

# Measurement of $\phi_s$ at LHCb

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THE UNIVERSITY  
of EDINBURGH

on behalf of:  
LHCb Collaboration



2013 Phenomenology Symposium May 6-8th

## Results presented in this talk:

- $B_s^0 \rightarrow J/\psi K^+K^-$  and  $B_s^0 \rightarrow J/\psi \pi^+\pi^-$   
(Commonly referred to as  $B_s^0 \rightarrow J/\psi \phi$  and  $B_s^0 \rightarrow J/\psi f^0$  Analyses)

“Measurement of  $\mathcal{CP}$  violation and the  $B_s^0$  meson decay width difference with  $B_s^0 \rightarrow J/\psi K^+K^-$  and  $B_s^0 \rightarrow J/\psi \pi^+\pi^-$  decays”

[arXiv:1304.2600](https://arxiv.org/abs/1304.2600) Submitted to Phys. Rev. D

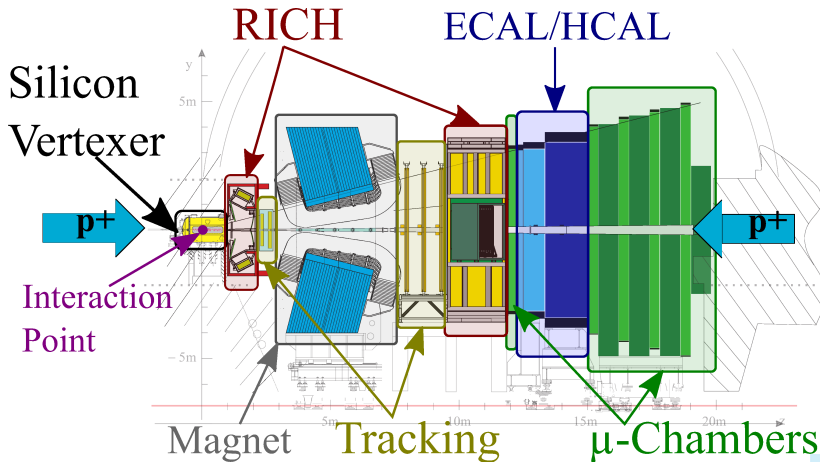
- $B_s^0 \rightarrow \phi \phi$

“First measurement of the  $\mathcal{CP}$ -violating phase in  $B_s^0 \rightarrow \phi \phi$  decays”

[arXiv:1303.7125](https://arxiv.org/abs/1303.7125) Submitted to Phys. Rev. Lett.



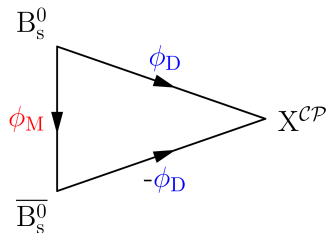
## LHCb Detector



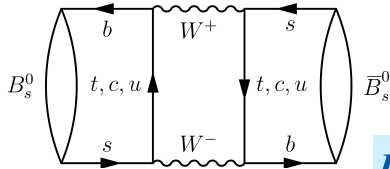
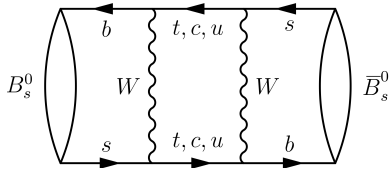
# Definition of $\phi_s$

$\phi_s$  is defined as the phase for  $\mathcal{CP}$ -violation between mixing ( $\phi_M$ ) and decay ( $\phi_D$ ):

$$\phi_s = \phi_M - 2\phi_D$$



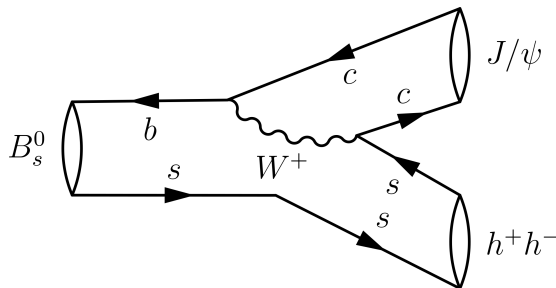
New physics could modify box diagrams and alter  $\phi_M$ .



$B_s^0 \rightarrow J/\psi K^+ K^-$  Phenomenology

$B_s^0 \rightarrow J/\psi K^+ K^-$  and  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$   
 proceed via  $b \rightarrow c \bar{c} s$  transition.

