

The Impact of B Physics Observables on SUSY Fits

Sven Heinemeyer, IFCA (Santander)

CERN, 12/2007

based on hep-ph/0706.0652, hep-ph/0707.3447, hep-ph/0709.0098
[Buchmüller, Cavanaugh, De Roeck, Ellis, Hahn, S.H., Isidori, Olive, Paradisi, Ronga, Weber, Weiglein]

1. Introduction
2. Impact of BPO on CMSSM fits
3. Impact of BPO on M_h fit in the CMSSM
4. Impact and prospects of BPO on NUHM fits
5. Conclusions

1. Introduction

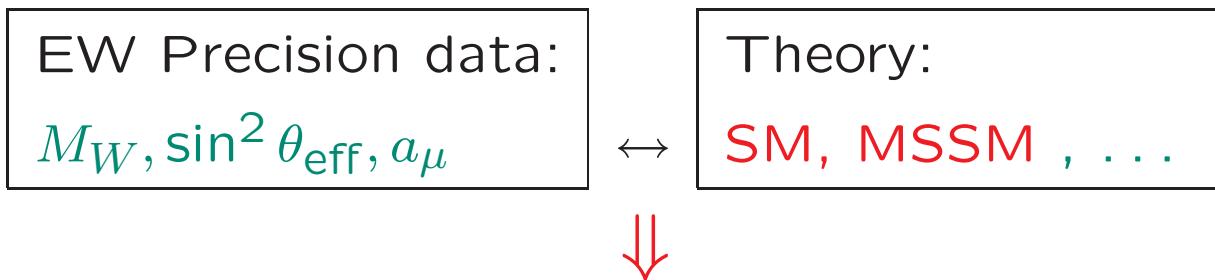
Let's assume that low-energy SUSY is realized in Nature
(But you can play the same game with any NP model!)

What do we know about the SUSY mass scale?

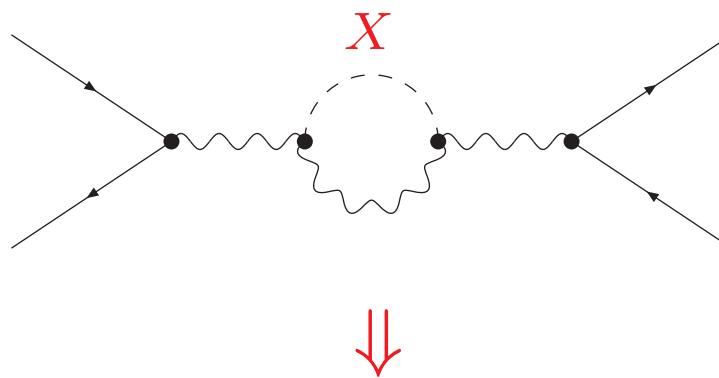
1. Coupling constant unification $\Rightarrow M_{\text{SUSY}} \approx 1 \text{ TeV}$
 2. Solution for the Hierarchy problem $\Rightarrow M_{\text{SUSY}} \lesssim 1 \text{ TeV}$
 3. Indirect hints from existing data?
 - Electroweak precision observables (**EWPO**) ?
 - B physics observables (**BPO**) ?
 - Cold dark matter (**CDM**) ?
- \Rightarrow combination of EWPO, BPO, CDM ?

Precision Observables (POs):

Comparison of electro-weak precision observables with theory:



Test of theory at quantum level: Sensitivity to loop corrections

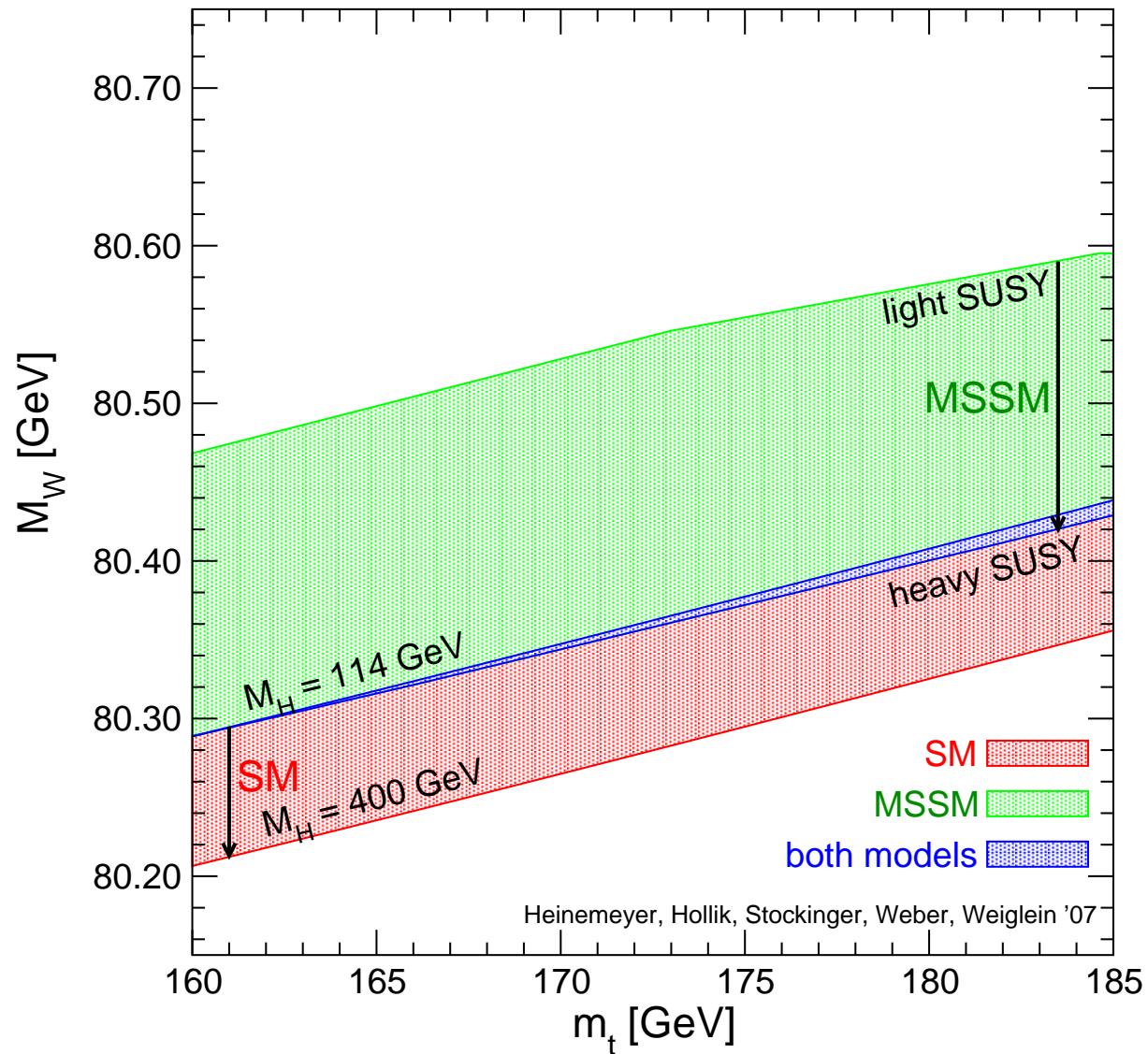


Very high accuracy of measurements and theoretical predictions needed

- Which model fits better?
- Does the prediction of a model contradict the experimental data?

Example: Prediction for M_W in the SM and the MSSM :

[S.H., W. Hollik, D. Stockinger, A.M. Weber, G. Weiglein '07]



MSSM band:

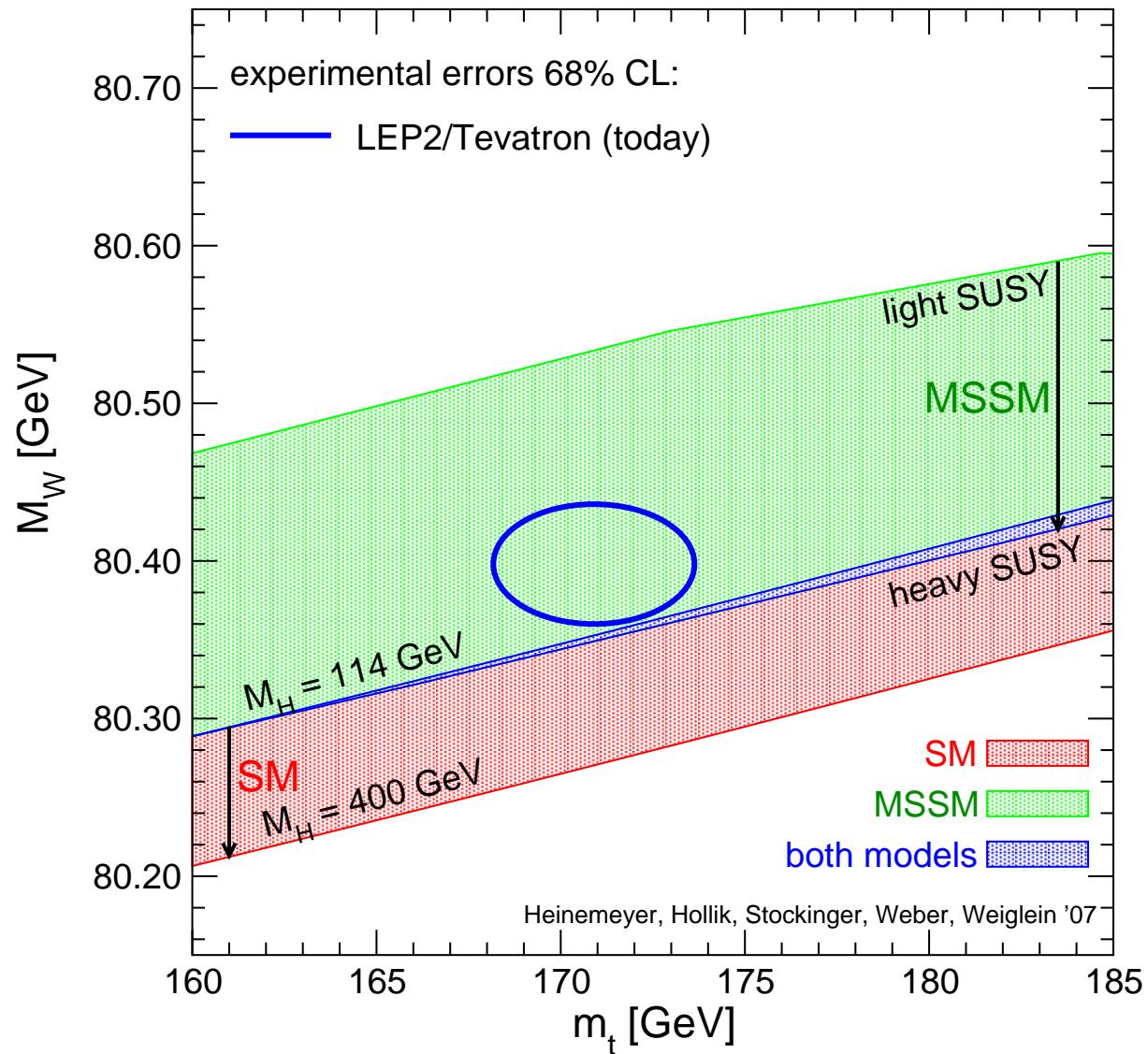
scan over
SUSY masses

overlap:
SM is MSSM-like
MSSM is SM-like

SM band:
variation of M_H^{SM}

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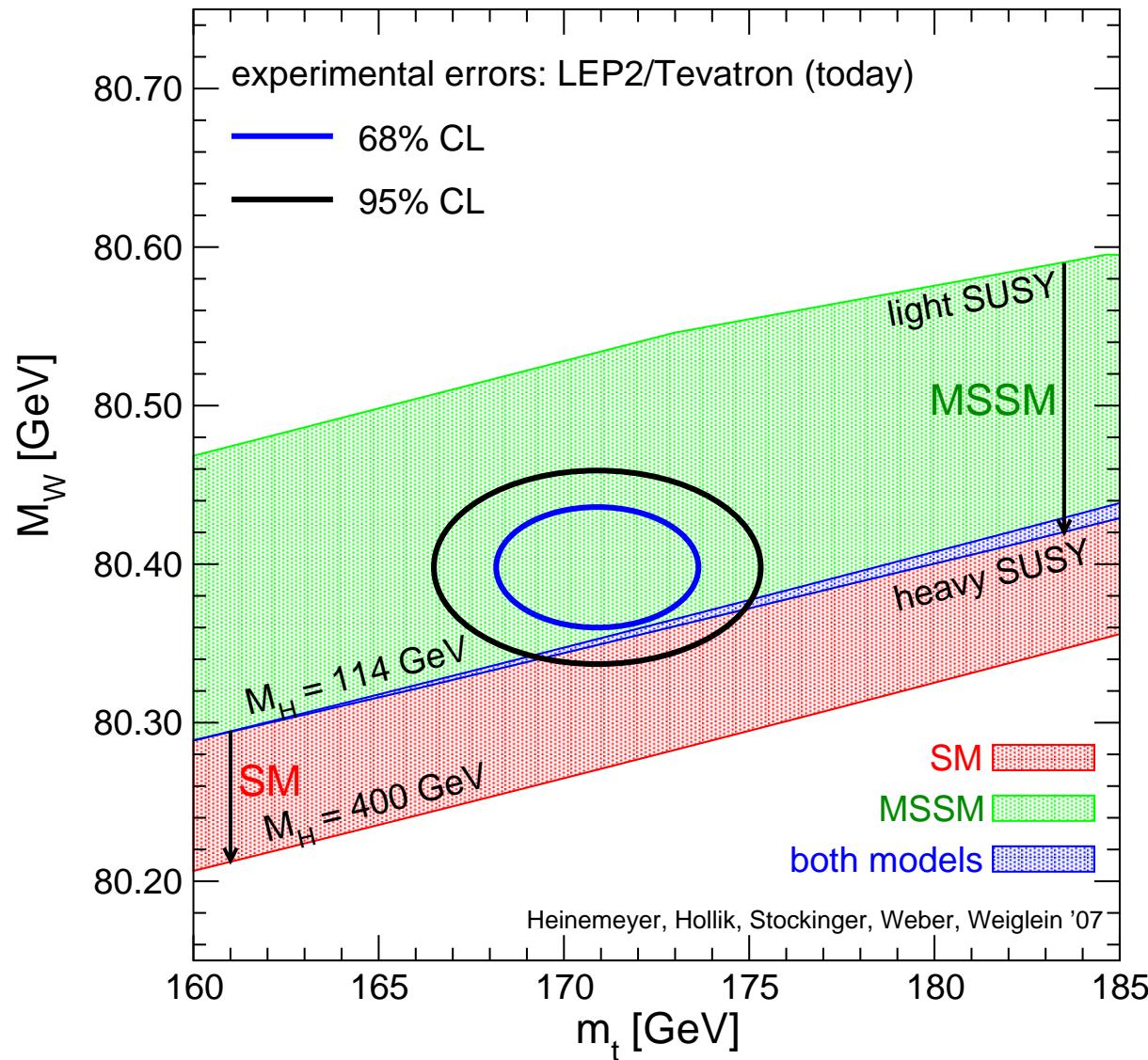
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Within the SM: fit for the last unknown parameter: M_H^{SM}

Global fit to all SM data:

[LEPEWWG '07]

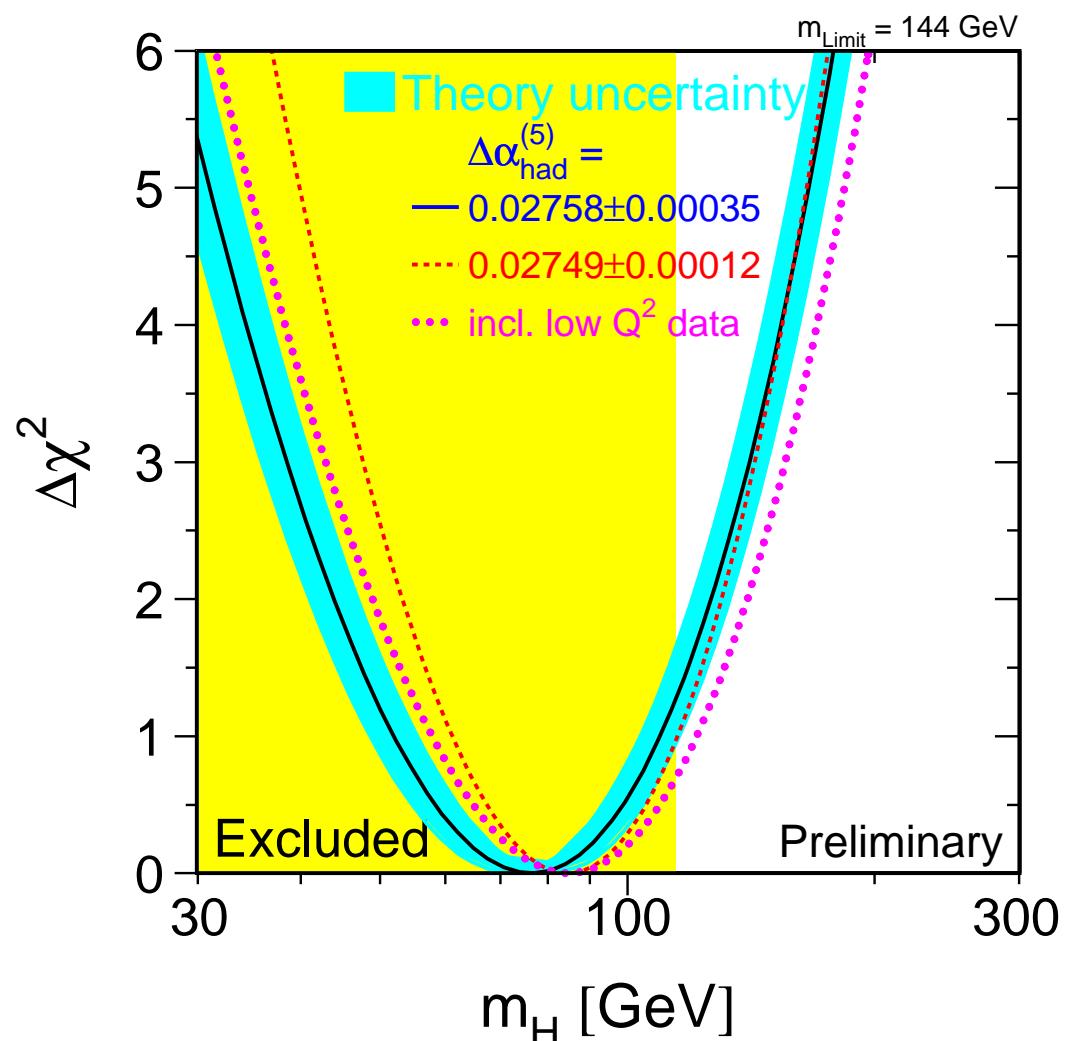
$$\Rightarrow M_H = 76^{+33}_{-24} \text{ GeV}$$

$M_H < 144 \text{ GeV}, 95\% \text{ C.L.}$

Assumption for the fit:

SM incl. Higgs boson

\Rightarrow no confirmation of
Higgs mechanism



\Rightarrow Higgs boson seems to be light, $M_H \lesssim 150 \text{ GeV}$

Indirect hints on M_{SUSY} from existing data?

