

# Elliptic flow and nuclear modification factor within a partonic transport model

Florian Senzel

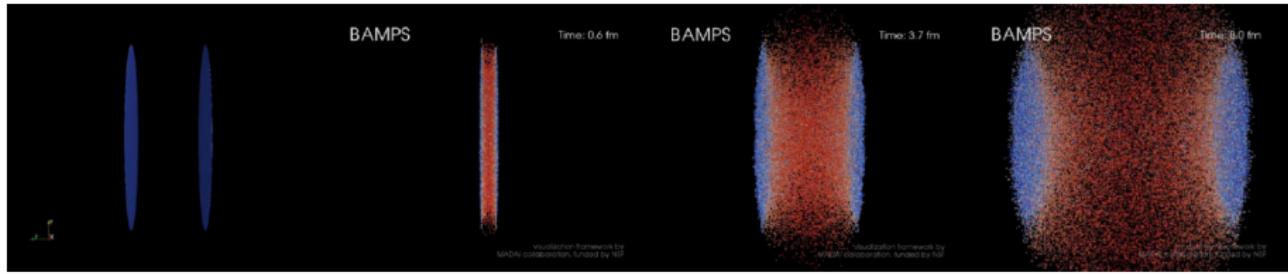
with J. Uphoff, O. Fochler, C. Wesp, Z. Xu and C. Greiner  
based on arXiv:1401.1364



Darmstadt, 19.05.2014

# Outline

- 1 Motivation
- 2 The partonic transport model BAMPS
- 3 Recent results about the...
  - ... nuclear modification factor  $R_{AA}$
  - ... elliptic flow  $v_2$
  - ... momentum imbalance  $A_J$  of reconstructed jets

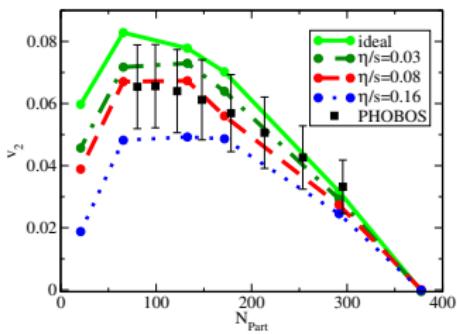
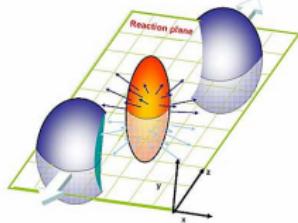


Visualization by Jan Uphoff  
Visualization framework courtesy MADAI collaboration  
funded by the NSF under grant NSF-PHY-09-41373

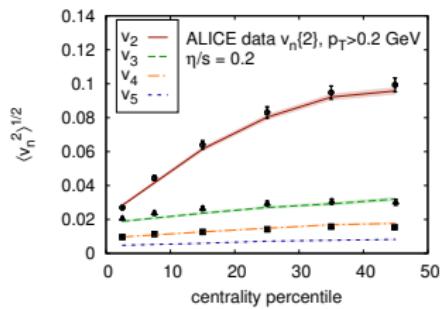
# Collectivity of the bulk regime: Elliptic flow $v_2$

## Fourier decomposition of particle spectra

$$\frac{d^3 N}{p_t dp_t dy d\phi} (p_t, y, \phi) = \frac{1}{2\pi} \frac{d^2 N}{p_t dp_t dy} [1 + 2v_2(p_t, y) \cos(2\phi) + \dots]$$



by Romatschke, Phys.Rev.Lett. 99, (2007)



by Gale et al., Phys.Rev.Lett. 110 (2013)

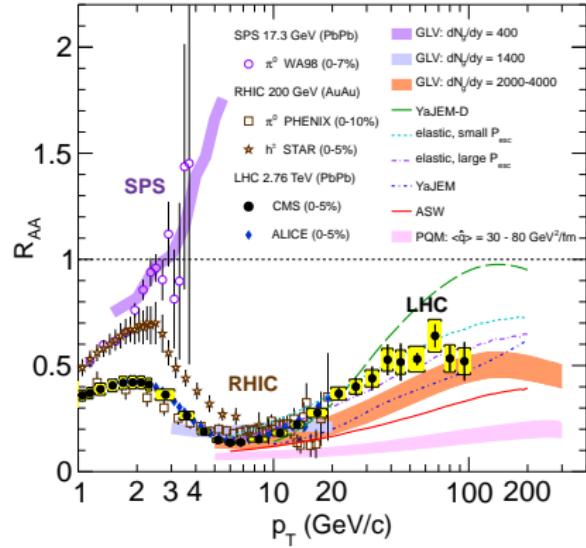
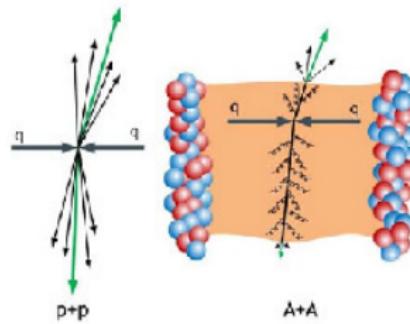
## State-of-the-art

