



# Generic framework for anisotropic flow analyses with multi-particle azimuthal correlations (arXiv:1312.3572)

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## Generic framework

- Generic framework for multi-particle correlators.
- Exact and efficient evaluation.
- Requires only single pass over data.
- Includes acceptance and efficiency corrections.
- Recursive algorithms extend implementation to  $n$ -particle correlations.
- New observables proposed.

## The complex made simple

Average  $m$ -particle correlation in harmonics  $n_1, n_2, \dots, n_m$ :

$$\langle m \rangle_{n_1, n_2, \dots, n_m} \equiv \left\langle e^{i(n_1 \varphi_{k_1} + n_2 \varphi_{k_2} + \dots + n_m \varphi_{k_m})} \right\rangle.$$

Factorization implies analytical mean value [1]:

$$\mu \langle m \rangle_{n_1, n_2, \dots, n_m} = v_{n_1} \dots v_{n_m} e^{i(n_1 \Psi_{n_1} + \dots + n_m \Psi_{n_m})}.$$

Values estimated directly in single pass over data, using the weighted Q-vectors,  $Q_{n,p} \equiv \sum_{k=1}^M w_k^p e^{in\varphi_k}$ . Equations given for the 2- to 4-particle correlators; Recursive algorithms for any  $n$ -particle correlators. This establishes a wealth of new observables to probe non-linear effects of hydrodynamics, e.g.:

$$\langle \langle \cos(m\varphi_1 + n\varphi_2 - m\varphi_3 - n\varphi_4) \rangle \rangle,$$

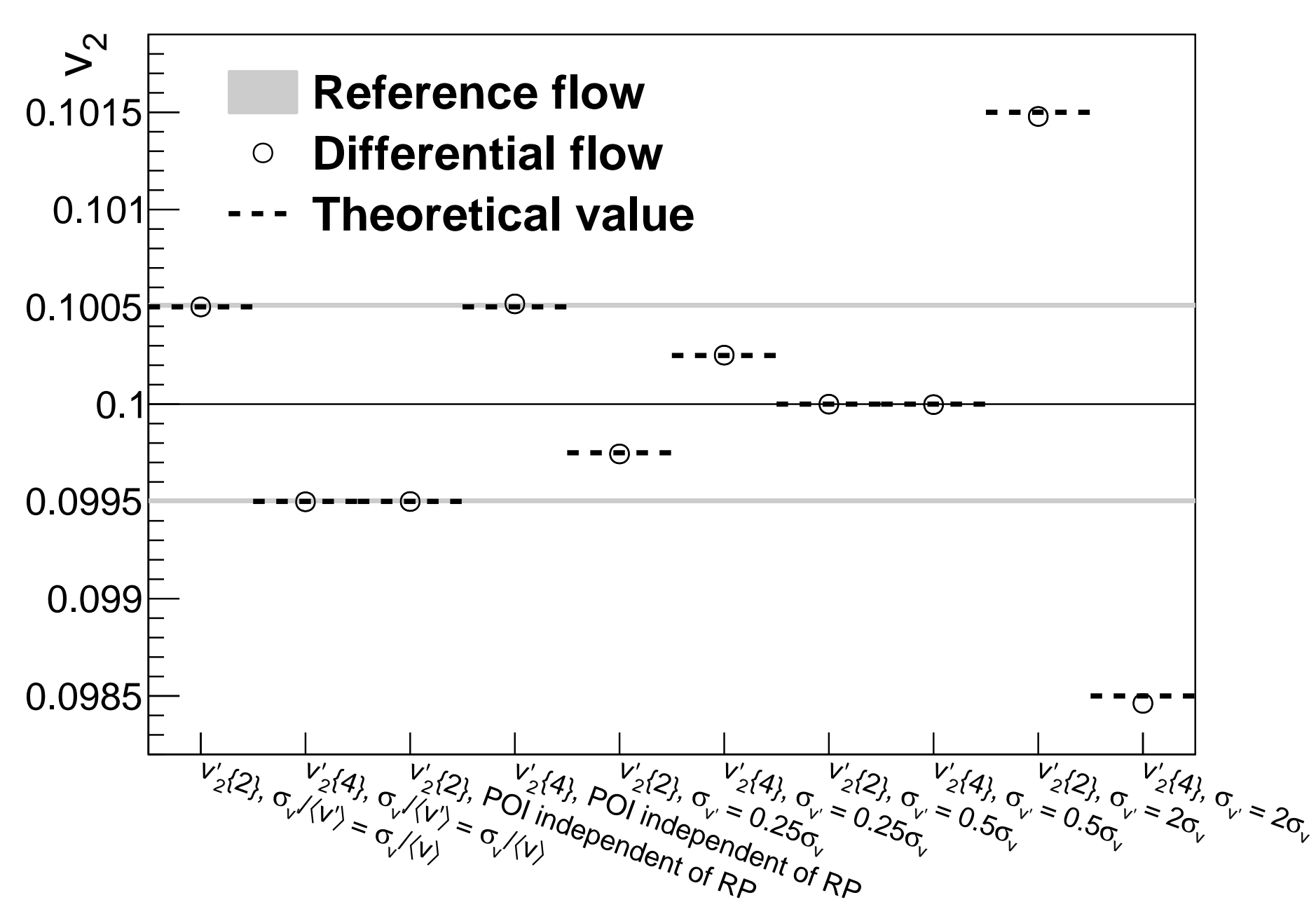
which for  $m \neq n$  has the isotropic parts of the 4-particle cumulant given by:

