

XXIV QUARK MATTER  
DARMSTADT 2014

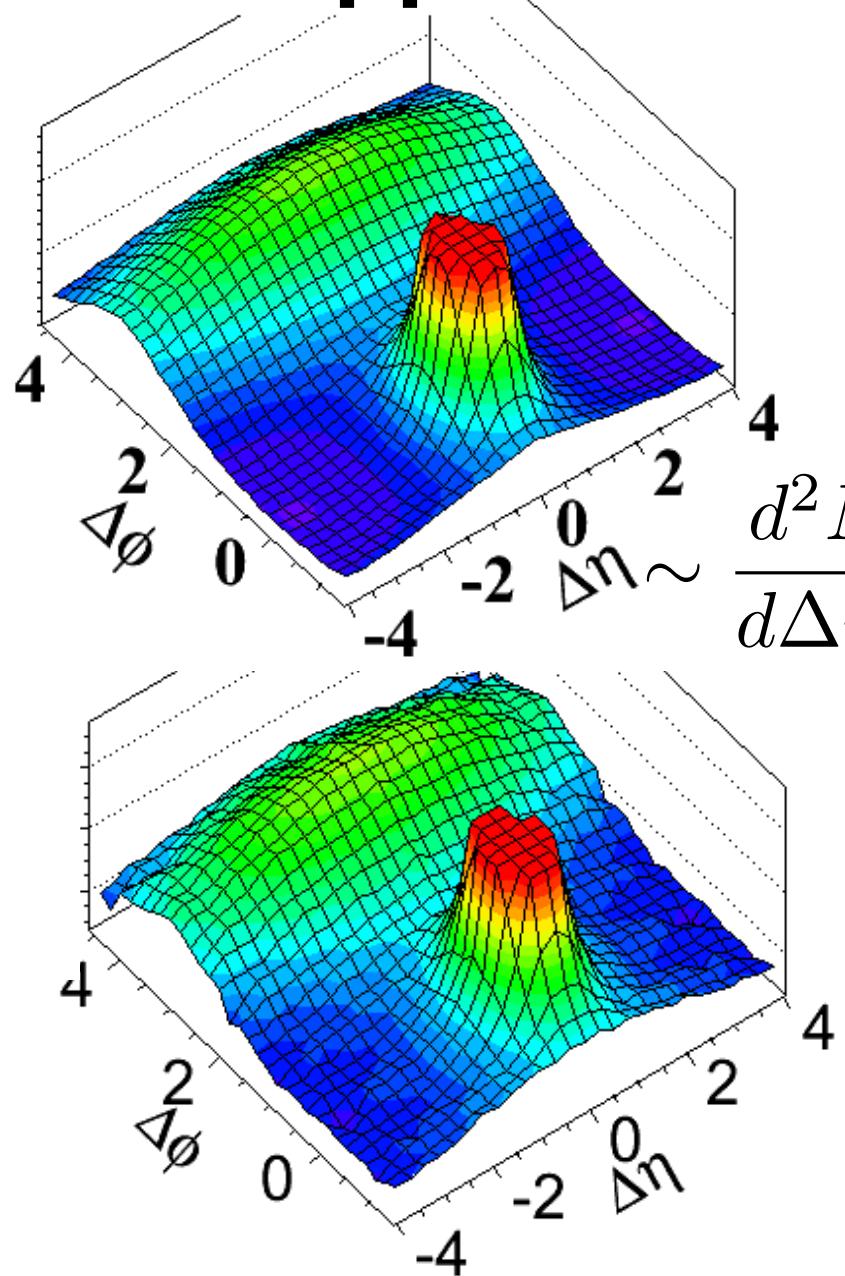
# Signatures of collective behavior in small collision systems

**I. Kozlov**, M. Luzum, G. Denicol, S. Jeon, C. Gale (1405.3976)

McGill, LBNL

CMS 1305.0609

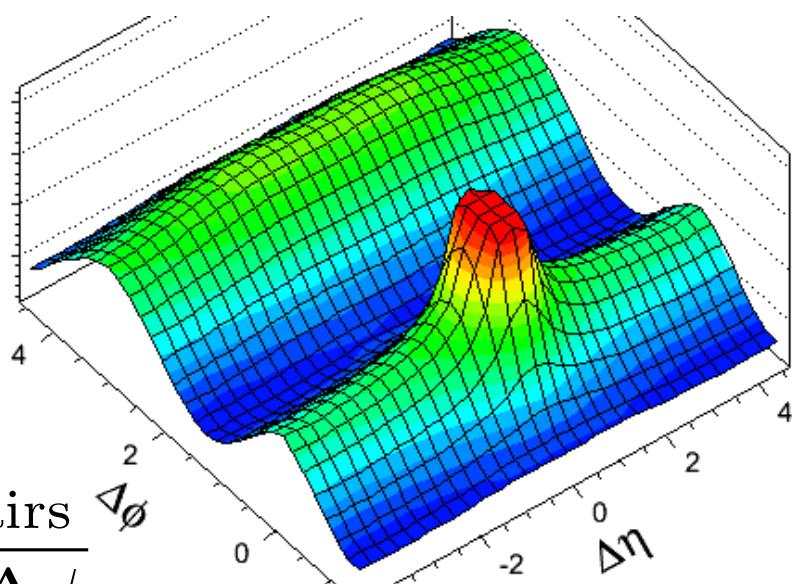
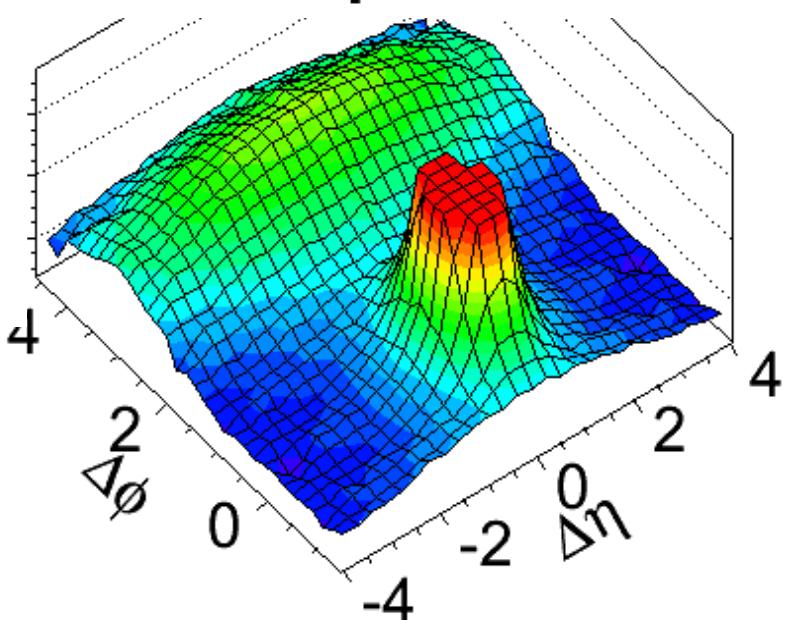
**pp**



Motivation

**PbPb**

$$\frac{d^2 N_{\text{pairs}}}{d\Delta\eta d\Delta\phi}$$



**pPb low multiplicity**

**pPb high multiplicity**

# Are particle azimuthal anisotropies due to hydro?

CMS 1305.0609

- Check whether experimental data can be described with hydrodynamics
- Introduce a more stringent test on hydrodynamics (observable  $\gamma_n$ ), which gives another handle to explore HIC
- Use MUSIC: Schenke, Jeon & Gale, PRL 106 (2011)