Decay dominated by tree level diagram:



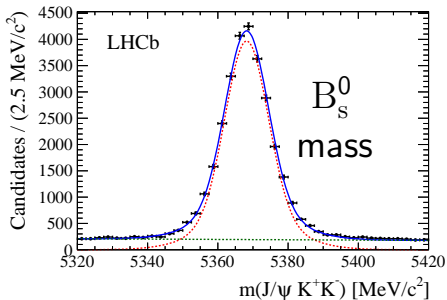
In Standard Model  
 (ignoring penguin pollution)

$$\begin{aligned} \phi_s &= -2\beta_s \\ &= -2 \arg \left( \frac{V_{ts} V_{tb}^*}{V_{cs} V_{cb}^*} \right) \end{aligned}$$

$$\approx -0.0364 \pm 0.0016 \text{ rad}$$

arXiv 1106.4041

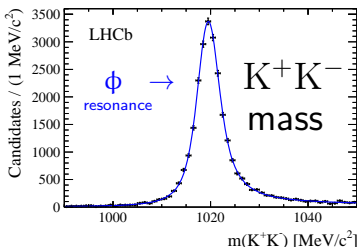
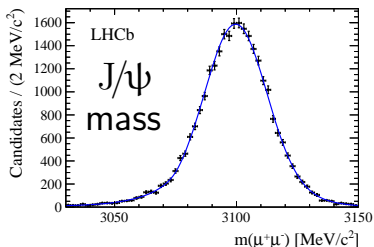


$B_s^0 \rightarrow J/\psi K^+ K^-$  Data

Analysed  $1.0 \text{ fb}^{-1}$  of data from LHCb in 2011.

Still another  $2 \text{ fb}^{-1}$  on disk from 2012 to be analysed.

$N \approx 27,600$  Signal events

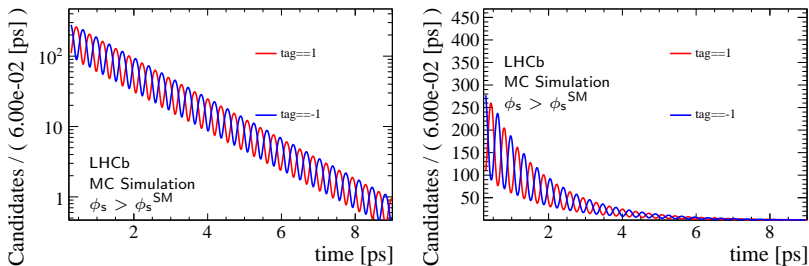


# Fitting for $\phi_s$

Terms sensitive to  $\phi_s$  in the PDF take the form:

$$D_{\text{tagging}}(\omega_{\text{mistag}}) D_{\text{time-res}}(\sigma_t) \sin(\phi_s) \sin(\Delta mt)$$

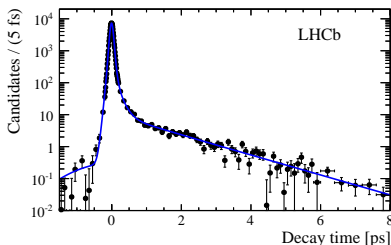
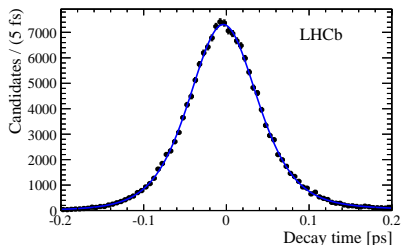
Oscillations in numbers of tagged events with time as below:



# Time Resolution

Time Resolution ( $\sigma_t$ ) calculated from fit to prompt  $J/\psi$  background.  $\sigma_t = 45\text{fs}$  for  $B_s^0 \rightarrow J/\psi K^+ K^-$ .

Peak at  $t=0$  composed of real  $J/\psi$  from IP + 2 random tracks, passing all of the selection cuts.





## Flavour Tagging at Production (t=0)

To fit for  $\phi_s$  we need to determine the flavour of  $B_s^0$  meson at production.  
i.e. Identify whether the signal meson was  $B_s^0$  or  $\overline{B}_s^0$  at t=0.

Flavour tagging at LHCb is discussed in more detail in a talk in Tuesday's parallel session by Katharina Kreplin.

For  $B_s^0 \rightarrow J/\psi K^+ K^-$ , the effective tagging efficiency is:

$$\epsilon_{\text{tag}} \mathcal{D}^2 = (3.13 \pm 0.12 \pm 0.20) \% \quad \text{Where: } \mathcal{D} = (1 - 2\omega_{\text{mistag}})$$

This gives us the same tagging power as a dataset containing  $\epsilon_{\text{tag}} \mathcal{D}^2 \times N$  perfectly tagged events.

