

Status of Space Charge Effects Studies during Bunch Compression in the future FAIR SIS-100

Sandra Aumon – GSI

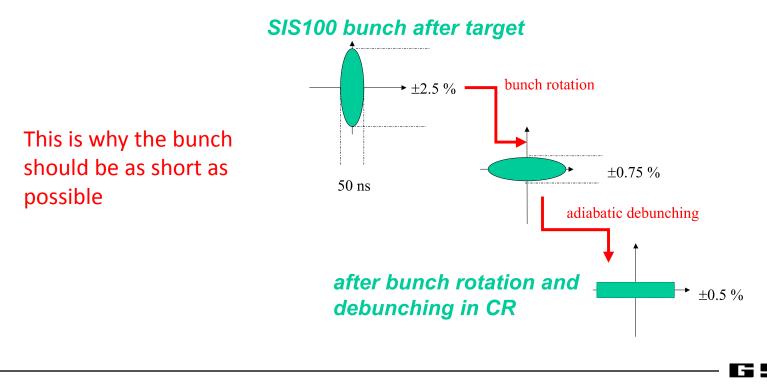
Acknowledgements to O. Boine Frankenheim, G. Franchetti, S. Appel, R. Bruce

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Final Bunch Compression in SIS-100 FAIR

- Intense short ions beam required by experiments for <u>plasma physics</u> and <u>exotic elements productions</u>
- 50ns ions beams after final bunch rotation. Why short beams ? Example:



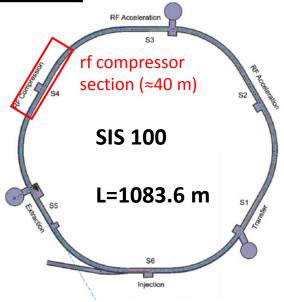
Final Bunch Compression in SIS-100 FAIR

RF cavity systems in SIS 100:

	#cav	ities	Voltage [kV]	Frequency [MHz]	Concept	
Acceleration	20		400	1.1-2.7 (h=10)	Ferrite	
Compression	16		600 (later 1MV)	0.4-0.5 (h=2)	MA (low duty cycle)	
		Partic	les/bunch	bunch length]	RF Acceleration
1.5 GeV/u U ²⁸⁺		5x10 ¹¹		50 ns		rf compressor
29 GeV/u p		2-4x10 ¹³		25 ns	2	section (≈40 m) s₂



Magnetic alloy RF cavity for bunch compression

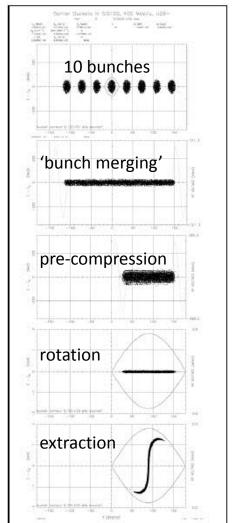


Courtesy O.Boine Frankenheim (HB2008)

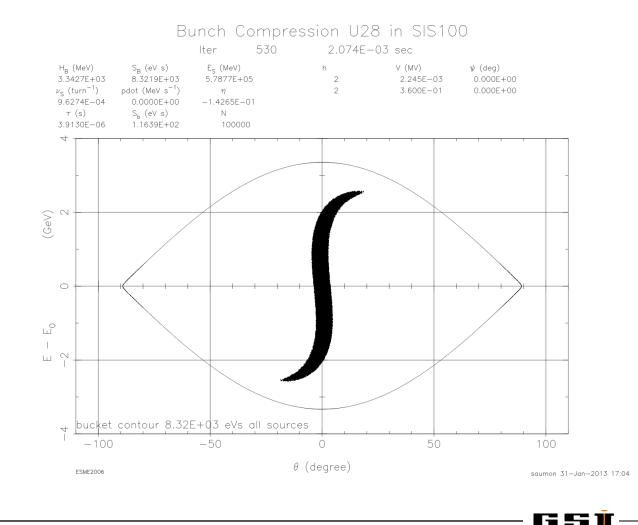


Final Bunch Compression in SIS-100 FAIR

Single bunch formation



50 ns full bunch length after compression required.