pPb low multiplicity

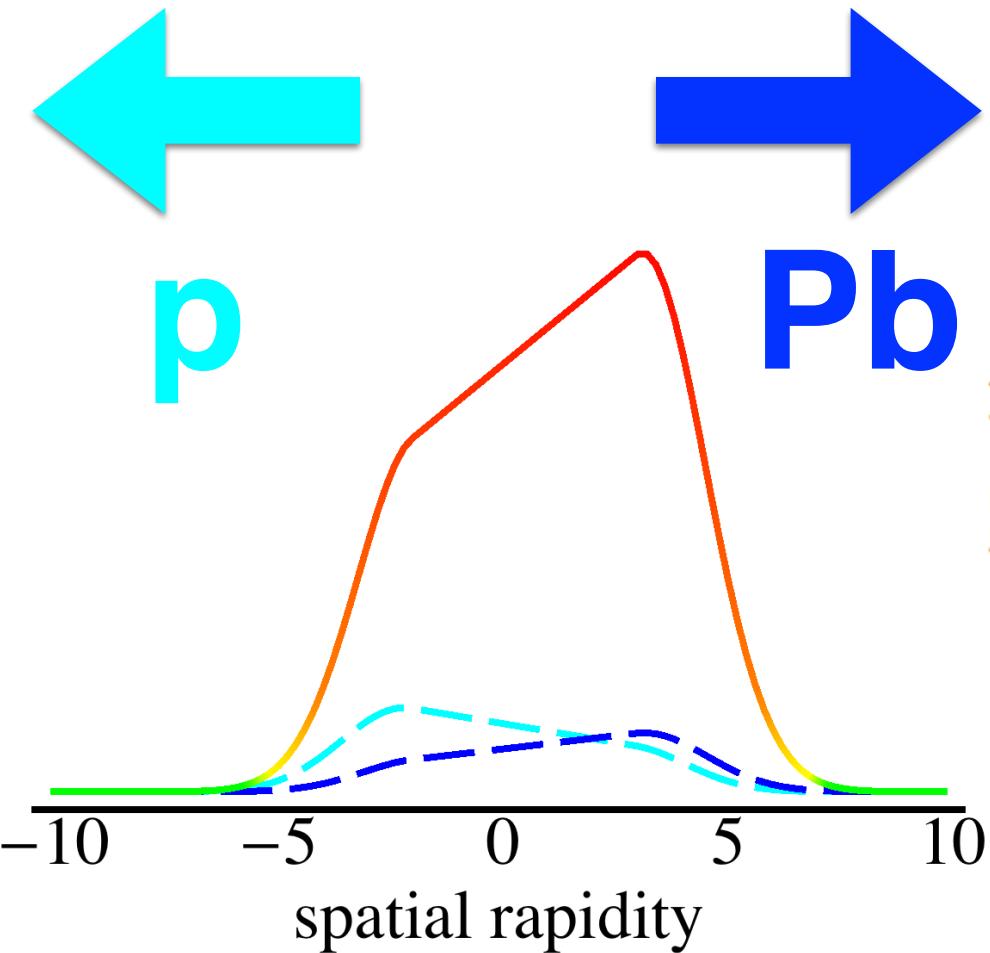
pPb high multiplicity

# Glauber + rapidity distribution

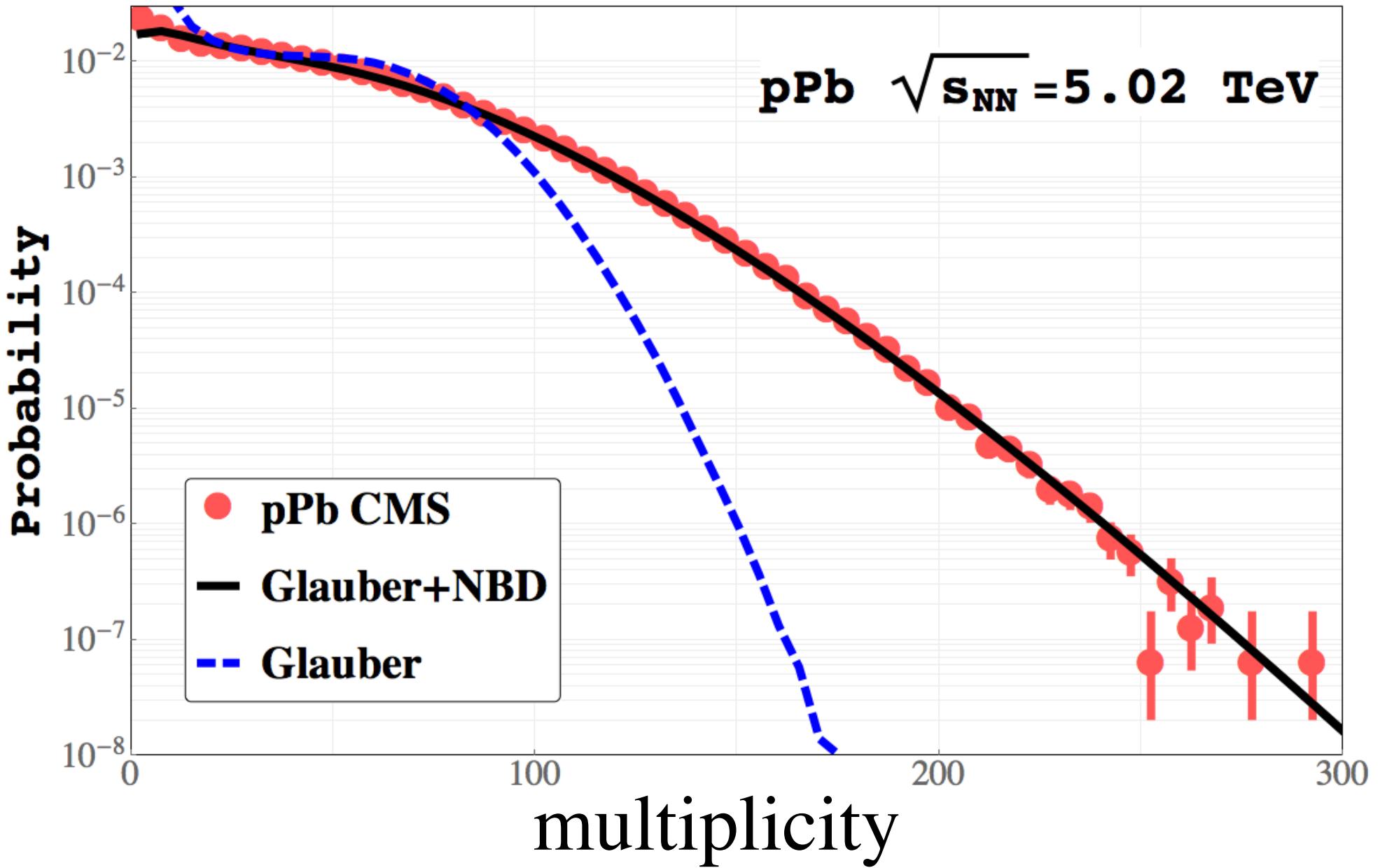
initial entropy profile



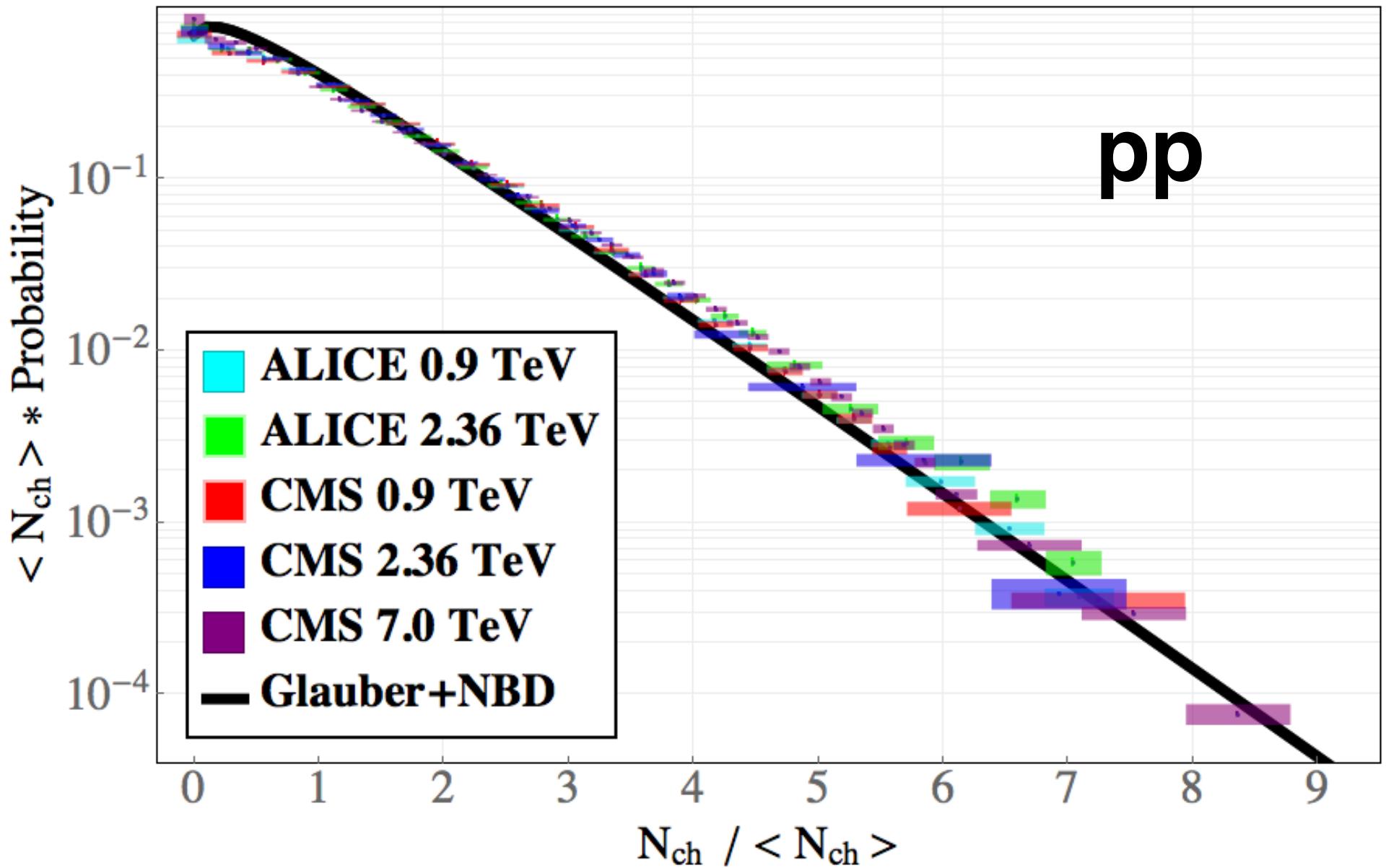
final multiplicity profile



# Glauber+NBD

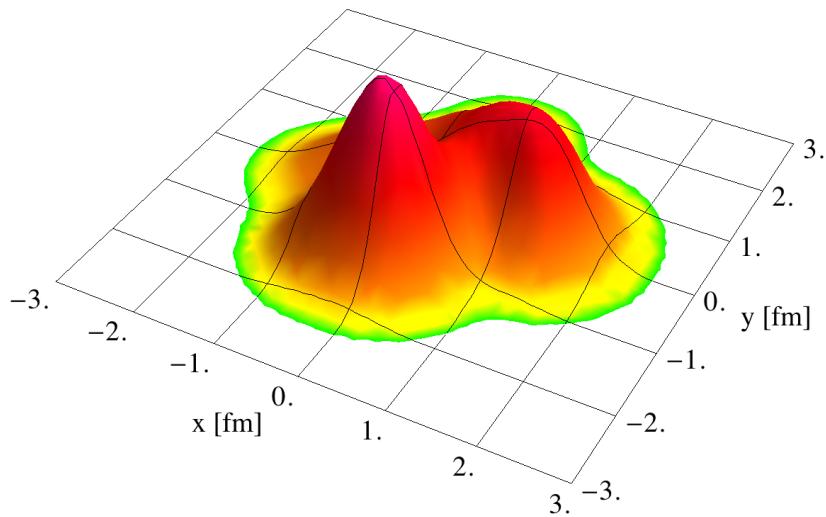


# pp multiplicity with **Glauber+NBD**

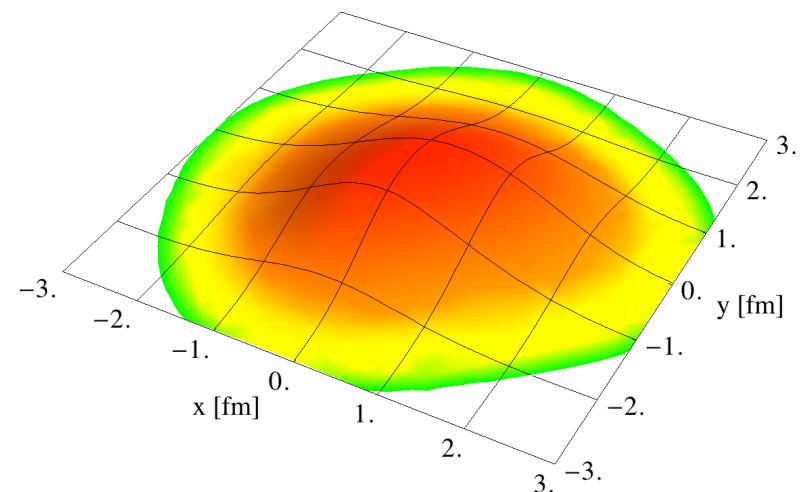


# Transverse granularity

$$\sigma = 0.40 \text{ fm}$$



$$\sigma = 0.80 \text{ fm}$$



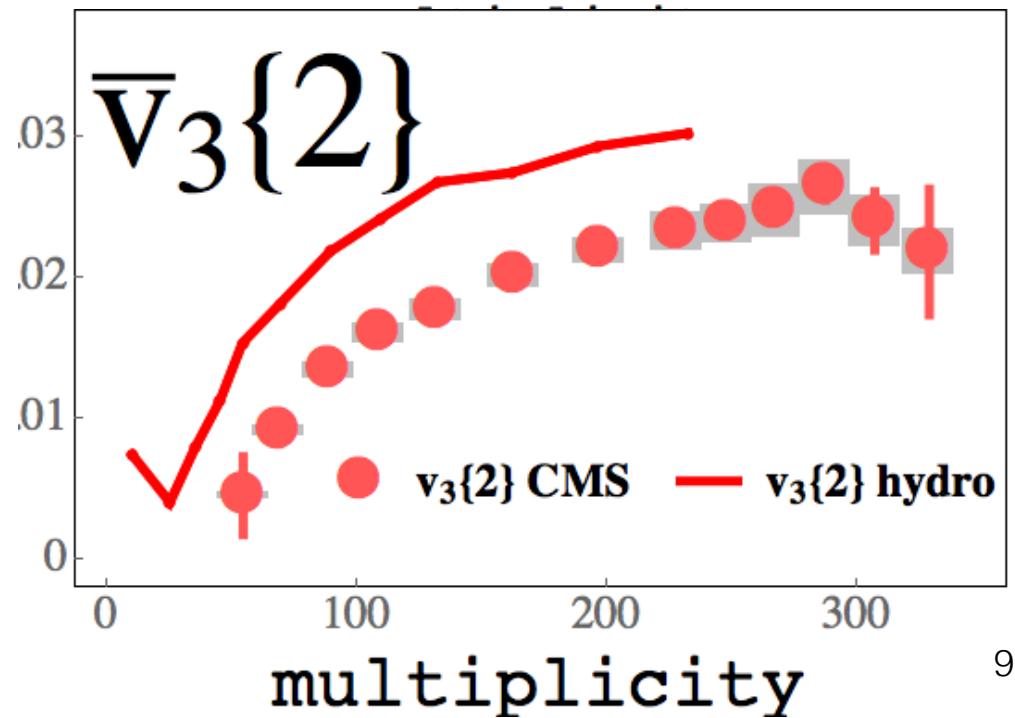
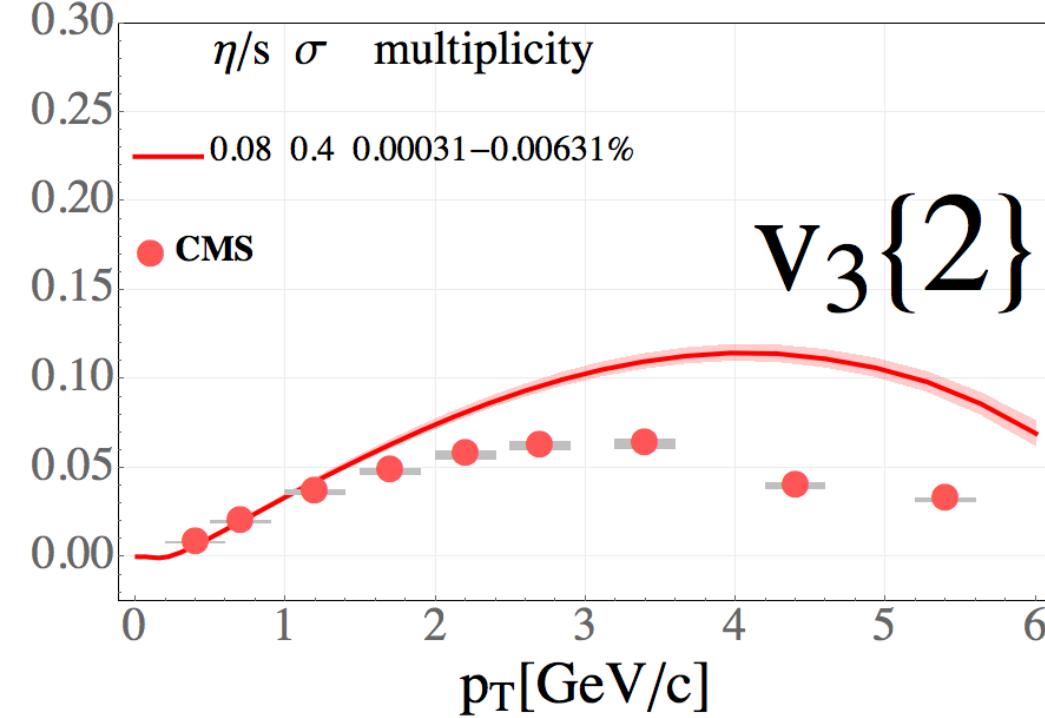
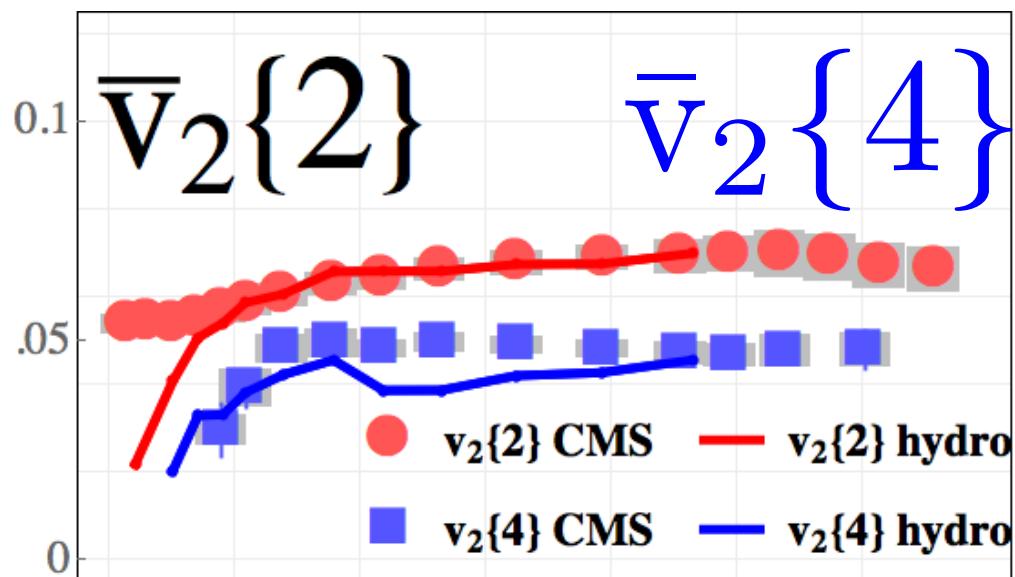
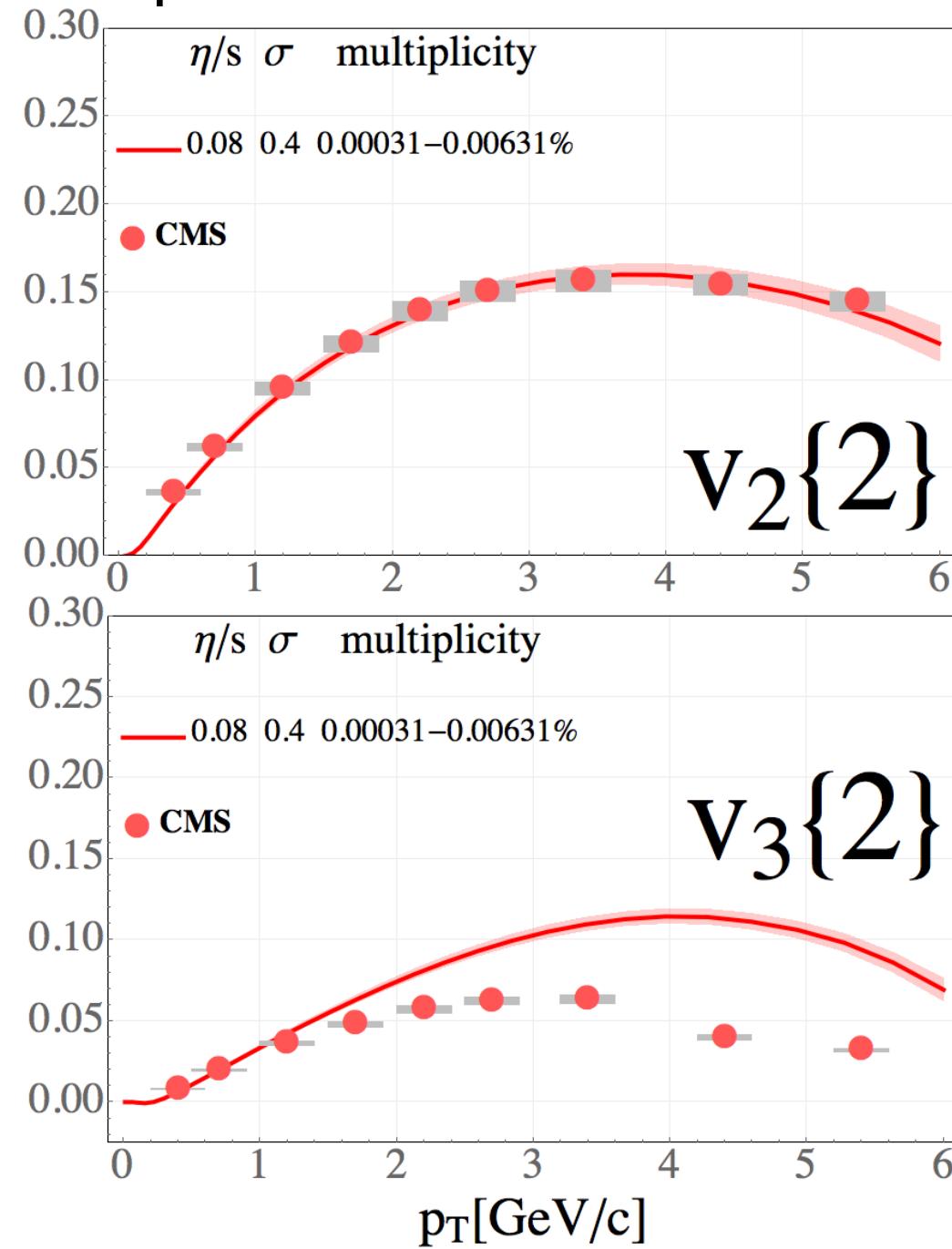
Compare with hydro; start with:

$$\sigma = 0.4 \text{ fm} \quad \eta/s = 0.08$$

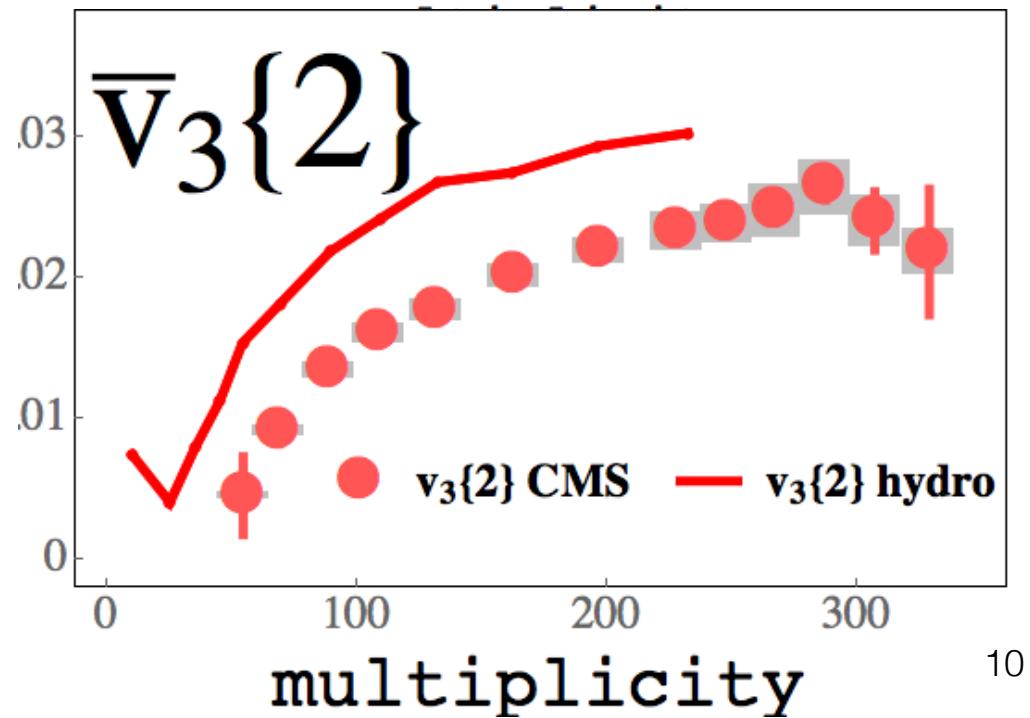
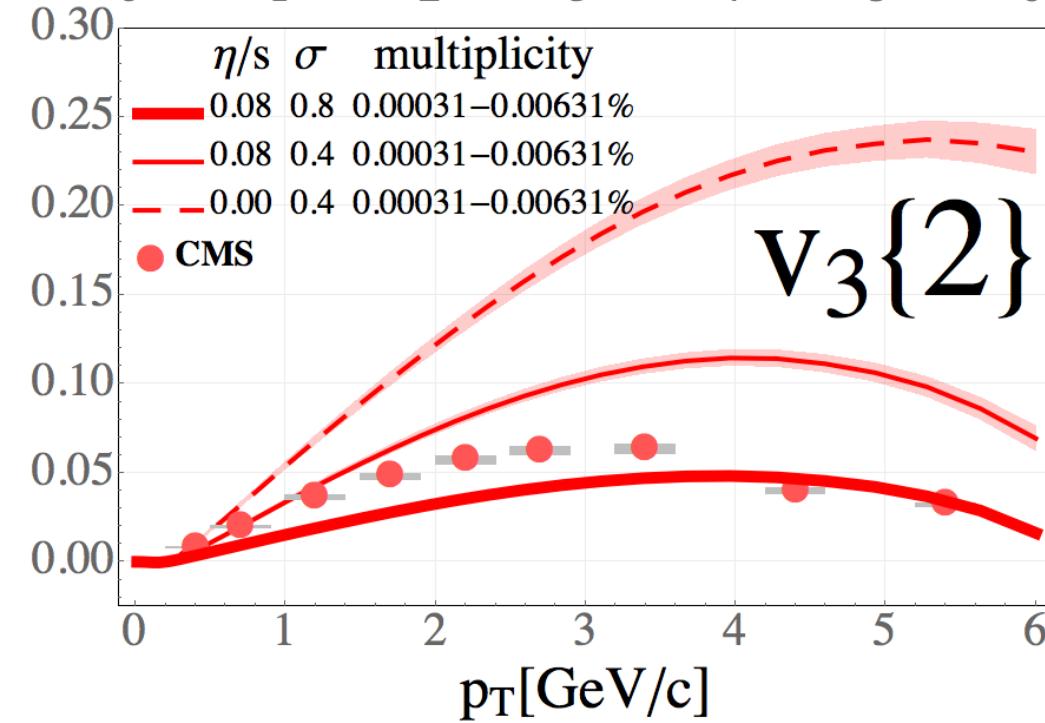
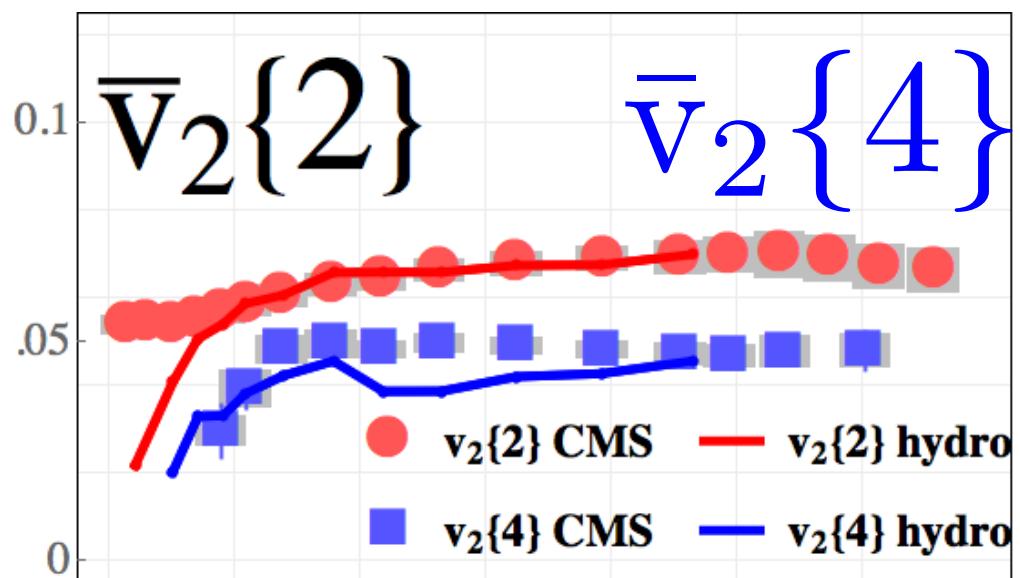
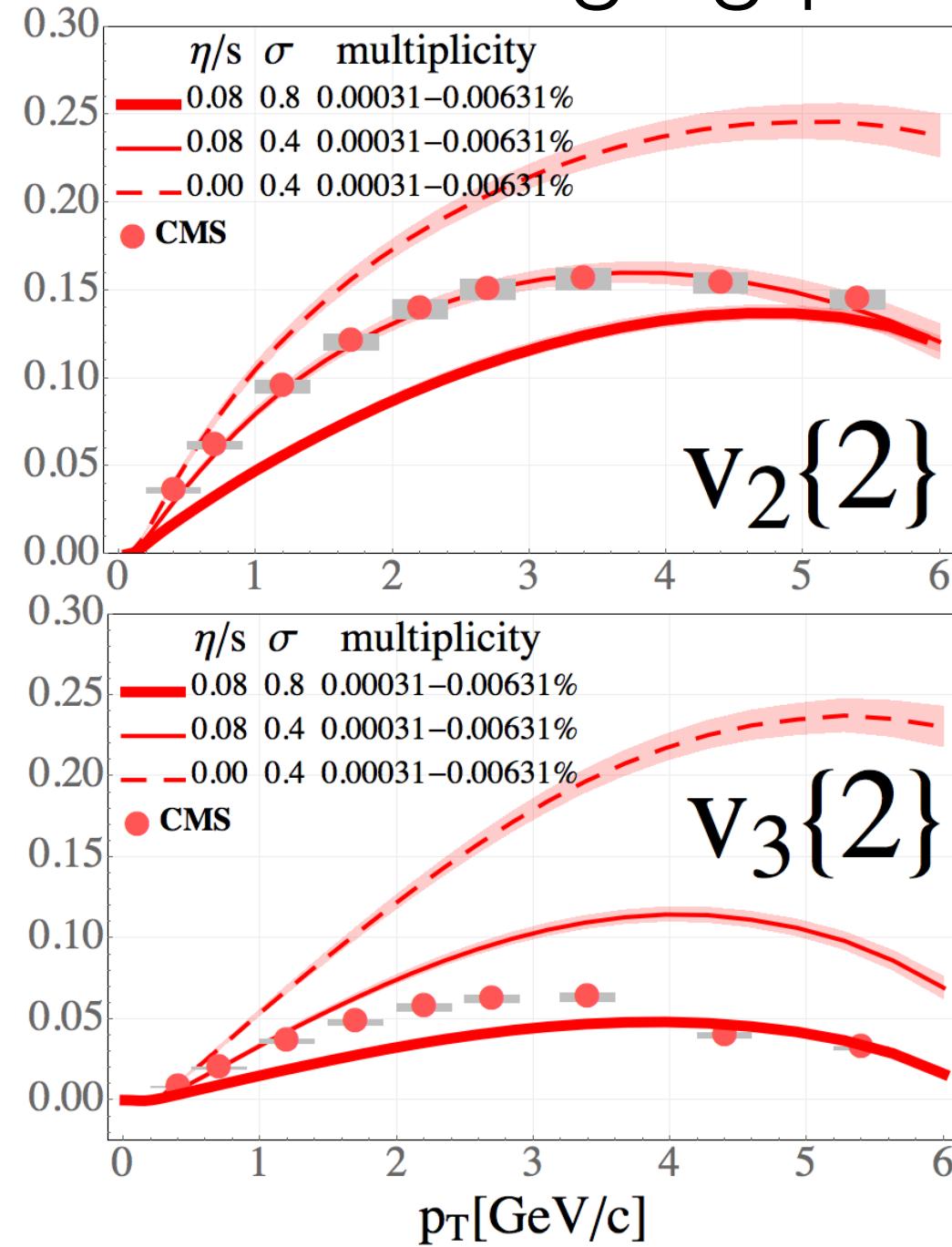
# **Comparing hydro calculations to existing pA data**