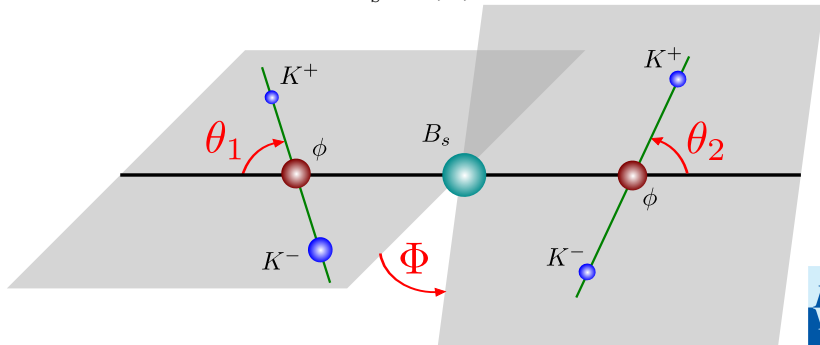


## Angular Definitions

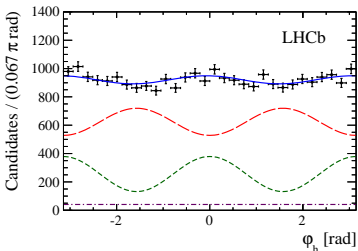
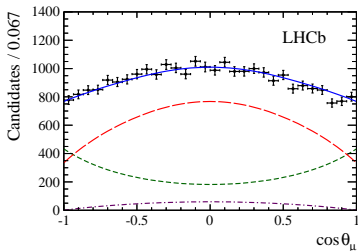
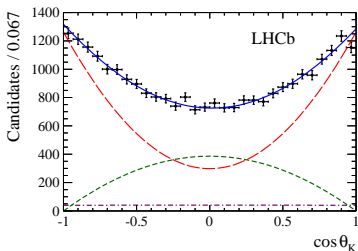
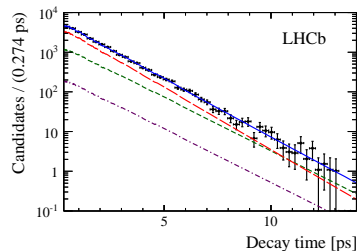
Both analyses have final states composed of  $\mathcal{CP}$ -Even and  $\mathcal{CP}$ -Odd components.

$\Rightarrow$  full angular analysis for both  $B_s^0 \rightarrow \phi \phi$  and  $B_s^0 \rightarrow J/\psi K^+ K^-$  using the Helicity basis.

$$B_s^0 \rightarrow \phi \phi$$



# Projections



Black: Data

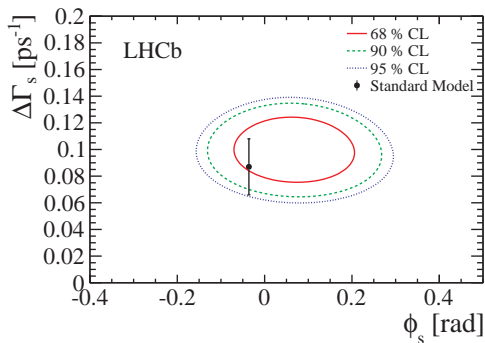
Red:  $CP$ -Even

Green:  $CP$ -Odd

Purple: S-wave

Blue: Total



$B_s^0 \rightarrow J/\psi K^+K^-$  Results

Using the  $S$ -Wave contribution to data the 2-fold ambiguity in  $(\phi_s, \Delta\Gamma_s)$  has been resolved.

$$\Delta\Gamma_s > 0$$

$$\begin{aligned} \phi_s &= 0.07 \pm 0.09 \text{ (stat)} \pm 0.01 \text{ (syst)} \text{ rad,} \\ \Gamma_s \equiv (\Gamma_L + \Gamma_H)/2 &= 0.663 \pm 0.005 \text{ (stat)} \pm 0.006 \text{ (syst)} \text{ ps}^{-1}, \\ \Delta\Gamma_s \equiv \Gamma_L - \Gamma_H &= 0.100 \pm 0.016 \text{ (stat)} \pm 0.003 \text{ (syst)} \text{ ps}^{-1}, \end{aligned}$$

$6\sigma$  significance for  $\Delta\Gamma \neq 0!$



$B_s^0 \rightarrow J/\psi \pi^+ \pi^-$  Data

Original  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$  analysis previously published

[arXiv:1204.5675](https://arxiv.org/abs/1204.5675).