- ✓ Well described by relativistic (viscous) hydrodynamics

# Jet quenching: Nuclear modification factor $R_{AA}$

Suppression of inclusive particle spectra

$$R_{AA} = \frac{d^2N_{AA}/dp_t dy}{N_{bin} d^2N_{pp}/dp_t dy}$$



by CMS Collaboration, Eur. Phys. J. C (2012)

State-of-the-art

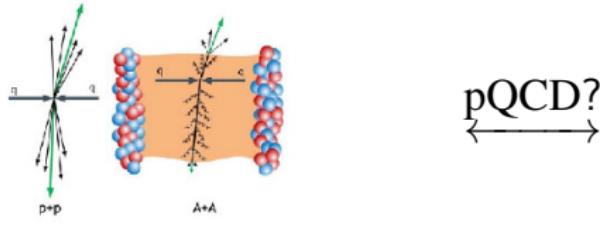
- ✓ Well described by perturbative quantum chromodynamics

Our question:

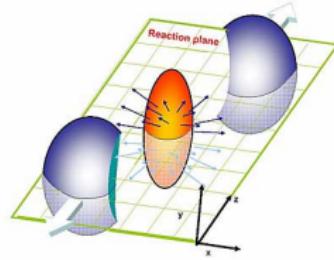
Can perturbative QCD interactions explain in a common framework

both the **high  $p_t$**  and the **bulk medium** regime

and thereby give microscopical insight into the QGP?



pQCD?



# The partonic transport model BAMPS

BAMPS  $\hat{=}$  Boltzmann Approach to Multi-Parton Scattering<sup>1</sup>

Numerical solver for the (3+1)D Boltzmann transport equation for partons on the mass-shell:

$$\frac{\partial f}{\partial t} + \frac{\mathbf{p}}{E} \frac{\partial f}{\partial \mathbf{r}} = C_{2 \rightarrow 2} + C_{2 \leftrightarrow 3}$$

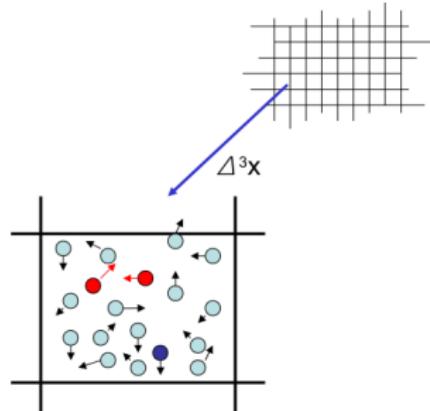
- Massless particles (gluons & quarks)
- Discretized space  $\Delta V$  and time  $\Delta t$ :

$$P_{2 \rightarrow 2} = v_{rel} \sigma_{2 \rightarrow 2} \frac{\Delta t}{\Delta V} \quad P_{2 \rightarrow 3} = v_{rel} \sigma_{2 \rightarrow 3} \frac{\Delta t}{\Delta V}$$

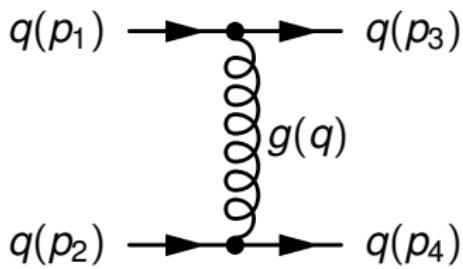
$$P_{3 \rightarrow 2} = \frac{l_{3 \rightarrow 2}}{8 E_1 E_2 E_3} v_{rel} \frac{\Delta t}{\Delta V^2}$$

- Test-particles ansatz  $N_{test}$

<sup>1</sup>Xu and Greiner, Phys.Rev.C71 (2005); Xu and Greiner, Phys.Rev.C76 (2007)



# Implemented processes - elastic collisions



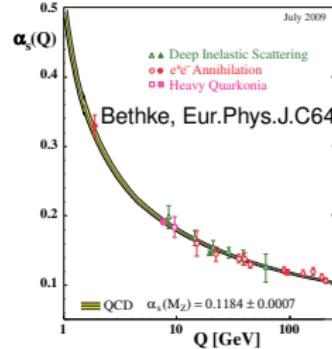
Screened ME with running coupling

$$|\overline{\mathcal{M}}_{X \rightarrow Y}|^2 = C_{X \rightarrow Y} 64\pi^2 \alpha_s^2(t) \frac{s^2}{[t - m_D^2(\alpha_s(t))]^2}$$

$$\text{with } m_D^2(\alpha_s(t)) = d_G \pi \alpha_s(t) \int \frac{d^3 p}{(2\pi)^3} \frac{1}{p} (N_c f_g + N_f f_q)$$

