

Jet quenching from the lattice

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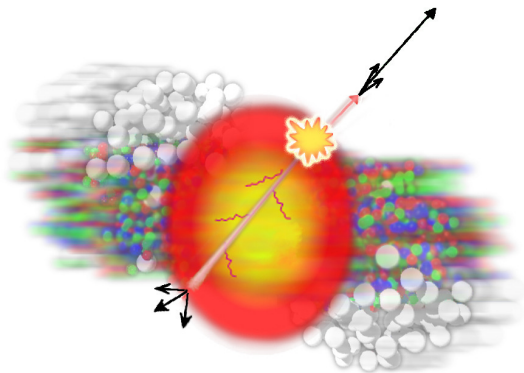
Outline

- 1 Introduction
- 2 Theoretical approach
- 3 Soft physics contribution from a Euclidean setup
- 4 Lattice implementation
- 5 Results
- 6 Conclusions



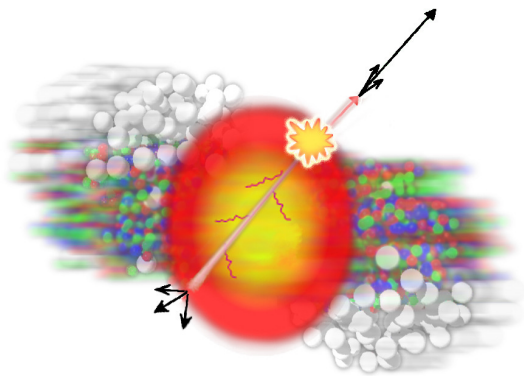
Momentum broadening of a hard parton in the QGP

Jet quenching is related to *energy loss* and *momentum broadening* experienced by a hard parton moving in deconfined medium [Bjorken, 1982](#)



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Multiple soft-scattering description, in the *eikonal approximation* [Baier et al., 1997](#)



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Can be evaluated in terms of a *collision kernel* $C(p_{\perp})$ (differential parton-plasma constituents collision rate)



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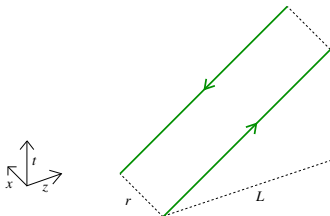
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$C(p_{\perp})$ is related to two-point correlator of *light-cone Wilson lines*



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Perturbative expansions may not be quantitatively reliable at RHIC or LHC temperatures



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Monte Carlo lattice computations rely *crucially* on a Euclidean setup, so are generally unsuitable for real-time phenomena



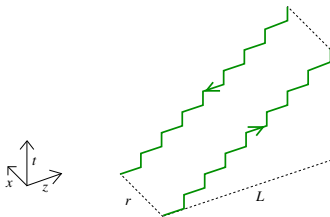
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A direct lattice evaluation of light-cone Wilson line correlators *very impractical*



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Key idea

Energy scale hierarchy in high-temperature, perturbative QCD:

$$g^2 T / \pi \text{ (ultrasoft)} \ll g T \text{ (soft)} \ll \pi T \text{ (hard)}$$

IR divergences accounted for by 3D effective theories [Braaten and Nieto, 1995](#)

[Kajantie et al., 1995](#):

- electrostatic QCD (3D Yang-Mills + adjoint scalar field) for soft scale
- magnetostatic QCD (3D pure Yang-Mills) for ultrasoft scale

Large NLO corrections hindering PT due to *soft*, essentially *classical* fields

Observation: Soft contributions to physics of light-cone partons *insensitive* to parton velocity \rightarrow Can turn the problem Euclidean! [Caron-Huot, 2008](#)



Proof

Spatially separated ($|t| < |z|$) light-like Wilson lines [Ghiglieri et al., 2013](#)

$$\begin{aligned}
 G^<(t, x_\perp, z) &= \int d\omega d^2 p_\perp dp^z \tilde{G}^<(\omega, p_\perp, p^z) e^{-i(\omega t - x_\perp \cdot p_\perp - z p^z)} \\
 &= \int d\omega d^2 p_\perp dp^z \left[\frac{1}{2} + n_B(\omega) \right] \left[\tilde{G}_R(\omega, p_\perp, p^z) - \tilde{G}_A(\omega, p_\perp, p^z) \right] e^{-i(\omega t - x_\perp \cdot p_\perp - z p^z)}
 \end{aligned}$$

Shift $p'^z = p^z - \omega t/z$, integrate over frequencies by analytical continuation into upper (lower) half-plane for retarded (advanced) contribution \rightarrow sum over Matsubara frequencies

$$G^<(t, x_\perp, z) = T \sum_{n \in \mathbb{Z}} \int d^2 p_\perp dp'^z \tilde{G}_E(2\pi n T, p_\perp, p'^z + 2\pi i n T t/z) e^{i(x_\perp \cdot p_\perp + z p'^z)}$$

- $n \neq 0$ contributions: exponentially suppressed at large separations
- Soft contribution: from $n = 0$ mode. Time-independent: evaluate in EQCD



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Electrostatic QCD on the lattice

Super-renormalizable EQCD Lagrangian

$$\mathcal{L} = \frac{1}{4} F_{ij}^a F_{ij}^a + \text{Tr} ((D_i A_0)^2) + m_E^2 \text{Tr} (A_0^2) + \lambda_3 (\text{Tr} (A_0^2))^2$$

Parameters chosen (by matching) to reproduce soft physics of high- T QCD

- 3D gauge coupling: $g_E^2 = g^2 T + \dots$
- Debye mass parameter: $m_E^2 = \left(1 + \frac{n_f}{6}\right) g^2 T^2 + \dots$
- 3D quartic coupling: $\lambda_3 = \frac{9-n_f}{24\pi^2} g^4 T + \dots$