$$\langle \langle \cos(m\varphi_1 + n\varphi_2 - m\varphi_3 - n\varphi_4) \rangle \rangle_c = \langle v_m^2 v_n^2 \rangle - \langle v_m^2 \rangle \langle v_n^2 \rangle \equiv SC_{m,n,-m,-n}.$$

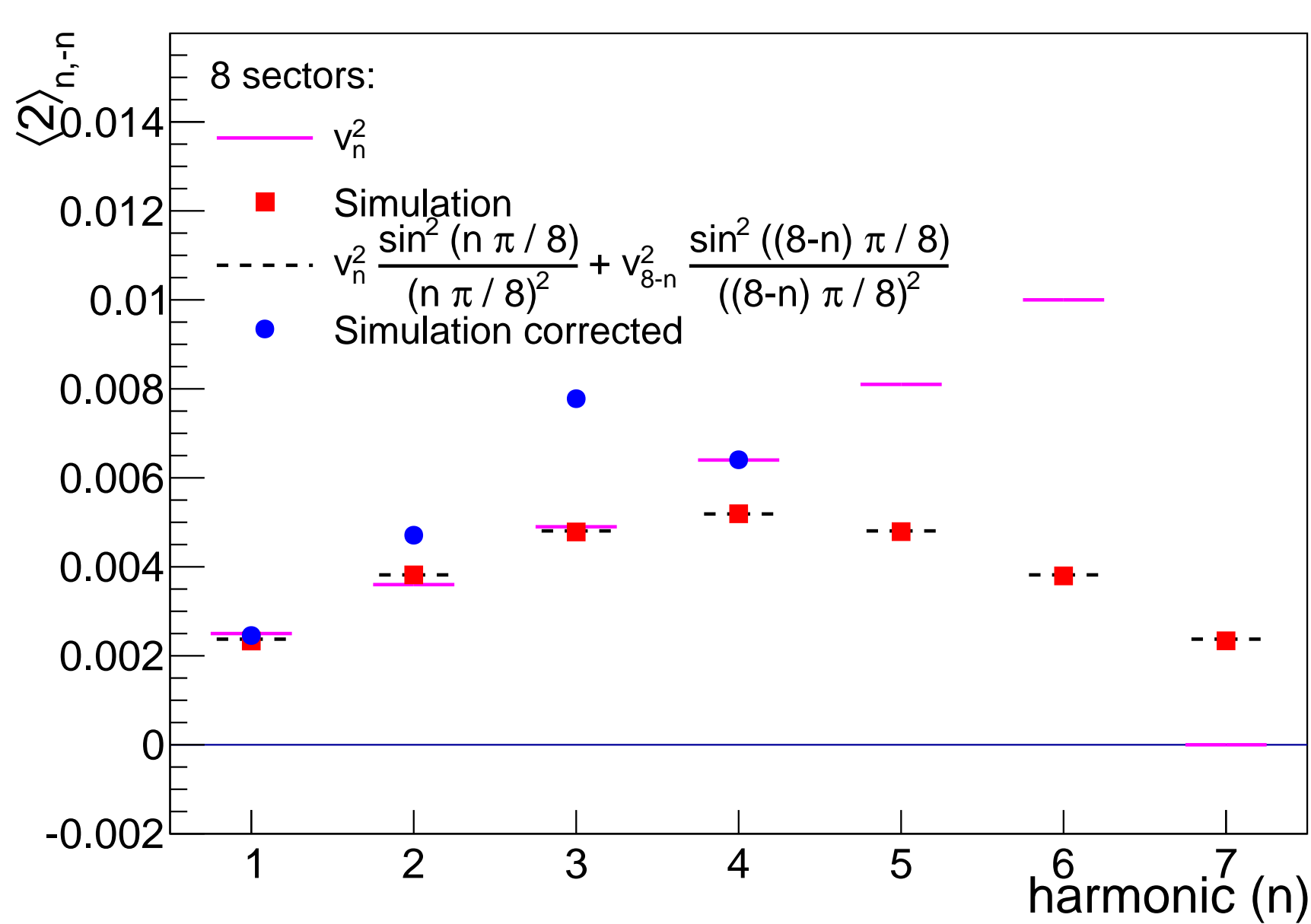
► C++ and Mathematica code at: <http://www.nbi.dk/~cholm/mcorrelations/>

