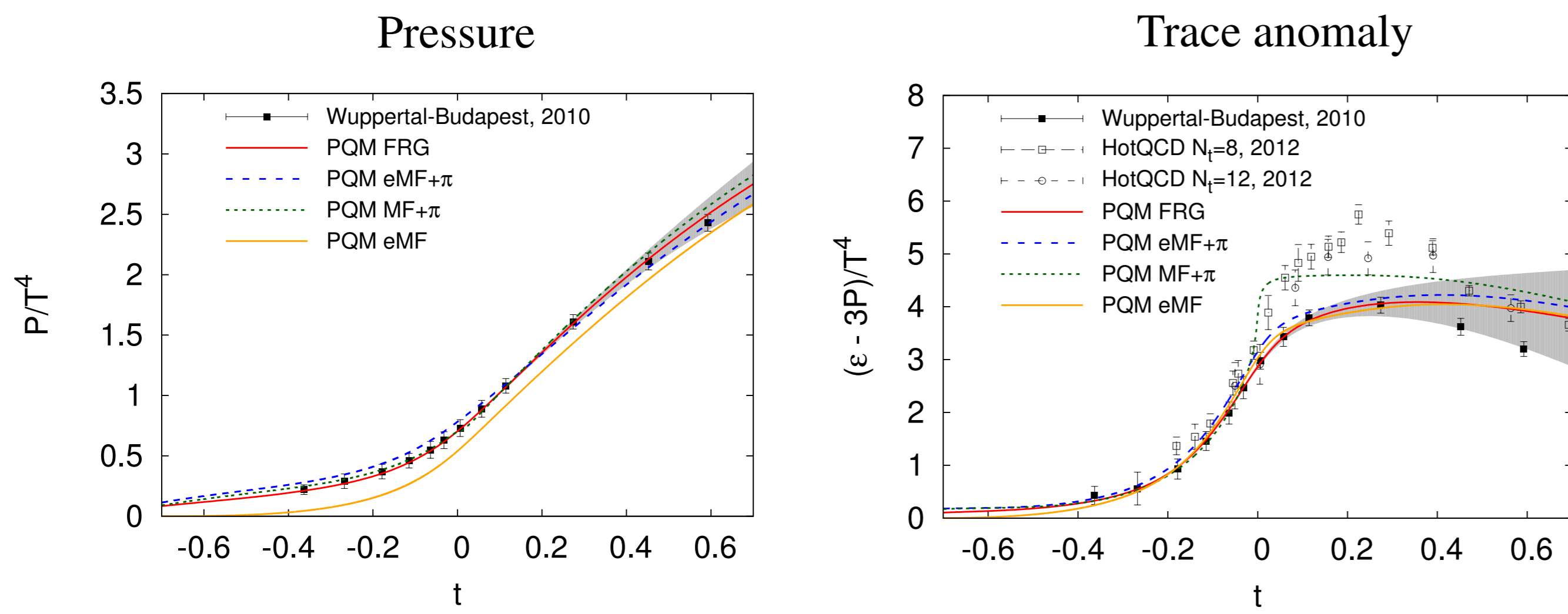
