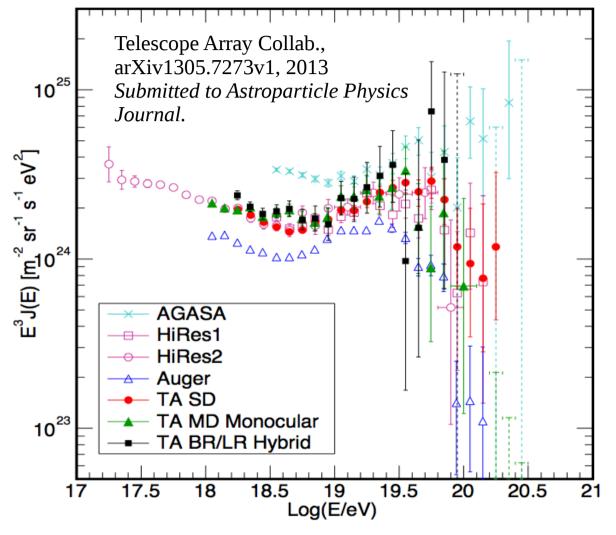
Time-Domain Waveform Studies for ARIANNA



Outline

- How we plan to detect high-energy neutrinos via the Askaryan effect
- Conversion of analytical electric fields to voltage waveforms in ARIANNA DAQ (LTI systems)
- Anechoic Chamber measurements performed at the University of Kansas
 - Experimental Setups (4)
 - Types of data taken (scalar versus frequency, time-domain waveforms)
- Calculation of effective height operator of the signal antenna
 - The best-fit effective height operator
 - Including the AC-coupled low-noise amplifier (LNA)
 - Checking off-axis
- Deriving template waveform induced by neutrino interaction in ice
- Future work

High Energy Cosmic Ray Spectral Cutoff (GZK effect)



$$p_{CR}^{+} + \gamma_{CMB} \rightarrow \Delta^{+} \rightarrow p^{+} + \pi^{0} \rightarrow p^{+} + 2\gamma$$

$$p_{CR}^{+} + \gamma_{2.7K} \rightarrow \Delta^{+} \rightarrow n^{0} + \pi^{+} \rightarrow n^{0} + \mu^{+} + \nu_{\mu} \rightarrow n^{0} + e^{+} + \nu_{e} + \nu_{\mu} + \overline{\nu_{\mu}}$$

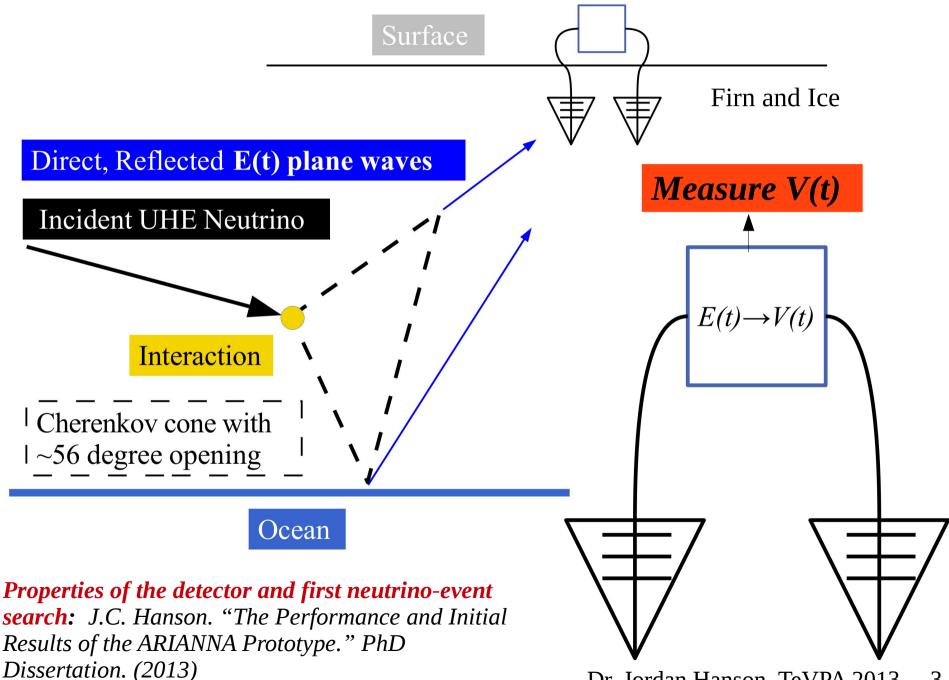
Nucleon-photon threshold effect which produces secondary particles, including neutrinos

What is the precise origin of these particles?

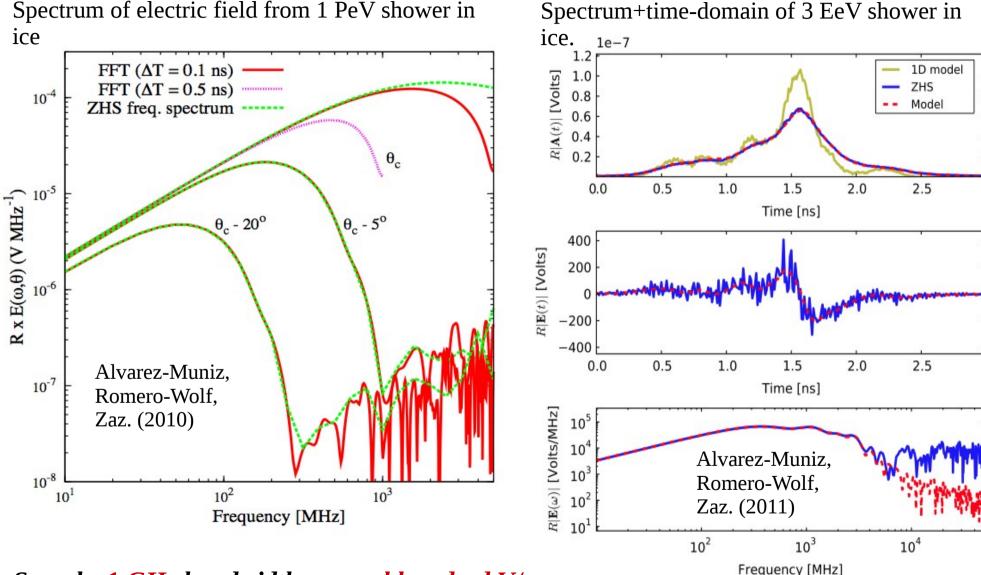
How heavy are they (are they mostly protons, or heavier)?