Standard Wilson lattice regularization [Hietanen et al., 2008](#)

Our setup: QCD with $n_f = 2$ light flavors, two temperature ensembles:

- $T \simeq 398$ MeV
- $T \simeq 2$ GeV

Closely related studies in MQCD [Laine, 2012](#) [Benzke et al., 2012](#)

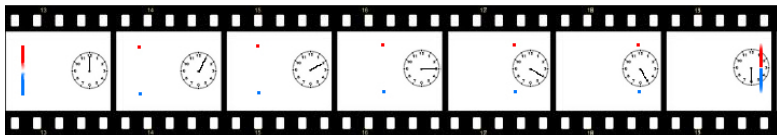


Operator implementation

Effective theory: purely spatial

but

Operator describes *real time* evolution



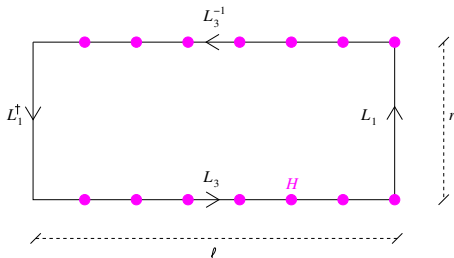
Operator implementation

Light-cone Wilson line correlator

$$\langle W(\ell, r) \rangle = \left\langle \text{Tr} \left(L_3 L_1 L_3^{-1} L_1^\dagger \right) \right\rangle \sim \exp[-\ell V(r)]$$

with

$$L_3 = \prod U_3 H \quad L_1 = \prod U_1 \quad H = \exp(-ag_E^2 A_0)$$



Well-defined renormalization properties [D'Onofrio et al., 2014](#)



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Contribution to \hat{q} related to the curvature of $V(r)$ near the origin



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Data fitted with a procedure similar to [Laine, 2012](#)

$$V/g_E^2 = A r g_E^2 + B (r g_E^2)^2 + C (r g_E^2)^2 \ln(r g_E^2) + \dots$$



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Purely NP soft contribution to \hat{q} is quite large

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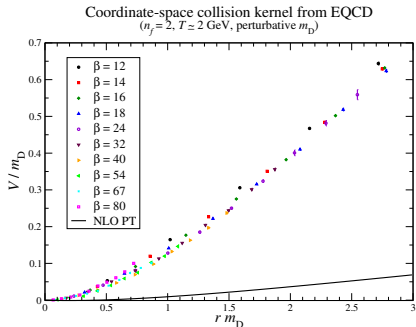
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Approximate estimate $\hat{q} \sim 6 \text{ GeV}^2/\text{fm}$ at RHIC temperatures



Lattice versus perturbation theory

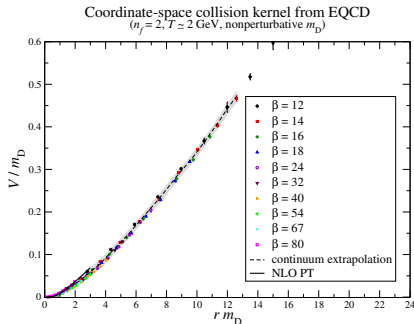
“Naïve” comparison with NLO PT



Lattice versus perturbation theory

Discrepancy reduced if data are plotted in terms of non-perturbative m_D

[Laine and Philipsen, 2008](#)

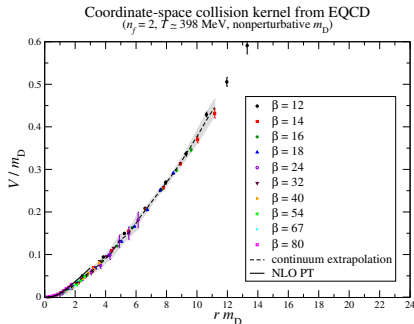


(For a discussion of screening masses and real-time rates, see also [Brandt et al., 2014](#))

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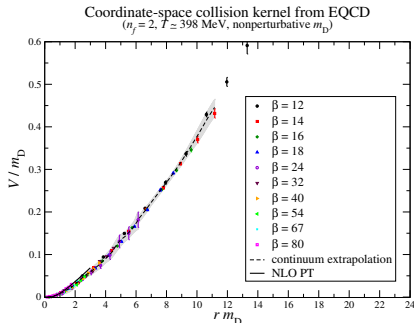


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Using NP value for m_D in

$$\hat{q}_{\text{EQCD}}^{\text{NLO}} = g^4 T^2 m_D C_f C_a \frac{3\pi^2 + 10 - 4 \ln 2}{32\pi^2}$$

yields again $\hat{q} \sim 6$ GeV²/fm at RHIC temperatures



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Conclusions

- Lattice approach *possible* for certain real-time problems—see also [Majumder, 2012](#)
[Ji, 2013](#)
- Here: focus on soft contributions [Laine and Rothkopf, 2013](#) [Cherednikov et al., 2013](#)
- A *systematic* approach
- Our results for jet quenching parameter give evidence of large non-perturbative effects
- Results in ballpark of
 - holographic computations [Liu, Rajagopal and Wiedemann, 2006](#) [Armesto, Edelman and Mas, 2006](#)
[Gürsoy, Kiritsis, Michalogiorgakis and Nitti, 2009](#) ✓
 - estimates from phenomenological models [Dainese et al., 2004](#) [Eskola et al., 2004](#)
[Bass et al., 2008](#) ✓—but see also [Burke et al., 2013](#) ✗
- Generalization to other observables (e.g. photon production rate, as suggested in [Chiglieri et al., 2013](#)) in progress