- Electroweak precision observables (**EWPO**) ?
- B physics observables (**BPO**) ?
- Cold dark matter (**CDM**) ?

⇒ combination of EWPO, BPO, CDM ?

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⇒ combination of **EWPO, BPO, CDM** ?

EWPO M_W : information on $m_{\tilde{t}}$, $m_{\tilde{b}}$ or M_A , $\tan \beta$ or ...

EWPO $(g - 2)_\mu$: information on $\tan \beta$ and/or $m_{\tilde{\chi}^0}$, $m_{\tilde{\chi}^\pm}$ and/or $m_{\tilde{\mu}}$, $m_{\tilde{\nu}_\mu}$

BPO $\text{BR}(b \rightarrow s\gamma)$: information on $\tan \beta$ and/or M_{H^\pm} and/or $m_{\tilde{t}}$, $m_{\tilde{\chi}^\pm}$

CDM (**LSP gives CDM**) : information on $m_{\tilde{\chi}_1^0}$ and $m_{\tilde{\tau}}$ or M_A or ...

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BPO $\text{BR}(b \rightarrow s\gamma)$: information on $\tan \beta$ and/or M_{H^\pm} and/or $m_{\tilde{t}}$, $m_{\tilde{\chi}^\pm}$

CDM (**LSP gives CDM**) : information on $m_{\tilde{\chi}_1^0}$ and $m_{\tilde{\tau}}$ or M_A or ...

⇒ combination makes only sense if all parameters are connected!

⇒ GUT based models, ...

The models: 1.) CMSSM (or mSUGRA):

⇒ Scenario characterized by

$$m_0, m_{1/2}, A_0, \tan\beta, \text{sign } \mu$$

m_0 : universal scalar mass parameter

$m_{1/2}$: universal gaugino mass parameter

A_0 : universal trilinear coupling

$\tan\beta$: ratio of Higgs vacuum expectation values

$\text{sign}(\mu)$: sign of supersymmetric Higgs parameter

} at the GUT scale

⇒ particle spectra from renormalization group running to weak scale

Lightest SUSY particle (LSP) is the lightest neutralino

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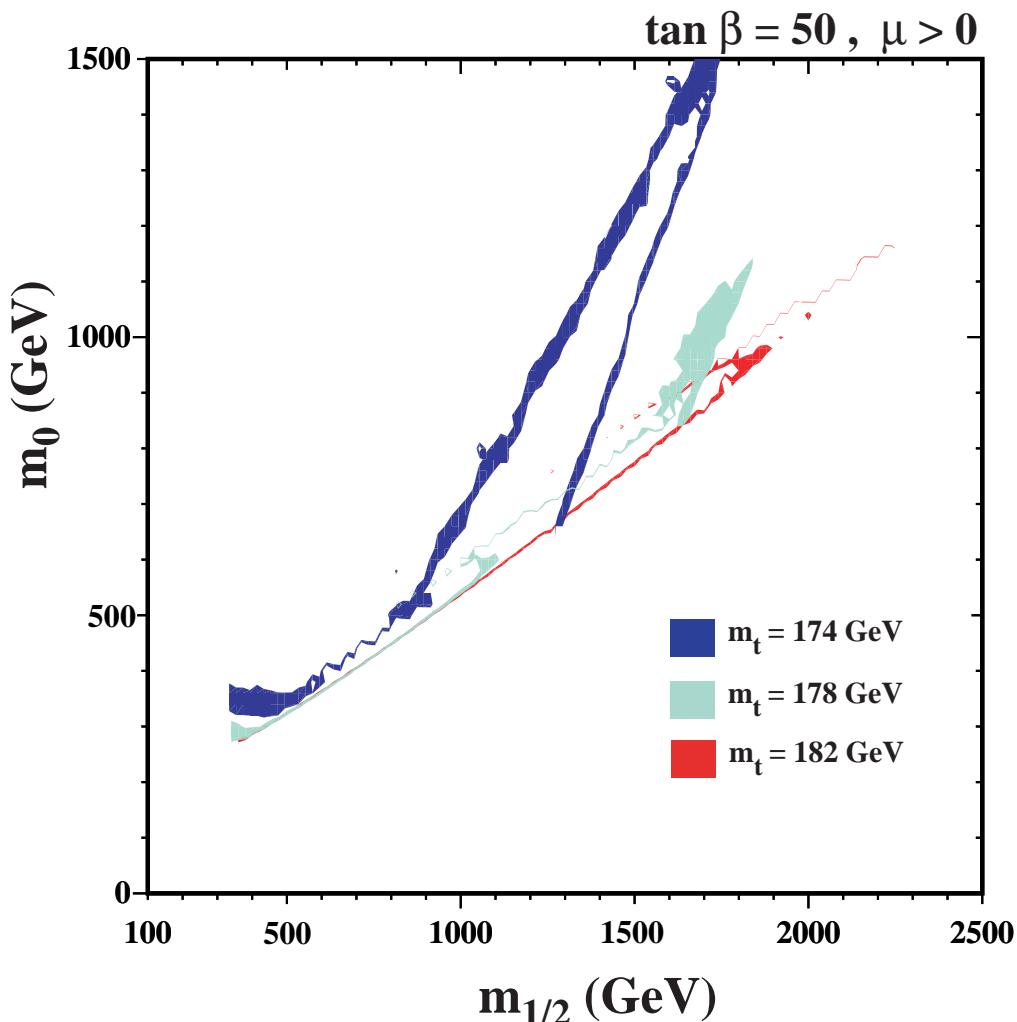
A_0 : universal trilinear

$\tan \beta$: ratio of Higgs

$\text{sign}(\mu)$: sign of superpartner mass

⇒ particle spectra from

Lightest SUSY particle



The models: 2.) NUHM: (Non-universal Higgs mass model)

⇒ besides the CMSSM parameters

M_A and μ

Assumption:

no unification of scalar fermion and scalar Higgs parameters
at the GUT scale

⇒ effectively M_A and μ free parameters at the EW scale

⇒ particle spectra from renormalization group running to weak scale

Lightest SUSY particle (LSP) is the lightest neutralino

⇒ possible: M_A – $\tan \beta$ planes in agreement with CDM :-)

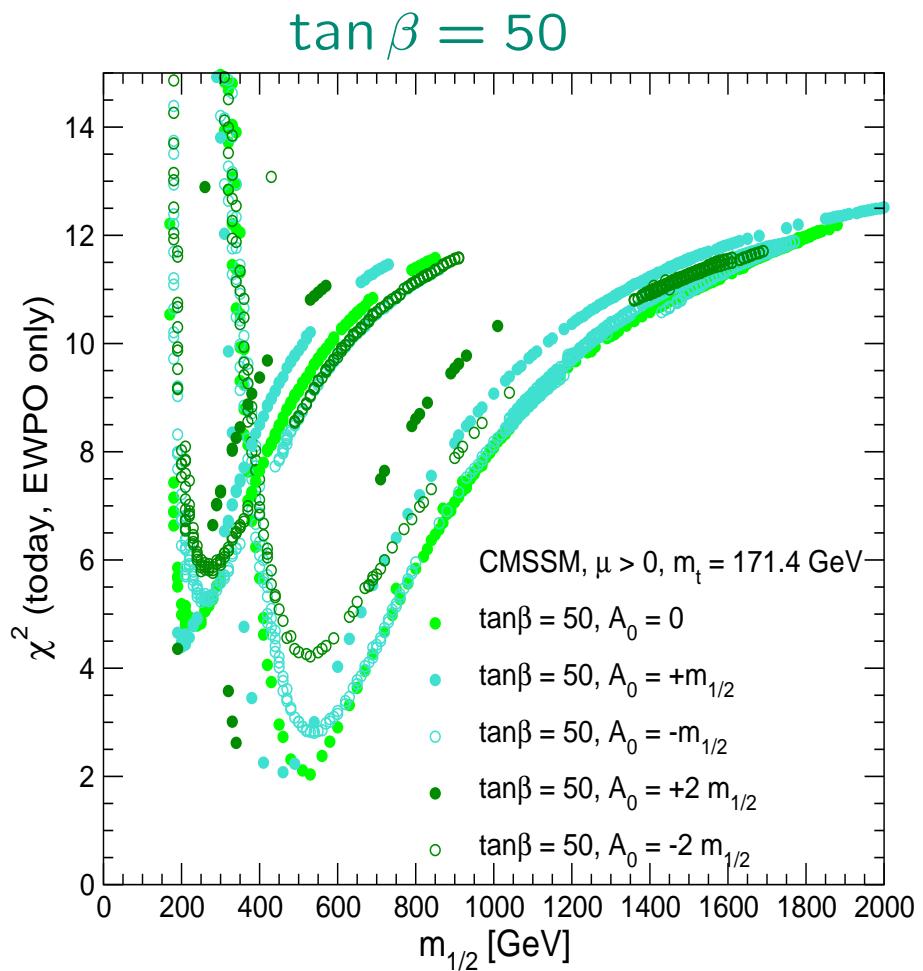
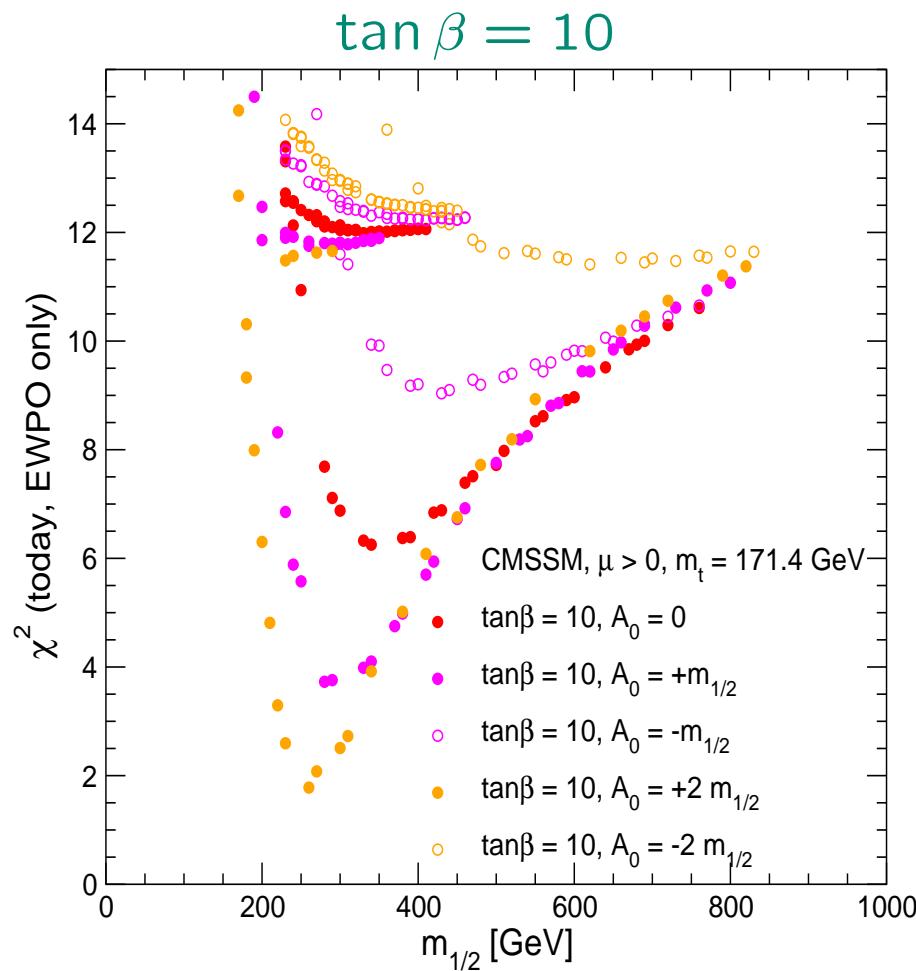
2. Impact of BPO on CMSSM fits

[J. Ellis, S.H., K. Olive, A.M. Weber, G. Weiglein '07]

What do we know about the SUSY mass scale?