CMS 1211.0989 McGill, LBNL 1405.3976

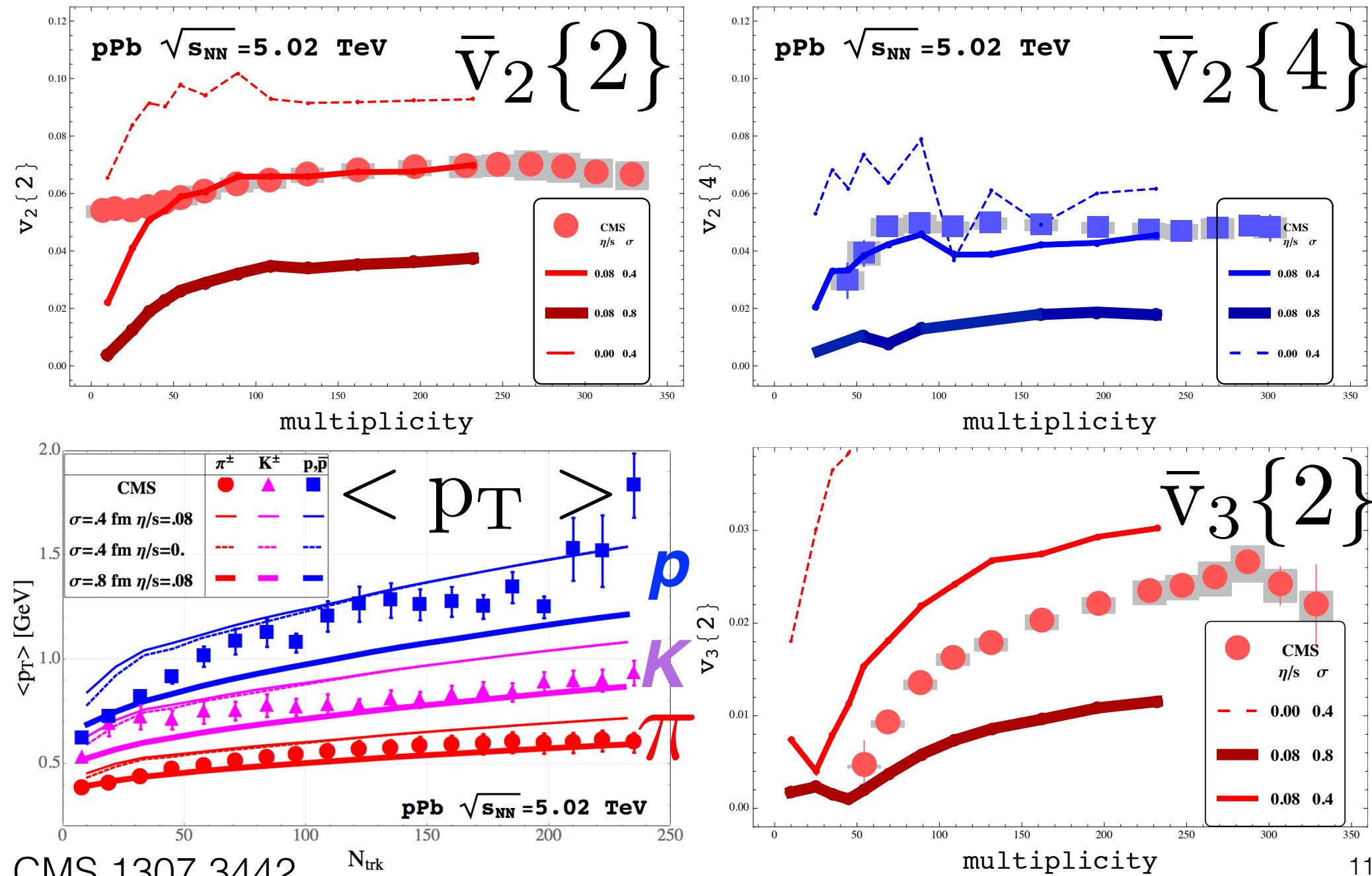
# pPb flow observables: CMS & hydro



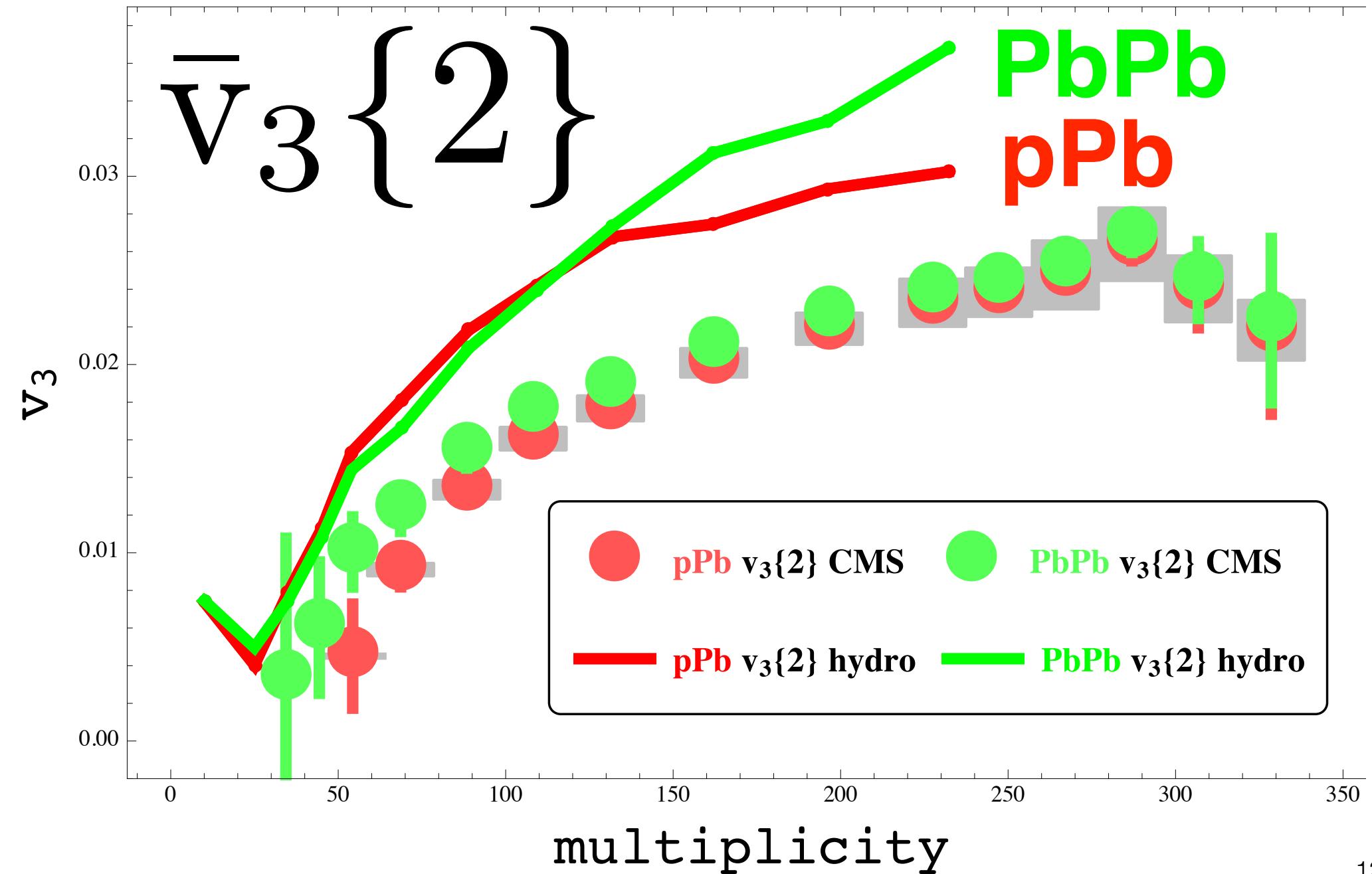
# Changing parameters $\sigma$ and $\eta/s$



# Flow observables dependence on $\sigma$ and $\eta/s$



CMS 1211.0989 McGill, LBNL 1405.3976  
CMS finding in hydro



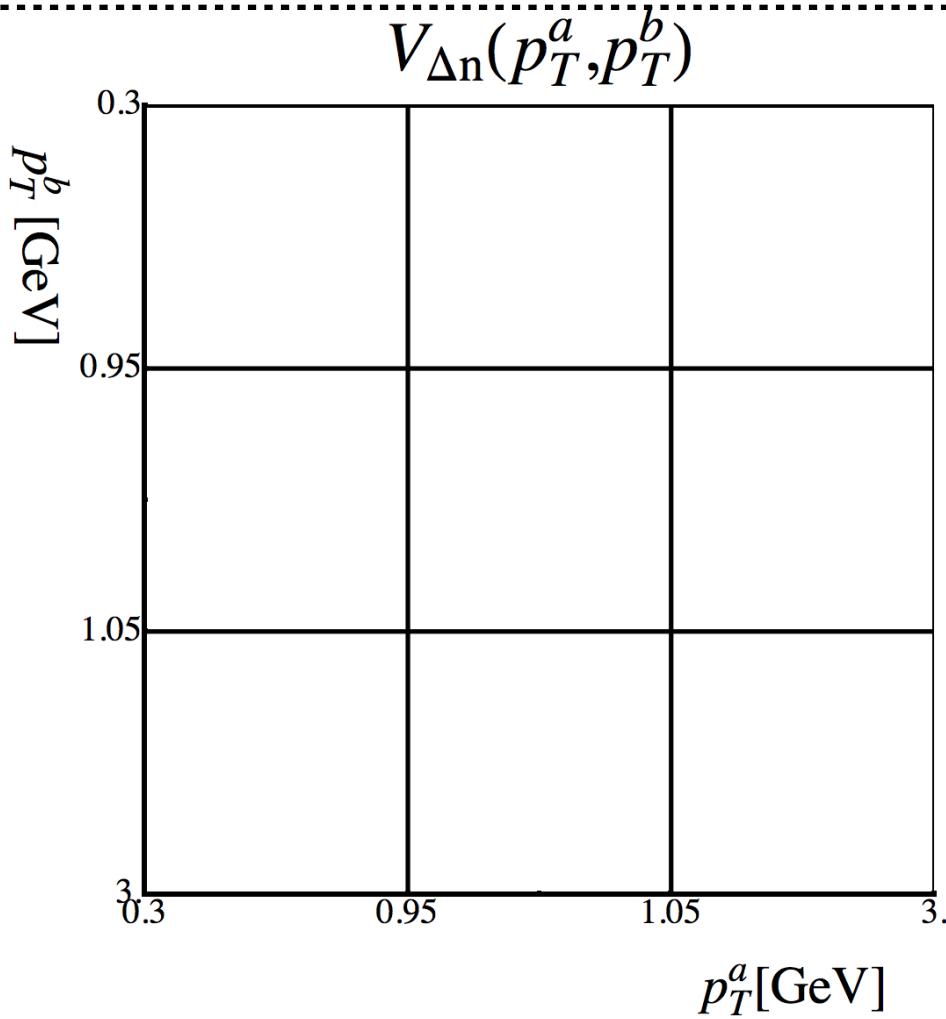
# All two-particle correlation observables

**theory:**

$$\frac{2\pi}{N} \frac{dN}{d\phi^a} = 1 + 2 \sum_{n=1}^{\infty} v_n(p_T^a) \cos n(\phi^a - \Psi_n)$$

**experiment:**

$$V_{n\Delta}(p_T^a, p_T^b) \equiv \langle \overline{\cos n(\phi^a - \phi^b)} \rangle$$