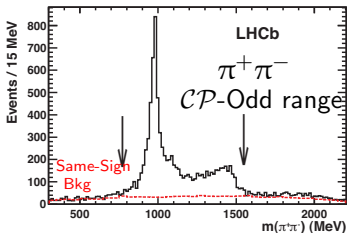
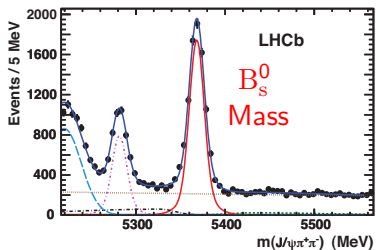
Analysis has been updated and latest tagging information is used.

Decay mode determined to be

$> 97.7\%$   $CP$ -Odd.

( $\Rightarrow$  no need for angular analysis)

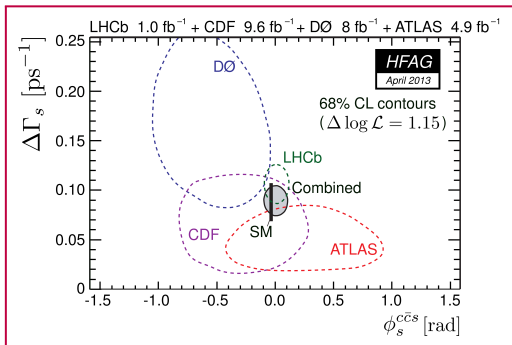
$\approx 7,400$  signal events



# $B_s^0 \rightarrow J/\psi K^+K^- + B_s^0 \rightarrow J/\psi \pi^+\pi^-$ Combined Results

Combined result gives the most precise measurements of:

$$\begin{aligned}\phi_s &= 0.01 \pm 0.07 \text{ (stat)} \pm 0.01 \text{ (syst) rad,} \\ \Gamma_s &= 0.661 \pm 0.004 \text{ (stat)} \pm 0.006 \text{ (syst) ps}^{-1}, \\ \Delta\Gamma_s &= 0.106 \pm 0.011 \text{ (stat)} \pm 0.007 \text{ (syst) ps}^{-1}.\end{aligned}$$



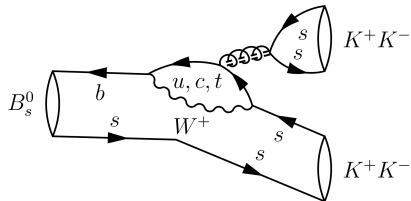
Latest HFAG Result as presented in [Beauty 2013](#)

(Without latest tagged results from ATLAS)



# $B_s^0 \rightarrow \phi \phi$ Phenomenology

Decay proceeds via  $b \rightarrow s\bar{s}$  transition.  
Dominated by penguin diagram:



In Standard Model:  $\phi_s = 0.0 \pm 0.2 \text{ rad}$ .

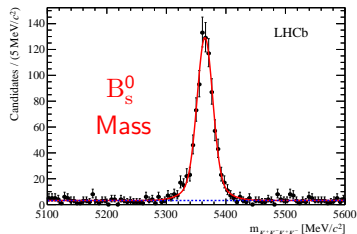
[arXiv 0810.0249](https://arxiv.org/abs/0810.0249)

[arXiv 0910.5237](https://arxiv.org/abs/0910.5237)

[arXiv hep-ph/0612290](https://arxiv.org/abs/hep-ph/0612290)

Clean Signal in purely hadronic channel:

$N \approx 900$  Signal events

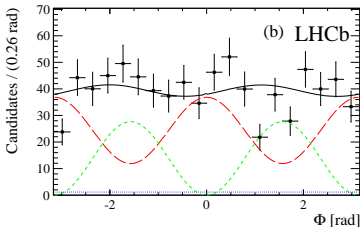
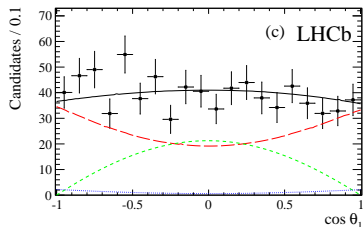
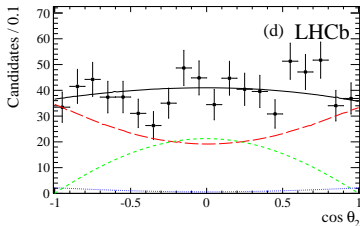
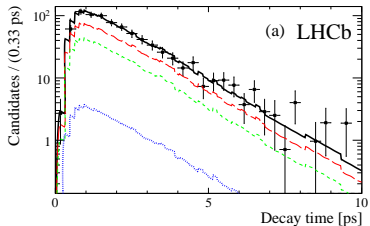


Time resolution in this analysis is  $\sigma_t = 40 \text{ fs}$ .