## LO pQCD cross-sections

- $g g \rightarrow g g$
- $g g \rightarrow q \bar{q}$
- $q \bar{q} \rightarrow g g \text{ and } q \bar{q} \rightarrow q' \bar{q}'$
- $q g \rightarrow q g \text{ and } \bar{q} g \rightarrow \bar{q} g$
- $\bar{q} \bar{q} \rightarrow \bar{q} \bar{q}$
- $q q \rightarrow q q \text{ and } \bar{q} \bar{q} \rightarrow \bar{q} \bar{q}$
- $q q' \rightarrow q q' \text{ and } q \bar{q}' \rightarrow q \bar{q}'$



Uphoff, Fochler, Xu, Greiner: Phys.Rev.C84 (2011)

# Implemented processes - radiative processes

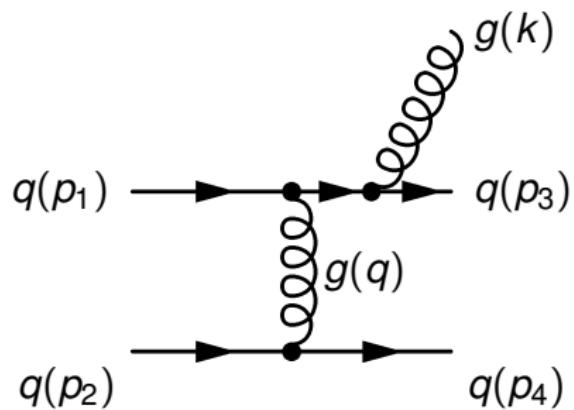
## Improved Gunion-Bertsch ME

$$|\overline{\mathcal{M}}_{X \rightarrow Y+g}|^2 = |\overline{\mathcal{M}}_{X \rightarrow Y}|^2 \cdot 48\pi\alpha_s(k_\perp^2) \cdot (1-\bar{x})^2 \times \left[ \frac{\mathbf{k}_\perp}{k_\perp^2} + \frac{\mathbf{q}_\perp - \mathbf{k}_\perp}{(\mathbf{q}_\perp - \mathbf{k}_\perp)^2 + m_D^2(\alpha_s(k_\perp^2))} \right]^2$$

with  $\bar{x} = k_\perp e^{|y|}/\sqrt{s}$

## 2 → 3 processes

$$\begin{aligned} gg &\rightarrow ggg \\ qg &\rightarrow qgg \quad \text{and} \quad \bar{q}g \rightarrow \bar{q}gg \\ q\bar{q} &\rightarrow q\bar{q}g \\ qq &\rightarrow qqg \quad \text{and} \quad \bar{q}\bar{q} \rightarrow \bar{q}\bar{q}g \\ qq' &\rightarrow qq'g \quad \text{and} \quad \bar{q}\bar{q}' \rightarrow \bar{q}\bar{q}'g \end{aligned}$$

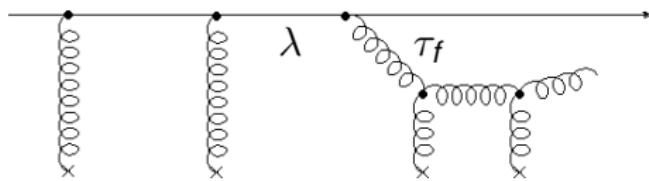


- Gunion, Bertsch: Phys.Rev.D25 (1982)
- Fochler, Uphoff, Xu, Greiner: Phys.Rev.D88 (2013)

# Effective modeling of the LPM effect

## Issue

Coherence effects within a **semi-classical** approach are not trivial.



## Effective method

Parent parton is not allowed to scatter before emitted gluon is formed:

$$|\mathcal{M}_{2 \rightarrow 3}|^2 \rightarrow |\mathcal{M}_{2 \rightarrow 3}|^2 \Theta(\lambda - X_{\text{LPM}} \tau_f)$$

$X_{\text{LPM}} = 0$       No LPM suppression

$X_{\text{LPM}} = 1$       Only independent scatterings (forbids too many emissions)

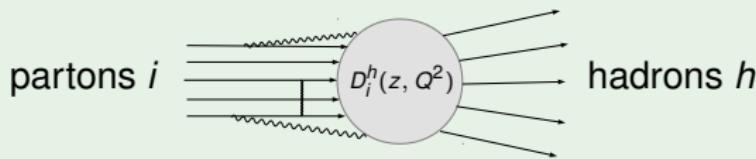
$X_{\text{LPM}} \in (0; 1)$       Allows effectively some interference effects

# From partons to hadronic observables

## “High $p_t$ ” observables

- Folding with fragmentation functions  $D_i^h(z, Q^2)$ ,

$$\frac{d^2N^h}{dp_t dy} \left( p_t^h \right) = \sum_i \int_{z_{min}}^1 dz \frac{d^2N^i}{dp_t dy} \left( \frac{p_t^h}{z} \right) D_i^h \left( z, Q^2 \right) \text{ with } z = \frac{p_t^h}{p_t^i}$$



