

Viscous corrections to photon emission in heavy-ion collisions

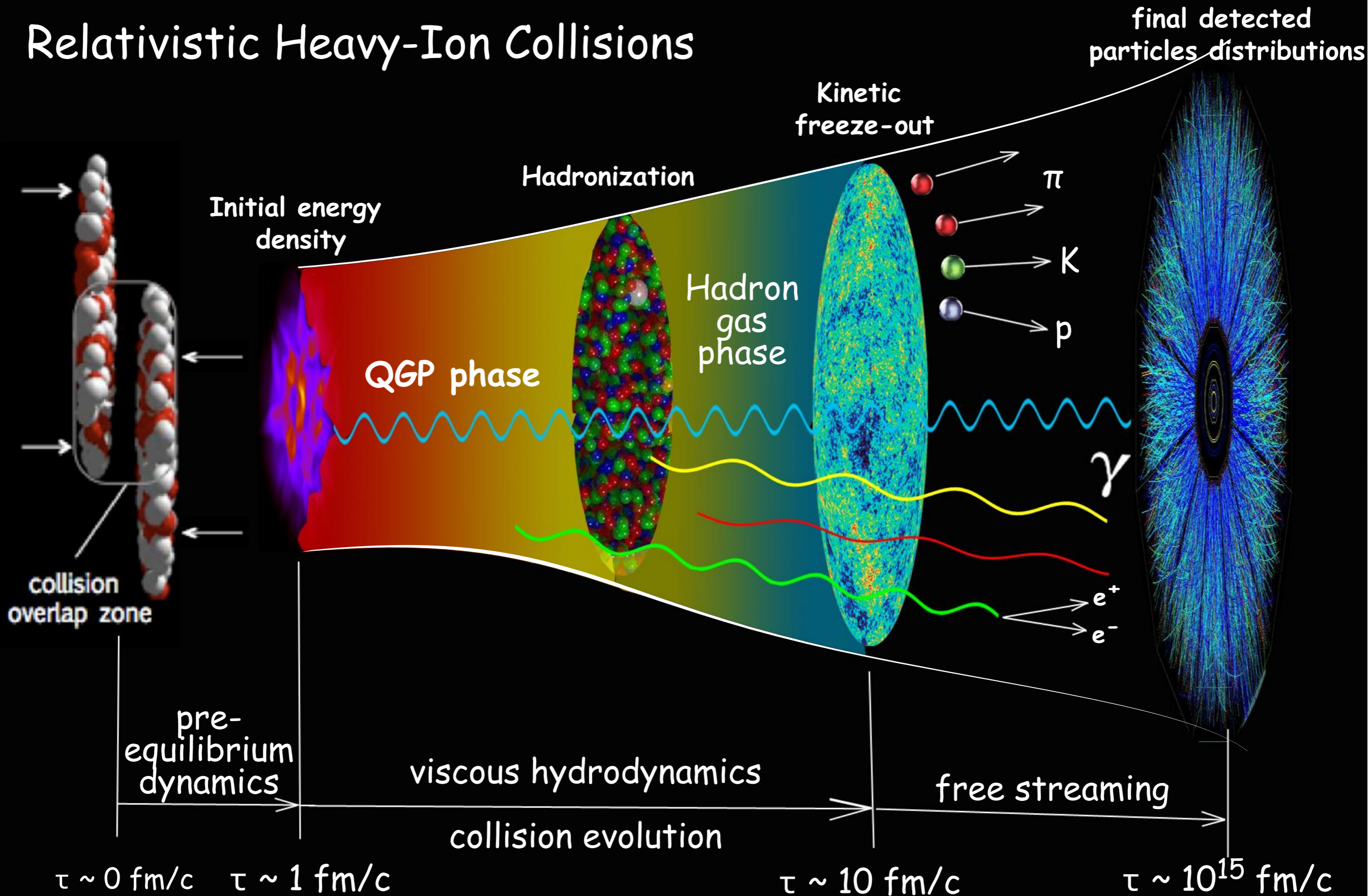
Chun Shen

The Ohio State University

In collaboration with Ulrich Heinz, Charles Gale, Gabriel Denicol, Jia Liu, and Jean-Francois Paquet

Little Bang

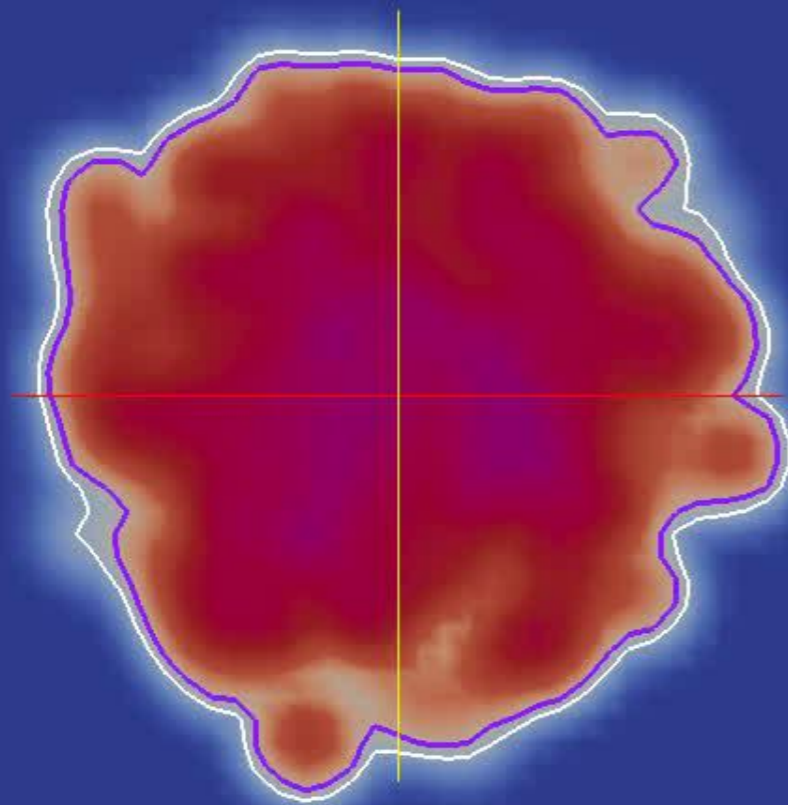
Relativistic Heavy-Ion Collisions



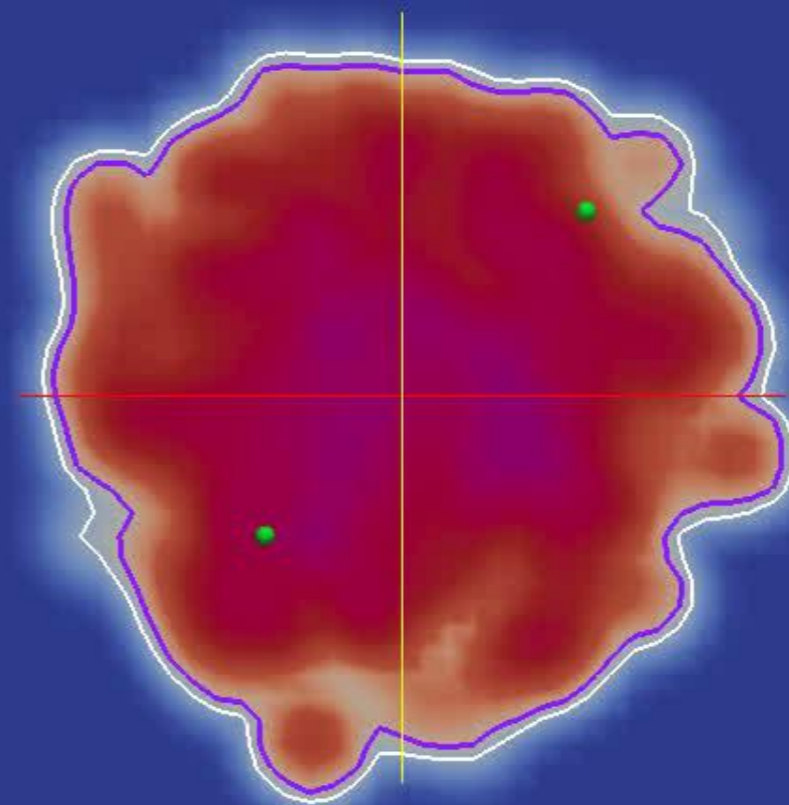
Photons from Heavy-Ion Collisions

time = 0.6 fm/c

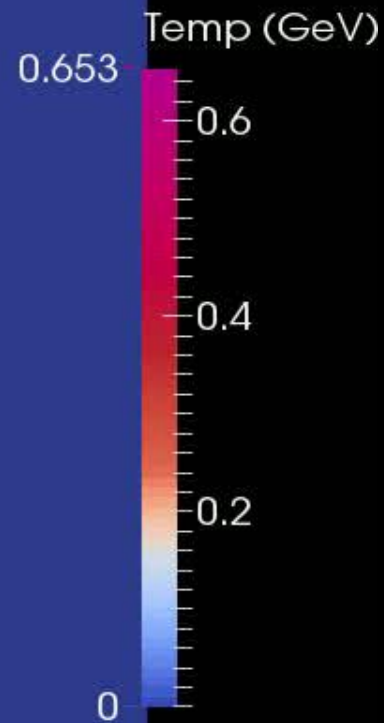
Pb+Pb @ 2.76 A TeV LHC



Charged Hadrons



Thermal Photons oversample = 10



State-of-the-art hydrodynamic modeling

<https://github.com/chunshen1987/iEBE.git>



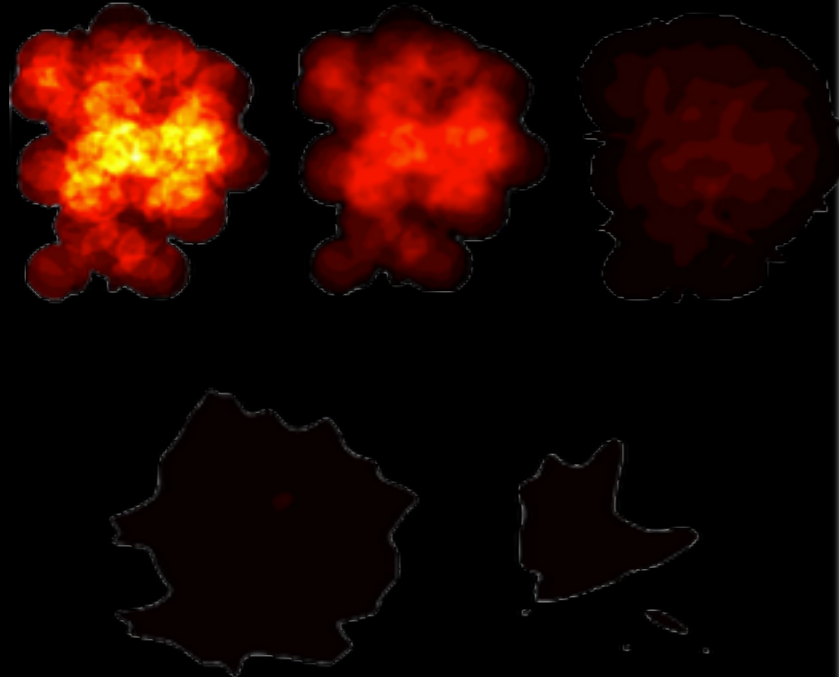
Initial Condition
Generators
(MC- KLN, MC- Glauber)

Thermal Photon
Emission Rates

Hydrodynamic
Simulations
(VISH2+1)

HydroInfo
Package

Thermal Photon
Interface



$e, s, p, T,$
 $u^\mu, \hat{u}^\mu \hat{e}$

$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\hat{u}^\mu \hat{e}^\nu q_\mu q_\nu}{2(e+p)} a_{\mu\nu} \Gamma^{\mu\nu}$$

$$E \frac{dN^Y}{d^3p} = \int d^4x q \frac{dR}{d^3q}$$

Hadrons spectra &
 v_n

Photon spectrum &
 v_n

State-of-the-art hydrodynamic modeling

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Initial Condition
Generators
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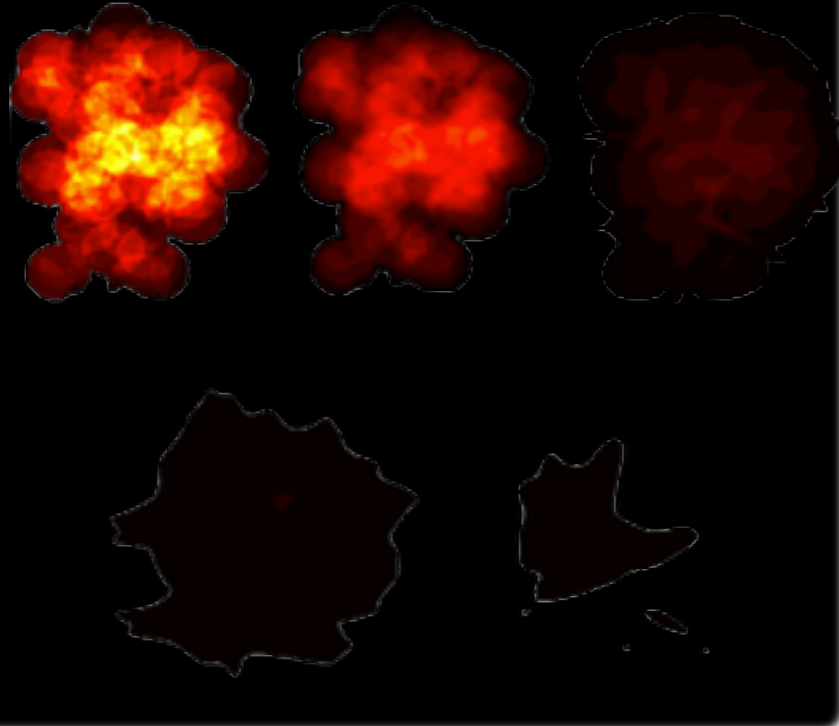
Thermal Photon
Emission Rates

viscous
corrections

Hydrodynamic
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$e, s, p, T,$
 $u^\mu, \hat{u}^{\mu\alpha}$

$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\hat{u}^{\mu\alpha} q_\mu q_\alpha}{2(e+p)} a_{\alpha\beta} \Gamma^{\alpha\beta}$$

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viscous
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Hadrons spectra &
 v_n

Photon spectrum &
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Viscous Photon Emission Rates: General Formalism

Thermal photon emission rates can be calculated by

$$E_q \frac{dR}{d^3q} = \frac{d^3p_1}{2E_1(2\pi)^3} \frac{d^3p_2}{2E_2(2\pi)^3} \frac{d^3p_3}{2E_3(2\pi)^3} \frac{1}{2(2\pi)^3} |M|^2$$

$$\rightarrow f_1(p_1^\mu) f_2(p_2^\mu) (1 \pm f_3(p_3^\mu)) (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p_3 - q)$$

With

$$f(p^\mu) = f_0(E) + f_0(E)(1 \pm f_0(E)) \frac{\hat{p}_\mu \hat{p}_\nu}{2(e+p)} \chi^{\mu\nu} \frac{p^\sigma}{T}$$

We can expand photon emission rates around the thermal equilibrium:

$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\pi^{\mu\nu} \hat{q}_\mu \hat{q}_\nu}{2(e+p)} a_{\alpha\beta} \Gamma^{\alpha\beta},$$

$$a_{\mu\nu} = \frac{3}{2(u \cdot \hat{q})^4} \hat{q}_\mu \hat{q}_\nu + \frac{1}{(u \cdot \hat{q})^2} u_\mu u_\nu + \frac{1}{2(u \cdot \hat{q})^2} g_{\mu\nu} - \frac{3}{2(u \cdot \hat{q})^3} (\hat{q}_\mu u_\nu + \hat{q}_\nu u_\mu).$$

Viscous Photon Emission Rates: General Formalism

Thermal photon emission rates can be calculated by

$$E_q \frac{dR}{d^3q} = \frac{d^3p_1}{2E_1(2\pi)^3} \frac{d^3p_2}{2E_2(2\pi)^3} \frac{d^3p_3}{2E_3(2\pi)^3} \frac{1}{2(2\pi)^3} |M|^2$$

$$\rightarrow f_1(p_1^\mu) f_2(p_2^\mu) (1 \pm f_3(p_3^\mu)) (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p_3 - q)$$

With

$$f(p^\mu) = \frac{\Gamma_0(q, T) + a_{\mu\nu} \Gamma^{\mu\nu}(q, T)}{e^{\beta(p^\mu u_\mu)} \pm 1} \chi \frac{p^\sigma}{T}$$

We can expand $\Gamma^{\mu\nu}$ calculated in fluid local rest frame and the thermal equilibrium:

$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\pi^{\mu\nu} \hat{q}_\mu \hat{q}_\nu}{2(e+p)} a_{\alpha\beta} \Gamma^{\alpha\beta},$$

$$a_{\mu\nu} = \frac{3}{2(u \cdot \hat{q})^4} \hat{q}_\mu \hat{q}_\nu + \frac{1}{(u \cdot \hat{q})^2} u_\mu u_\nu + \frac{2}{2(u \cdot \hat{q})^2} \dots$$

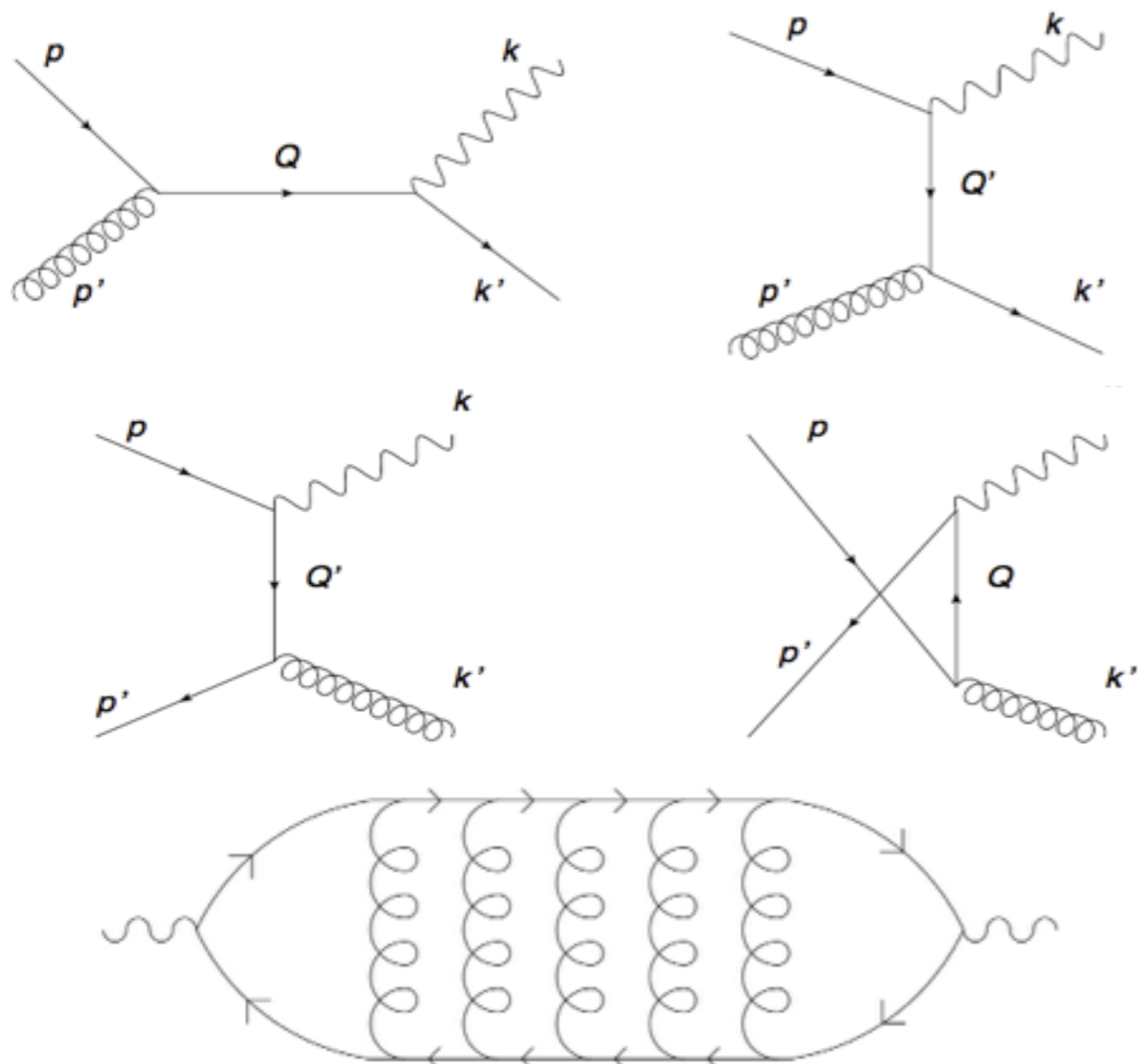
calculated in lab frame

Viscous Photon Emission Rates: General Formalism

$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\hat{\mu}^{\leftarrow x} \hat{q}_{\mu} \hat{q}_{\leftarrow x}}{2(e + p)} a_{\leftarrow \beta} \Gamma^{\leftarrow \beta}$$

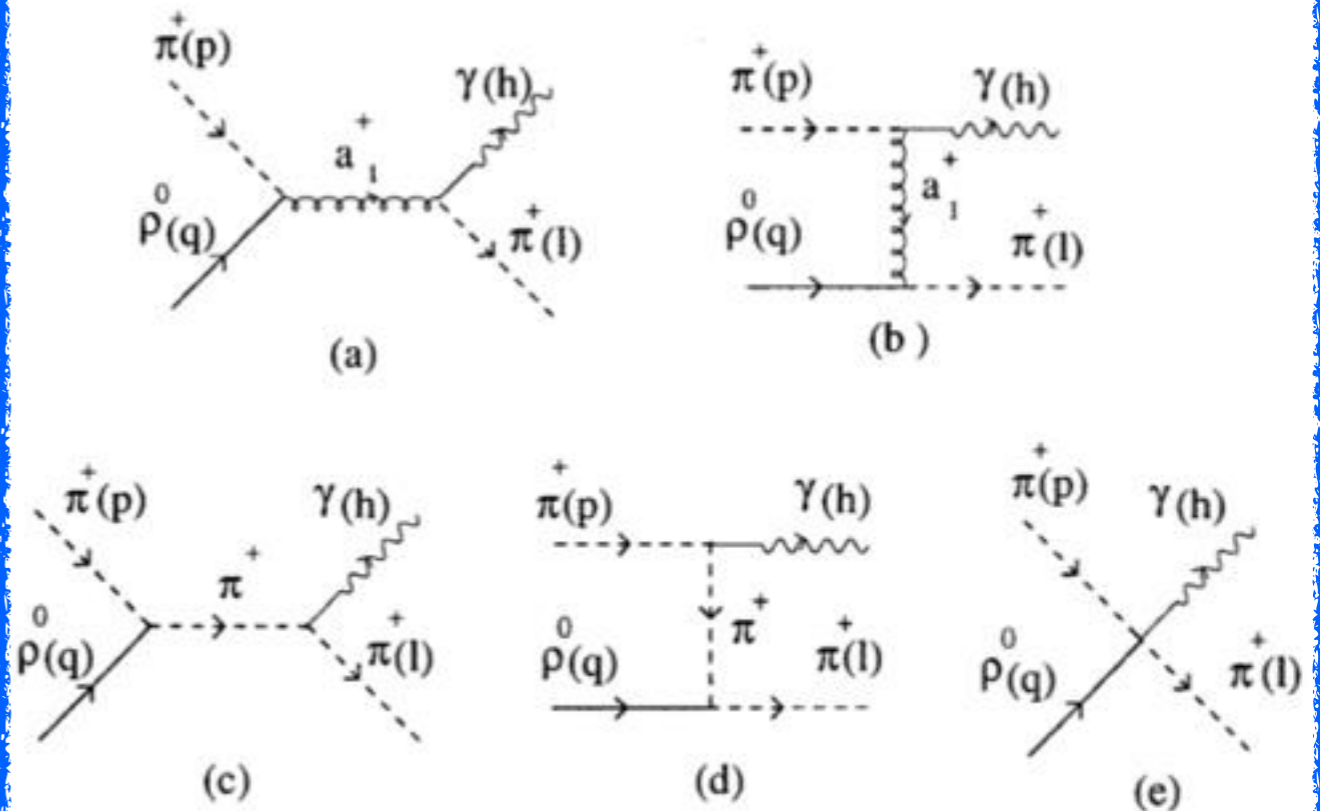
Equilibrium rates

QGP (AMY 2001)



Hadron Gas

(TRG 2004)



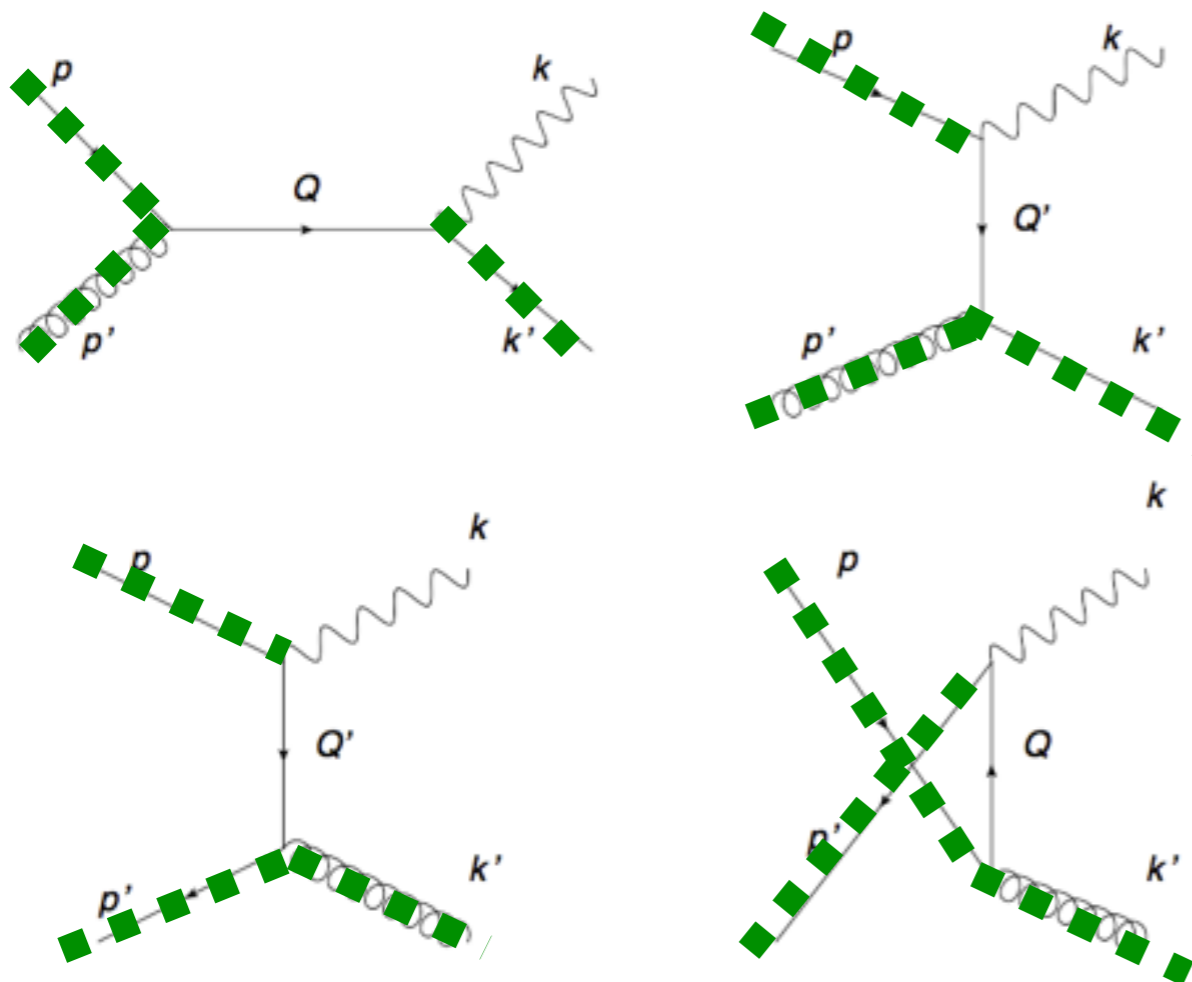
Viscous Photon Emission Rates: General Formalism

$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\hat{\mu}^{\leftarrow \alpha} \hat{q}_\mu \hat{q}_\nu}{2(e + p)} a_{\leftarrow \beta} \Gamma^{\leftarrow \beta}$$

Equilibrium rates

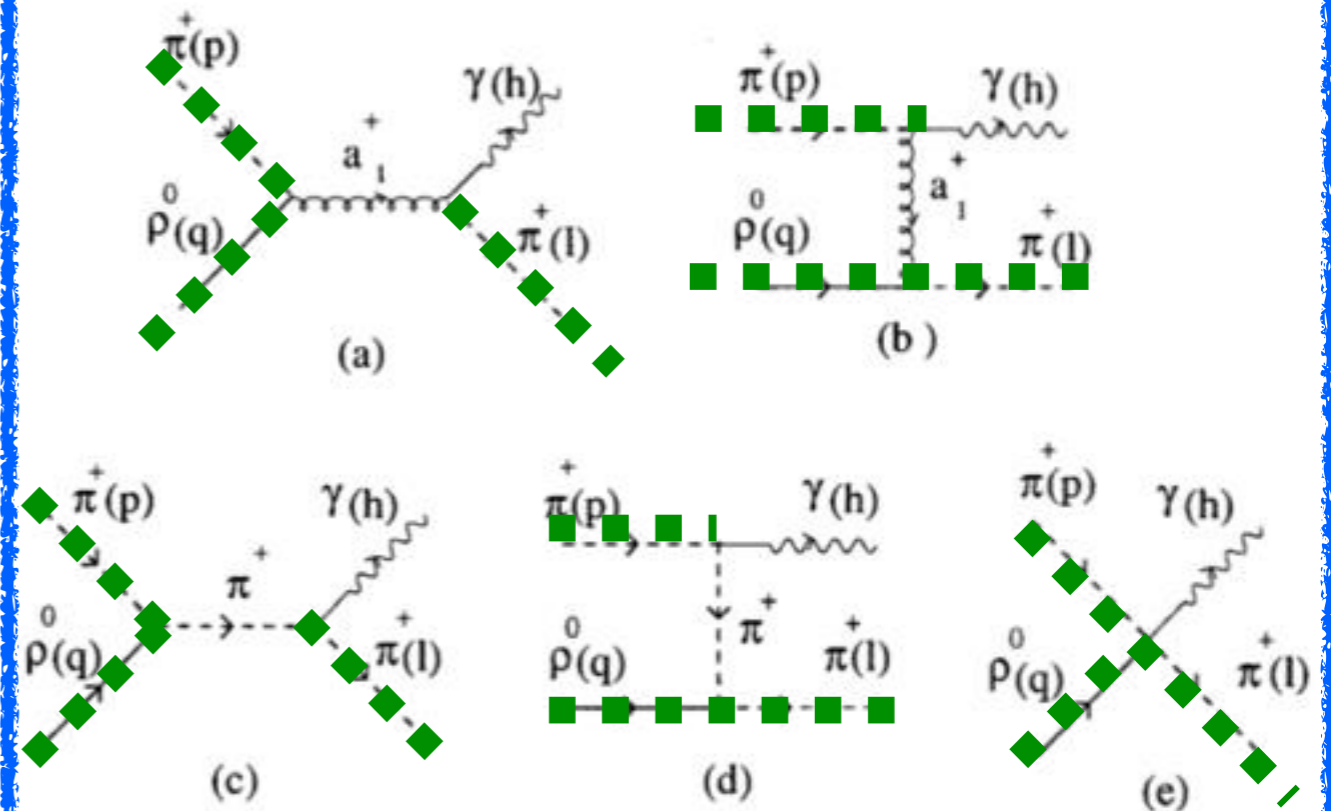
off-equilibrium δf corrections

QGP



Dusling NPA839 (2010) 70

Hadron Gas



Dion et al. PRC84 (2011) 064901

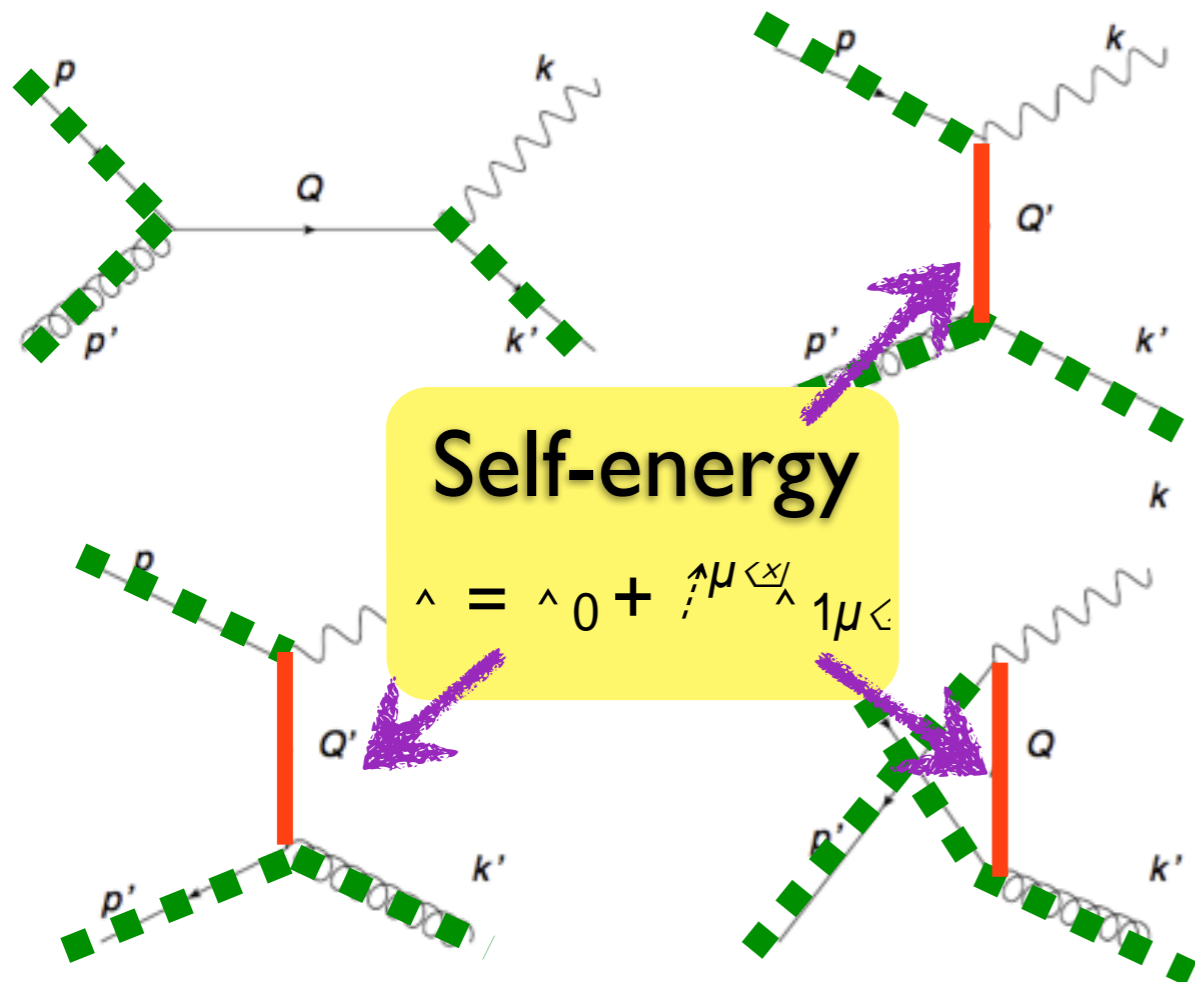
Viscous Photon Emission Rates: General Formalism

