{m}$ (magnification is not crucial)
- $L_x \approx 0, L_y = 22.4 \text{ m}$
- beam divergence $\sigma_{\theta^*} \approx 17\text{-}18 \mu\text{rad}$

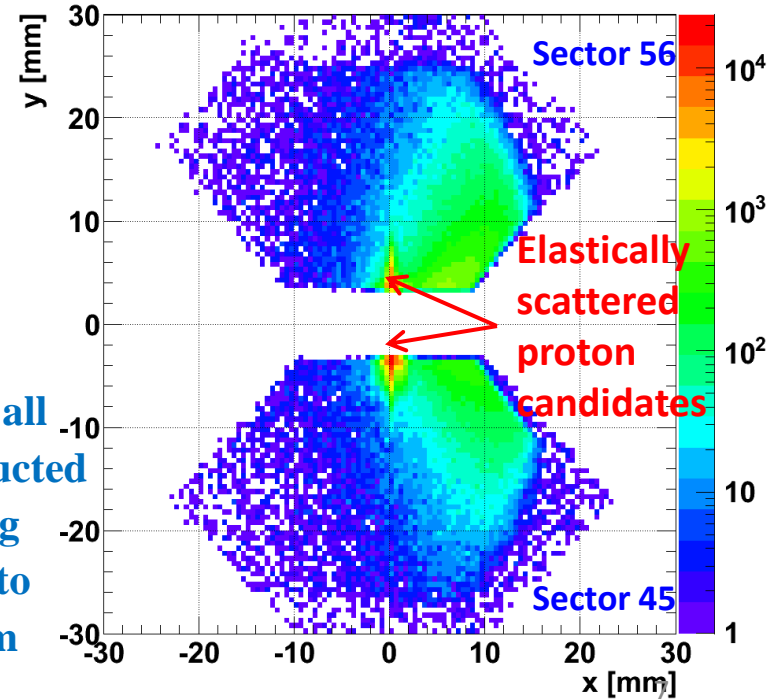
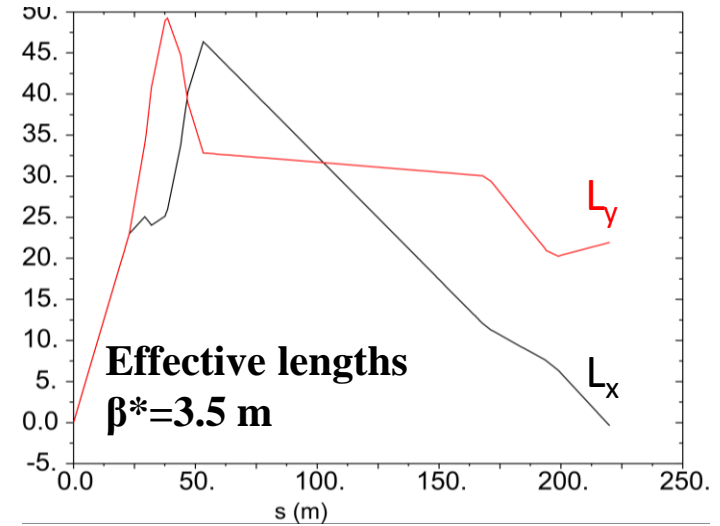
Data sources to improve our optics understanding:

- TIMBER database magnet currents
- FIDEL team conversion curves, implemented with LSA
- WISE field harmonics, magnet's displacements`

$$t = -p^2 \theta^2$$

$$\xi = \Delta p/p$$

The intercepts of all selected reconstructed tracks in a scoring plane transverse to the beam at 220 m



The effect of machine imperfections $\beta^*=3.5\text{m}$

Machine imperfections:

- Strength conversion error, $\sigma(B)/B \approx 10^{-3}$
- Beam momentum offset, $\sigma(p)/p \approx 10^{-3}$
- Magnet rotations, $\sigma(\phi) \approx 1 \text{ mrad}$
- Beam harmonics, $\sigma(B)/B \approx 10^{-4}$
- Power converter errors, $\sigma(I)/I \approx 10^{-4}$
- Magnet positions $\Delta x, \Delta y \approx 100 \mu\text{m}$



Perturbed element	$\delta L_{y,b1}/L_{y,b1} [\%]$
MQXA.1R5	0.98
MQXB.A2R5	-2.24
MQXB.B2R5	-2.42
MQXA.3R5	1.45
MQY.4R5.B1	-0.10
MQML.5R5.B1	0.05
$\Delta p/p$	-2.19

Imperfections alter the optics !

Constraints from proton tracks in the Roman Pots $\beta^*=3.5\text{m}$

Optics imperfections can be determined from proton

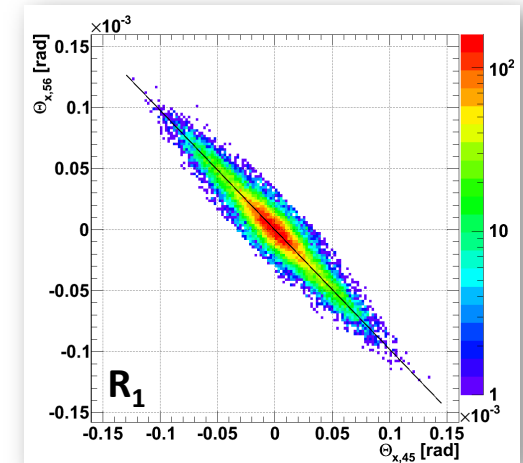
tracks *measured* in the Roman Pots. The method is based on:

- elastic events are easy to tag
- the elements of the transport matrix are mutually correlated
- elastic scattering ensures that

$$\Theta_{y,b1}^* = \Theta_{y,b2}^*$$

$$\Theta_{x,b1}^* = \Theta_{x,b2}^*$$

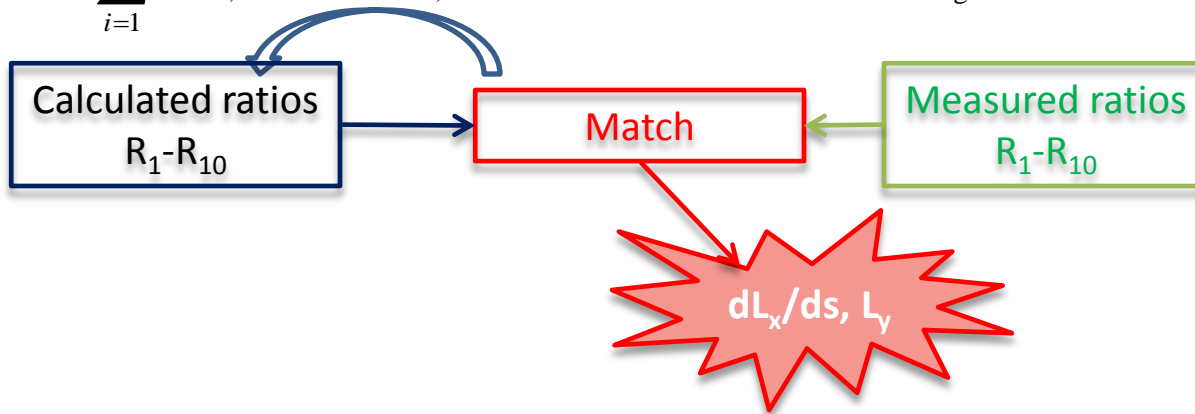
$$\rightarrow R_1 \equiv \frac{\Theta_{x,b1,RP}}{\Theta_{x,b2,RP}} \approx \frac{dL_{x,b1,RP}}{ds} \frac{ds}{dL_{x,b2,RP}}$$



