

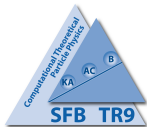
# Electroweak effects in vector-boson pair production at the LHC

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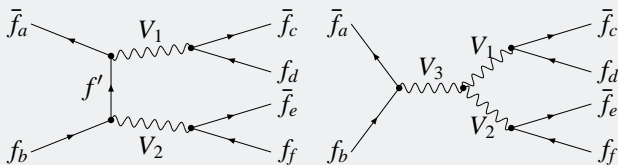
13–15 May 2013, LoopFest XII, Tallahassee, Florida



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- 2 NLO EW Corrections and Leptonic decays
- 3 HERWIG++ Monte Carlo Implementation
- 4 Separation of QED
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# Introduction – Weak-Boson Pair Production at the LHC

Vector-boson pair production:  $pp \rightarrow WW/ZZ/WZ \rightarrow 4l$



- $ZZ/WW/\gamma\gamma$  production important **irreducible background** to inclusive SM Higgs-boson production
- Probe **non-abelian structure** of the Standard Model (SM) at high energies
- Search for **anomalous couplings**
- Backgrounds to **new-physics searches**, i.e. leptons +  $\cancel{E}_T$  signatures  
→ SUSY-particle pair production

## High-energy limit

$$s, |t|, |u| \gg M_V^2, \quad V = W, Z$$

→ **bosons have to be produced at large  $p_T$**

- EW corrections at high energies dominated by **universal large logarithms**

$$\propto \alpha^L \ln^{2L}(M_V/\sqrt{s}) \quad (\text{LL}),$$

$$\propto \alpha^L \ln^{2L-1}(M_V/\sqrt{s}) \quad (\text{NLL}), \dots$$

at the  $L$ -loop level

- **Corrections of  $\sim -40\%$  at  $p_T = 500 \text{ GeV}$  (Z-pair production)**
- **Change of sign** going from LL to NLL (to NNLL ...)
- **substantial cancellations possible!**

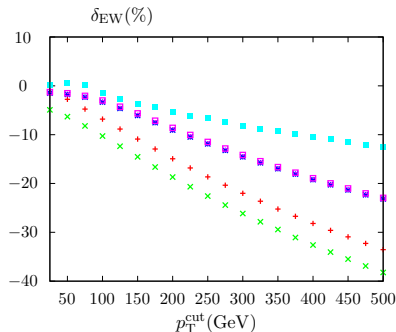
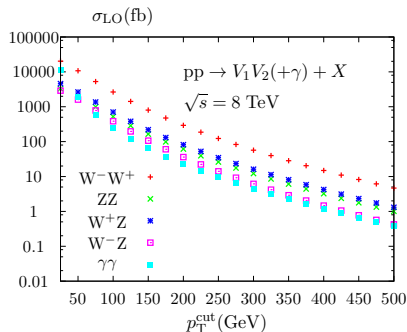
- Only consider **on-shell** vector bosons  $\oplus$  include all **mass effects**
- Include **leptonic decays**  $\rightarrow$  **physical final states phenomenologically accessible**

## Setup

- **Renormalization:**  
On-shell scheme ( $G_\mu$ ,  $M_W$ ,  $M_Z$ ) to obtain UV finite
- **Virtual corrections:**  
IR divergent (regularized by  $m_\gamma$ ,  $m_q$ ), compensated by
- **Real radiation:**  
remaining collinear singularities to be absorbed in PDFs
- **Practical implementation:**  
use MSTW2008LO PDFs [Martin et al. 2009]  
(impact of QED and factorization scheme small, in general sub-percent)

# Numerical Results for $WW/WZ/ZZ/\gamma\gamma$ Production

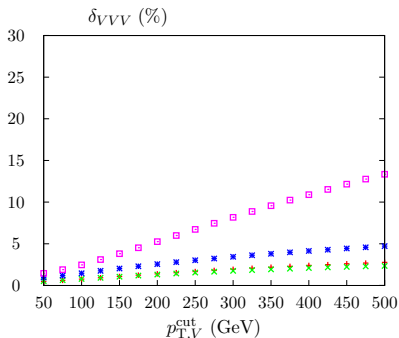
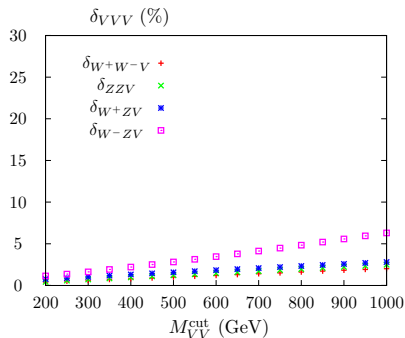
**LHC at 8 TeV, default cuts:**  $p_{T,V} > 15$  GeV,  $|y_V| < 2.5$