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Equilibrium rates

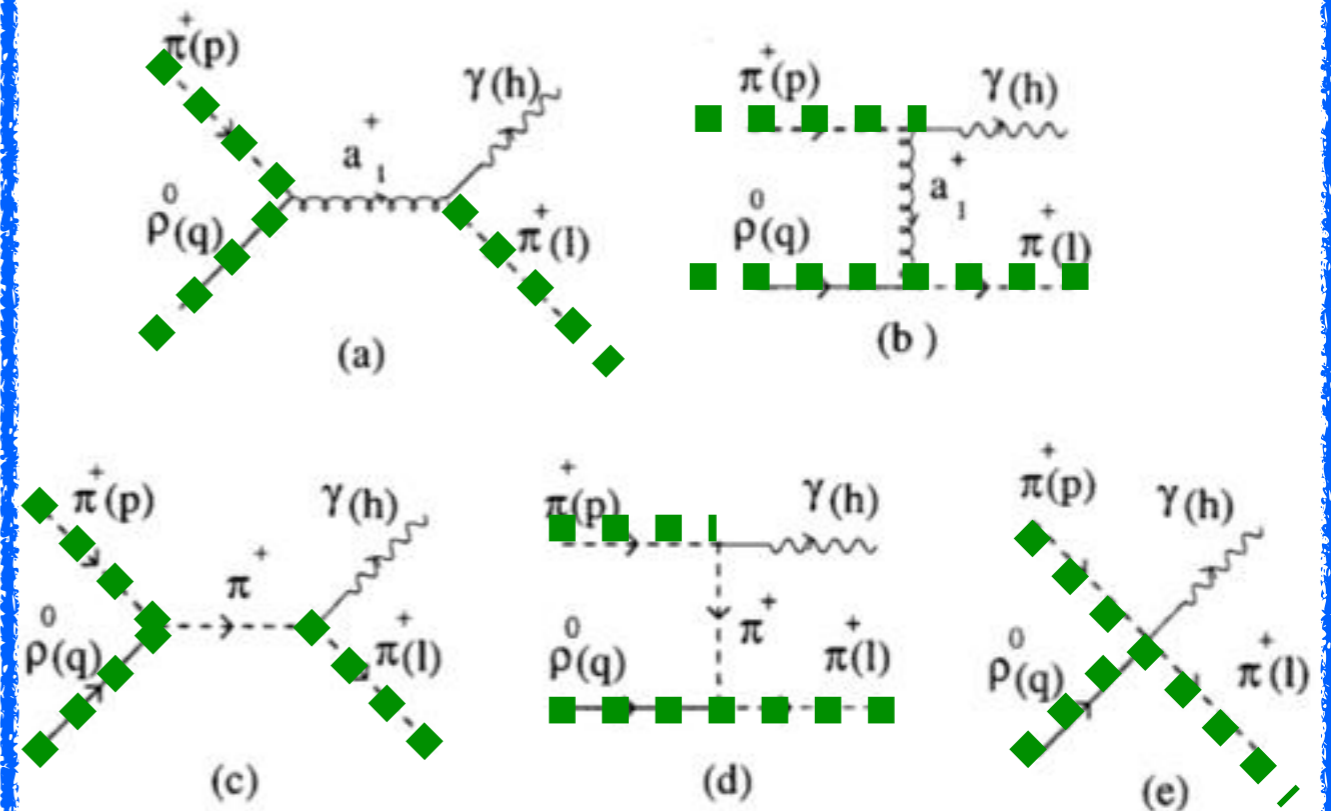
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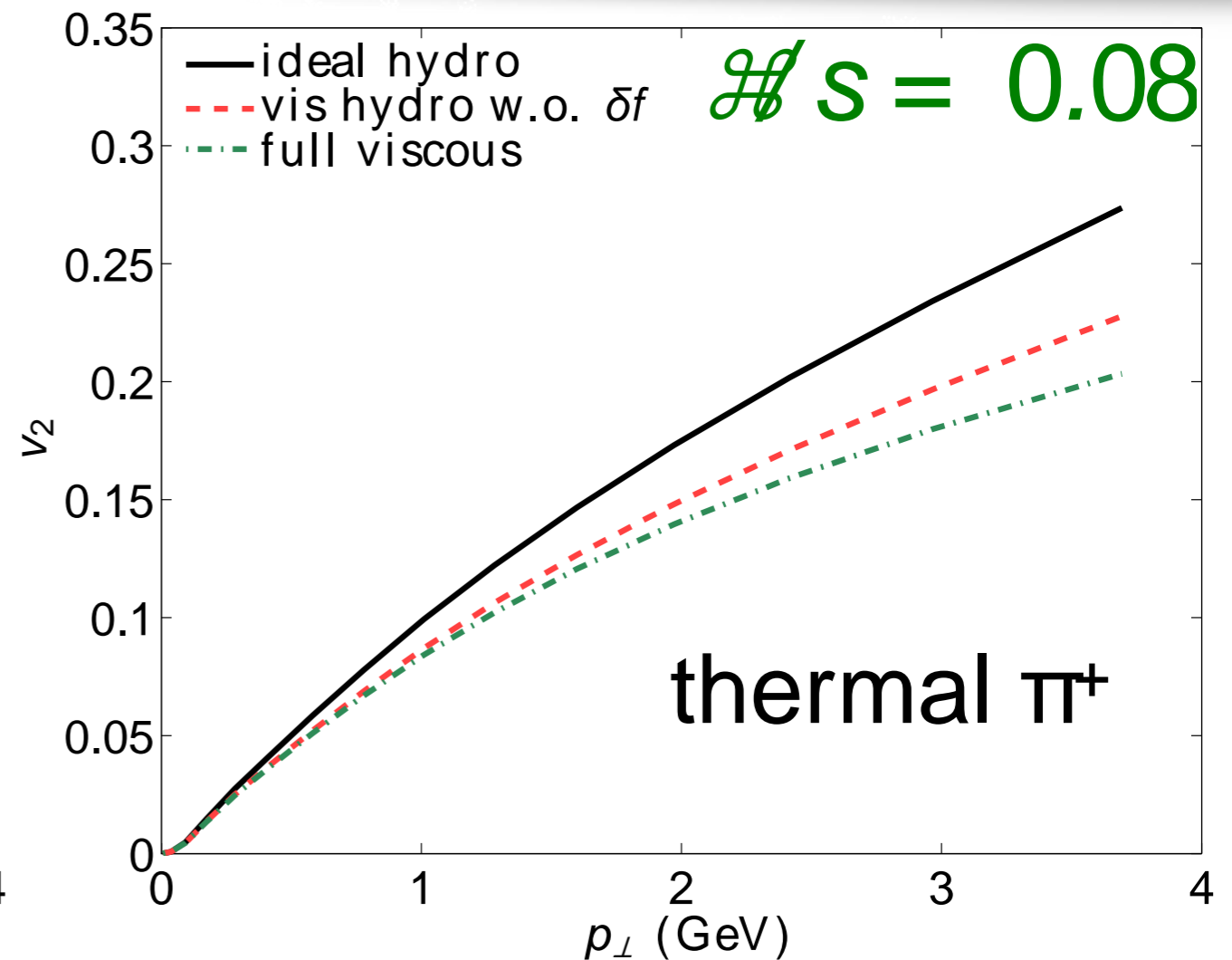
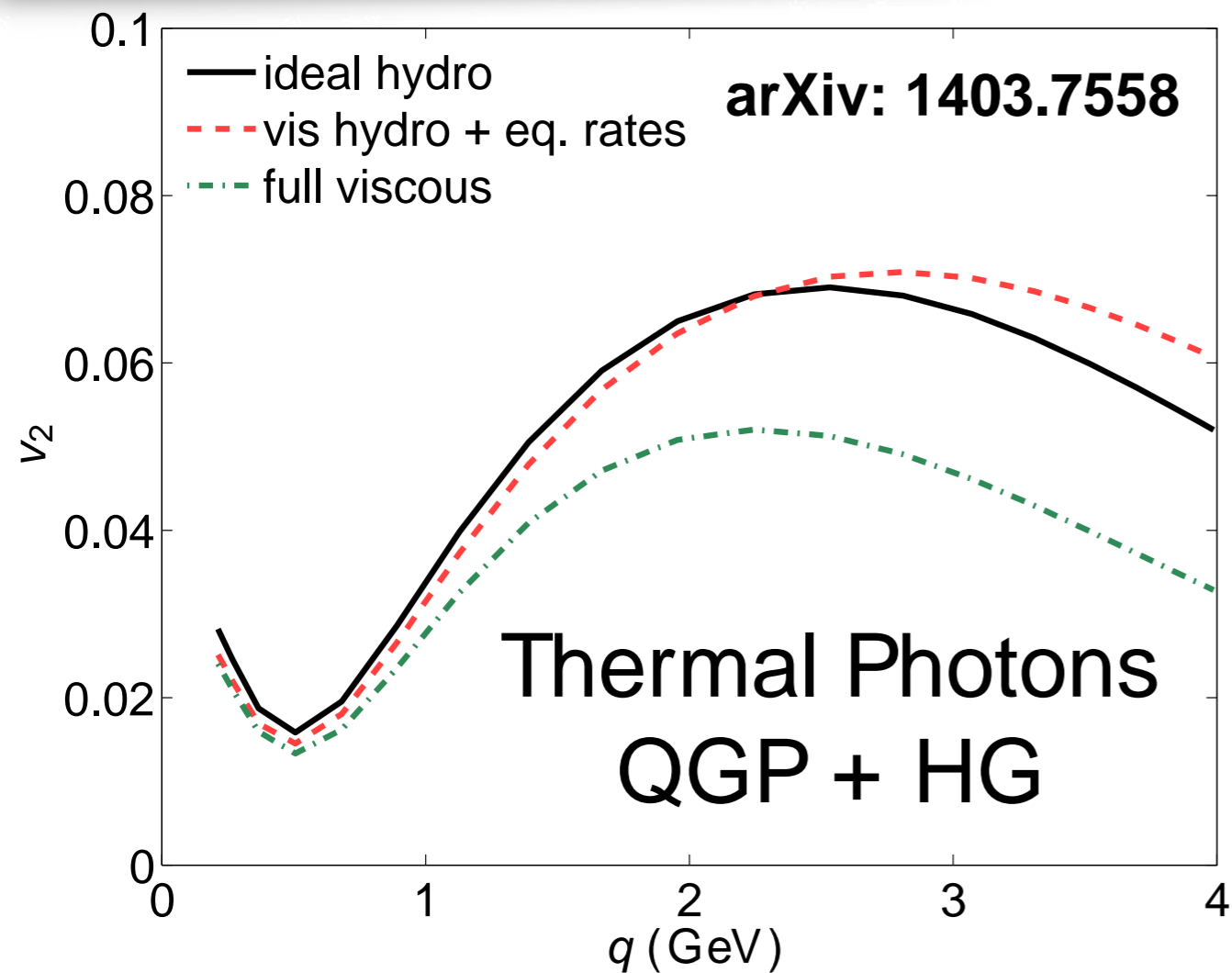


Shen, Paquet et al. (2014)

Hadron Gas

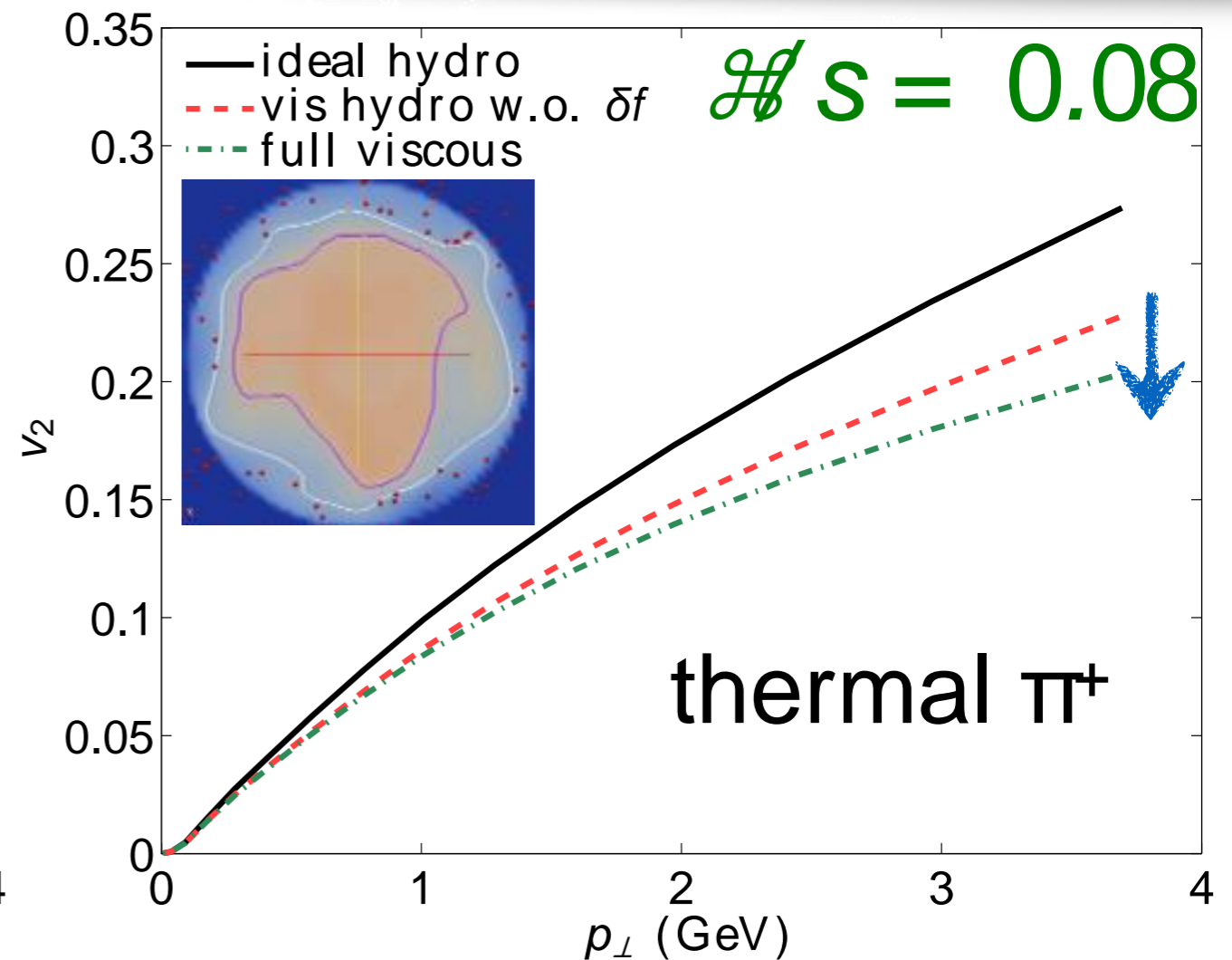
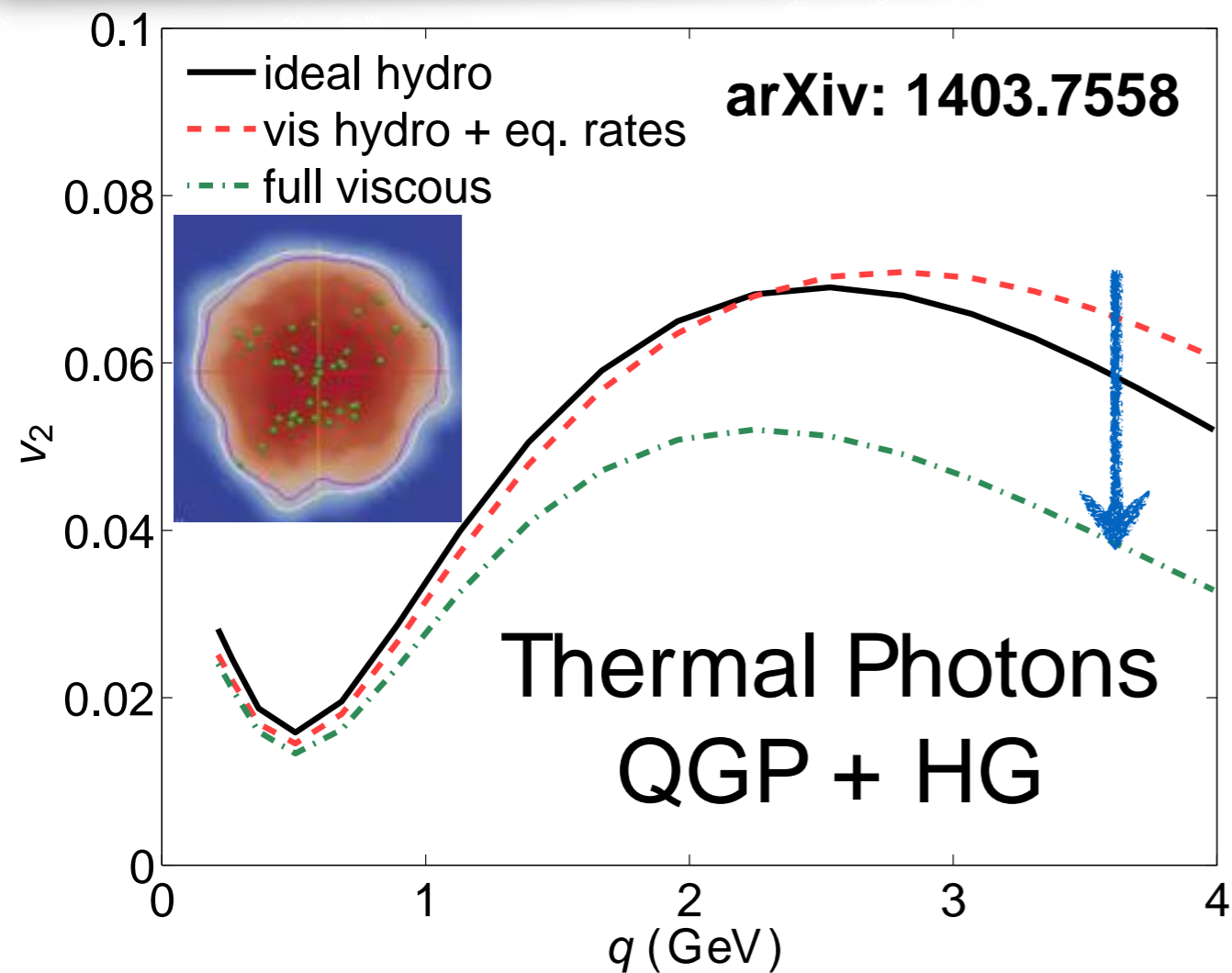


Viscous effects on photon elliptic flow



- Shear viscous suppression of photon v_2 is dominated by the viscous corrections to the photon emission rate
- Photon elliptic flow is sensitive to the larger shear stress tensor at early times

Viscous effects on photon elliptic flow



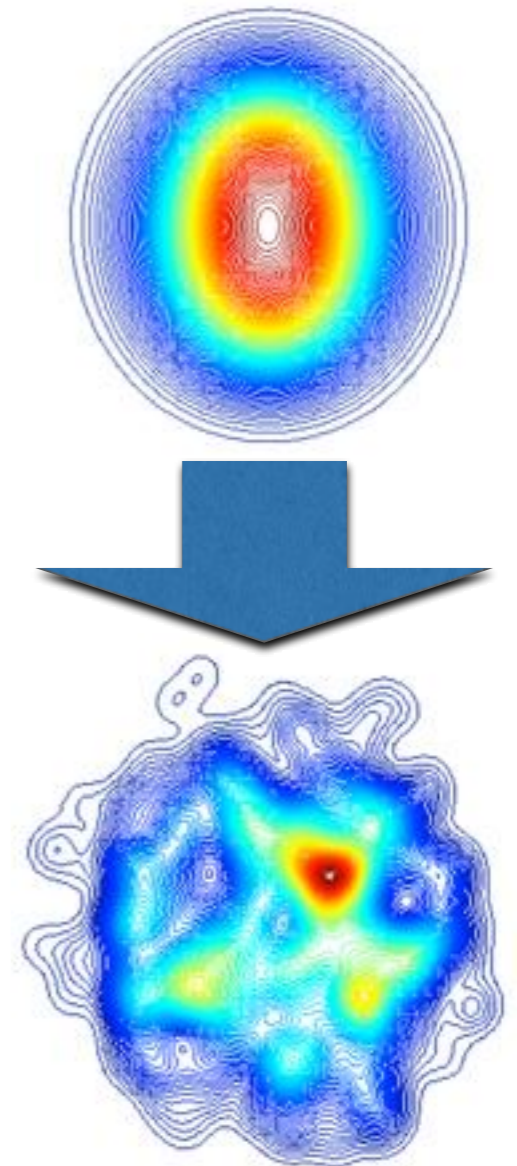
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Definition of event-by-event $v_n^{Y,dir}$

$$v_n^{dir}(p_T) = \frac{R^Y(p_T) v_n^{incl}(p_T) - v_n^{bg}(p_T)}{R^Y(p_T) - 1}$$

$$R^Y = \frac{N^{Yincl}}{N^{Ybg}}$$

exact for a single event



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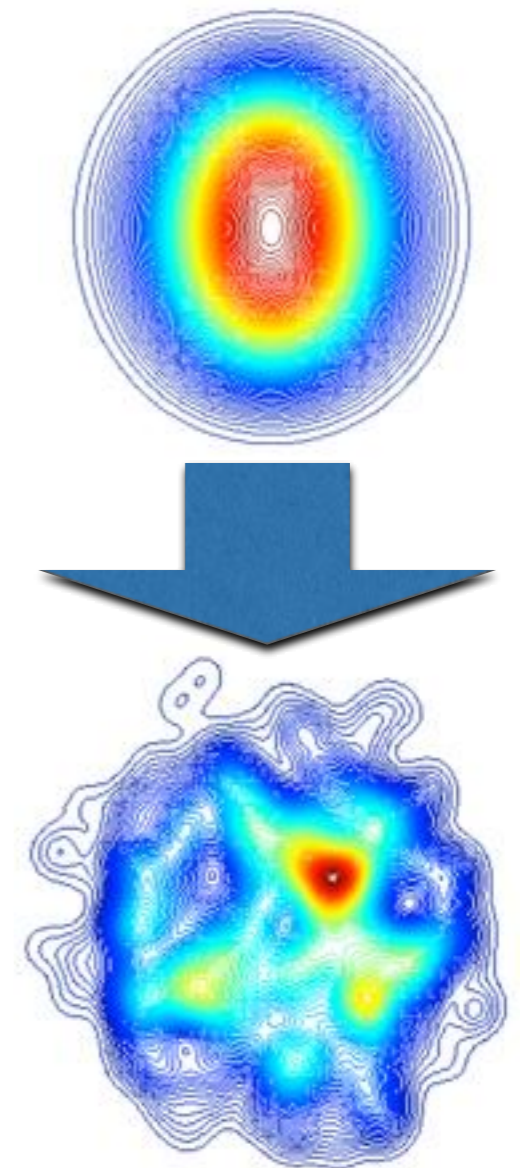
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exact for a single event

But for **multiple** events,

Experiment:
$$\frac{R^Y(p_T) \langle h v_n^{incl}(p_T) \rangle - \langle h v_n^{bg}(p_T) \rangle}{R^Y(p_T) - 1}$$

$$\bar{R}^Y(p_T) = \frac{\langle h dN^{Yincl} / dy p_T dp_T \rangle}{\langle h dN^{Ybg} / dy p_T dp_T \rangle}$$



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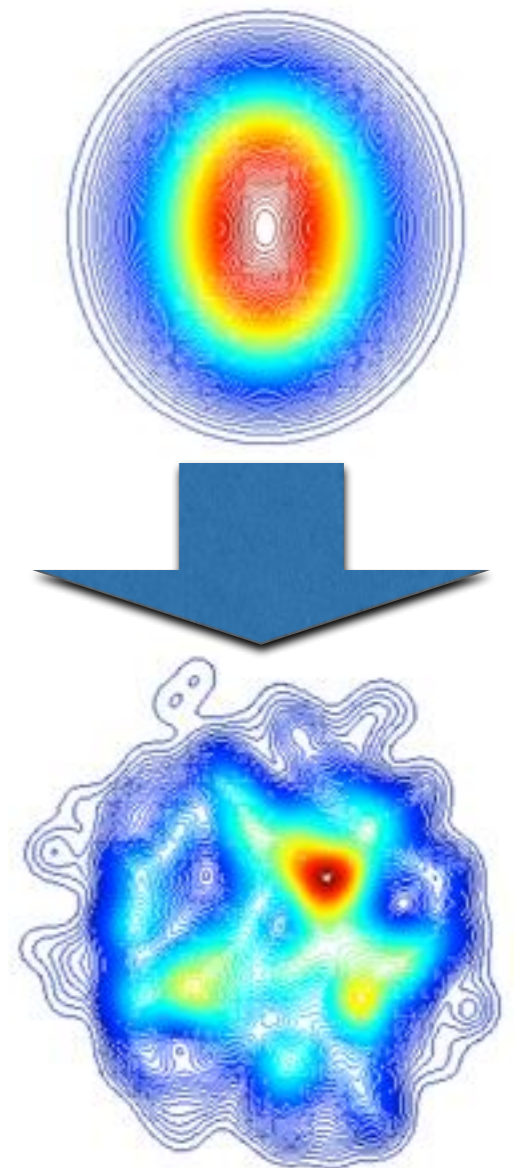
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Theory:
$$\langle h v_n^{dir}(p_T) \rangle = \left\langle \frac{R^Y(p_T) v_n^{incl}(p_T) - v_n^{bg}(p_T)}{R^Y(p_T) - 1} \right\rangle$$



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$$v_n^{dir}(p_T) = \frac{R^Y(p_T) v_n^{incl}(p_T) - v_n^{bg}(p_T)}{R^Y(p_T) - 1}$$

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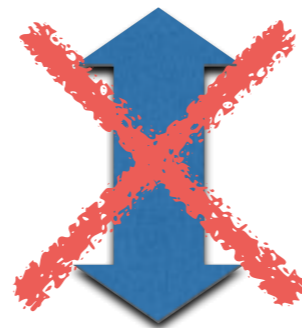
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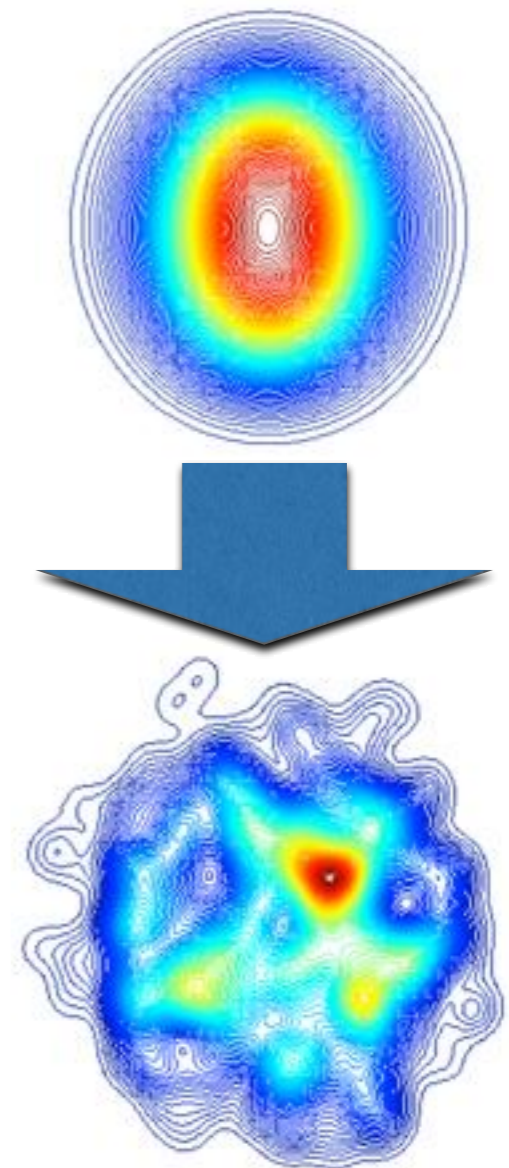
Experiment:

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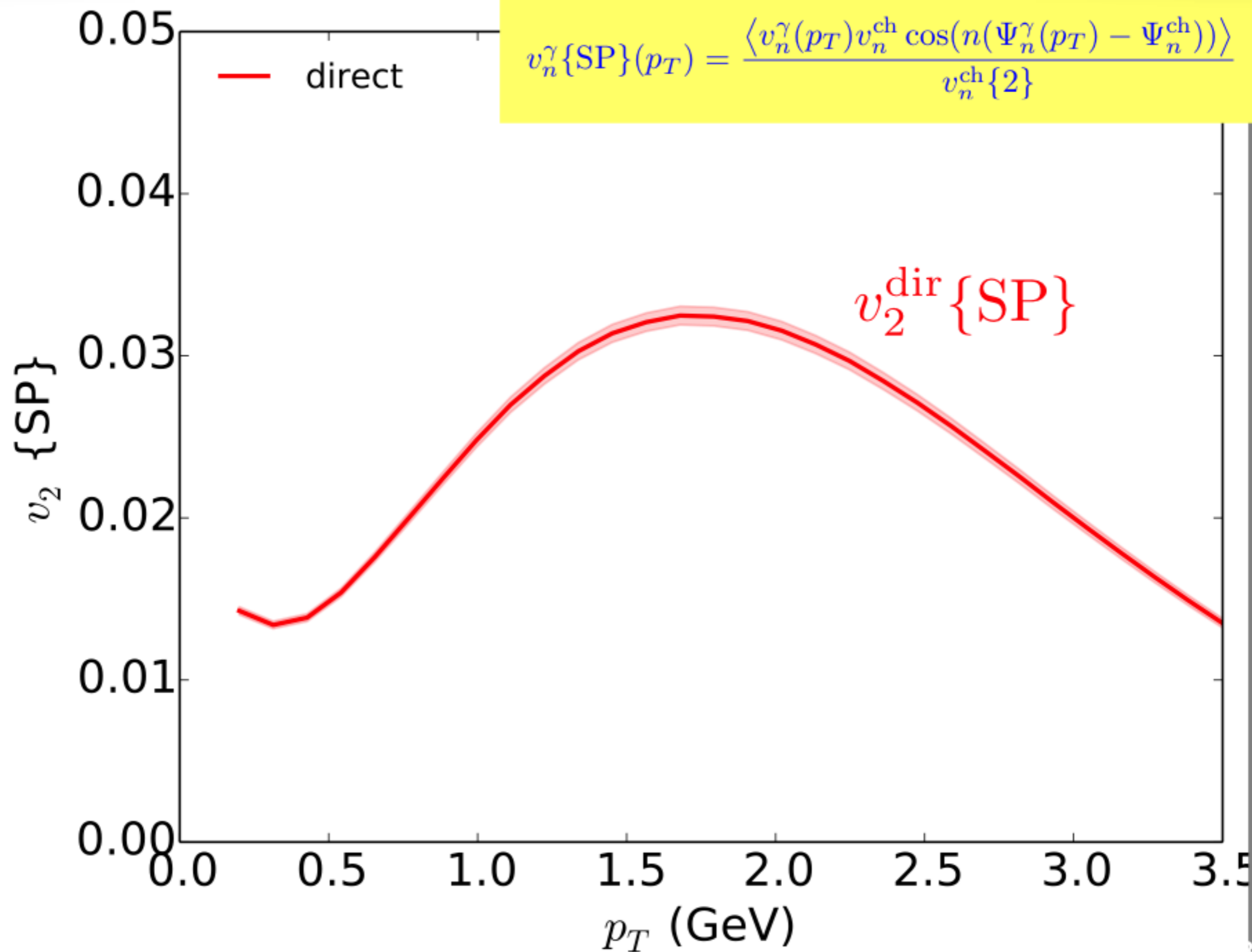
$$\bar{R}^Y(p_T) = \frac{\langle dN^{Yincl} / dy p_T dp_T \rangle}{\langle dN^{Ybg} / dy p_T dp_T \rangle}$$