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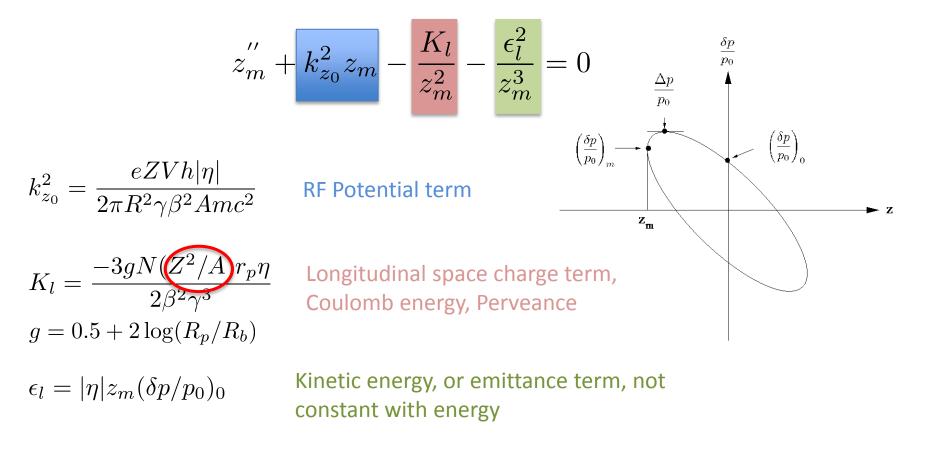
Aim SC studies during the rotation

- What can be wrong during the compression ?
 - Influence of longitudinal space charge
 - Transverse space charge tune shift
 - Resonance crossing ?
 - Effects of transverse space charge on the dispersion and beta functions.
- Squeleton of the study
 - Longitudinal studies (Need the simulations)
 - Analytical study with Venturini transverse envelop equations
 - Apply to the SIS100 and the beam transfer

Effect of transverse space charge on the optics and beam spot at the target (Still on going)

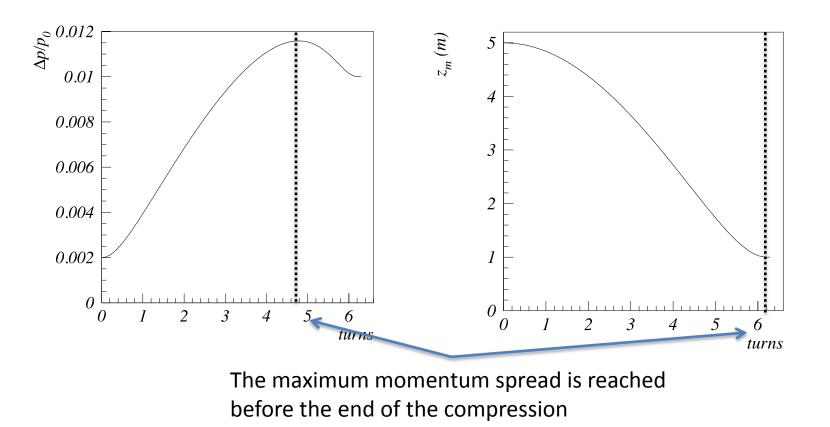
- Should be supported by simulations (for instance with PyOrbit, 3D) (preliminary convergence studies on going)
- SIS-100 has a tiny loss budget (!!! See Giuliano's talk)

Longitudinal envelop equation



Ref[1]: M. Reiser, "Theory and Design of Charged Particle Beams". Ref[2]: G. Franchetti, I. Hofmann, G. Rumolo, *PhysRevSTAB.3.084201*

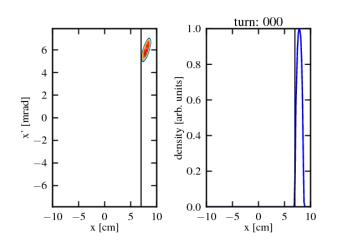
Effect of longitudinal space charge during the bunch compression



Examples from G. Franchetti, I. Hofmann, G. Rumolo, PhysRevSTAB.3.084201

Beam parameters at SIS-18 injection FA

Beam Parameters				
Kinetic Energy (MeV/u)	11.4			
Particle	U ²⁸⁺			
Total Energy (MeV)	224 415			
beta/gamma	0.15/1.01			
Momentum Compaction factor η	-0.94			
Harmonic number h	2			
Revolution number (µs)	4.68			



Parabolic distribution in momentum

<u>Δp/p=1e-3</u>

Courtesy S. Appel

Longitudinal bunch area is computed from coasting beam SIS-18 injection parameters.