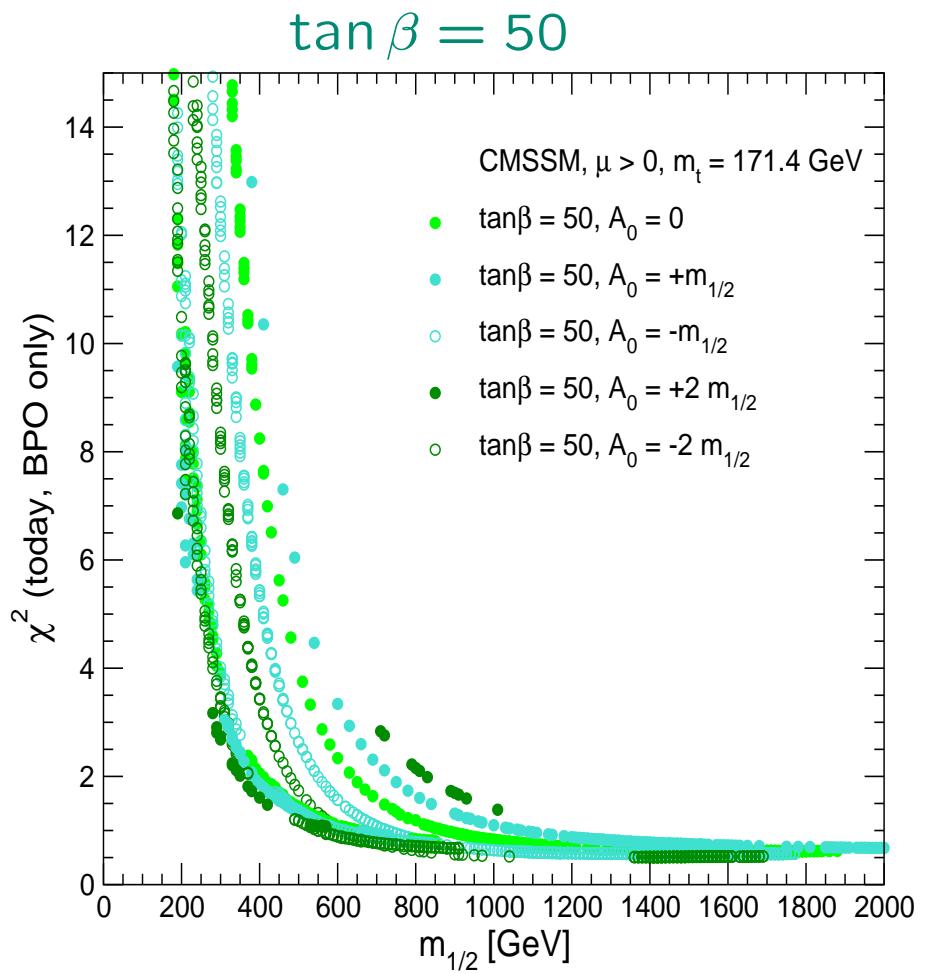
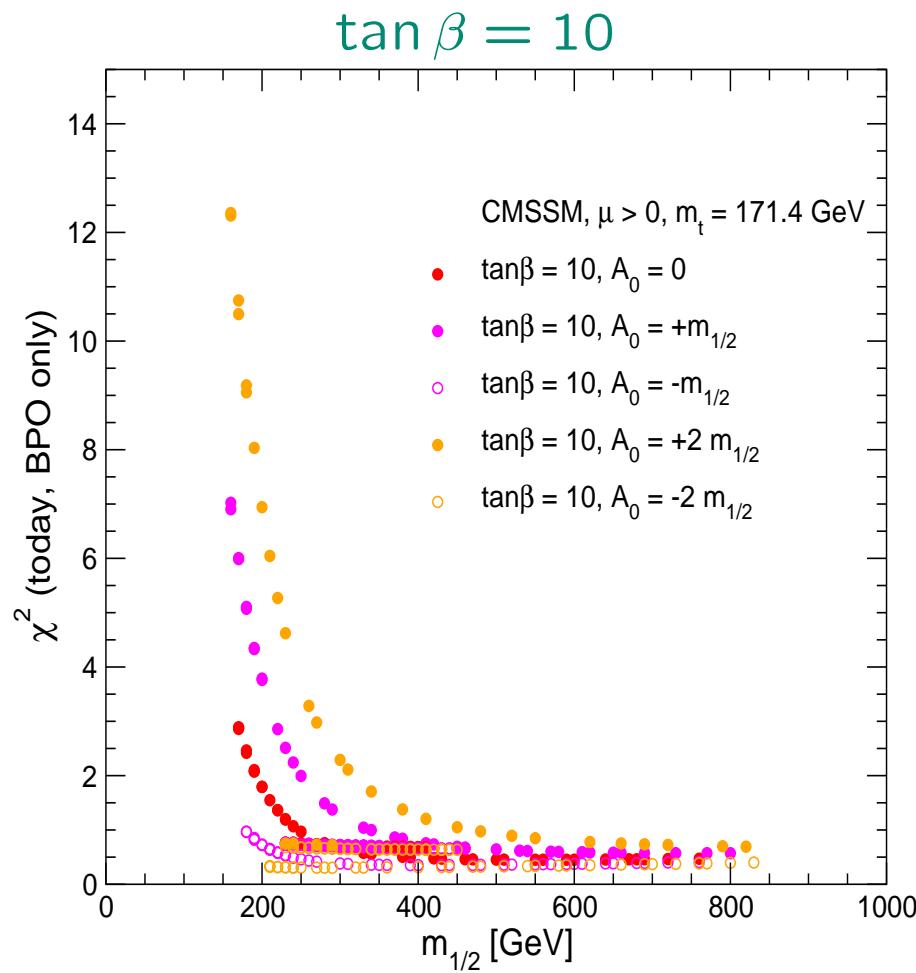
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2. Solution for the Hierarchy problem $\Rightarrow M_{\text{SUSY}} \lesssim 1 \text{ TeV}$
3. Indirect hints from existing data?
 - Focus on CMSSM
small number of free parameters
 - hard constraint: LSP gives right amount of cold dark matter
CMSSM: only thin strips allowed in the $m_{1/2}$ – m_0 plane
 - Use existing data of M_W , $\sin^2 \theta_{\text{eff}}$, Γ_Z , $(g - 2)_\mu$, M_h
 $\text{BR}(b \rightarrow s\gamma)$, $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$, $\text{BR}(B_u \rightarrow \tau \nu_\tau)$, ΔM_{B_s}
 $\Rightarrow \chi^2$ fit with these observables
 - \Rightarrow best fit values for masses, couplings, . . .

Results: CMSSM: EWPO alone



⇒ preference for relatively small $m_{1/2}$

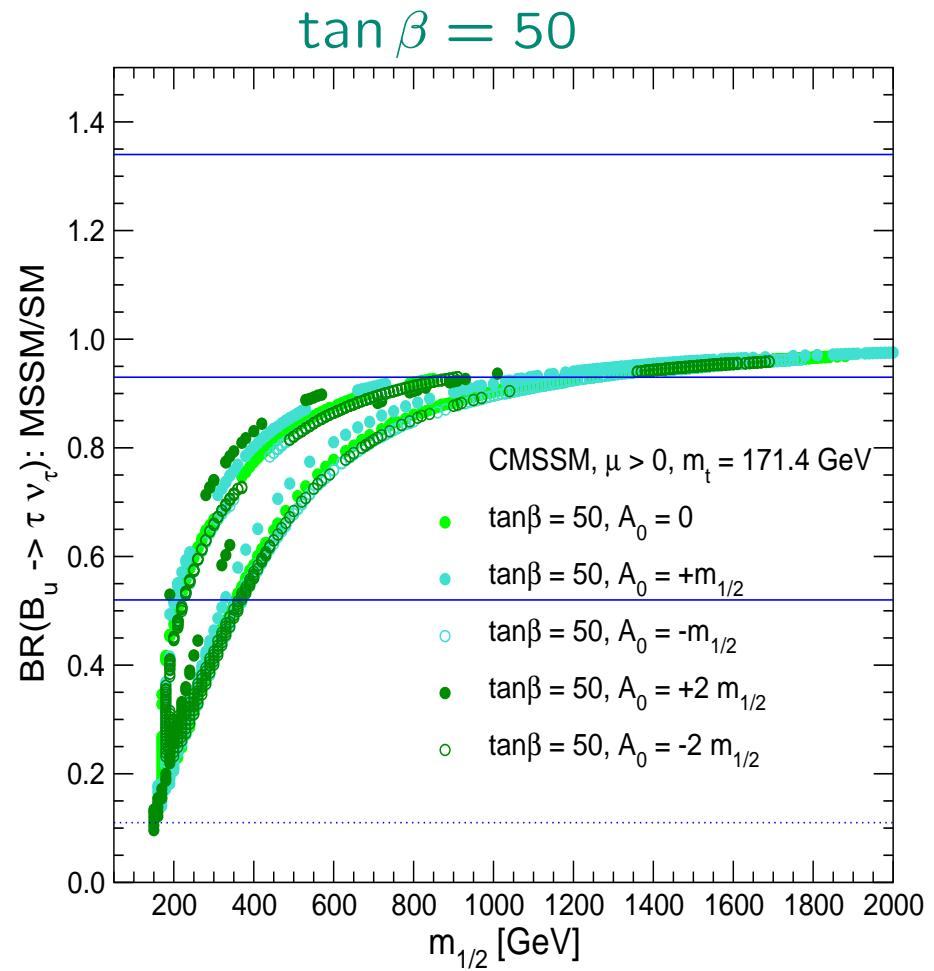
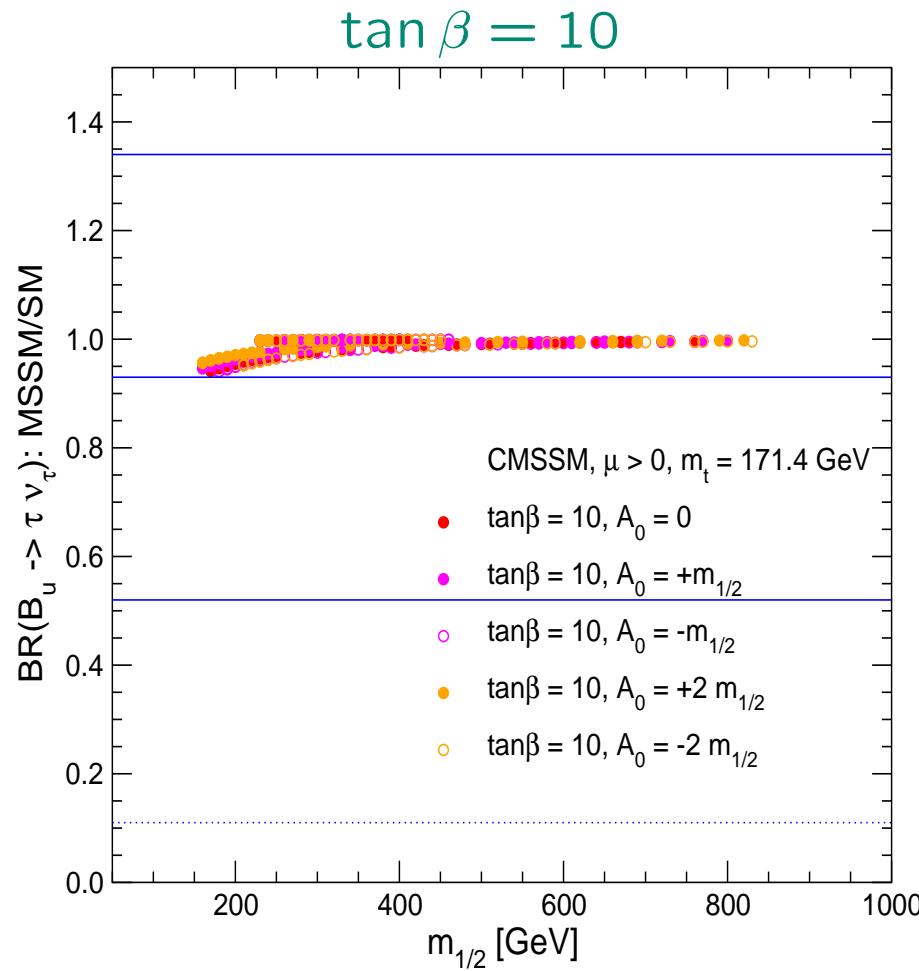
Results: CMSSM: BPO alone



⇒ preference for relatively large $m_{1/2}$

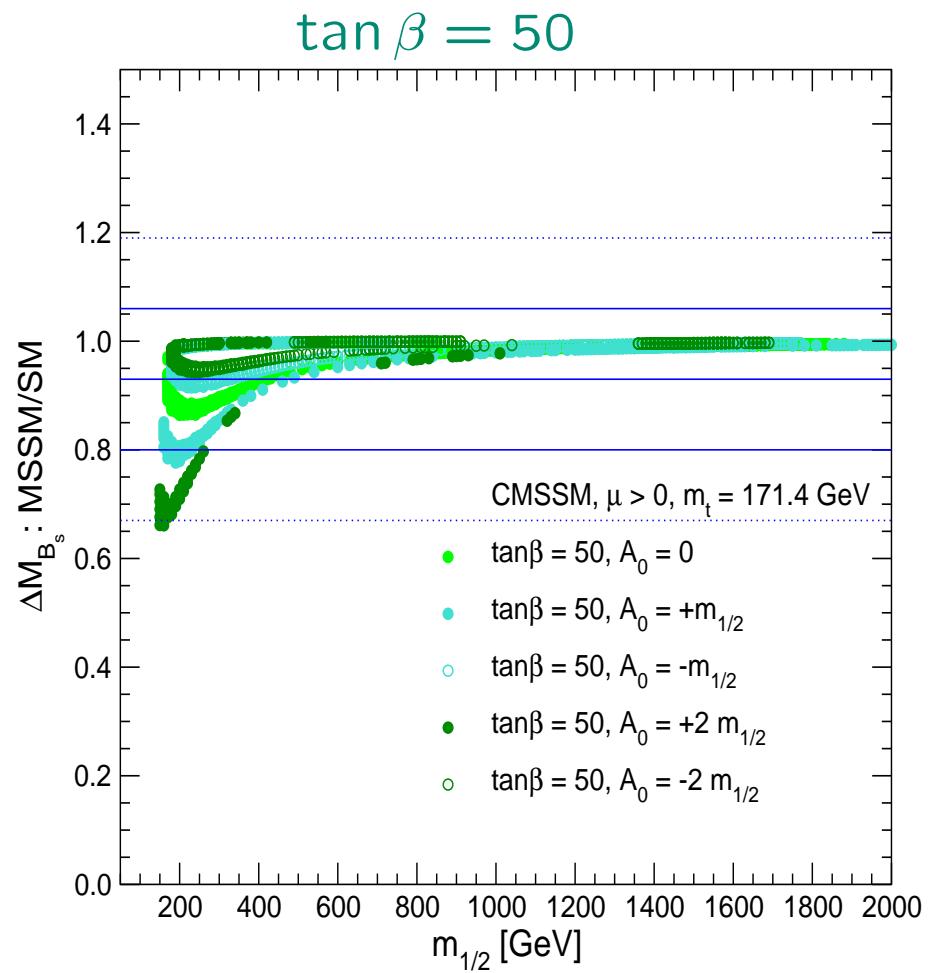
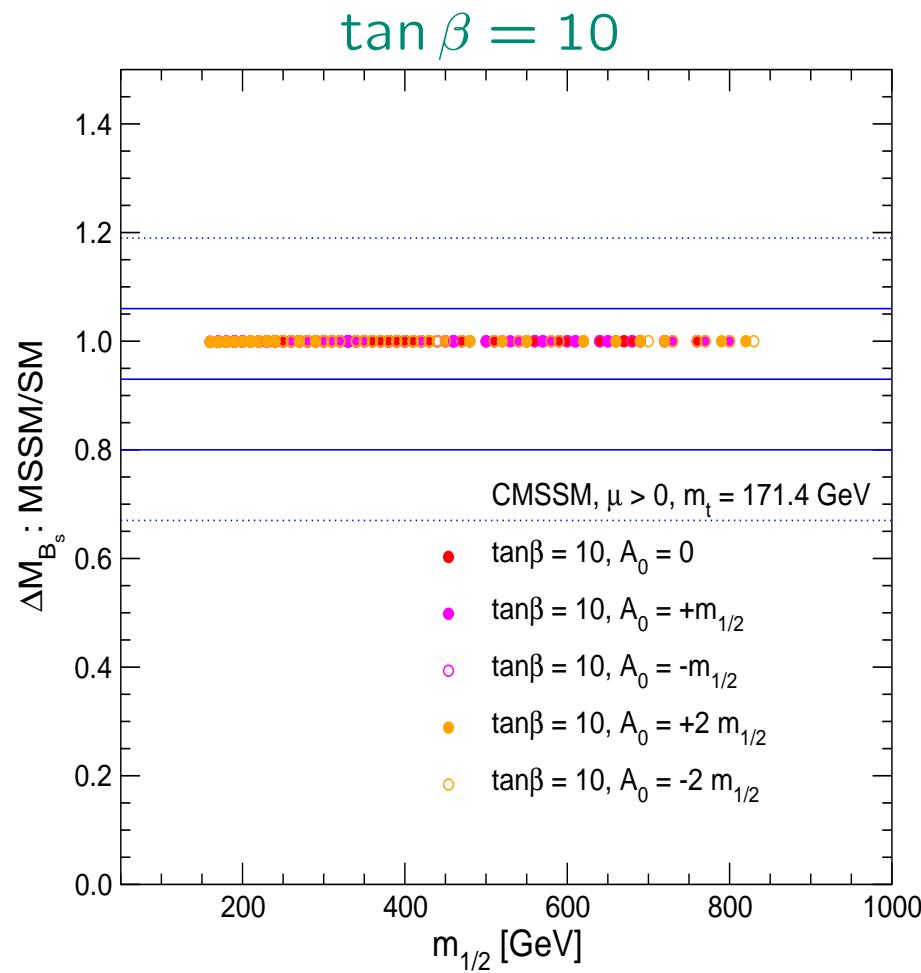
Problem of BPO: not precise enough yet