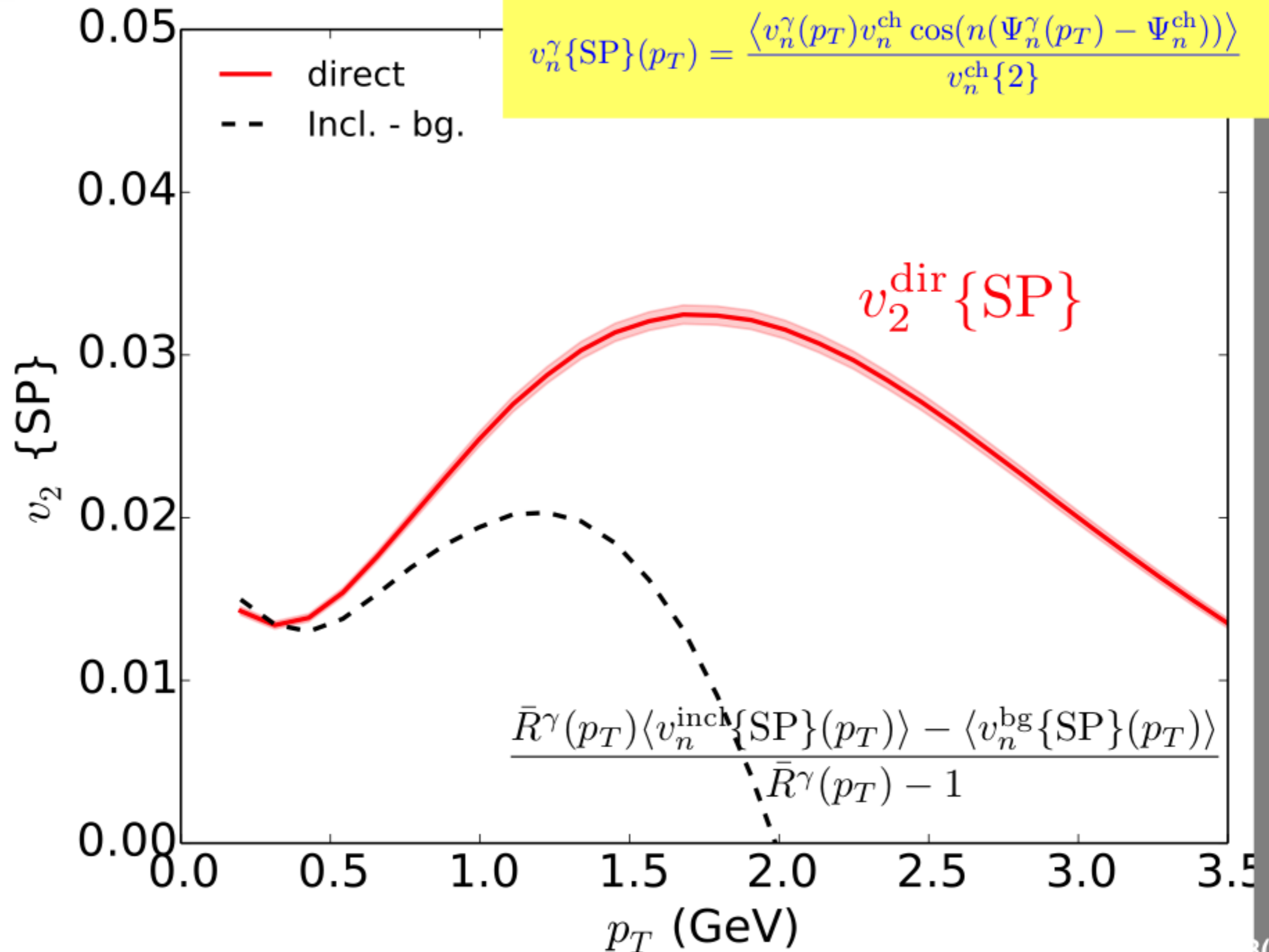
Theory: $\langle v_n^{dir}(p_T) \rangle = \left\langle \frac{R^Y(p_T) v_n^{incl}(p_T) - v_n^{bg}(p_T)}{R^Y(p_T) - 1} \right\rangle$



Definition of event-by-event $v_n^{\gamma, \text{dir}}$



Definition of event-by-event $v_n^{\gamma, \text{dir}}$



Definition of event-by-event $v_n^{Y,dir}$

$$v_n^{dir}(p_T) = \frac{R^Y(p_T) v_n^{incl}(p_T) - v_n^{bg}(p_T)}{R^Y(p_T) - 1} \quad R^Y = \frac{N^{Yincl}}{N^{Ybg}}$$

exact for a single event

But for **multiple** events,

“**extraction safe**”

$$v_n^Y\{SP\}(p_T) = \frac{\overline{\frac{dN^Y}{dy p_T dp_T}(p_T) v_n^Y(p_T) v_n^{ch} \cos(n(\phi_n^Y(p_T) - \phi_n^{ch}))}}{\overline{\frac{dN^Y}{dy p_T dp_T}(p_T) v_n^{ch}\{2\}}}$$

$$v_n^{dir}\{SP\}(p_T) = \frac{R^Y(p_T) \overline{h v_n^{incl}\{SP\}(p_T) i} - \overline{h v_n^{bg}\{SP\}(p_T) i}}{R^Y(p_T) - 1}$$

theory

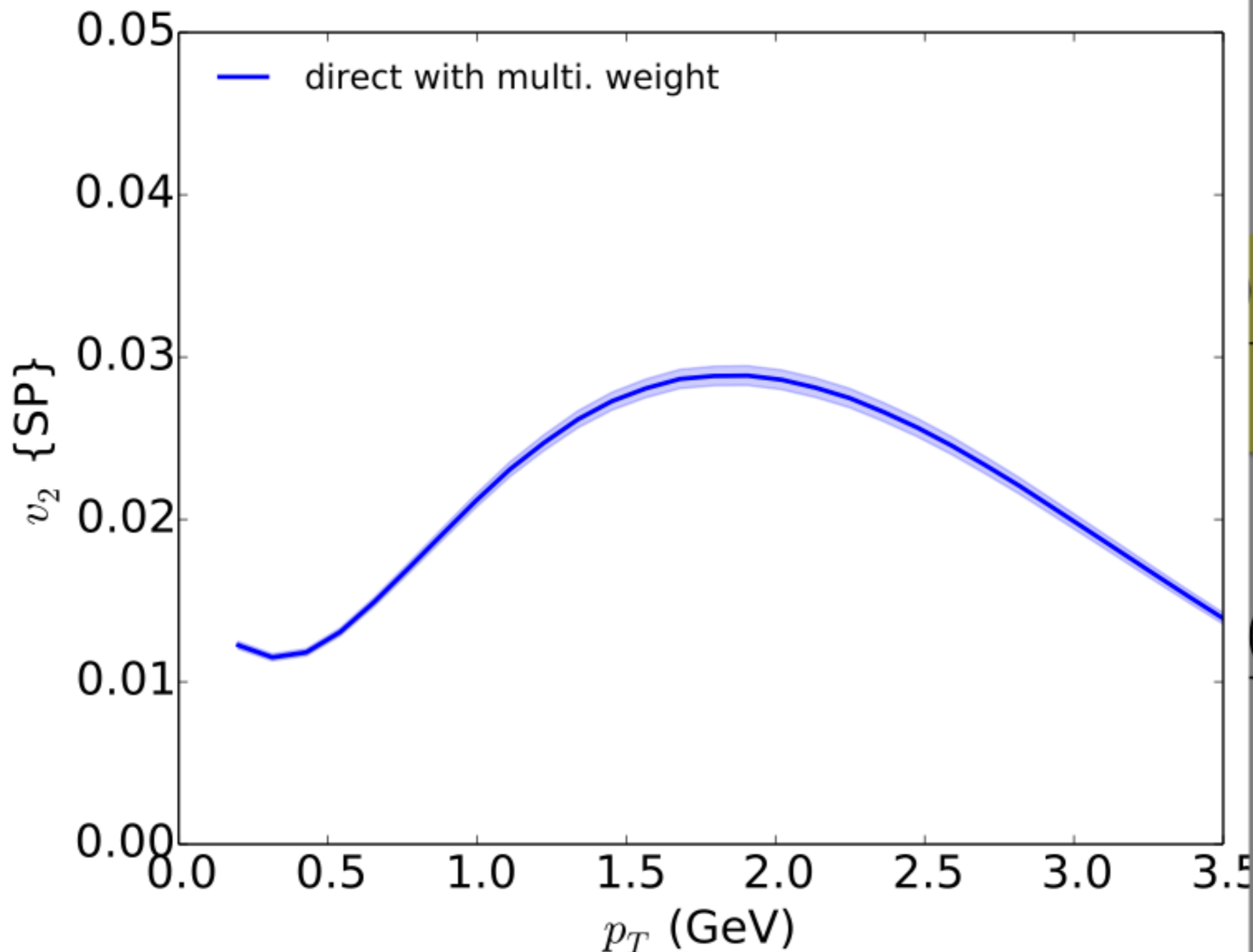


experiment

Poster:!
J-F. Paquet, G21

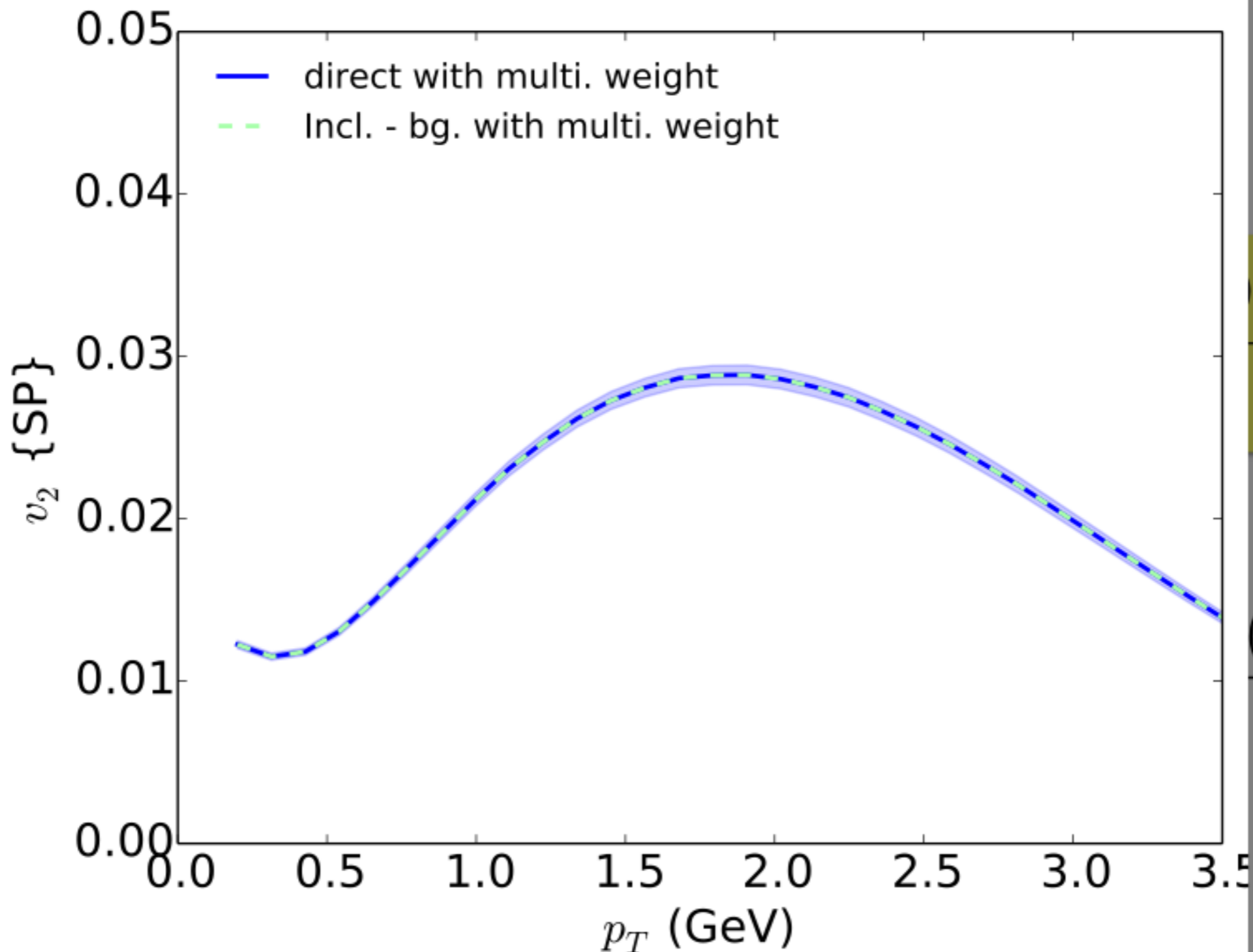
Definition of event-by-event $v_n^{\gamma, \text{dir}}$

$$v_n^{\gamma} \{ \text{SP} \} (p_T) = \frac{\left\langle \frac{dN^{\gamma}}{dy p_T dp_T} (p_T) v_n^{\gamma} (p_T) v_n^{\text{ch}} \cos(n(\Psi_n^{\gamma}(p_T) - \Psi_n^{\text{ch}})) \right\rangle}{\left\langle \frac{dN^{\gamma}}{dy p_T dp_T} (p_T) \right\rangle v_n^{\text{ch}} \{ 2 \}}.$$



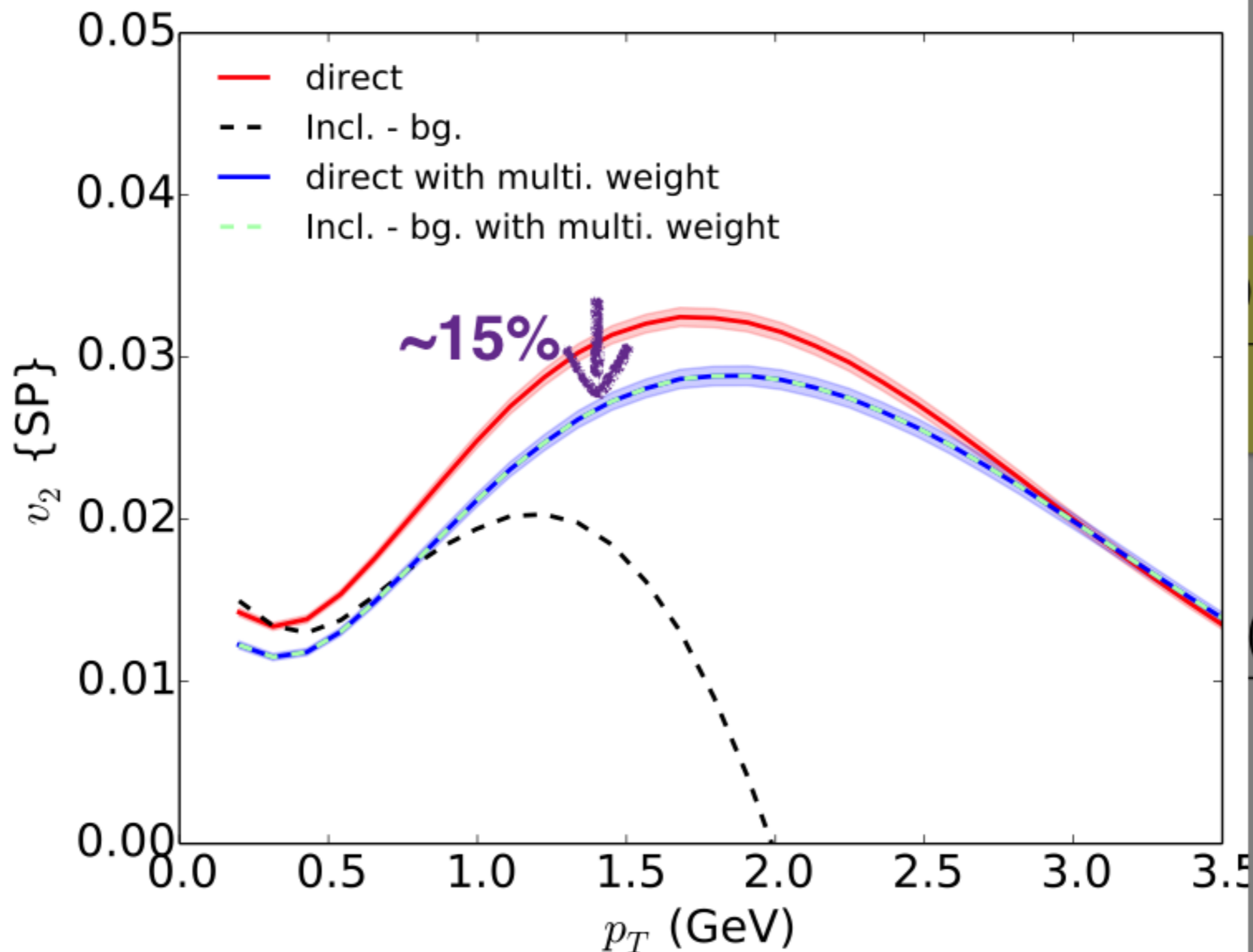
Definition of event-by-event $v_n^{\gamma, \text{dir}}$

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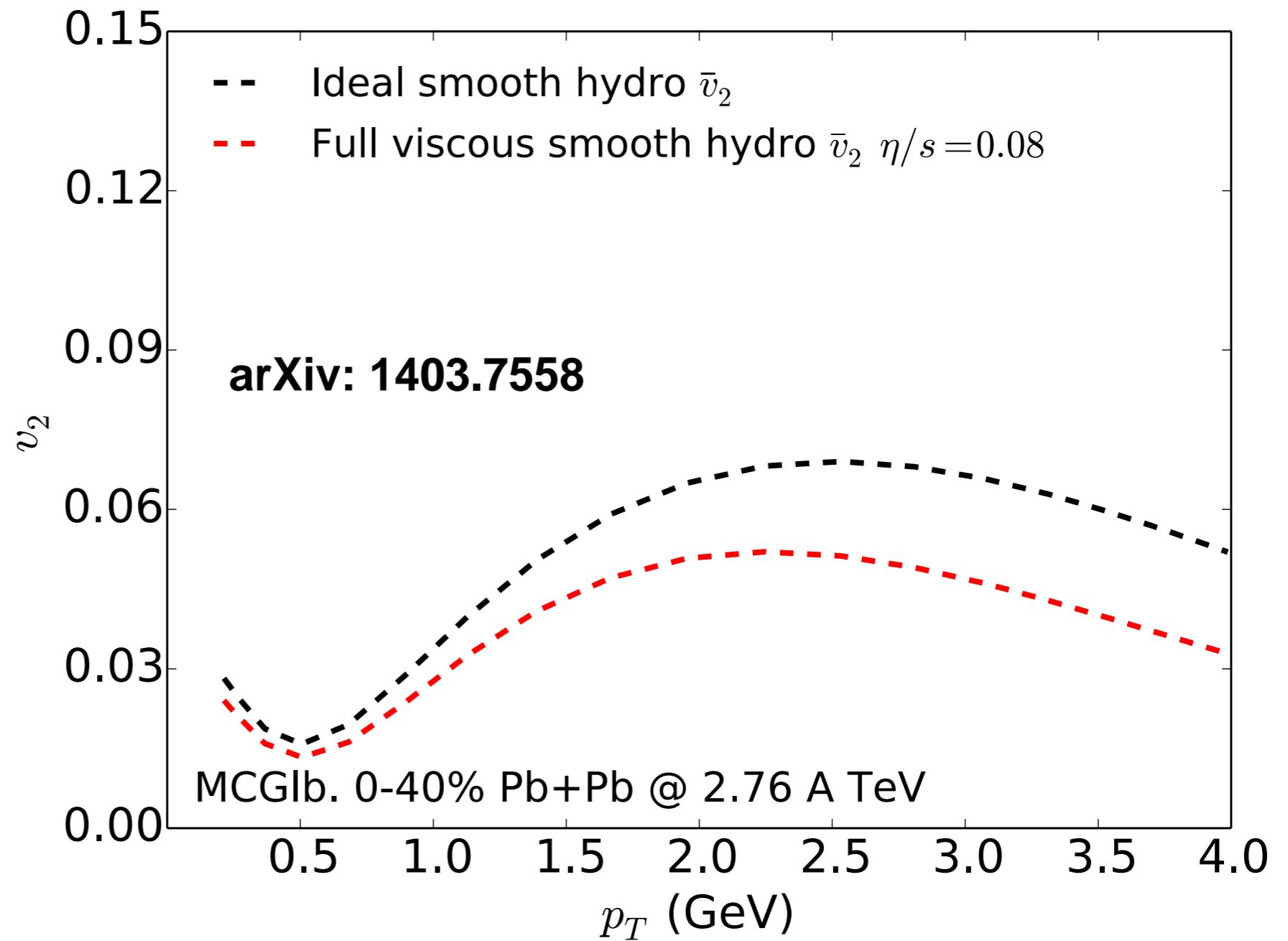
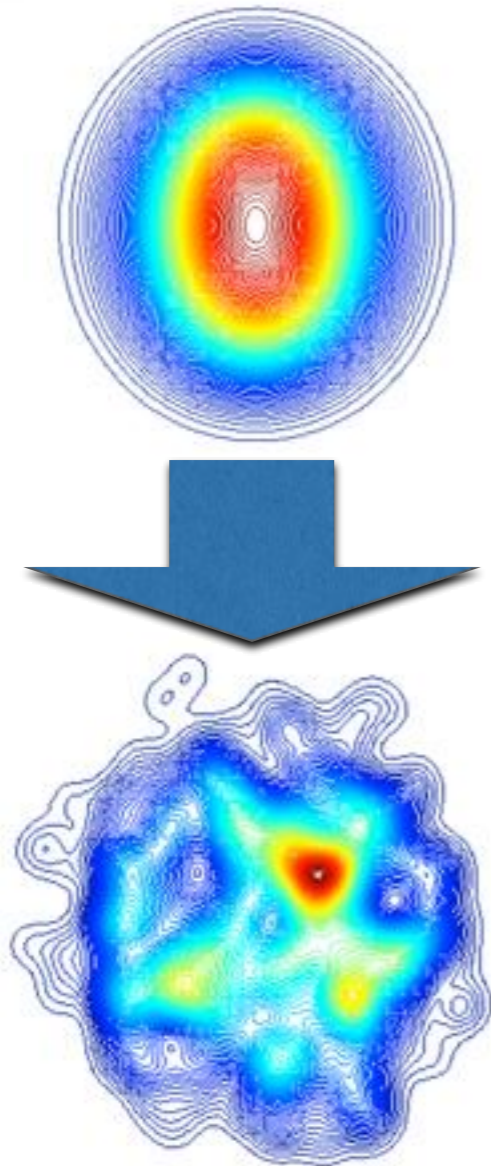


Definition of event-by-event $v_n^{\gamma, \text{dir}}$

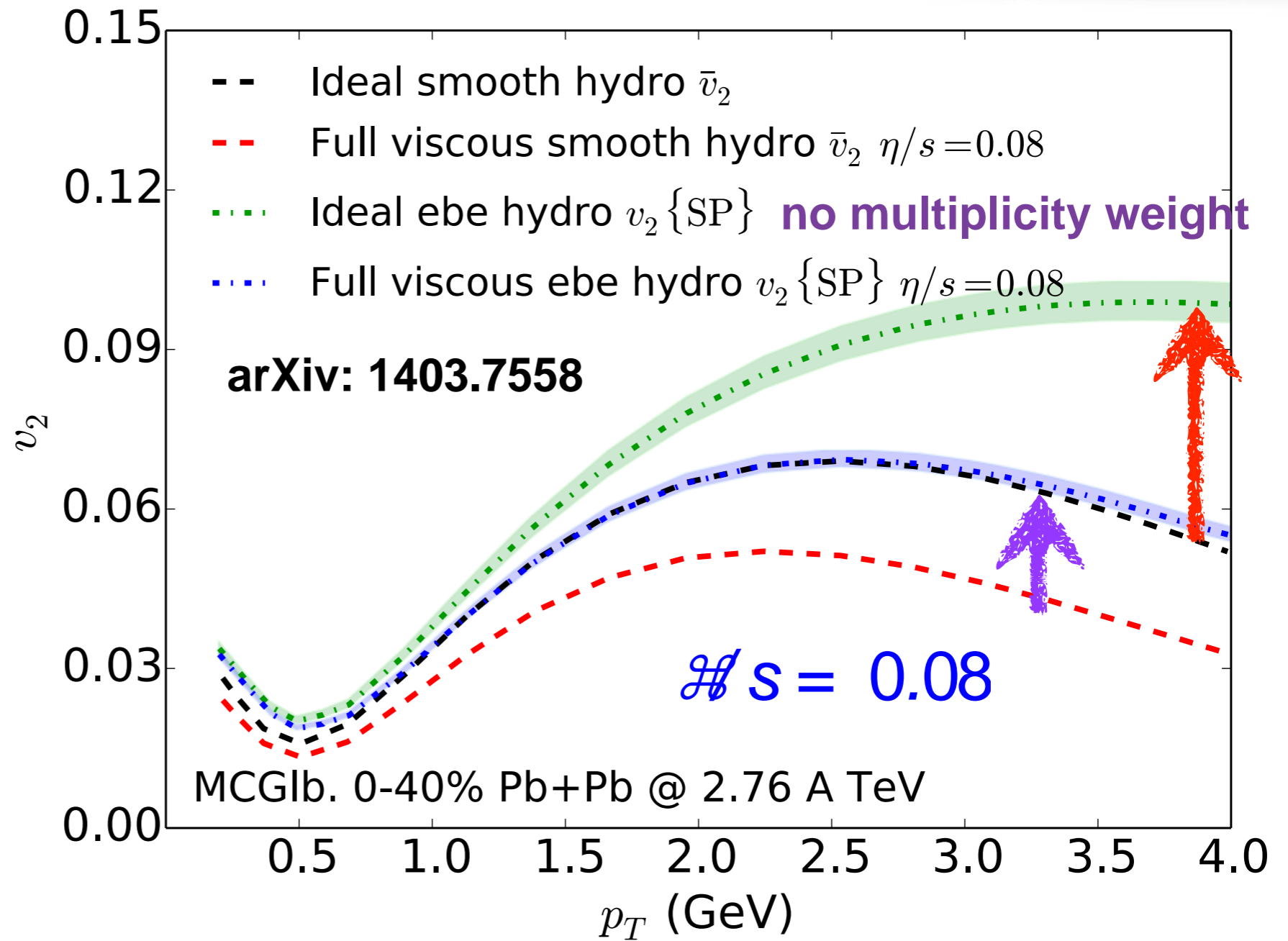
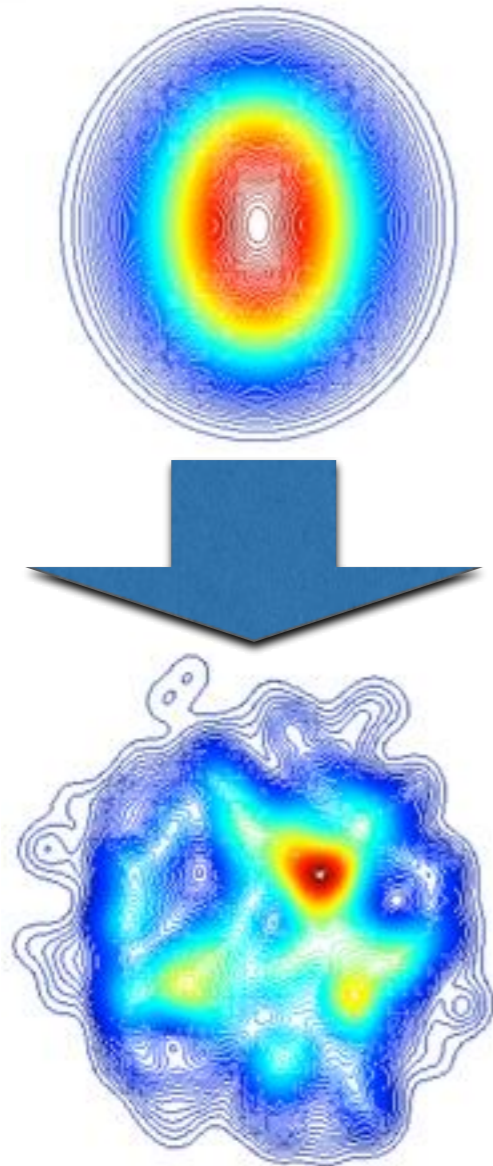
$$v_n^{\gamma \{ \text{SP} \}}(p_T) = \frac{\left\langle \frac{dN^\gamma}{dy p_T dp_T}(p_T) v_n^\gamma(p_T) v_n^{\text{ch}} \cos(n(\Psi_n^\gamma(p_T) - \Psi_n^{\text{ch}})) \right\rangle}{\left\langle \frac{dN^\gamma}{dy p_T dp_T}(p_T) \right\rangle v_n^{\text{ch}} \{2\}}$$