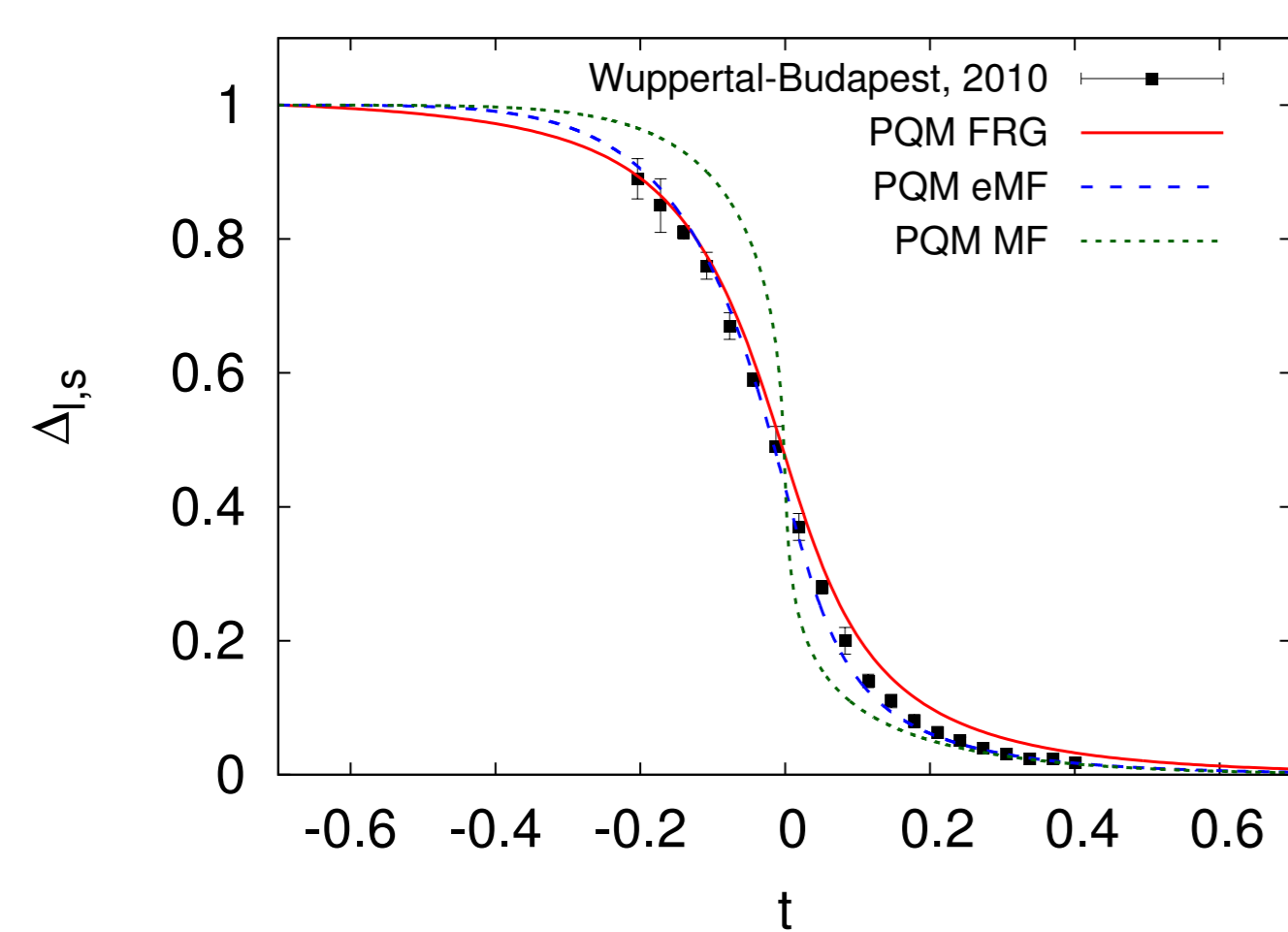