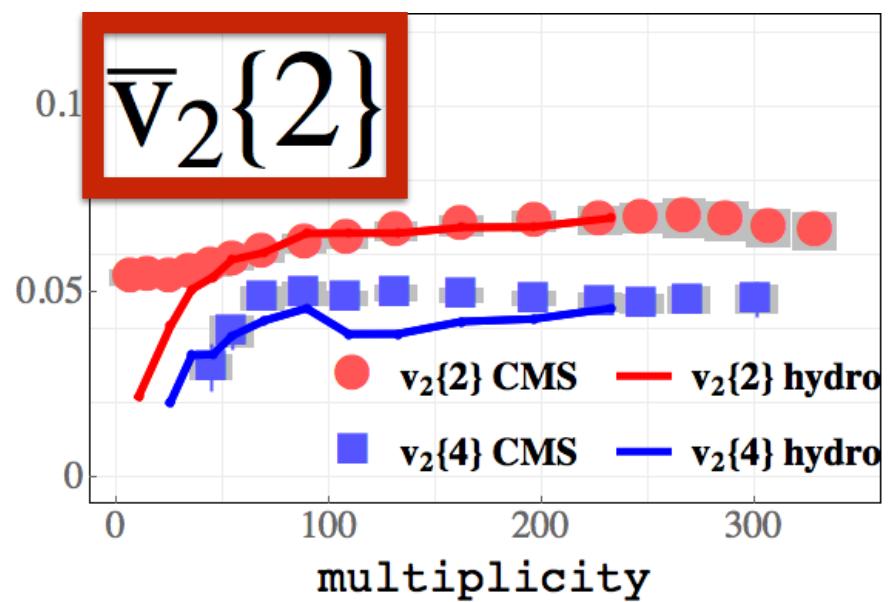
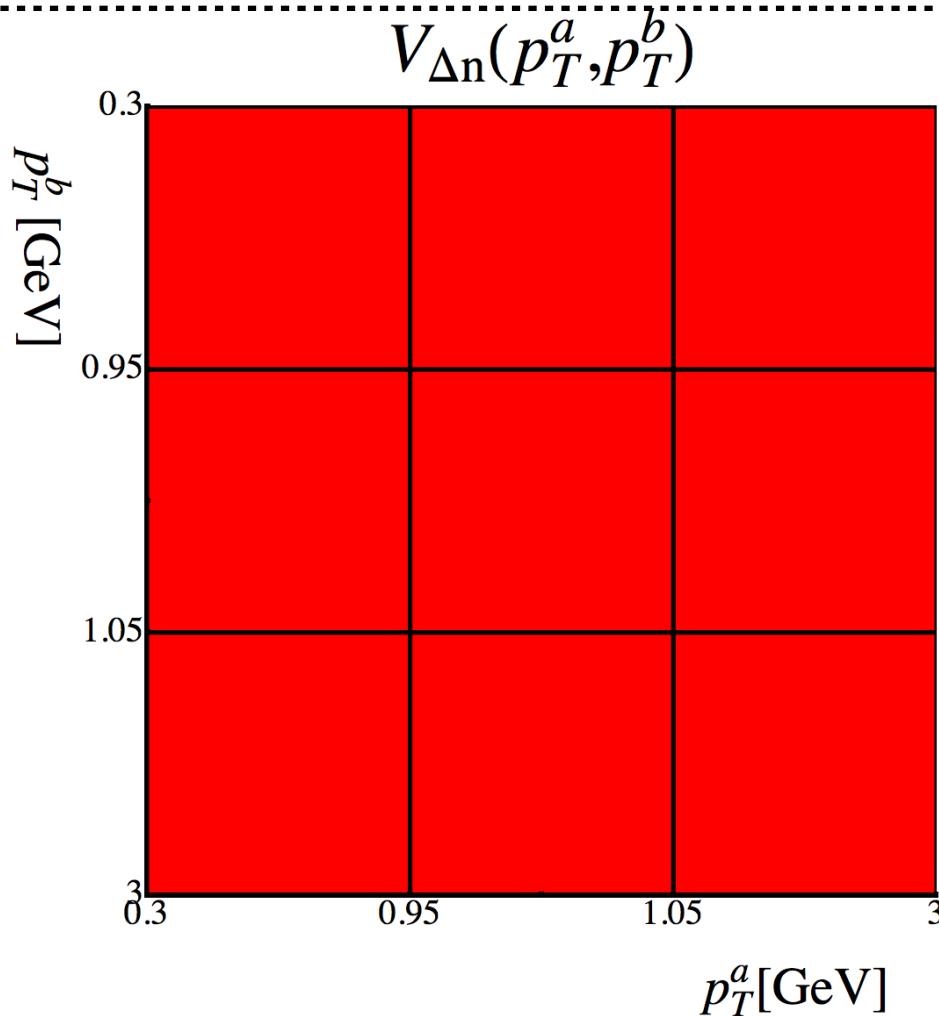
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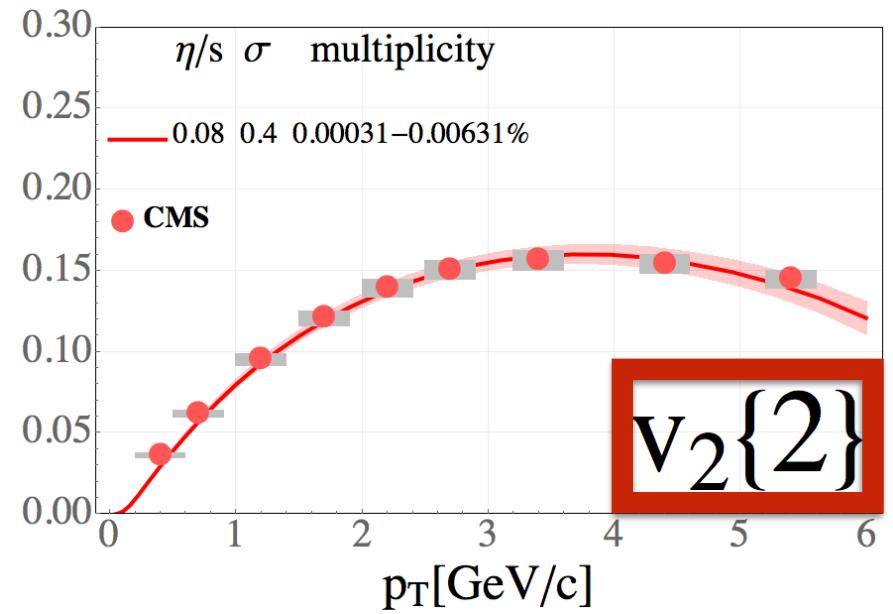
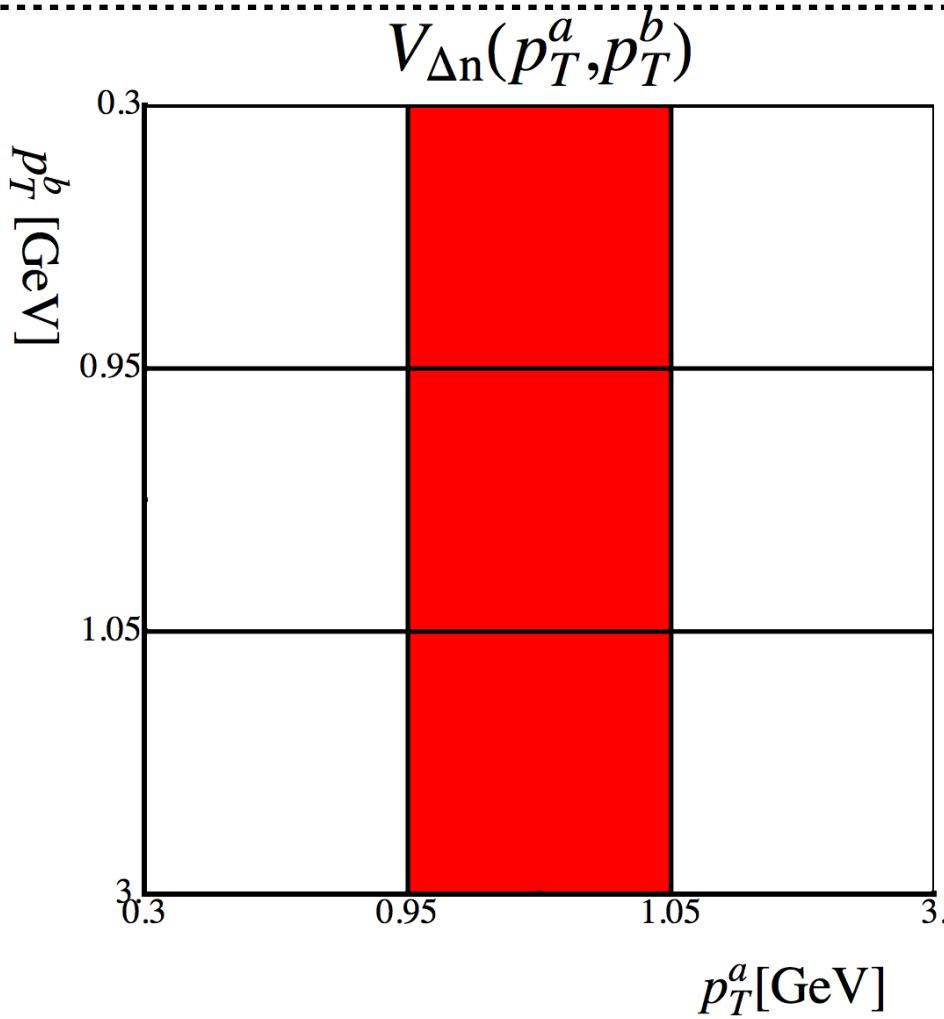
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$$V_{n\Delta}(p_T^a, p_T^b) \equiv \langle \overline{\cos n(\phi^a - \phi^b)} \rangle$$



# Two-particle correlation in hydro

**theory:**

$$\frac{2\pi}{N} \frac{dN}{d\phi^a} = 1 + 2 \sum_{n=1}^{\infty} v_n(p_T^a) \cos n(\phi^a - \Psi_n)$$

**experiment:**

$$V_{n\Delta}(p_T^a, p_T^b) \equiv \langle \overline{\cos n(\phi^a - \phi^b)} \rangle$$

Abs[r<sub>n</sub>]

p<sub>T</sub><sup>b</sup> [GeV]

= 1

< 1

= 1

< 1

< 1

= 1

p<sub>T</sub><sup>a</sup> [GeV]

$$r_n \equiv \frac{V_{n\Delta}(p_T^a, p_T^b)}{\sqrt{V_{n\Delta}(p_T^a, p_T^a)V_{n\Delta}(p_T^b, p_T^b)}}$$

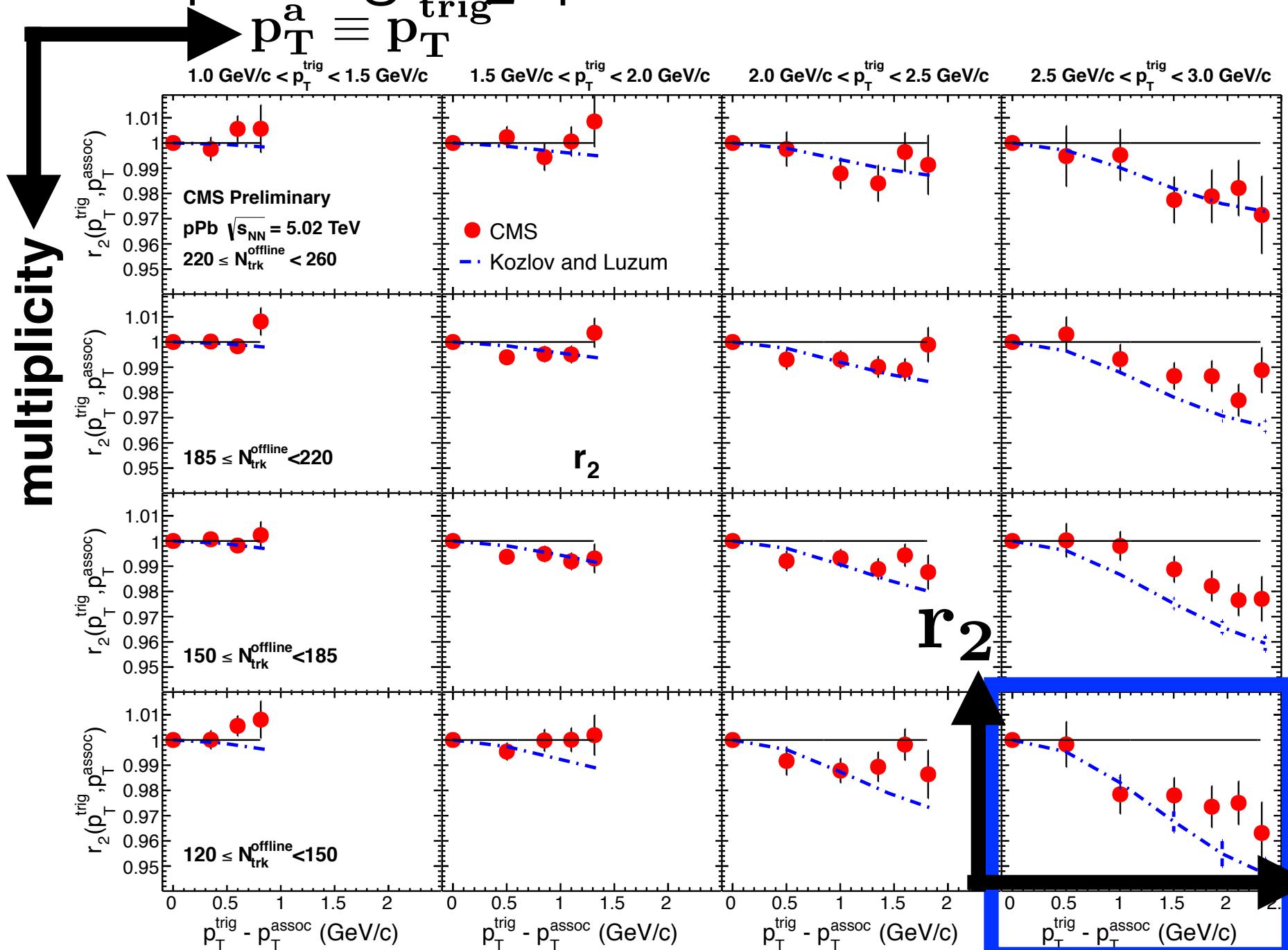
**hydro:**

$$\frac{dN_{pairs}}{d^3p^a d^3p^b} \stackrel{\text{(flow)}}{=} \frac{dN}{d^3p^a} \times \frac{dN}{d^3p^b}$$

$$V_{n\Delta}(p_T^a, p_T^a) \geq 0$$

$$V_{n\Delta}(p_T^a, p_T^b)^2 \leq V_{n\Delta}(p_T^a, p_T^a)V_{n\Delta}(p_T^b, p_T^b)$$

# Comparing $r_2$ predictions to CMS data

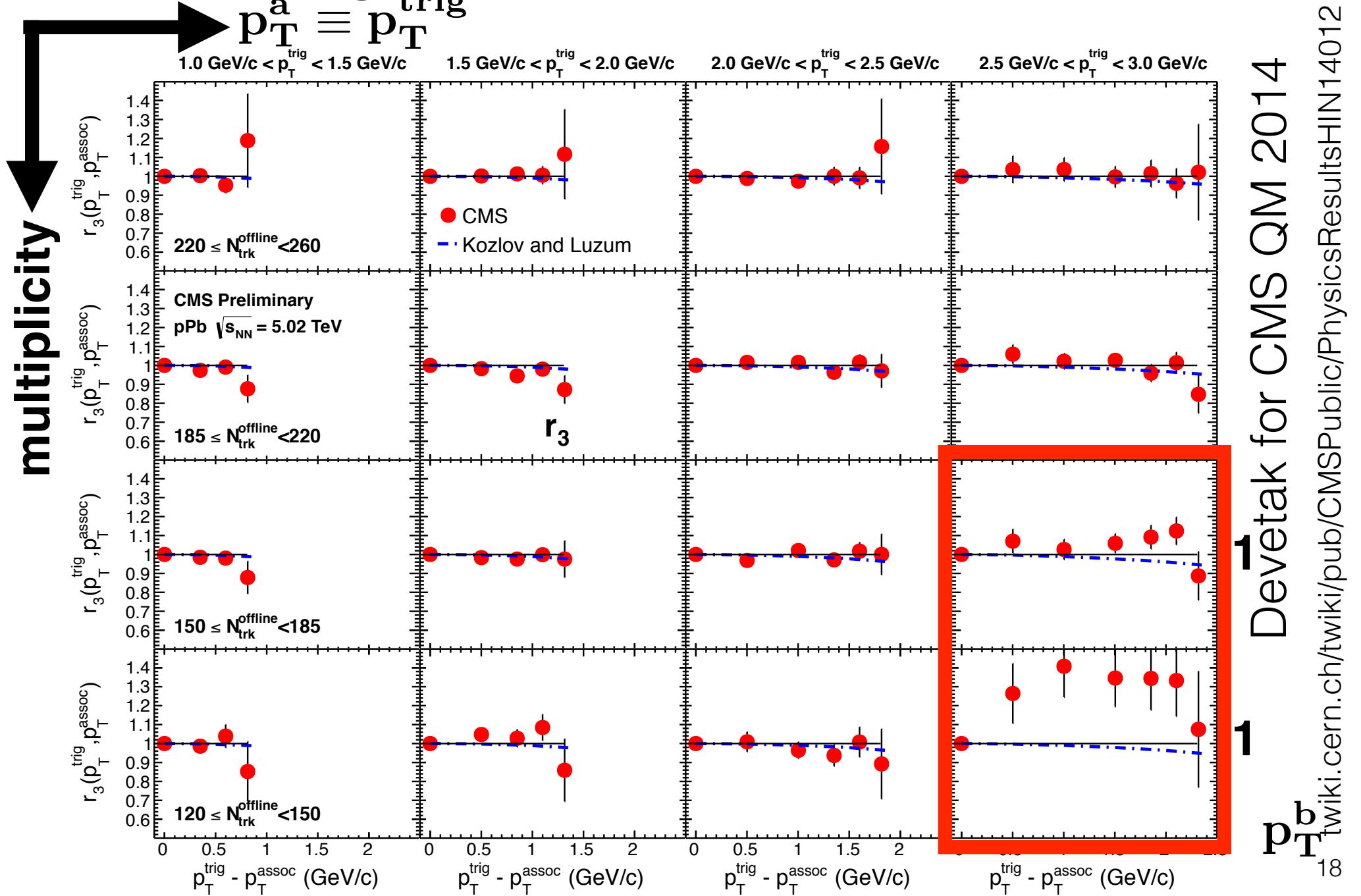


Devetak for CMS QM 2014  
<https://twiki.cern.ch/twiki/pub/CMS/PhysicsResultsHIN14012>