Fluctuation effects on photon elliptic flow

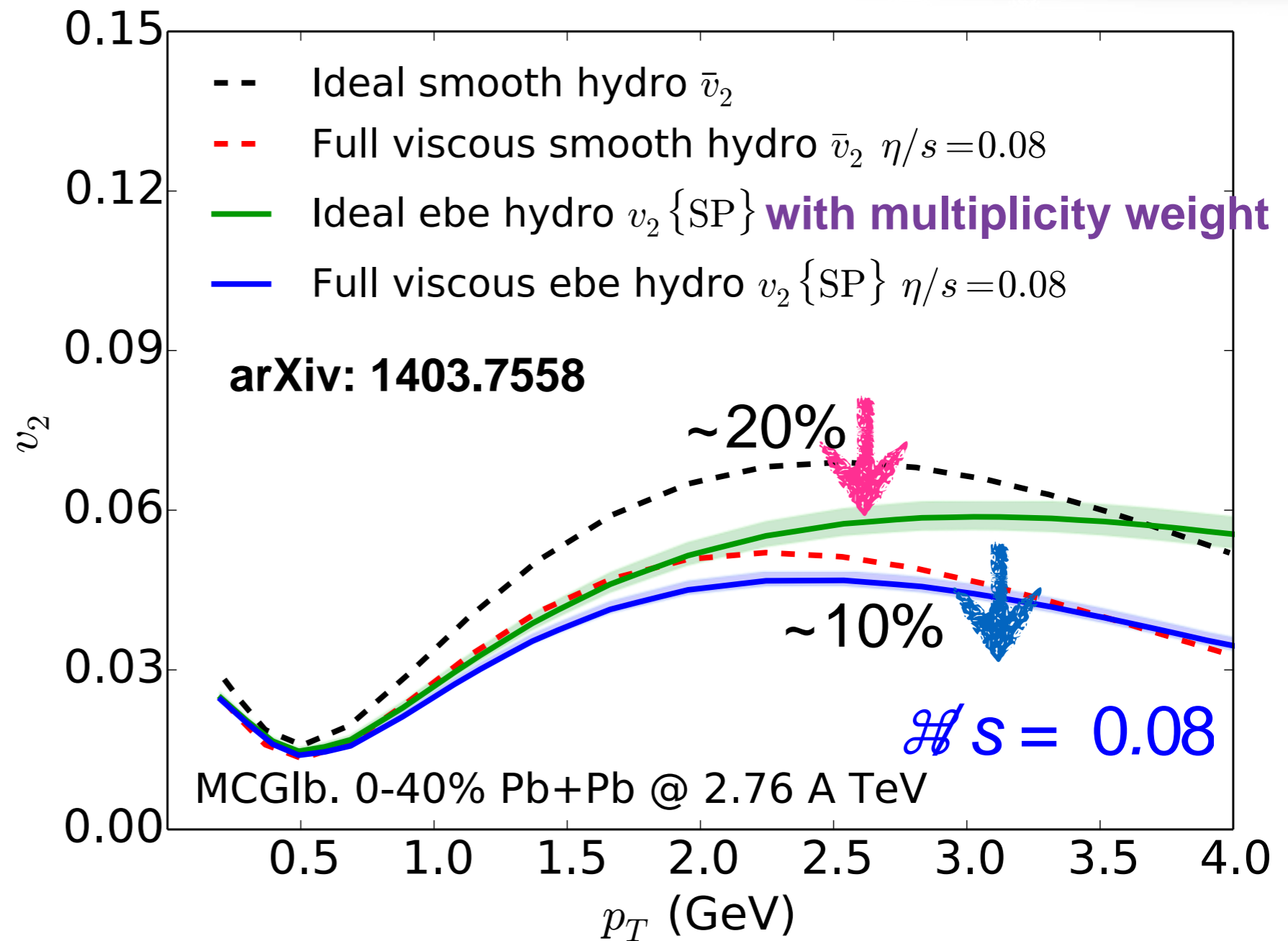
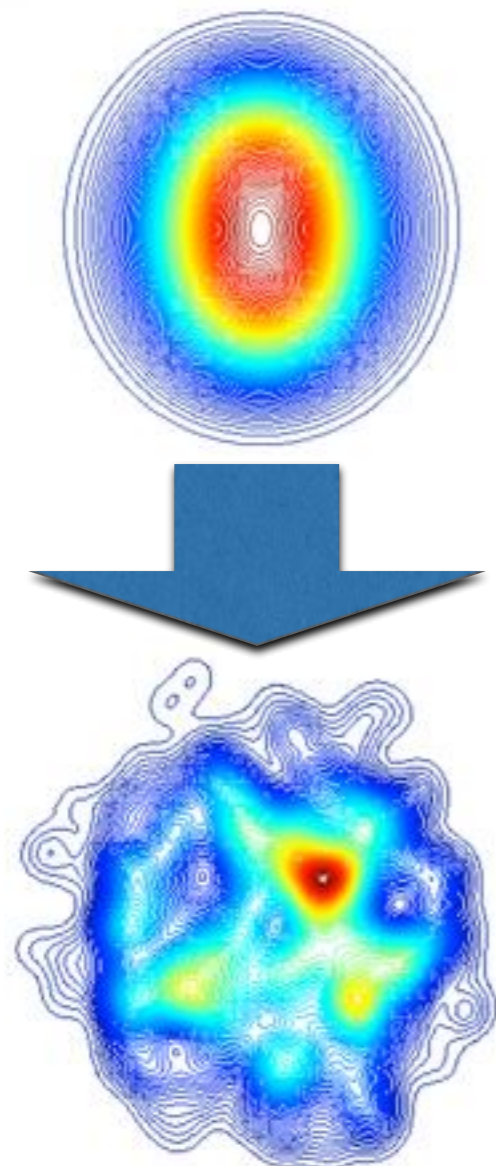


Fluctuation effects on photon elliptic flow



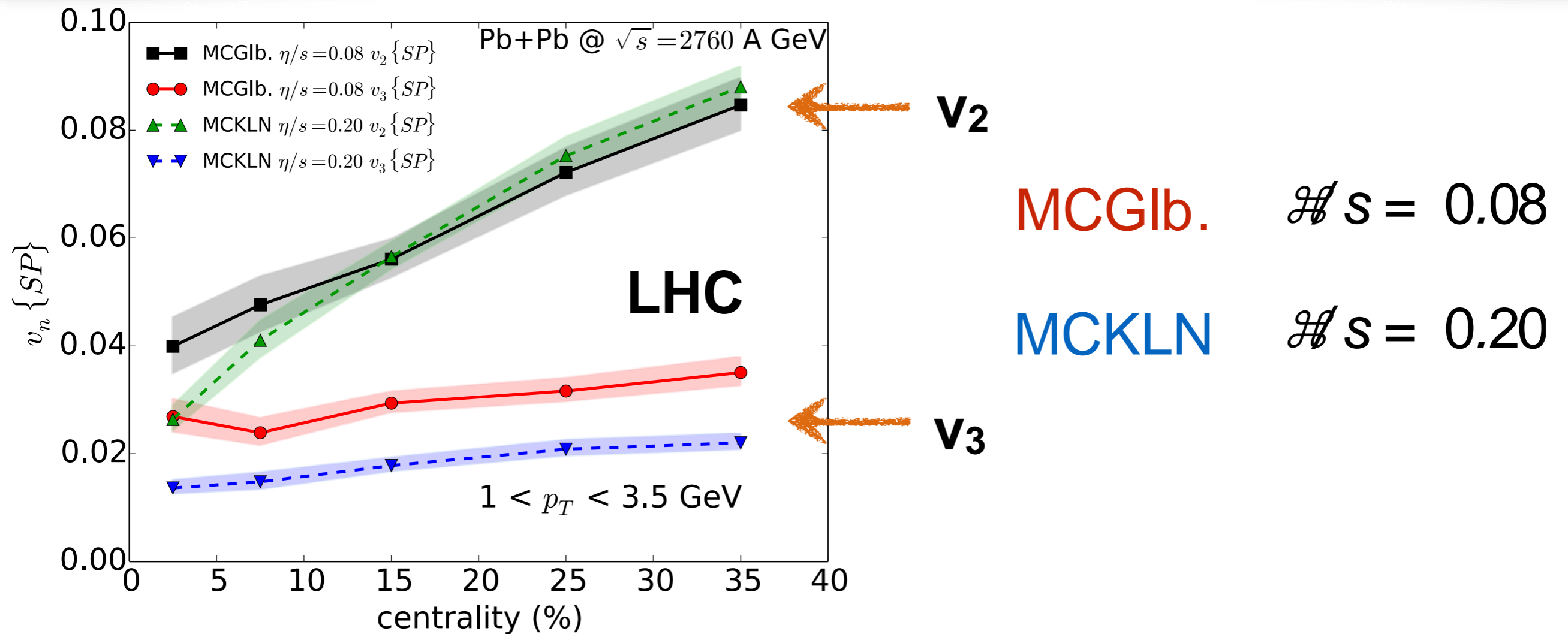
- ▶ Initial fluctuations increase photons' elliptic flow

Fluctuation effects on photon elliptic flow



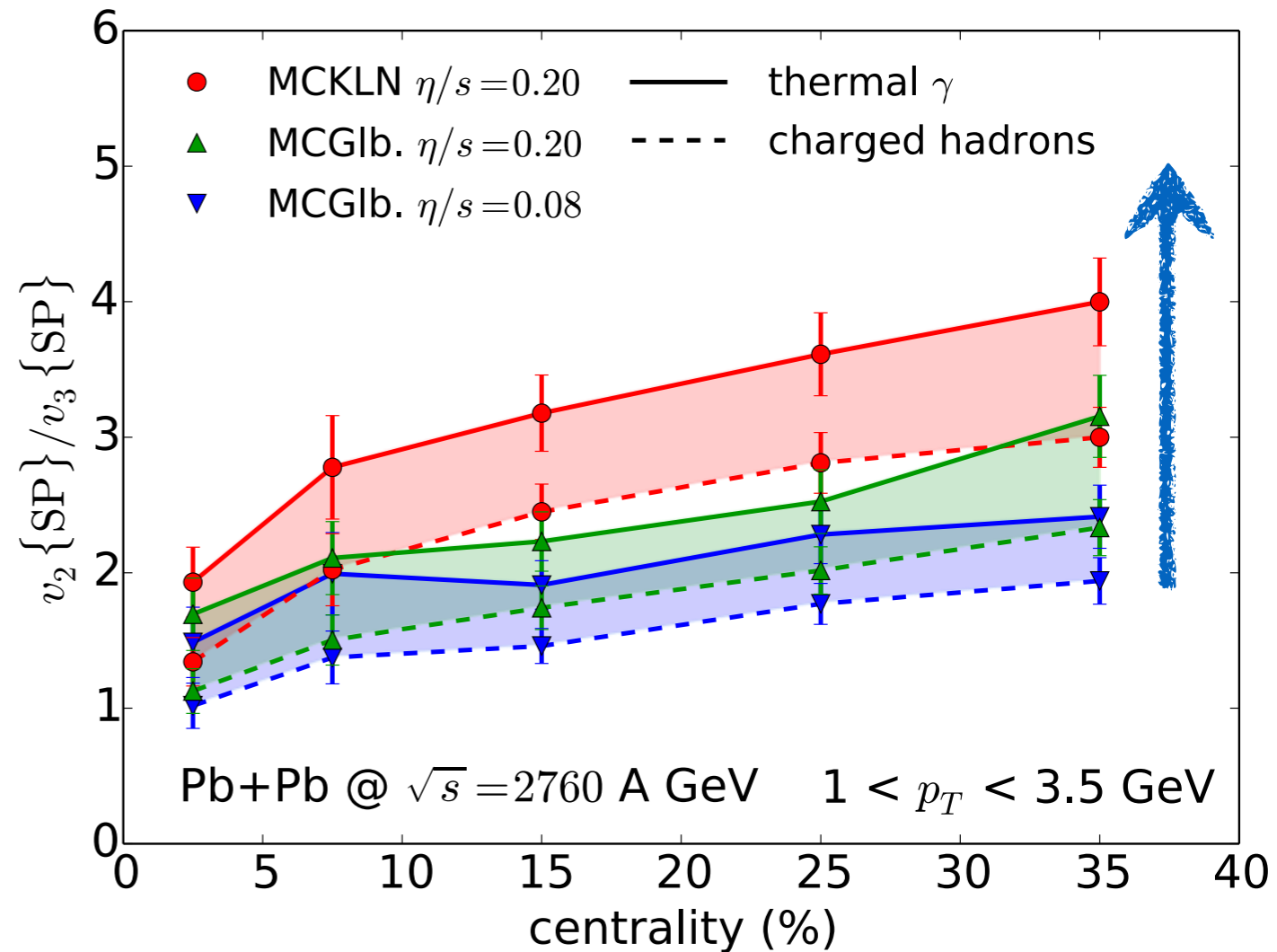
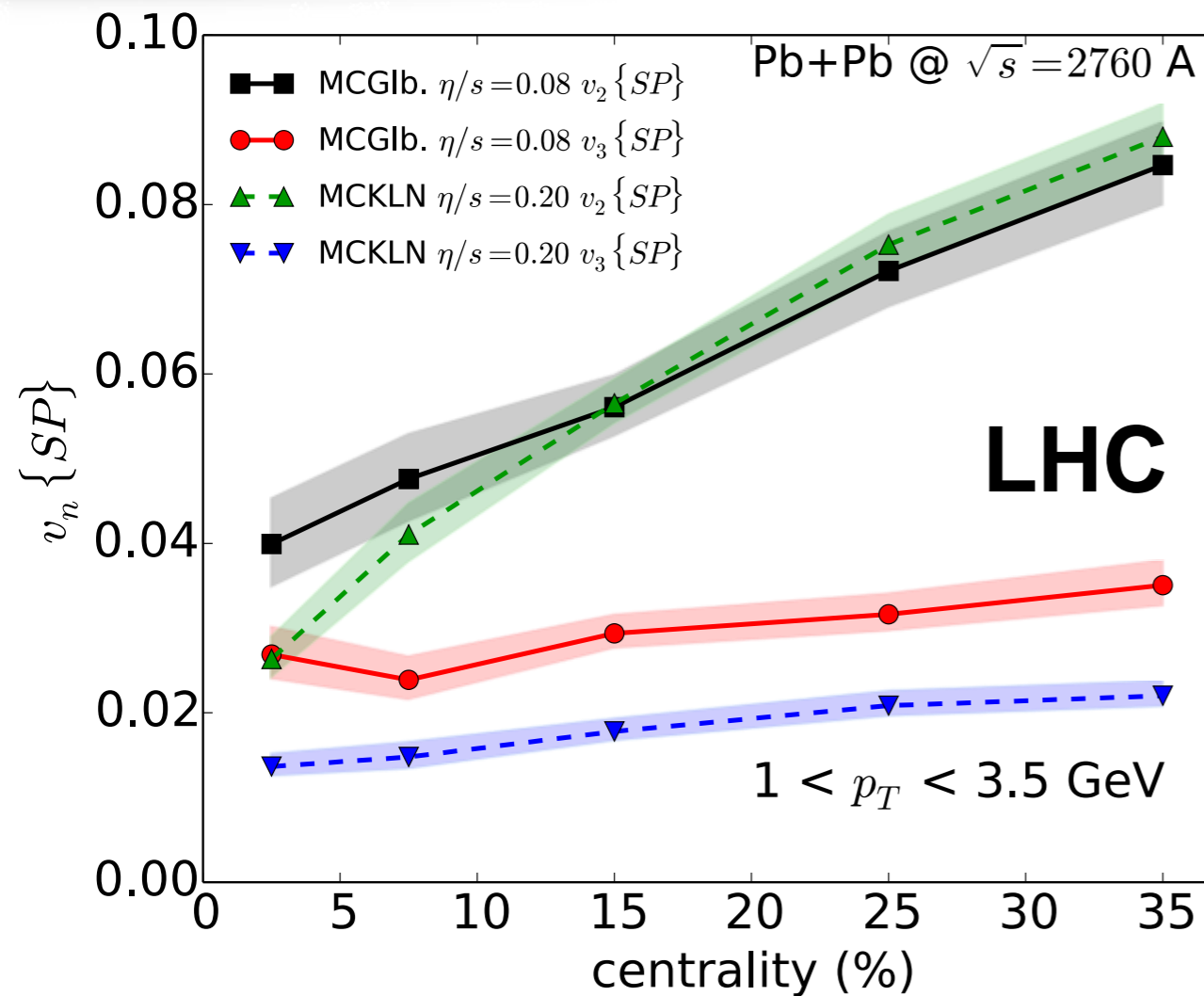
- ▶ Initial fluctuations increase photons' elliptic flow
- ▶ The additional photon multiplicity weighting biases e-b-e v_2 towards central collisions, resulting in ~ 10 - 20% smaller v_2 compared to smooth hydro

Event-by-Event Full Viscous Photon v_n



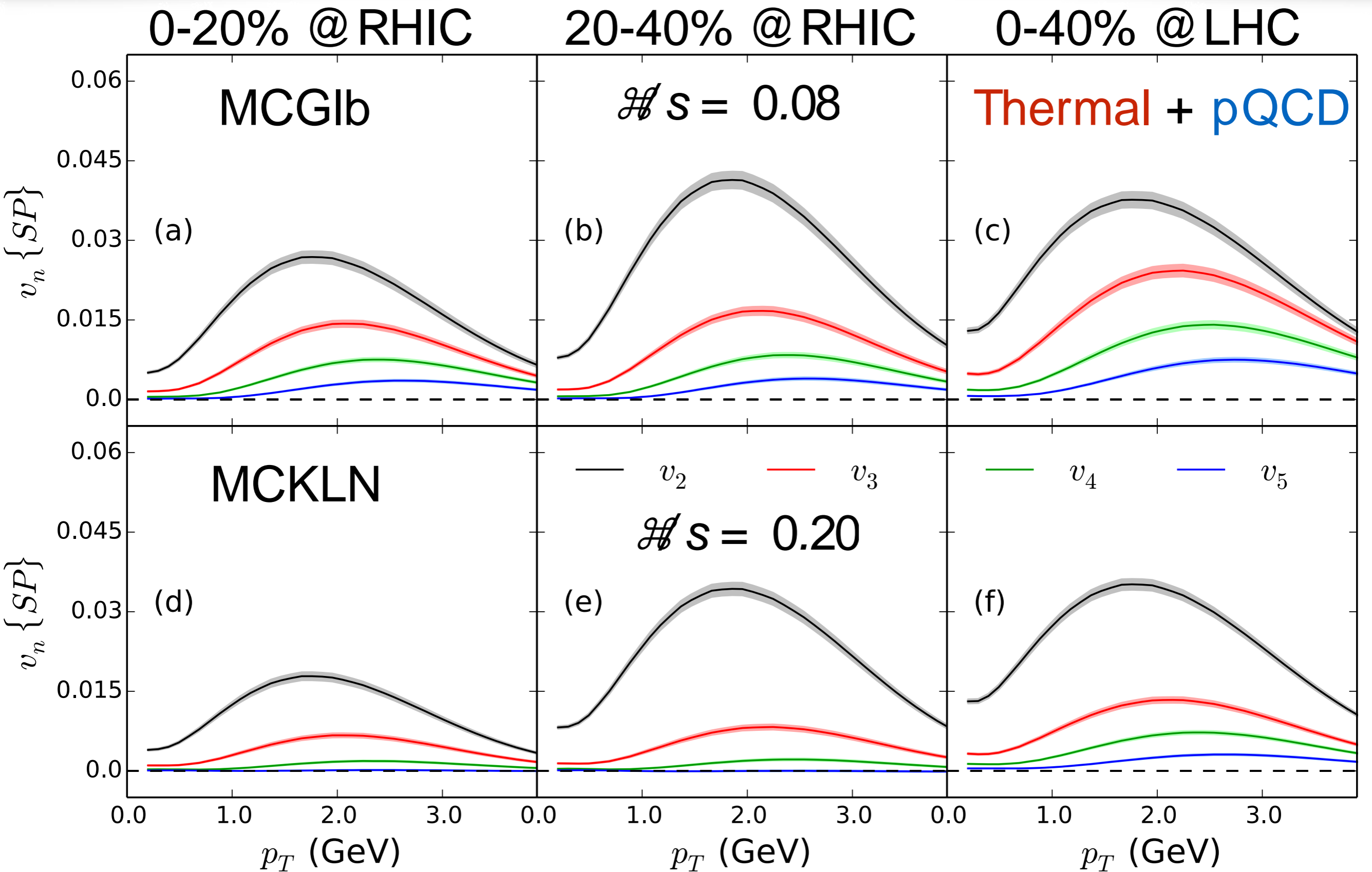
- The anisotropic flows of photons show similar centrality dependence as hadron v_n

Event-by-Event Full Viscous Photon v_n



- The anisotropic flows of photons show similar centrality dependence as hadron v_n
- The ratio v_2/v_3 increases with the shear viscosity
- The centrality dependence of this ratio is stronger for the MCKLN model, driven by η^2

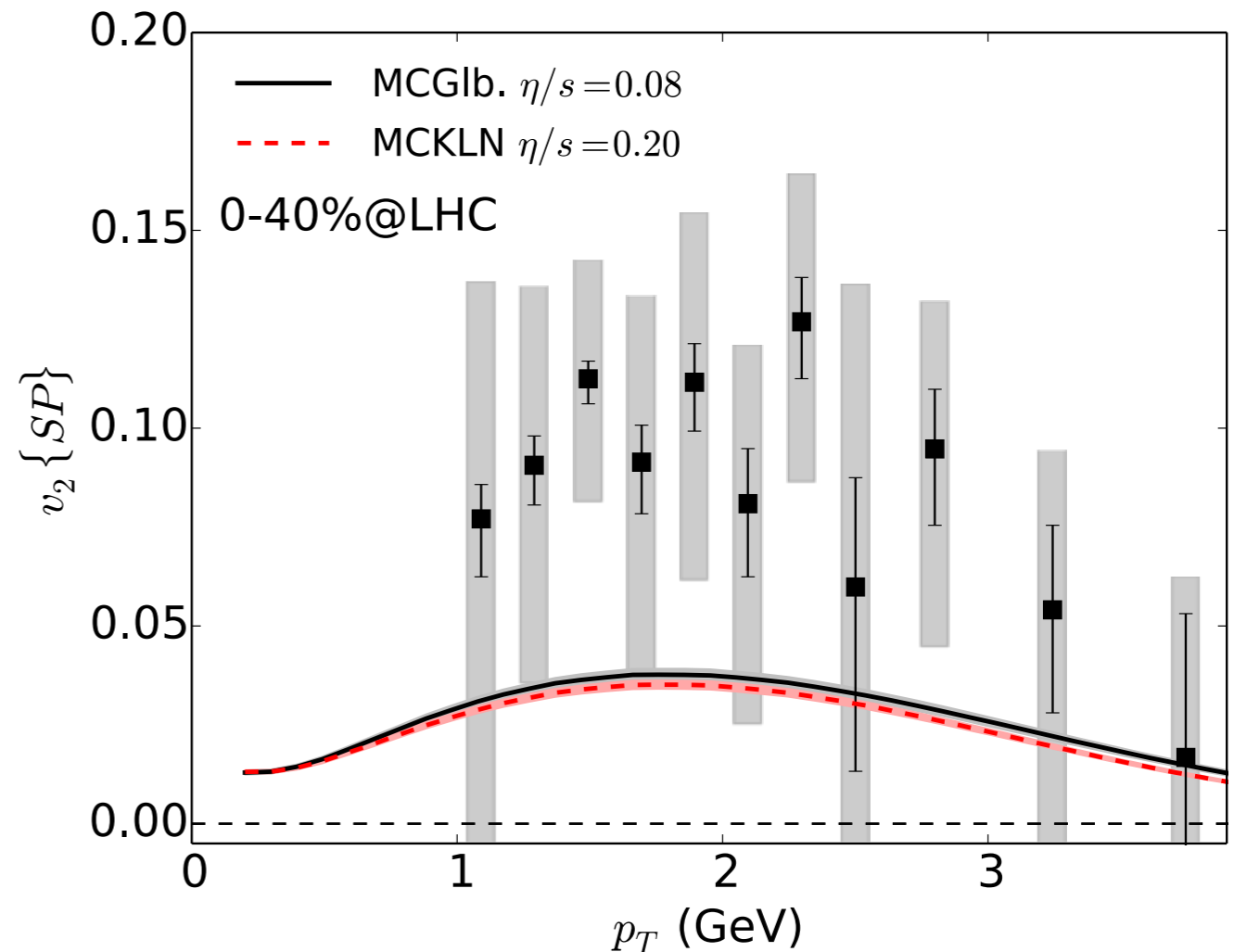
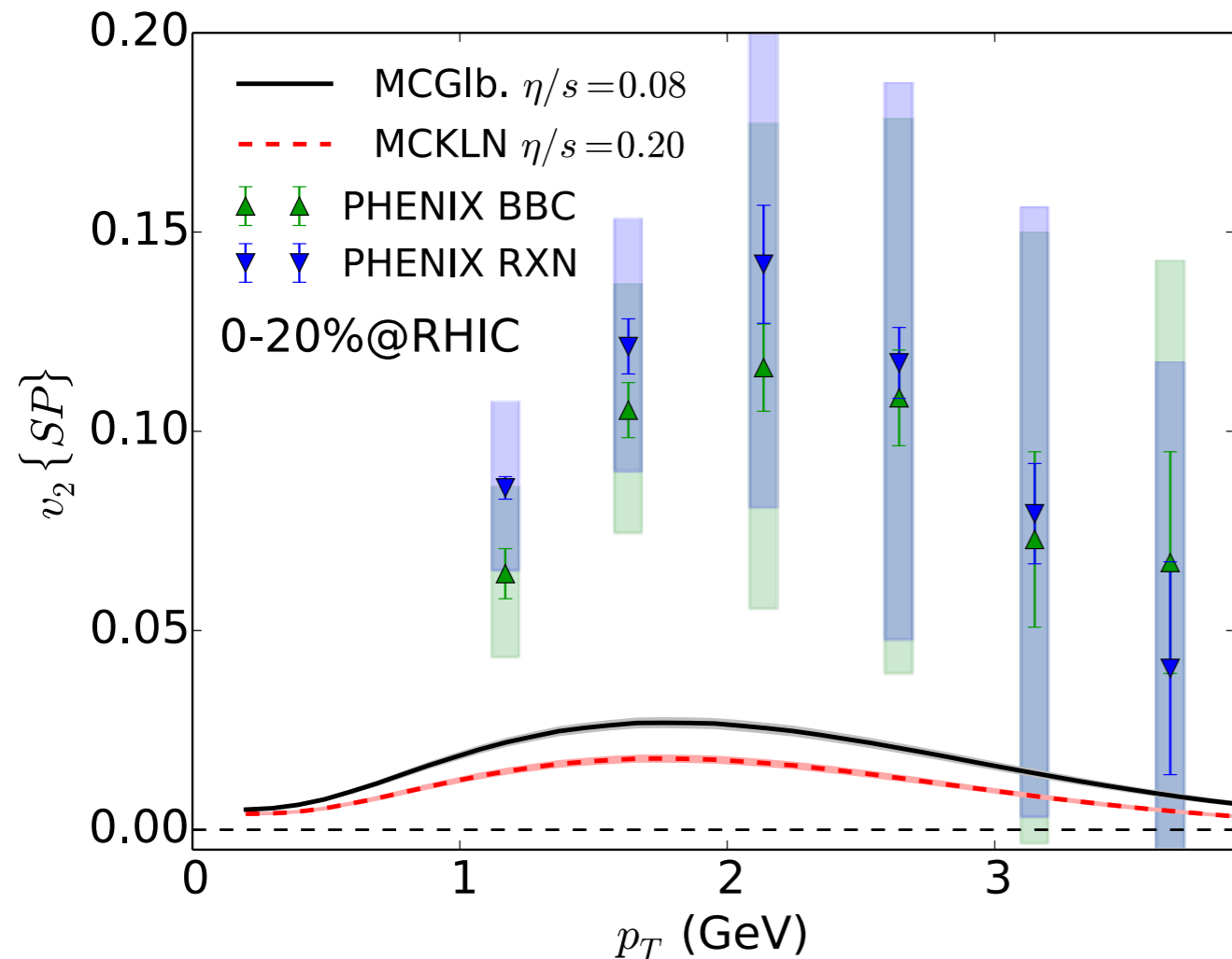
Event-by-Event Full-Viscous Photon v_n



Comparisons with exp. data

RHIC 0-20%

LHC 0-40%

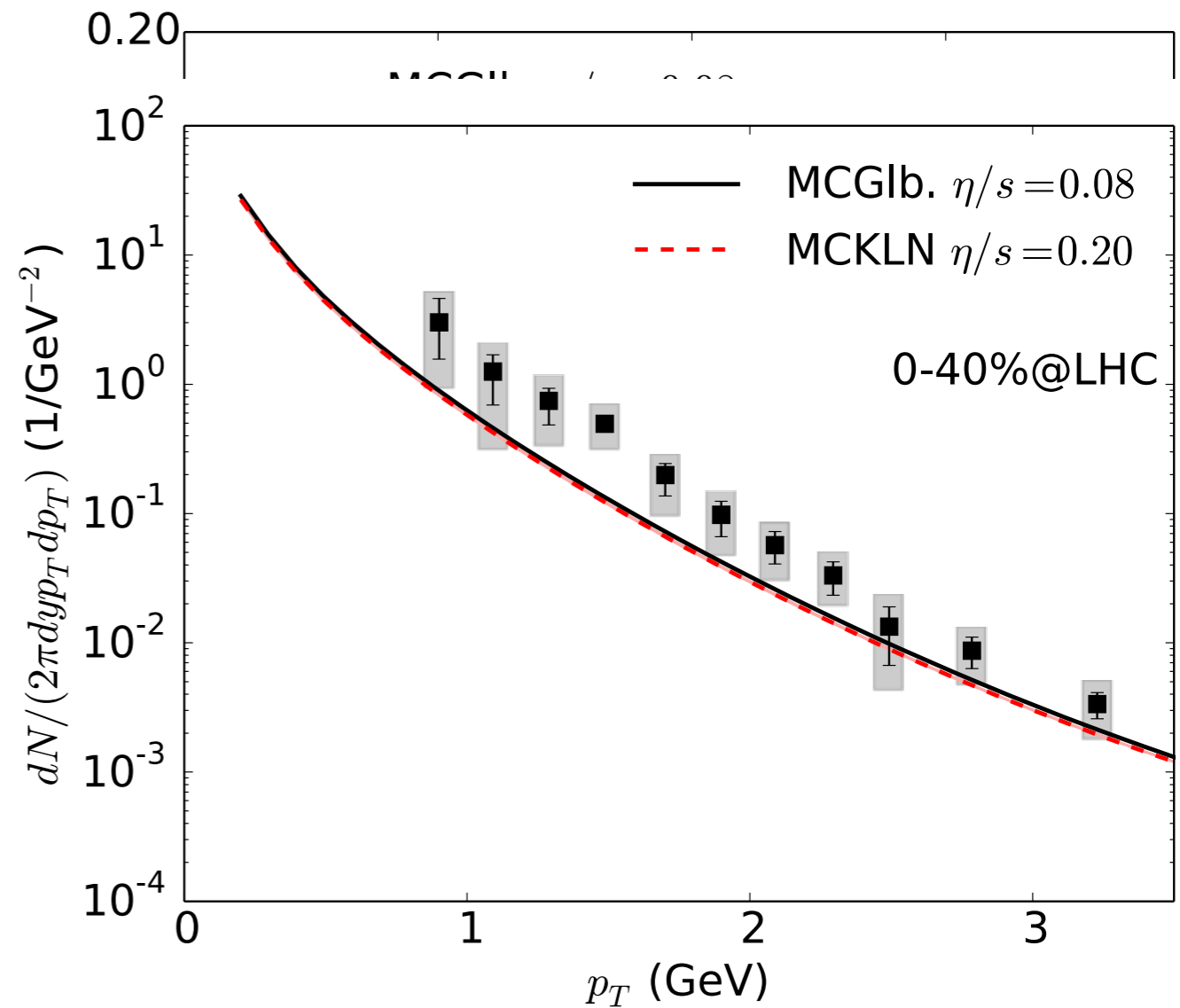
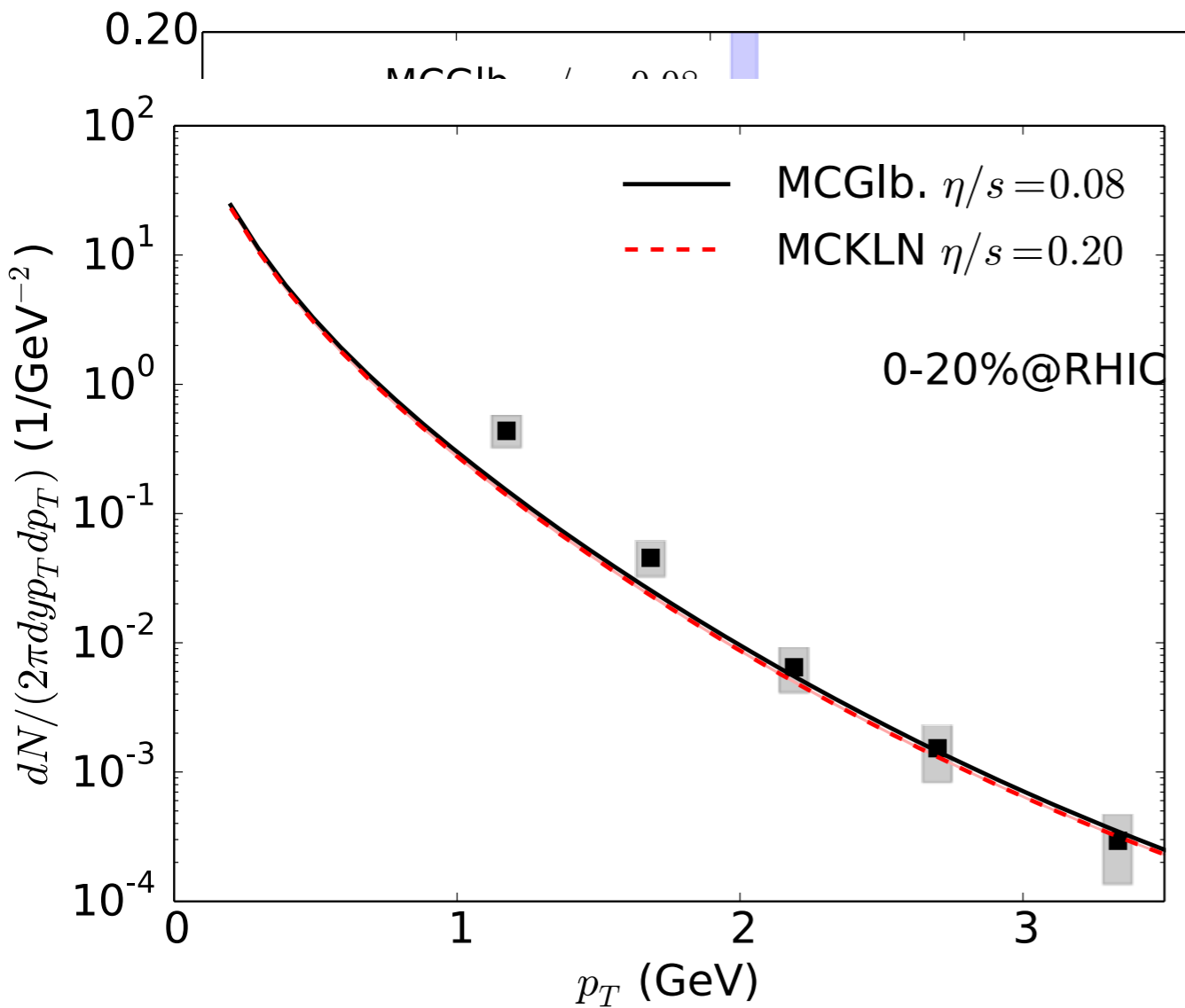