$\text{BR}(B_u \rightarrow \tau \nu_\tau)$: CMSSM/SM



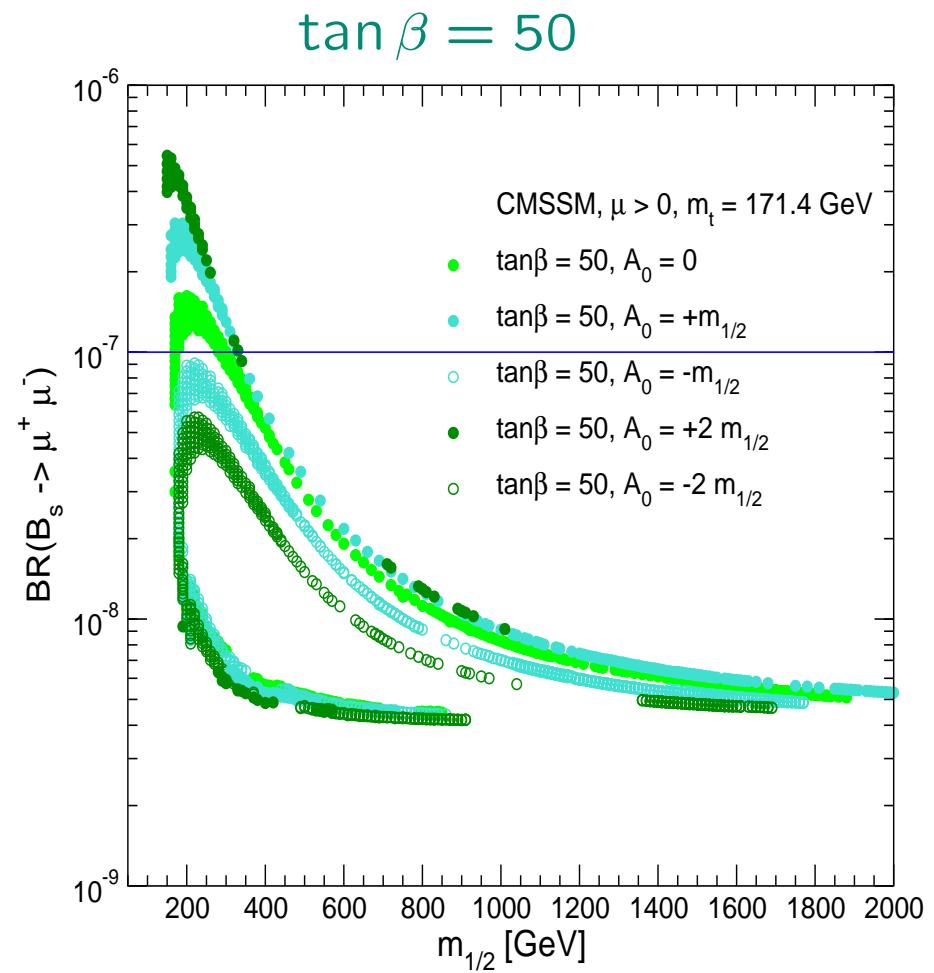
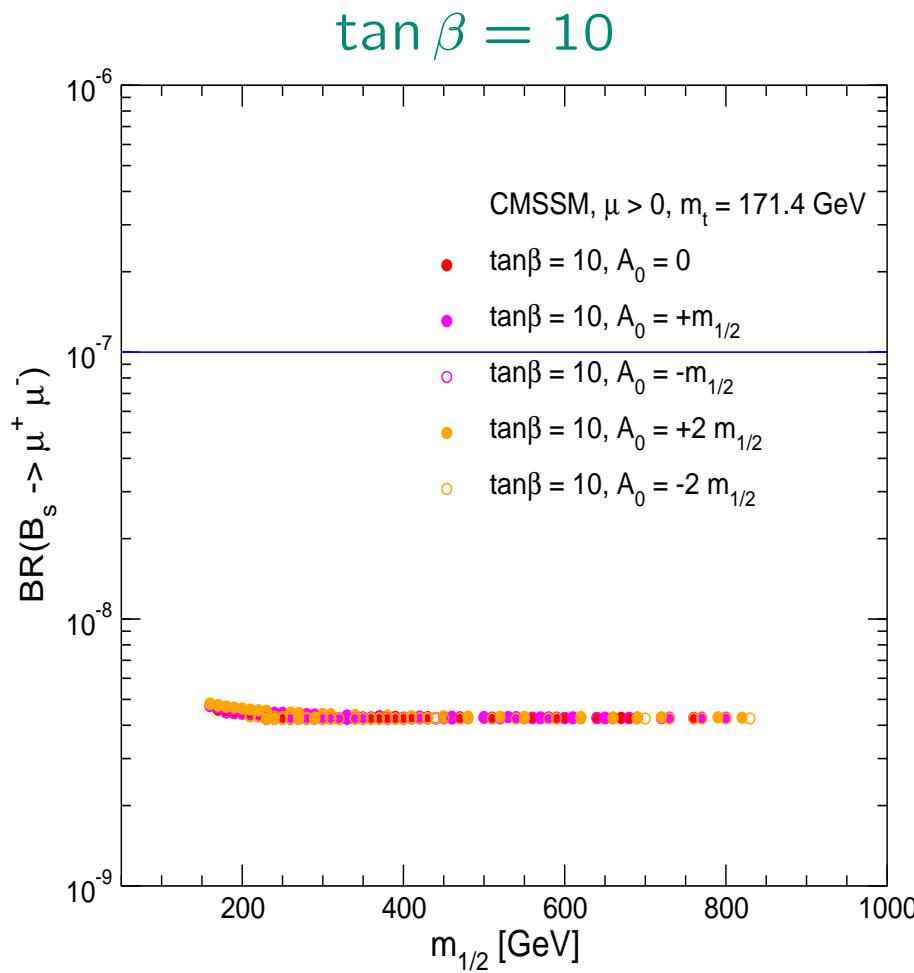
Problem of BPO: not precise enough yet

ΔM_{B_s} : CMSSM/SM



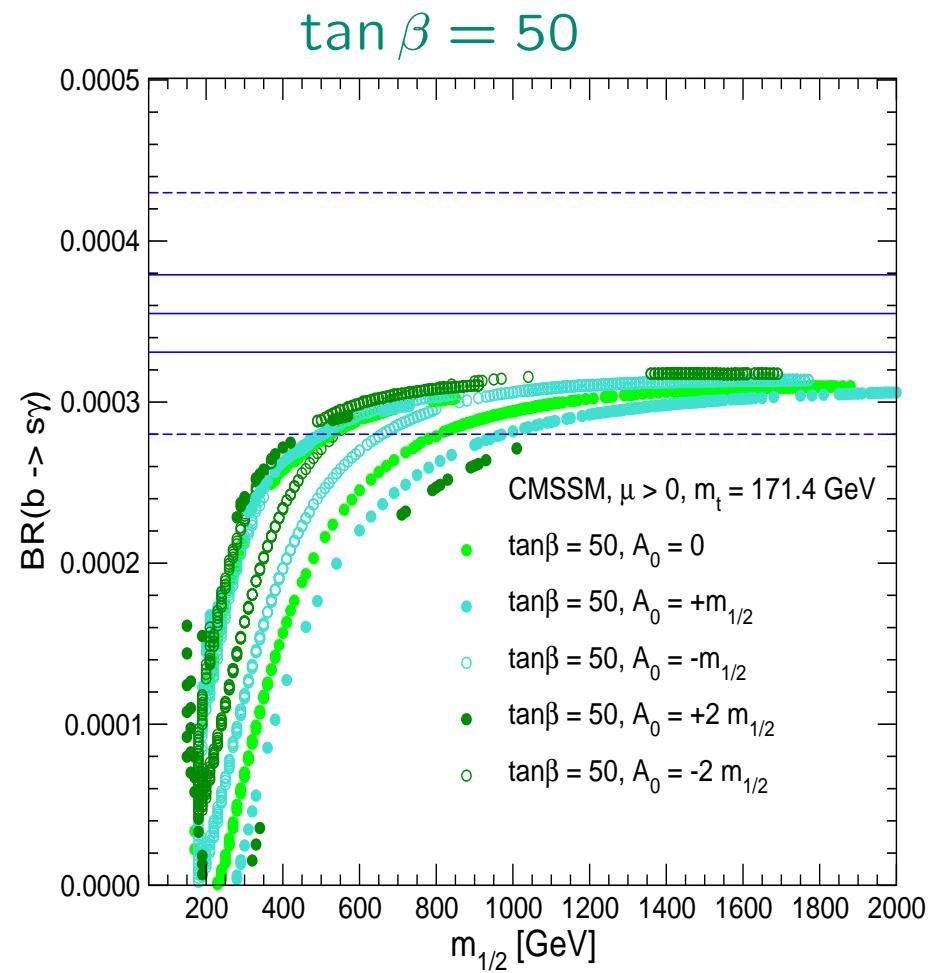
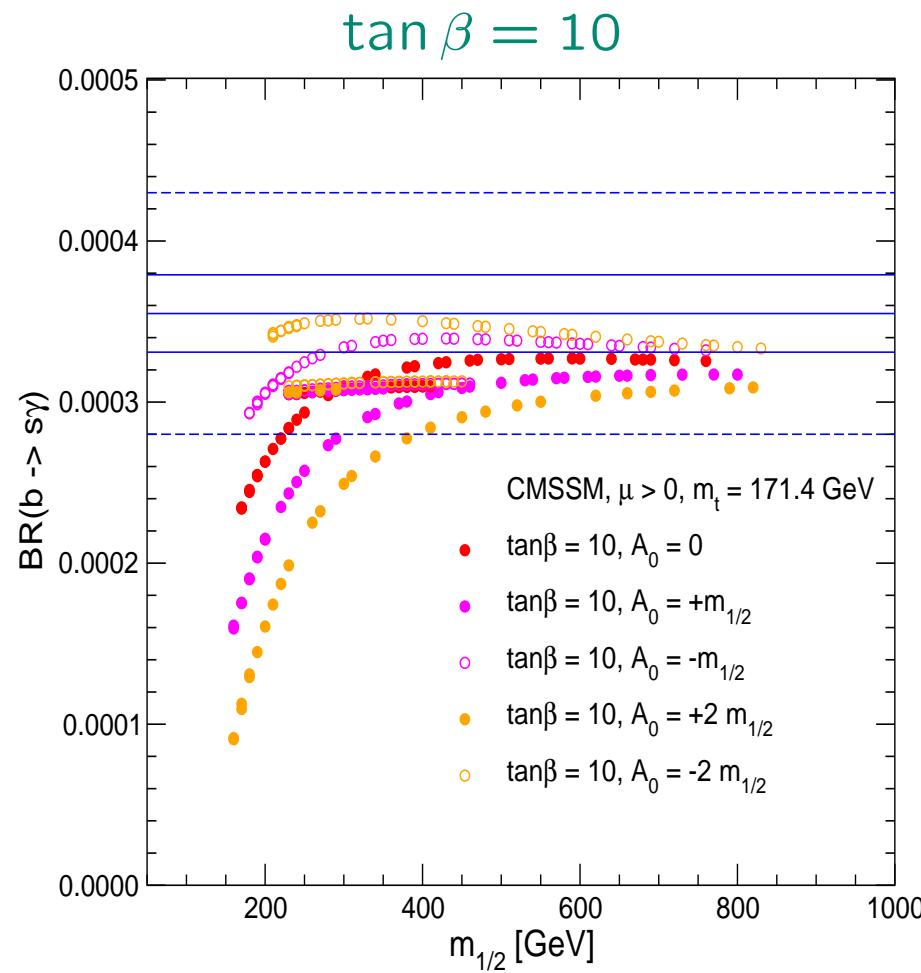
Problem of BPO: not precise enough yet (getting better)

$\text{BR}(B_s \rightarrow \mu^+ \mu^-)$: CMSSM

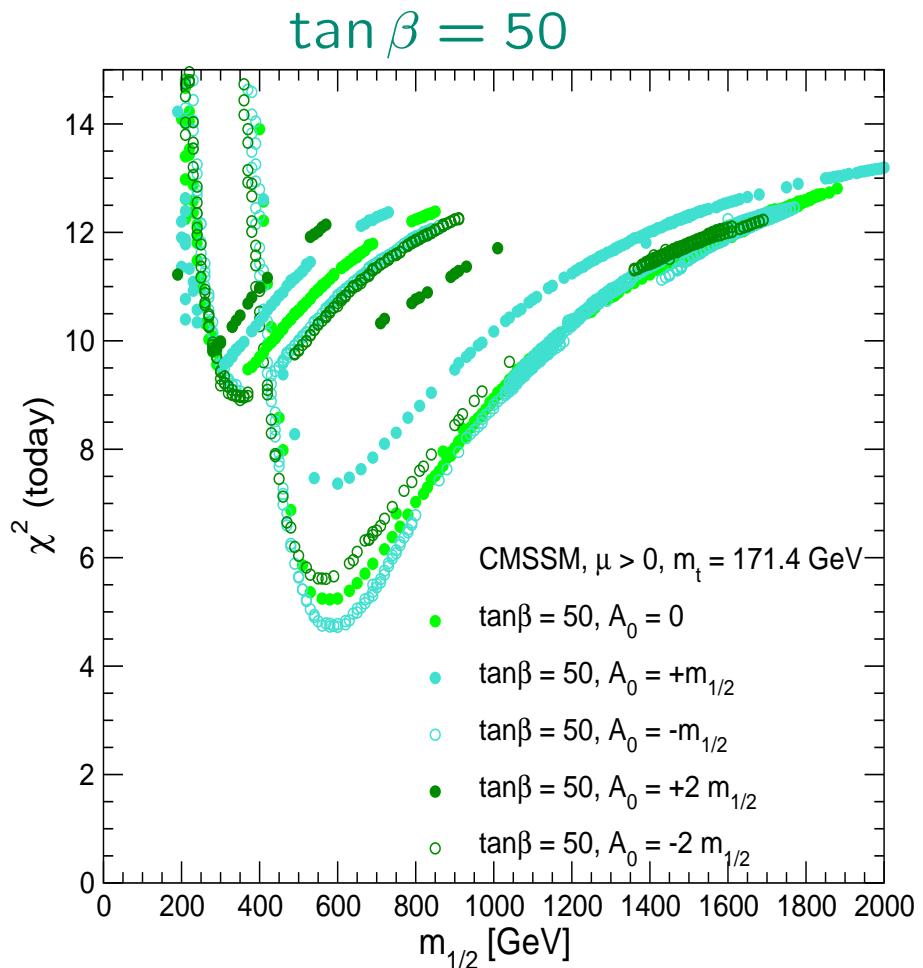
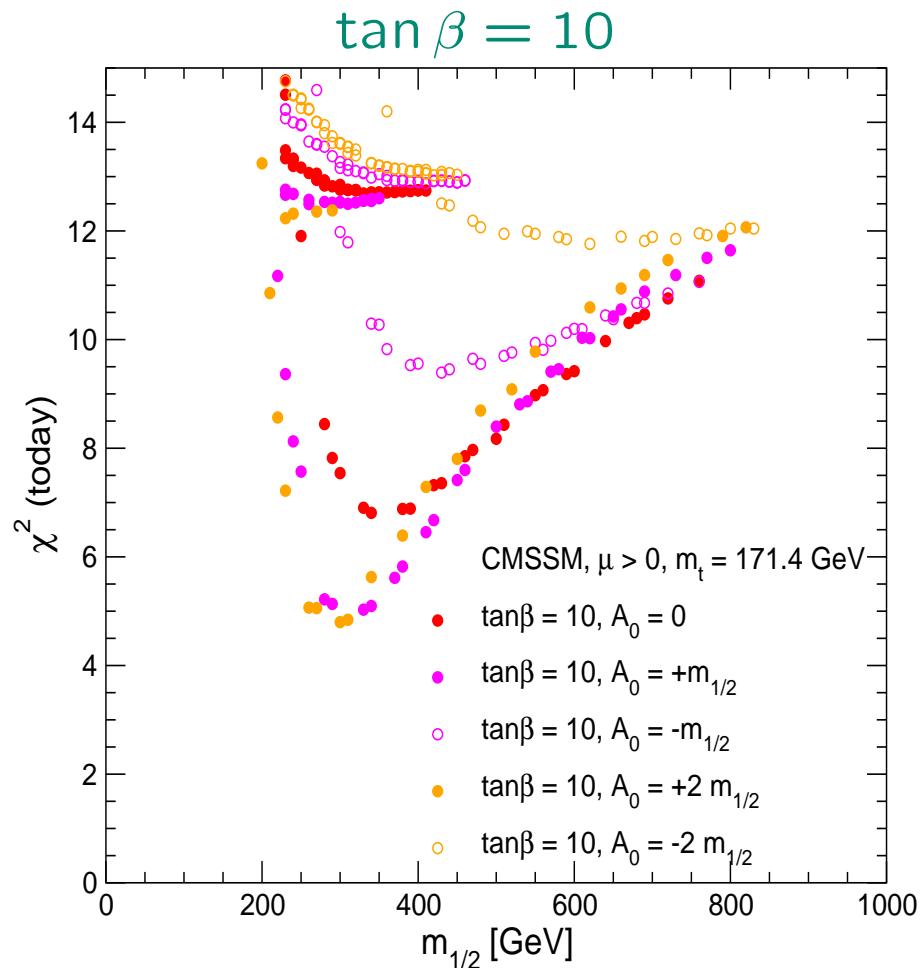


Problem of BPO: not precise enough yet (partial exception)