**$p_T^b$**

17

# Comparing $r_3$ predictions to CMS data

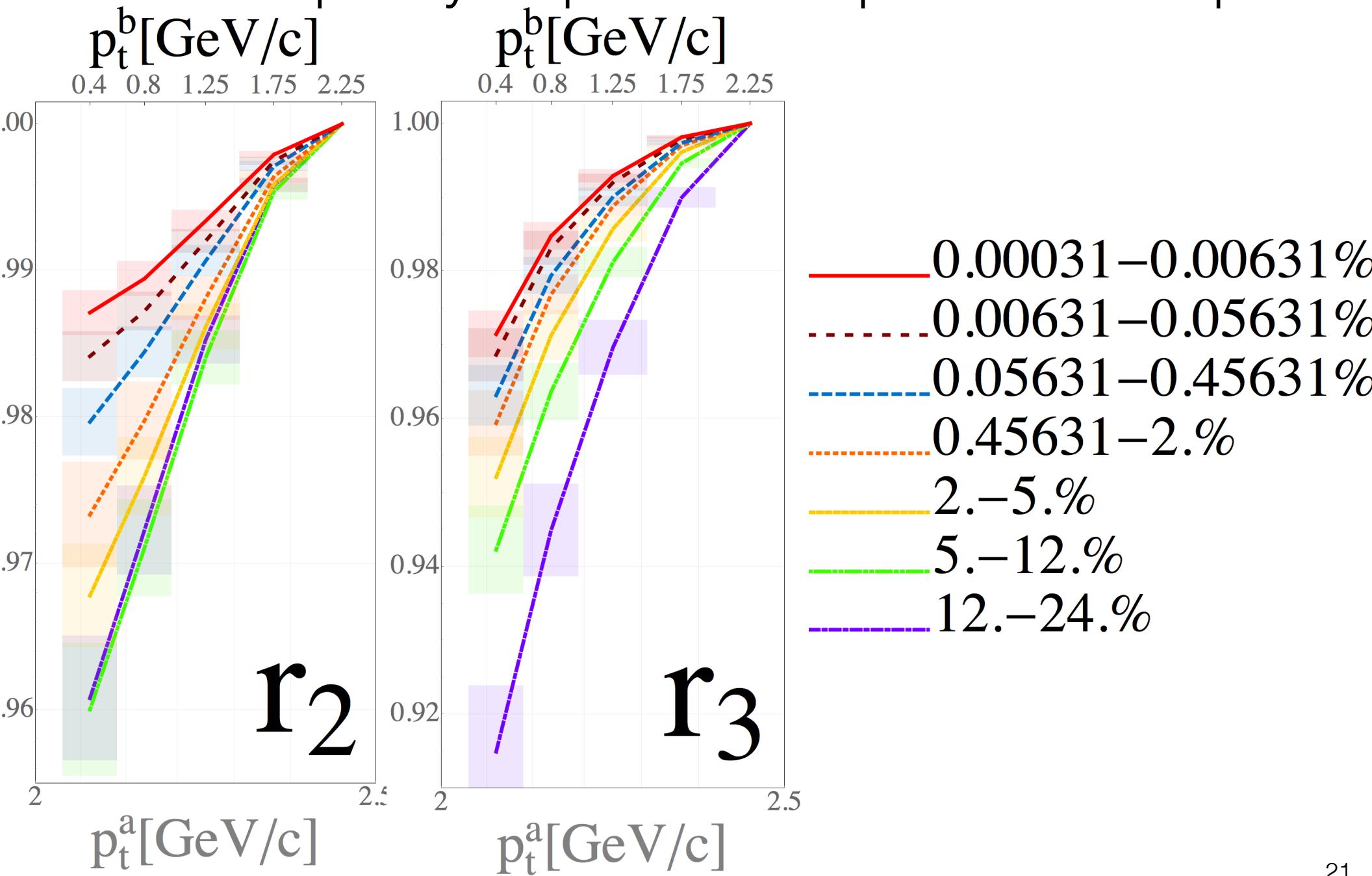


# Section conclusions

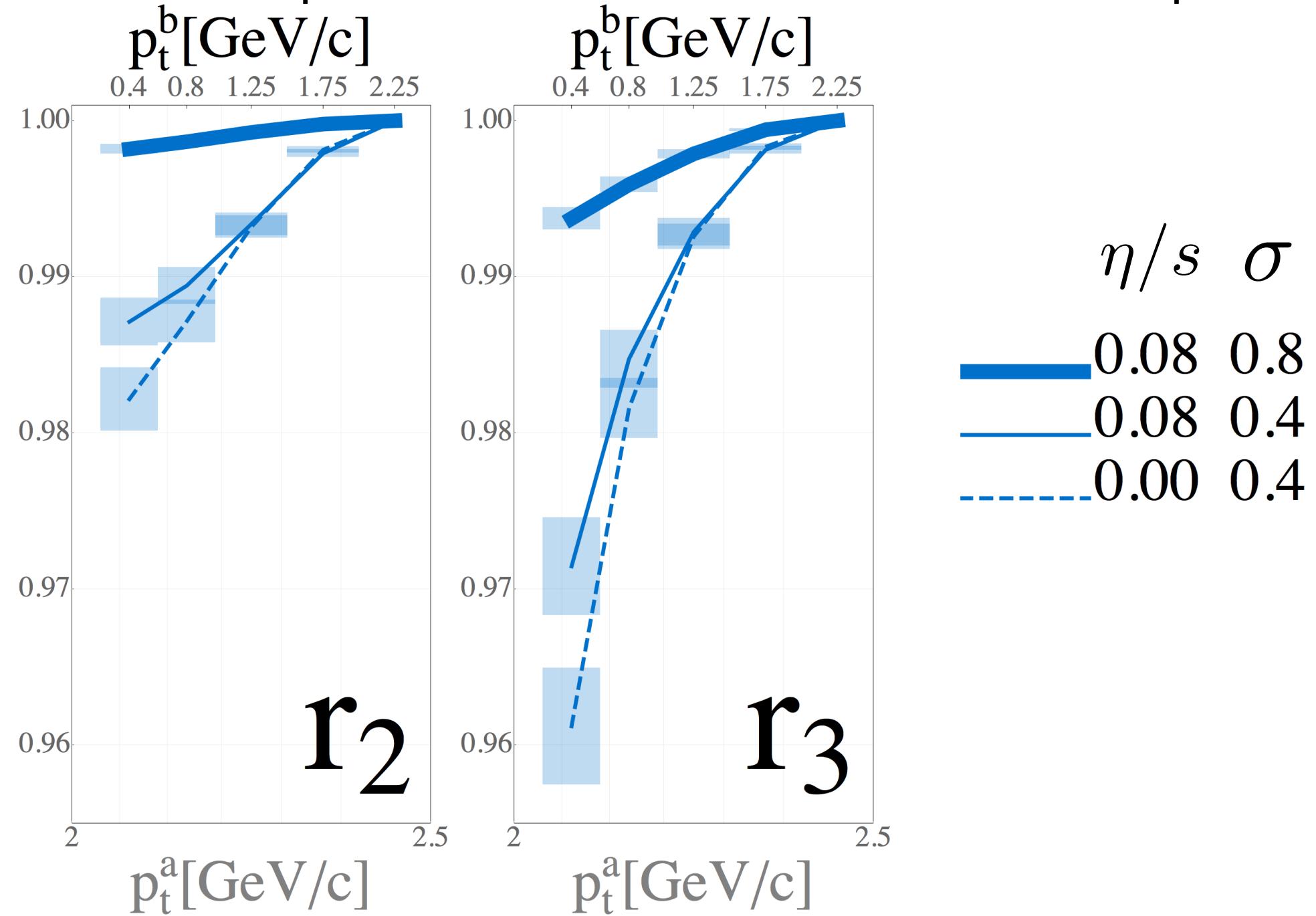
- Hydrodynamics can reasonably describe a wide range of flow observables for pPb system at high multiplicity  $v_2\{2\}$ ,  $v_3\{2\}$ ,  $v_2\{4\}$  and  $r_n$

**Another handle  
to study HIC**

# multiplicity dependence prediction in pPb



# $r_n$ dependence on $\sigma$ and $\eta/s$ in pPb



$r_n$  dependence on  $\sigma$  and  $\eta/s$  in pPb

$p_t^b$ [GeV/c]

0.4 0.8 1.25 1.75 2.25

$p_t^b$ [GeV/c]

0.4 0.8 1.25 1.75 2.25

$r_n$  is sensitive to  
transverse granularity

$r_2$

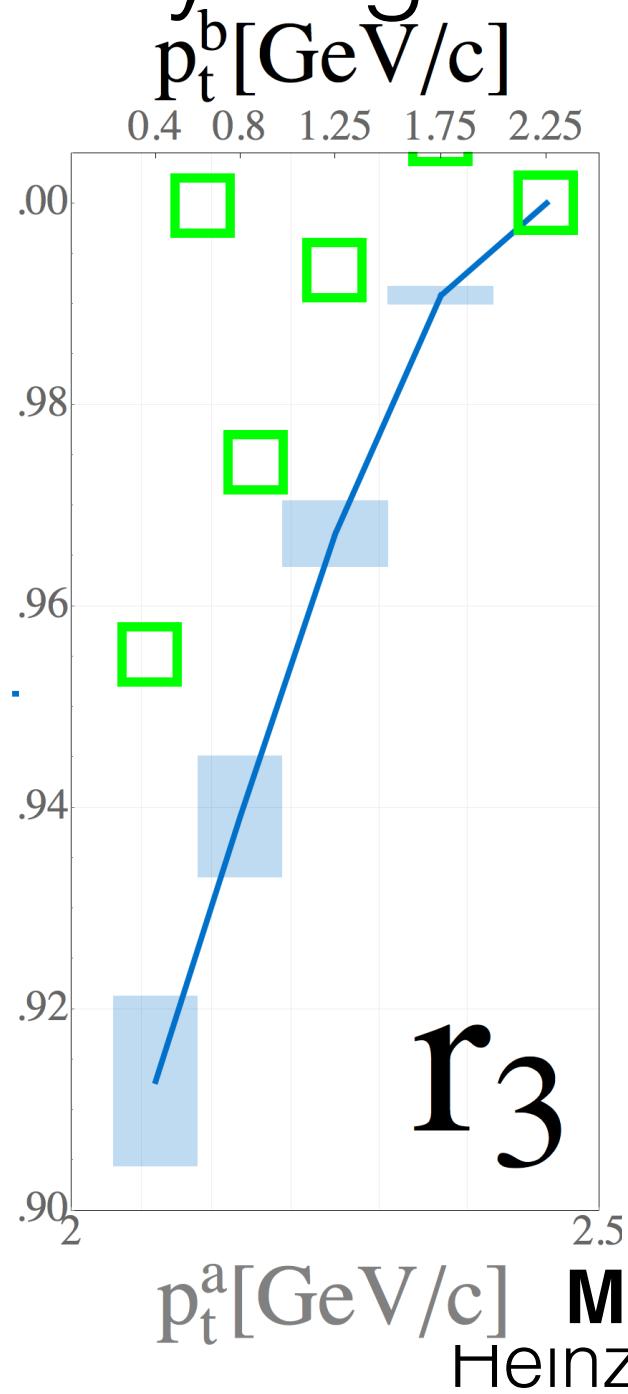
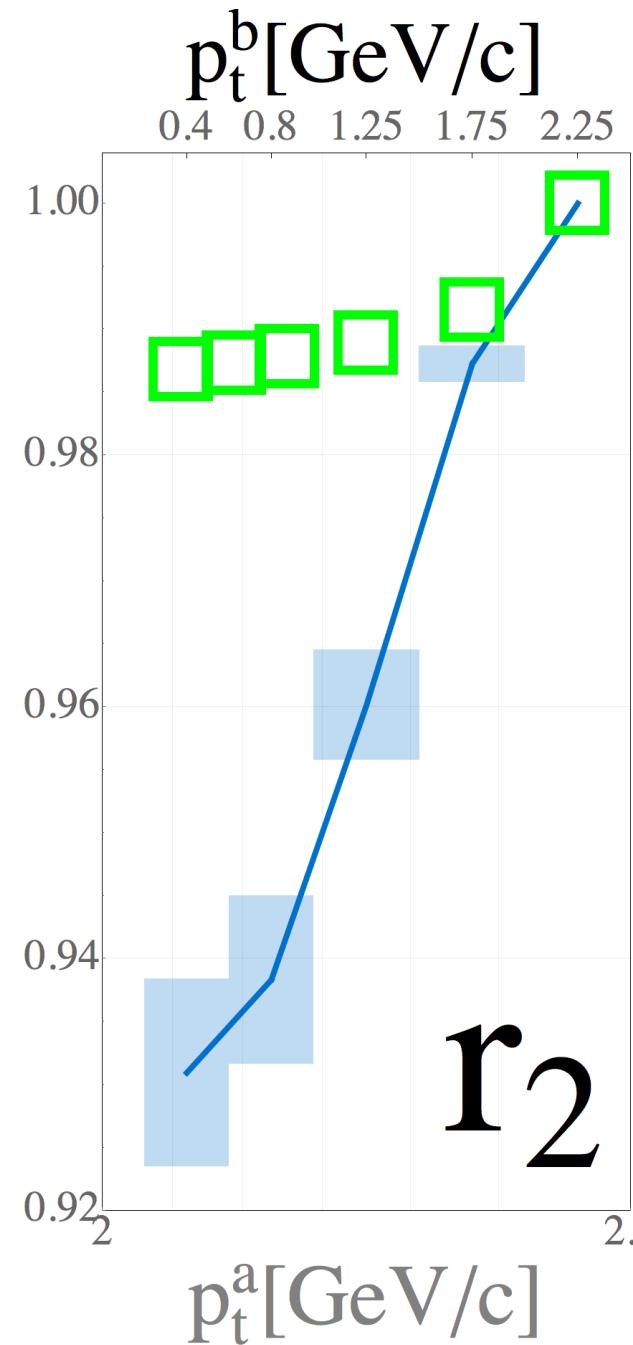
$p_t^a$ [GeV/c]

$r_3$

$p_t^a$ [GeV/c]

$\eta/s$      $\sigma$   
0.08 0.8  
0.08 0.4  
0.00 0.4

# Reanalyzing PbPb data

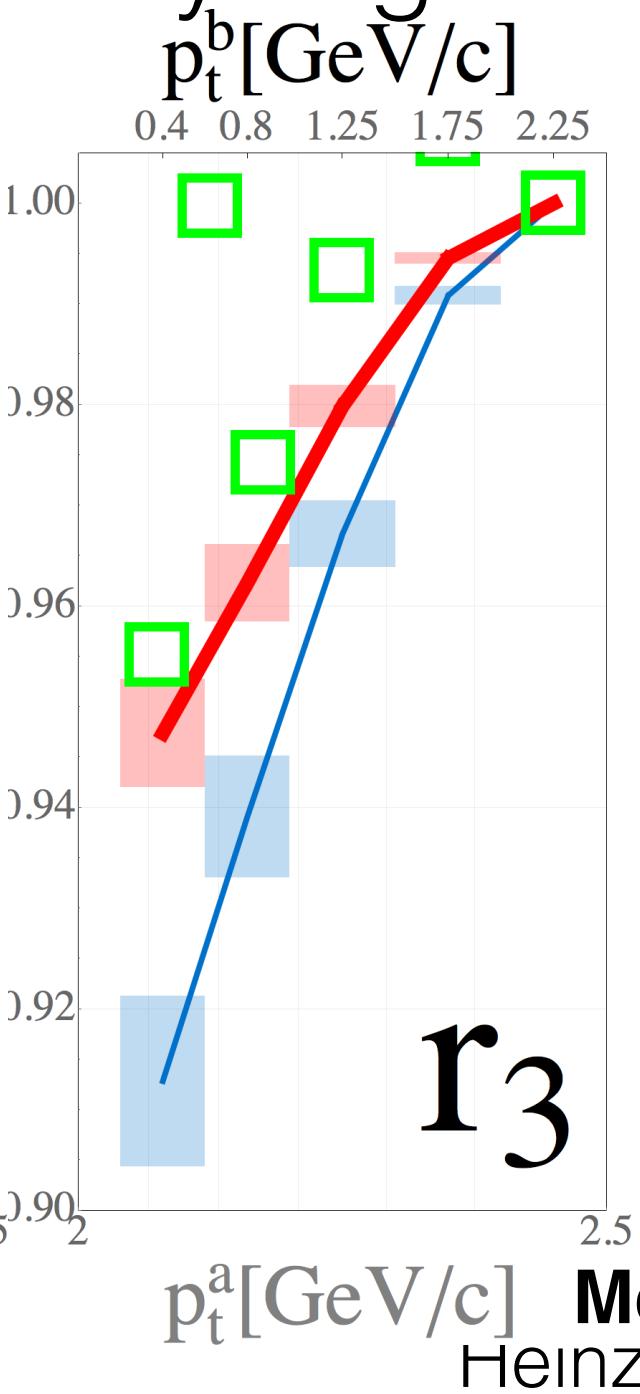
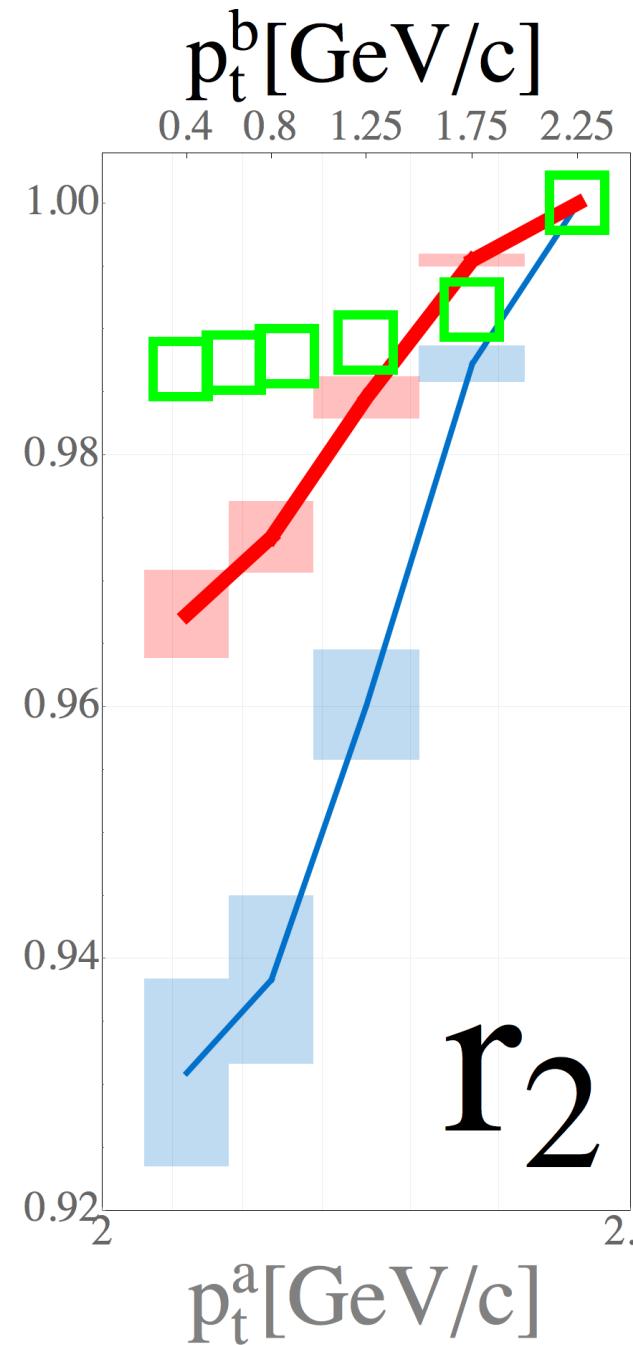