## In depth analysis of biases

- Generic framework extended to differential flow.

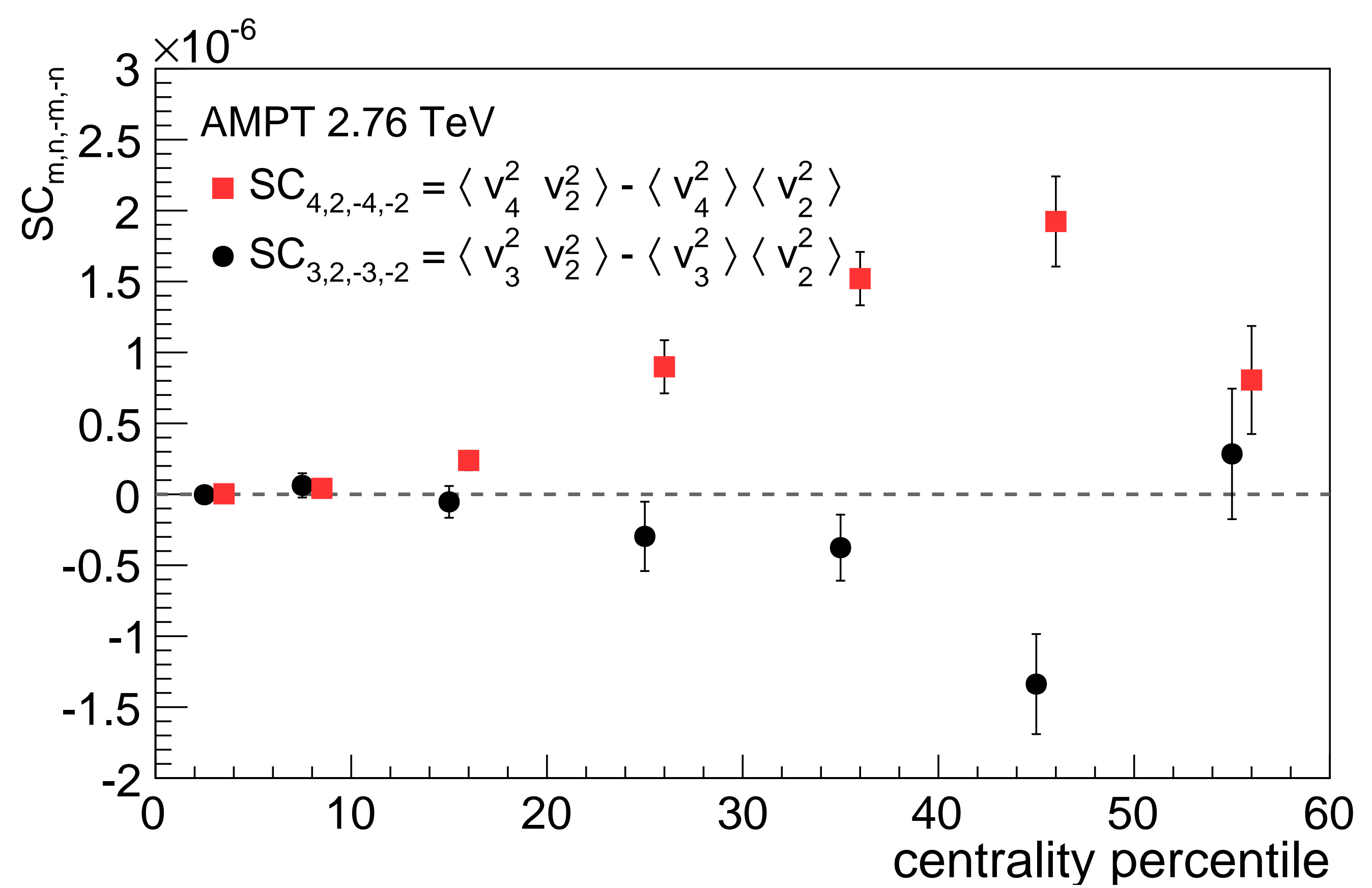


- Possible biases from particle selection criteria in differential flow analyses.