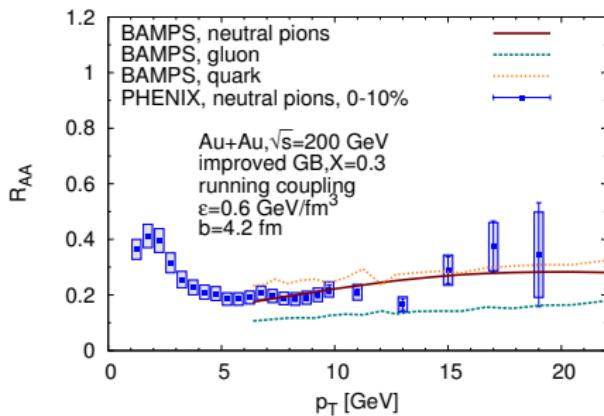
Fragmentation functions by e.g. Albino,  
Kniehl, Kramer: Nucl.Phys.B803(2008)

## “Low $p_t$ ” observables

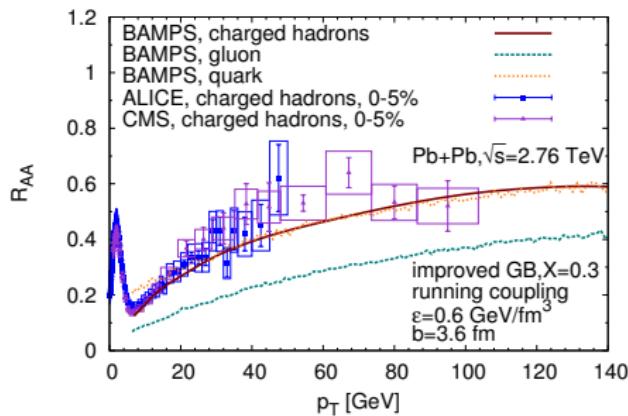
- Microscopic hadronization processes are unknown.
- Integrated flow should not be sensitive to phase transition.

# Nuclear modification factor $R_{AA}$ of central HI-collisions

RHIC

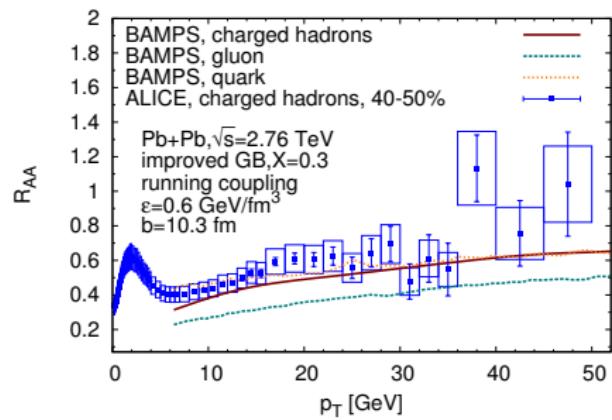
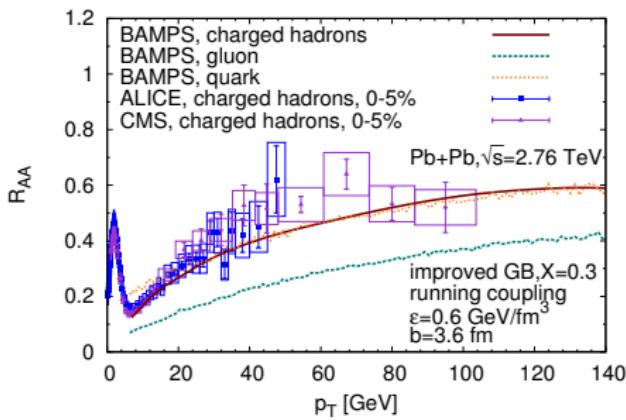
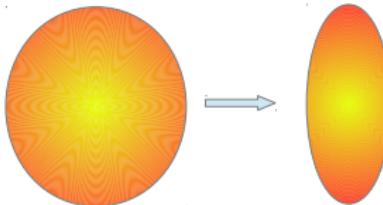