Effective tagging power of  $\epsilon_{\text{tag}} \mathcal{D}^2 = (3.29 \pm 0.48) \%$ .



# Projections

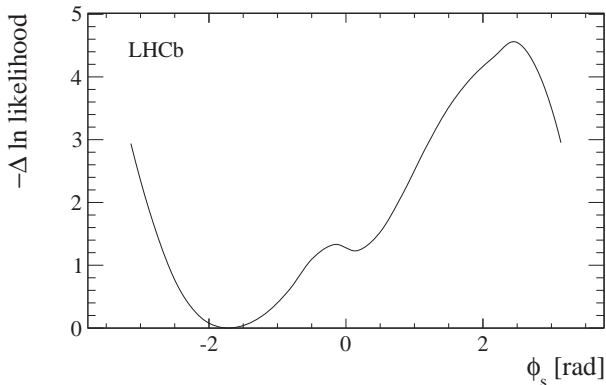


Points: Data  
Black: Total

Red:  $\mathcal{CP}$ -Even  
Green:  $\mathcal{CP}$ -Odd  
Blue: S-wave





Fit Results for  $\phi_s$ 

From Plot:

$$\phi_s = [-2.31, -0.92] \pm 0.22 \text{ (syst)} \text{ rad}$$

From FC:

p-value of Standard Model hypothesis is 16%

Small Dataset  $\Rightarrow$  Feldman-Cousins analysis provides coverage corrected 68% confidence limits (inc. systematics) of:

$$\phi_s = [-2.46, -0.76] \text{ rad}$$



## Summary

- Most precise measurement of  $\phi_s$  in  $B_s^0 \rightarrow J/\psi K^+ K^-$  and  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$  analysis.

$$\begin{aligned}\phi_s &= 0.01 \pm 0.07 \text{ (stat)} \pm 0.01 \text{ (syst) rad,} \\ \Gamma_s &= 0.661 \pm 0.004 \text{ (stat)} \pm 0.006 \text{ (syst) ps}^{-1}, \\ \Delta\Gamma_s &= 0.106 \pm 0.011 \text{ (stat)} \pm 0.007 \text{ (syst) ps}^{-1}.\end{aligned}$$

- **First** measurement of  $\phi_s$  in  $B_s^0 \rightarrow \phi \phi$ .

$$\phi_s = [-2.46, -0.76] \text{ rad}$$

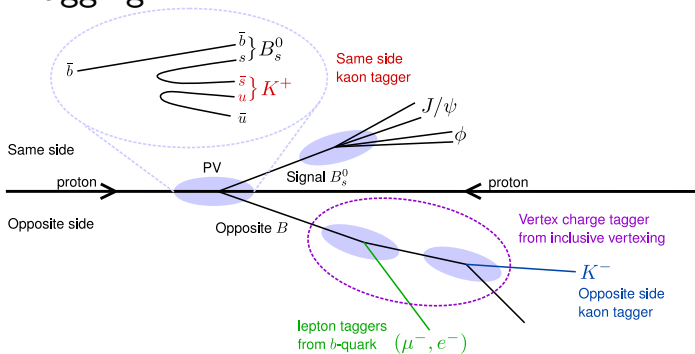
- **200% more data** recorded in 2012 yet to analyse!



# Backups



# Flavour Tagging



For  $B_s^0 \rightarrow J/\psi K^+ K^-$  the Effective tagging Efficiency is:

$$\langle \mathcal{D}^2 \rangle = (3.13 \pm 0.12 \pm 0.20) \%$$

Where:  $\mathcal{D} = (1 - 2\omega_{\text{mistag}})$

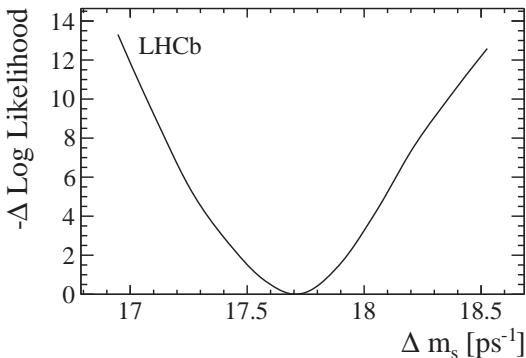
For  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$  the Effective tagging Efficiency is:

$$\langle \mathcal{D}^2 \rangle = (3.37 \pm 0.12 \pm 0.27) \%$$

Both analyses use Opposite and Same Side Taggers



## $\Delta LL$ function for $\Delta m_s$



Fitting for  $\Delta m_s$  in  $B_s^0 \rightarrow J/\psi \phi$  gives a value for which is compatible with external measurements.