**ALICE** 1109.2501  
 $\eta/s$   $\sigma$  fluct

0.08 0.4 NBD

**McGILL LBNL** 1405.3976  
Heinz, Qiu, Shen 1302.3535<sup>24</sup>

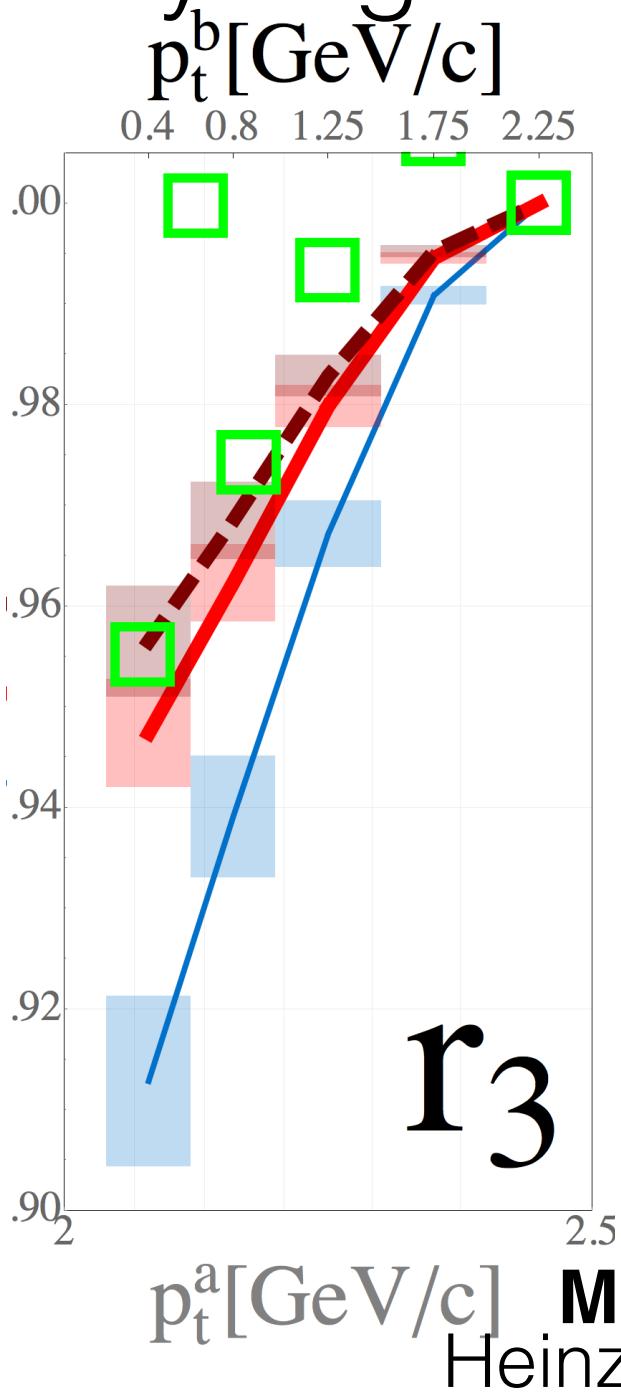
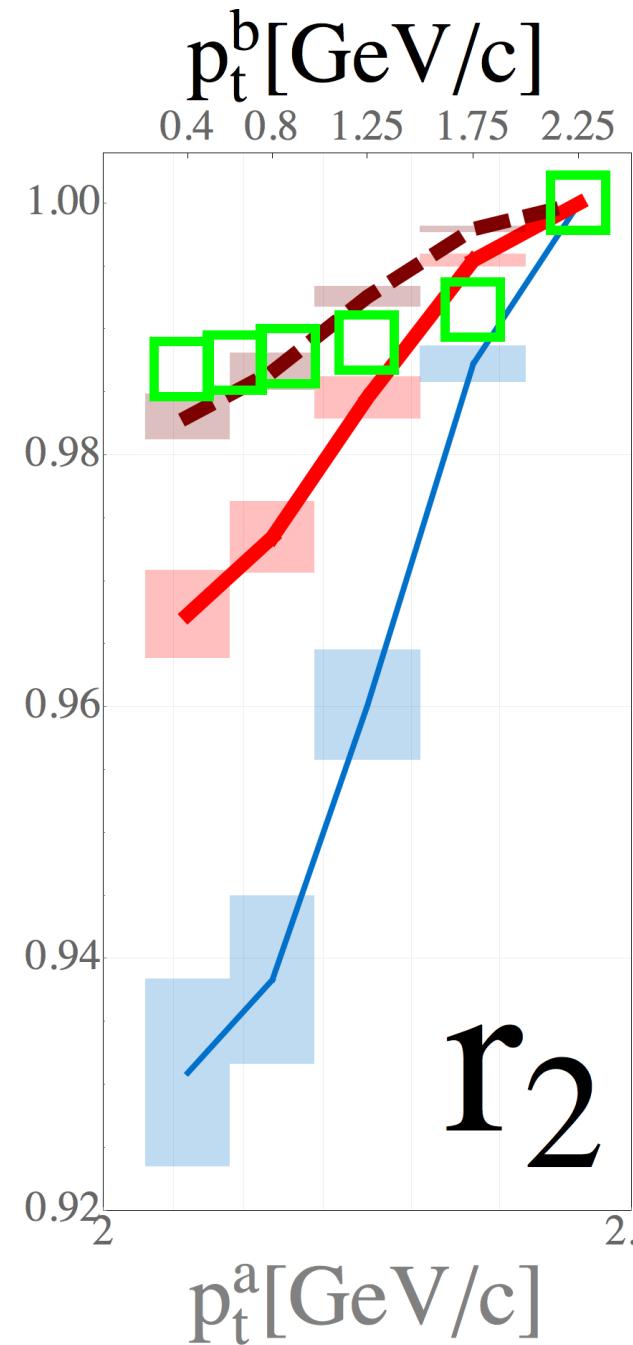
# Reanalyzing PbPb data



□ **ALICE** 1109.2501  
 $\eta/s$     $\sigma$    fluct  
— 0.08   0.8   NBD  
— 0.08   0.4   NBD

**McGill LBNL** 1405.3976  
 Heinz, Qiu, Shen 1302.3535<sup>25</sup>

# Reanalyzing PbPb data



□ **ALICE** 1109.2501  
 $\eta/s$     $\sigma$    fluct  
 —— 0.08   0.8  
 —— 0.08   0.8   NBD  
 —— 0.08   0.4   NBD

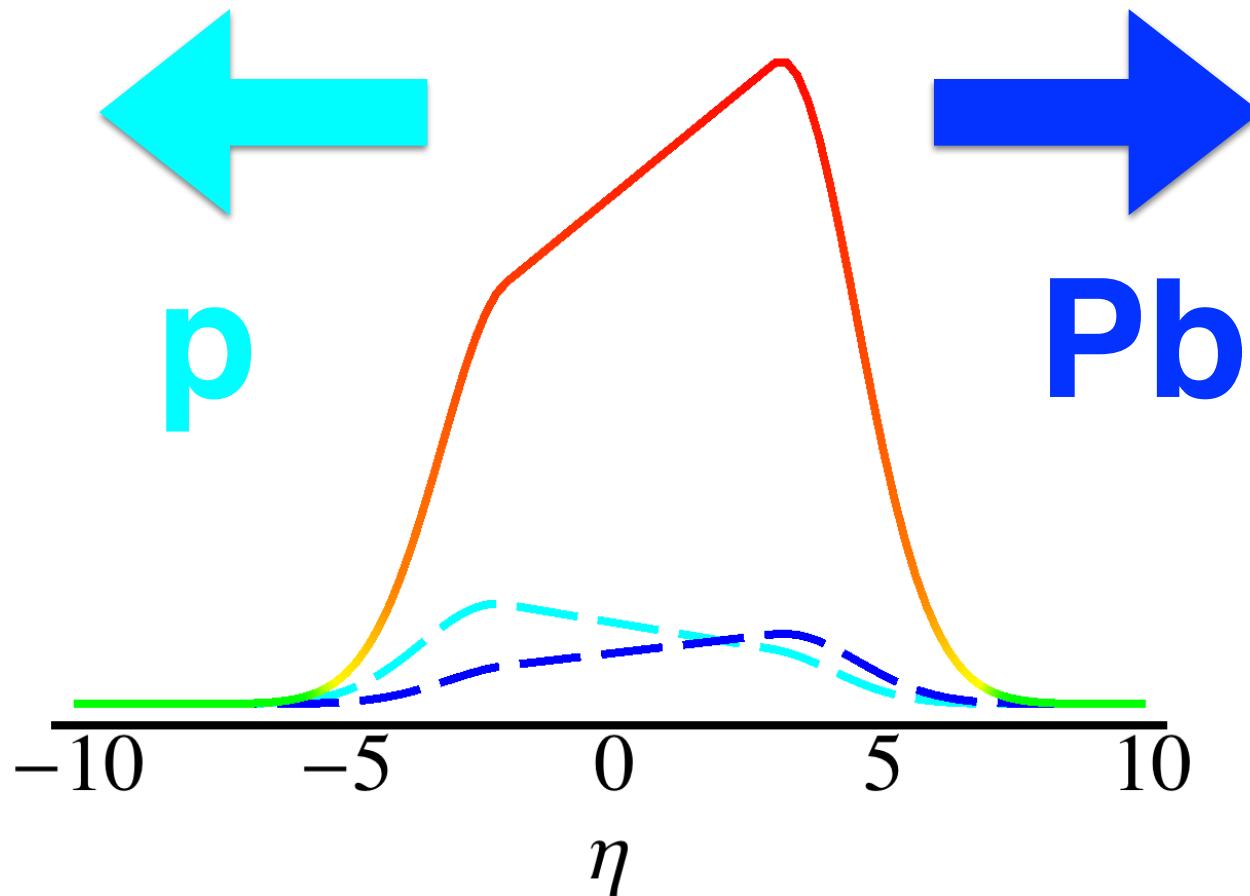
**McGill LBNL** 1405.3976  
 Heinz, Qiu, Shen 1302.3535<sup>26</sup>

# Conclusion

- Hydrodynamics can reasonably describe a wide range of flow observables for pPb system at high multiplicity  $v_2\{2\}$ ,  $v_3\{2\}$ ,  $v_2\{4\}$  and  $\mathcal{R}_n$
- $\mathcal{R}_n$  predictions provide another handle to explore HIC
  - ▶ it tells us where hydro breaks down
  - ▶ a way to probe initial conditions (granularity)
  - ▶ a way to study differences between pA and AA

# Backup

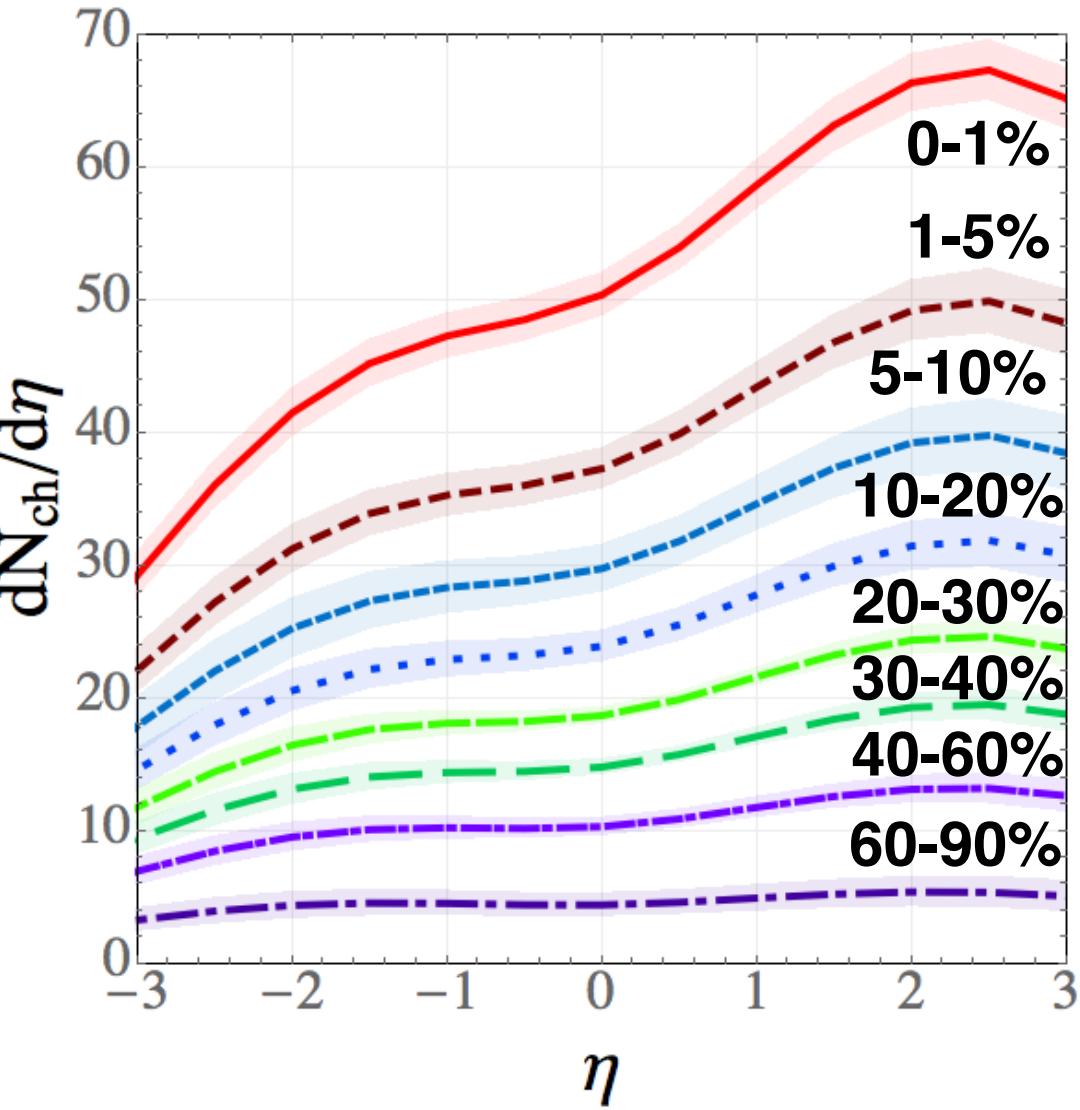
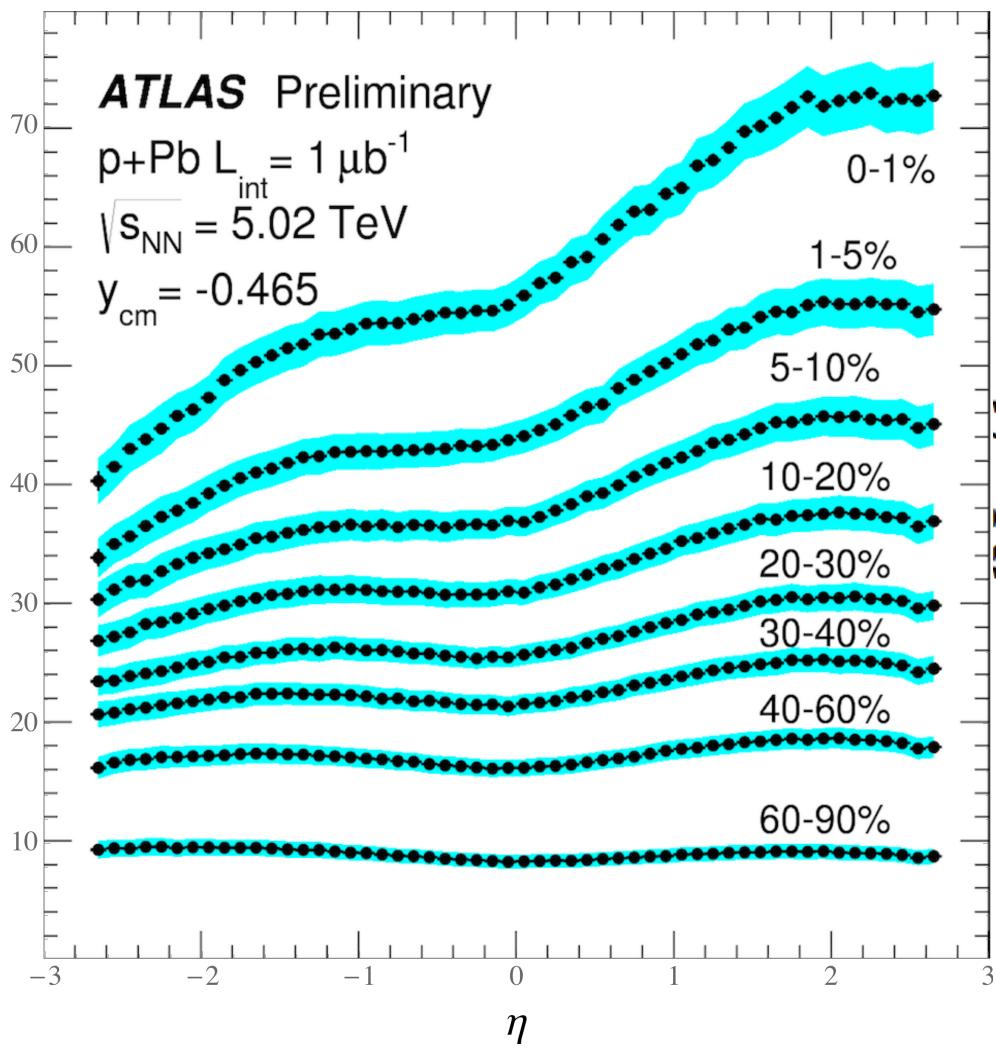
# Initial conditions: longitudinal profile



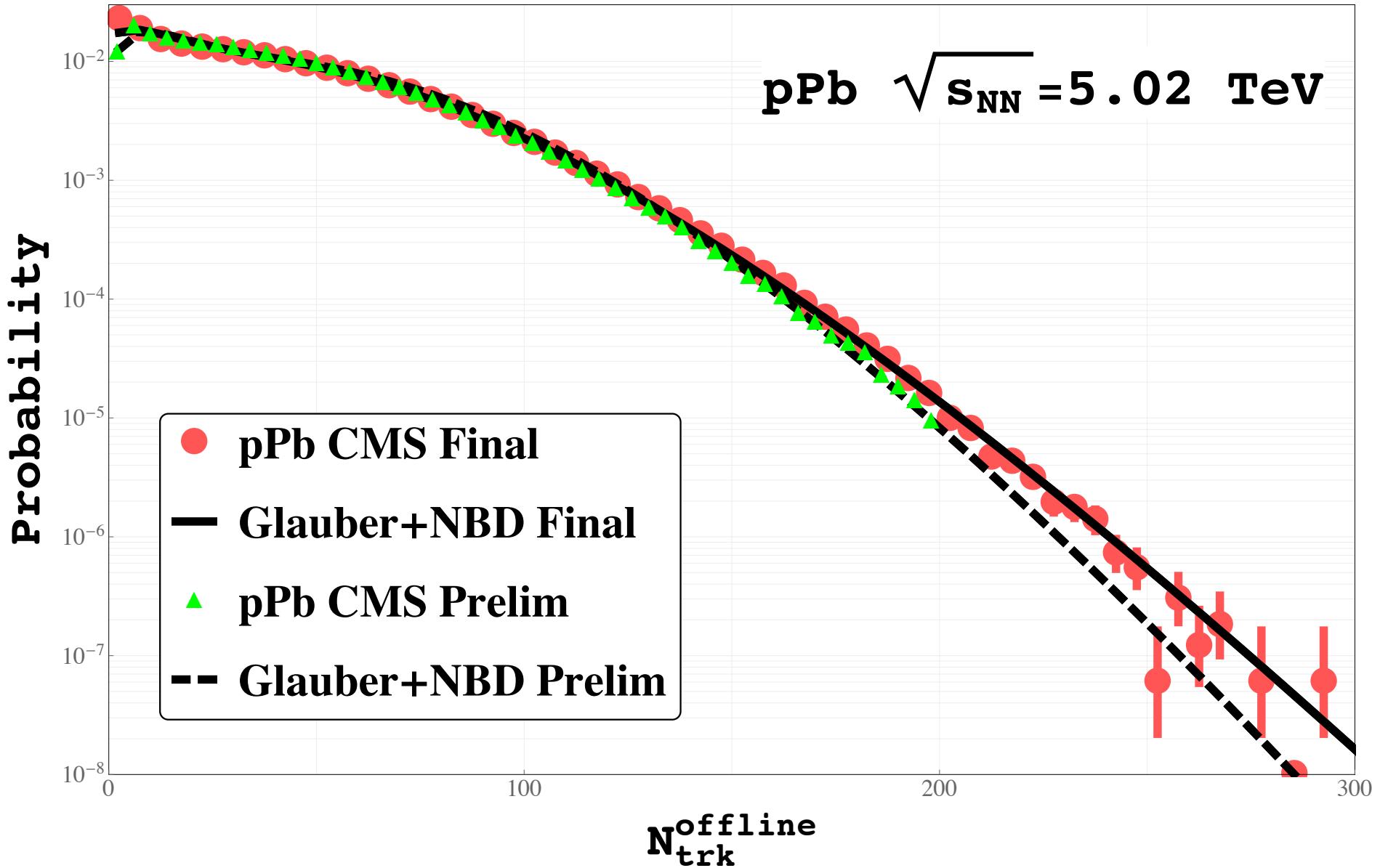
$$\left(1 \pm \frac{\eta}{y_{\text{beam}}}\right) \exp\left(-\frac{(|\eta| - \eta_0)^2}{2\sigma_\eta^2} \theta(|\eta| - \eta_0)\right)$$