Matching the optics $\beta^*=3.5\text{m}$

On the basis of constraints R_1 - R_{10} the optics can be estimated.

$$\chi^2 = \sum_{i=1}^{10} ((R_{i,\text{measured}} - R_{i,\text{calculated}}) / \sigma(R_i))^2 + \chi_{\text{LHC Design}}^2$$

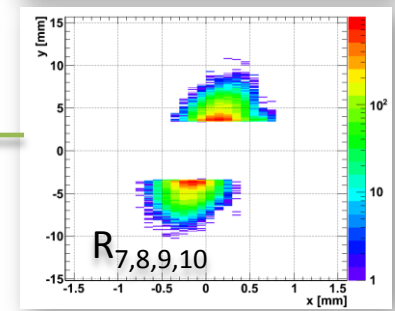
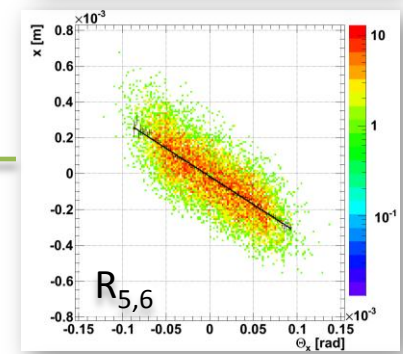
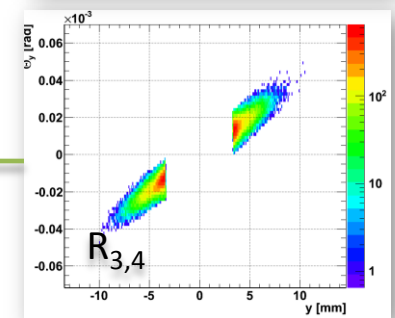
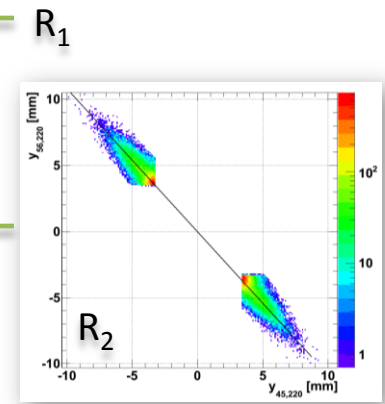


$$R_2 \equiv \frac{y_{b1,RP}}{y_{b2,RP}} \approx \frac{L_{y,b1,RP}}{L_{y,b2,RP}}$$

$$R_3 \equiv \frac{\Theta_{y,b1,RP}}{y_{b1,RP}} \approx \frac{\frac{dL_{y,b1,RP}}{ds}}{L_{y,b1,RP}}$$

$$R_7 \equiv \frac{x_{b1,RP}}{y_{b1,RP}} \approx \frac{m_{14,b1,near_pots}}{L_{y,b1,near_pots}}$$

$$R_5 \equiv \frac{x_{b1,RP}}{\Theta_{x,b1,RP}} \approx \frac{L_{x,b1,RP}}{dL_{x,b1,RP}/ds}$$



Monte-Carlo confirmation of the method (presented @IPAC 2012)

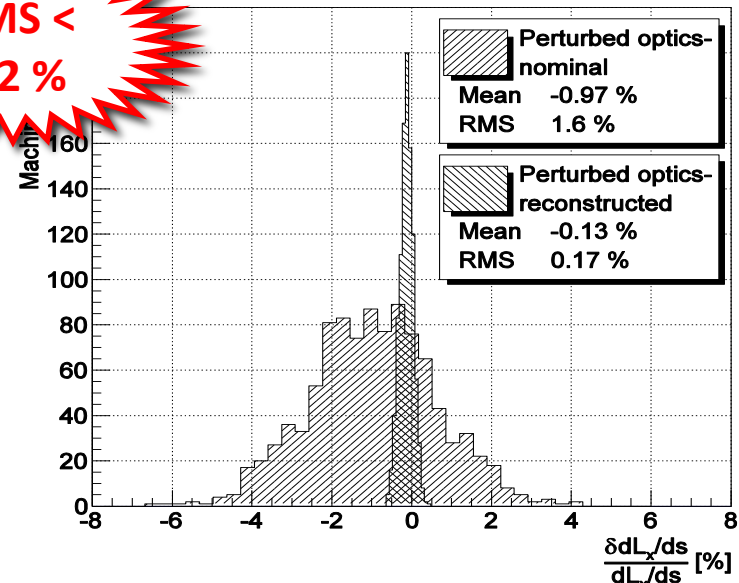
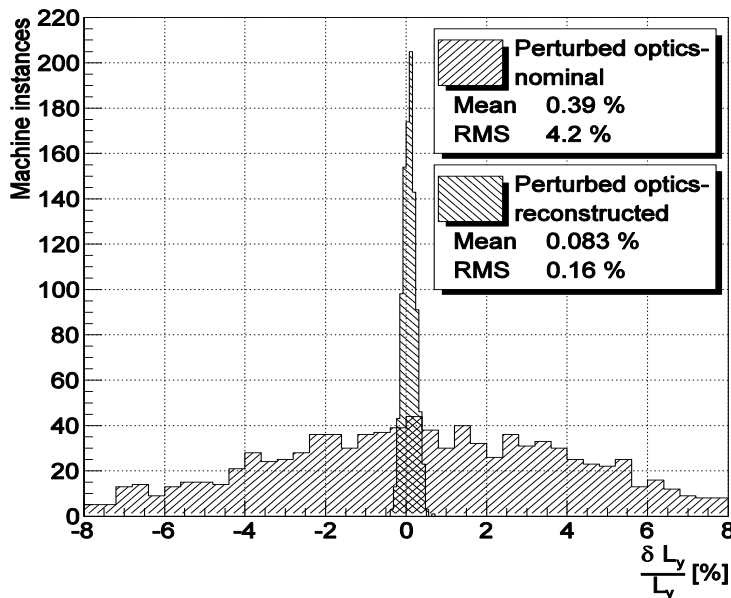
The Monte-Carlo study included the effect of:

- magnet strengths
- beam momenta
- displacements, rotations
- kickers, field harmonics
- elastic scattering Θ -distributions

Optical function relative error	Before		Matched	
	Mean [%]	RMS [%]	Mean [%]	RMS [%]
$\delta L_{y,b1}/L_{y,b1}$	0.39	4.2	$8.3 \cdot 10^{-2}$	0.16
$\delta (dL_{x,b1}/ds)/(dL_{x,b1}/ds)$	-0.97	1.6	-0.13	0.17
$\delta L_{y,b2}/L_{y,b2}$	-0.14	4.9	0.21	0.16
$\delta (dL_{x,b2}/ds)/(dL_{x,b2}/ds)$	0.10	1.7	$-9.7 \cdot 10^{-2}$	0.17

Conclusion: for $\beta^*=3.5\text{m}$ TOTEM can measure the transfer matrix between IP5 and RPs with a precision