Evidence that flavour tagging is working and that we understand our time resolution model.



# Full $B_s^0 \rightarrow J/\psi K^+ K^-$ PDF

$$\frac{d^4\Gamma(B_s^0 \rightarrow J/\psi K^+ K^-)}{dt d\Omega} \propto \sum_{k=1}^{10} f_k(\Omega) h_k(t)$$

$$h_k(t) = N_k e^{\Gamma_S t} \left[ a_k \cosh\left(\frac{\Delta\Gamma_S t}{2}\right) + b_k \sinh\left(\frac{\Delta\Gamma_S t}{2}\right) + c_k \cos(\Delta m_S t) + d_k \sin(\Delta m_S t) \right]$$

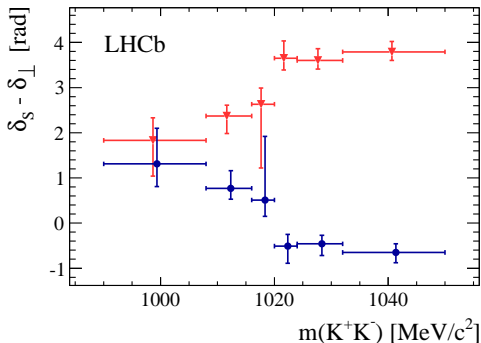
$k$	$f(\theta_\mu, \theta_K, \phi_h)$	$N_k$	$a_k$	$b_k$	$c_k$	$d_k$
1	$2 \cos^2 \theta_K \sin^2 \theta_\mu$	$ A_0(0) ^2$	1	D	C	-S
2	$\sin^2 \theta_K (1 - \sin^2 \theta_\mu \cos^2 \phi_h)$	$ A_{\parallel}(0) ^2$	1	D	C	-S
3	$\sin^2 \theta_K (1 - \sin^2 \theta_\mu \sin^2 \phi_h)$	$ A_{\perp}(0) ^2$	1	-D	C	S
4	$\sin^2 \theta_K \sin^2 \theta_\mu \sin 2\phi_h$	$ A_{\parallel}(0) A_{\perp}(0) $	$C \sin(\delta_{\perp} - \delta_{\parallel})$	$S \cos(\delta_{\perp} - \delta_{\parallel})$	$\sin(\delta_{\perp} - \delta_{\parallel})$	$D \cos(\delta_{\perp} - \delta_{\parallel})$
5	$\frac{1}{2} \sqrt{2} \sin 2\theta_K \sin 2\theta_\mu \cos \phi_h$	$A_0(0) A_{\parallel}(0)$	$\cos(\delta_{\parallel} - \delta_0)$	$D \cos(\delta_{\parallel} - \delta_0)$	$C \sin(\delta_{\parallel} - \delta_0)$	$-S \cos(\delta_{\parallel} - \delta_0)$
6	$-\frac{1}{2} \sqrt{2} \sin 2\theta_K \sin 2\theta_\mu \cos \phi_h$	$A_0(0) A_{\perp}(0)$	$C \sin(\delta_{\perp} - \delta_0)$	$S \cos(\delta_{\perp} - \delta_0)$	$\sin(\delta_{\perp} - \delta_0)$	$D \cos(\delta_{\perp} - \delta_0)$
7	$\frac{2}{3} \sin^2 \theta_\mu$	$ A_S(0) ^2$	1	-D	C	S
8	$\frac{1}{3} \sqrt{6} \sin \theta_K \sin 2\theta_\mu \cos \phi_h$	$ A_S(0) A_{\parallel}(0) $	$C \cos(\delta_{\parallel} - \delta_S)$	$S \sin(\delta_{\parallel} - \delta_S)$	$\cos(\delta_{\parallel} - \delta_S)$	$D \sin(\delta_{\parallel} - \delta_S)$
9	$-\frac{1}{3} \sqrt{6} \sin \theta_K \sin 2\theta_\mu \sin \phi_h$	$ A_S(0) A_{\perp}(0) $	$\sin(\delta_{\perp} - \delta_S)$	$-D \sin(\delta_{\perp} - \delta_S)$	$C \sin(\delta_{\perp} - \delta_S)$	$S \sin(\delta_{\perp} - \delta_S)$
10	$\frac{4}{3} \sqrt{3} \cos \theta_L \sin^2 \theta_\mu$	$ A_S(0) A_0(0) $	$C \cos(\delta_0 - \delta_S)$	$S \sin(\delta_0 - \delta_S)$	$\cos(\delta_0 - \delta_S)$	$D \sin(\delta_0 - \delta_S)$