How does a neutrino interact with matter at COM energy of 100 TeV?

Statement of the Problem

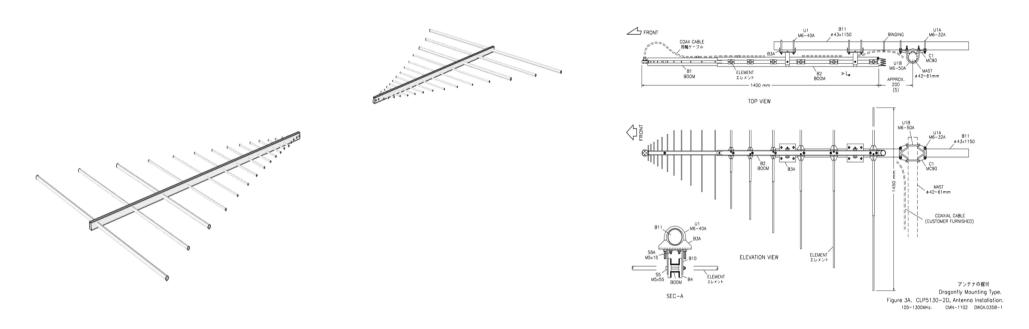


Statement of the Problem, II: the signal to detect



Search: 1 GHz bandwidth, several hundred V/m electric field pulse traveling ~ 1 km through ice

The signal antenna: Log-Periodic Dipole Array



Example of a *frequency-independent* antenna (bandwidth of 100-1300 MHz)

Radiation pattern is maximal in direction of **bore-sight**. The **bore-sight** configuration (shown above) optimizes reception.

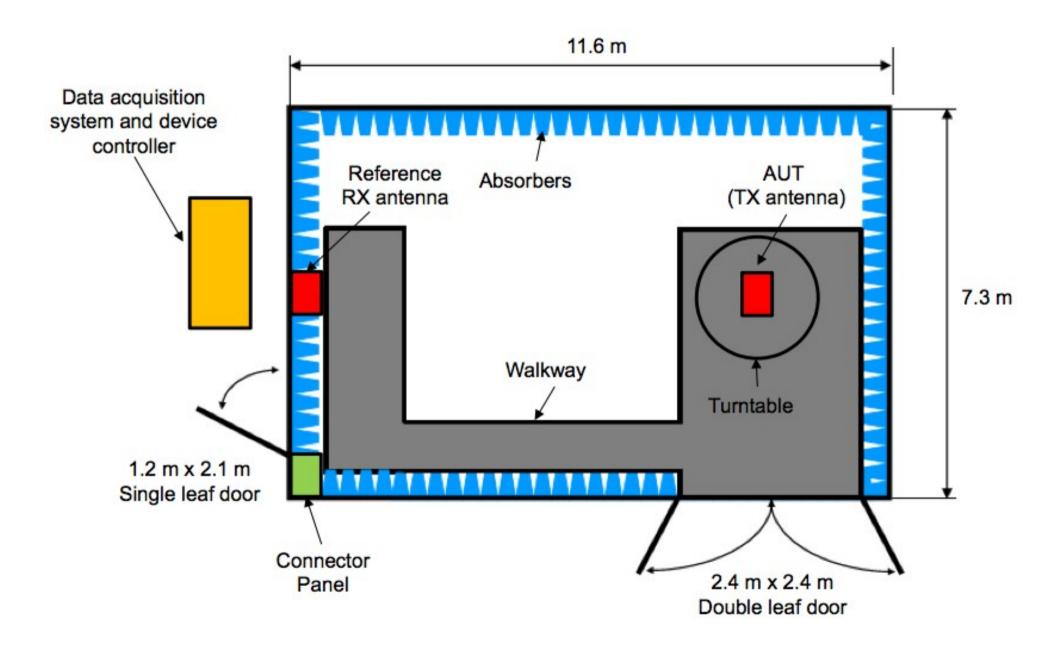
Linearly polarized. The E-plane is the plane containing the dipole elements, the H-plane is perpendicular to E-plane, containing only the **spine** of the antenna