LHC

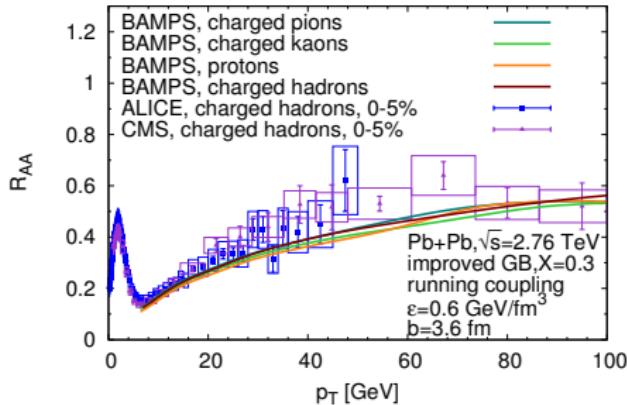
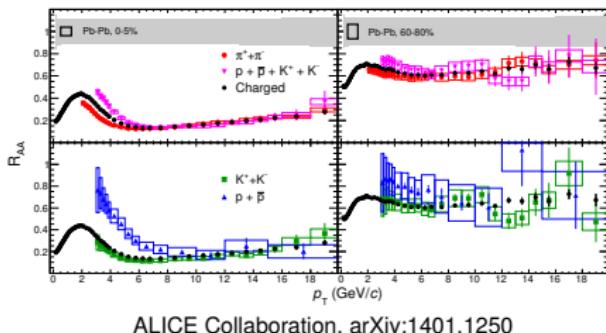
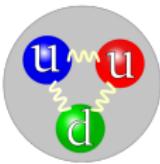
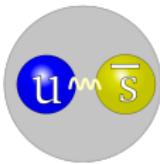


- PYTHIA initial conditions distributed by Glauber model.
- After fixing the LPM parameter  $X_{LPM} = 0.3$  by comparing to RHIC data, BAMPS describes the  $R_{AA}$  also at LHC.
- Suppression caused by the interplay between the improved GB matrix element and the microscopic running coupling.

# $R_{AA}$ of peripheral HI-collisions

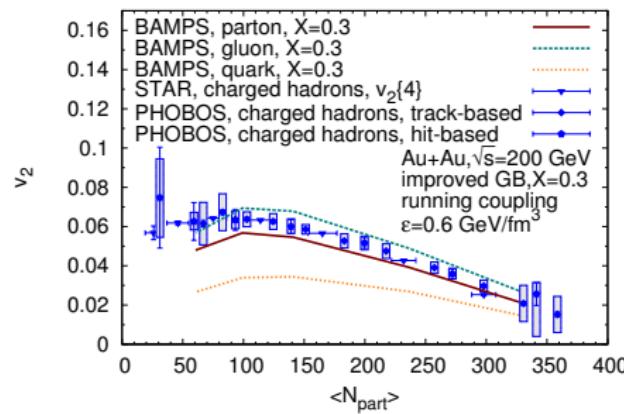


# $R_{AA}$ of central HI collisions for different hadron species

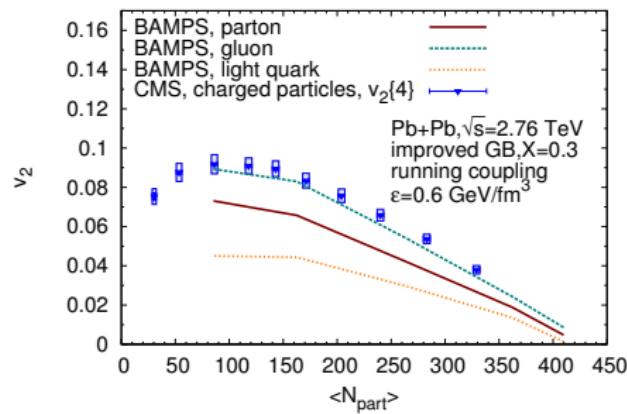


# Integrated elliptic flow $v_2$ ( $N_{\text{part}}$ )

RHIC



LHC



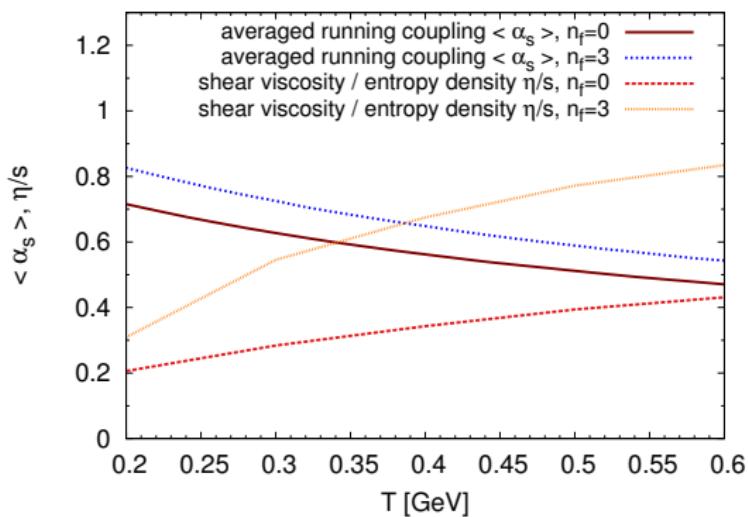
Same setup with LPM parameter  $X_{\text{LPM}} = 0.3$  leads to a sizable elliptic flow built up in the partonic phase.

