



# **Simulation of space charge effects during multiturn injection with the codes PATRIC and pyORBIT**

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**Space charge workshop 2013, CERN**

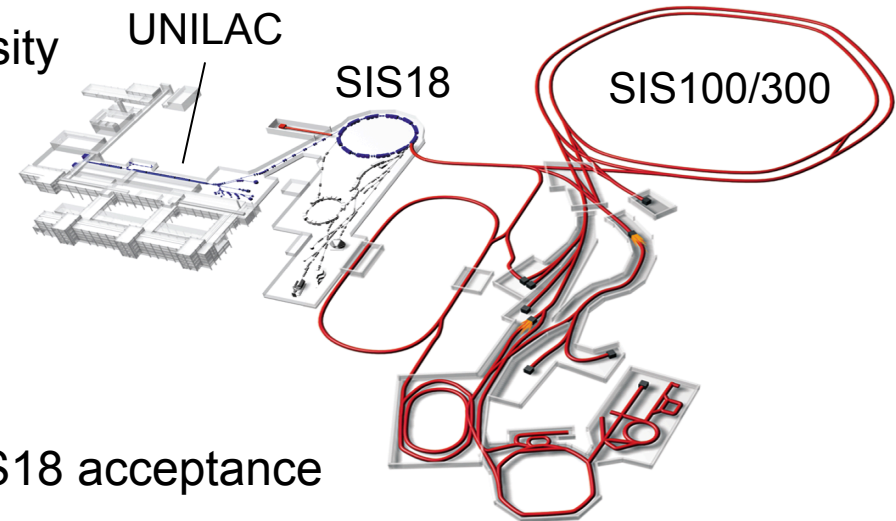
# Outline

- SIS18 upgrade program for FAIR: Optimization of the multiturn injection
- Multiturn injection into SIS18: Horizontal betatron stacking
- Simulation code:
  - PATRIC
  - pyORBIT
- MTI simulation studies
  - Comparison between codes (low and high current)
  - Comparison between experiments and simulations (low current)
- Summary and Outlook

# SIS18 upgrade program

## Optimization of the **M**ulti**T**urn **I**njection (MTI)

- SIS18 upgrade to increase the beam intensity
- Crucial point: **Optimization of MTI**
- Minimal beam loss:
  - To achieve design intensities
  - Dynamic vacuum pressure
- Max. number of inj. turns are limited by SIS18 acceptance and UNILAC beam emittance

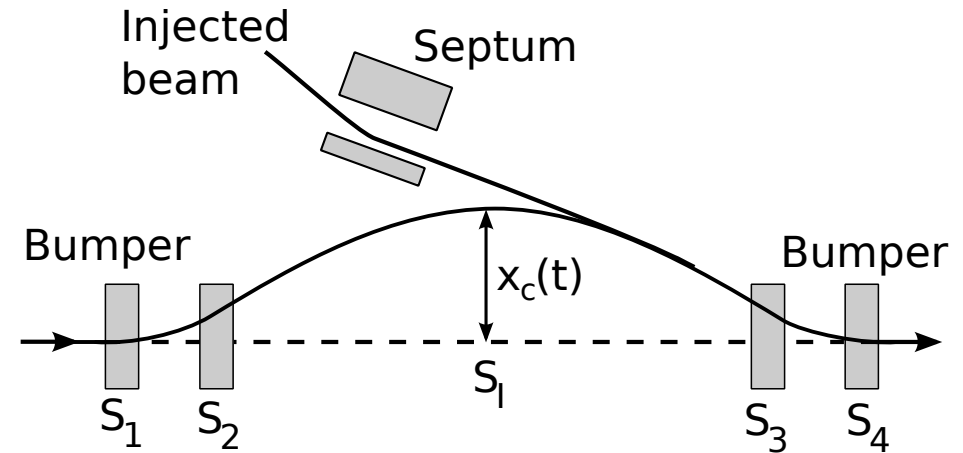
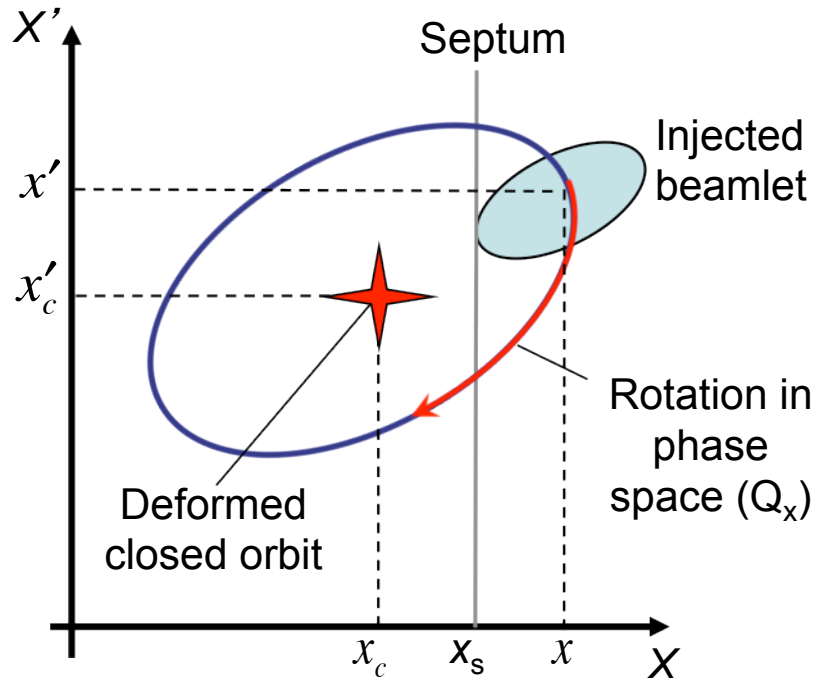