$\text{BR}(b \rightarrow s\gamma)$: CMSSM

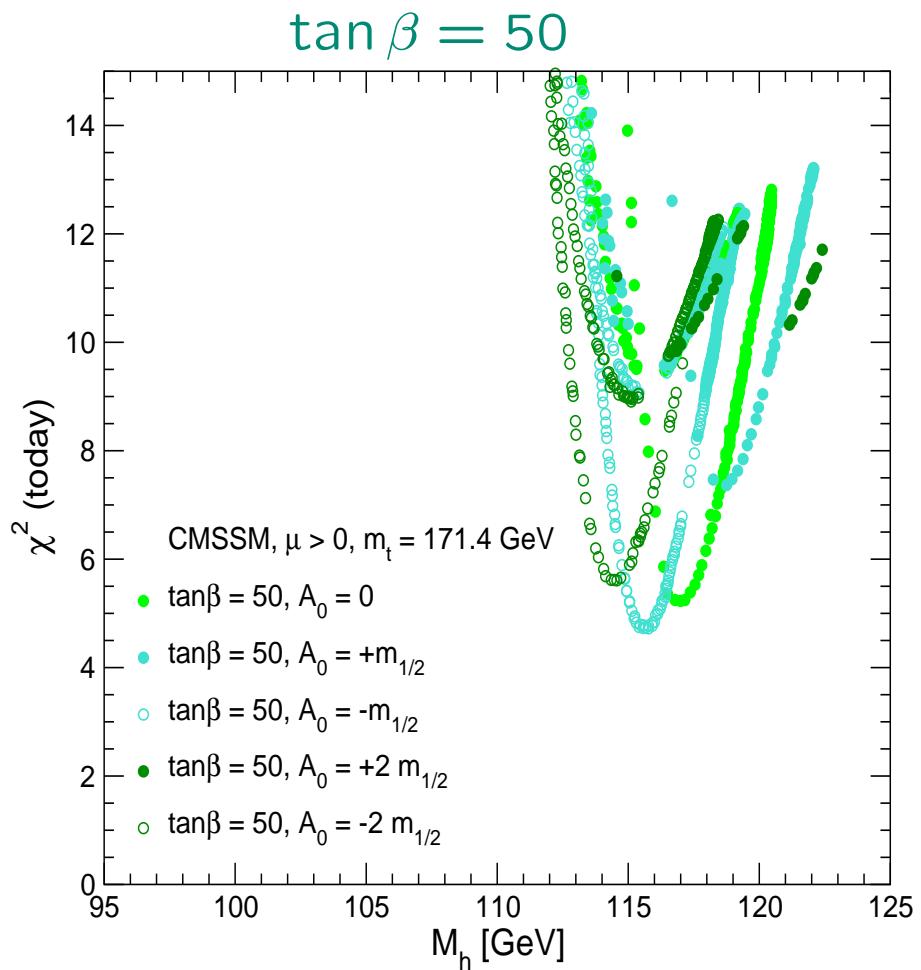
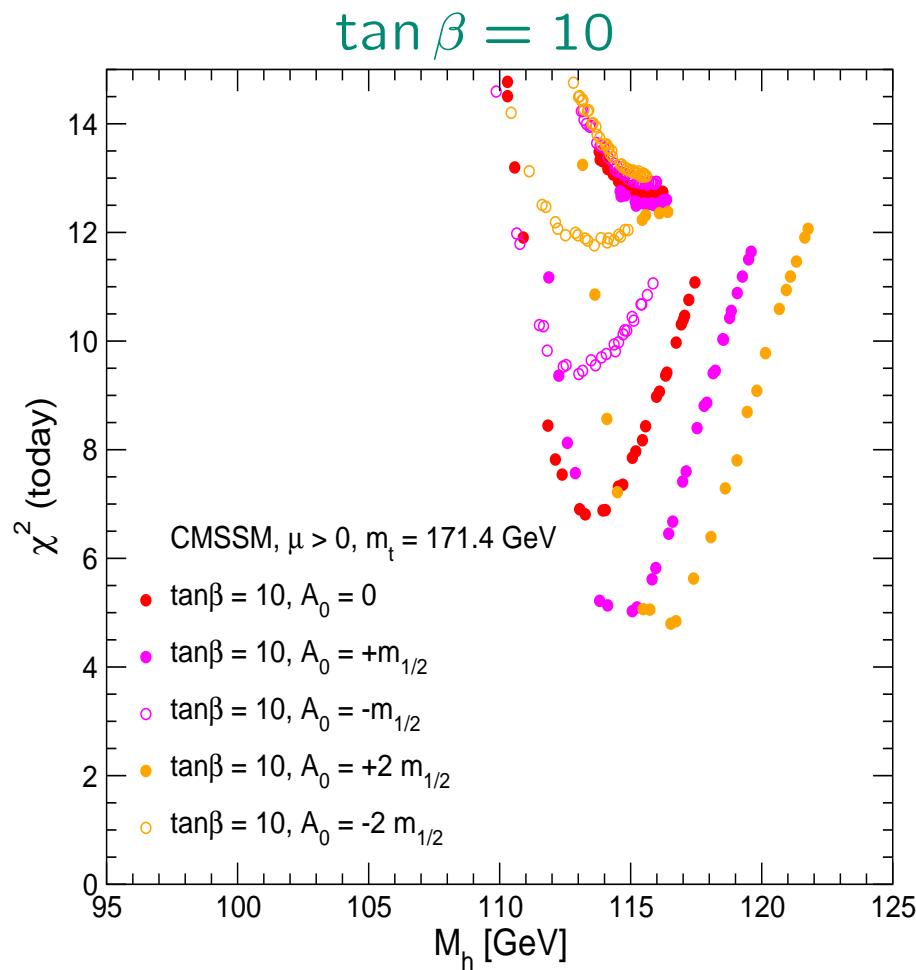


Results: CMSSM: everything combined



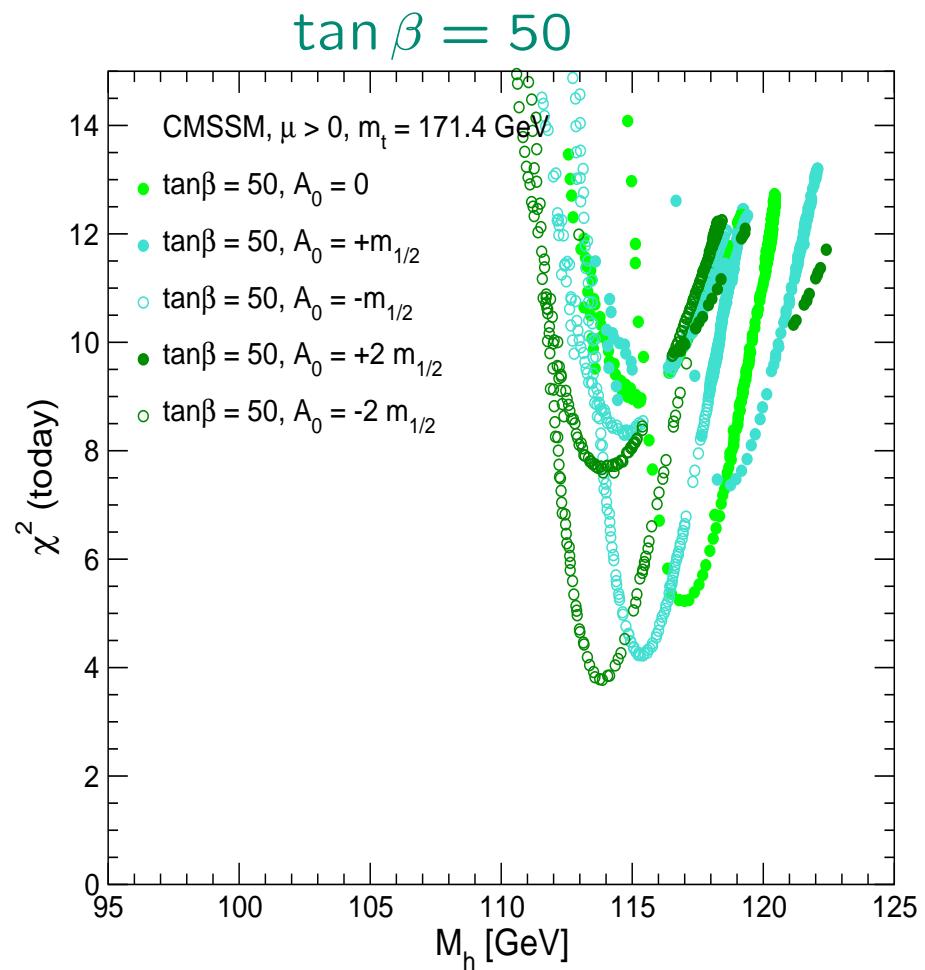
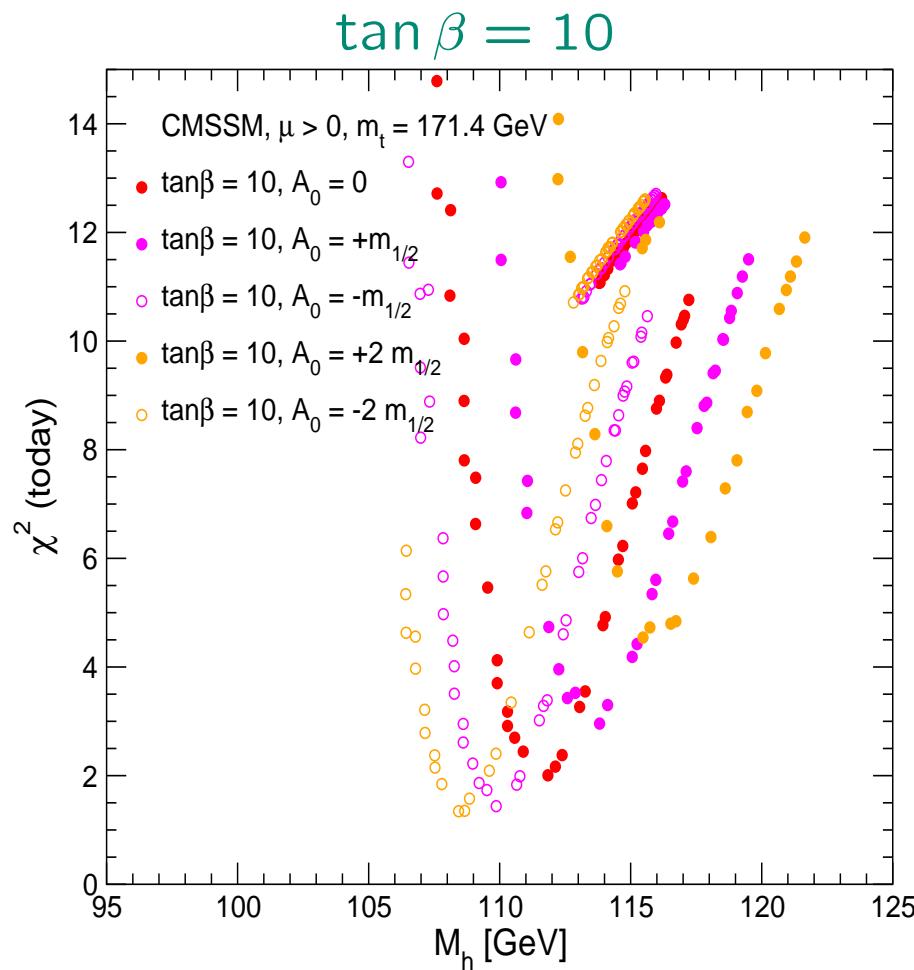
⇒ preference for somewhat smallish $m_{1/2}$ – but with a little tension
⇒ still a very good fit!

Results: CMSSM: prediction for M_h



⇒ preference for $M_h \sim 115$ GeV (LEP ...)

Results: CMSSM: “blue band” for M_h (without LEP results)



⇒ much “better” than in the SM

3. Impact of BPO on M_h in the CMSSM

[Buchmüller, Cavanaugh, de Roeck, S.H., Isidori, Paradisi, Ronga, Weber, Weiglein '07]

Main idea:

- combine all electroweak precision data as in the SM
- combine B physics observables
- include SM parameters with their errors: m_t, \dots
- scan over the full CMSSM parameter space

⇒ preferred CMSSM parameters

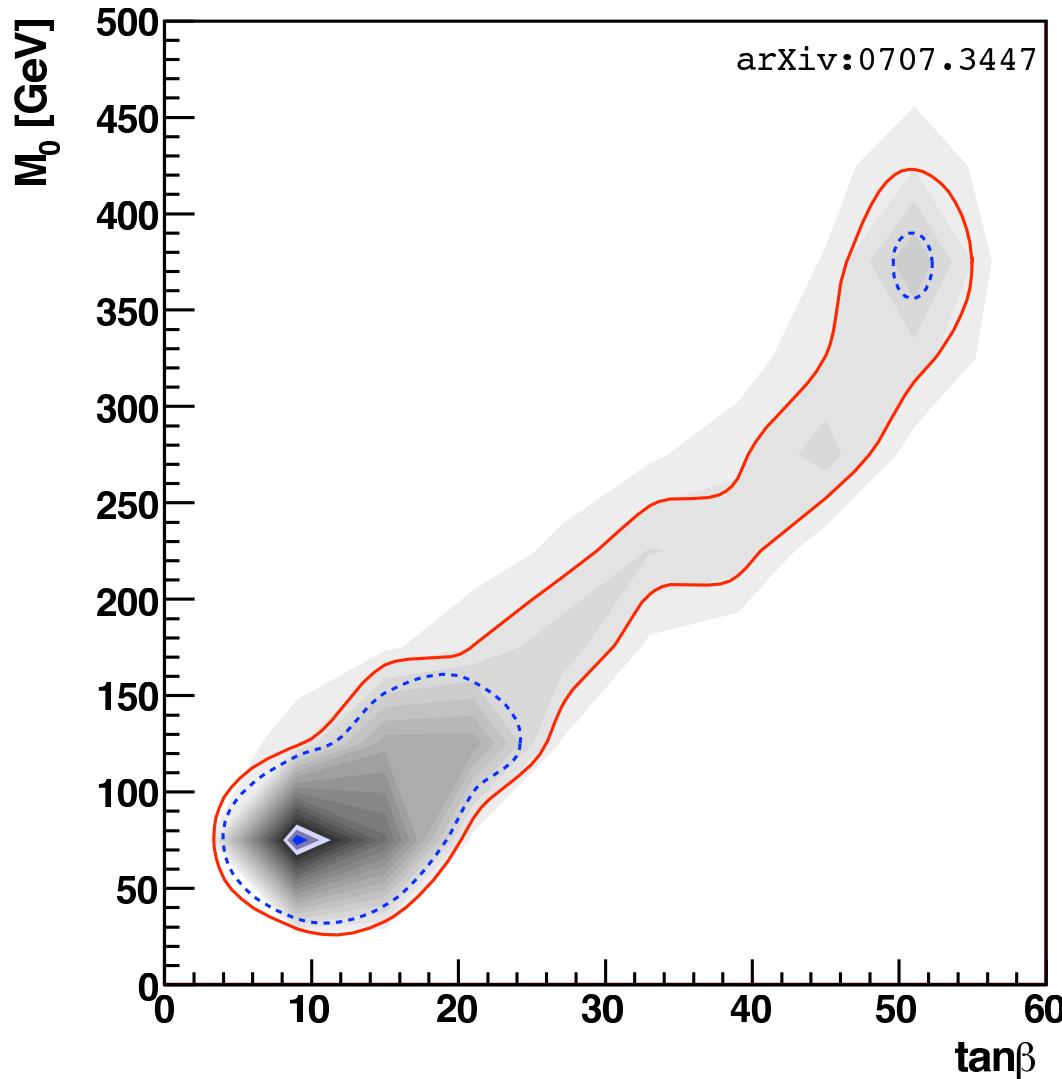
⇒ preferred M_h values

⇒ LHC/ILC reach

Most important:

Produce better graphics! :-)

Preferred region in the m_0 – $\tan\beta$ plane:



Pull distributions:

CMSSM

Variable	Measurement	Fit	$ O^{\text{meas}} - O^{\text{fit}} /\sigma^{\text{meas}}$
$\Delta\alpha_{\text{had}}^{(5)}(m_Z)$	0.02758 ± 0.00035	0.02774	0
m_Z [GeV]	91.1875 ± 0.0021	91.1873	0
Γ_Z [GeV]	2.4952 ± 0.0023	2.4952	0
σ_{had}^0 [nb]	41.540 ± 0.037	41.486	1
R_t	20.767 ± 0.025	20.744	1
$A_{\text{fb}}^{0,t}$	0.01714 ± 0.00095	0.01641	1
$A_t(P_\tau)$	0.1465 ± 0.0032	0.1479	0
R_b	0.21629 ± 0.00066	0.21613	0
R_c	0.1721 ± 0.0030	0.1722	0
$A_{\text{fb}}^{0,b}$	0.0992 ± 0.0016	0.1037	2
$A_{\text{fb}}^{0,c}$	0.0707 ± 0.0035	0.0741	1
A_b	0.923 ± 0.020	0.935	0
A_c	0.670 ± 0.027	0.668	0
$A_t(\text{SLD})$	0.1513 ± 0.0021	0.1479	1
$\sin^2\theta_{\text{eff}}^{\text{lept}}(Q_{\text{fb}})$	0.2324 ± 0.0012	0.2314	1
m_W [GeV]	80.398 ± 0.025	80.382	0
m_t [GeV]	170.9 ± 1.8	170.8	0
$R(b \rightarrow s\gamma)$	1.13 ± 0.12	1.12	0
$B_s \rightarrow \mu\mu$ [$\times 10^{-8}$]	< 8.00	0.33	N/A (upper limit)
Δa_μ [$\times 10^{-9}$]	2.95 ± 0.87	2.95	
Ωh^2	0.113 ± 0.009	0.113	