$$\mathcal{A} = 400.4 \text{ eVs}$$



Beam parameters before the final bunch compression in the SIS-100

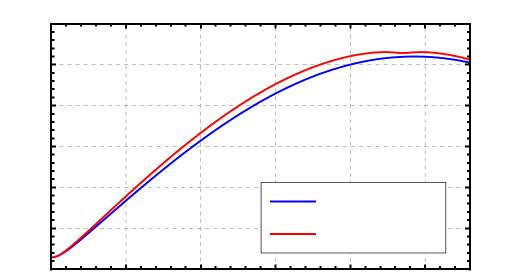
Beam Parameters					
Radius (m)	172.5				
Circumference (m)	1083.6				
Extraction Kinetic Energy (GeV/u)	1.5				
Total Energy (GeV)	552.553				
Beta/gamma	0.91/2.49				
Gamma transition	15.6				
Harmonic number h	2				
Revolution period (µs)	3.95				
# bunches	1 (one empty bucket)				
Momentum Compaction factor η	-0.15				
RMS transverse emittance @ 1.5GeV/u	H 3.4, V 1.1 mm.mrad				

F4

Bunch Compression in SIS-100

The longitudinal space charge is a weak effect on the final momentum spread at the end of the bunch compression

Will depend on the g factor.



$$g = 0.5 + 2\ln\left(\frac{R_p}{R_b}\right)$$

Rp Radius pipe Rb Radius beam

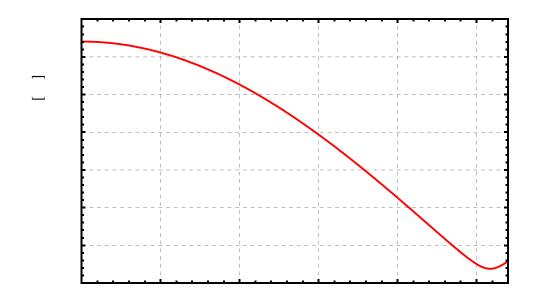


FAIR

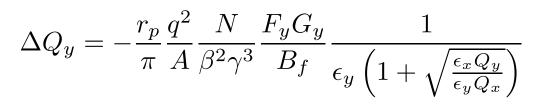
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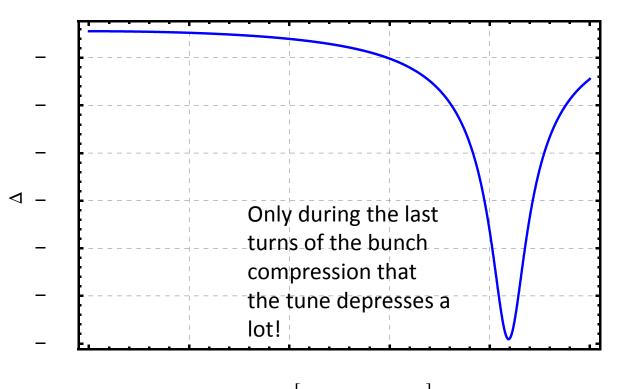
Present Situation

- If the bunch to bucket transfer from SIS-18 to SIS-100 is not improved, longitudinal dilution **by factor 2** is the present situation.
- 360 kV available for compression voltage day 1, a full bunch length of 75 ns is expected from longitudinal envelop equation.



Transverse Space Charge Tune Shift FAIR



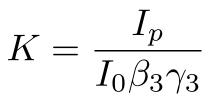


Transverse Envelope Equations

Transverse envelop model (see Reiser book)) = a(s + L), b(s) = b(s + L)

ferential equation solvers can be dominated beams. The matcher closed orbit condition of Eq. (a: hor. Beam size b: vert. Beam size

(11)



Interesting for beam with high momentum spread

$$H = \frac{1}{2} p_x^2 + \frac{k_x(z)}{2} x^2 + \frac{m^2 c^4}{E_o^2} \delta^2 - \frac{x}{\rho(z)} \delta.$$

$$\overline{H} = \frac{1}{2} \overline{p}_x^2 + \frac{k_x}{2} \overline{x}^2 + \frac{m^2 c^4}{E_o^2} \delta^2 + \delta \overline{x} \left(D'' + k_x D - \frac{1}{\rho} \right) + \dots.$$

$$\epsilon_{\overline{x}}^2 = \epsilon_{dx}^2 = (\langle x^2 \rangle - 2D \langle x \delta \rangle + D^2 \langle \delta^2 \rangle) + \langle \langle p_x^2 \rangle - 2D' \langle p_x \delta \rangle + D'^2 \langle \delta^2 \rangle) + \langle \langle x p_x \rangle - D \langle p_x \delta \rangle - D' \langle x \delta \rangle + DD' \langle \delta^2 \rangle)^2.$$