## Thermodynamics [1]



- perfect agreement of pressure and trace anomaly with lattice QCD data
- larger temperatures: need additional unquenching effects and meson suppression

## QCD crossover [1]



- perfect agreement with data from lattice QCD simulations
- subtracted condensate:

$$\Delta_{l,s} = \frac{\left(\langle\sigma_l\rangle - \frac{c_l}{c_s}\langle\sigma_s\rangle\right)_T}{\left(\langle\sigma_l\rangle - \frac{c_l}{c_s}\langle\sigma_s\rangle\right)_{T=0}}$$

- reduced temperature  $t = (T - T_c)/T_c$

## Fluctuations and nonperturbative dynamics: Functional Renormalization Group Equation (FRG)

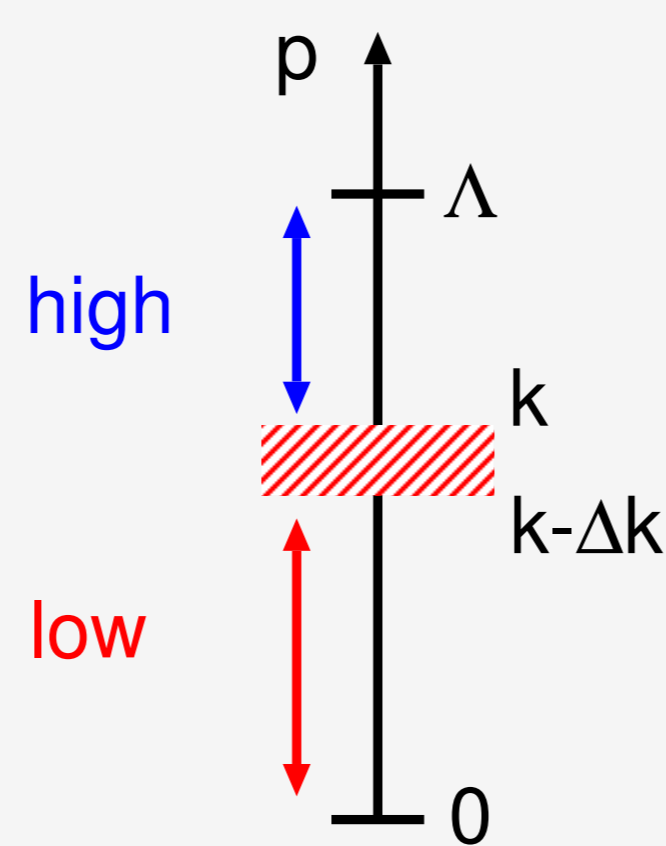
$$\partial_t \Gamma_k[\phi] = \frac{1}{2} \left( \text{loop diagrams} \right)$$

- connects bare action  $\Gamma_\Lambda[\phi] = S[\phi]$  with full effective action

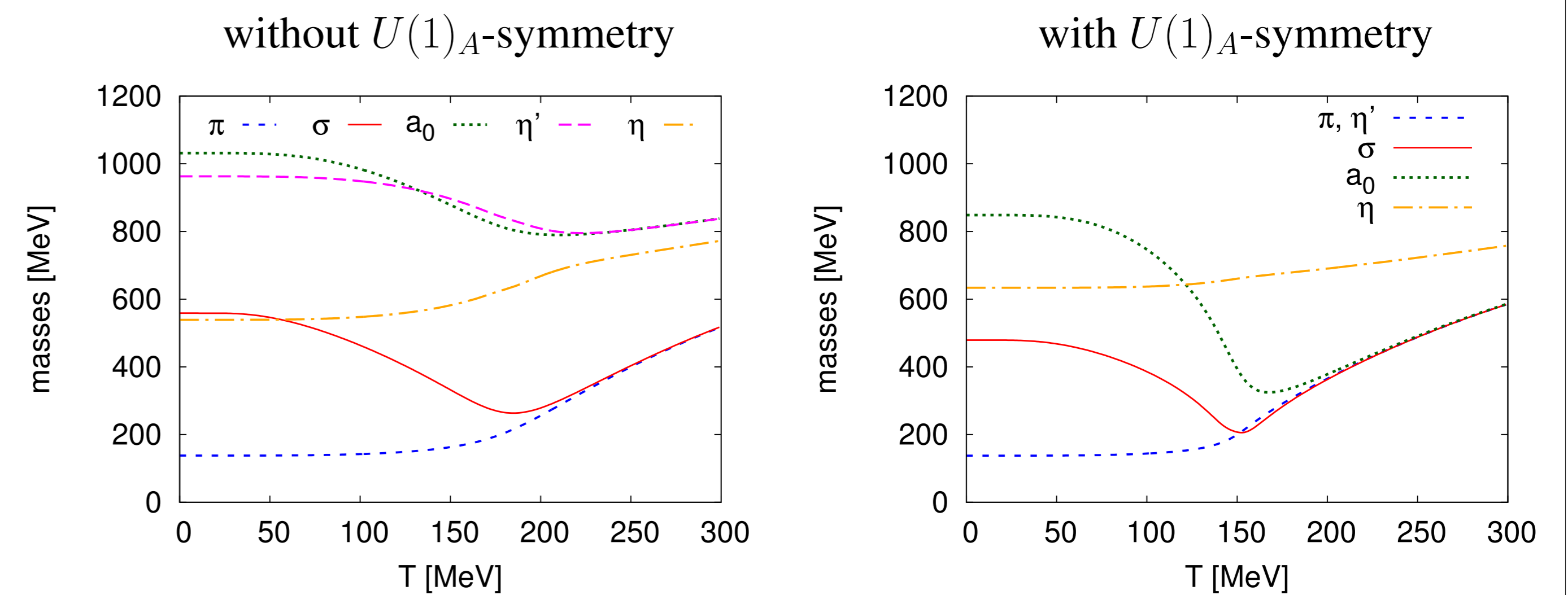
$$\Gamma[\phi] = \lim_{k \rightarrow 0} \Gamma_k[\phi]$$