- Development of detailed simulation model
- Validation of the current model used in operation control program (SISMODI)
- Comparison between experiments and simulations for low and high currents
- Impact of space charge on MTI efficiency

|                        | UNILAC           | SIS18            |
|------------------------|------------------|------------------|
| Reference primary ion  | U <sup>28+</sup> | U <sup>28+</sup> |
| Reference energy (MeV) | 11.4             | 200              |
| Ions per bunch/cycle   | 1.5E10           | 1.5E11           |
| Hor. Emittance (rms)   | 2-3              | 50               |

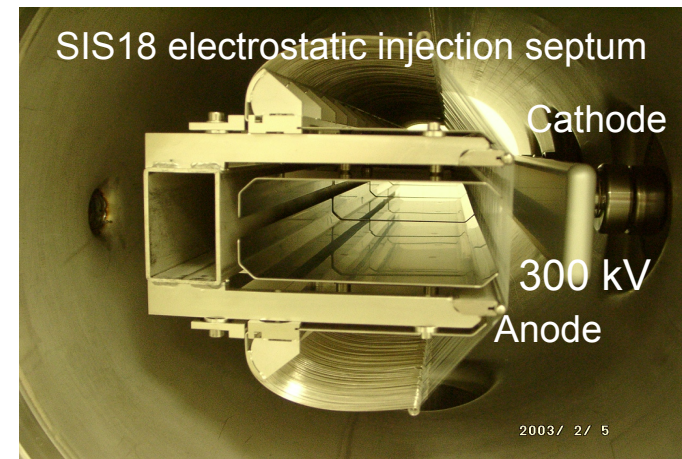
# Multiturn injection into SIS18

## ”Horizontal betatron Stacking”



- Liouville's theorem: Injection only into free phase space
- Betatron oscillation and changing of orbit bump  
→ free phase space
- Loss of ions at the septum due to the betatron oscillation

▪ Dilution during injection 
$$D = \frac{\epsilon_f}{n_{mti} \epsilon_i}$$



# Simulation code

## PARTICLE TRACKING CODE (PATRIC)

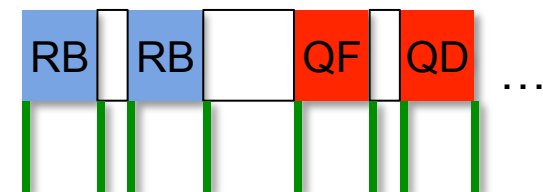
- Pic class (representation of particles)
  - Number of particles increases during injection and decreases by losses

- SectorMap + BeamLine class (container for ion optical elements)

- Input from MADX (thick lens)
- Transport of particles



- Several classes to represent particle kicks
  - Self-consistent space charge kicks
  - Poisson's equation is solved on 2D transverse grid