- Current calculations still underestimate the experimental data by a factor of 3

Comparisons with exp. data

RHIC 0-20%

LHC 0-40%



- Current calculations still underestimate the experimental data by a factor of 3
- Thermal yield is also missing in the azimuthally integrated photon spectra at low p_T

EM decays of short-lived resonances (I)

Thanks to Ralf Rapp and EMMI RRTF

Contributions from the short-lived resonances:

reaction	branching ratio
$\rho^0 \rightarrow \pi^+ + \pi^- + \gamma$	1%
$b_1(1235) \rightarrow \pi^\pm + \gamma$	$1.6 * 10^{-3}$
$h_1(1170) \rightarrow \pi^0 + \gamma$	$1.7 * 10^{-3}$
$a_1(1260) \rightarrow \pi^0 + \gamma$	$1.7 * 10^{-3}$
$f_1(1285) \rightarrow \rho_0 + \gamma$	5.5%
$a_2(1320) \rightarrow \pi^\pm + \gamma$	$2.68 * 10^{-3}$
$K^*(892) \rightarrow K^0 + \gamma$	$2.4 * 10^{-3}$
$K^*(892) \rightarrow K^\pm + \gamma$	$1 * 10^{-3}$
$K_1(1270) \rightarrow K^0 + \gamma$	$8.4 * 10^{-4}$
$K_1(1400) \rightarrow K^0 + \gamma$	$1.6 * 10^{-3}$
$K_2^*(1430) \rightarrow K^+ + \gamma$	$2.4 * 10^{-3}$
$K_2^*(1430) \rightarrow K^0 + \gamma$	$9 * 10^{-4}$

reaction	branching ratio
$N(1440) \rightarrow p + \gamma$	$4.15 * 10^{-4}$
$N(1440) \rightarrow n + \gamma$	$3 * 10^{-4}$
$N(1520) \rightarrow p + \gamma$	$4.15 * 10^{-3}$
$N(1520) \rightarrow n + \gamma$	$4.15 * 10^{-3}$
$N(1530) \rightarrow p + \gamma$	$2.25 * 10^{-3}$
$N(1530) \rightarrow n + \gamma$	$2.25 * 10^{-3}$
$N(1650) \rightarrow p + \gamma$	$1.2 * 10^{-3}$
$N(1650) \rightarrow n + \gamma$	$8.5 * 10^{-4}$
$N(1675) \rightarrow p + \gamma$	$1 * 10^{-4}$
$N(1675) \rightarrow n + \gamma$	$7.5 * 10^{-4}$
$N(1680) \rightarrow p + \gamma$	$2.65 * 10^{-3}$
$N(1680) \rightarrow n + \gamma$	$3.35 * 10^{-4}$
$N(1700) \rightarrow p + \gamma$	$3 * 10^{-4}$
$N(1700) \rightarrow n + \gamma$	$1.2 * 10^{-3}$
$N(1710) \rightarrow p + \gamma$	$4.1 * 10^{-4}$
$N(1710) \rightarrow n + \gamma$	$1 * 10^{-4}$
$N(1720) \rightarrow p + \gamma$	$1.5 * 10^{-3}$
$N(1720) \rightarrow n + \gamma$	$8 * 10^{-5}$

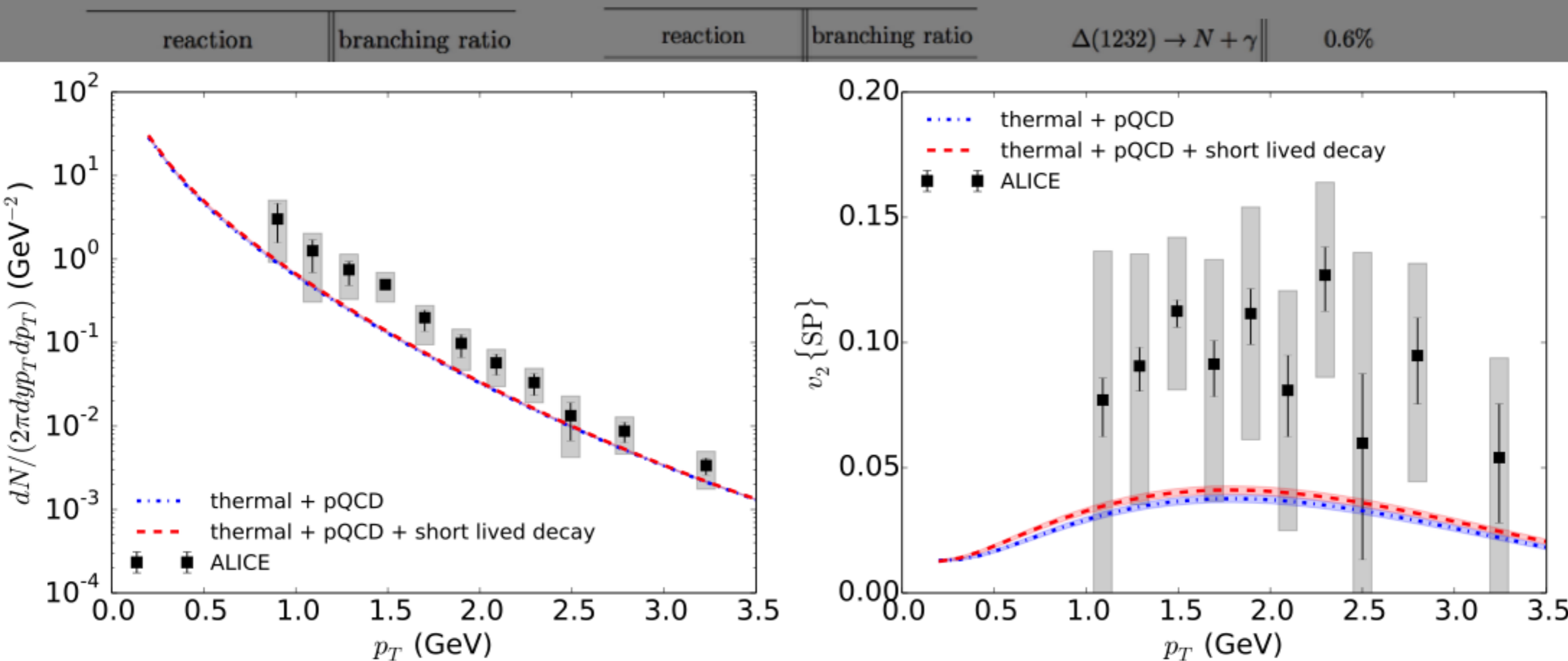
$\Delta(1232) \rightarrow N + \gamma$	0.6%
$\Delta(1600) \rightarrow N + \gamma$	$1.8 * 10^{-4}$
$\Delta(1620) \rightarrow N + \gamma$	$6.5 * 10^{-4}$
$\Delta(1700) \rightarrow N + \gamma$	$4.1 * 10^{-3}$
$\Delta(1905) \rightarrow N + \gamma$	$2.4 * 10^{-4}$
$\Delta(1910) \rightarrow N + \gamma$	$1 * 10^{-4}$
$\Delta(1920) \rightarrow N + \gamma$	$2 * 10^{-3}$
$\Delta(1950) \rightarrow N + \gamma$	$1.05 * 10^{-3}$

reaction	branching ratio
$\Lambda(1405) \rightarrow \Lambda + \gamma$	$5.4 * 10^{-4}$
$\Lambda(1405) \rightarrow \Sigma^0 + \gamma$	$2 * 10^{-4}$
$\Lambda(1520) \rightarrow \Lambda + \gamma$	$8.5 * 10^{-3}$
$\Lambda(1520) \rightarrow \Sigma^0 + \gamma$	2%
$\Sigma^0(1385) \rightarrow \Lambda + \gamma$	1.25%
$\Xi(1530) \rightarrow \Xi + \gamma$	4%

EM decays of short-lived resonances (II)

Thanks to Ralf Rapp and EMMI RRTF

Contributions from the short-lived resonances:

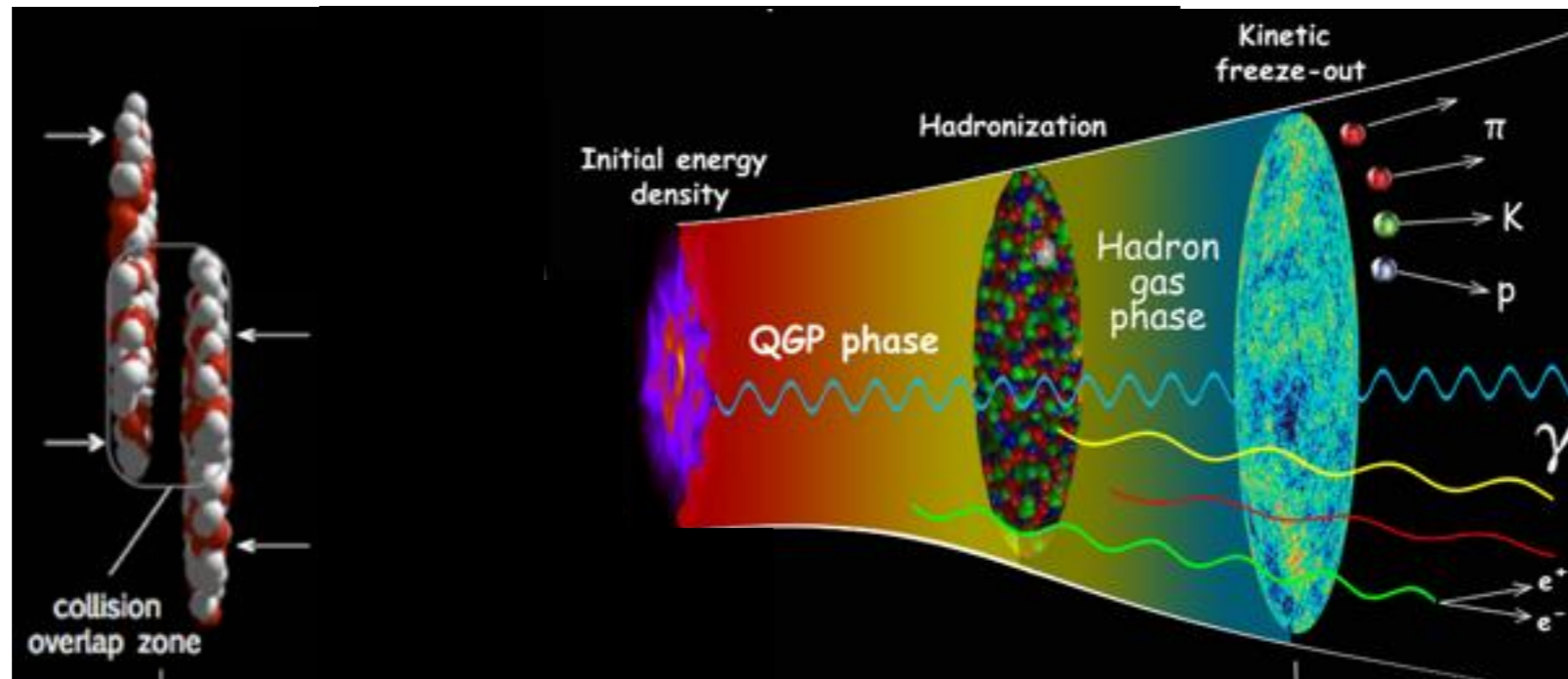


Small but significant effects in the right direction

$N(1700) \rightarrow n + \gamma$	1.2×10^{-3}	$\Lambda(1520) \rightarrow \Sigma^0 + \gamma$	2%
$N(1710) \rightarrow n + \gamma$	1×10^{-4}	$\Xi(1530) \rightarrow \Xi + \gamma$	4%
$N(1720) \rightarrow p + \gamma$	1.5×10^{-3}		
$N(1720) \rightarrow n + \gamma$	8×10^{-5}		

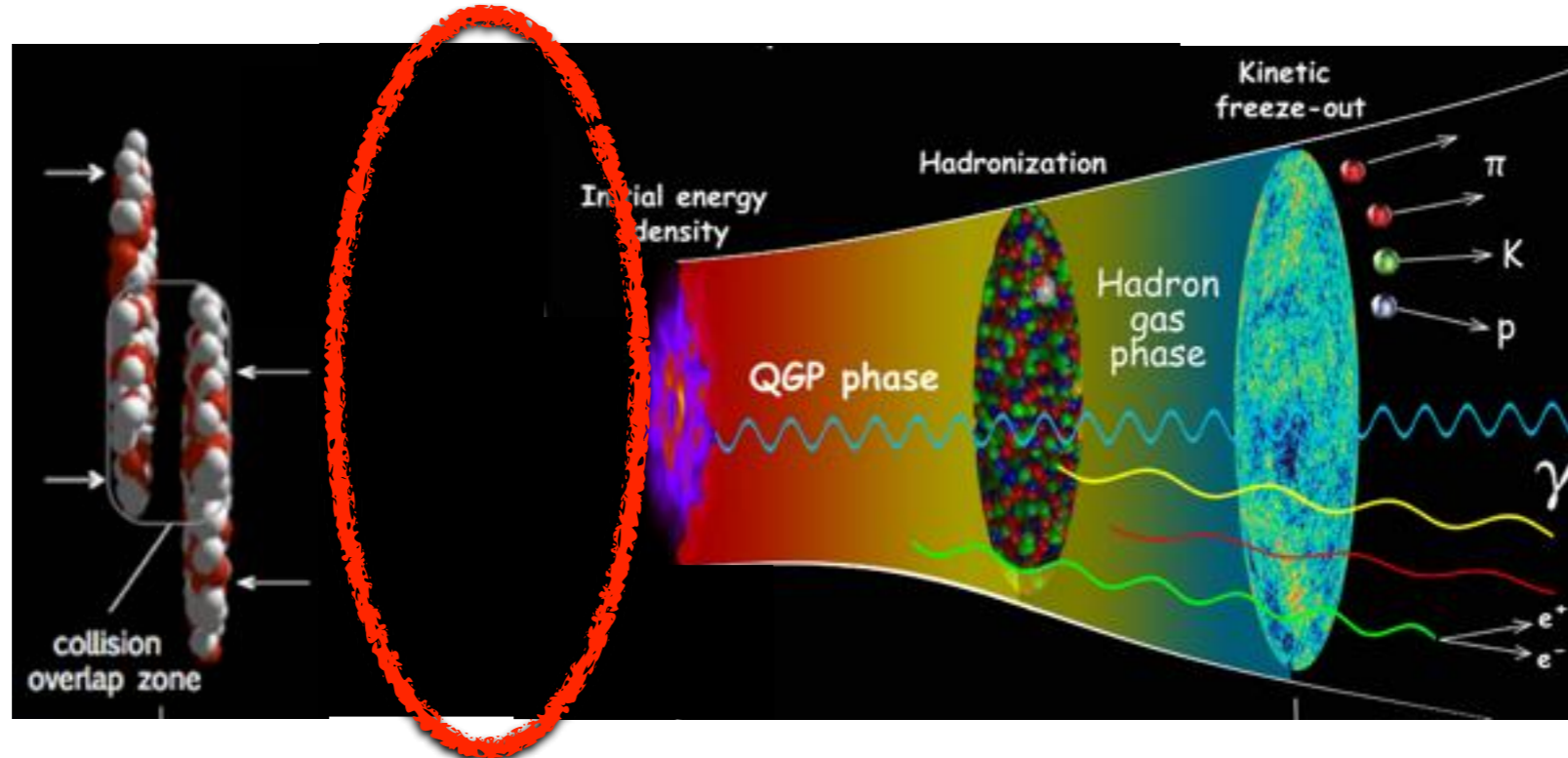
Pre-equilibrium flow (I)

Contributions from pre-equilibrium flow and $\hat{\mu} \ll \epsilon$:



Pre-equilibrium flow (II)

Contributions from pre-equilibrium flow and $\hat{\mu}^{\langle x \rangle}$:



Free-streaming

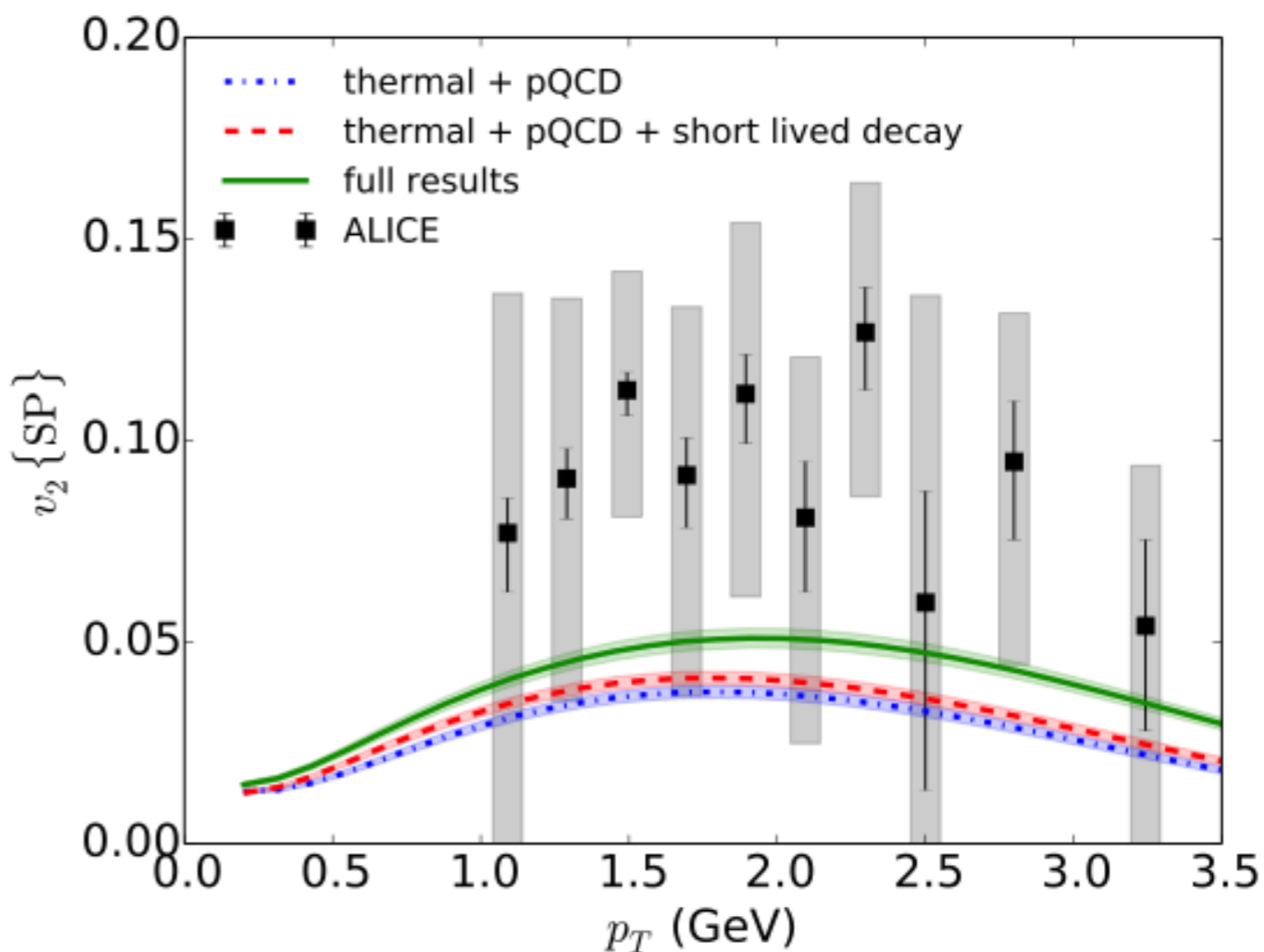
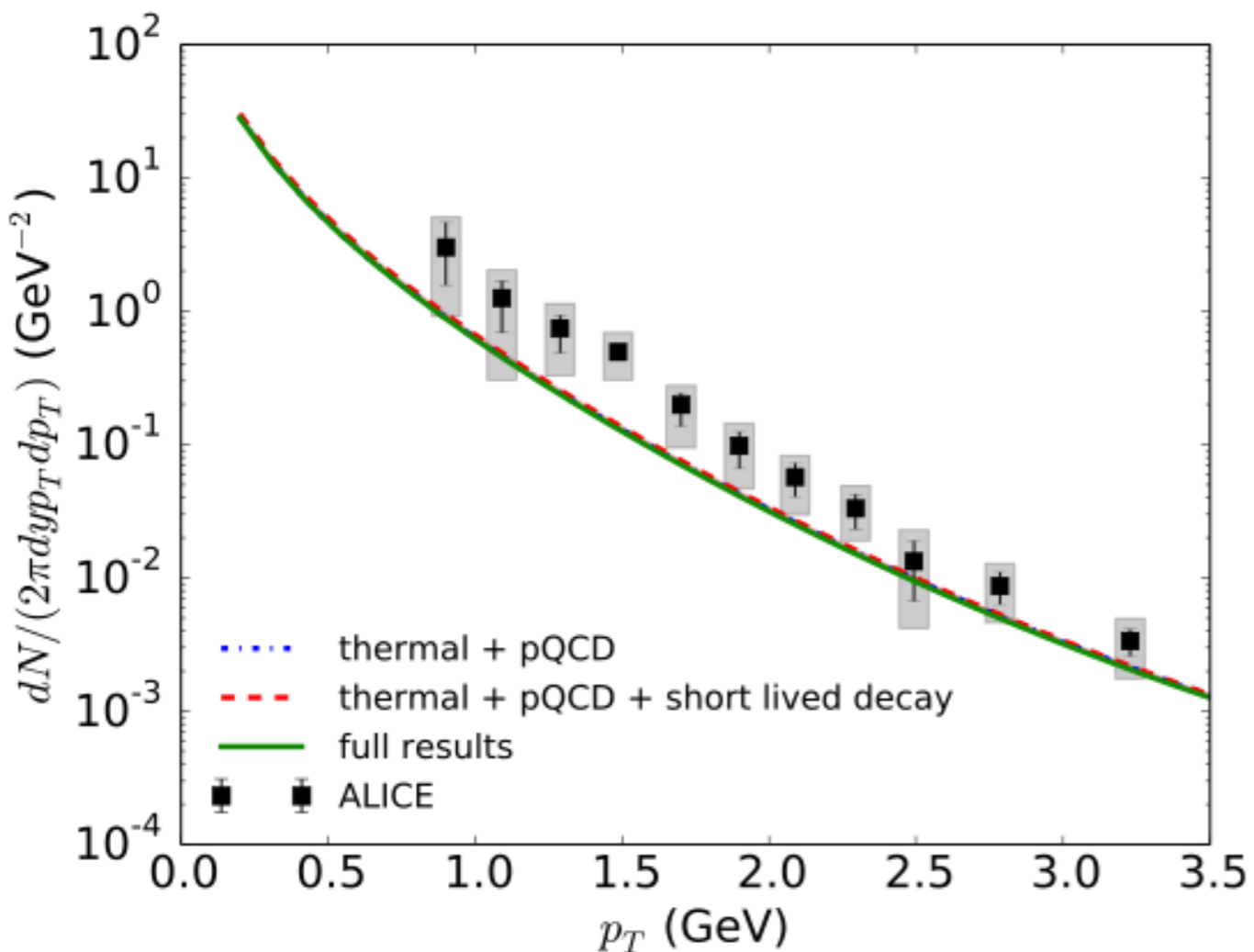
$$f(\underline{x}, \mathbf{x}, p) = f(\underline{x}_0, \mathbf{x} - \hat{p}(\underline{x} - \underline{x}_0), p)$$

$$T^{\mu \langle x \rangle}(\underline{x}, \mathbf{x}) = \int \frac{d^3 p}{E} p^\mu p^{\langle x \rangle} f(\underline{x}, \mathbf{x}, p)$$

$$T^{\mu \langle x \rangle} u_{\langle x \rangle} = eu^\mu \longrightarrow = eu^\mu u^{\langle x \rangle} - (P + \uparrow) \Delta^{\mu \langle x \rangle} + \hat{\mu}^{\langle x \rangle}$$

Pre-equilibrium flow (III)

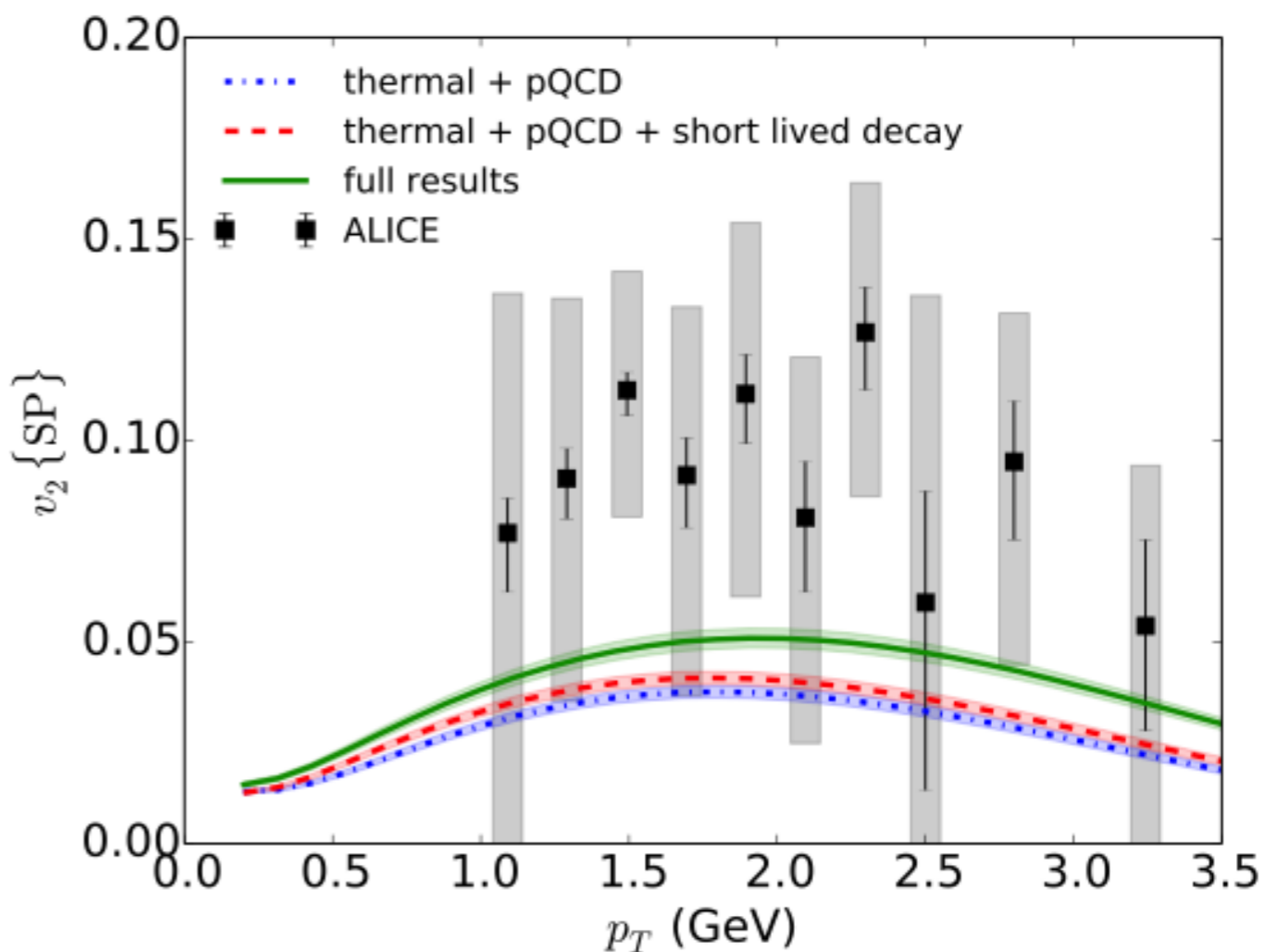
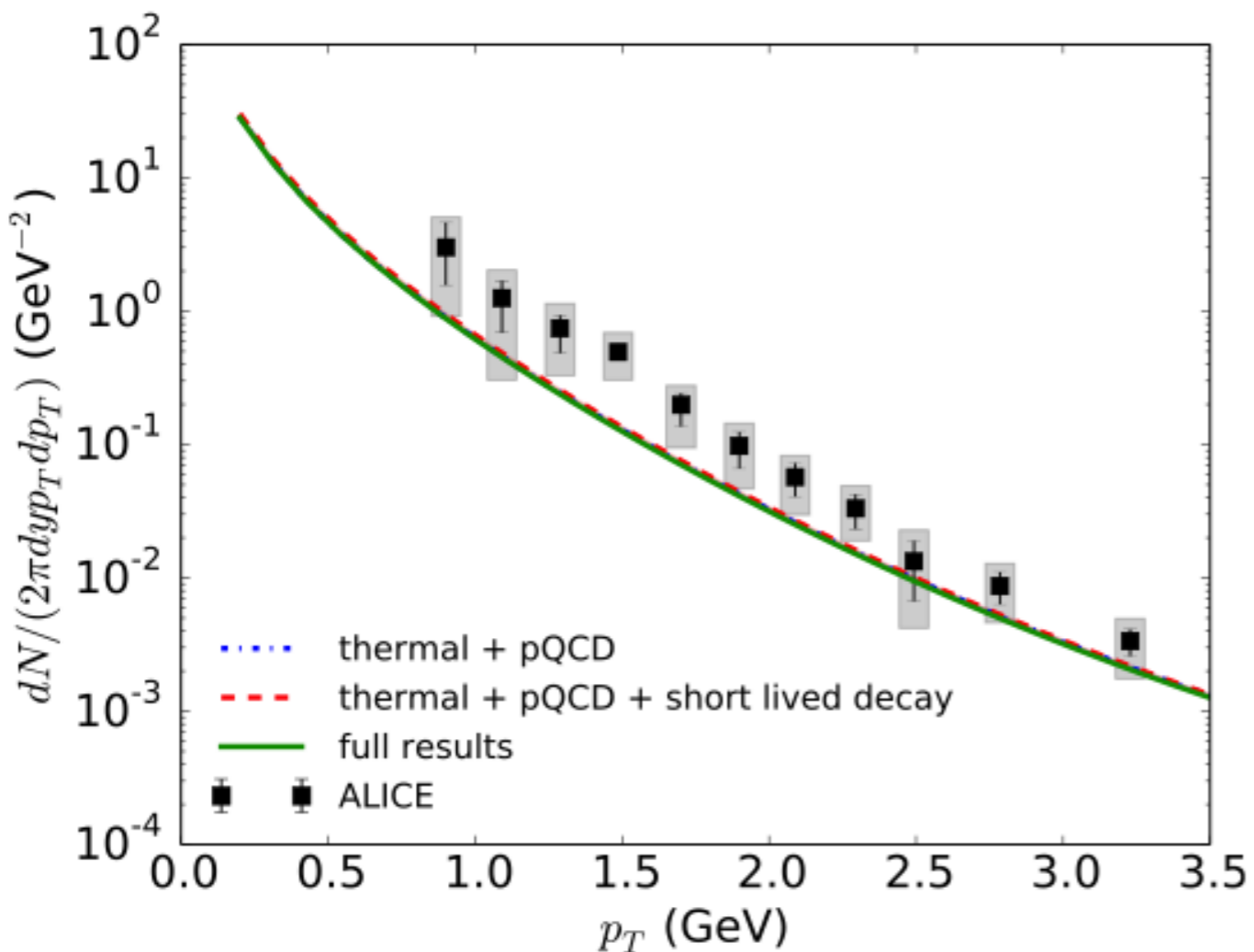
Contributions from pre-equilibrium flow and $\pi^{\mu\nu}$:



Small but significant effects in the right direction

Pre-equilibrium flow (III)

Contributions from pre-equilibrium flow and $\pi^{\mu\nu}$:



Small but significant effects in the right direction

Poster:
J-F. Paquet, **G21**

Conclusions

- We studied photon spectra and their anisotropic flows v_n from *event-by-event* viscous hydrodynamic medium

$$v_n^{\gamma} \{SP\} (p_T) = \frac{\overline{\frac{dN^{\gamma}}{dy p_T dp_T} (p_T) v_n^{\gamma} (p_T) v_n^{\text{ch}} \cos(n(\phi_n^{\gamma} (p_T) - \phi_n^{\text{ch}}))}}{\overline{\frac{dN^{\gamma}}{dy p_T dp_T} (p_T) v_n^{\text{ch}} \{2\}}}$$

- Shear viscosity suppresses** photon v_n . Dominant suppression comes not from flow, but from the **viscous correction to the production rates**.
- Elliptic** and **triangular** flow of photons are **more sensitive** than hadrons to shear stress at early times and to initial state fluctuations.
- Short-lived resonance decays** and **pre-equilibrium flow** cause measurable **increase** of direct photon anisotropic flow.
- Still, experimental **data** appear to **require significantly more photon rate from the late evolution stage** than implemented in the model

Conclusions

- We studied photon spectra and their anisotropic flows v_n from *event-by-event* viscous hydrodynamic medium