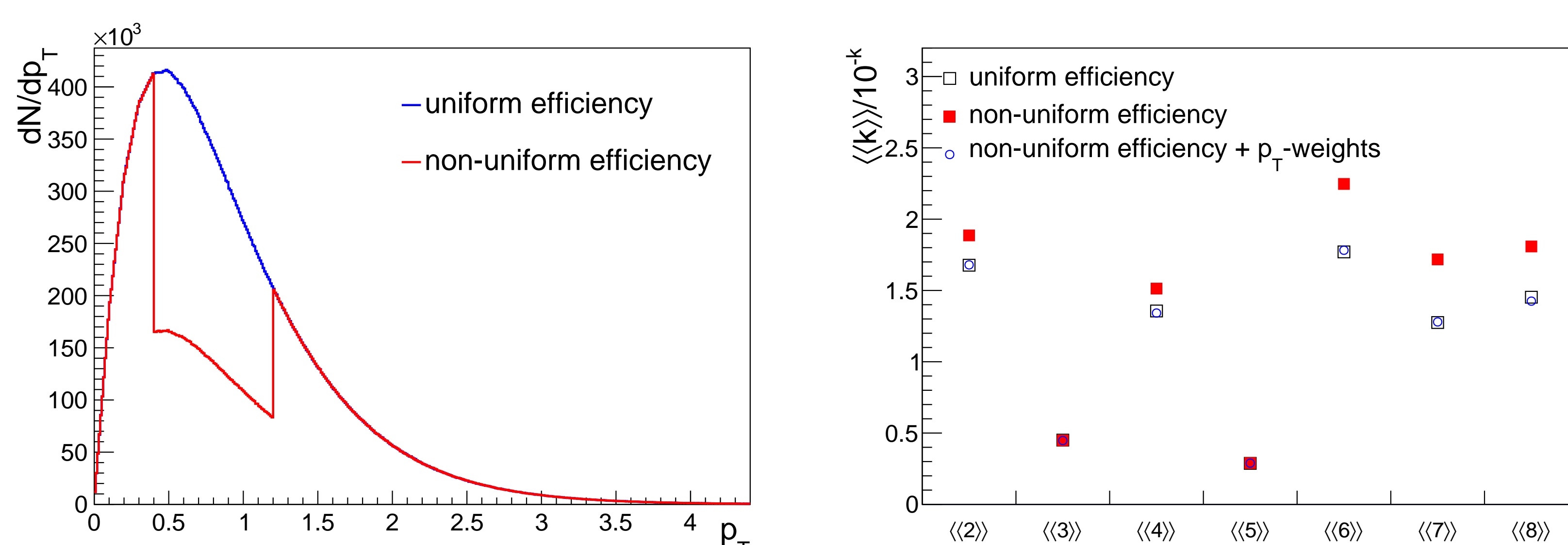
- Biases due to finite detector granularity calculated.

## New observables - The Standard Candles



AMPT[2] with LHC tune[3] for new observables. AMPT predicts non-zero values for correlations of event-by-event fluctuations between  $v_2$  and  $v_3$  and between  $v_2$  and  $v_4$ . New observables provide valuable information on non-linear hydrodynamic effects.

## Using $p_T$ -weights for efficiency and $\varphi$ -weights for acceptance corrections



Left: Example  $p_T$  efficiency profile. Right:  $p_T$ -weights (blue circles) removes bias from efficiency (red squares), recovers input (black squares).

## References and further information

### References

- [1] R. S. Bhalerao, M. Luzum and J. -Y. Ollitrault, Phys. Rev. C **84** (2011) 034910 [arXiv:1104.4740 [nucl-th]].
- [2] Z. -W. Lin, C. M. Ko, B. -A. Li, B. Zhang and S. Pal, Phys. Rev. C **72** (2005) 064901 [nucl-th/0411110].
- [3] J. Xu and C. M. Ko, Phys. Rev. C **83** (2011) 034904 [arXiv:1101.2231 [nucl-th]].



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