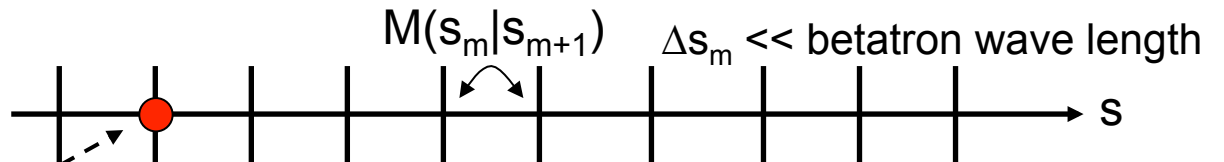
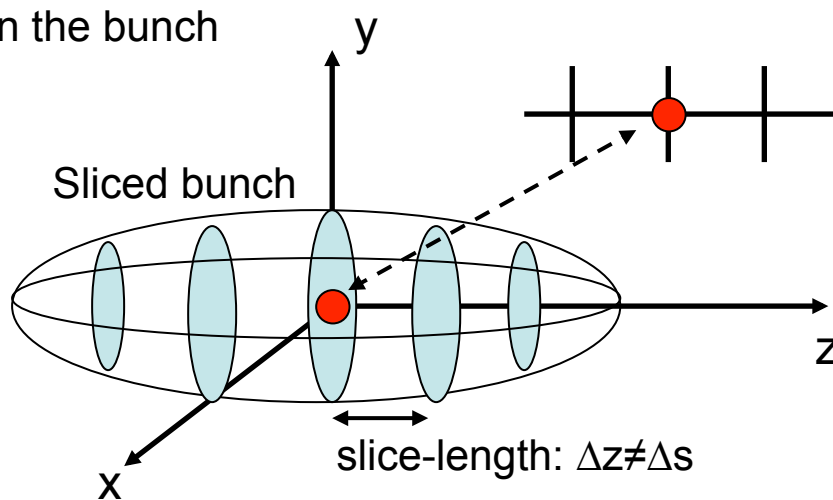
- Bump class (represents injection kickers)



# PATRIC Code: Space charge solver

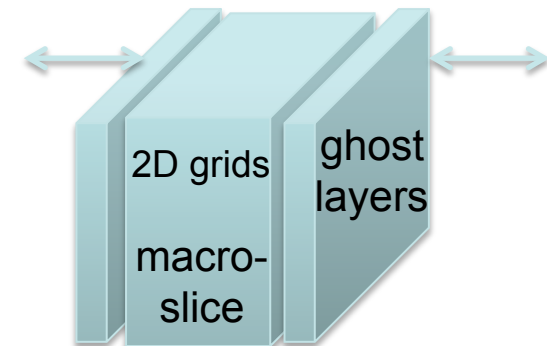
z: longitudinal position  
in the bunch

$s_m$ : position in the lattice



The transfer maps M are  
'sector maps' taken from MADX.

MPI send/receive  
to neighbor slices



2D space charge field for each slice:

$$\rho(x, y, z, s_m) = \sum_j Q_j S(\vec{x} - \vec{x}_j) \quad (\text{3D bi-linear interpolation})$$

$$\frac{\partial E_x}{\partial x} + \frac{\partial E_y}{\partial y} = \frac{\rho(x, y, \{z, s_m\})}{\epsilon_0} \quad (\text{fast 2.5D Poisson solver})$$

Transverse potential obtained for the 2D grid at z  
and lattice position s:

3D Grid-> Particle / Particle->Grid interpolation

➤ Grid slices "feel" all other slices

O. Boine-Frankenheim, ICAP 2012

# Simulation code

## Python Objective Ring Beam Injection and Tracking (pyORBIT)

- Bunch class (representation of particles)
  - Number of particles increases during injection and decreases by losses

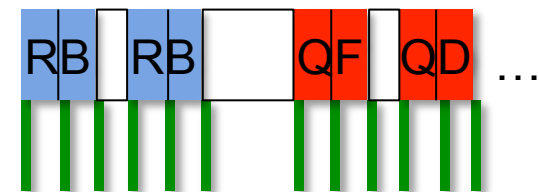
- Teapot class (container for ion optical elements)

- Input from MADX (thin lens)
- Notes for optical elements + collimator, injection, sc, ...