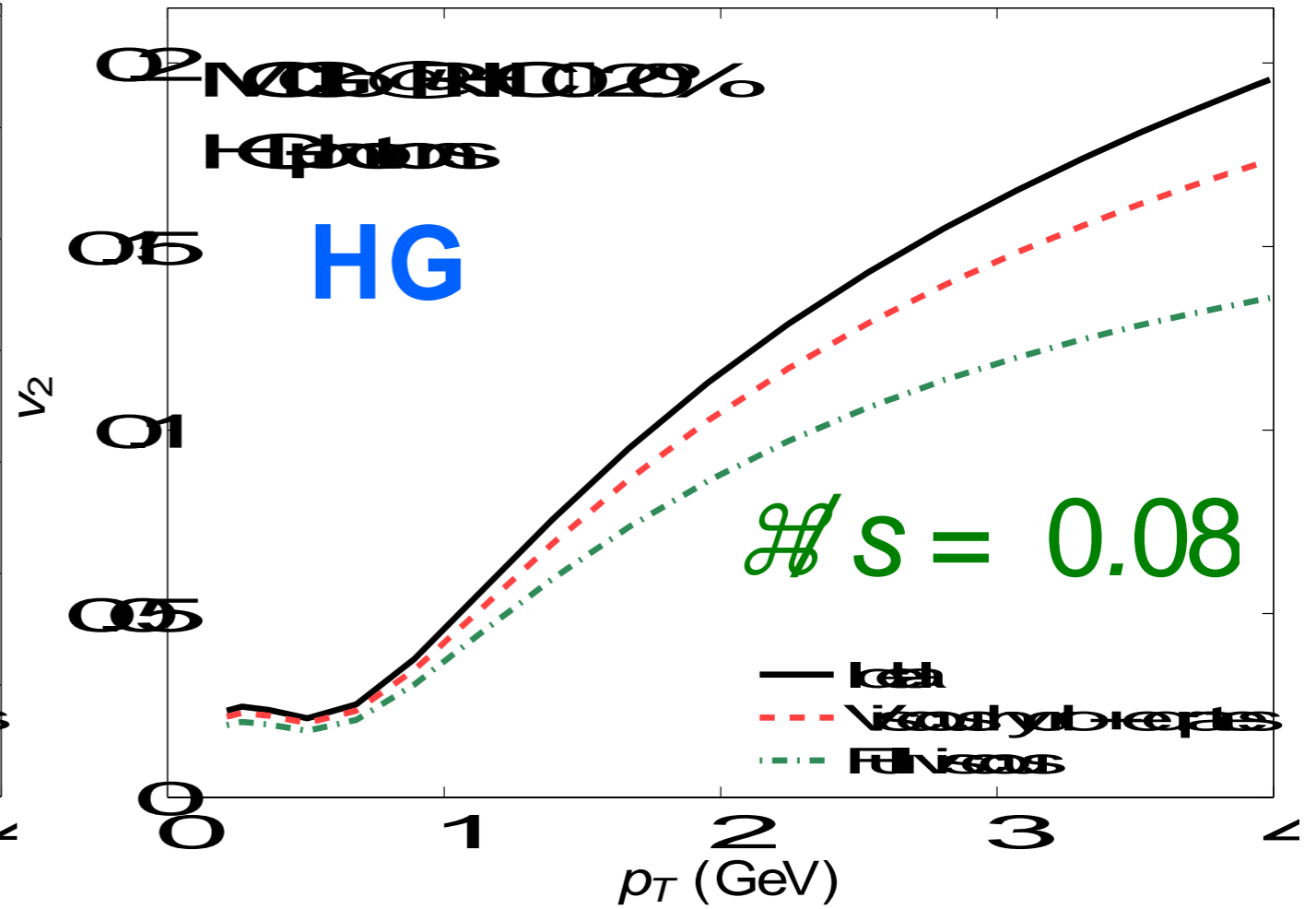
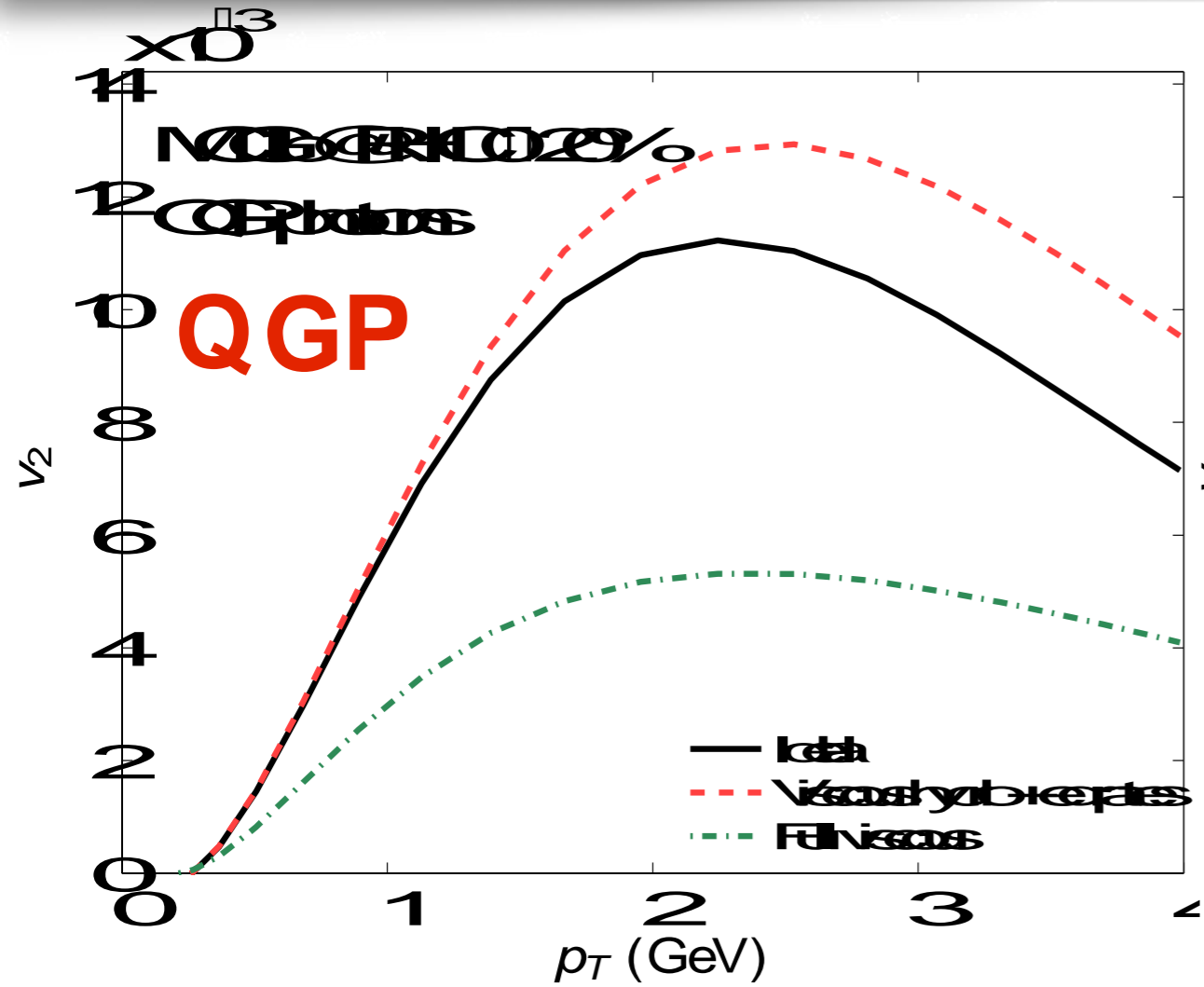
$$v_n^{\gamma}\{\text{SP}\}(p_T) = \frac{\overline{\frac{dN^{\gamma}}{dy p_T dp_T}(p_T)} v_n^{\gamma}(p_T) v_n^{\text{ch}} \cos(n(\phi_n^{\gamma}(p_T) - \phi_n^{\text{ch}}))}{\overline{\frac{dN^{\gamma}}{dy p_T dp_T}(p_T)} v_n^{\text{ch}}\{2\}}$$

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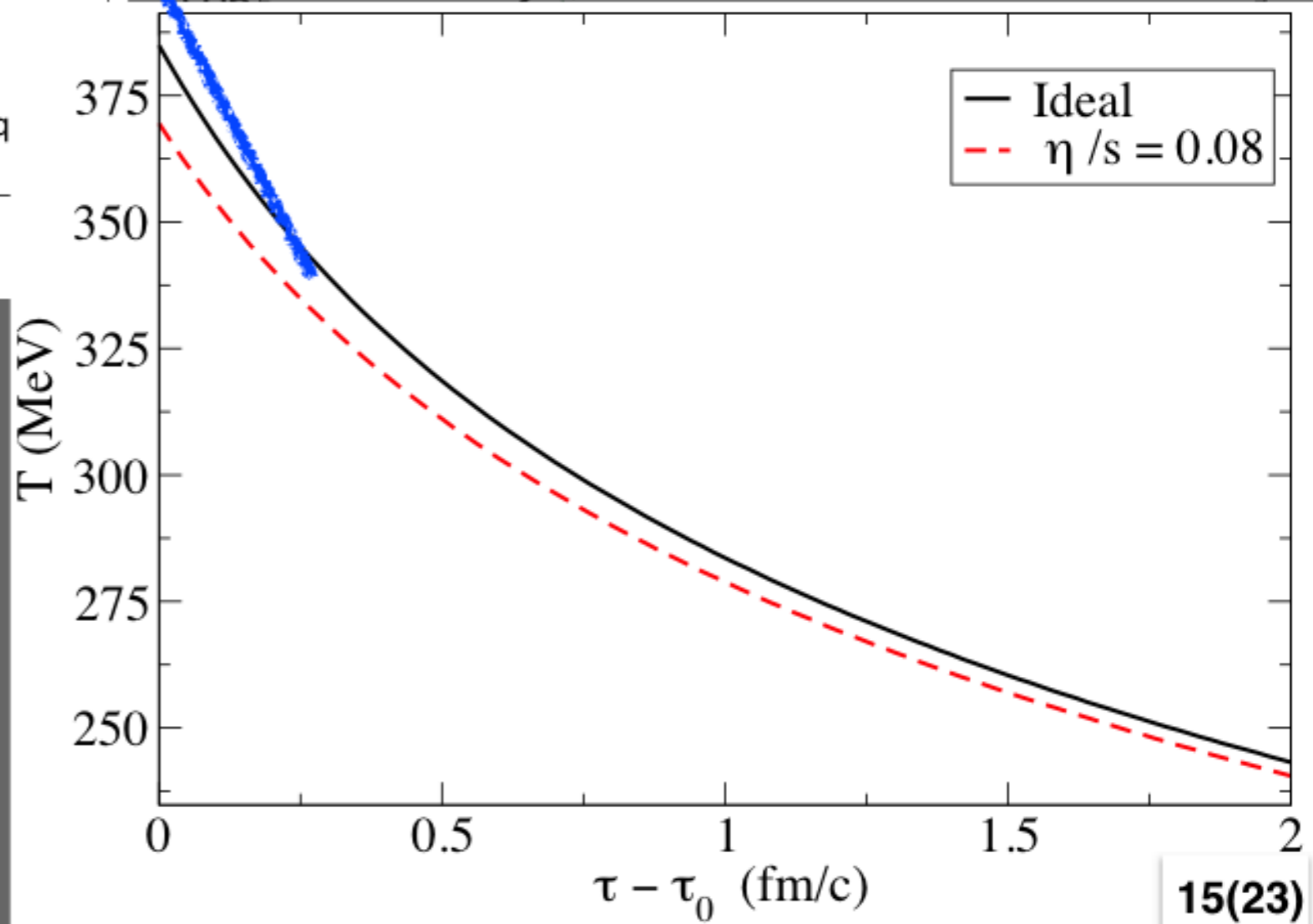
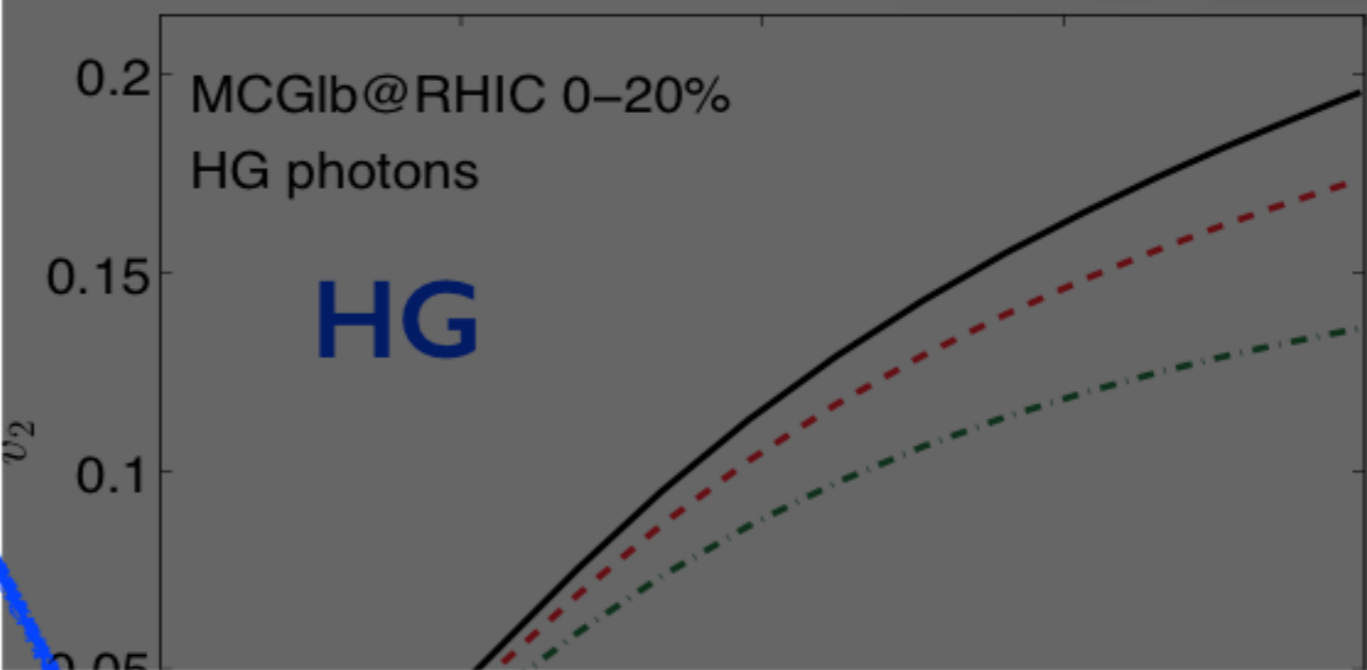
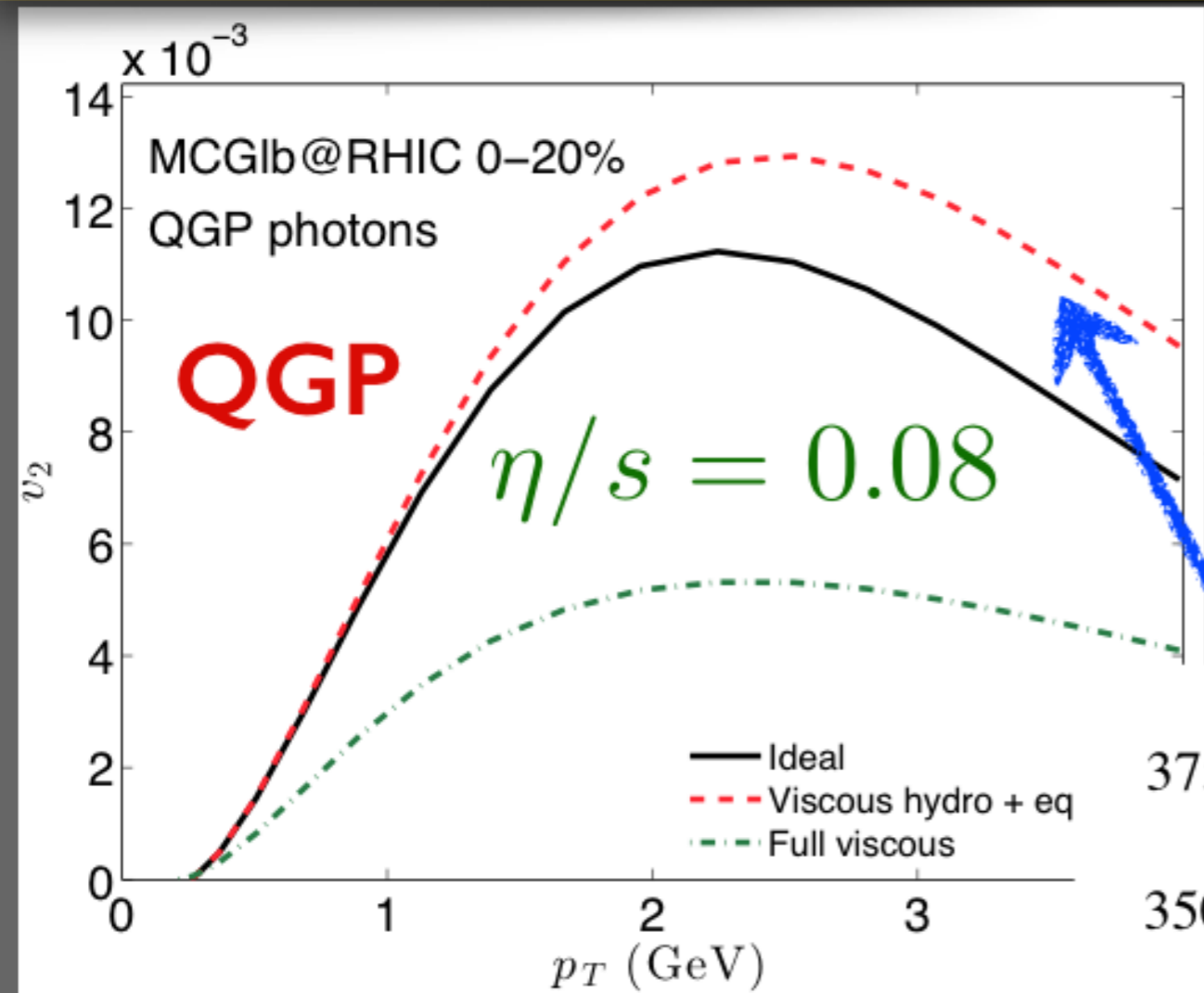
R. Rapp
Mon. 15:20

Back up

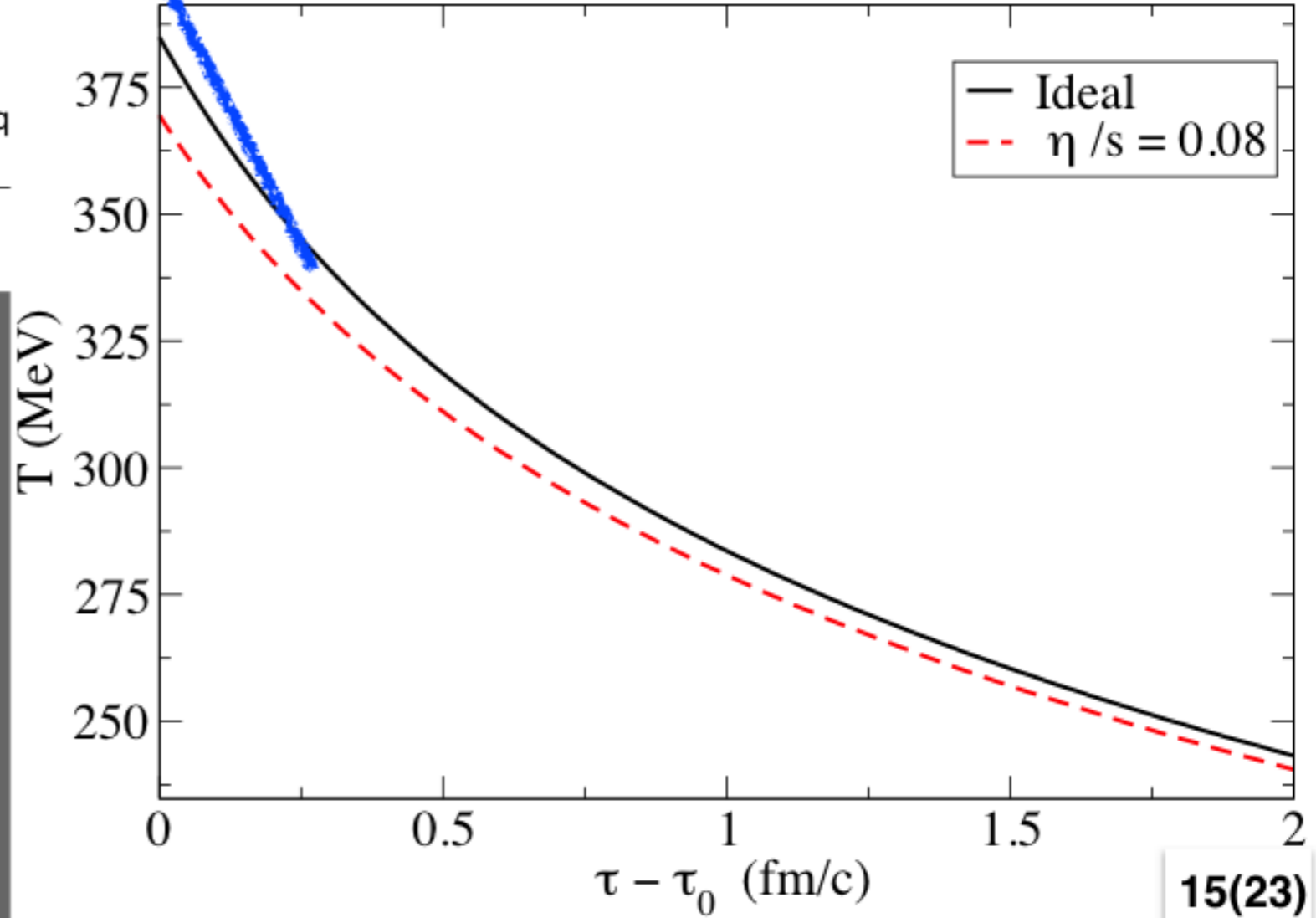
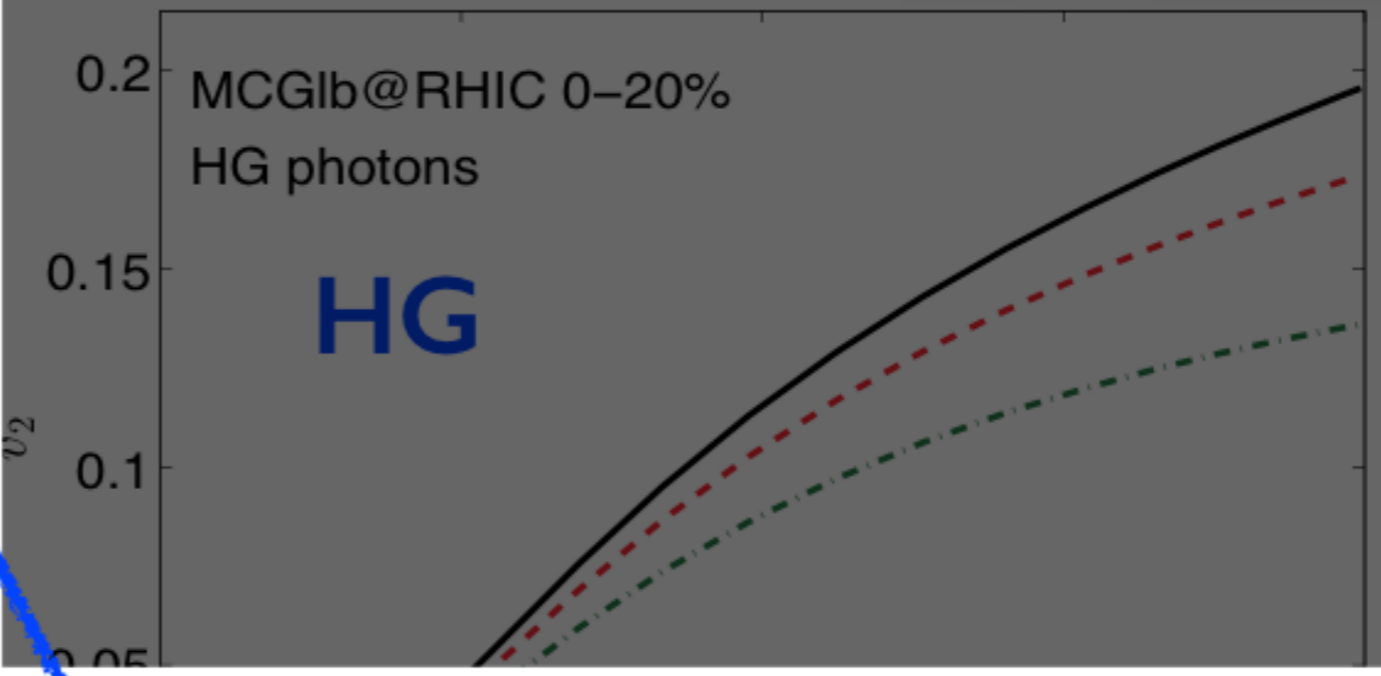
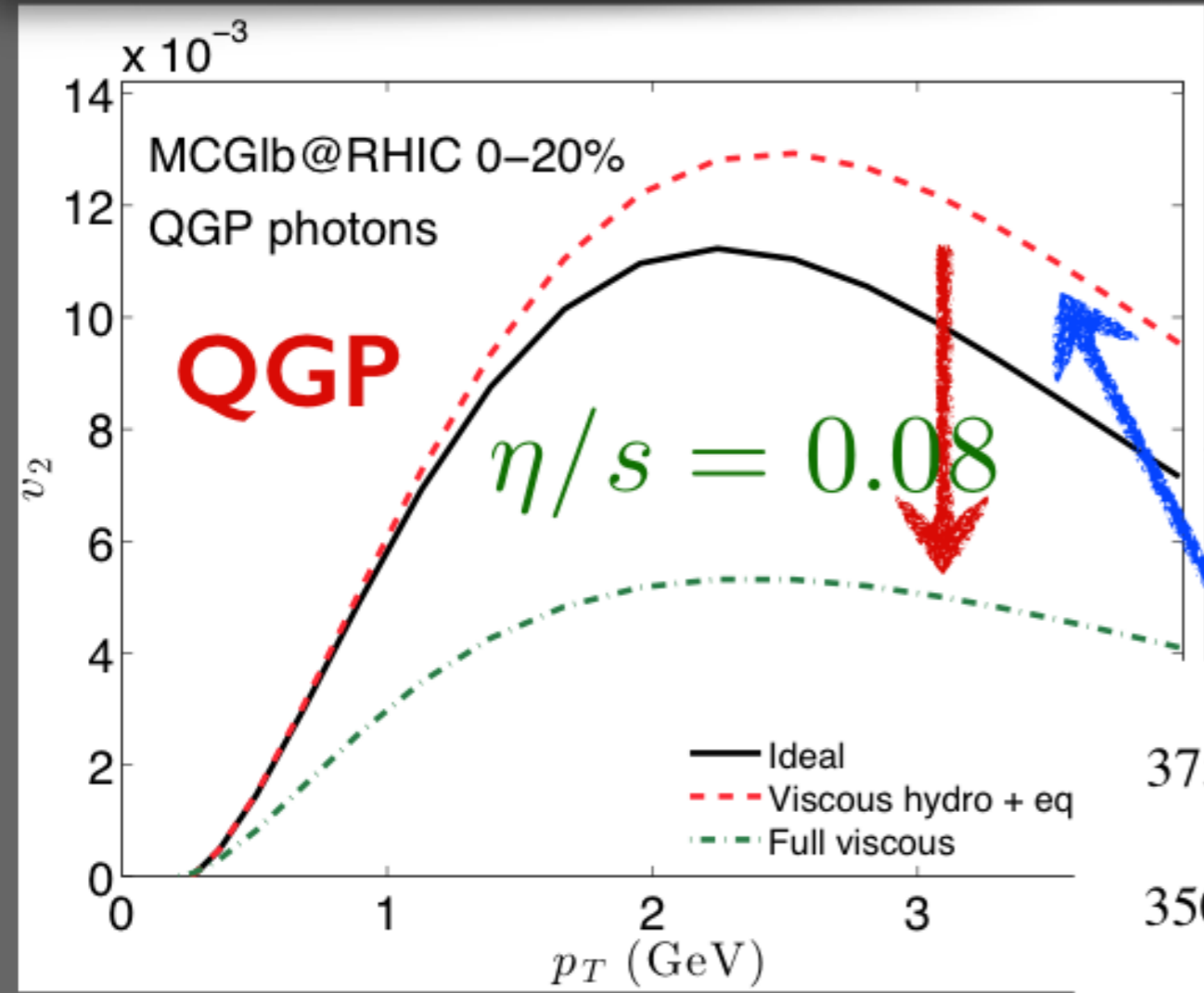
Viscous effects on photon elliptic flow



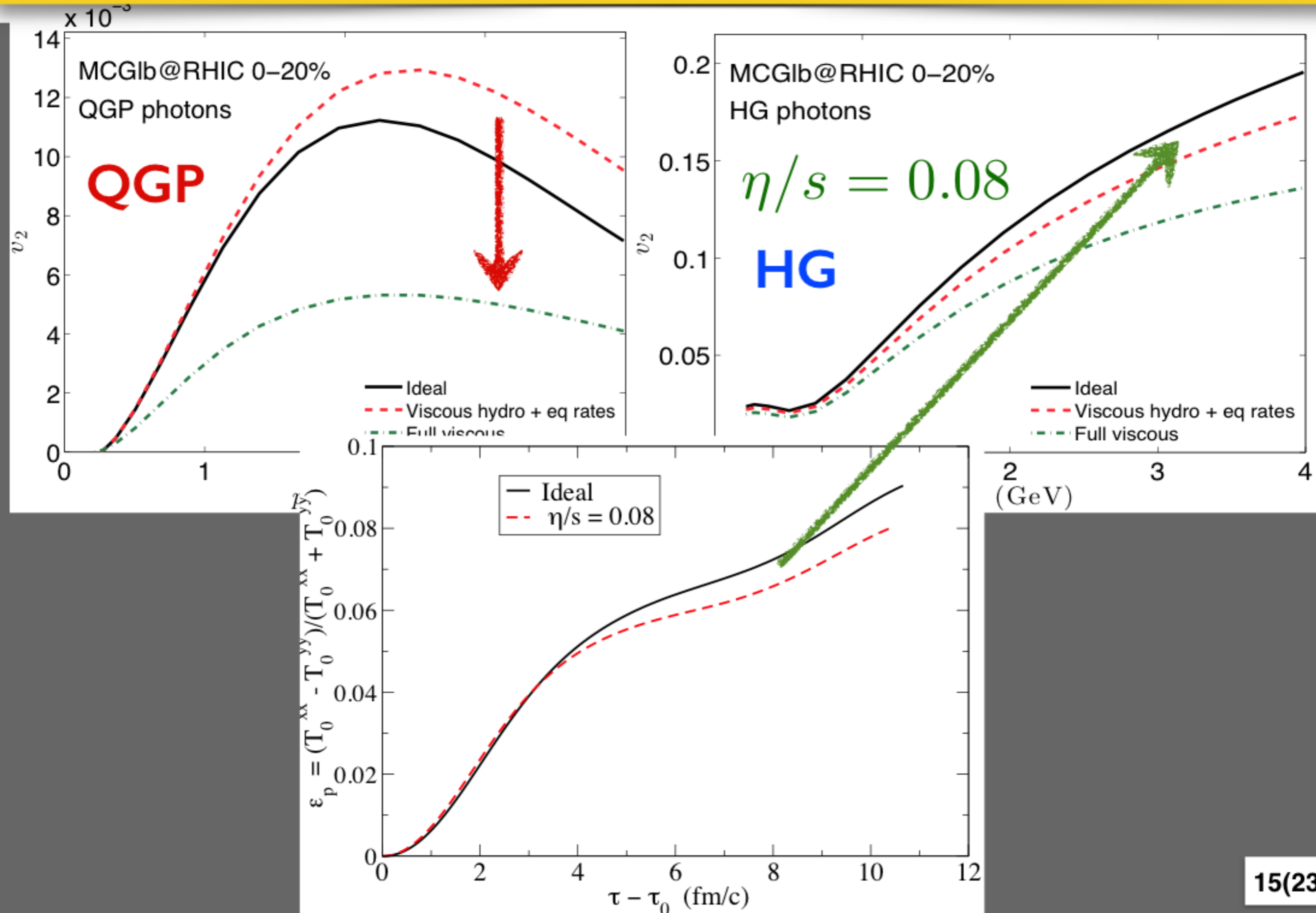
Viscous effects on photon elliptic flow



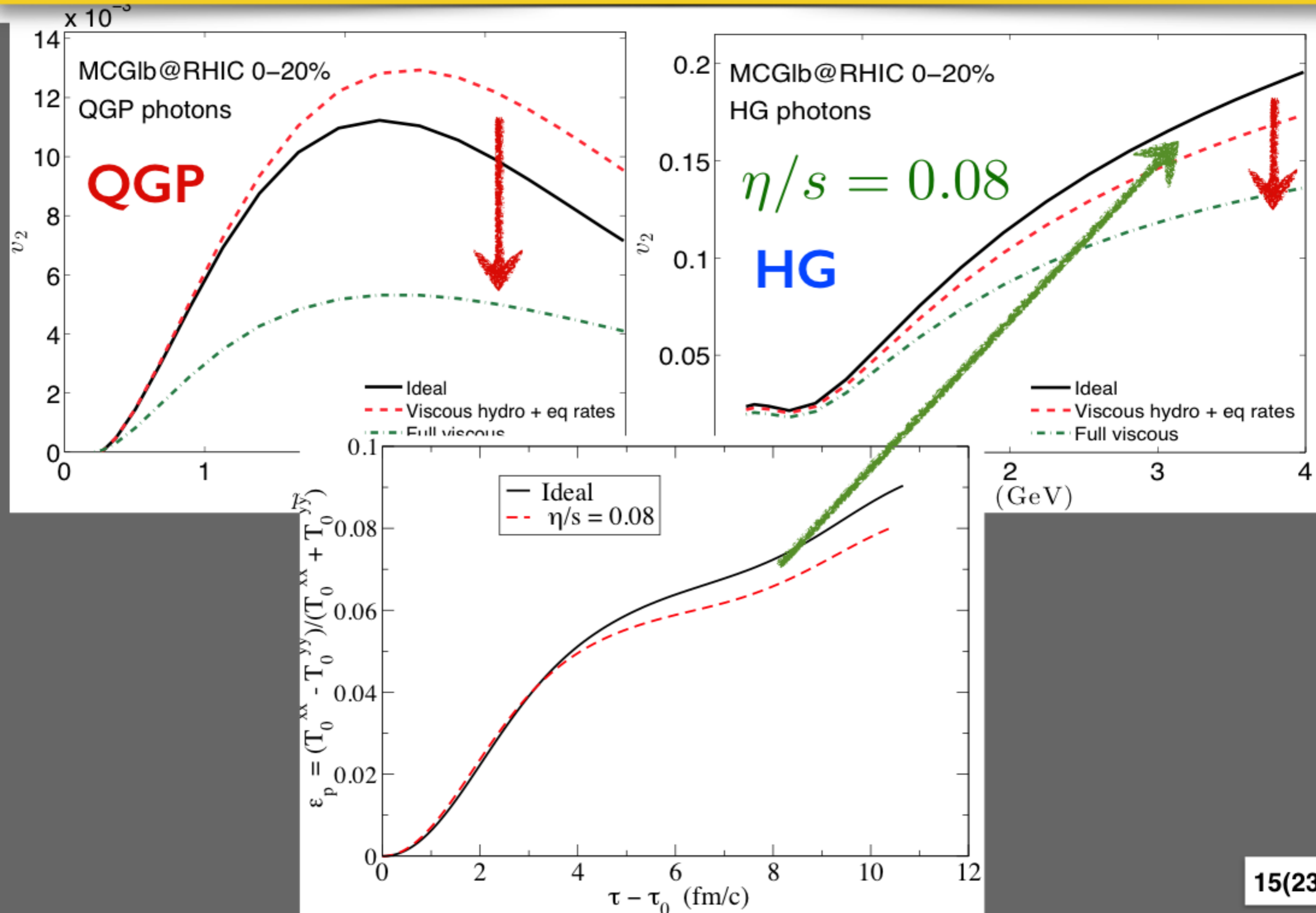
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Viscous effects on photon elliptic flow