Linear Time-Invariant System

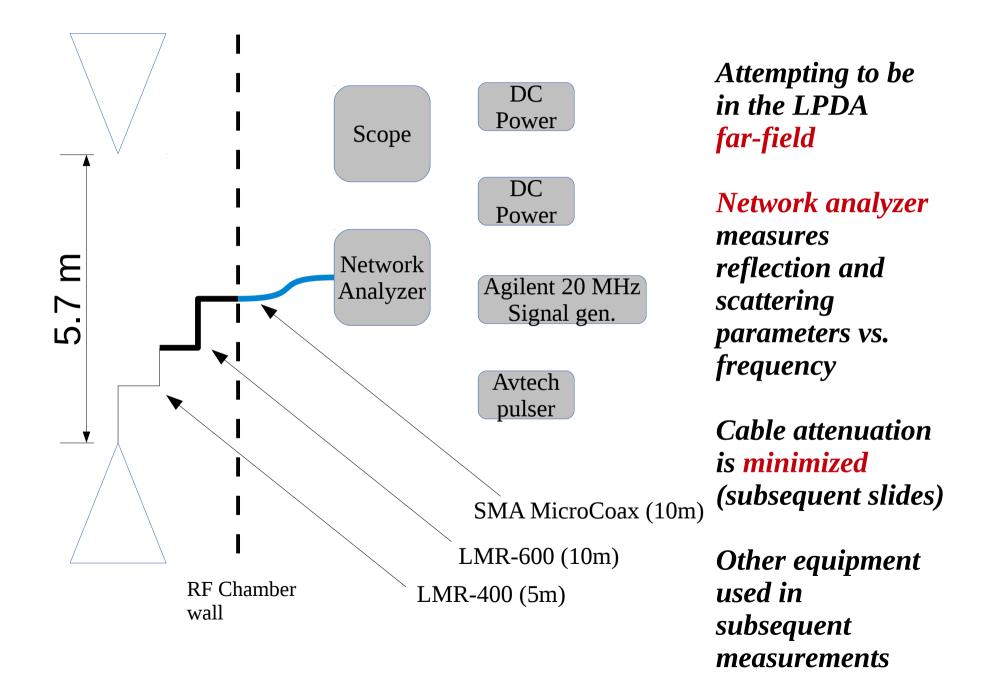
- Two property system with single input x(t), single output y(t)
 - Linearity: $ax_1(t)+bx_2(t) = ay(t)+by(t)$
 - Time-invariance: ax(t-T) = ay(t-T)
 - The convolution integral with kernel r satisfies these two criteria
- Convolution: $y(t) = \int_{-\infty} r(\tau) x(t-\tau) d\tau$
- Specifically, for antennas, let y(t) = V(t), the time-dependent voltage. Taking r = h(t), the effective height, we have:

$$V(t) = \int_{-\infty}^{\infty} \vec{h}(\tau) \cdot \vec{E}(t - \tau) d\tau$$

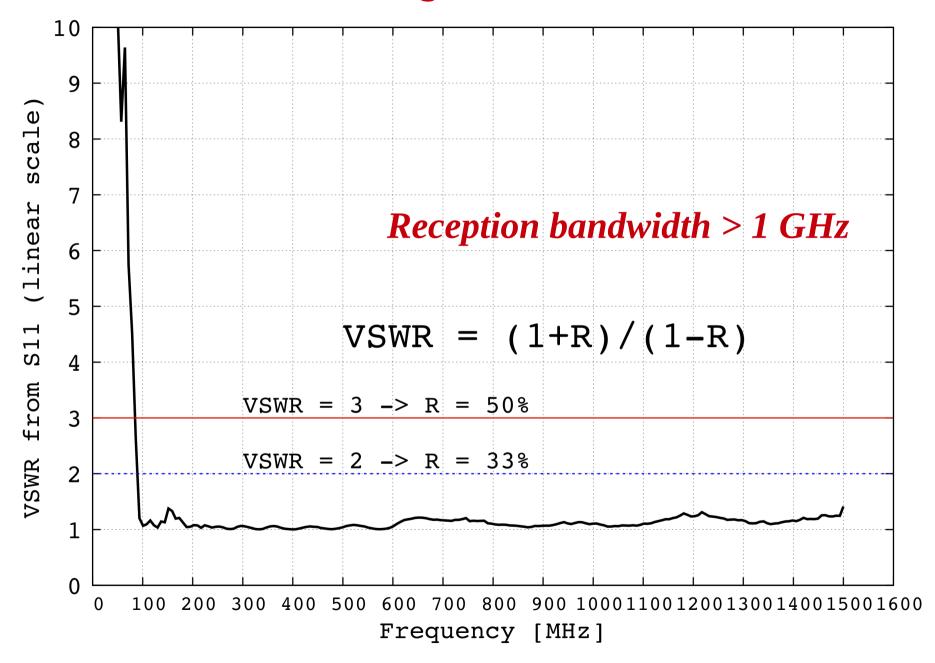
Experimental Setup: The Anechoic Chamber



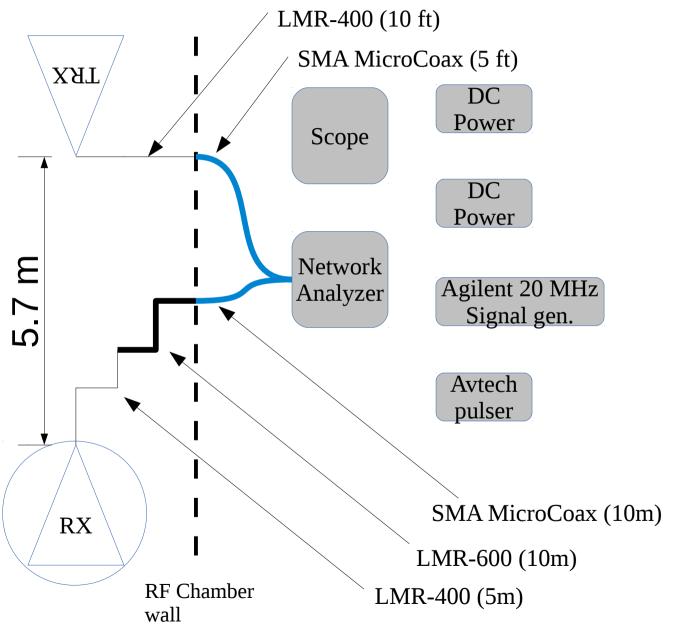
Experimental Setup: scalar LPDA properties (*e.g.* bandwidth)