$$S = -\frac{2|\lambda|}{1+|\lambda|^2} \sin(\phi_S), \quad D = -\frac{2|\lambda|}{1+|\lambda|^2} \cos(\phi_S), \quad C = \frac{1-|\lambda|^2}{1+|\lambda|^2}$$



# $B_s^0 \rightarrow J/\psi K^+K^-$ Ambiguity Resolution

In order to resolve the 2-fold ambiguity resolution present in the  $\phi_s/\Delta\Gamma_s$  plane the phase difference between the S and P-wave is used.



Blue:  $\Delta\Gamma_s > 0$ .

Red:  $\Delta\Gamma_s < 0$ .

Physical Solution (Blue) corresponds to -ve trend in  $\delta_S - \delta_\perp$  across  $K^+K^-$  mass range  $\Rightarrow \Delta\Gamma_s$  is +ve.



# $B_s^0 \rightarrow J/\psi K^+ K^-$ Systematic Uncertainties

Source	$\Gamma_s$ [ps <sup>-1</sup> ]	$\Delta\Gamma_s$ [ps <sup>-1</sup> ]	$ A_{\perp} ^2$	$ A_0 ^2$	$\delta_{\parallel}$ [rad]	$\delta_{\perp}$ [rad]	$\phi_s$ [rad]	$ \lambda $
Stat. uncertainty	0.0048	0.016	0.0086	0.0061	$^{+0.13}_{-0.21}$	0.22	0.091	0.031
Background subtraction	0.0041	0.002	–	0.0031	0.03	0.02	0.003	0.003
$B^0 \rightarrow J/\psi K^{*0}$ background	–	0.001	0.0030	0.0001	0.01	0.02	0.004	0.005
Ang. acc. reweighting	0.0007	–	0.0052	0.0091	0.07	0.05	0.003	0.020
Ang. acc. statistical	0.0002	–	0.0020	0.0010	0.03	0.04	0.007	0.006
Lower decay time acc. model	0.0023	0.002	–	–	–	–	–	–
Upper decay time acc. model	0.0040	–	–	–	–	–	–	–
Length and mom. scales	0.0002	–	–	–	–	–	–	–
Fit bias	–	–	0.0010	–	–	–	–	–
Quadratic sum of syst.	0.0063	0.003	0.0064	0.0097	0.08	0.07	0.009	0.022
Total uncertainties	0.0079	0.016	0.0107	0.0114	$^{+0.15}_{-0.23}$	0.23	0.091	0.038





$B_s^0 \rightarrow J/\psi h^+ h^-$  Results

Parameter	Value
$\Gamma_s$ [ps <sup>-1</sup> ]	$0.661 \pm 0.004 \pm 0.006$
$\Delta\Gamma_s$ [ps <sup>-1</sup> ]	$0.106 \pm 0.011 \pm 0.007$
$ A_\perp ^2$	$0.246 \pm 0.007 \pm 0.006$
$ A_0 ^2$	$0.523 \pm 0.005 \pm 0.010$
$\delta_\parallel$ [rad]	$3.32^{+0.13}_{-0.21} \pm 0.08$
$\delta_\perp$ [rad]	$3.04 \pm 0.20 \pm 0.07$
$\phi_s$ [rad]	$0.01 \pm 0.07 \pm 0.01$
$ \lambda $	$0.93 \pm 0.03 \pm 0.02$