## Attention

No hadronization for bulk  $\Rightarrow$  No hadronic after-burner  $\Rightarrow$  Missing 10-20%?!

# Macroscopic quantities from microscopic interactions

## Static medium



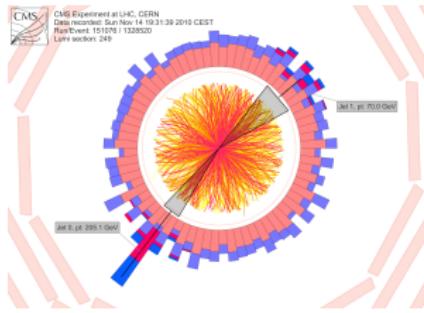
## Shear viscosity ratio $\eta/s$

- Reason for large flow: small shear viscosity over entropy ratio
- Calculated with Green-Kubo formalism
- Recent viscous hydro:  $\eta/s = 0.2$

## Running coupling $\alpha_s(T)$

- Temperature dependent coupling by microscopically evaluated interactions.

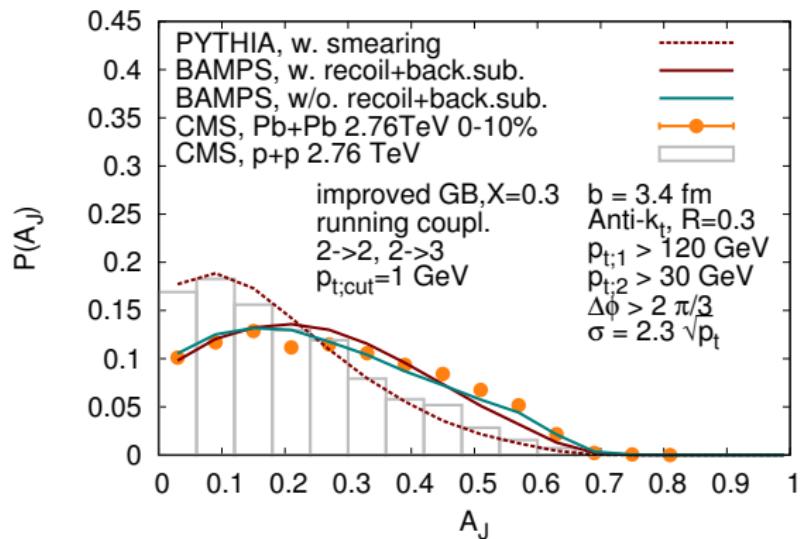
# Reconstructed jets in heavy-ion collisions



# Momentum imbalance $A_J$ of reconstructed di-jets

## Definition

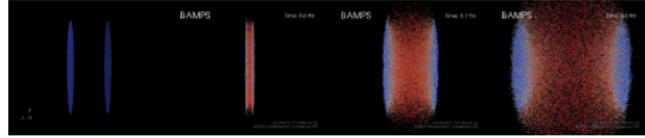
$$A_J = \frac{p_{t;Leading\ Jet} - p_{t;Subleading\ Jet}}{p_{t;Leading\ Jet} + p_{t;Subleading\ Jet}}$$



FS, Fochler, Uphoff, Xu, Greiner: arXiv:1309.1657

# Conclusions

- Partonic transport provides means for...
  - exploring dynamics of the QGP evolution based on pQCD processes.
  - exploring different observables within a common framework.
- Realistic suppression of jets both at RHIC and LHC.
- Sizable collective flow within the medium by microscopic pQCD cross sections.



## Future plans:

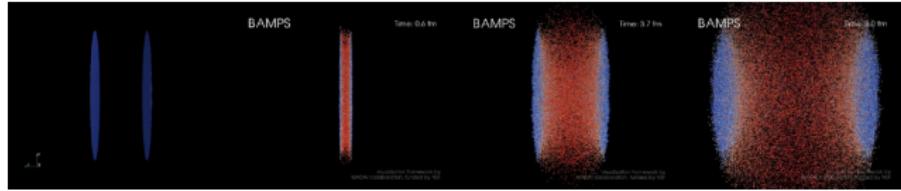
- How does a revisited modeling of the LPM effect change the energy loss and its path-length dependence?
- Systematic studies!