Main Result #1: Checking the SWR



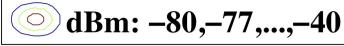
Experimental Setup: 3D radiation pattern, gain

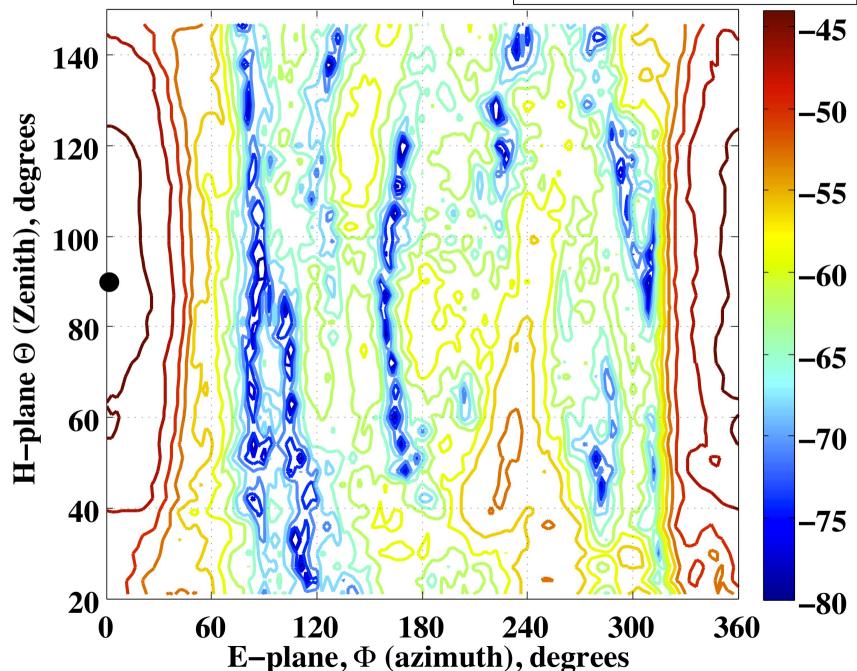


Measured the full radiation pattern vs. frequency, azimuth, and zenith angles.

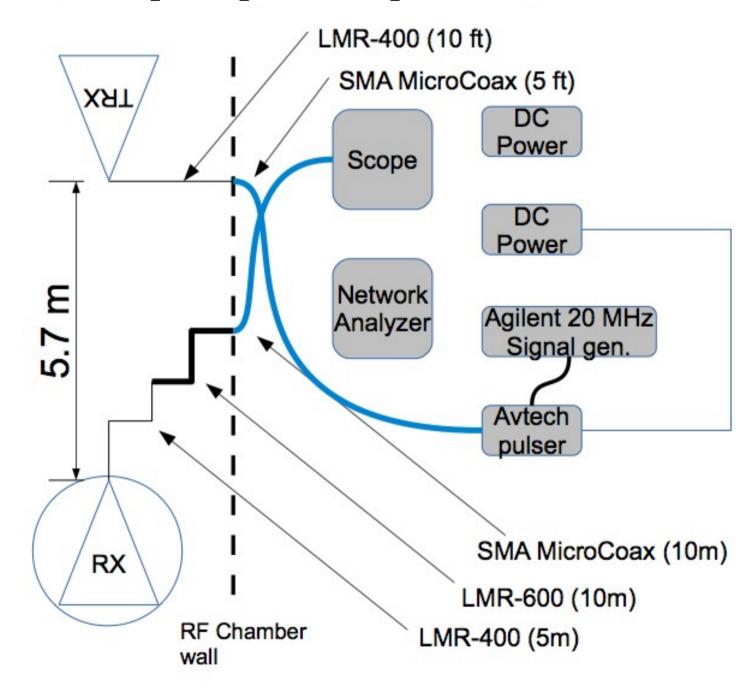
Achieved 73% coverage of the unit sphere (limited in zenith angle by the mounting stock in the chamber)

Freq: 1 GHz. Black dot: boresight.





Experimental Setup: impulse response



Derivation of effective height using this experimental setup:

r = antenna separation,

c = light speed,

 V_{L} = antenna voltage delivered to load,

 Z_{T} = load resistance (and coaxial line resistance, 50 Ohms),

 Z_{in} = antenna input resistance (~50 Ohms),

 Z_0 = impedance of free space (120 π Ohms) (c.)

(c.f. P. Miocinonic, 2006)