- Space charge solver

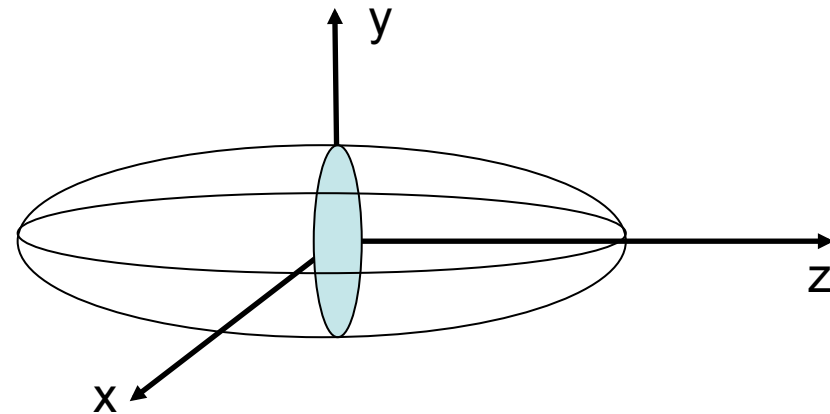
- Self-consistent space charge kicks
- Poisson's equation is solved on 2D transverse grid



- Kickernodes class (represents injection kickers)

# PyORBIT: Transverse Space Charge

- Solving Poisson equation on 2D grid
- Transverse momentum kicks between lattice elements



Particles are binned in 2D rectangular grid (momentum-conserving interpolation scheme)

Fast FFT solver  
Space charge direct force solver

Particle kicks are obtained by interpolating the potentials  
Kicks are weighted by local longitudinal density (bunch factor)

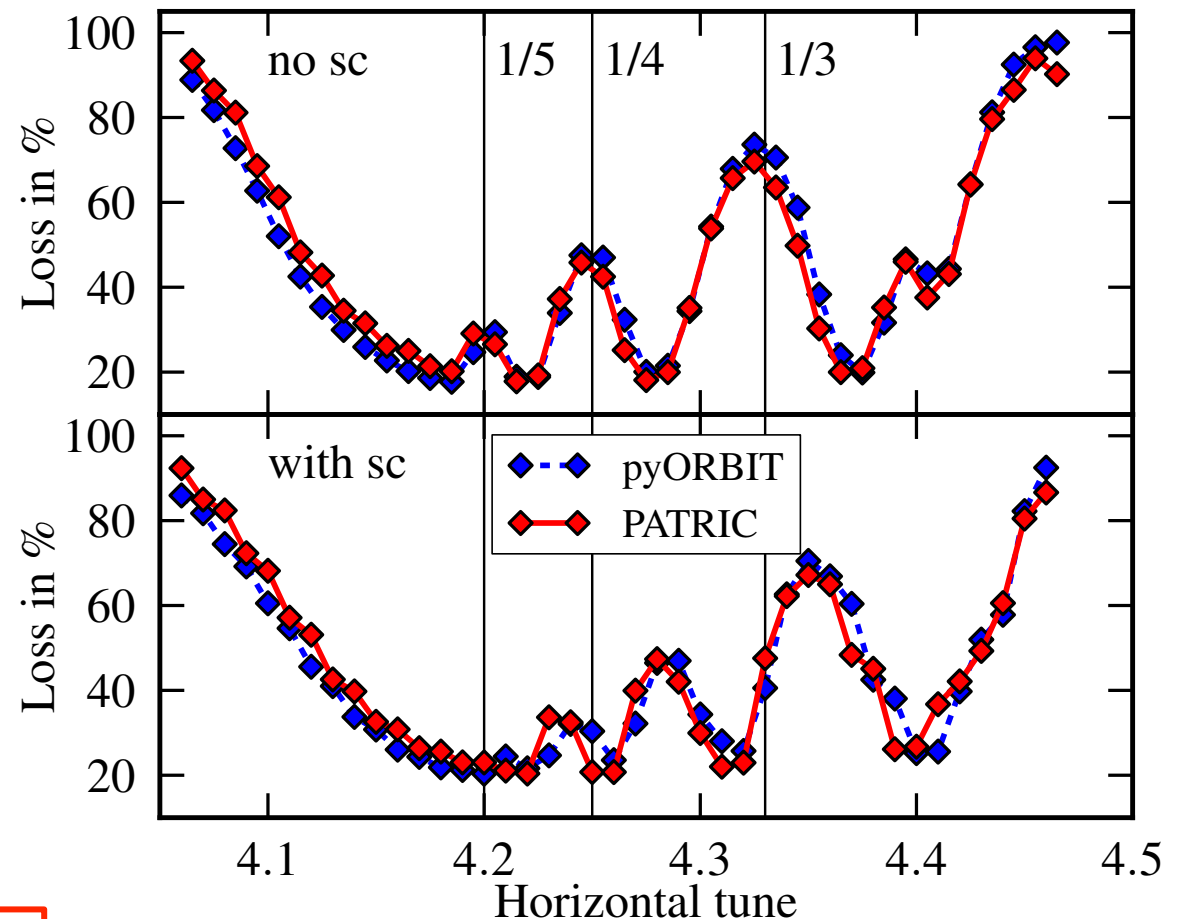
Source: Talks by S. Cousineau and J.A. Holmes, ORNL