SM

Variable	Measurement	Fit	$ O^{\text{meas}} - O^{\text{fit}} /\sigma^{\text{meas}}$
$\Delta\alpha_{\text{had}}^{(5)}(m_Z)$	0.02758 ± 0.00035	0.02768	0
m_Z [GeV]	91.1875 ± 0.0021	91.1875	0
Γ_Z [GeV]	2.4952 ± 0.0023	2.4957	0
σ_{had}^0 [nb]	41.540 ± 0.037	41.477	2
R_t	20.767 ± 0.025	20.744	1
$A_{\text{fb}}^{0,t}$	0.01714 ± 0.00095	0.01645	1
$A_t(P_\tau)$	0.1465 ± 0.0032	0.1481	0
R_b	0.21629 ± 0.00066	0.21586	0
R_c	0.1721 ± 0.0030	0.1722	0
$A_{\text{fb}}^{0,b}$	0.0992 ± 0.0016	0.1038	2
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m_W [GeV]	80.398 ± 0.025	80.374	0
m_t [GeV]	170.9 ± 1.8	171.3	0
Γ_W [GeV]	2.140 ± 0.060	2.091	1

⇒ note the new observables: $\text{BR}(b \rightarrow s\gamma)$, $[\text{BR}(B_s \rightarrow \mu^+ \mu^-)]$, $(g-2)_\mu$, CDM

Pull distributions:

CMSSM

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$A_{fb}^{0,l}$	0.01714 ± 0.00095	0.01641	1
$A_l(P_\tau)$	0.1465 ± 0.0032	0.1479	0.5
R_b	0.21629 ± 0.00066	0.21613	0.5
R_c	0.1721 ± 0.0030	0.1722	0
$A_{fb}^{0,b}$	0.0992 ± 0.0016	0.1037	3
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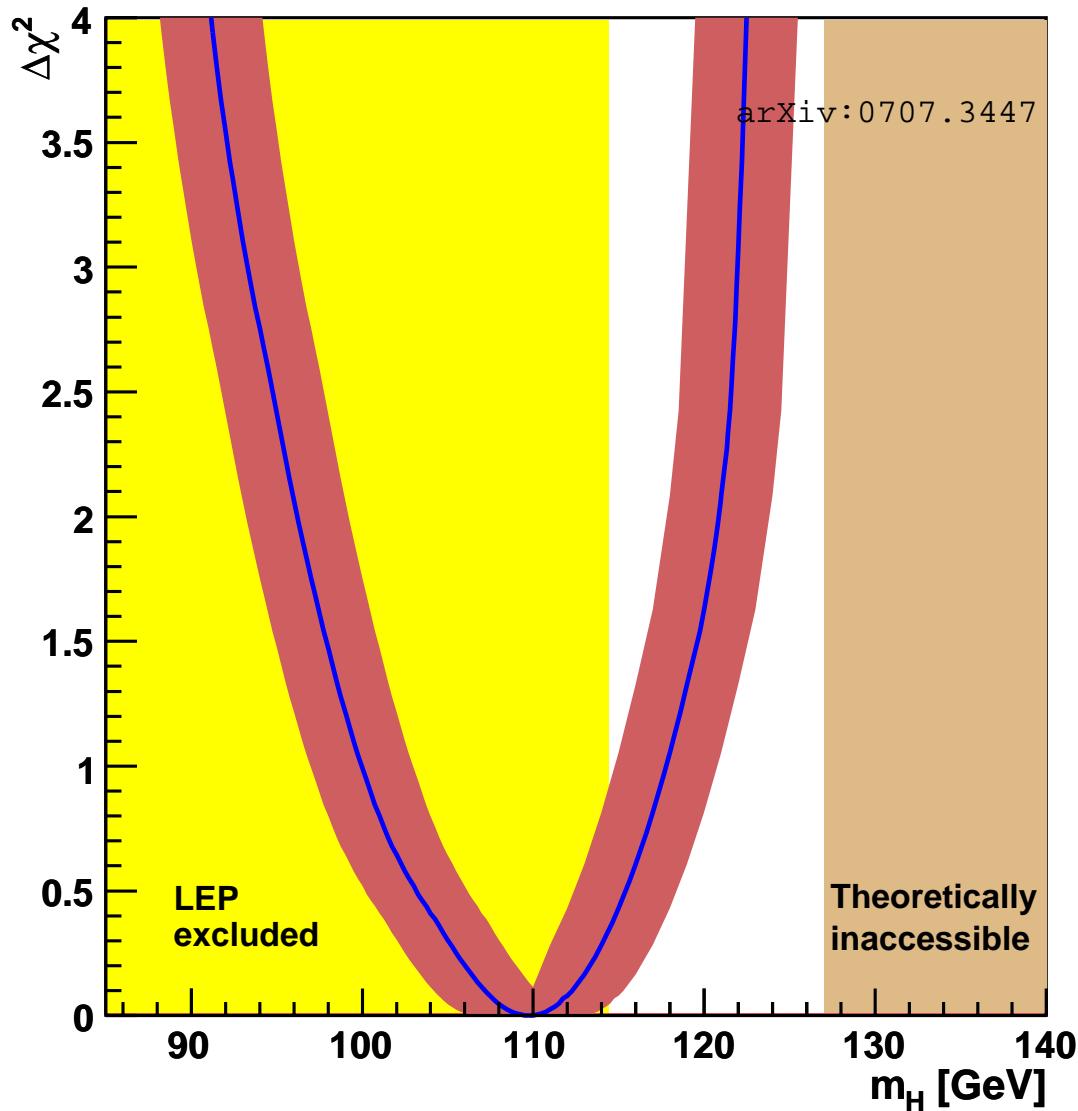
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Probabilities: 24% / 20%

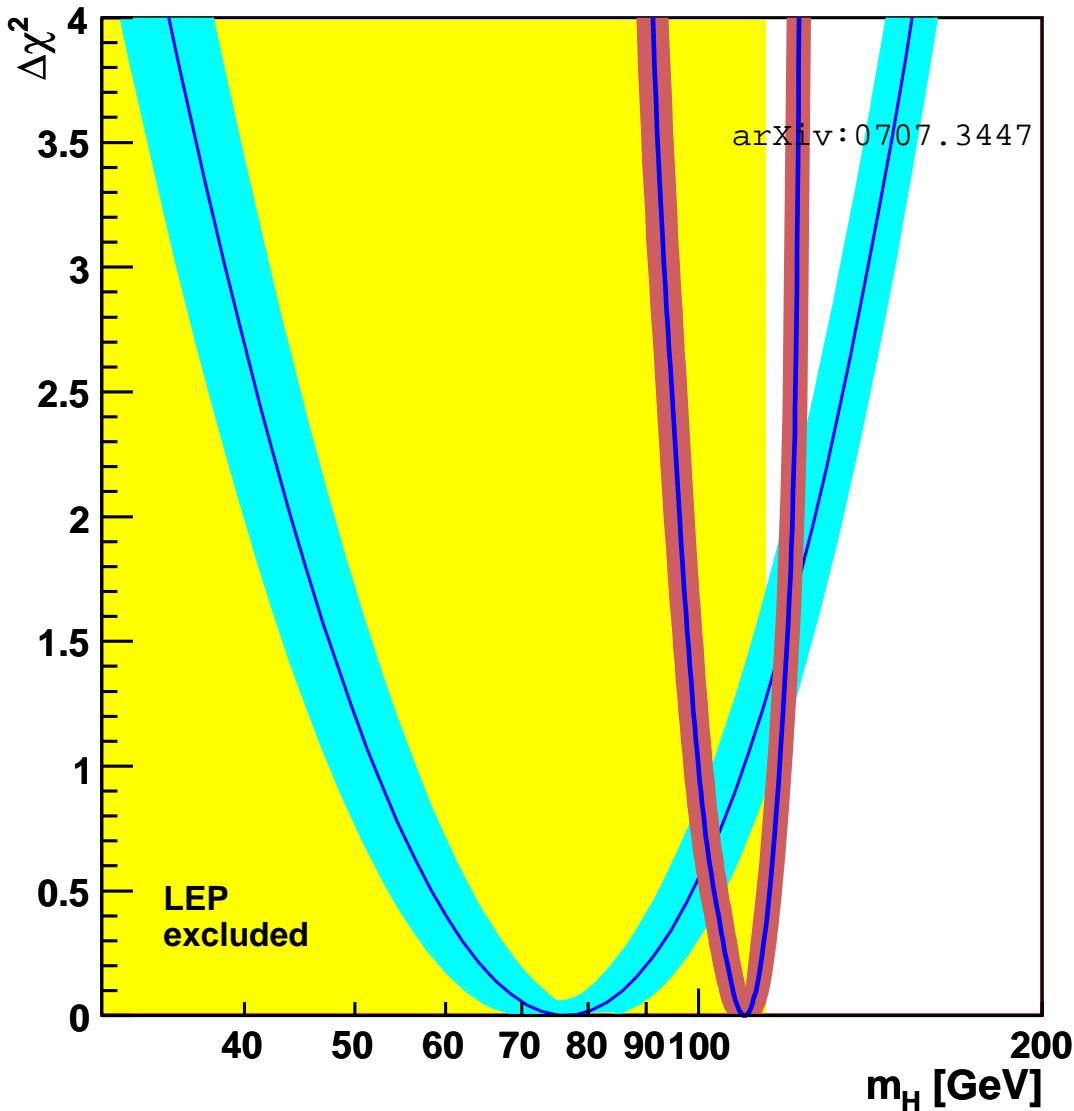
15% / 15% (incl. / excl. M_h)

Red band plot:



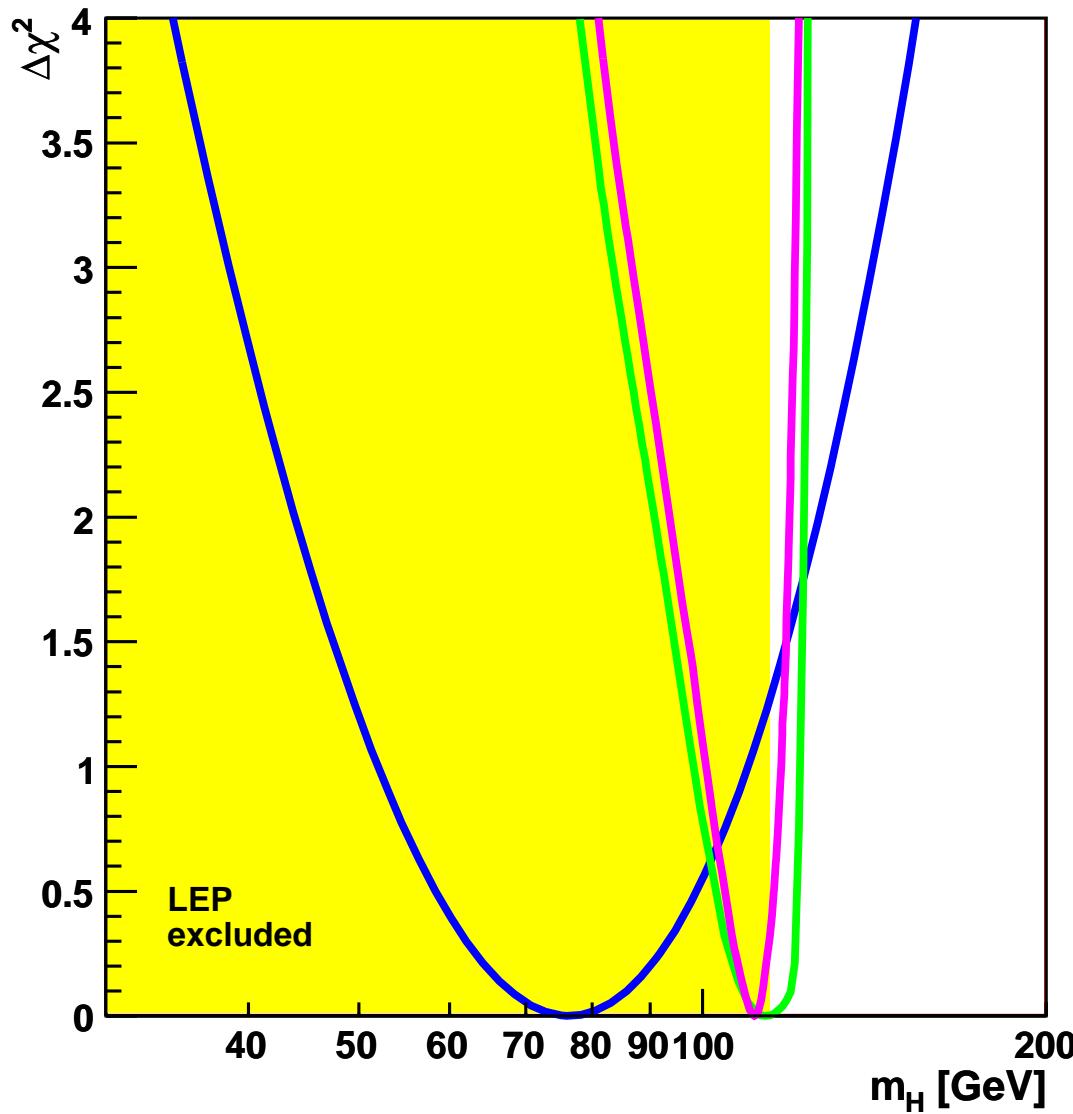
$$M_h = 110^{+8}_{-10} \text{ (exp)} \pm 3 \text{ (theo)} \text{ GeV}$$

Blue/Red band plot:



CMSSM (despite its simplicity) is better than the SM

Impact of $\text{BR}(b \rightarrow s\gamma)$: \Rightarrow green curve (preliminary!)

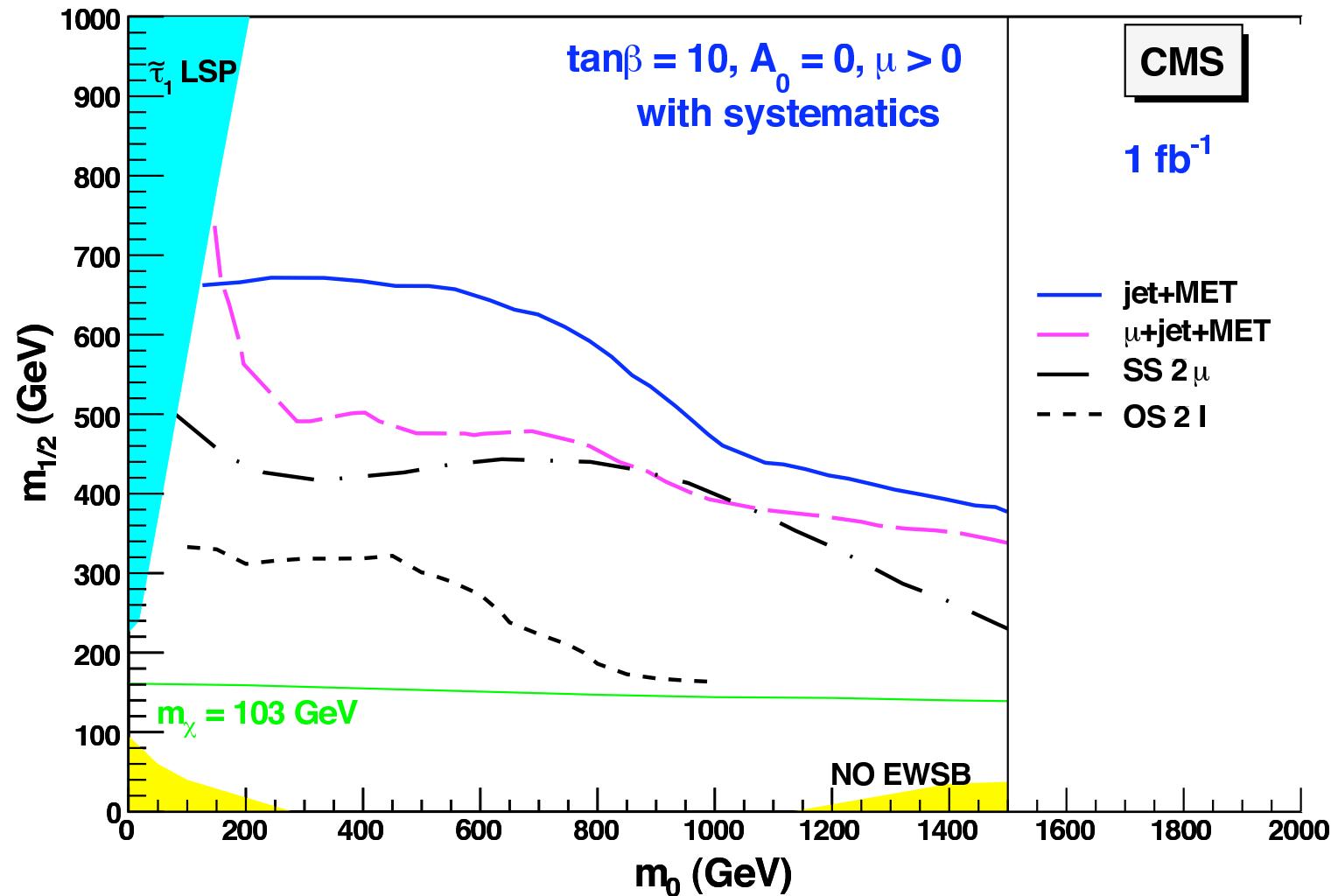


\Rightarrow impact visible, but not decisive (location of minimum)