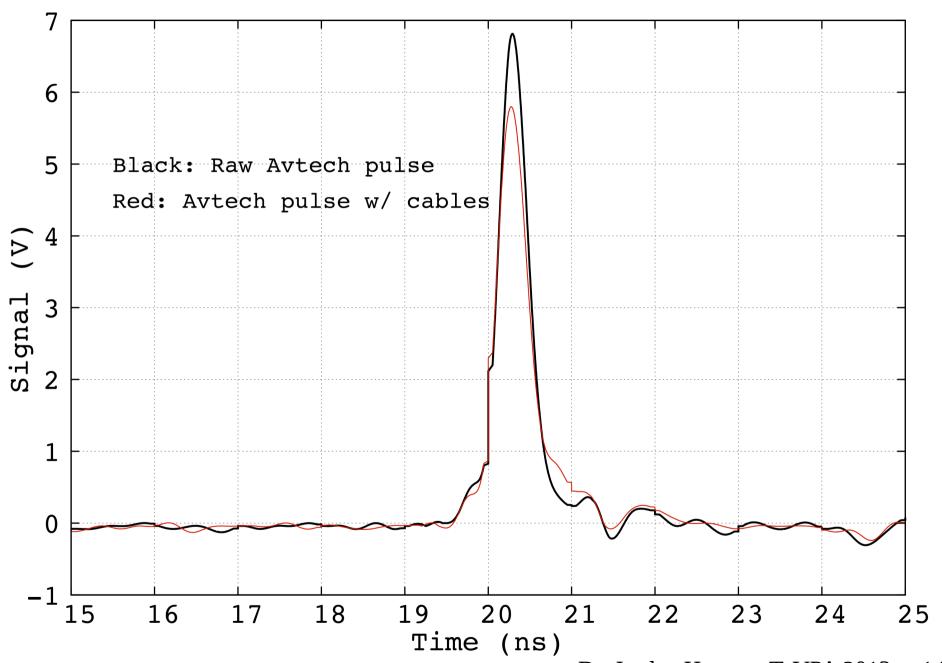
$$V_{L}(t) = 2 \left(\frac{Z_{L}}{Z_{L} + Z_{in}} \right) \vec{h}_{rx}(t) \circ \vec{E}(t)$$

$$\vec{E}(t) = \frac{2}{4\pi r c} \left(\frac{Z_{\text{in}}}{Z_{\text{in}} + Z_L} \right) \frac{Z_0}{Z_{\text{in}}} \vec{h}_{tx} \circ V_{\text{src}}(t)$$

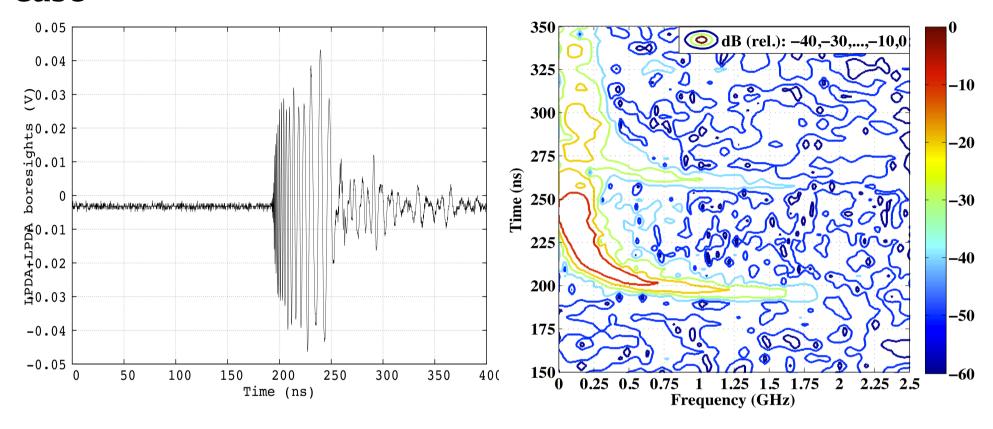
$$V_L(t) = \frac{1}{(2\pi rc)} \frac{Z_0}{Z_L} \vec{h}_{rx}(t) \circ \vec{h}_{rx}(t) \circ \partial_t V_{src}(t) \qquad (\vec{h}_{tx} = -2 \partial_t \vec{h}_{rx}(t))$$

Avtech (pulser) signal

Reception bandwidth > 1 GHz



Time-domain Results: raw, bore-sight case



Left: Bore-sight signal data.

Right: Spectrogram of the data on the left; magnitude of the short-time Fourier transform in dB (color scale).

Method for Obtaining $h_{rx}(t)$

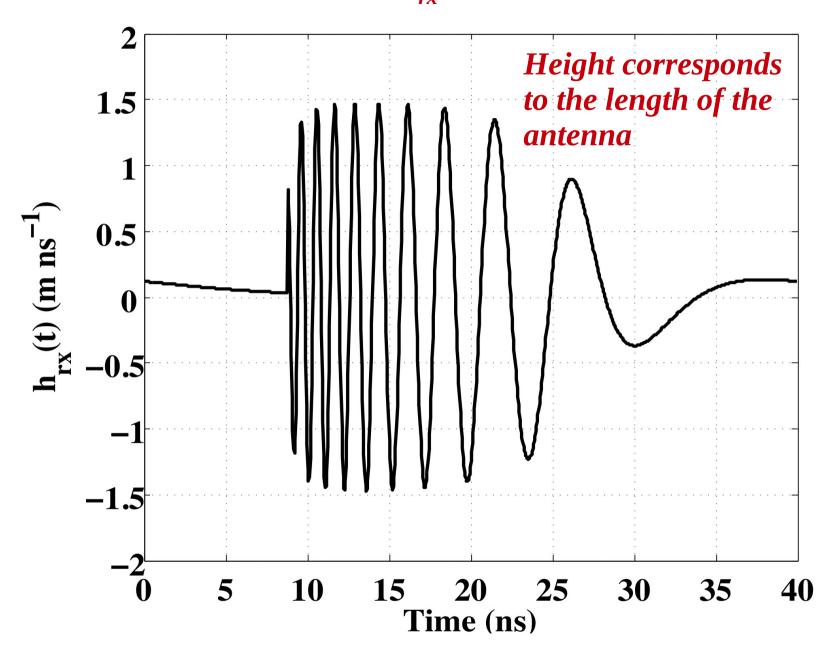
- Rotating to Fourier domain and back amplifies noise
- Assume a trial function with parameters, a(t) chosen to turn on/off the function
- Perform a fit that minimizes R after scanning the full parameter space