Transverse envelop model Venturini et al.PhysRevLetter, Volume 81, number 1

$$\sigma_x'' = \underbrace{\epsilon_{dx}^2 + (\sigma_x \sigma_x' - DD'\langle \delta^2 \rangle)^2}_{\sigma_x (\sigma_x^2 - D^2 \langle \delta^2 \rangle)} - \frac{1}{\sigma_x} (\sigma_x')^2 - k_x \sigma_x + \frac{K}{2(\sigma_x + \sigma_y)} + \frac{\langle \delta^2 \rangle}{\sigma_x} \Big(\frac{D}{\rho} + D'^2\Big),$$
(10)

$$\sigma_y'' = \frac{\epsilon_y^2}{\sigma_y^3} - k_y \sigma_y + \frac{K}{2(\sigma_x + \sigma_y)}.$$

$$D'' + \left[k_x(z) - \frac{K}{2\sigma_x(\sigma_x + \sigma_y)}\right] D = \frac{1}{\rho(z)}.$$

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Circumference L	1083.6 m
Radius R	172.6 m
Transverse tune Q	18.8
Lorentz factor β/Y	0.92/2.60
Βρ	63 T.m
Bending radius ρ	31.68 m
Smooth k	0.01188 m ⁻²
Smooth β function	9.17 m
Smooth dispersion D	2.66 m
Transverse RMS ε	H 3.4, V 1.1
	mm.mrad
Final bunch length	50 ns (full)

Strength smooth focusing approximation

$$< k > = \left(\frac{2\pi Q}{L}\right)^2$$

Beta function smooth focusing approximation

$$<\beta>=\frac{R}{Q}$$

Dispersion smooth focusing approximation No space charge

$$D'' + kD = \rho$$

With D"=0 Matched beam

$$D = \frac{\rho}{\langle k \rangle}$$

Supposing no longitudinal dilution between SIS18 and SIS100 – <u>very optimistic</u>



FAI

• Stationary solutions for constant focusing $D'' = \sigma_x'' = \sigma_y'' = \sigma_x' = \sigma_y' = D' = 0$ (matched beam)

$$\frac{\epsilon_{dx}^2}{\sigma_x(\sigma_x^2 - (D\delta)^2)} - \langle k \rangle \sigma_x + \frac{K_{sc}}{2(\sigma_x + \sigma_y)} + \frac{\delta^2}{\sigma_x} \left(\frac{D}{\rho}\right) = 0$$

$$\frac{\epsilon_y^2}{\sigma_y^3} - \langle k \rangle \sigma_y + \frac{K_{sc}}{2(\sigma_x + \sigma_y)} = 0$$

Simple (!) system of equations to solve

$$D\left(\langle k \rangle - \frac{K_{sc}}{\sigma_x(\sigma_x + \sigma_y)}\right) = \frac{1}{\rho}$$



F₄



FAIR

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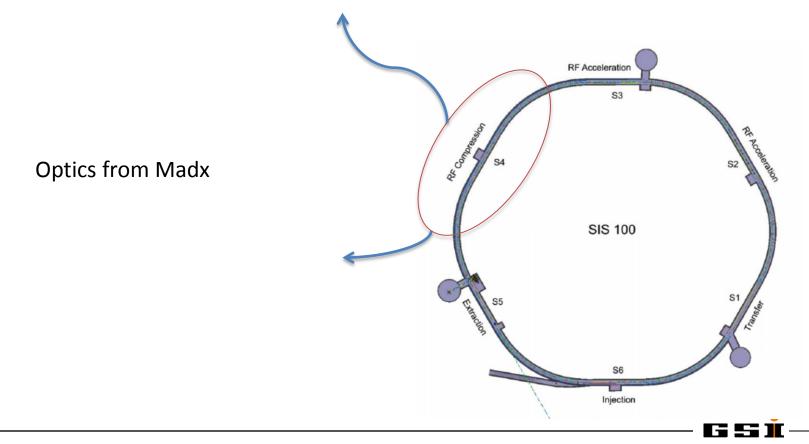
Sens of compression

Moderate effect In constant focusing



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- SIS-100: 6 sectors of ~ 180 m
- Dispersion suppression



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- Read a Madx file with : s location, Kxy (strenght of quad), I (length of each element), bending angle
- Integration of the equations element by element.
- Method used for integration Runge-Kutta with a maximum step size integration 1mm
- Small envelop tracking w/wo space charge.
- Any other suggestion for other integrator ?
- This is not final, because extraction line is going up ! <u>Vertical dispersion</u>! Will be add later.