# Pseudorapidity distribution

ATLAS arXiv/1403.5738

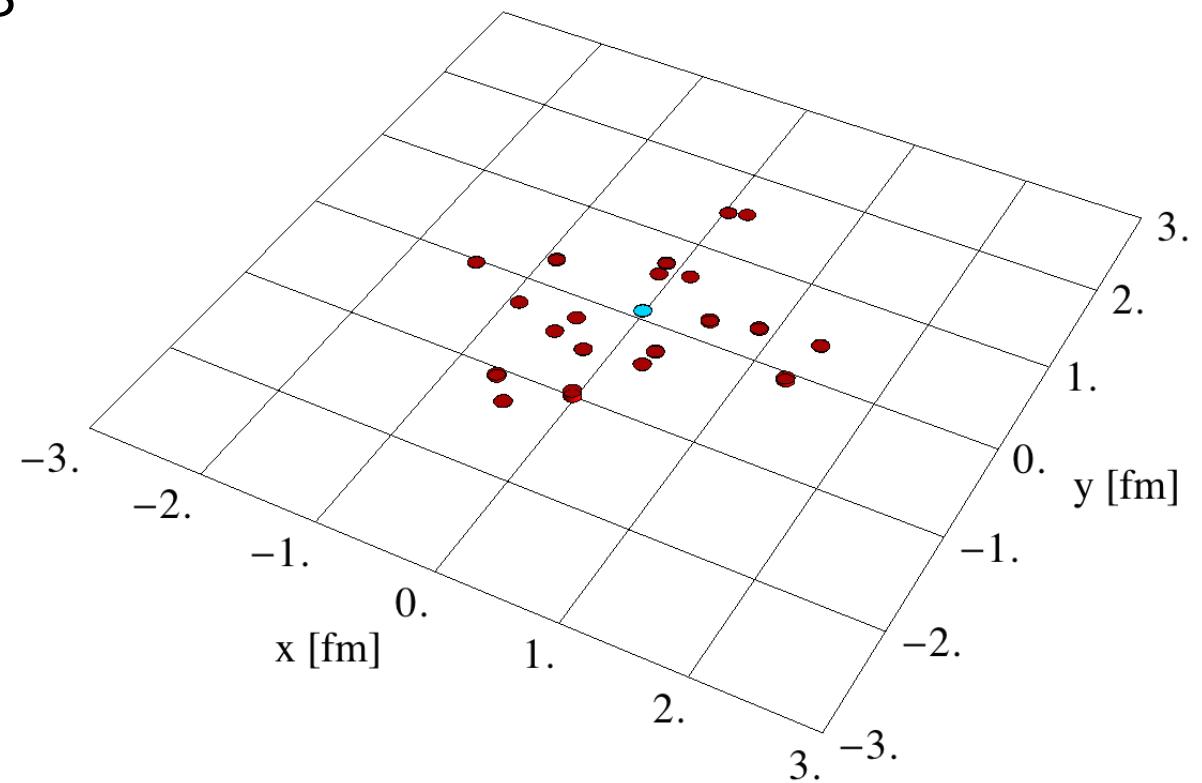


# Initial conditions: Glauber+NBD



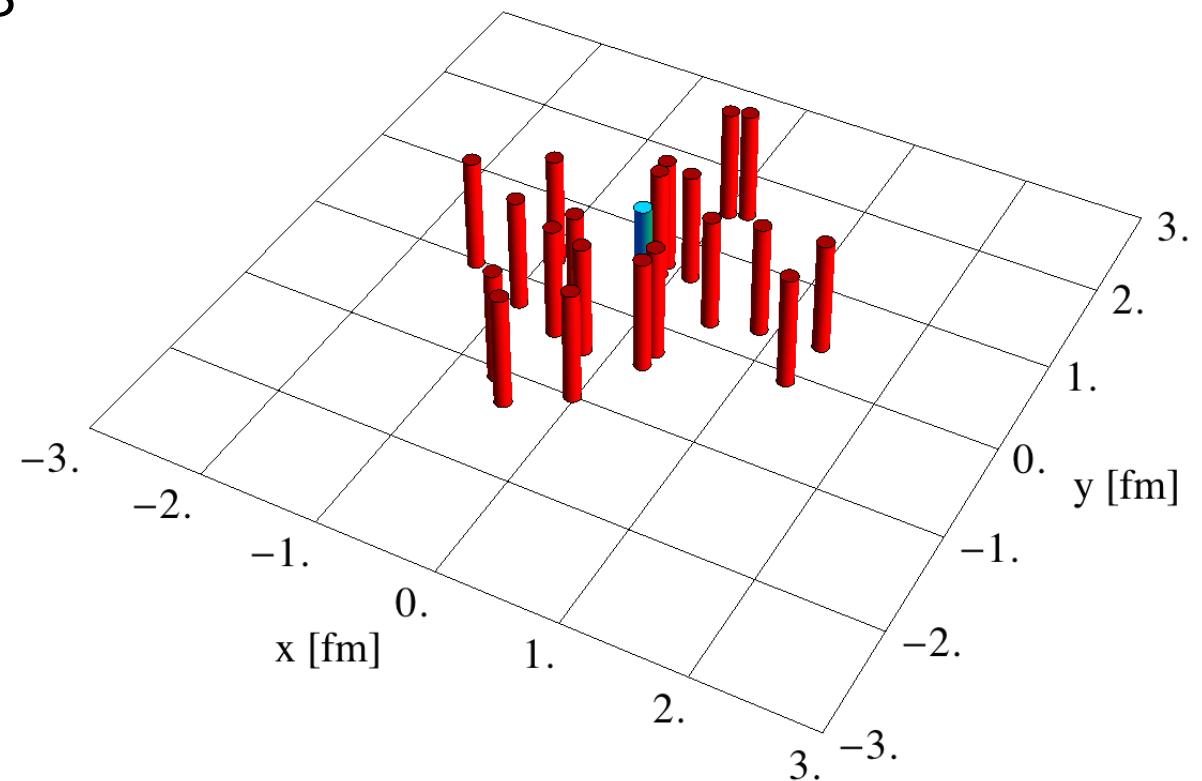
# Initial conditions: Glauber

- sample participants



# Initial conditions: Glauber

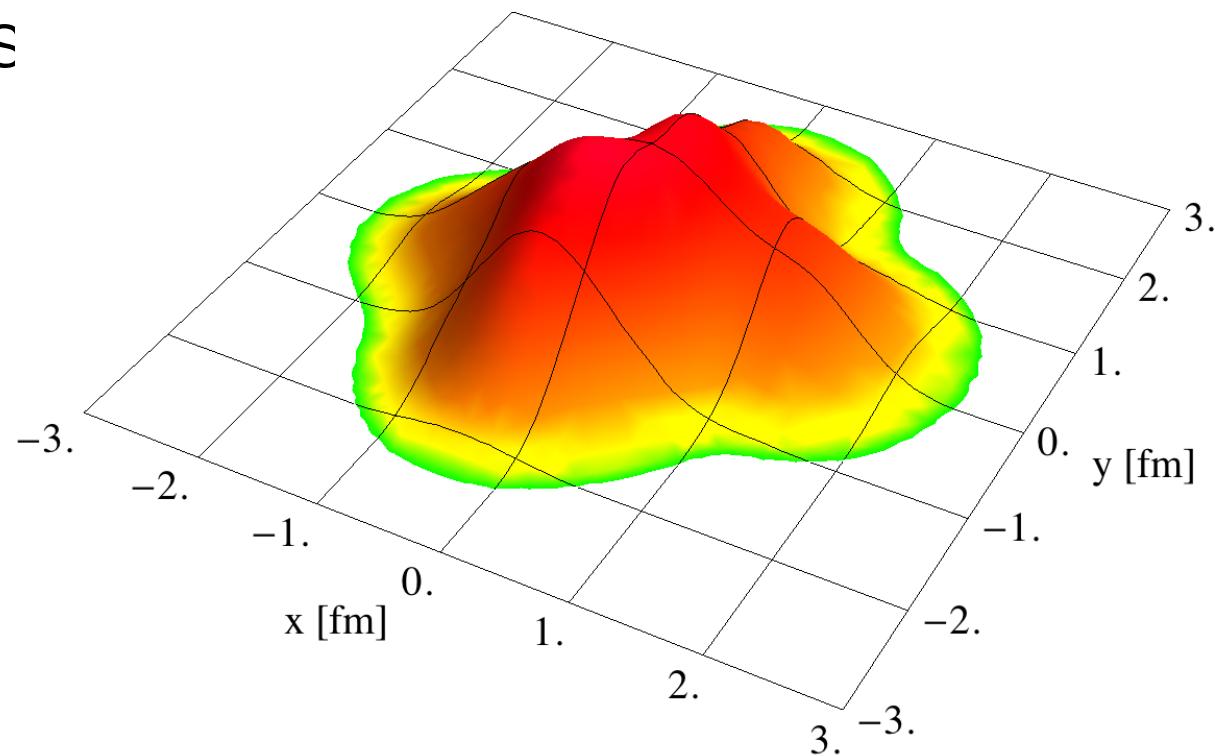
- sample participants
- add sources



# Initial conditions: Glauber

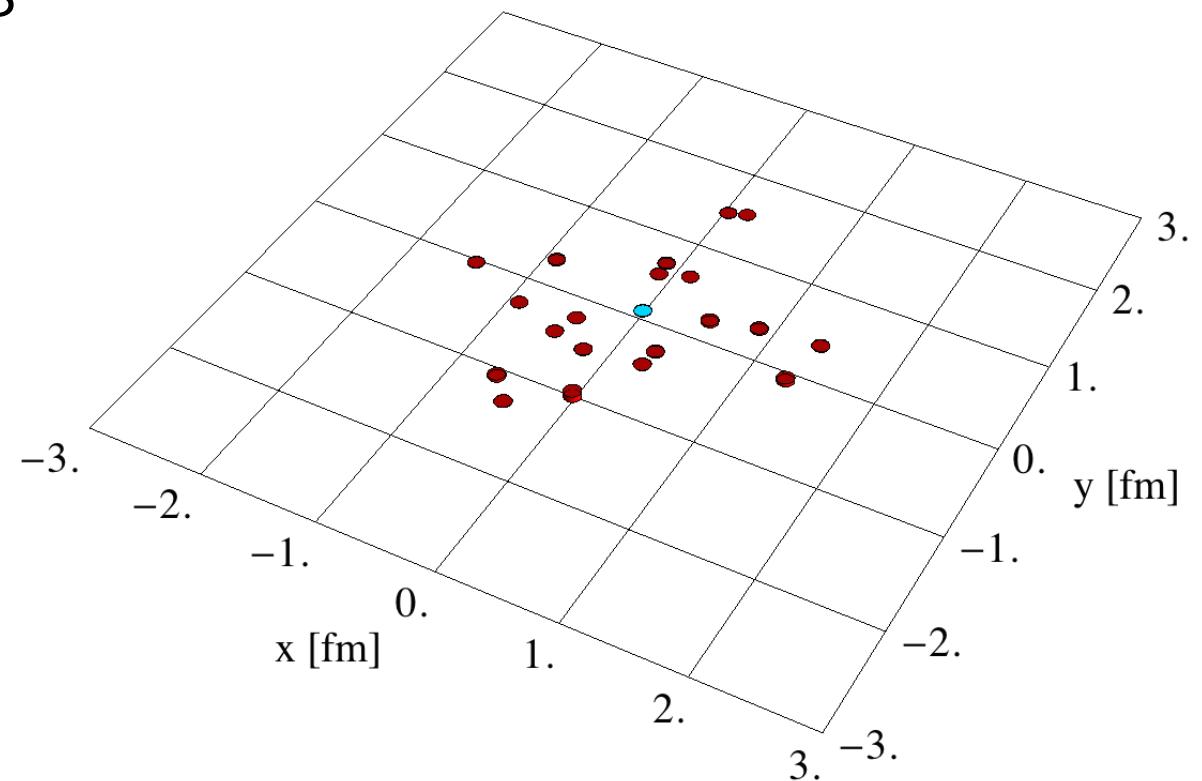
$$\sigma = 0.40 \text{ fm}$$

- sample participants
- add sources
- increase  $\sigma$



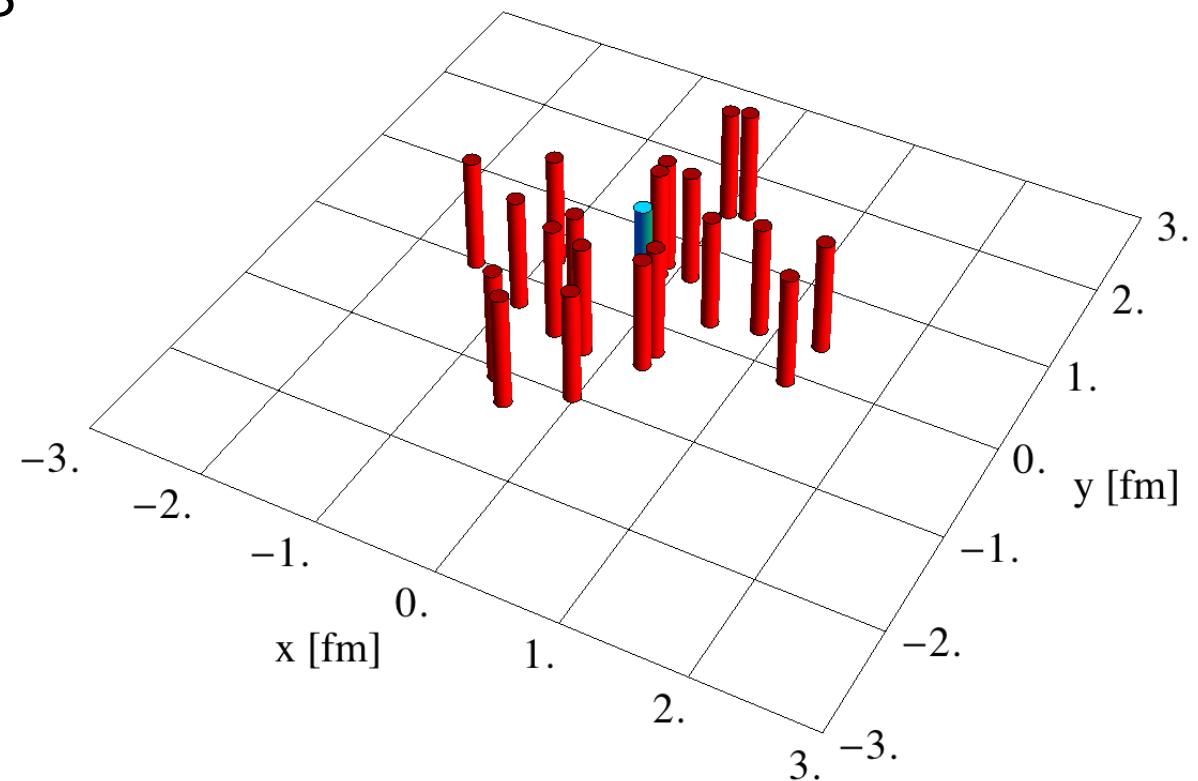
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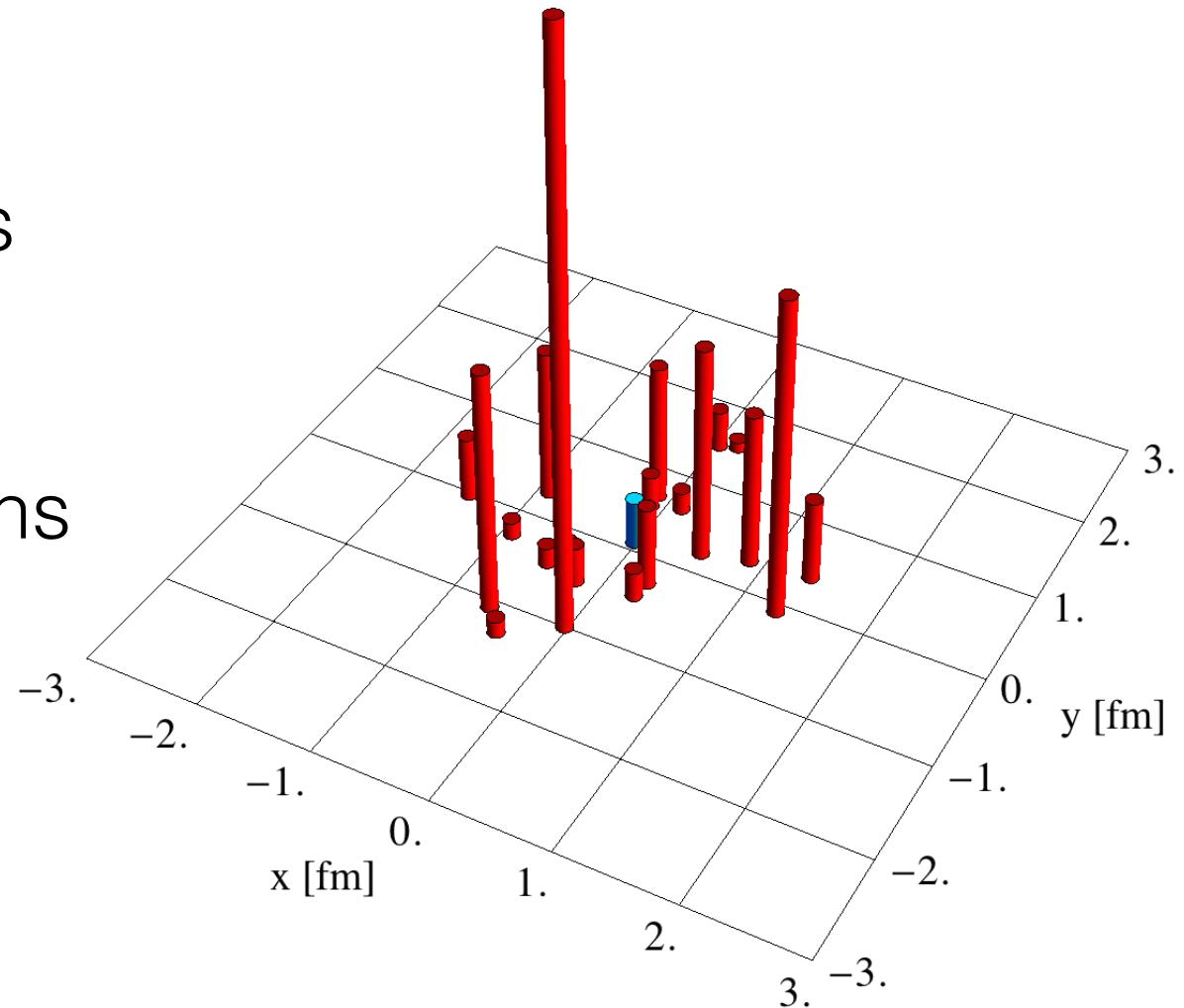
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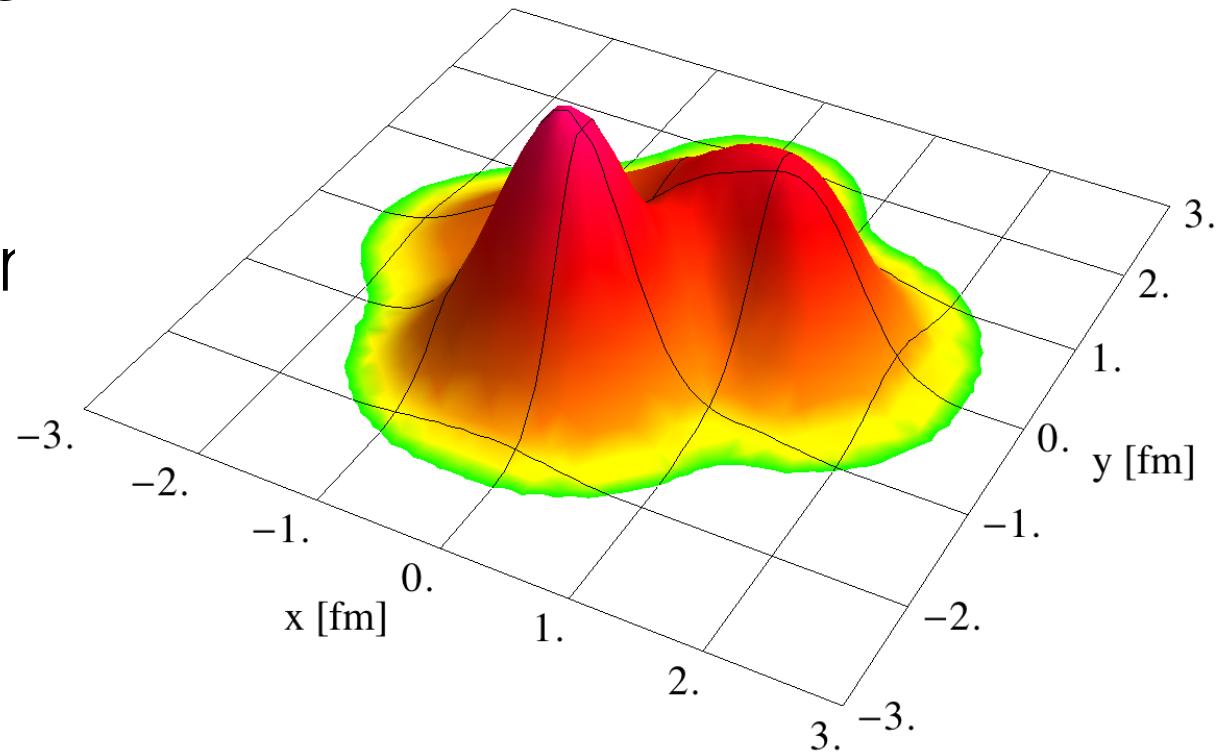
- sample participants
- add sources
- add NBD fluctuations