# Conclusions

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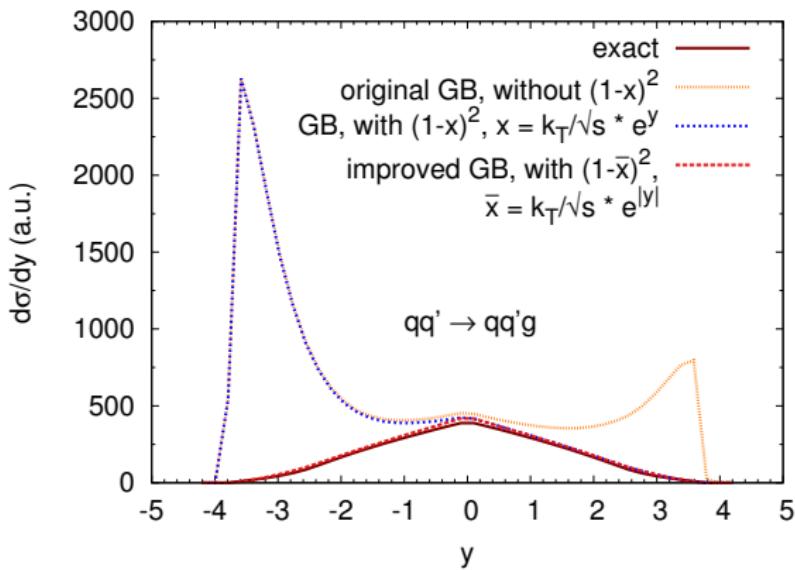
## BAMPS@QM2014

- Heavy quarks:  
Talk by J. Uphoff
- Mach cones:  
Poster by I. Bouras
- Reconstructed jets:  
Poster by FS



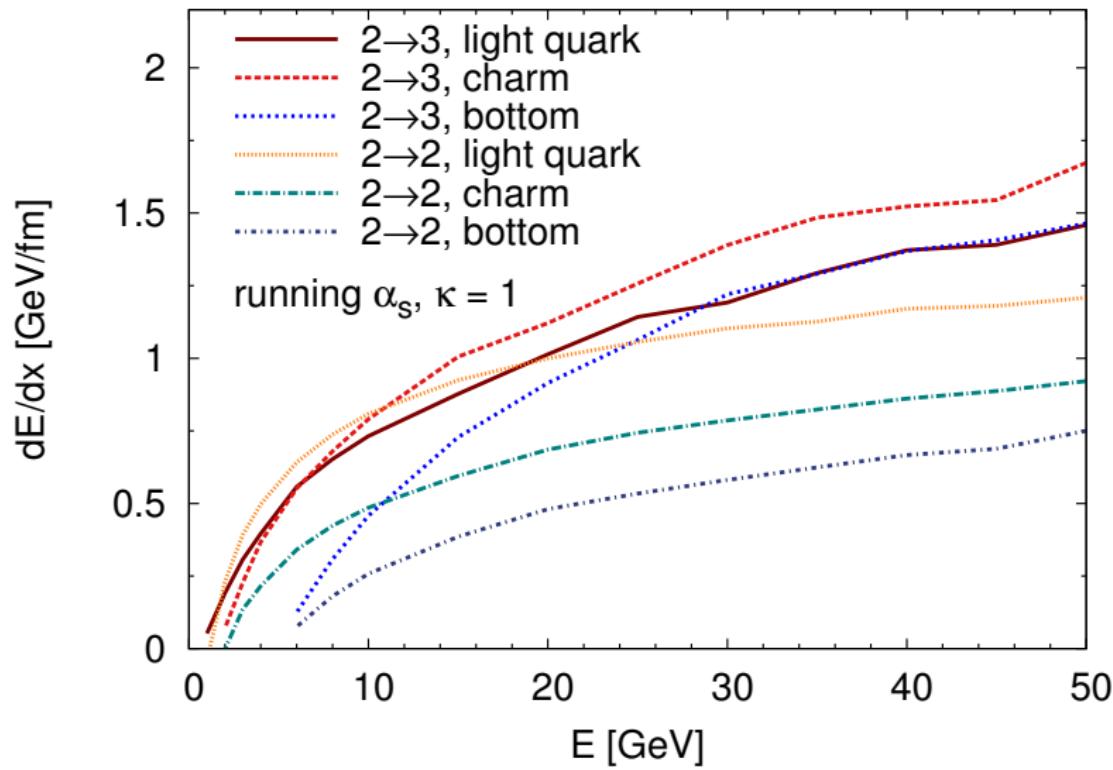
# Backup slides

# Improved Gunion-Bertsch matrix element



- Infrared screening for both GB and exact:  $\theta(\text{cut}) = \theta(p_i p_j - \lambda)$ .
- Integration both in GB coordinates and in standard phase space with numeric  $\delta$ -functions.