# MTI simulation studies

## Comparison between codes

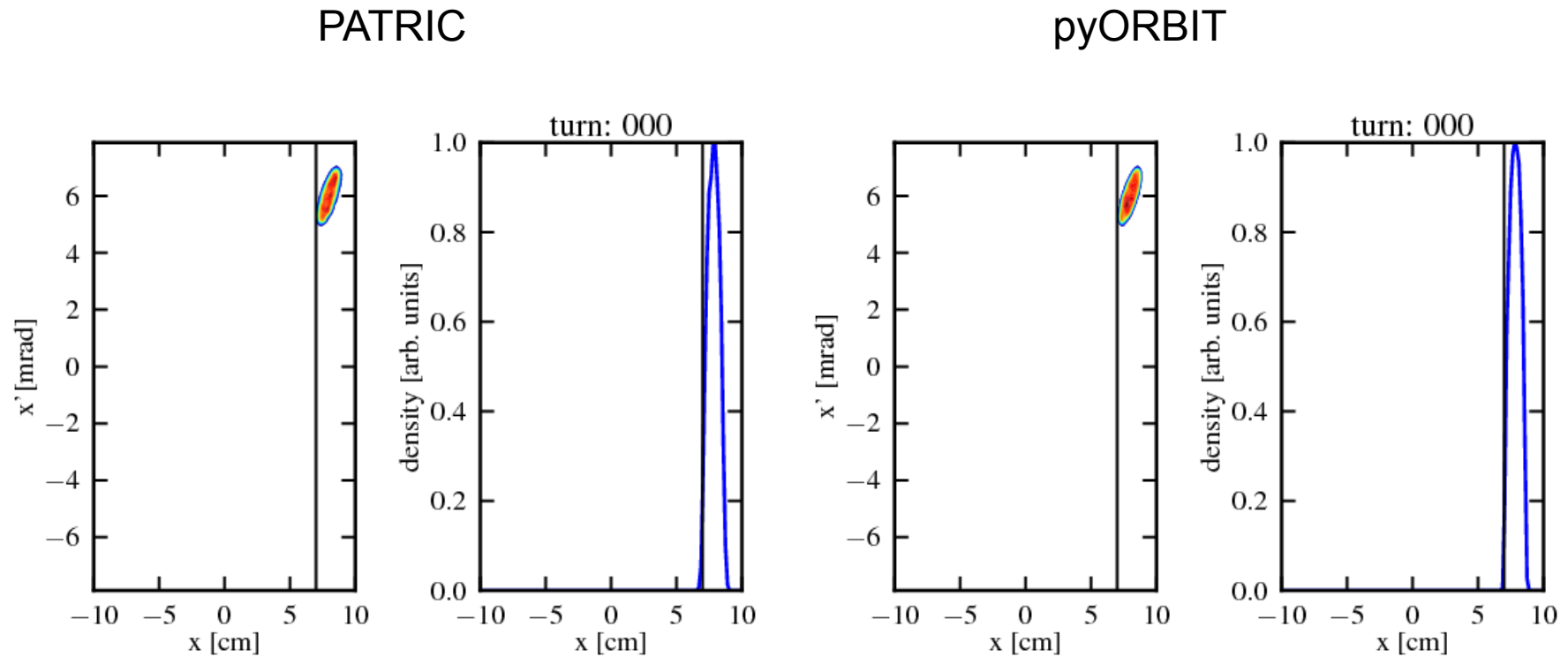
- Simulation settings:
  - KV+ Coasting beam
  - Injection of 20 beamlets
  - Linear orbit bump reduction
  - Linear SIS18 lattice
  - Collimation only at septum
- The loss maxima are located at 0, 1/2, 1/3, 1/4
- Both codes show the resonant character
- With space charge the maxima and minima of the efficiency are shifted
- Codes are in good agreement for loss calculation