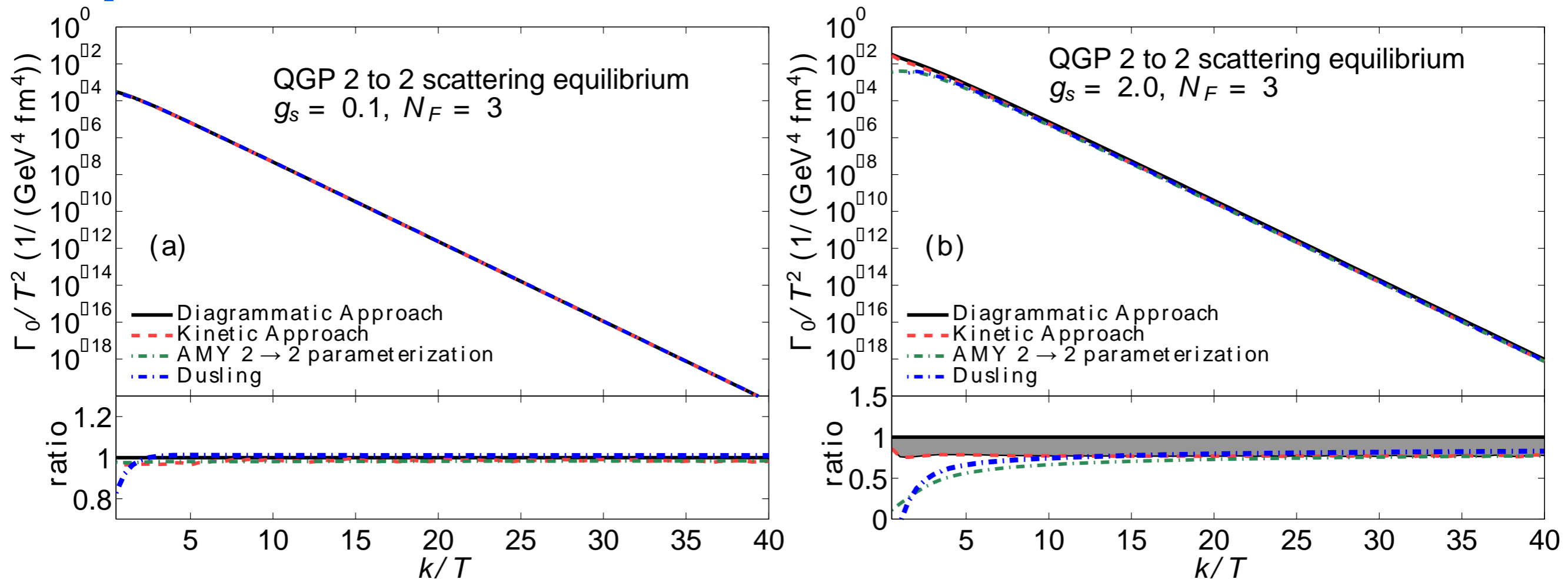


Viscous effects on photon elliptic flow



Photon Rates (QGP 2 to 2 processes only)

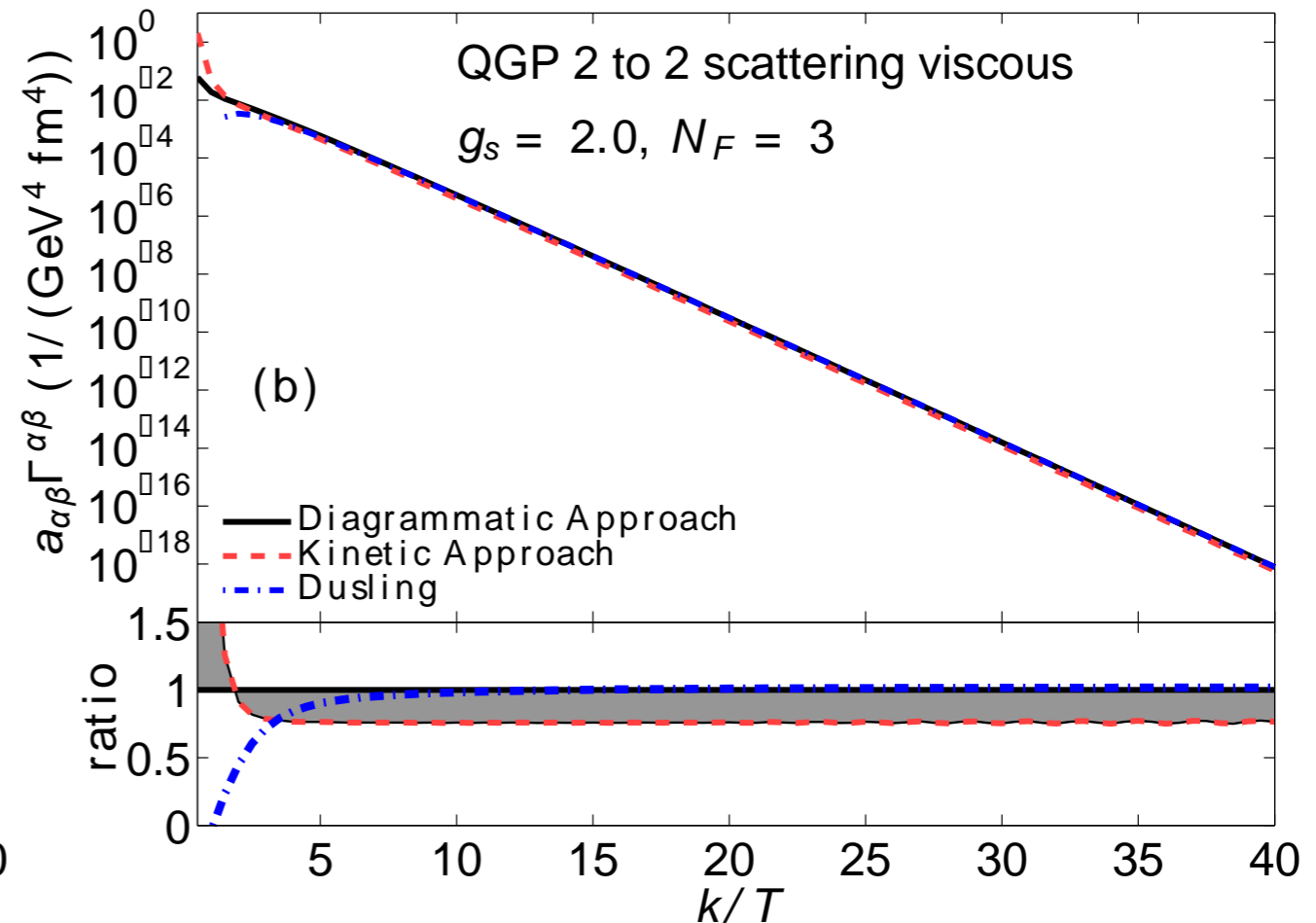
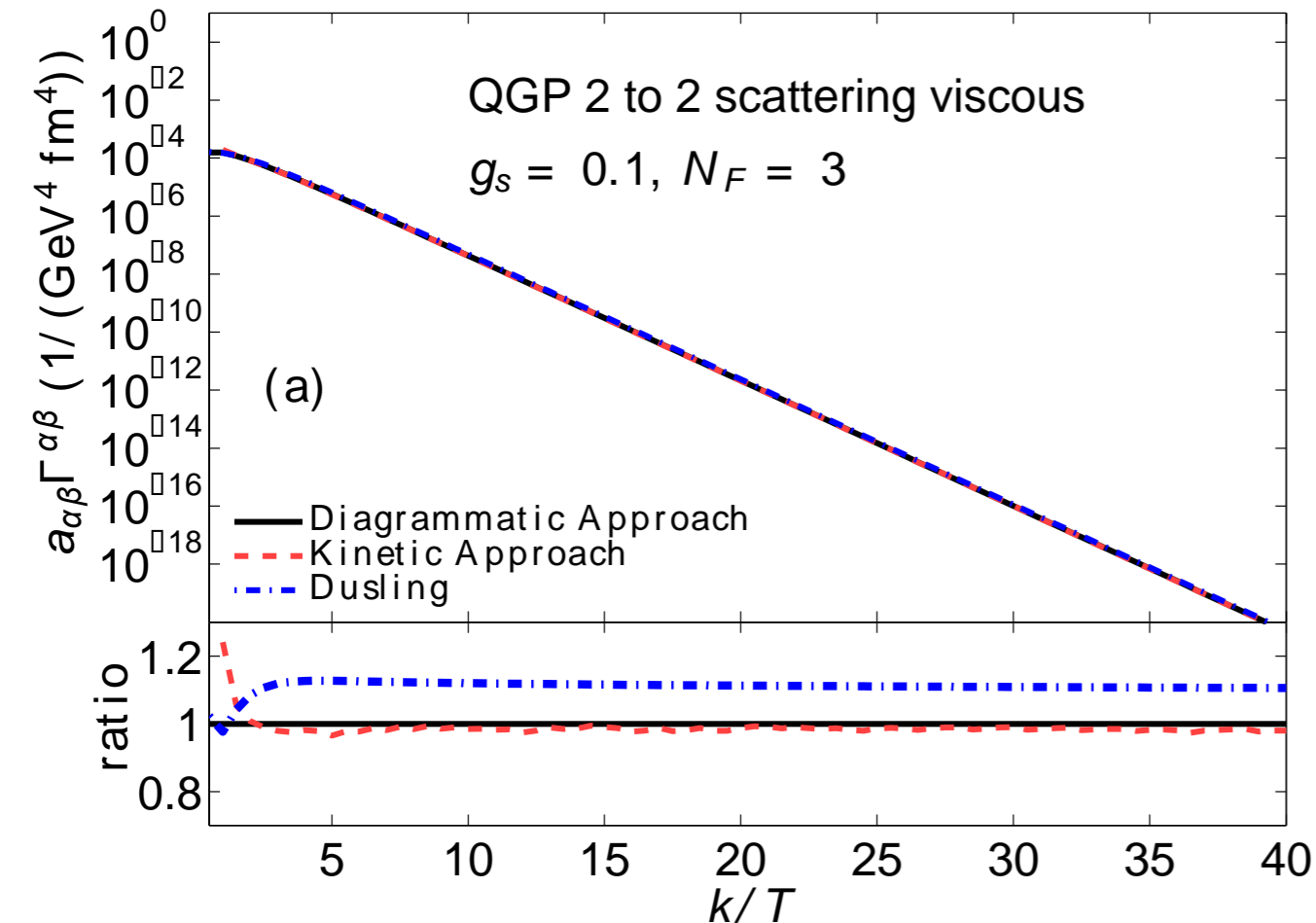
Equilibrium rates:



- For small g , results from diagrammatic approach agree well with kinetic approach and AMY
- For $g = 2.0$, diagrammatic approach gives 25% larger results compared to kinetic approach; difference are due to cut-off dependence.

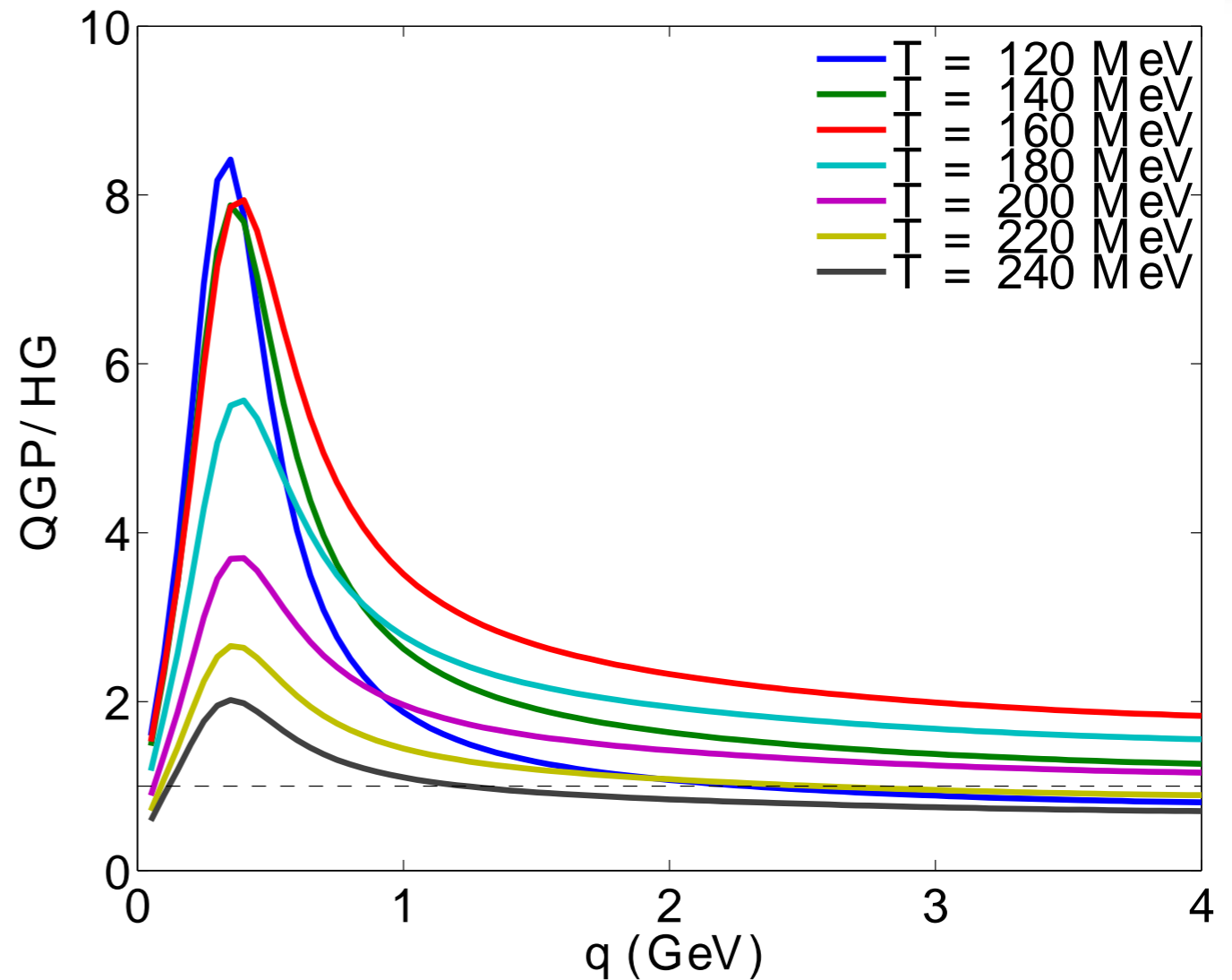
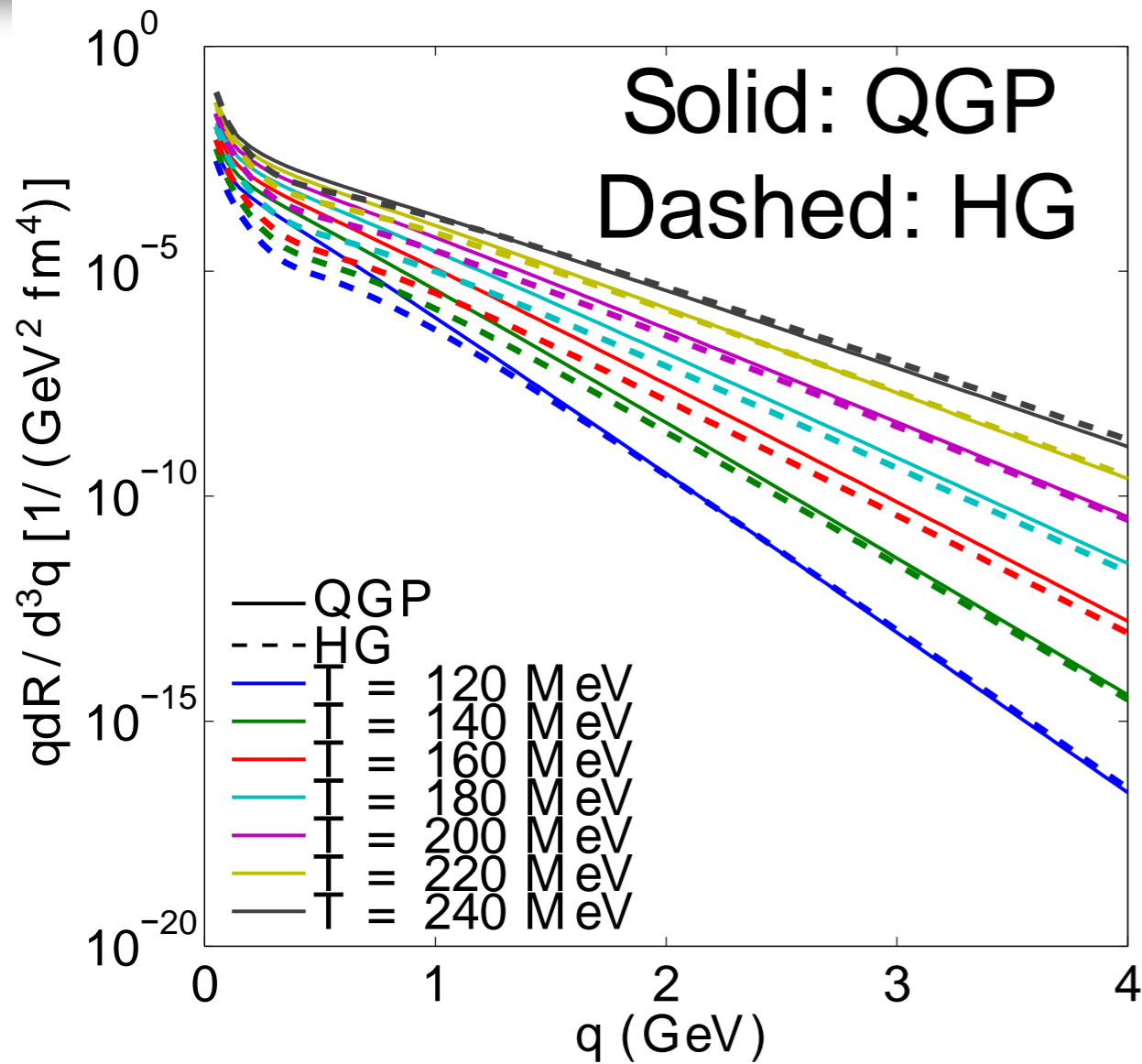
Photon Rates (QGP 2 to 2 processes only)

Viscous corrections:



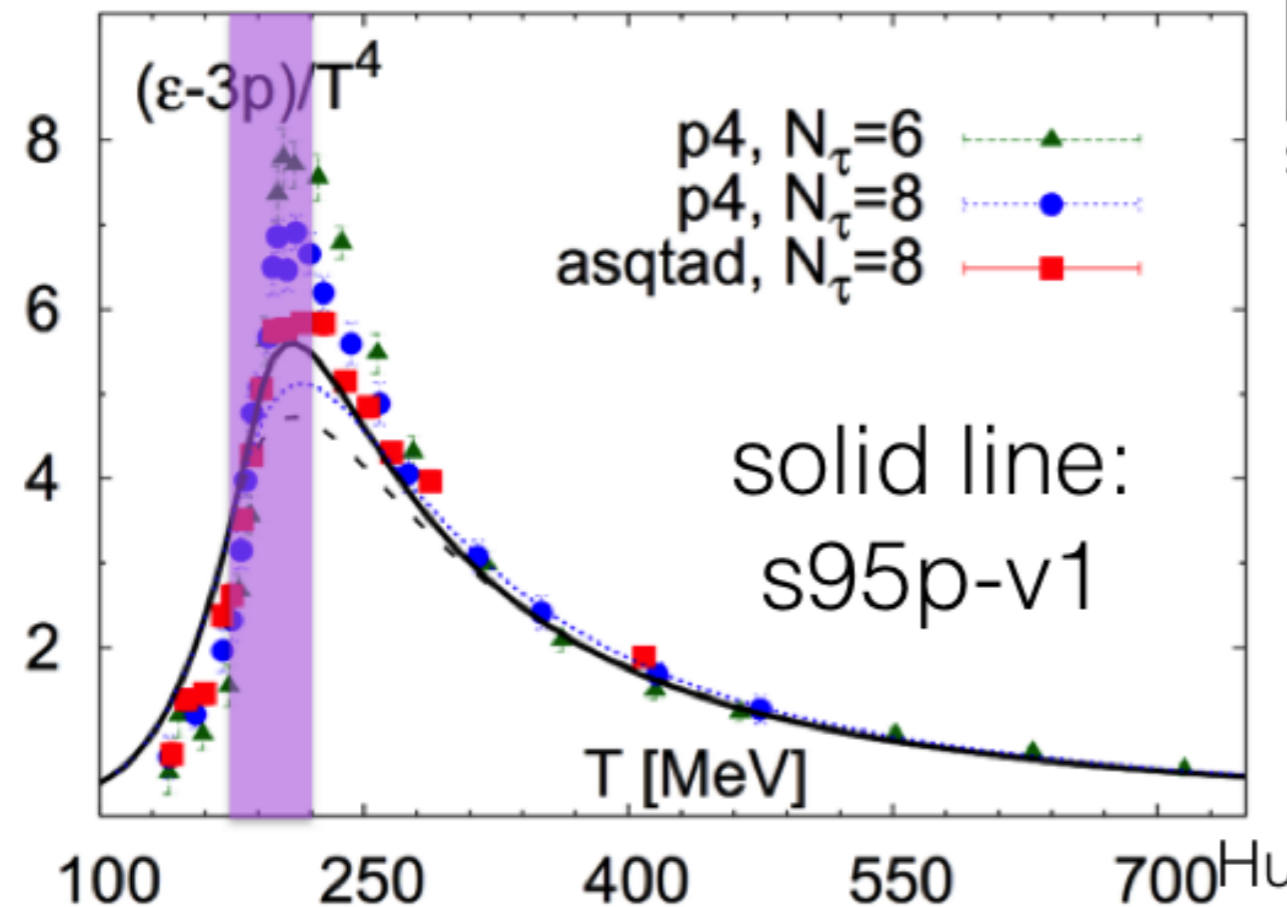
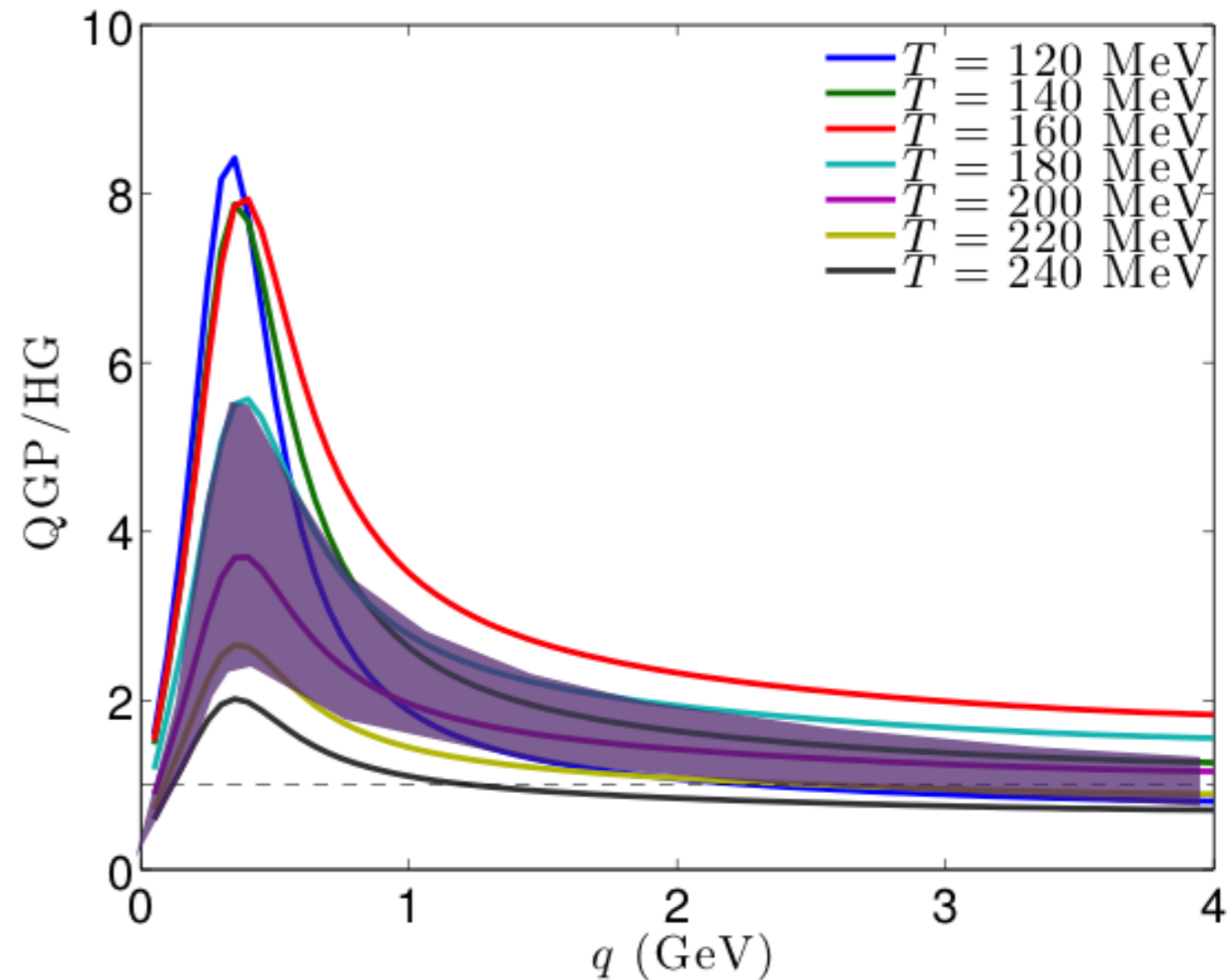
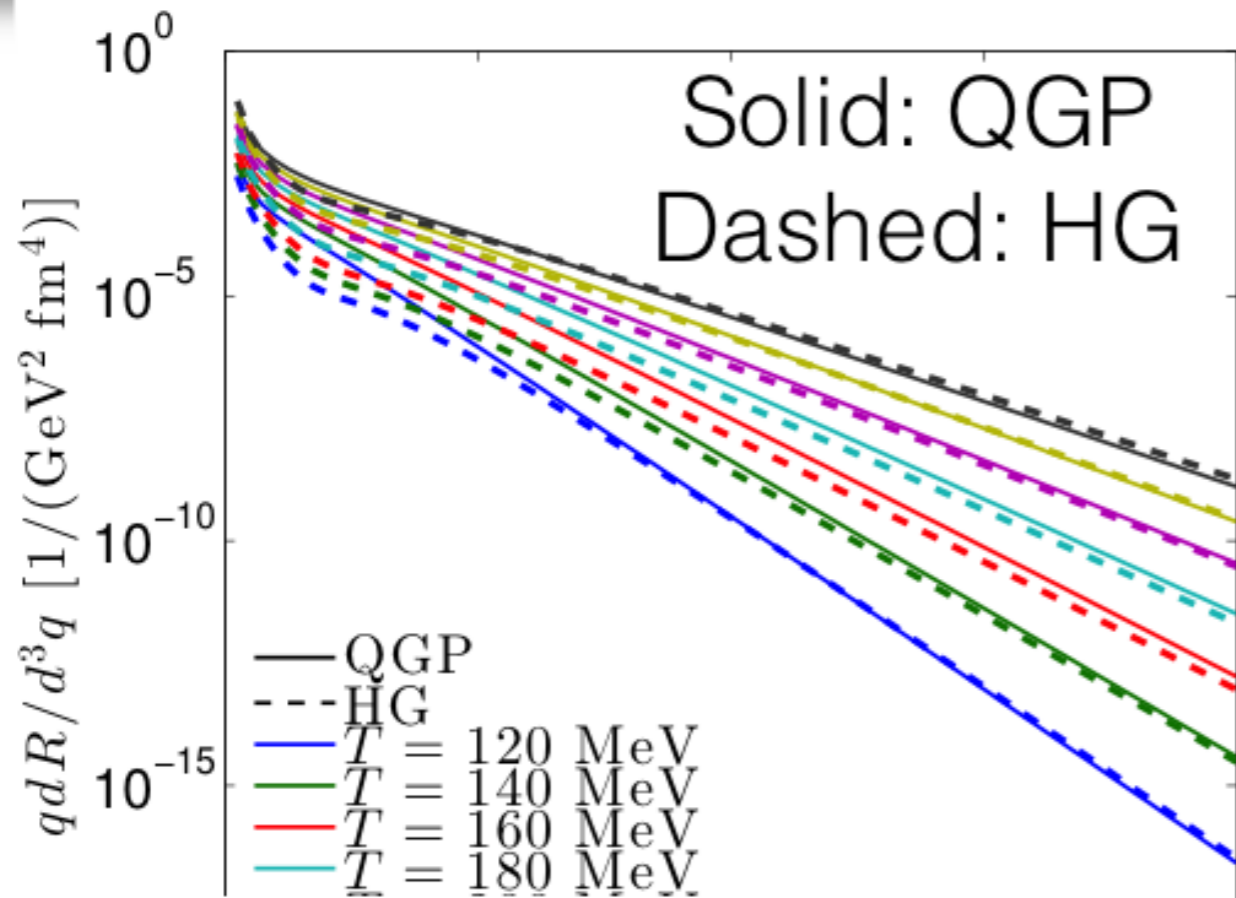
- For small g , diagrammatic approach agrees with kinetic approach
- For $g = 2$, the deviations at small k/T may originate from different higher order $O(g^2 T)$ contributions