RMS < 0.2 %

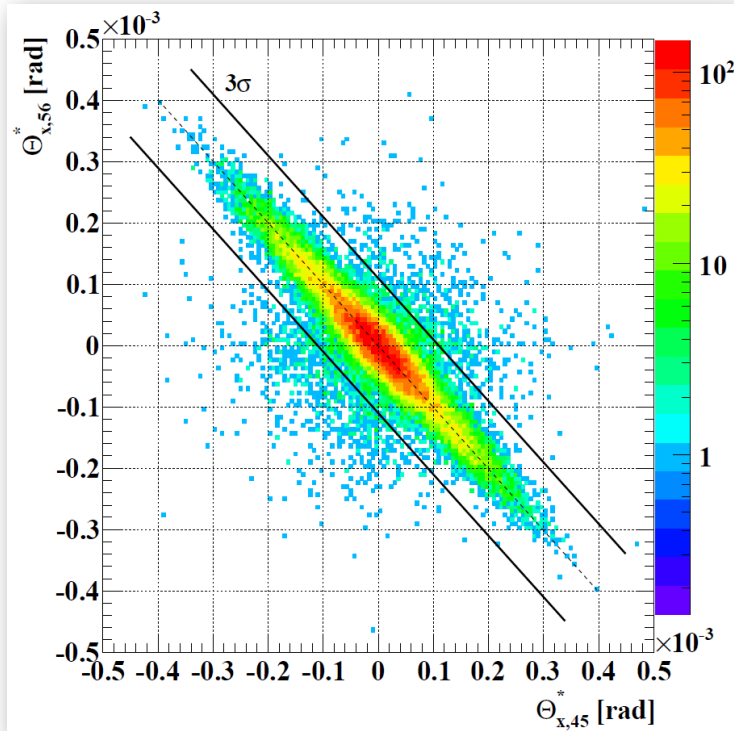


Relative error distributions **before** and **after** matching

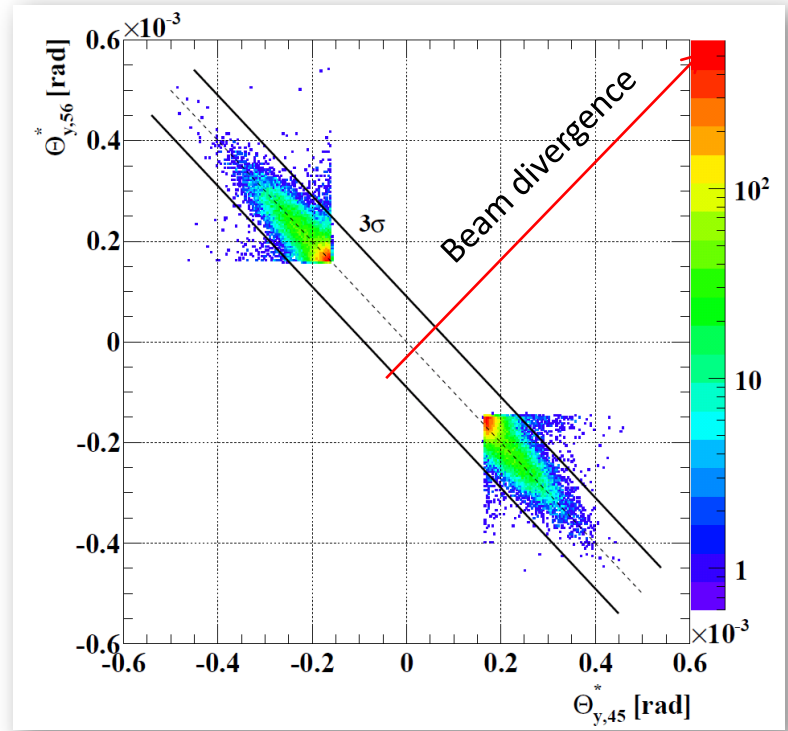
ELASTIC SCATTERING WITH $\beta^*=3.5$ m

Results (the **matched** L_y and dL_x/ds are used for reconstruction):

- RP approaches the beam down to $7 \sigma_{\text{beam size@RP}}$
- published in EPL **95** (2011) 41001
- $\xi \approx 0$



Collinearity Θ_x
Spread in agreement with beam divergence (17-18 μrad)



Collinearity Θ_y

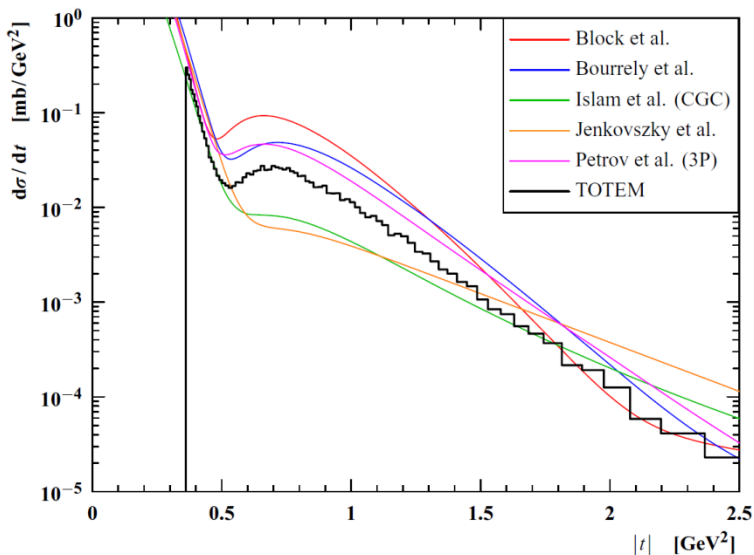
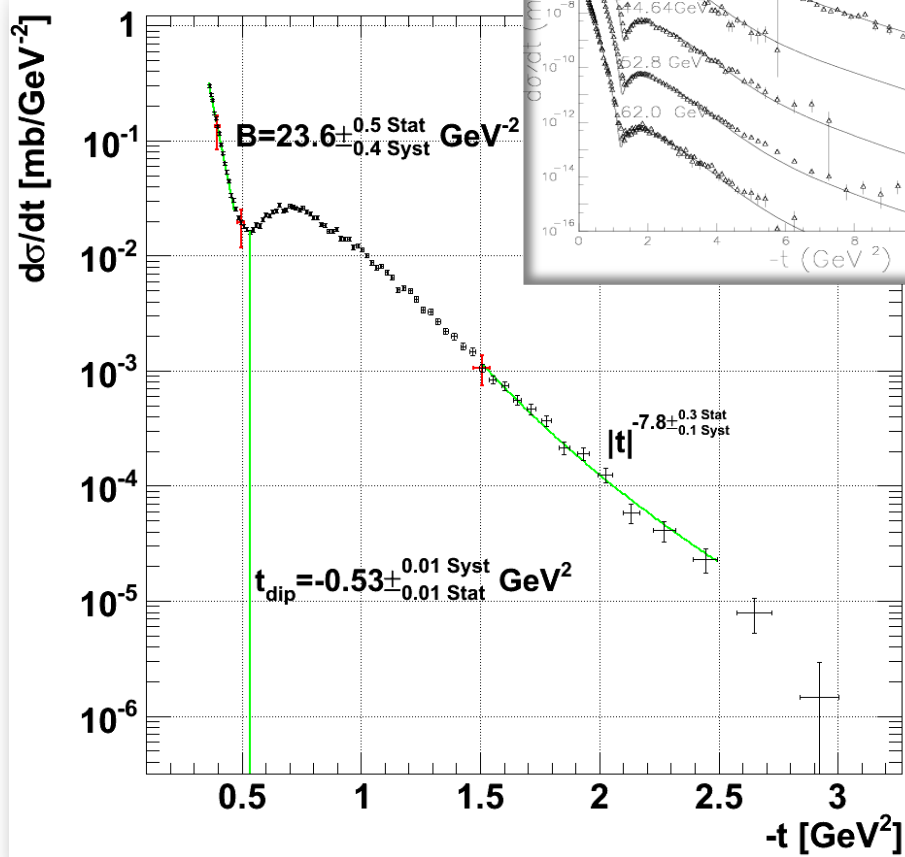
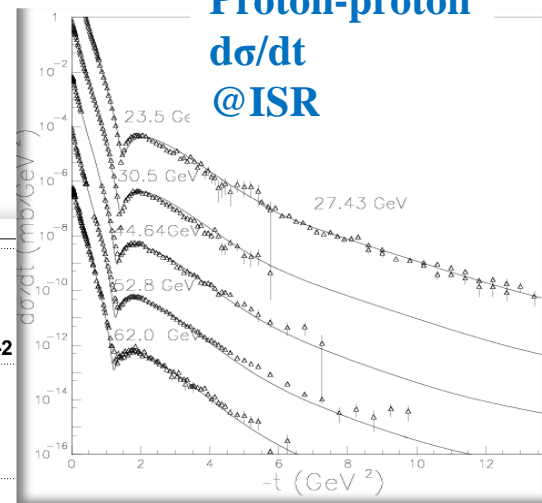