via momentum-shell integration.

- nonperturbative equation: full field-dependent propagators
- integrates thermal as well as quantum fluctuations
- comparison with (extended) mean-field results: (e)MF



## $\eta'$ -meson mass at chiral transition [2]



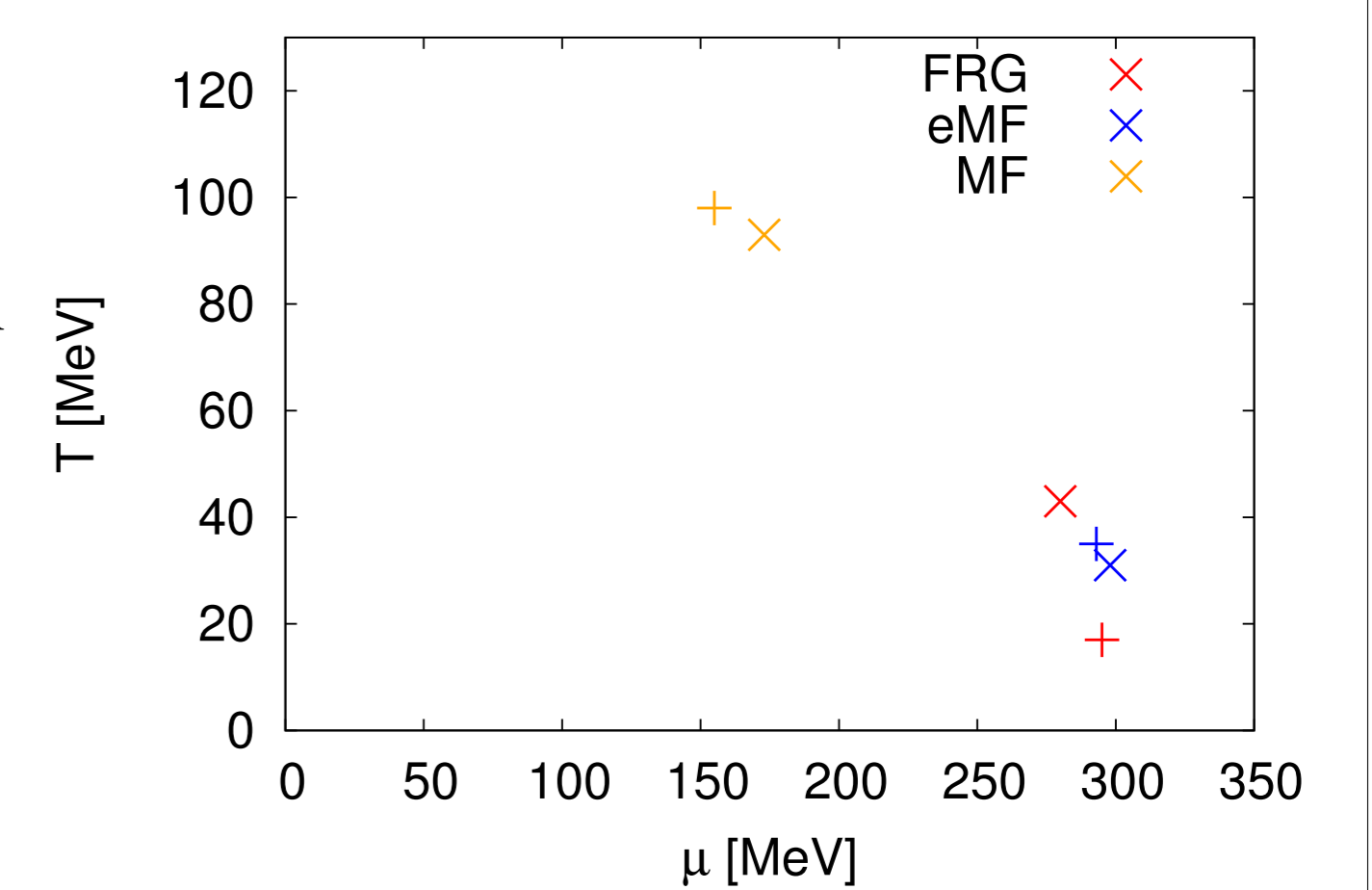
- drop in (screening) mass of  $\eta'$  meson due to melting of light condensate
- consistent with indirect measurements [3]