Photon Emission Rates QGP vs HG



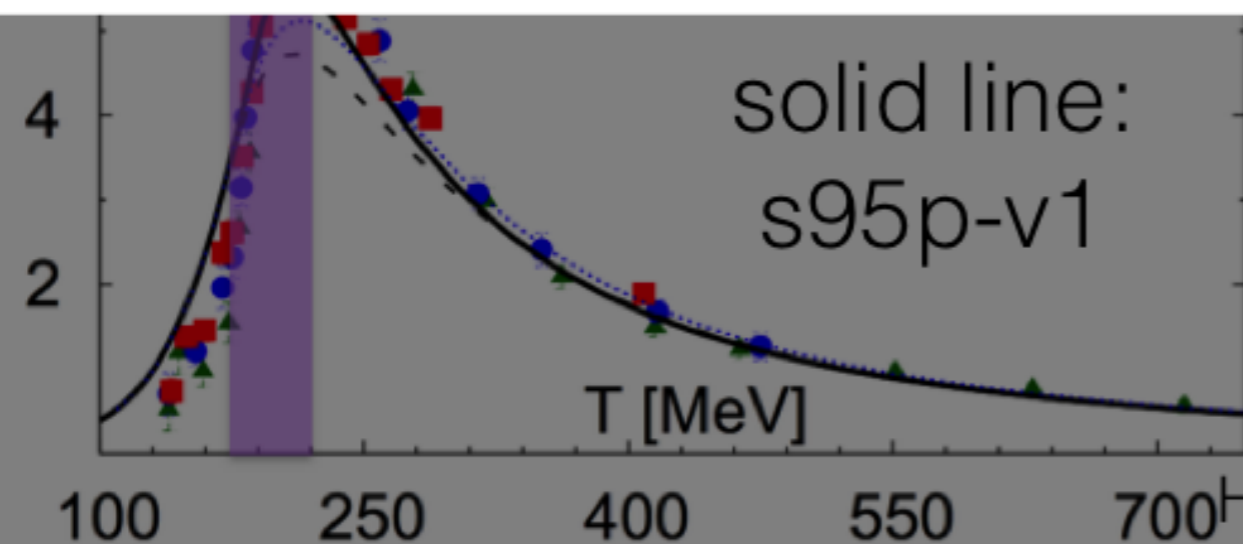
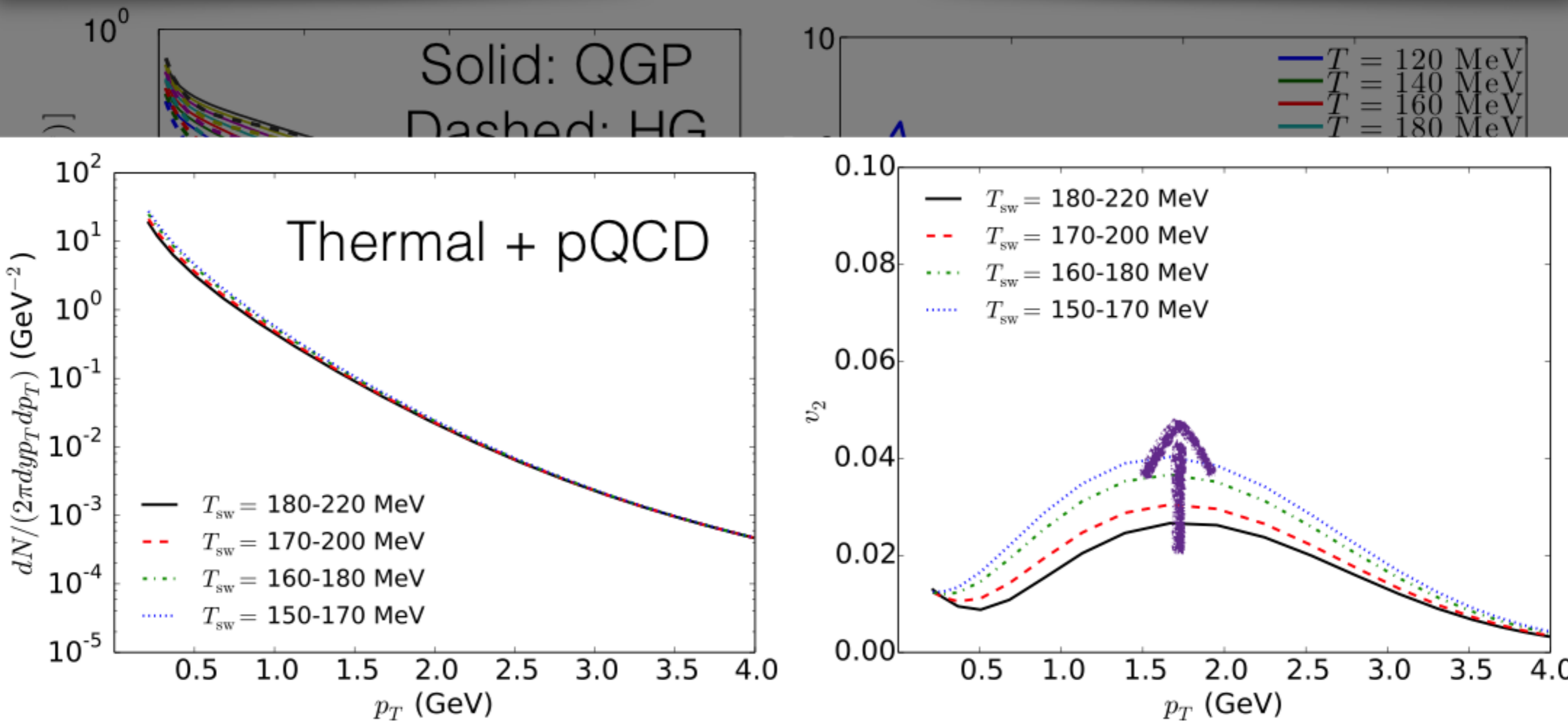
- QGP rates have very different p_T dependence compared to HG rates

Photon Emission Rates QGP vs HG



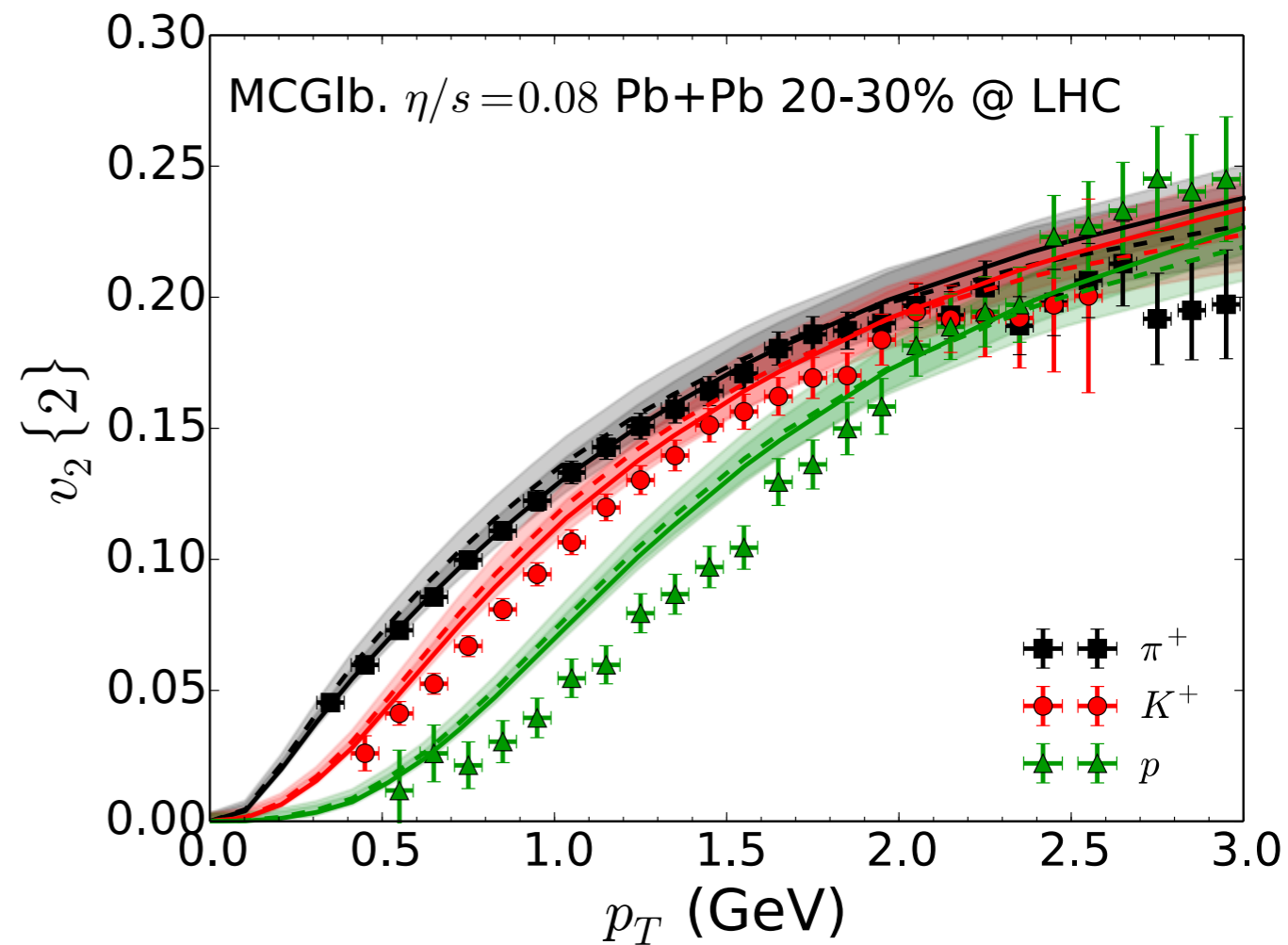
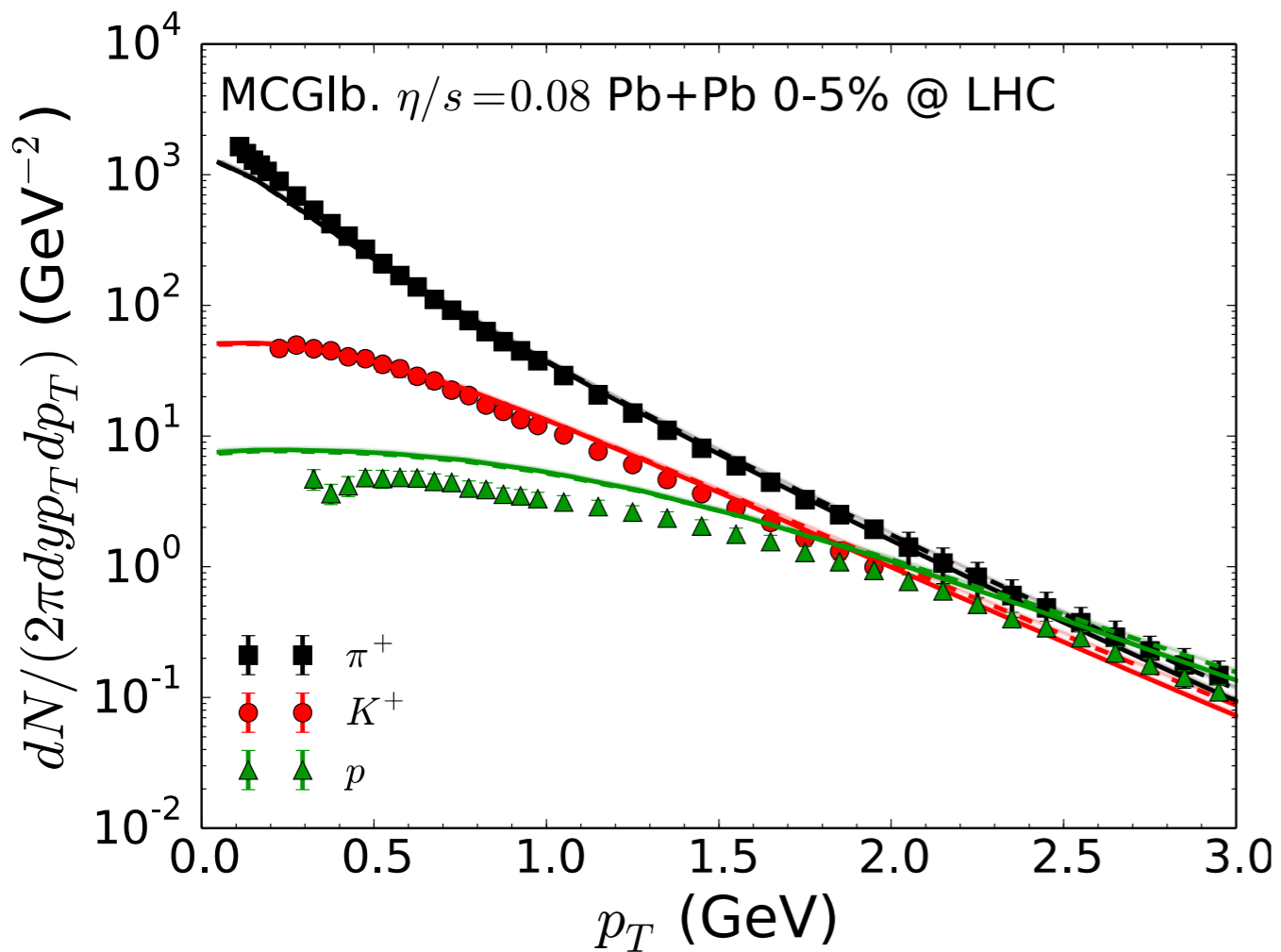
- QGP rates have very different p_T dependence compared to HG rates
- Estimated transition region for production rates,
 $T \sim \mathbf{184 - 220 \text{ MeV}}$

Photon Emission Rates QGP vs HG



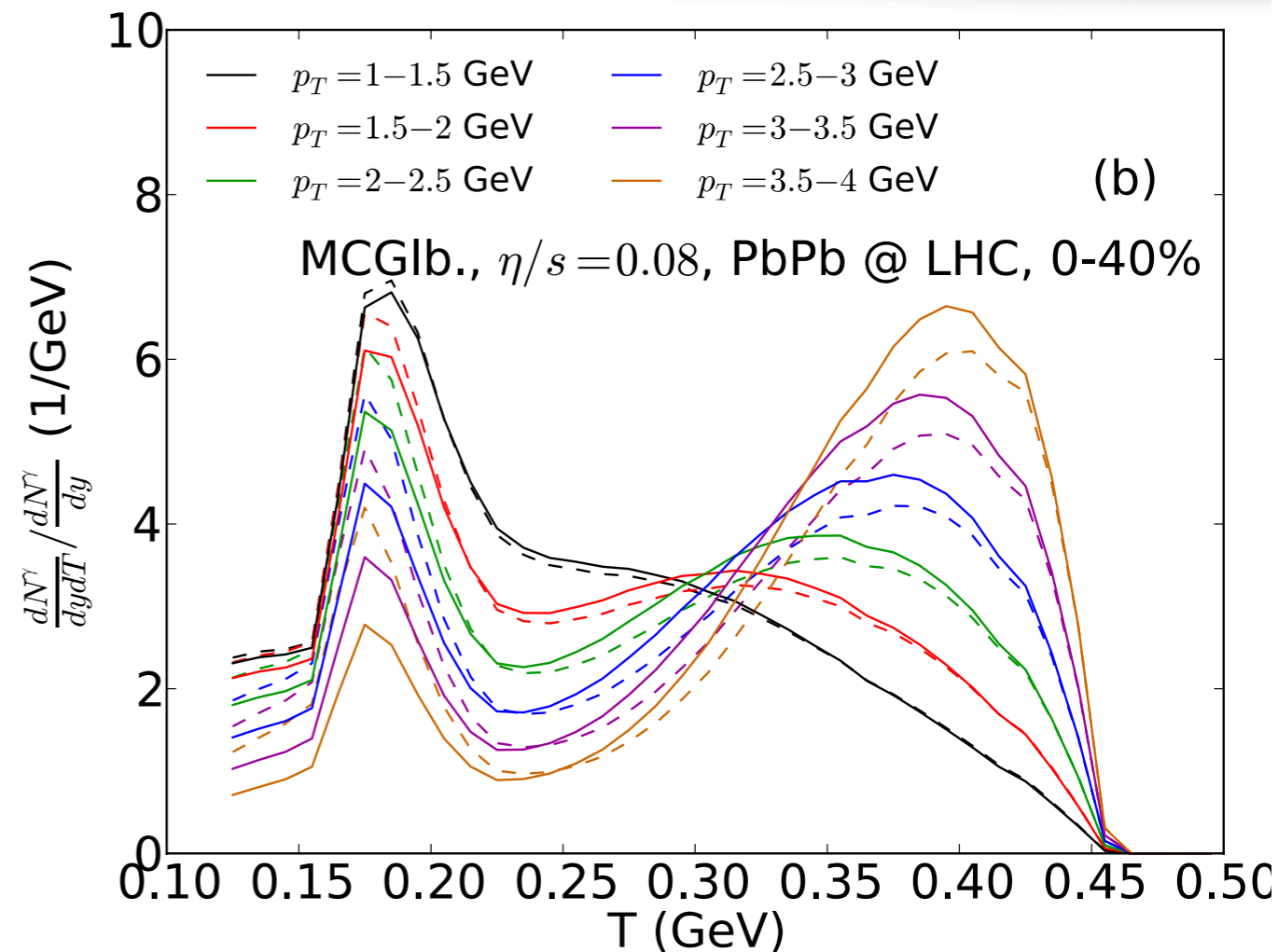
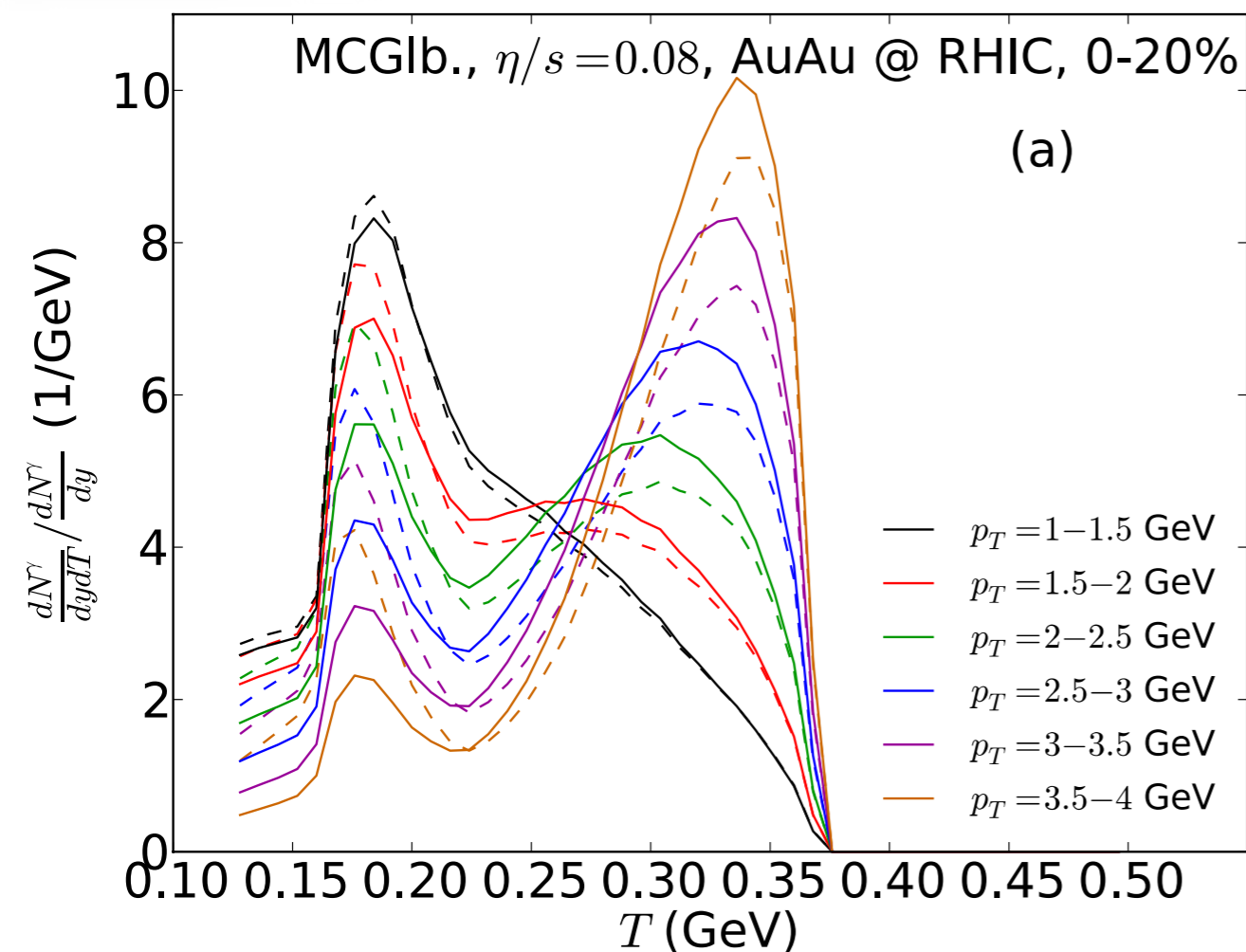
- Estimated transition region for production rates, $T \sim \mathbf{184 - 220}$ MeV

Pre-equilibrium flow effects on hadrons



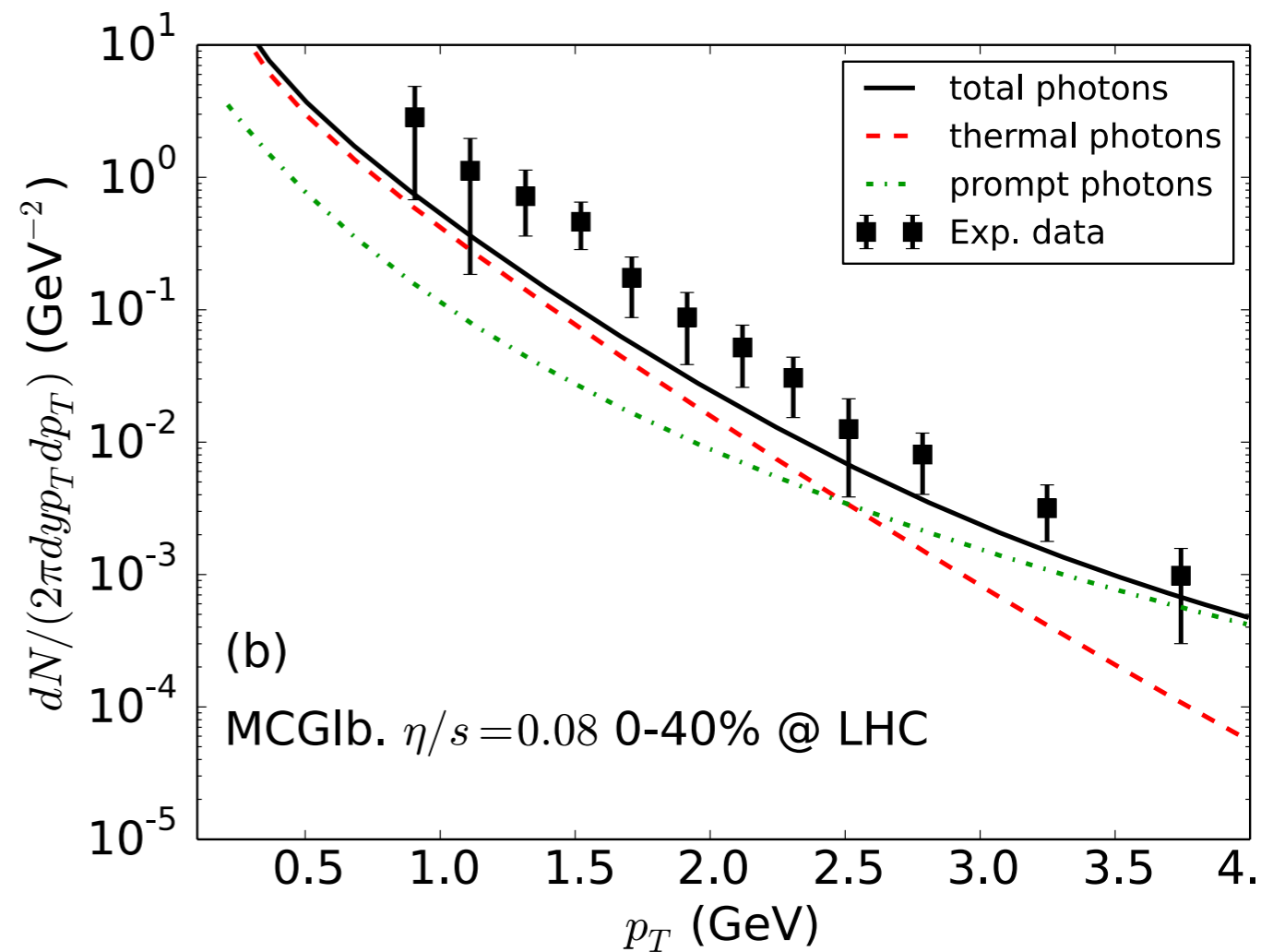
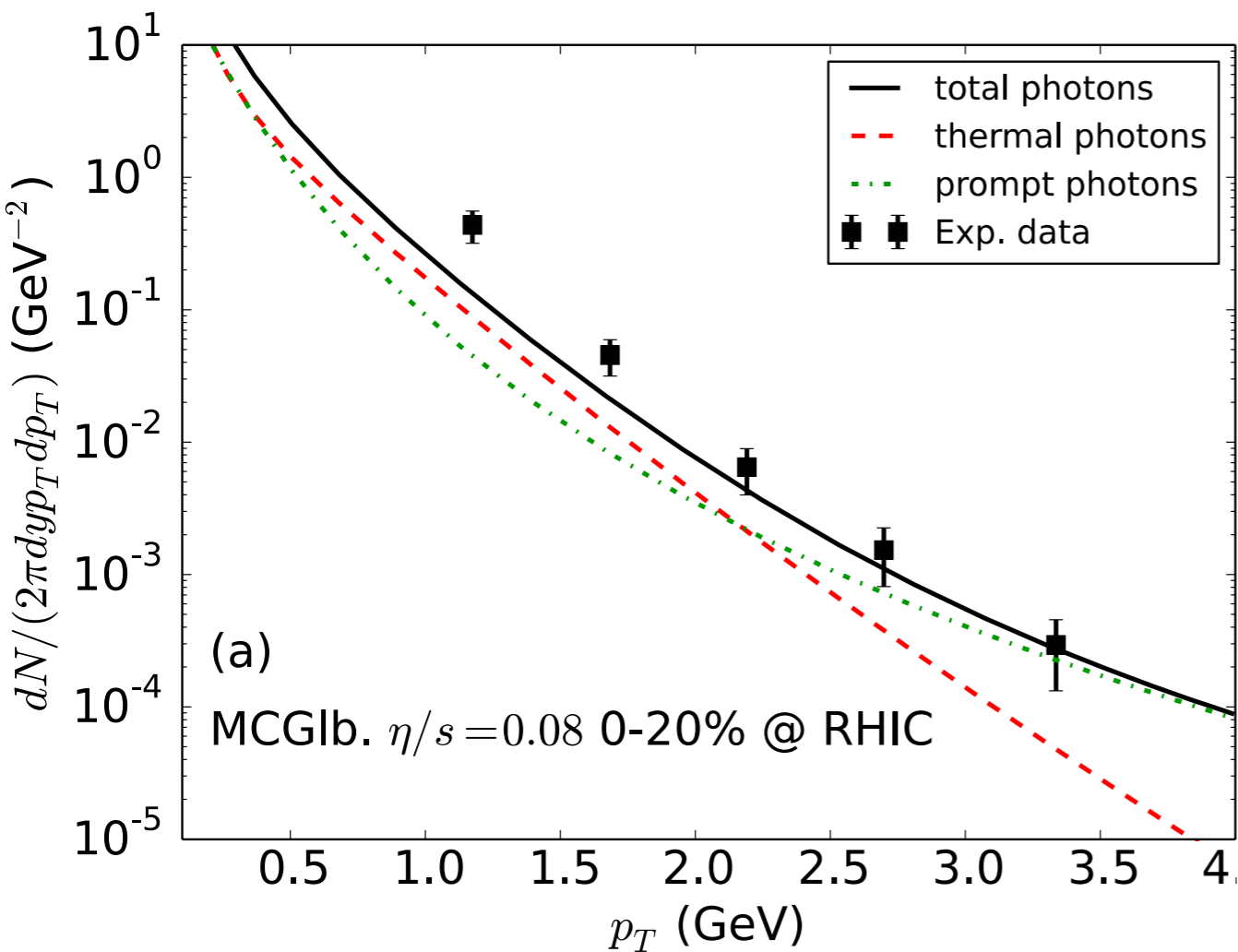
Dashed: with initial flow
Solid: without initial flow

Emission vs. temperature



- High p_T photons are mostly emitted from high temperature region
- Peak photon production around $T = 165-200 \text{ MeV}$ due to large hydrodynamic space-time volume

Thermal Photon Spectra



- With all available thermal emission sources, our current calculations still underestimate measured direct photon spectra at low p_T at both RHIC and LHC energies
- Additional emission sources need to be included to improve the agreement between theory and data

State-of-the-art hydrodynamic modeling

<https://github.com/chunshen1987/iEBE.git>

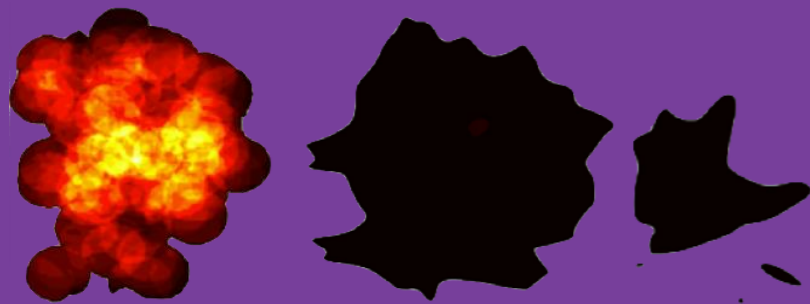
[hen1987/iEBE.git](https://github.com/chunshen1987/iEBE.git)



Initial Condition Generators
(MC-KLN, MC-Glauber)

Thermal Photon
Emission Rates

Hydrodynamic
Simulations (VISH2+1)



HydroInfo

**e-b-e
VISHNU**

$u^\mu, \pi^{\mu\nu}$

Thermal Photon
Interface

$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\pi^{\mu\nu} q_\mu q_\nu}{2(e+p)} a_{\alpha\beta} \Gamma^{\alpha\beta}$$

$$E \frac{dN^\gamma}{d^3p} = \int d^4x q \frac{dR}{d^3q}$$

UrQMD

Hadrons spectra & v_n

Photon spectrum & v_n

State-of-the-art hydrodynamic

modeling

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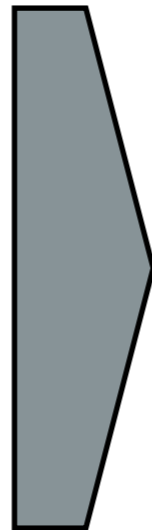
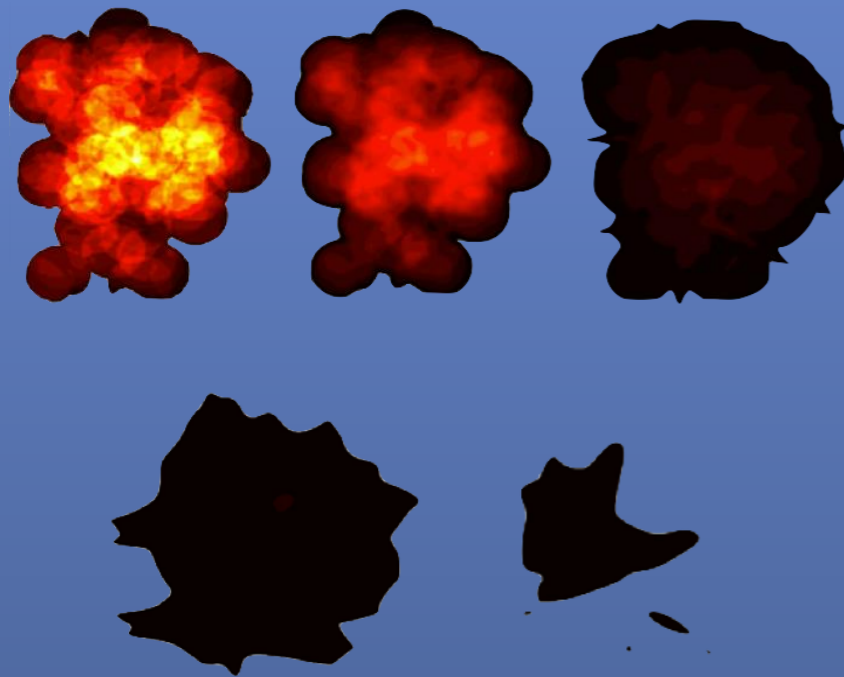
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HydroInfo
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Hadrons spectra & v_n



Your own
Jet
Quenching
or Heavy
Quark
Package