# Initial conditions: Glauber+NBD

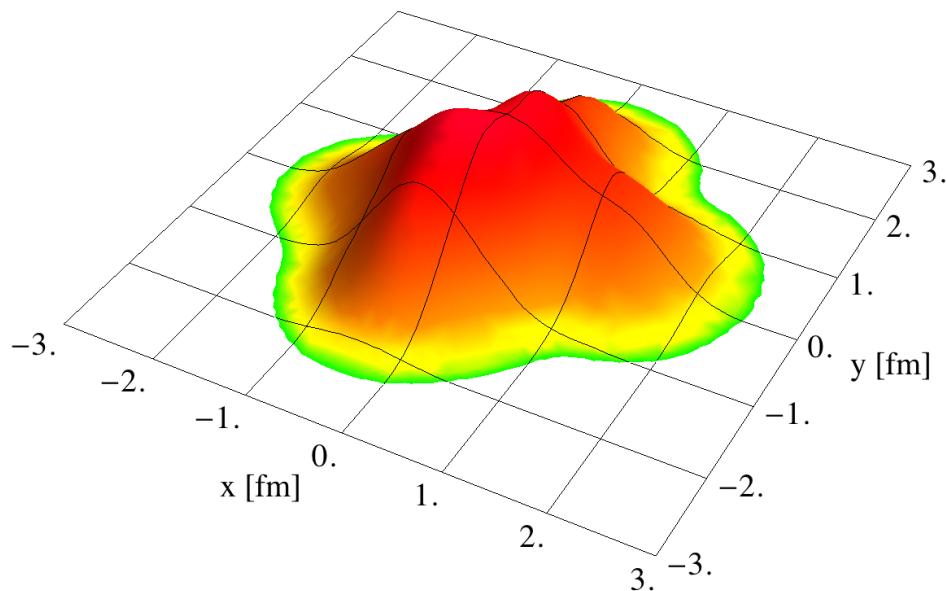
$$\sigma = 0.40 \text{ fm}$$

- sample participants
- add sources
- add NBD fluctuation
- increase  $\sigma$



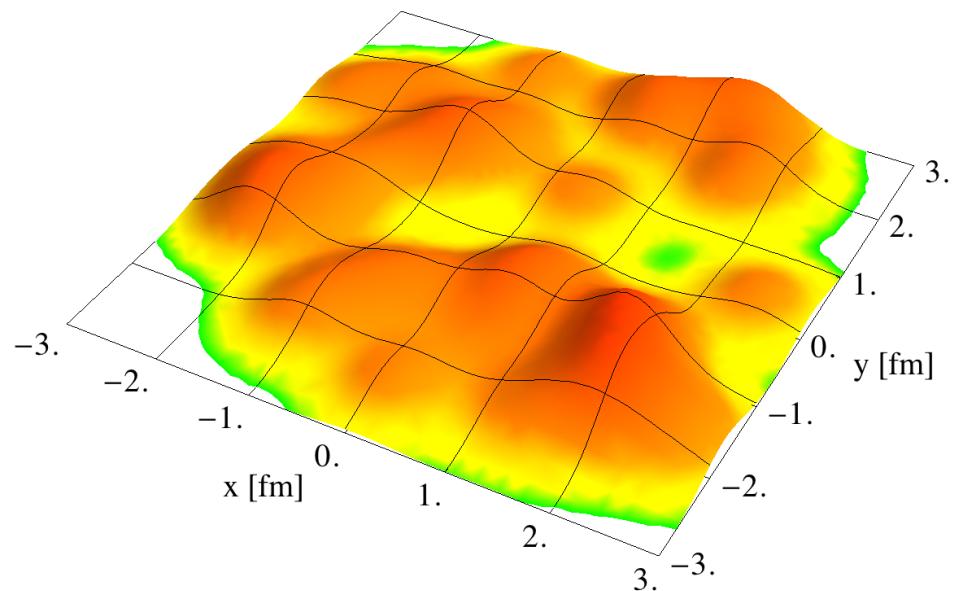
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pPb

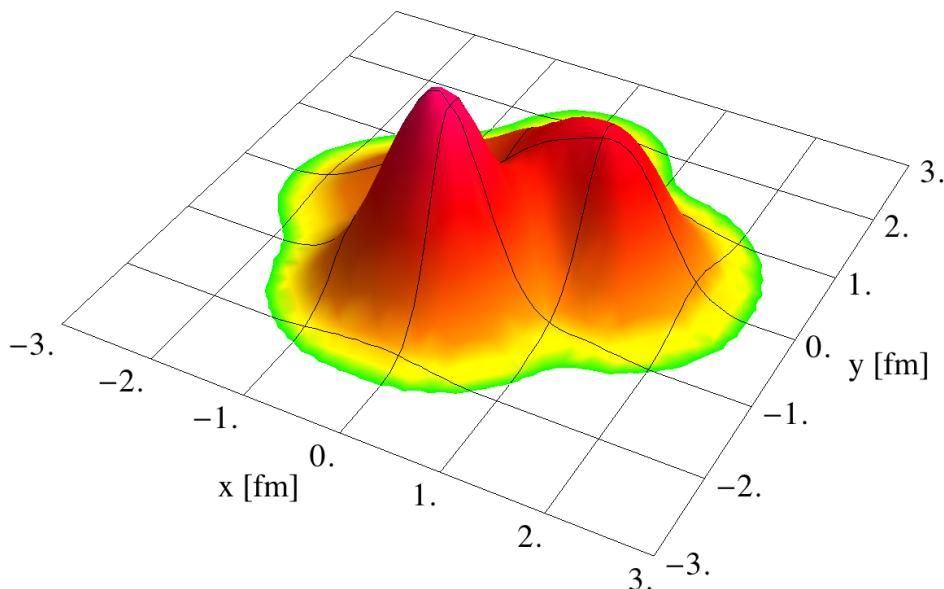
$$\sigma = 0.40 \text{ fm}$$



PbPb

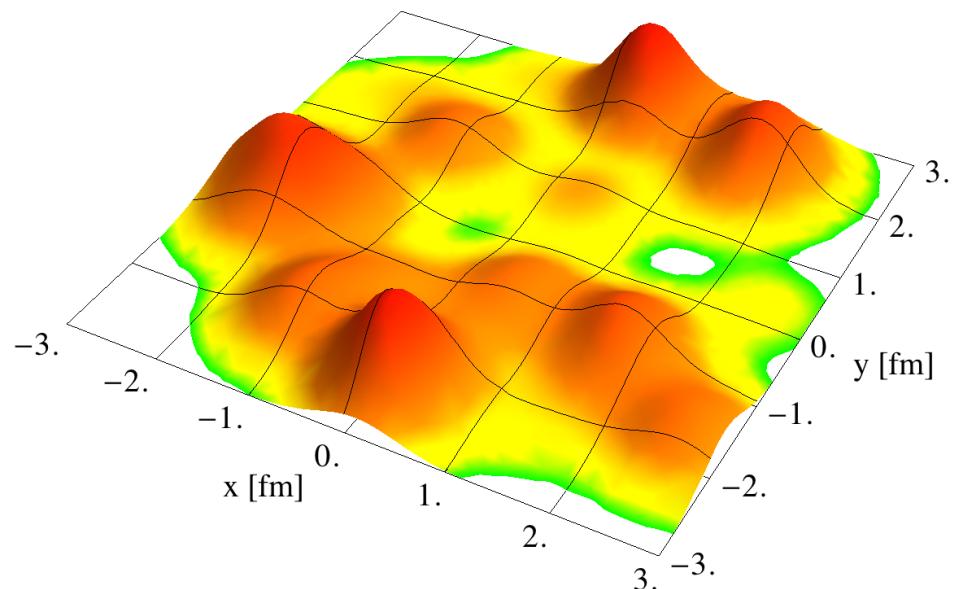
# Initial conditions: Glauber+NBD

$$\sigma = 0.40 \text{ fm}$$



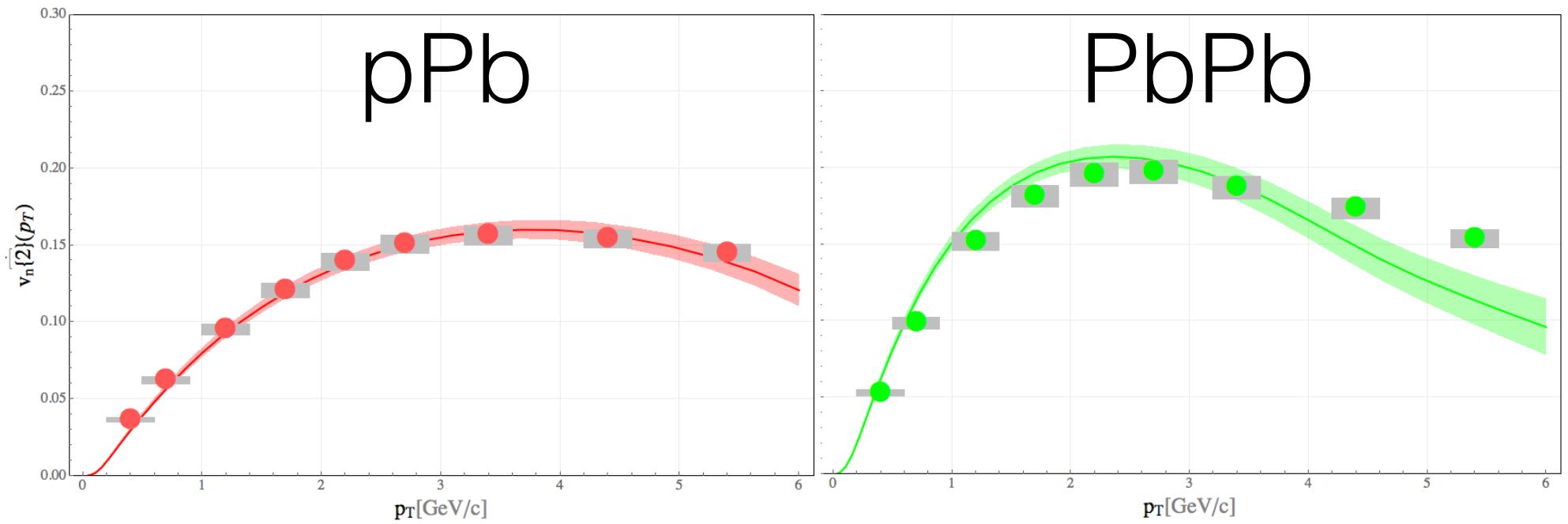
pPb

$$\sigma = 0.40 \text{ fm}$$

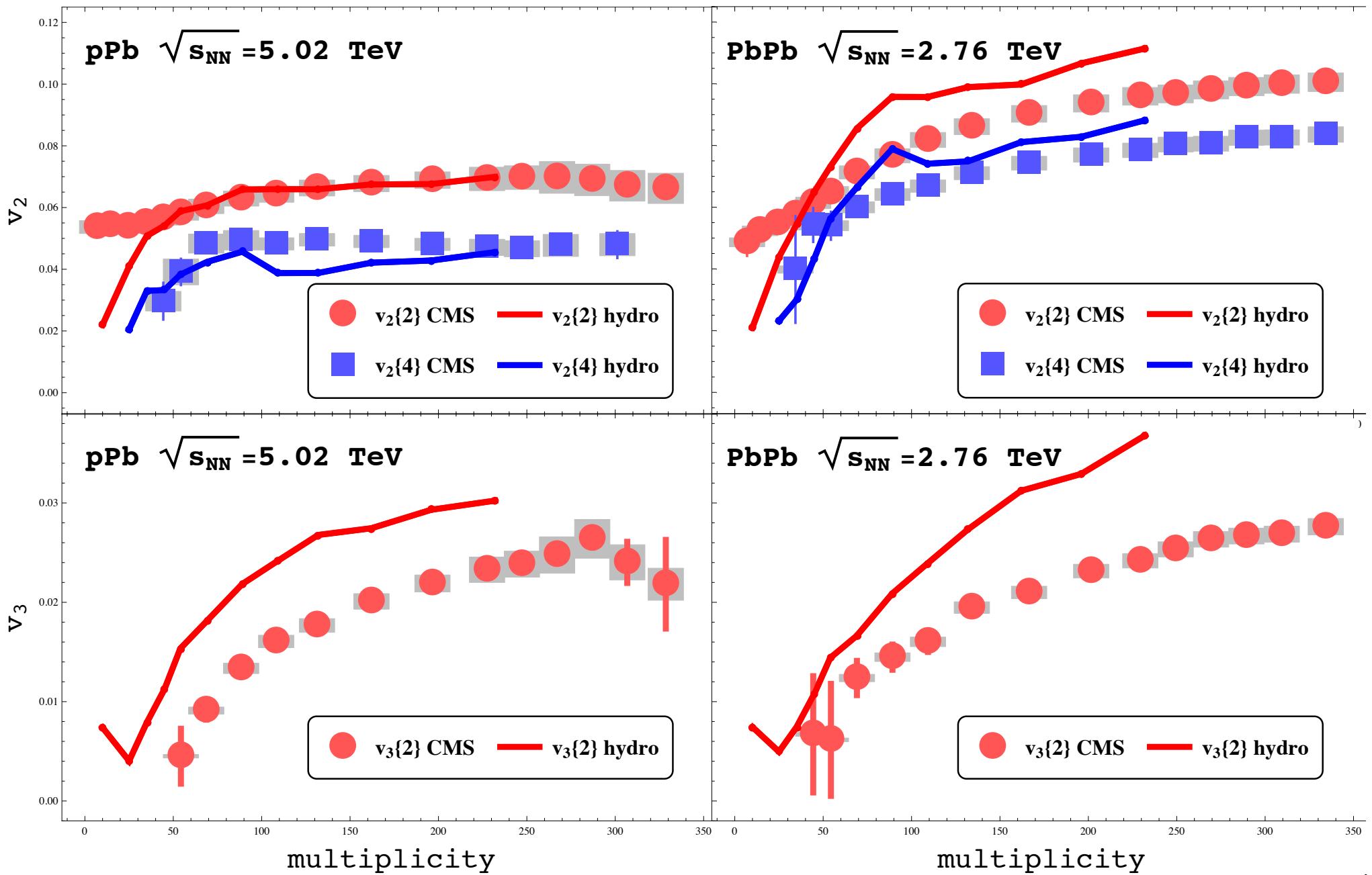


PbPb

# Flow observables for pPb and PbPb



# Flow observables for pPb and PbPb



## experiment:

$$V_{n\Delta}(p_T^a, p_T^b) \equiv \langle \overline{\cos n(\phi^a - \phi^b)} \rangle$$

$$\frac{dN_{pairs}}{d^3p^a d^3p^b} \stackrel{\text{(flow)}}{=} \frac{dN}{d^3p^a} \times \frac{dN}{d^3p^b}$$

$$\langle \overline{e^{in(\phi^a - \phi^b)}} \rangle = \langle \overline{e^{in\phi^a}} \cdot \overline{e^{-in\phi^b}} \rangle$$

$$v_n^a e^{in\Psi_n^a} \equiv \overline{e^{in\phi^a}}$$

$$V_{n\Delta}^{ab}(p_T^a, p_T^b) = \langle v_n^a v_n^b e^{in(\Psi_n^a - \Psi_n^b)} \rangle$$

$$V_{n\Delta}(p_T^a, p_T^a) \geq 0$$

$$\begin{aligned} V_{n\Delta}(p_T^a, p_T^b)^2 &\leq \\ V_{n\Delta}(p_T^a, p_T^a) V_{n\Delta}(p_T^b, p_T^b) & \end{aligned}$$

$$r_n \equiv \frac{V_{n\Delta}(p_T^a, p_T^b)}{\sqrt{V_{n\Delta}(p_T^a, p_T^a) V_{n\Delta}(p_T^b, p_T^b)}}$$