$$h_{rx}(t) = Aa(t)\cos(2\pi k \ln(t/t_{end}))$$

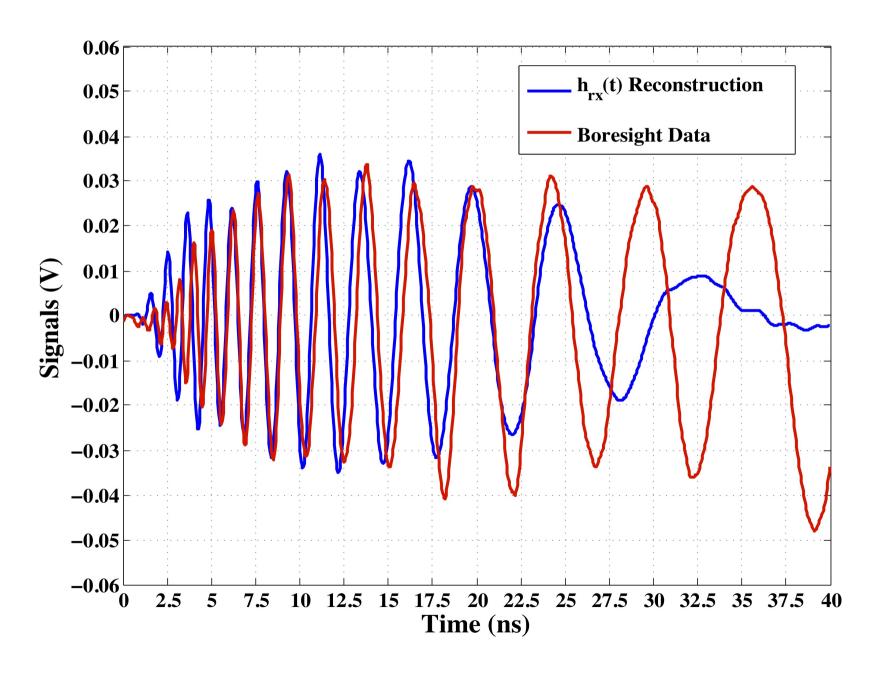
$$a(t) = (2/\pi)^{2} \tan^{-1}(t/t_{0}) \tan^{-1}(-(t-t_{end})/t_{1})$$

$$R = \frac{1}{N} \sum_{i}^{N} (f_{data}(t_{i}) - f_{model}(t_{i}))^{2}$$

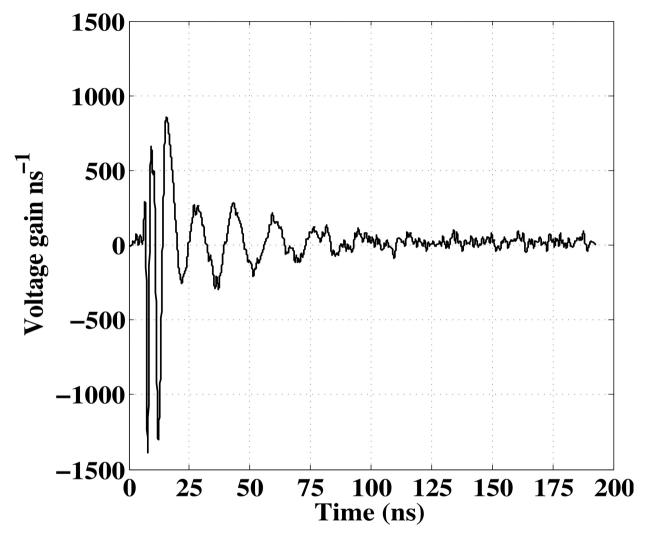
Main Result #3: Bore-sight $h_{rx}(t)$



Main Result #3: Bore-sight $h_{rx}(t)$



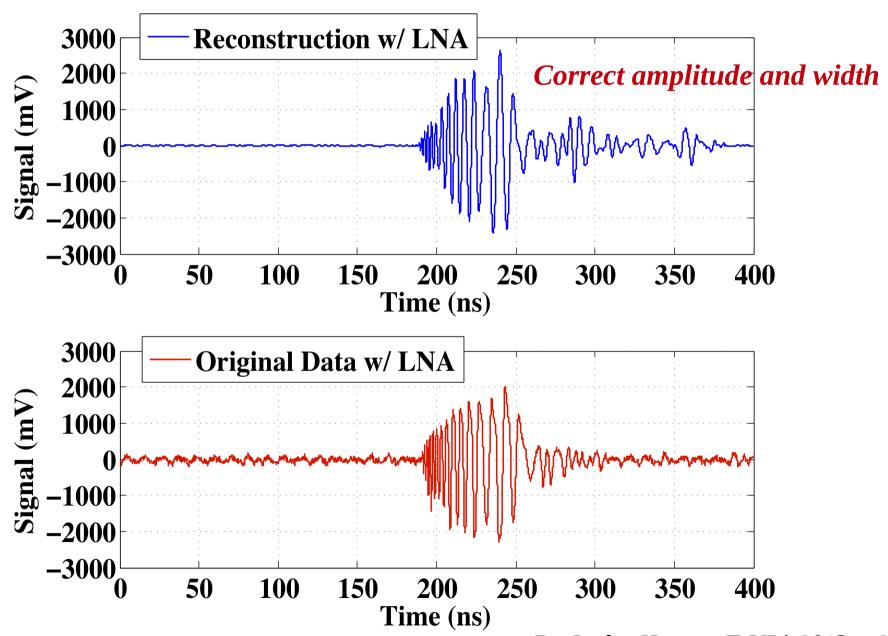
Main Result #4: Bore-sight h_{rx}(t) w/ Amplifier



