# Inverse Seesaw in NMSSM and 126 GeV Higgs Boson

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- Both ATLAS and CMS have reported the discovery of a scalar particle consistent with the SM Higgs boson of mass  $m_h \approx 126~{\rm GeV}$
- In MSSM it requires a very large stop quark mass to accommodate  $m_h \sim 126 \text{ GeV}$  ("little hierarchy" problem).
- NMSSM can alleviate the "little hierarchy" problem due to a tree level contribution to the Higgs potential.
- However, the couplings  $(\lambda, \kappa, y_t)$  in NMSSM will be all of  $\mathcal{O}(1)$  at the GUT scale.

## NMSSM

The NMSSM is obtained by adding to the MSSM a gauge singlet chiral superfield S and including the following superpotential terms:

$$W \supset \lambda SH_uH_d + \frac{\kappa}{3}S^3$$

The upper limit on the lightest CP-even Higgs boson mass in the NMSSM is given by

$$\begin{bmatrix} m_h^2 \end{bmatrix}_{NMSSM} = M_Z^2 \left( \cos^2 2\beta + \frac{2\lambda^2}{g_1^2 + g_2^2} \sin^2 2\beta \right) \left( 1 - \frac{3}{8\pi^2} y_t^2 t \right) \\ + \frac{3}{4\pi^2} y_t^2 m_t^2 \sin^2 \beta \left[ \frac{1}{2} \widetilde{X}_t + t + \frac{1}{(4\pi)^2} \left( \frac{3}{2} y_t^2 - 32\pi\alpha_s \right) \left( \widetilde{X}_t + t \right) t \right]$$

where

$$t = \log\left(\frac{M_{S}^{2}}{M_{t}^{2}}\right), \ \widetilde{X}_{t} = \frac{2\widetilde{A}_{t}^{2}}{M_{S}^{2}}\left(1 - \frac{\widetilde{A}_{t}^{2}}{12M_{S}^{2}}\right), \ \widetilde{A}_{t} = A_{t} - \lambda \langle S \rangle \cot \beta$$

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# NMSSM

#### For comparison

$$\begin{split} [m_h^2]_{NMSSM} &= M_Z^2 \left( \cos^2 2\beta + \frac{2\lambda^2}{g_1^2 + g_2^2} \sin^2 2\beta \right) \left( 1 - \frac{3}{8\pi^2} y_t^2 t \right) \\ &+ \frac{3}{4\pi^2} y_t^2 m_t^2 \sin^2 \beta \left[ \frac{1}{2} \widetilde{X}_t + t + \frac{1}{(4\pi)^2} \left( \frac{3}{2} y_t^2 - 32\pi\alpha_s \right) \left( \widetilde{X}_t + t \right) t \right] \\ [m_h^2]_{MSSM} &= M_Z^2 \cos^2 2\beta \left( 1 - \frac{3}{8\pi^2} y_t^2 t \right) \\ &+ \frac{3}{4\pi^2} y_t^2 m_t^2 \left[ \frac{1}{2} \widetilde{X}_t + t + \frac{1}{(4\pi)^2} \left( \frac{3}{2} y_t^2 - 32\pi\alpha_s \right) \left( \widetilde{X}_t + t \right) t \right] \end{split}$$

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Figure: Upper bounds on the lightest CP-even Higgs boson mass versus tan  $\beta$ , for  $M_S = 1$  TeV (left panel) and  $M_S = 200$  GeV (right panel). Maximum value of  $\lambda$  is used. Red lines correspond to the NMSSM, and blue lines correspond to the MSSM. The solid lines show the Higgs mass bounds for  $\tilde{X}_t = 6$ , while the dashed lines show the bounds with  $\tilde{X}_t = 0$ . The gray band shows the Higgs mass range of  $126 \pm 3$  GeV.

One can incorporate the observed solar and atmospheric neutrino oscillations in the NMSSM by introducing an effective dimension six operator:

 $\frac{LLH_uH_uS}{M_6^2}$ 



		Q	Uc	D <sup>c</sup>	L	Ec	H <sub>u</sub>	H <sub>d</sub>	S
case I	<i>Z</i> <sub>3</sub>	1	$\omega^2$	$\omega^2$	1	$\omega^2$	ω	ω	ω
case II	<i>Z</i> <sub>3</sub>	1	ω	1	$\omega^2$	ω	$\omega^2$	1	ω
case III	<i>Z</i> <sub>3</sub>	1	1	ω	ω	1	1	$\omega^2$	ω

Table:  $Z_3$  charge assignments of the NMSSM superfields corresponding to dimension six operators for neutrino masses. Here  $\omega = e^{i2\pi/3}$ .

The simplest way to generate this operator is to introduce the gauge singlet chiral superfields  $(N_n^c + N_n)$  in the NMSSM.

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	<i>Z</i> <sub>3</sub>	<i>Z</i> <sub>2</sub>
N <sup>c</sup> <sub>n</sub>	1	1	0	$\omega^2$	_
N <sub>n</sub>	1	1	0	ω	_

Table: Charge assignments of  $N_n^c + N_n$  superfields. Here  $\omega = e^{i2\pi/3}$ .