$B_s^0 \rightarrow J/\psi h^+ h^-$  Correlation

	$\Gamma_s$ [ps <sup>-1</sup> ]	$\Delta\Gamma_s$ [ps <sup>-1</sup> ]	$ A_\perp ^2$	$ A_0 ^2$	$\delta_\parallel$ [rad]	$\delta_\perp$ [rad]	$\phi_s$ [rad]	$ \lambda $
$\Gamma_s$ [ps <sup>-1</sup> ]	1.00	0.10	0.08	0.03	-0.08	-0.04	0.01	0.00
$\Delta\Gamma_s$ [ps <sup>-1</sup> ]		1.00	-0.49	0.47	0.00	0.00	0.00	-0.01
$ A_\perp ^2$			1.00	-0.40	-0.37	-0.14	0.02	-0.05
$ A_0 ^2$				1.00	-0.05	-0.03	-0.01	0.01
$\delta_\parallel$ [rad]					1.00	0.39	-0.01	0.13
$\delta_\perp$ [rad]						1.00	0.21	0.03
$\phi_s$ [rad]							1.00	0.06
$ \lambda $								1.00



$B_s^0 \rightarrow \phi \phi$  Full PDF

$i$	$K_i$	$f_i$
1	$ A_0(t) ^2$	$4 \cos^2 \theta_1 \cos^2 \theta_2$
2	$ A_{\parallel}(t) ^2$	$\sin^2 \theta_1 \sin^2 \theta_2 (1 + \cos 2\Phi)$
3	$ A_{\perp}(t) ^2$	$\sin^2 \theta_1 \sin^2 \theta_2 (1 - \cos 2\Phi)$
4	$Im(A_{\parallel}^*(t)A_{\perp}(t))$	$-2 \sin^2 \theta_1 \sin^2 \theta_2 \sin 2\Phi$
5	$Re(A_{\parallel}^*(t)A_0(t))$	$\sqrt{2} \sin 2\theta_1 \sin 2\theta_2 \cos \Phi$
6	$Im(A_0^*(t)A_{\perp}(t))$	$-\sqrt{2} \sin 2\theta_1 \sin 2\theta_2 \sin \Phi$
7	$ A_{SS}(t) ^2$	$\frac{4}{9}$
8	$ A_S(t) ^2$	$\frac{4}{3}(\cos \theta_1 + \cos \theta_2)^2$
9	$Re(A_S^*(t)A_{SS}(t))$	$\frac{8}{3\sqrt{3}}(\cos \theta_1 + \cos \theta_2)$
10	$Re(A_0(t)A_{SS}^*(t))$	$\frac{8}{3} \cos \theta_1 \cos \theta_2$
11	$Re(A_{\parallel}(t)A_{SS}^*(t))$	$\frac{4\sqrt{2}}{3} \sin \theta_1 \sin \theta_2 \cos \Phi$
12	$Im(A_{\perp}(t)A_{SS}^*(t))$	$-\frac{4\sqrt{2}}{3} \sin \theta_1 \sin \theta_2 \sin \Phi$
13	$Re(A_0(t)A_S^*(t))$	$\frac{8}{\sqrt{3}} \cos \theta_1 \cos \theta_2 (\cos \theta_1 + \cos \theta_2)$
14	$Re(A_{\parallel}(t)A_S^*(t))$	$\frac{4\sqrt{2}}{\sqrt{3}} \sin \theta_1 \sin \theta_2 (\cos \theta_1 + \cos \theta_2) \cos \Phi$
15	$Im(A_{\perp}(t)A_S^*(t))$	$-\frac{4\sqrt{2}}{\sqrt{3}} \sin \theta_1 \sin \theta_2 (\cos \theta_1 + \cos \theta_2) \sin \Phi$

Blue:

P-Wave

Yellow:

S-Wave  $\mathcal{CP}$ -Odd  
+ $\mathcal{CP}$ -Even

Red:

 $\phi\phi$ ,  $f_0 f_0$  interference

Green:

 $\phi\phi$ ,  $\phi f_0$  interference

$$\frac{d^4\Gamma(B_s^0 \rightarrow \phi\phi)}{dtd\Omega} \propto \sum_{i=1}^{15} K_i(\Omega) f_i(t)$$



$B_s^0 \rightarrow \phi \phi$  Results

Parameter	Value	$\sigma_{\text{stat.}}$	$\sigma_{\text{syst.}}$
$\phi_s$ [rad] (68 % CL)		$[-2.37, -0.92]$	0.22
$ A_0 ^2$	0.329	0.033	0.017
$ A_\perp ^2$	0.358	0.046	0.018
$ A_S ^2$	0.016	$^{+0.024}_{-0.012}$	0.009
$\delta_1$ [rad]	2.19	0.44	0.12
$\delta_2$ [rad]	-1.47	0.48	0.10
$\delta_S$ [rad]	0.65	$^{+0.89}_{-1.65}$	0.33