Final result: unfolded elastic scattering distribution $\beta^*=3.5m$

Published in EPL 95 (2011) 41001:

- $|t|$ range spans from 0.36 to 2.5 GeV^2
- below $|t| = 0.47 \text{ GeV}^2$ exponential $e^{-B|t|}$ behavior
- dip moves to lower $|t|$, proton becomes "larger"
- 1.5 - 2.0 GeV^2 power low behavior $|t|^{-n}$

Proton-proton $d\sigma/dt$ @ISR



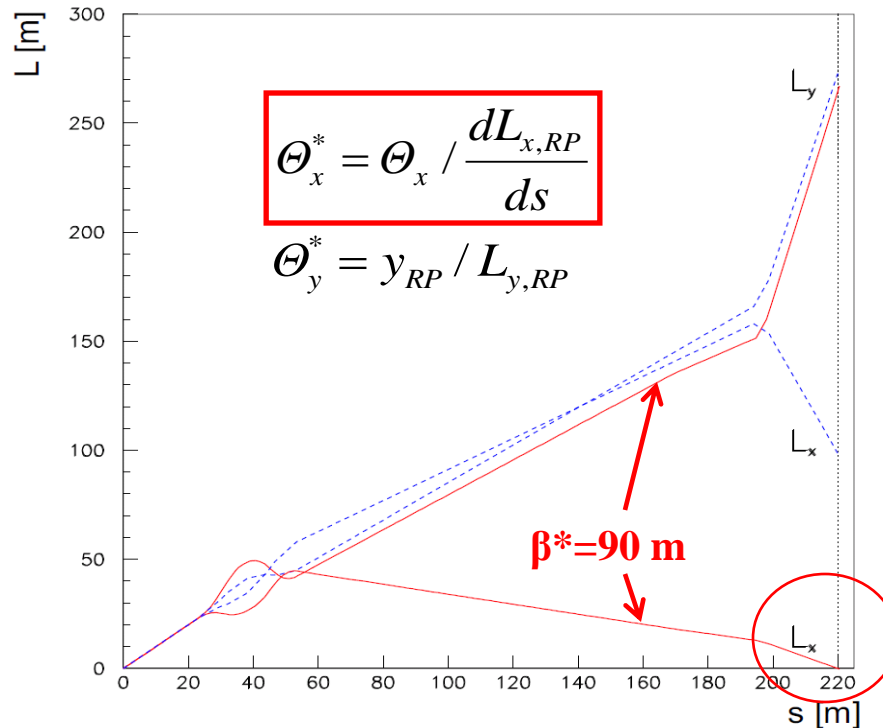
The measured $d\sigma/dt$ compared with predictions of several models

HIGH β^* = 90 m OPTICS AND RESULTS

$\beta^* = 90$ m optics achievable using the standard LHC injection optics. Properties:

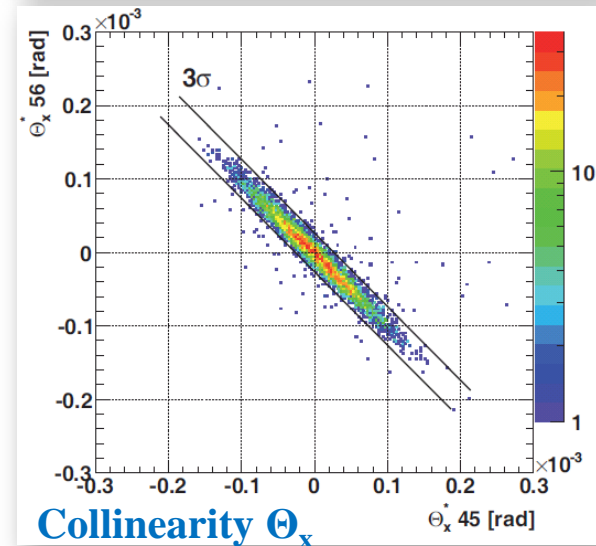
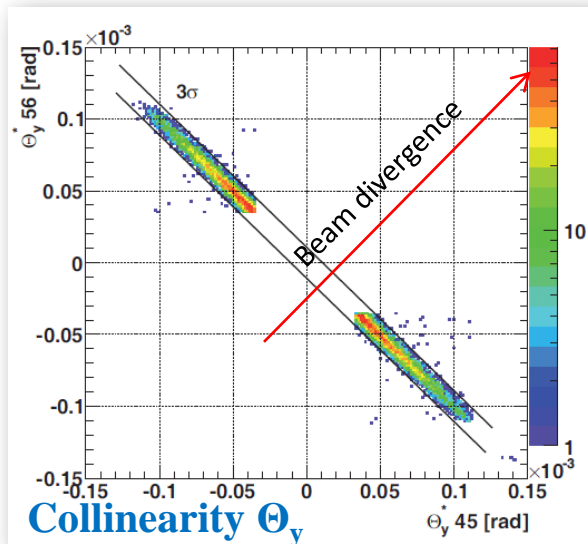
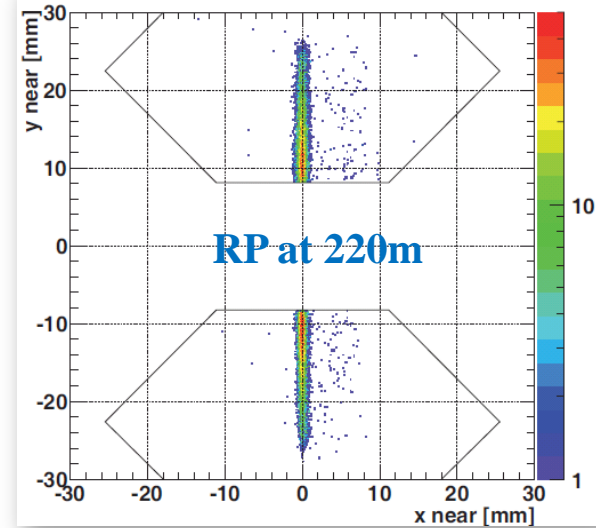
- $\sigma_{\Theta^*} = 2.5 \mu\text{rad}$, $L_x \approx 0$, $L_y \approx 260$ m
- vertex size $\sigma_{\text{IP}} \approx 212 \mu\text{m}$
- Acceptance: $|t| > 3 \cdot 10^{-2} \text{ GeV}^2$, RP distance from beam center $10 \sigma_{\text{beam size@RP}}$
- parallel to point focusing **only** in **vertical** plane @RP220