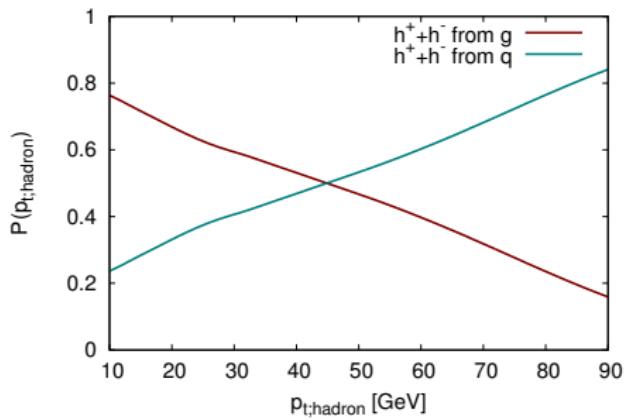
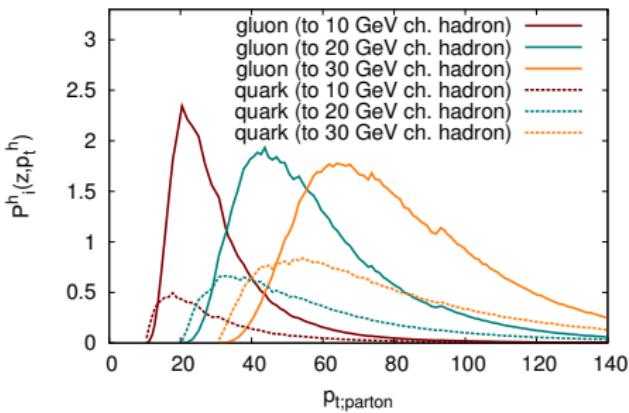
# Differential energy loss in a static medium



# Closer look on the role of fragmentation

Probability for hadron  $h$  with  $p_t^h$  out of parton  $i$  with  $p_t^i = p_t^h/z$

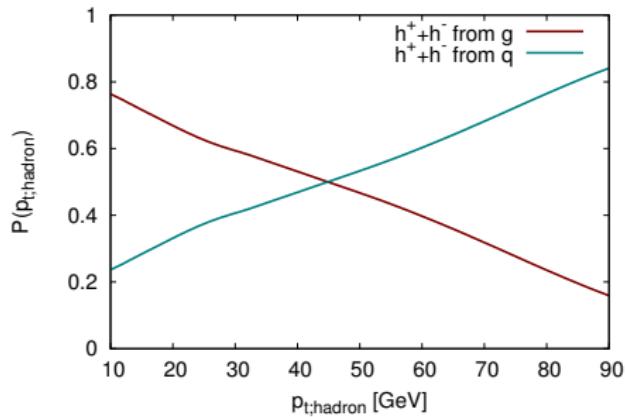
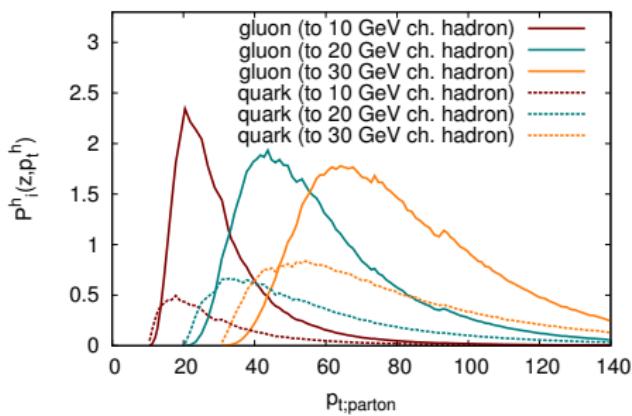
$$P^{i \rightarrow h} (z, p_t^h) = \frac{1}{\frac{d^2 N^i}{dp_t dy} (p_t^h)} \frac{d^2 N^i}{dp_t dy} \left( \frac{p_t^h}{z} \right) D_i^h (z, Q^2)$$



# Example: $R_{AA}$ for hadrons with $p_t^h = 30 \text{ GeV}$

Hadrons with  $p_t^h = 30 \text{ GeV}$  stem...

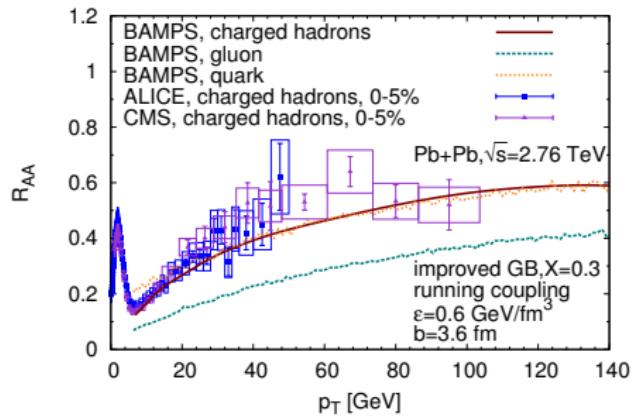
- ... mainly from  $\approx 60 \text{ GeV}$  gluon and  $\approx 45 \text{ GeV}$  quark.
- ...  $\approx 60\%$  from gluons and  $\approx 40\%$  from quarks. 6



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- ...  $\approx 60\%$  from gluons and  $\approx 40\%$  from quarks. 6



$$R_{AA}^h(30 \text{ GeV}) = 0.4 R_{AA}^g(60 \text{ GeV}) + 0.6 R_{AA}^q(45 \text{ GeV}) \approx 0.3$$

# Example: Shower event with first 100 recoil partons