## Critical point: fluctuations and chiral anomaly [2]

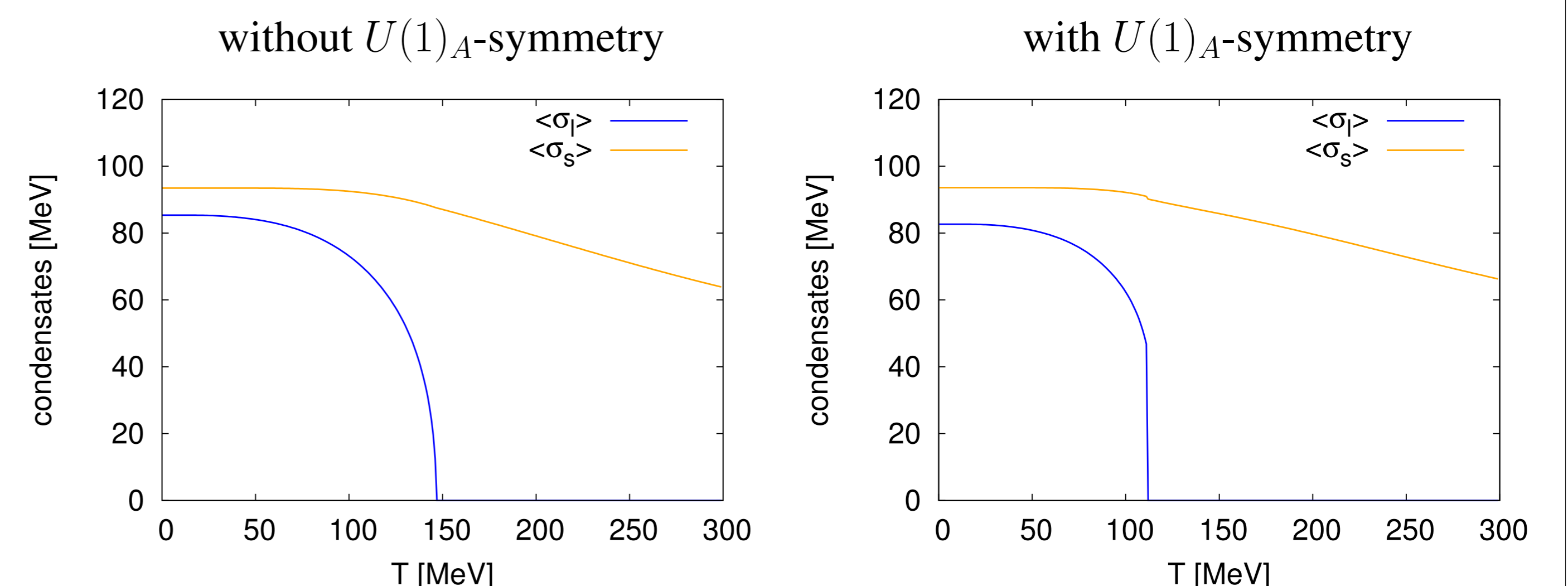
- chiral anomaly with full fluctuations: stronger effect on critical point location
- with anomaly: effect of fluctuations as in two-flavor QM-model with  $\sigma, \vec{\pi}$  mesons