Effective lengths from IP5 to RP @220 m



The properties of the measured data:

- divergence is reduced with respect to 3.5 m optics (from 17-18 μrad to 2.5 μrad)
- lower background compared to 3.5 m ($< 0.1\%$)
- uncertainty of luminosity 4% (CMS)
- low intensity bunches and $\beta^*=90$ m \rightarrow no pile-up from single diffraction



Intermediate $\beta^*=90$ m optics: robustness

Objectives:

- First measurement of σ_{tot} elastic scattering in a wide $|t|$ range
- inclusive studies of diffractive processes
- measurement of forward charged multiplicity

Sensitivity of the effective length L_y :

- 1 ‰ perturbations magnet strength, beam momenta
- **Conclusion: not necessary to improve our understanding about $\beta^*=90$ m optics**

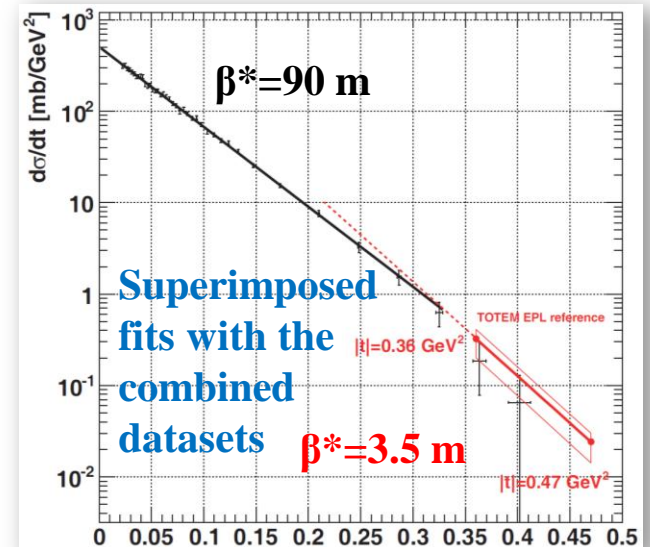
Perturbed element	$\delta_{L_{y,b1}/L_{y,b1}}$ [%]
MQXA.1R5	0.14
MQXB.A2R5	-0.23
MQXB.B2R5	-0.25
MQXA.3R5	0.20
MQY.4R5.B1	-0.01
MQML.5R5.B1	0.04
$\Delta p/p$	0.01

Obtained $d\sigma/dt$ with $\beta^*=90$ m optics

Published in EPL 96 (2011) 21002

Properties:

- $|t|$ range of the new set is 0.02 - 0.33 GeV^2
- $B = (20.1 \pm 0.2^{\text{stat}} \pm 0.3^{\text{syst}}) \text{GeV}^{-2}$ confirms that B increases with \sqrt{s}
- excellent agreement between the two measurements with different optics





Conclusions

- **TOTEM has measured the inelastic and elastic cross sections and the total cross section with the luminosity independent method at $\sqrt{s}=7$ TeV**
- Measurement of elastic scattering at very low- t and determination of the ρ parameter will be in reach during the high β ($\beta^*= 500$ m, 1000 m) runs
- Several analyses on diffractive physics are going on, results are expected soon

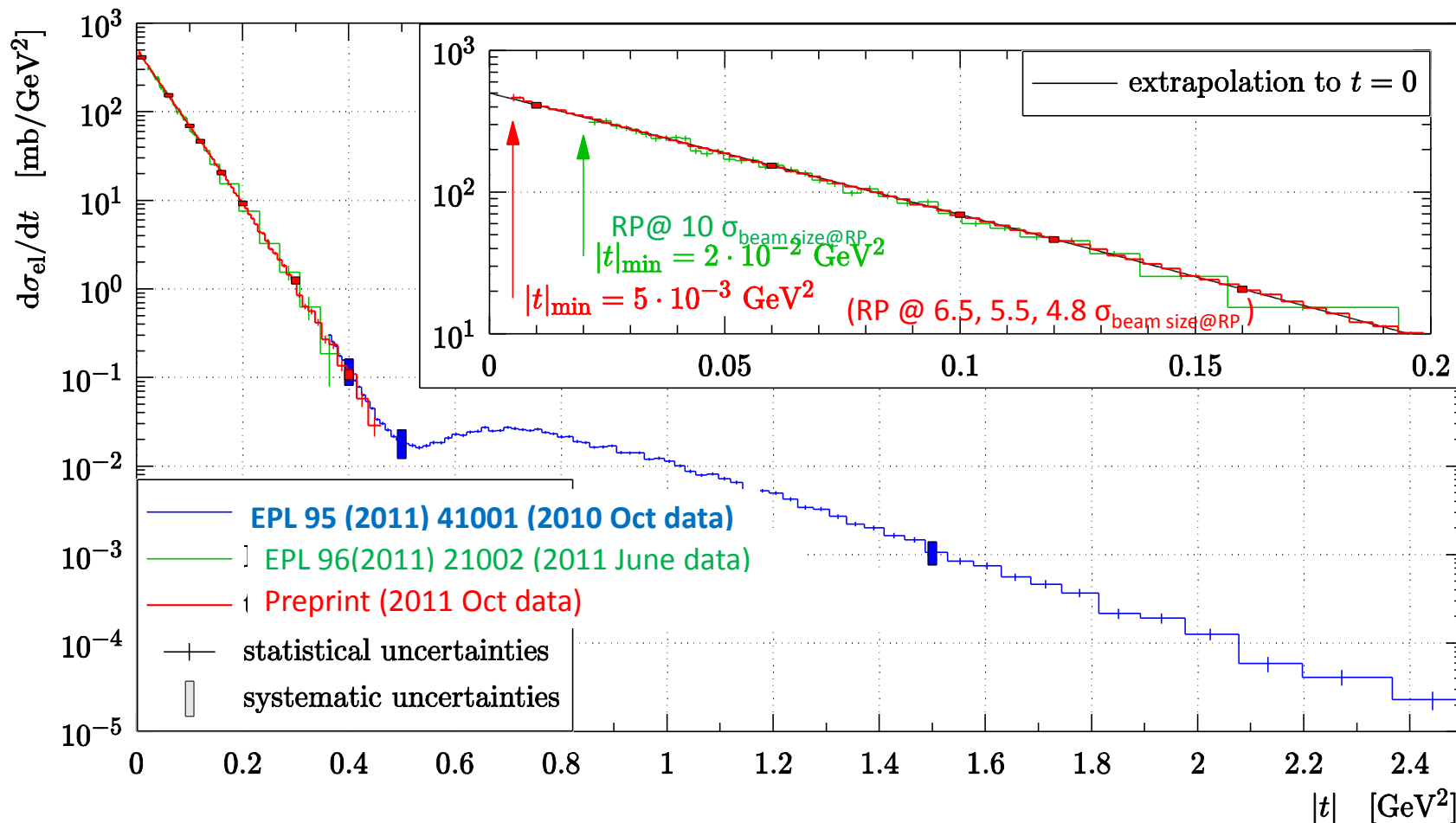
Thank you for you attention !