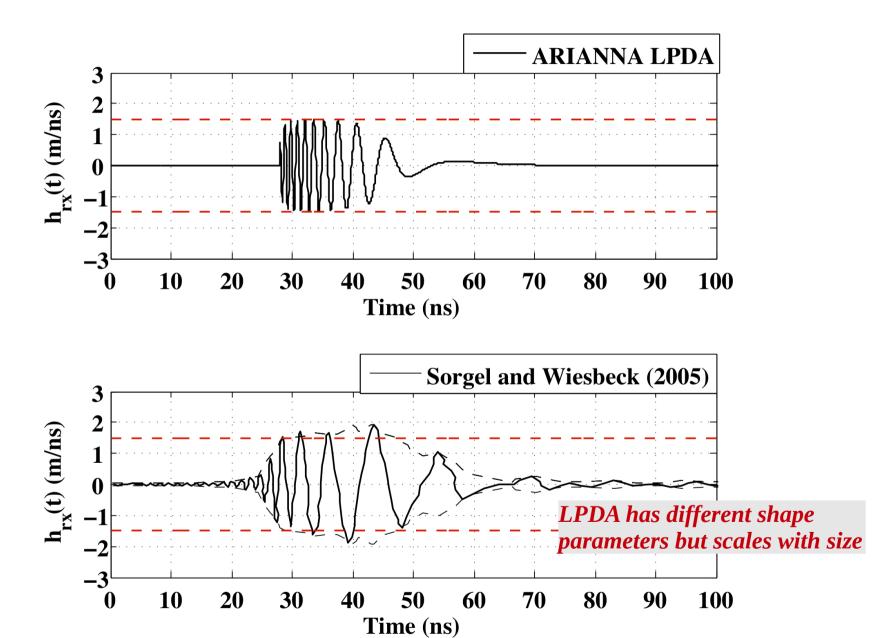
Credit: James Walker and Steve Barwick, UCI

$$V_L(t) = \frac{1}{(2\pi r c)} \frac{Z_0}{Z_L} H_{amp}(t) \circ \vec{h}_{rx}(t) \circ \vec{h}_{rx}(t) \circ \partial_t V_{src}(t)$$

Main Result #4: Bore-sight h_{rx}(t) w/ Amplifier

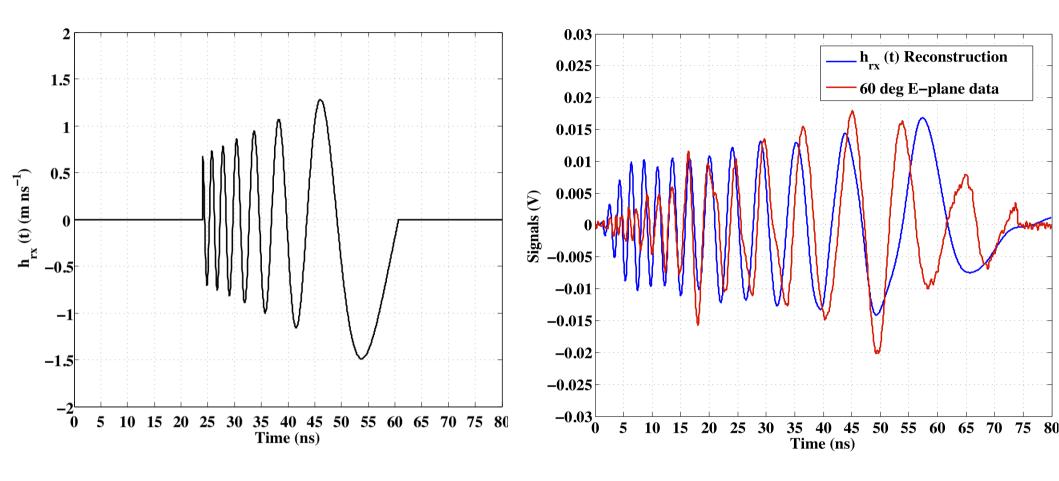


Comparing Effective Height to Others' Results



Note: data from this reference has been scaled to match LPDA sizes.

Checking off-axis: 60 degrees in E-plane



Effective height: Similar height at late times and lower frequencies, but frequency modes above 600 MHz are missing (early times).

Reconstruction: Early times (500-600 MHz) are large, but excellent match after 15 ns. The overall signal is much longer.

Dr. Jordan Hanson, TeVPA 2013

Interactions with Askaryan Electric Fields, Comparisons with Monte Carlo simulation

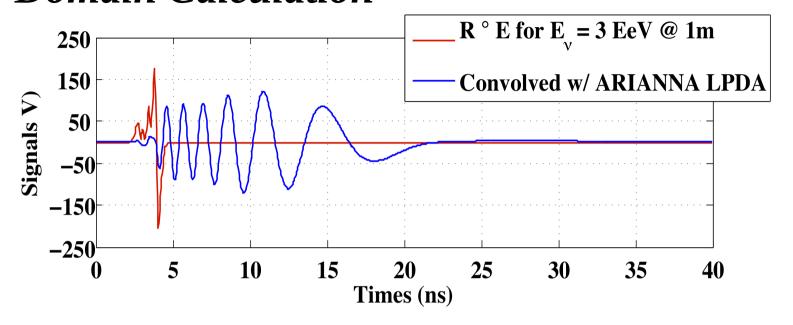
- Electric field strength typically parameterized from data, with respect to energy and frequency (Saltzberg et al., 2000), (Alvarez-Munis et al., 2010)
- Observed strength depends on viewing-angle with respect to Cherenkov angle
- Propagation and attenuation (lambda = attenuation length)
- Signal voltage depends on viewing angle of the antenna