Connection to high P_T physics:

LHC (CMS) reach with 1 fb^{-1} :

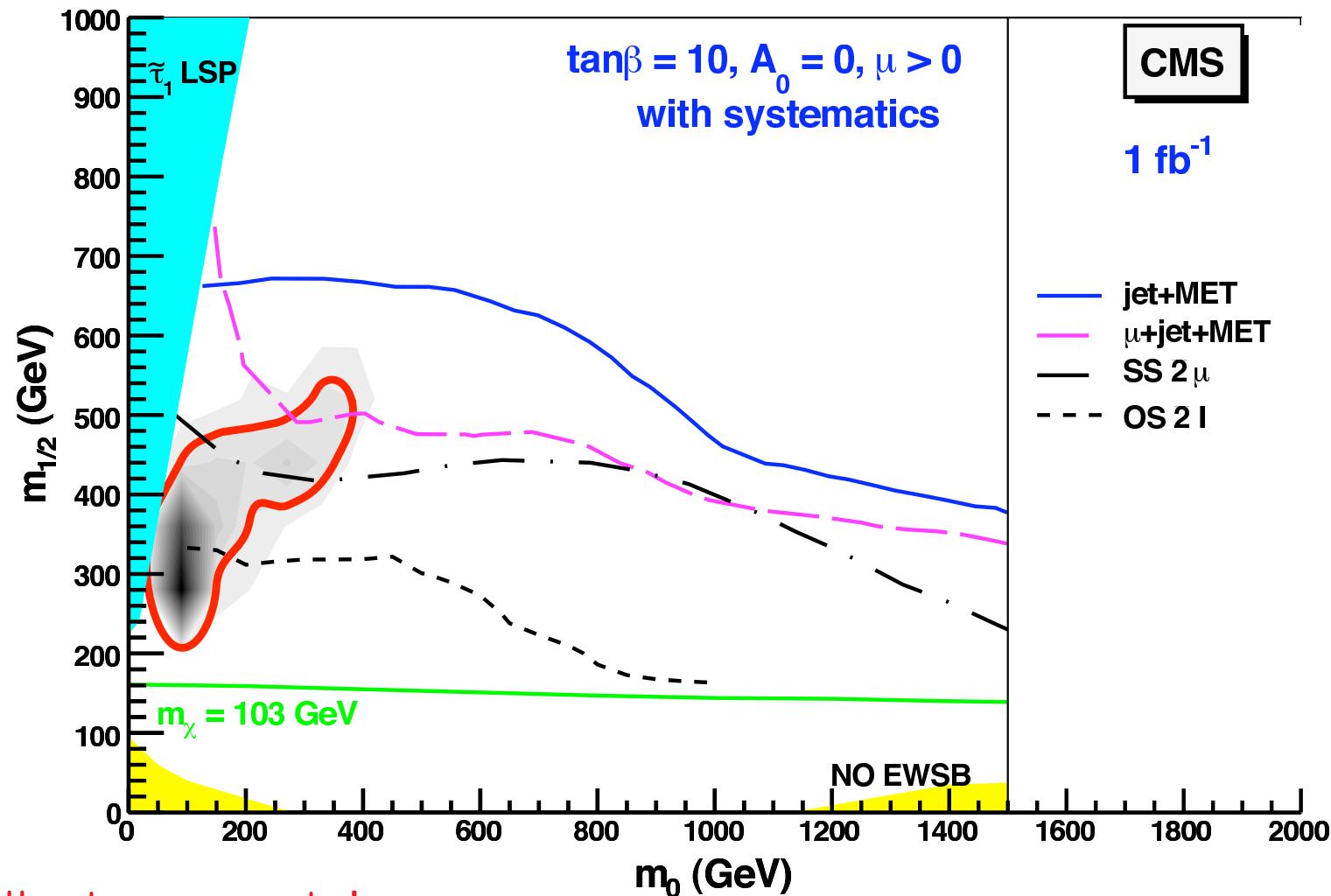
[CMS '07]



Connection to high P_T physics:

LHC (CMS) reach with 1 fb^{-1} :

[CMS '07]



⇒ excellent prospects!

4. Impact and prospects of BPO on NUHM fits

[J. Ellis, S.H., K. Olive, A.M. Weber, G. Weiglein '07][J. Ellis, T. Hahn, S.H., K. Olive, G. Weiglein '07]

NUHM: (Non-universal Higgs mass model)

⇒ besides the CMSSM parameters

M_A and μ

Assumption:

no unification of scalar fermion and scalar Higgs parameters
at the GUT scale

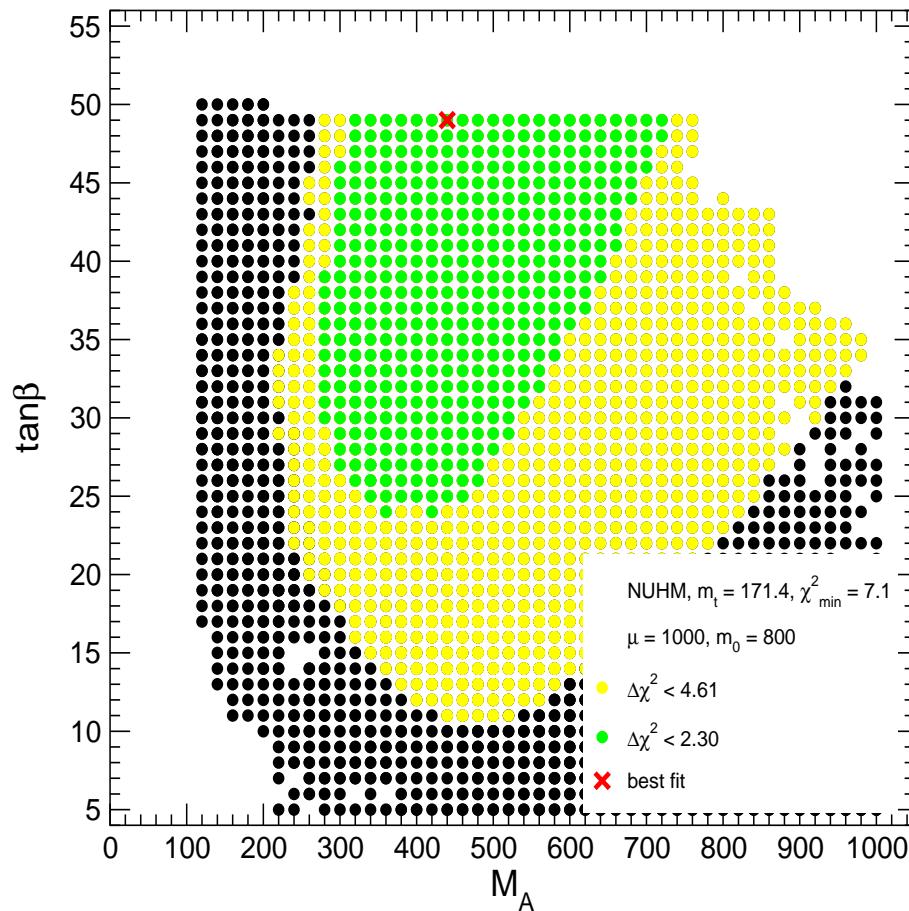
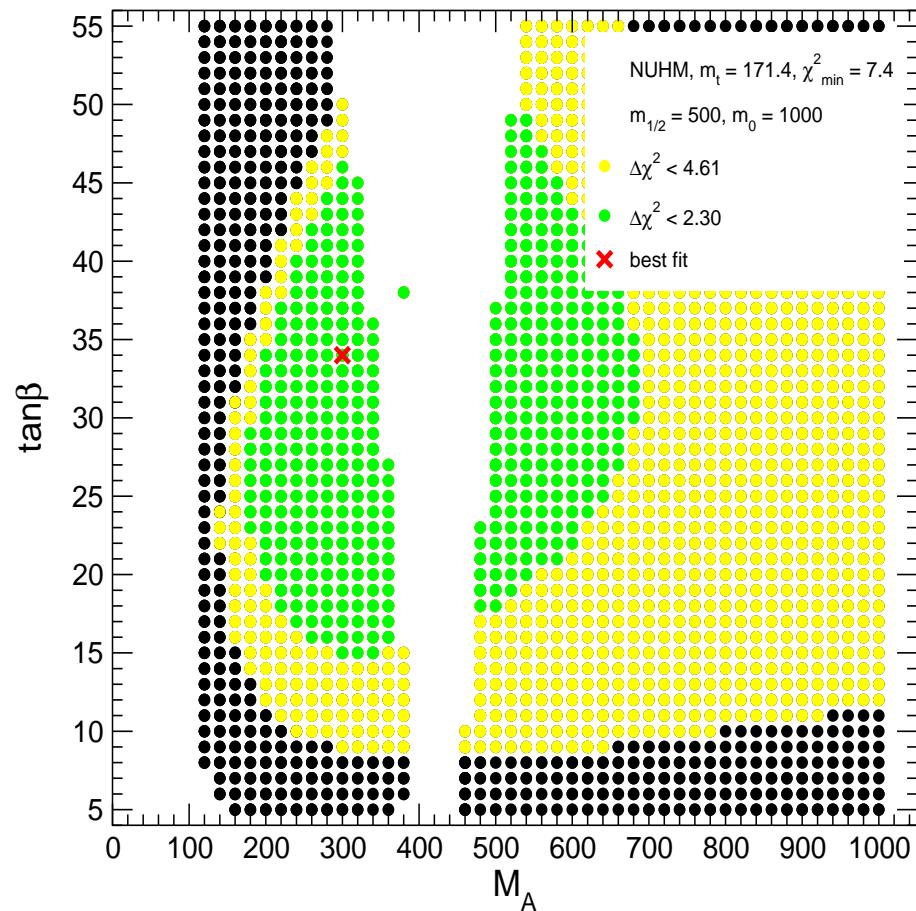
⇒ effectively M_A and μ free parameters at the EW scale

⇒ particle spectra from renormalization group running to weak scale

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⇒ possible: M_A – $\tan\beta$ planes in agreement with CDM :-)

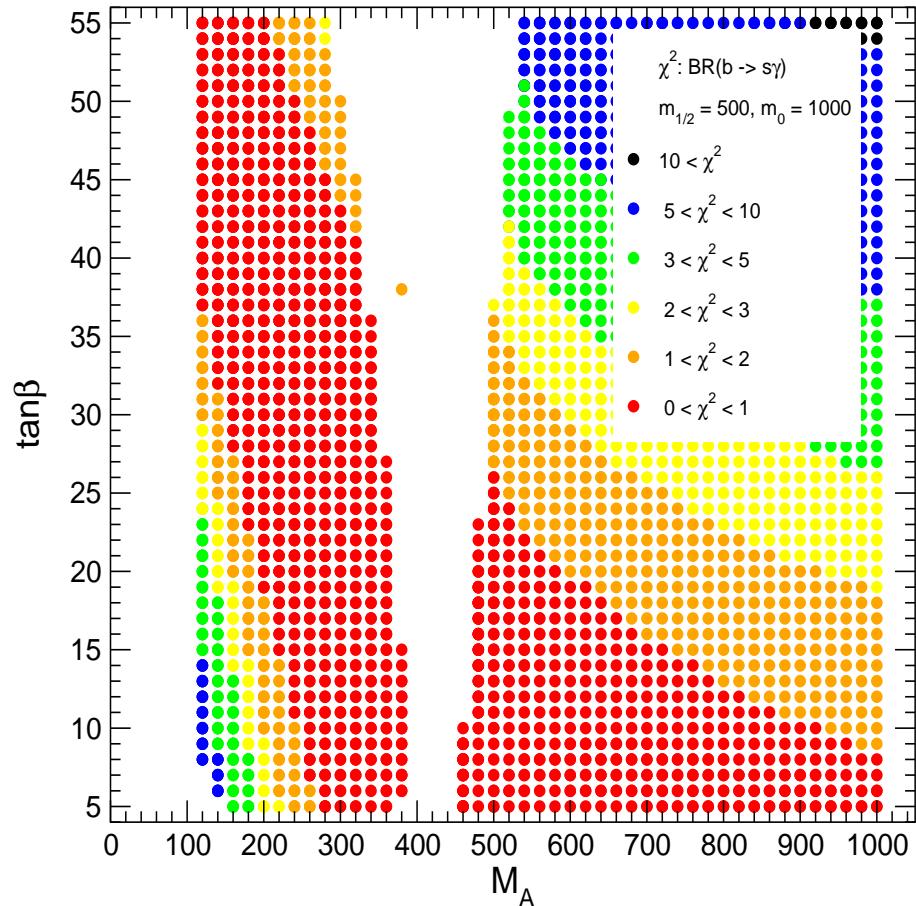
Example: NUHM planes 2,3



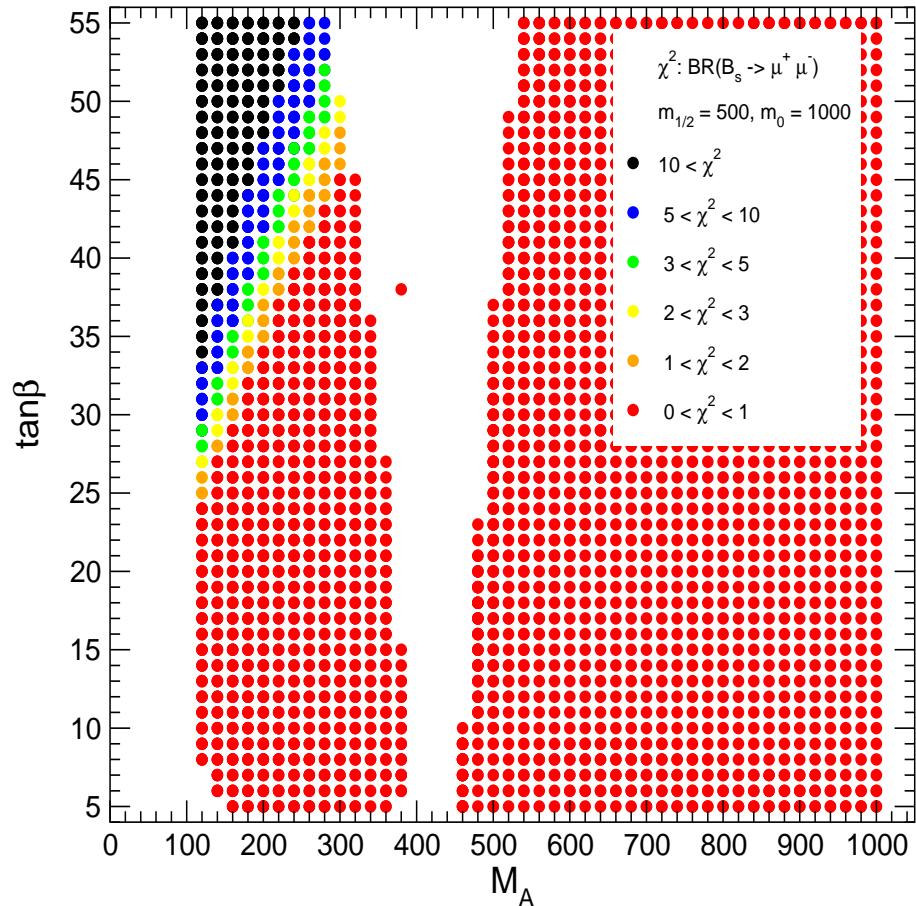
→ good χ^2 (M_W , $\sin^2 \theta_{\text{eff}}$, Γ_Z , M_h , $(g - 2)_\mu$, $\text{BR}(b \rightarrow s\gamma)$ and other BPO)
 → larger regions o.k.