Backup part



Obtained $d\sigma/dt$ with the most recent result





Total Cross-Section with 4 methods

1. Low luminosity (CMS) + Elastic $d\sigma/dt$ + Optical th. (EPL 96(2011) 21002)

- depends on CMS luminosity for low-L bunches, elastic efficiencies and on ρ

$$\sigma_{tot}^2 = \frac{16\pi(\hbar c)^2}{1 + \rho^2} \cdot \left. \frac{d\sigma_{el}}{dt} \right|_{t=0} \quad \sigma_{TOT} = 98.3 \pm 2.8 \text{ mb}$$

2. High luminosity (CMS) + Elastic + Optical theorem (to be published)

$$\sigma_{TOT} = 98.6 \pm 2.2 \text{ mb}$$

3. High luminosity (CMS) + Elastic + Inelastic (to be published)

- minimizes dependence on elastic efficiencies and **ρ independent**

$$\sigma_{tot} = \sigma_{el} + \sigma_{inel} \quad \sigma_{TOT} = 99.1 \pm 4.3 \text{ mb}$$

4. Elastic ratios + Inelastic ratios + Optical theorem (preprint)

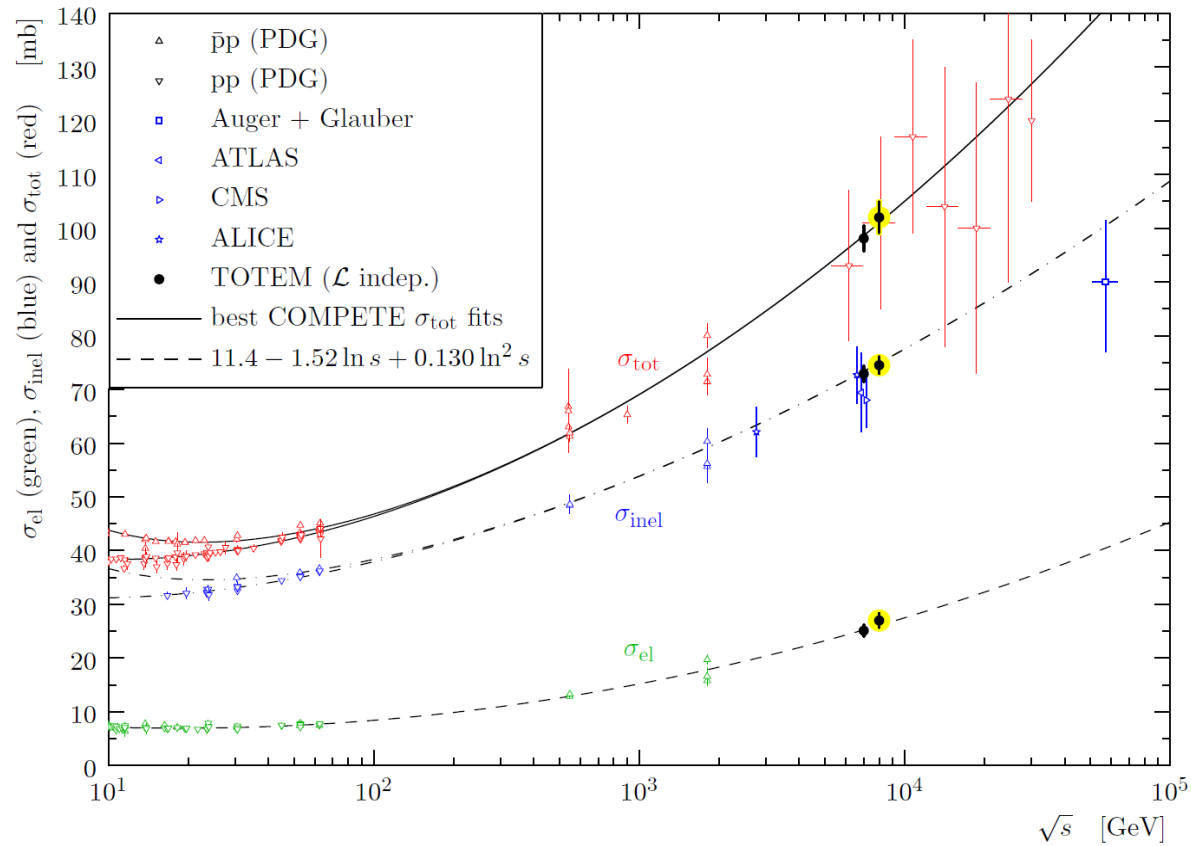
- Eliminates dependence on luminosity**

$$\sigma_{TOT, 7 \text{ TeV}} = 98.0 \pm 2.5 \text{ mb}$$

$$\sigma_{tot} = \frac{16\pi(\hbar c)^2}{1 + \rho^2} \cdot \frac{\left. \frac{dN_{EL}}{dt} \right|_{t=0}}{N_{EL} + N_{INEL}}$$

$$\sigma_{TOT, 8 \text{ TeV}} = 101.7 \pm 2.9 \text{ mb}$$

Total Cross-Section with the luminosity independent method including the 8 TeV result





Luminosity calibration

TOTEM is able to determine the CMS luminosity:

- Elastic and inelastic rates are used

$$L = \frac{1 + \rho^2}{16\pi(\hbar c)^2} \cdot \frac{(N_{EL} + N_{INEL})^2}{dN_{EL} / dt|_{t=0}}$$

Obtained luminosity values

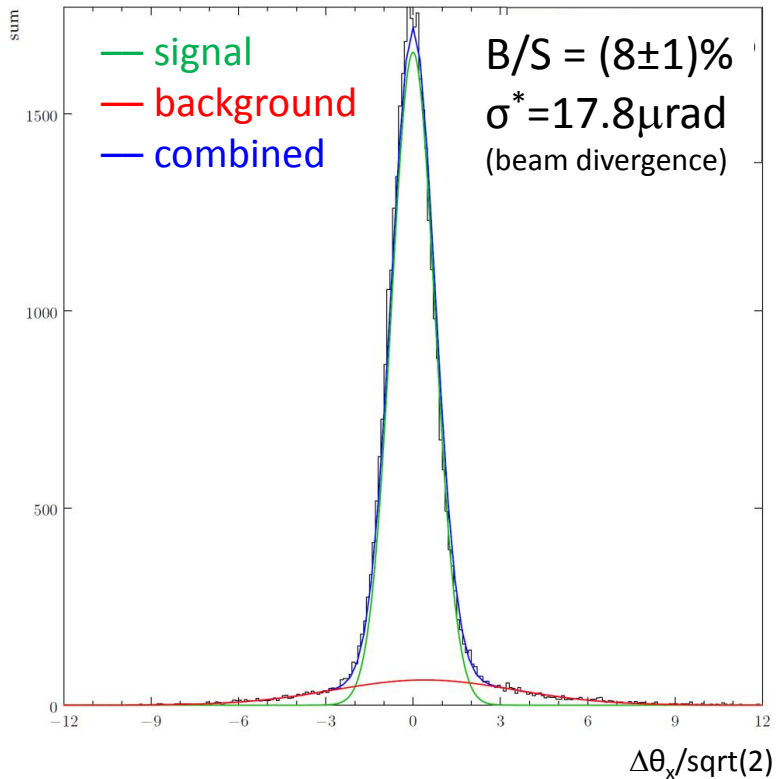
Octoberdata : $L_{CMS} = 82.8 \mu b^{-1} \pm 4\%$