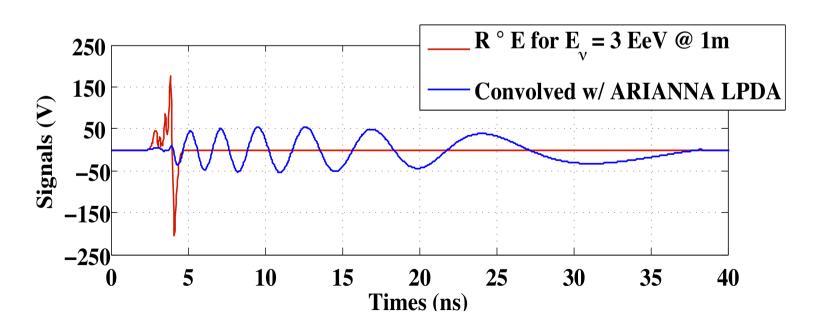
$$E_{1m} = \frac{2.53 \times 10^{-7} E_{v} [TeV] (v/v_{0})}{1 + (v/v_{0})^{1.44}} (V m^{-1} MHz^{-1})$$

$$E_{1m}(\theta_{v}) = E_{1m} \frac{\sin(\theta_{v})}{\sin(\theta_{c})} \exp\left[-\ln 2((\theta_{v} - \theta_{c})/\Delta \theta)^{2}\right] (V m^{-1} MHz^{-1})$$

$$V_{\text{LPDA}} = P(\theta_{v}) \frac{\Delta v}{\sqrt{2}} \frac{\sin \theta_{v}}{\sin \theta_{c}} \exp \frac{-r/\lambda}{r} \sum_{i} E_{1\text{m}}(\theta_{v}) h_{\text{eff}}(v_{i})$$

Main Result #5: Comparing Monte Carlo with Time-Domain Calculation





Conclusion

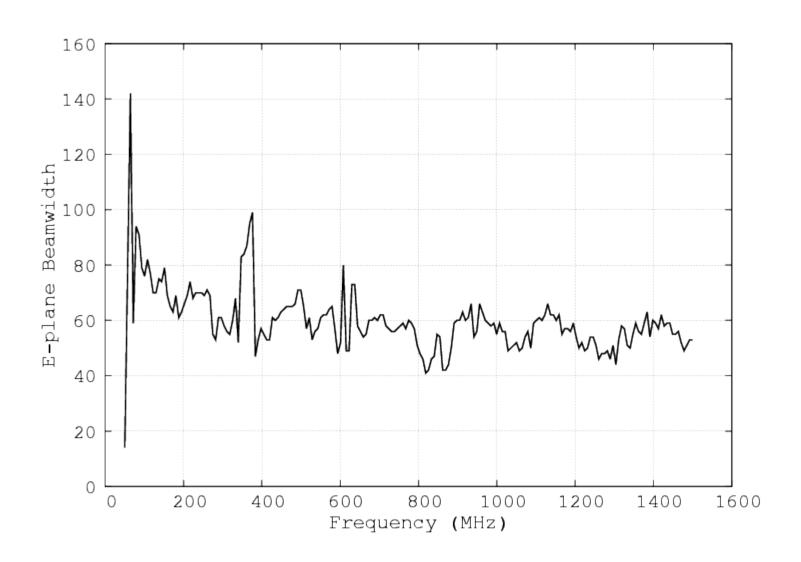
- Discussed UHE neutrinos, the Askaryan Effect
- Mathematics of converting electric field waveform to voltage waveform
- Measured antenna properties, including conversion from E-field to voltage waveform
- Demonstrated angular monte carlo agreement, and computed neutrino waveforms entering ARIANNA DAQ.
- Future work: must span the angular space to generalize the fits, improve high-frequency agreement

References

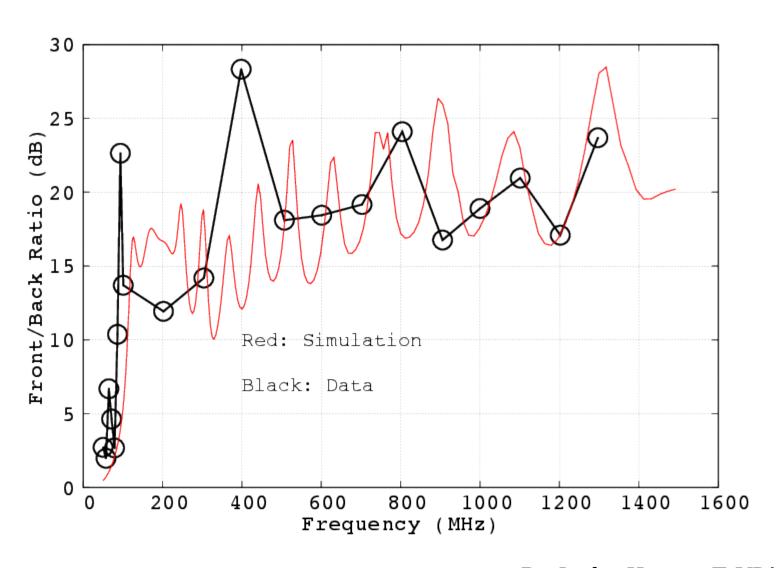
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E-Plane beam-width ~ 60 degrees



Front-Back Ratio ~ -15 dB



Gain vs. Frequency