The additional contribution to the lightest CP-even Higgs mass is given by

$$[m_{h}^{2}]_{N} = n \times \left[ -M_{Z}^{2} \cos^{2} 2\beta \left( \frac{1}{8\pi^{2}} Y_{N}^{2} t_{N} \right) + \frac{1}{4\pi^{2}} Y_{N}^{4} v^{2} \sin^{2} \beta \left( \frac{1}{2} \widetilde{X}_{Y_{N}} + t_{N} \right) \right]$$

where

$$t_{N} = \log\left(\frac{M_{5}^{2} + M_{6}^{2}}{M_{6}^{2}}\right), \ \widetilde{X}_{Y_{N}} = \frac{4\widetilde{A}_{Y_{N}}^{2}\left(3M_{5}^{2} + 2M_{6}^{2}\right) - \widetilde{A}_{Y_{N}}^{4} - 8M_{5}^{2}M_{6}^{2} - 10M_{5}^{4}}{6\left(M_{5}^{2} + M_{6}^{2}\right)^{2}},$$

and

$$\widetilde{A}_{Y_N} = A_{Y_N} - Y_N \langle S \rangle \cot \beta$$

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8/14

## NMSSM+gauge singlet field



(a) Upper bounds on the lightest CP-even Higgs boson (b) Upper bounds on the lightest CP-even Higgs bomass versus tan  $\beta$ , with  $M_S = 300$  GeV,  $M_6 = 3$  TeV, son mass versus tan  $\beta$ , with  $M_S = 300$  GeV,  $M_6 = 3$   $\tilde{X}_{Y_N} = 4$ . Maximum value of  $\lambda$  is used. Red lines TeV,  $\tilde{X}_t = 6$ ,  $\tilde{X}_{Y_N} = 4$ ,  $Y_N = 0.7$  and  $\lambda = 0.1$ . correspond to NMSSM, while blue lines correspond to Red dashed line corresponds to NMSSM. Blue, purple NMSSM with one additional pair of  $(N_n^c + N_n)$  singlets. and black solid lines (from bottom to top) correspond to Purple lines correspond to NMSSM with 3 additional pairs NMSSM+singlets with n=1, 2 and 3.

of  $(N_n^c + N_n)$  singlets. In both cases  $Y_N = 0.7$ . The solid lines show the Higgs mass bounds with  $\widetilde{X}_t = 6$ , while the dashed lines show the bounds with  $\widetilde{X}_t = 0$ .

Another way for generating the dimension six operator is to introduce  $SU(2)_L$  triplets  $(\Delta_n^c + \Delta_n)$  with unit hypercharge.

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	<i>Z</i> <sub>3</sub>	<i>Z</i> <sub>2</sub>
$\Delta_1$	1	3	1	1	+
$\overline{\Delta}_1$	1	3	-1	1	+
$\Delta_2$	1	3	-1	ω	+
$\overline{\Delta}_2$	1	3	1	$\omega^2$	+

Table: Charge assignments of  $(\Delta_n + \overline{\Delta}_n)$  superfields, where n = 1, 2.  $\omega = e^{i2\pi/3}$  and  $Z_2$  is matter parity. The additional contributions to the NMSSM superpotential in this case contain the following terms

$$W \supset \qquad Y_{ij}(L_i \Delta_1 L_j) + Y_{H_u}(H_u \Delta_2 H_u) + \lambda_N S \operatorname{tr} \left[ \overline{\Delta}_1 \overline{\Delta}_2 \right] \\ + m_1 \operatorname{tr} \left[ \overline{\Delta}_1 \Delta_1 \right] + m_2 \operatorname{tr} \left[ \overline{\Delta}_2 \Delta_2 \right]$$

The coupling  $Y_H(H_u\Delta H_u)$  will generate a tree level contribution to the lightest CP-even Higgs boson mass given by

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11/14

$$\left[m_{h}^{2}\right]_{\Delta} = 4Y_{H_{u}}^{2}v^{2}\sin^{4}\beta$$

### NMSSM+triplets



(C) Upper bounds on the lightest CP-even Higgs boson (d) Upper bounds on the lightest CP-even Higgs boson rass versus tan  $\beta$ , for  $M_S = 200$  GeV,  $\tilde{X}_t = 6$ ,  $Y_{H_u} =$  son mass versus tan  $\beta$ , with  $M_S = 200$  GeV,  $\tilde{X}_t = 6$ , 0.15,  $m_1 = m_2 = 3$  TeV. Maximum value of  $\lambda$  is used.  $m_1 = m_2 = 3$  TeV, and  $\lambda = 0.3$ . Red dashed line cor-Red dashed line corresponds to NMSSM, and the blue responds to the NMSSM, and blue and purple solid lines solid line corresponds to NMSSM +  $(\Delta_n + \overline{\Delta}_n)$ . correspond to NMSSM +  $(\Delta_n + \overline{\Delta}_n)$ , with  $Y_{H_u} = 0.15$ 

and 0.2.

- We have considered extensions of the next-to-minimal supersymmetric model (NMSSM) in which the observed neutrino masses are generated through a TeV scale inverse seesaw mechanism.
- Introducing the gauge singlet superfields can yield a large contribution to the mass of the lightest CP-even Higgs.
- This new contribution makes it possible to have a 126 GeV Higgs with order of 300 GeV stop quarks mass and a broad range of tan  $\beta$  values.

The renormalizable superpotential terms involving only the new chiral superfields are given by

$$W \supset y_{ni}^{N} N_{n}^{c}(H_{u}L_{i}) + rac{\lambda_{N_{nm}}}{2} SN_{n}N_{m} + m_{nm}N_{n}^{c}N_{m}$$

Following the electroweak symmetry breaking, the neutrino Majorana mass matrix is generated:

$$m_{\nu} = rac{(Y_N^T Y_N) {v_u}^2}{M_6} imes rac{\lambda_N \langle S \rangle}{M_6}.$$

This implies that even if  $Y_N \sim O(1)$  and  $M_S \sim 1$  TeV, the correct mass scale for the light neutrinos can be reproduced by suitably adjusting  $\lambda_N$ .