# MTI simulation studies

## Comparison between codes

- Movie of a MTI without space charge effects



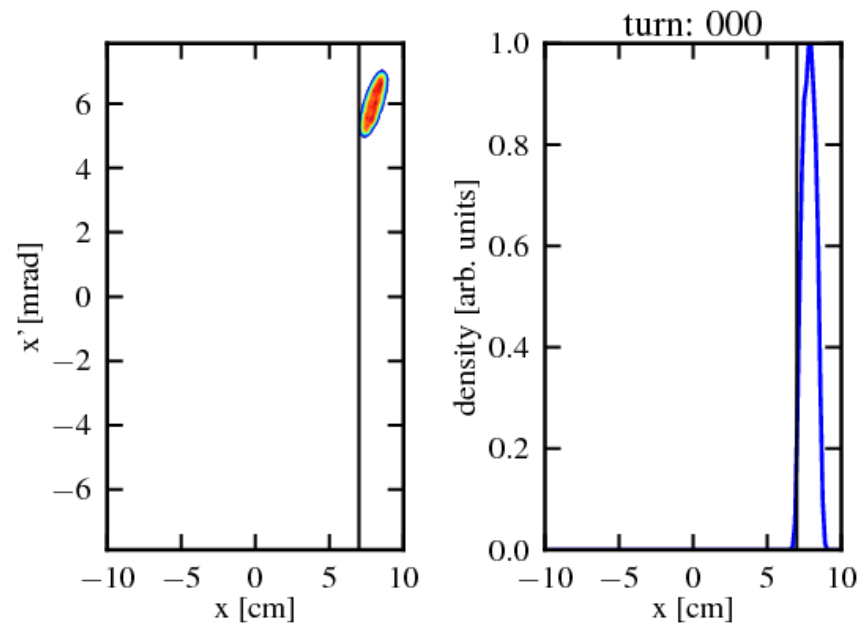
- Kaleidoscope images at injection point