Impact of BPO on plane 2:

$\text{BR}(b \rightarrow s\gamma)$



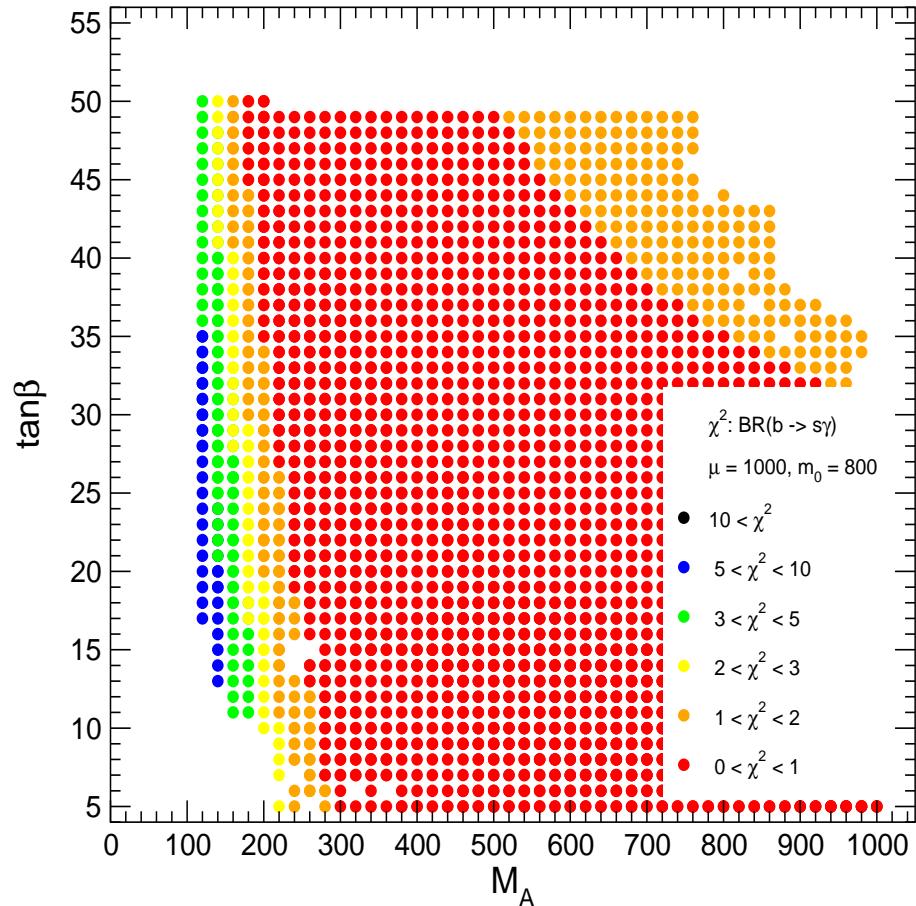
$\text{BR}(B_s \rightarrow \mu^+ \mu^-)$



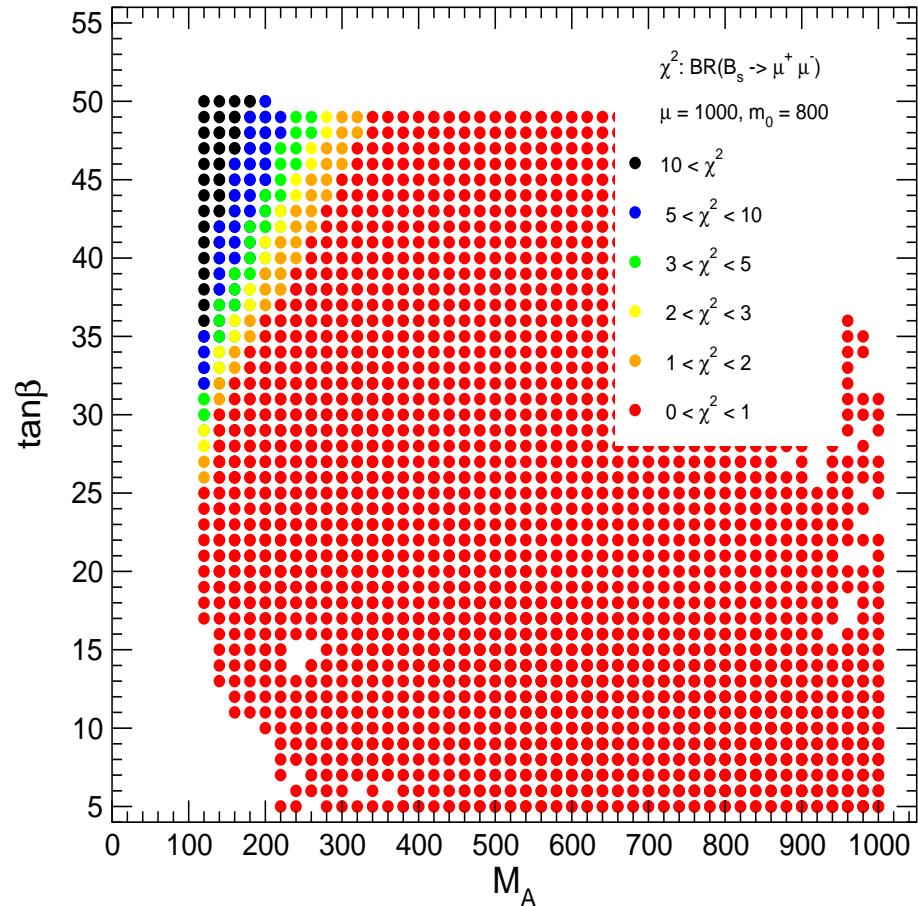
⇒ so far mostly “mild” impact

Impact of BPO on plane 3:

$\text{BR}(b \rightarrow s\gamma)$

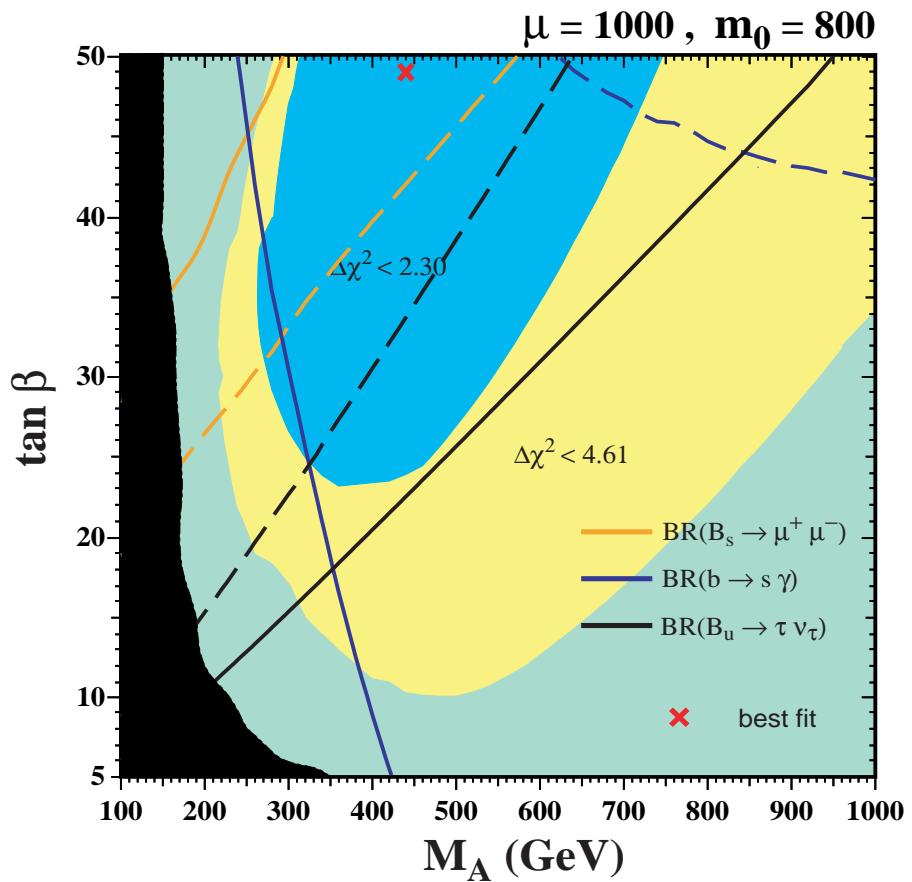
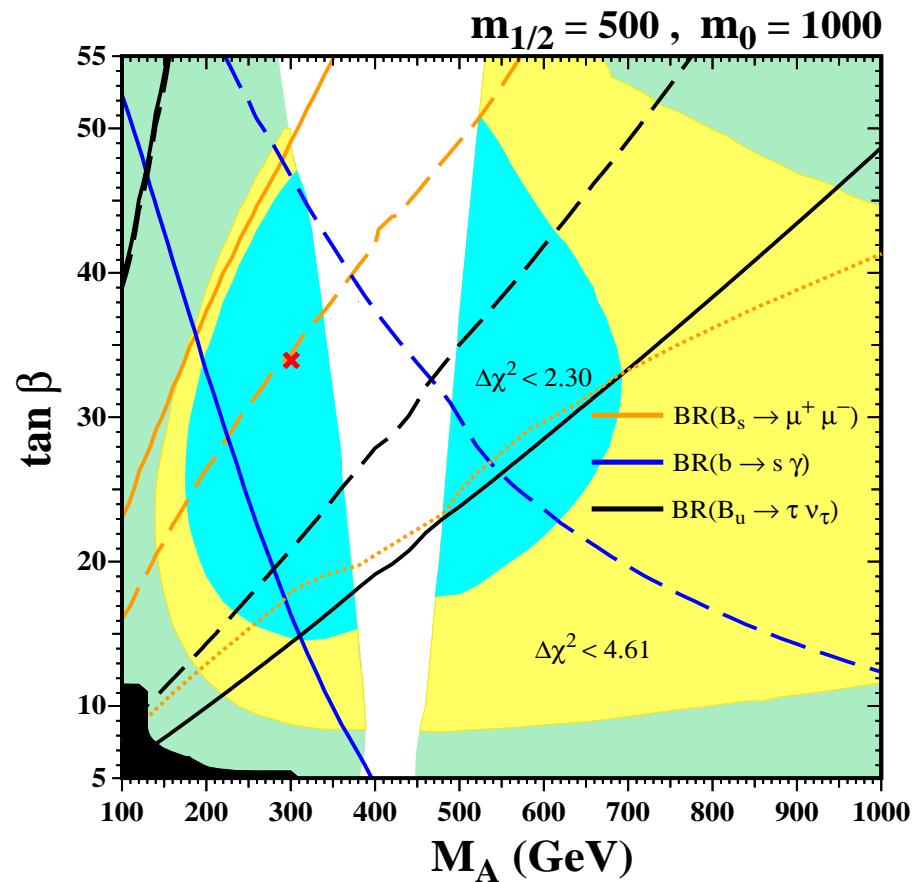


$\text{BR}(B_s \rightarrow \mu^+ \mu^-)$



⇒ so far mostly “mild” impact

Future prospects:

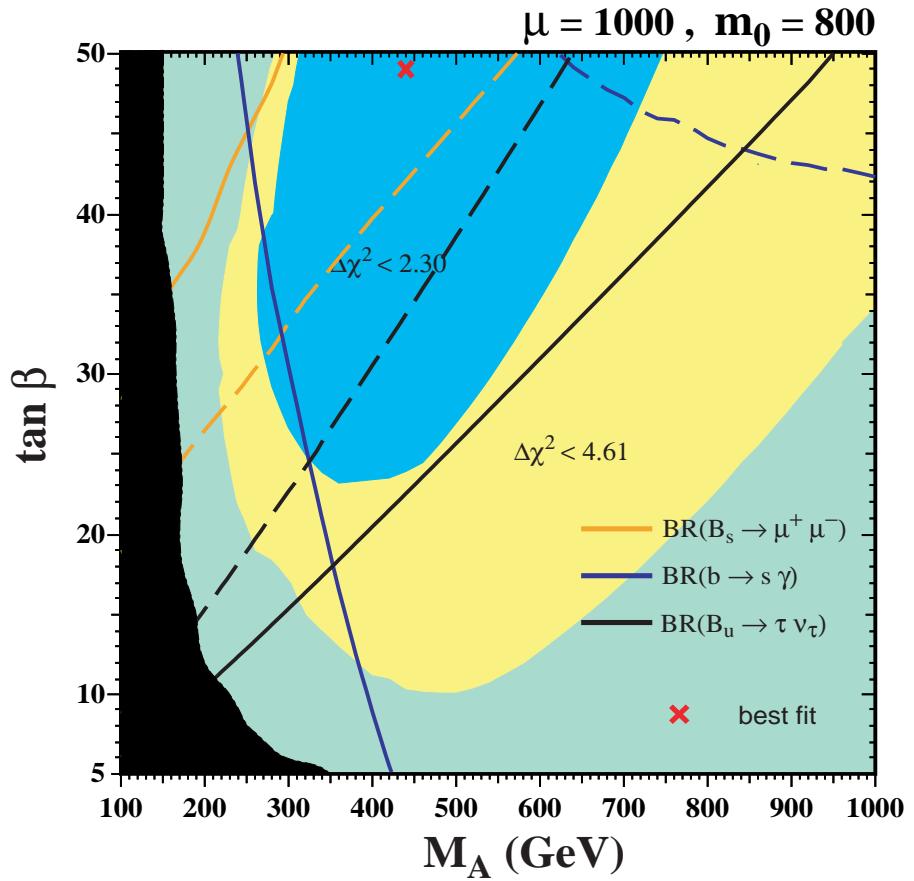
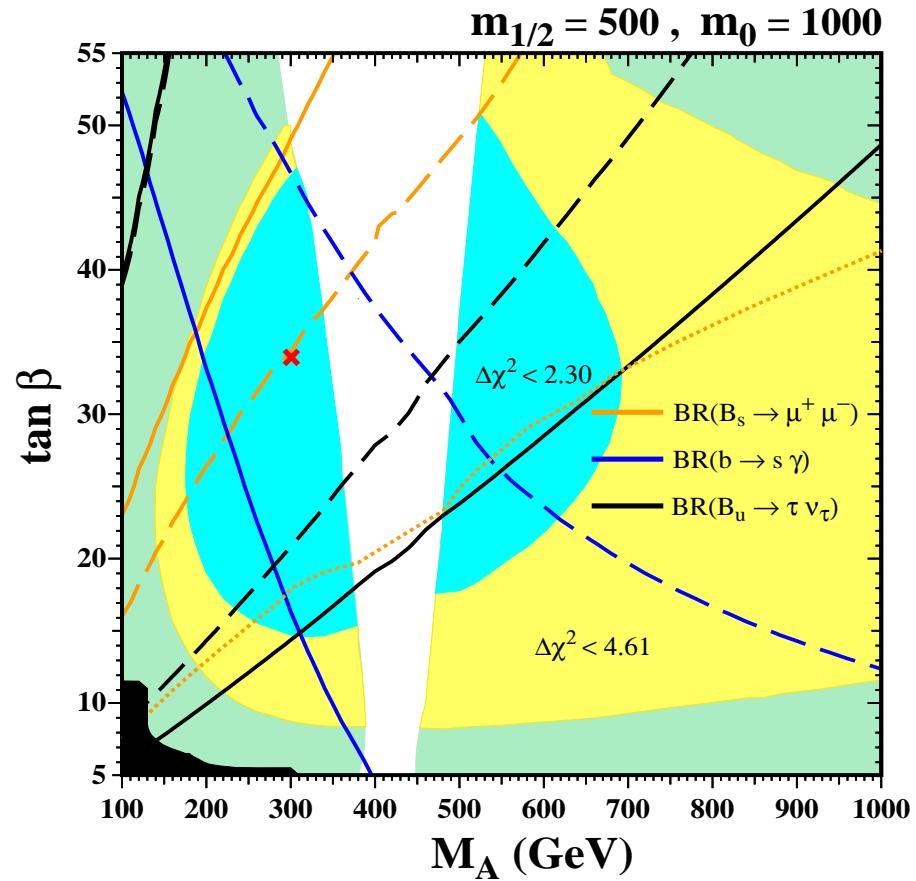


$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) = 1.0(0.2) \times 10^{-7} [, \text{ LHCb}]$$

$$\text{BR}(b \rightarrow s \gamma) = 4.0(3.0) \times 10^{-4}$$

$$\text{BR}(B_u \rightarrow \tau \nu_\tau) = 0.9(0.7)$$

Future prospects:



⇒ Improvement in precision for BPO is needed!
Improvement in precision for BPO will help a lot!

5. Conclusions

- EWPO and BPO and CDM can give valuable information on the underlying Lagrangian
- Combination makes only sense in GUT based models
- CMSSM: (free parameters: $m_{1/2}$, m_0 , A_0 , $\tan \beta$)
 - slight tension between EWPO and BPO
BPO not yet precise enough . . .
 - EWPO fit for M_h similar to “blue band” in the SM,
but including $\text{BR}(b \rightarrow s\gamma)$, $(g - 2)_\mu$ and CDM:
 $\Rightarrow M_h = 110^{+8}_{-10} \pm 3 \text{ GeV}$
 \Rightarrow impact of BPO still small
- NUHM: (effectively M_A and μ as additional free parameters)
 - M_A – $\tan \beta$ planes in agreement with CDM possible
 - impact of BPO so far “mild”
 - good future prospects , especially for LHCb