$L_{TOTEM} = 83.7 \mu b^{-1} \pm 3.8\%$

June data : $L_{CMS} = 1.65 \mu b^{-1} \pm 4\%$

$L_{TOTEM} = 1.65 \mu b^{-1} \pm 4.5\%$

Background and resolution determination $\beta^*=3.5\text{m}$



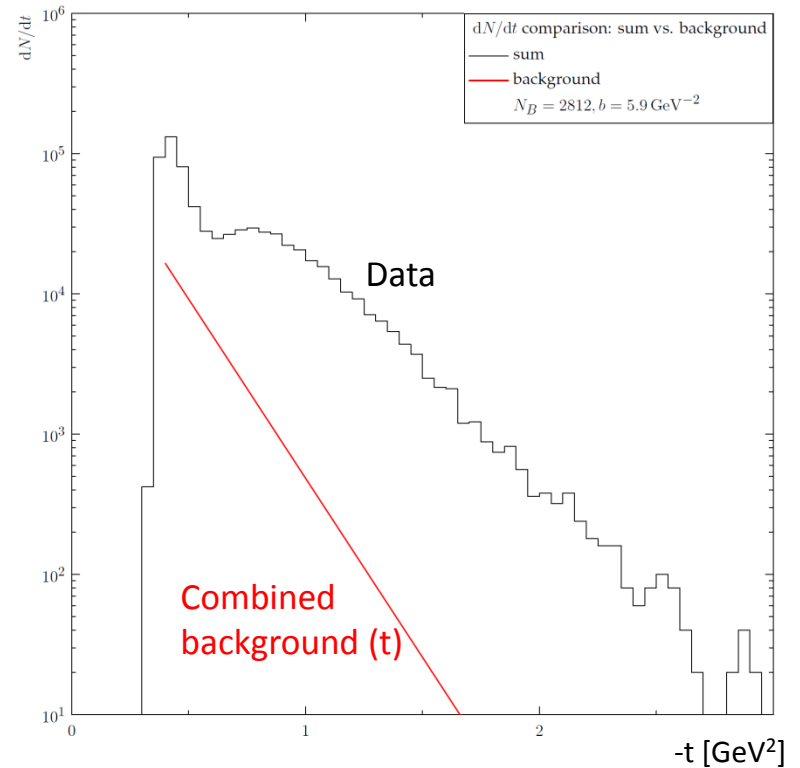
Signal to background normalisation
(also as a function of $\Delta\theta_y$)

$\sigma^* \rightarrow$ **t-reconstruction resolution:**

$$\frac{\sigma(t)}{\sqrt{t}} = \frac{\sqrt{2}p\sigma^*}{\sqrt{t}}$$

12/3/2012

0.4 GeV ² : 14%
1 GeV ² : 8.8%
3 GeV ² : 5.1%



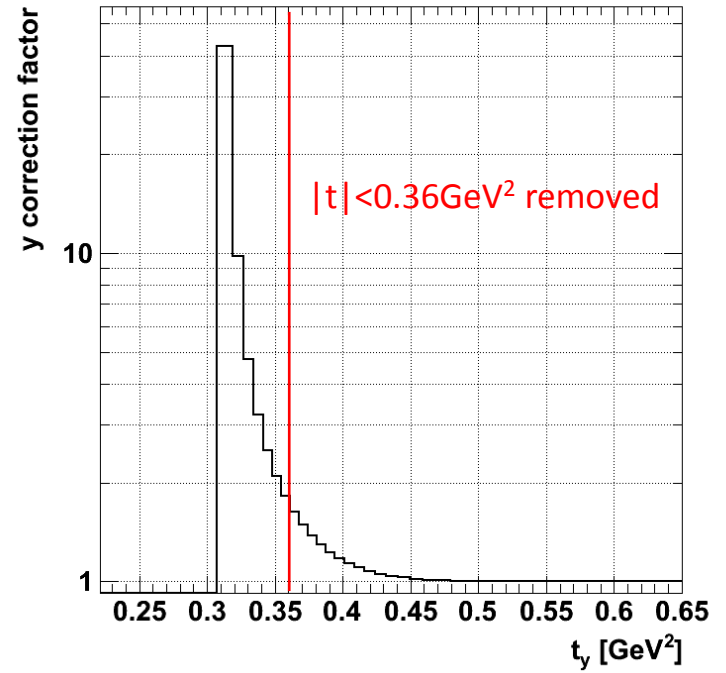
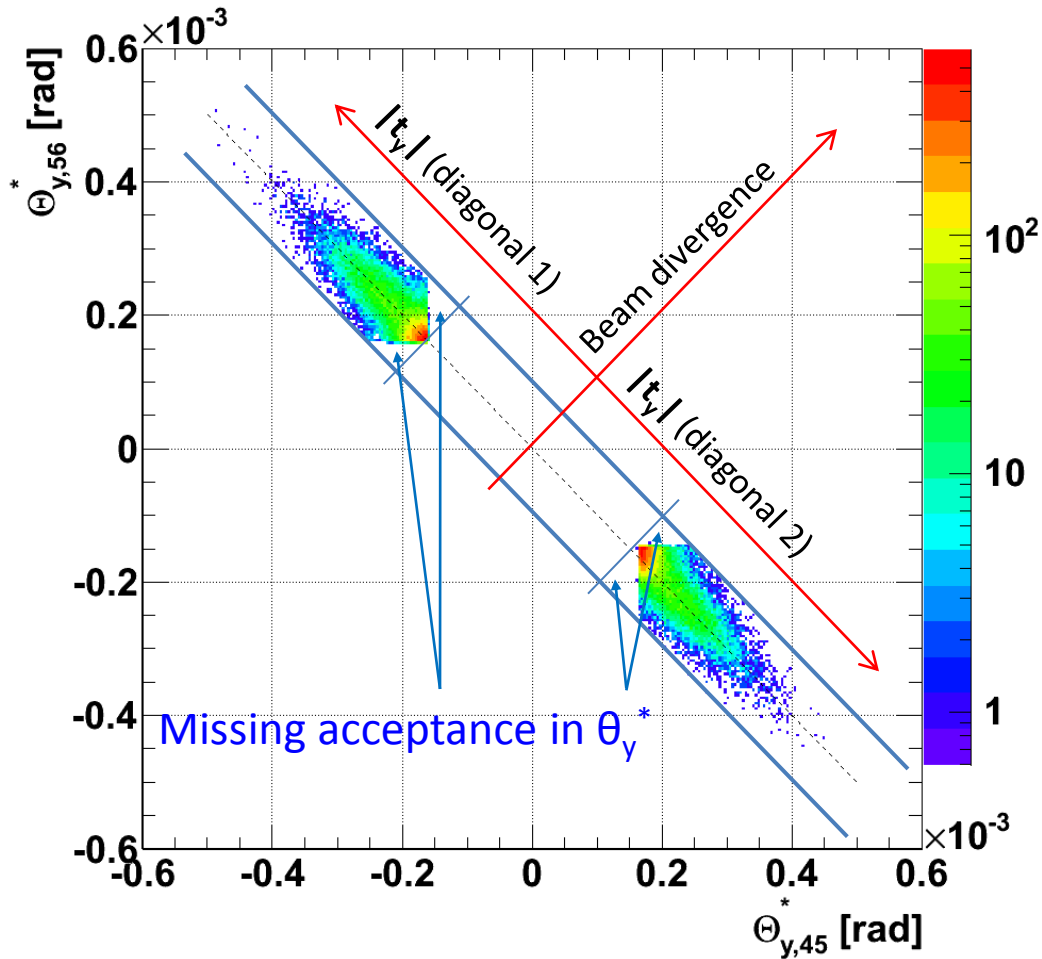
Signal vs. background (t)