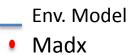
$$\sigma_x'' = \frac{\epsilon_{dx}^2 + (\sigma_x \sigma_x' - DD'\langle \delta^2 \rangle)^2}{\sigma_x (\sigma_x^2 - D^2 \langle \delta^2 \rangle)} - \frac{1}{\sigma_x} (\sigma_x')^2 - k_x \sigma_x + \frac{K}{2(\sigma_x + \sigma_y)} + \frac{\langle \delta^2 \rangle}{\sigma_x} \left(\frac{D}{\rho} + D'^2\right),$$
(10)

$$\sigma_y'' = \frac{\epsilon_y^2}{\sigma_y^3} - k_y \sigma_y + \frac{K}{2(\sigma_x + \sigma_y)}.$$
 (11)

$$D'' + \left[k_x(z) - \frac{K}{2\sigma_x(\sigma_x + \sigma_y)}\right] D = \frac{1}{\rho(z)}.$$

1 SIS-100 sector

1 SIS-100 sector



Comparison of my small tracking code with the optics computing by Madx. No space charge and (delta p/p=0) Good agreement.

$$Q_{x,y} = \frac{1}{2\pi} \int_{s}^{s+C} \frac{1}{\beta_{x,y}(s)} ds$$

Qx=18.84 Qy=18.63

From envelope equation

18.72 with madx

Vertical Beta change with space charge for the expected vertical tune shift, initial conditions in the tracker the same as the non-SC case.

- No space charge
- Space charge

dQx~-0.39 dQy~-0.73

Zoom on half sector

Preliminary results shows about 5% change in beta-function at some location

- No SC
- ____ dQy~-0.7

F_A

- ____ Int. x5
- Int. x10

Focus on one part of the SIS-100 sector



- No SC
- dQy~-0.7

FAIR

- ____ Int. x5
 - Int. x10

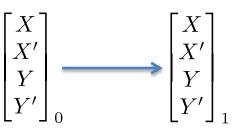
Focus on one part of the SIS-100 sector



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Lattice matching

- Transverse space charge strong enough to change even slightly the optics functions.
- Consequences can be emittance blow up and/or beam size breathing during the transport of the compressed bunch to the target.
- New matching: find new matched solutions.
- Now, Newton Method, not robust yet.



Then delta are applied at each component of the vector

$$\begin{bmatrix} X + \Delta X \\ X' \\ Y \\ Y' \end{bmatrix}$$

In one dimension, with xfp is the fixed point

$$x_{fp} = \frac{x_1 - Jm(x_0)x_0}{1 - Jm(x_0)}$$

$$Jm = \frac{f(x_0 + \Delta x) - x_1}{\Delta x}$$

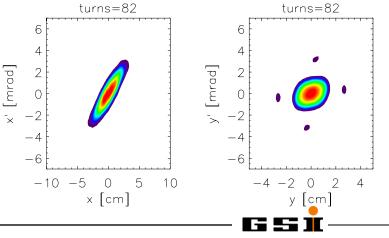
This idea would be to go for Jacobian method like done in Madx (thanks R. De Maria, F. Schmidt)

PIC Simulation

- Use PyOrbit (see the talk of S. Appel for PyOrbit @ GSI)
- What is planned ?
 - Purely longitudinal plan first for bunch compression
 - Longitudinal + Transverse through the full SIS-100 accelerator with space charge.
 - Then transport to the target to see any deformation of the beam spot.
- Status: still in parameterization of the code, testing.
 - Transverse KV distribution from PyOrbit
 - Longitudinal parabolic distribution.

Conclusions - Outlooks

- Longitudinal space charge should not be a problem for SIS-100 operation.
- Large transverse space charge tune shift (~dQx=-0.3, dQy=-0.7) during bunch compression.
- The optics is affected by space charge (up to this point, moderate effect, can be corrected), HOWEVER this has to be propagate through the full lattice and until the target. Vertical dispersion ?
- New periodic solutions for mismatch beams wrt to the extraction line.
- 3D simulations to observe the beam spot at the target but also to compare envelope with analytical formula.
- Other effects during bunch compression (quadrupolar error, resonances etc..)





Spare Slides