× without  $U(1)_A$  symmetry

+ with  $U(1)_A$  symmetry



## Order of transition for $m_l \rightarrow 0$ [2]



- second-order transition in  $O(4)$  universality class without  $U(1)_A$  symmetry
- first-order transition with  $U(1)_A$  symmetry
- consistent with two-flavor dominated dynamics [4]
- inclusion of mesonic fluctuations (FRG) crucial

## Low-energy effective description: quarks and mesons with 2 + 1 flavors

### (De-)Confinement dynamics (PQM):

- effective Polyakov Loop potential  $\mathcal{U}(\Phi)$  with

$$\Phi = \langle \text{tr} \mathcal{P} \exp[ig \int_0^\beta A_0] \rangle / N_c$$

- dynamical quark effects parametrized with linear rescaling  $t_{YM}(t_{QCD})$  [5, 6]

$$\mathcal{U}_{QCD}(t_{QCD}) \equiv \mathcal{U}_{YM}(t_{YM}(t_{QCD}))$$

- very good approximation close to  $T_c$ , [cf. poster R. Stiele]

### Quark-Meson Model (QM):

$$\mathcal{L}_{QM} = \bar{q} \left( \partial_\mu \gamma_\mu + h (\sigma^a + i \gamma_5 \pi^a) \frac{\lambda_a}{2} \right) q + \text{tr} [\partial_\mu \Sigma^\dagger \partial_\mu \Sigma] + U(\Sigma, \xi) + (\text{expl. symmetry breaking})$$

- $\Sigma$ :  $SU(3)$  mesonic field matrix,  $\lambda_a$ : Gell-Mann matrices
- Yukawa type interaction  $h$  between quarks and mesons
- $U(1)_A$ -symmetry breaking via Kobayashi-Maskawa-'t Hooft determinant [7], [8]

$$\xi = \det(\Sigma) + \det(\Sigma^\dagger)$$

## References

- [1] T. K. Herbst, M. Mitter, J. M. Pawłowski, B.-J. Schaefer, and R. Stiele, Phys.Lett. **B731**, 248 (2014).
- [2] M. Mitter and B.-J. Schaefer, Phys.Rev. **D89**, 054027 (2014).
- [3] T. Csorgo, R. Vertesi, and J. Sziklai, Phys.Rev.Lett. **105**, 182301 (2010).
- [4] R. D. Pisarski and F. Wilczek, Phys.Rev. **D29**, 338 (1984).
- [5] J. Braun, L. M. Haas, F. Marhauser, and J. M. Pawłowski, Phys.Rev.Lett. **106**, 022002 (2011).
- [6] L. M. Haas, R. Stiele, J. Braun, J. M. Pawłowski, and J. Schaffner-Bielich, Phys.Rev. **D87**, 076004 (2013).
- [7] M. Kobayashi and T. Maskawa, Prog.Theor.Phys. **44**, 1422 (1970).
- [8] G. 't Hooft, Phys.Rev.Lett. **37**, 8 (1976).

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