$|t|=0.4\text{GeV}^2$: $B/S = (11 \pm 2)\%$

$|t|=0.5\text{GeV}^2$: $B/S = (19 \pm 3)\%$

$|t|=1.5\text{GeV}^2$: $B/S = (0.8 \pm 0.3)\%$

t_y -acceptance corrections $\beta^*=3.5\text{m}$

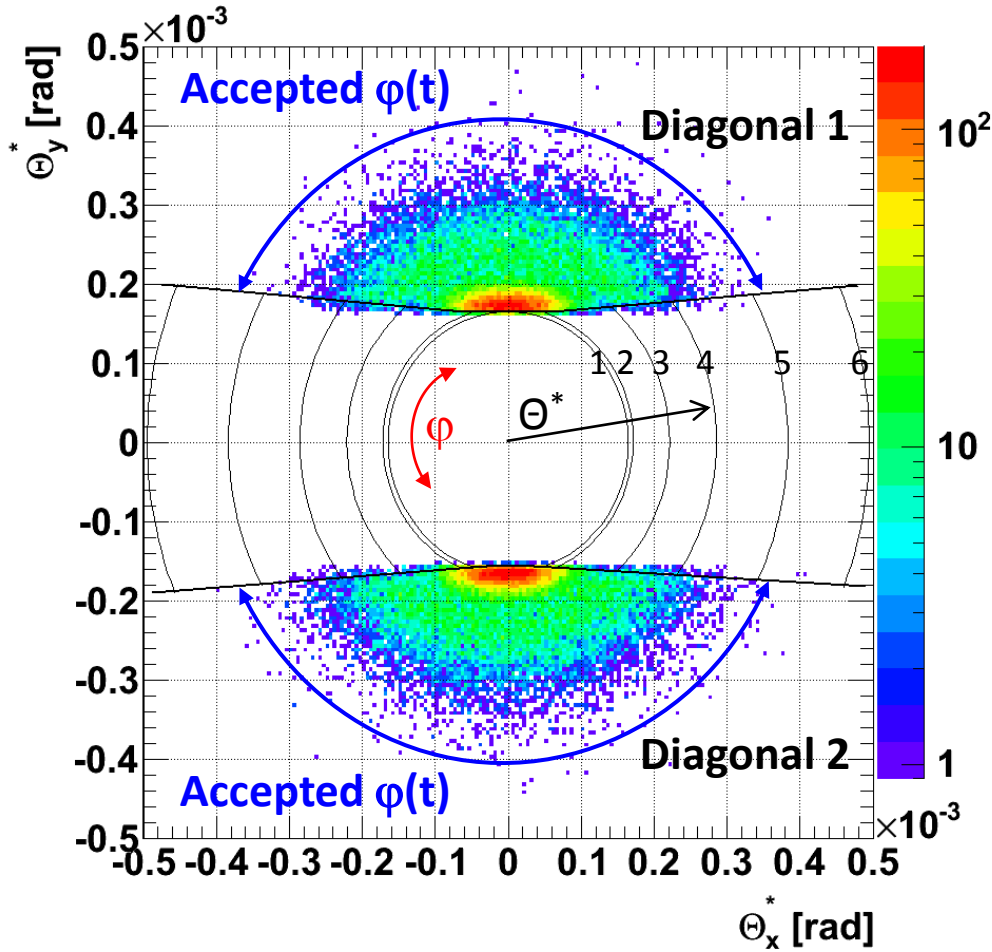


Correction error (t_y):

- 0.31 GeV 2 : 30%
- 0.33 GeV 2 : 11%
- 0.35 GeV 2 : 2%
- 0.4 GeV 2 : 0.8%
- 0.5 GeV 2 : 0.1%

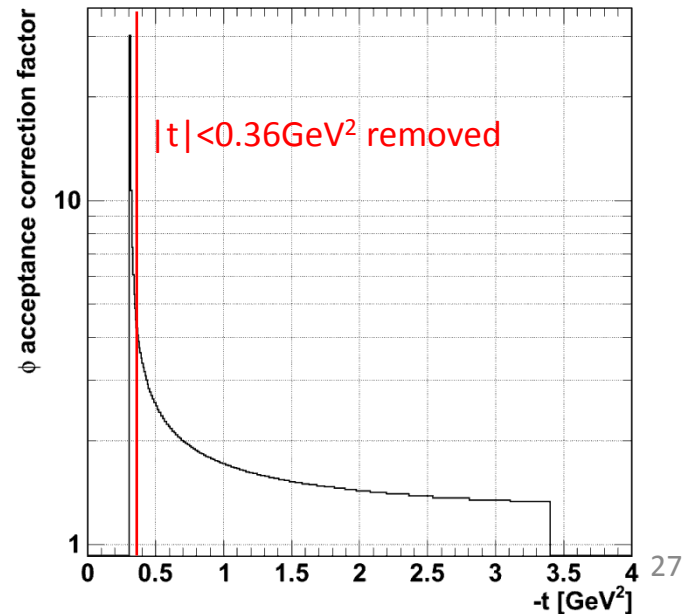


Acceptance corrections $\beta^*=3.5\text{m}$



Total φ -acceptance correction

No.	t [GeV^2]	Θ^* [rad]	Accepted φ (2 diag.) [$^\circ$]	φ accept. correct. factor
1	0.33	1.65E-04	38.6	$9.3 \pm 4.7\%$
2	0.36	1.71E-04	76.4	$4.7 \pm 1.8\%$
3	0.60	2.21E-04	162.5	$2.2 \pm 0.3\%$
4	1.00	2.86E-04	209.8	$1.7 \pm 0.1\%$
5	1.80	3.83E-04	246.3	1.5
6	3.00	4.95E-04	269.0	1.3



Critical at low t -acceptance limit