# MTI simulation studies

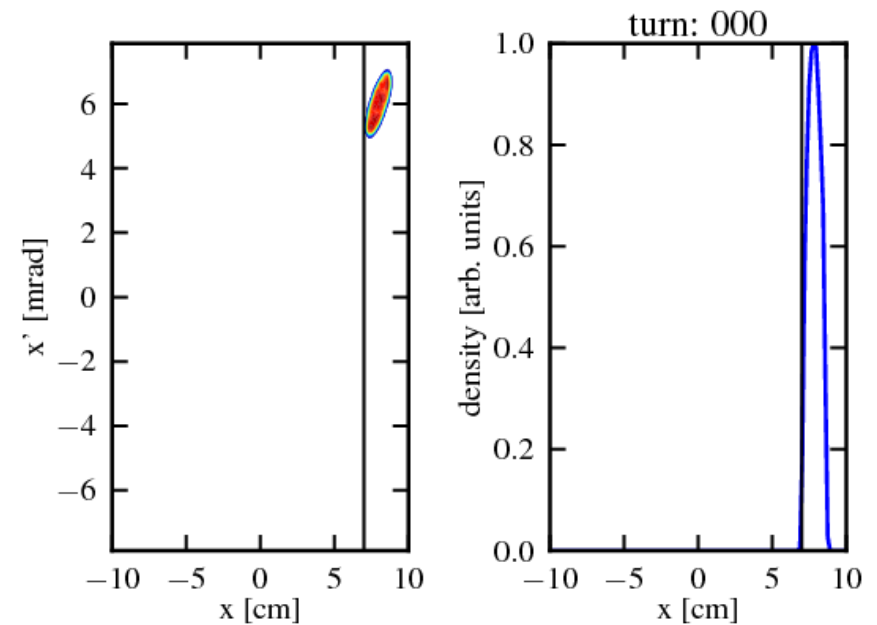
## Comparison between codes

- Movie of a MTI with space charge effects

PATRIC



pyORBIT

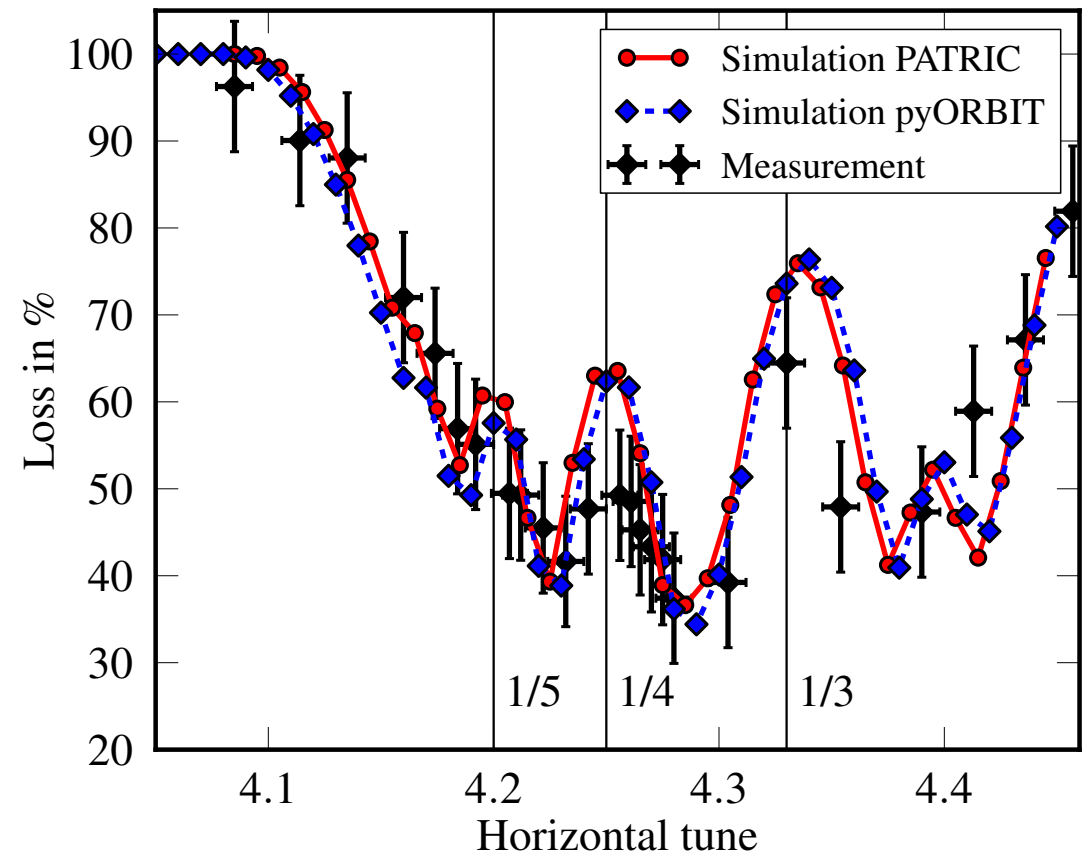


- Kaleidoscope images at injection point

# MTI simulation studies

## Comparison between experiments and simulations

- Simulation settings:
  - Machine settings of  $x_c = 85$  mm and  $\Delta x_c = 2.5$  mm per turn
  - SISMODI Model
  - Measured beamlet emittance
  - Injection of 21 beamlets
- Measurement results provided by Y. El-Hayek, GSI
  - Low current, no sc effects
  - Error bars: current fluctuation
- The loss maxima are located at the same fractional tunes



- Measurement and simulations are in good agreement

# Summary

Summary:

- Comparison between codes
  - For loss calculation in good agreement
- Comparison between experiments and simulation
  - For low beam currents a good agreement is obtained
- Impact of space charge on MTI efficiency
  - Strongly changes the particle distribution
  - Affects the losses (strength depends on the horizontal tune)