- **LO:** Drastically decreasing cross sections for large  $p_T$
- **NLO:**
  - Full result, i.e. virtual, soft, hard, and collinear photons included
  - all mass effects included
  - corrections largest for  $ZZ$ , smallest for  $\gamma\gamma$
- results published in [arXiv:1208.3147](https://arxiv.org/abs/1208.3147), [arXiv:1208.3404](https://arxiv.org/abs/1208.3404)

# Numerical Results (II)– “Real Radiation” of W/Z

**LHC at 8 TeV, default cuts:**  $p_{T,V} > 15$  GeV,  $|y_V| < 2.5$



- corrections **below 5%** even for large transverse momenta and invariant masses
- corrections to  $W^-Z$  production enhanced due to  $W^-ZW^+$  final states (PDFs!)
- could easily be implemented in MC studies

## Purely weak corrections well defined in ZZ production

→ contributions of QED in general below 1%

- compute **purely weak corrections** to  $pp \rightarrow (Z/\gamma^*)(Z/\gamma^*) \rightarrow e^+e^-\mu^+\mu^-$
- **LO: full calculation**, non-resonant and off-shell effects included.
  - naive fixed-width scheme
  - Complex-Mass Scheme (CMS) [Denner, Dittmaier, Roth, Wieders 2005]
- **NLO: Two different approaches**, including full spin correlations
  - **Double-Pole Approximation (DPA)**: only doubly resonant contributions included, finite width taken into account  
(On-shell projection, **caveat**: non-factorizable corrections neglected)
  - **Narrow-Width Approximation (NWA)**: particles strictly on shell

$$\frac{1}{(Q^2 - M^2)^2 + M^2\Gamma^2} \rightarrow \frac{\pi}{M\Gamma} \delta(Q^2 - M^2),$$

valid if  $\Gamma/M \rightarrow 0$ .



# Numerical Results: $pp \rightarrow ZZ \rightarrow e^+e^-\mu^+\mu^-$

$pp \rightarrow (Z/\gamma^*)(Z/\gamma^*) + X \rightarrow e^+e^-\mu^+\mu^- + X,  \Delta y_{ZZ}  < 3$					
$M_{\text{inv}}^{\text{cut}}(4l)/\text{GeV}$	$\sigma_{\text{LO}}^{\text{naive}}/\text{pb}$	$\sigma_{\text{LO}}^{\text{CMS}}/\text{pb}$	$\sigma_{\text{LO}}^{\text{DPA}}/\text{pb}$	$\sigma_{\text{LO}}^{\text{NWA}}/\text{pb}$	$\delta_{\text{weak}}^{\text{DPA}}/\%$
LHC14					
500	$0.326 \times 10^{-3}$	$0.326 \times 10^{-3}$	$0.319 \times 10^{-3}$	$0.343 \times 10^{-3}$	-15.9
600	$0.168 \times 10^{-3}$	$0.168 \times 10^{-3}$	$0.164 \times 10^{-3}$	$0.177 \times 10^{-3}$	-19.3
700	$0.962 \times 10^{-4}$	$0.962 \times 10^{-4}$	$0.941 \times 10^{-4}$	$1.017 \times 10^{-4}$	-22.3
800	$0.587 \times 10^{-4}$	$0.587 \times 10^{-4}$	$0.575 \times 10^{-4}$	$0.621 \times 10^{-4}$	-24.9
900	$0.374 \times 10^{-4}$	$0.374 \times 10^{-4}$	$0.367 \times 10^{-4}$	$0.397 \times 10^{-4}$	-27.4
1000	$0.247 \times 10^{-4}$	$0.247 \times 10^{-4}$	$0.242 \times 10^{-4}$	$0.262 \times 10^{-4}$	-29.7

## LHC14, standard leptonic cuts

- **LO:** DPA works well, NWA: discrepancy of 5–10%
  - **NLO:** Good agreement ( $\sim 1\%$ ) with  $K$ -factors obtained in Sudakov approximation [Accomando, Denner, Kaiser 2004]
- QED contributions (real-photon radiation, photon-loops, non-factorizable contributions, corrections to Z-boson decay) **only at the 1% level**

**Conclusion:** weak  $K$ -factors of hard process sufficient to describe resonant 4-lepton production at reasonable accuracy

## Our strategy

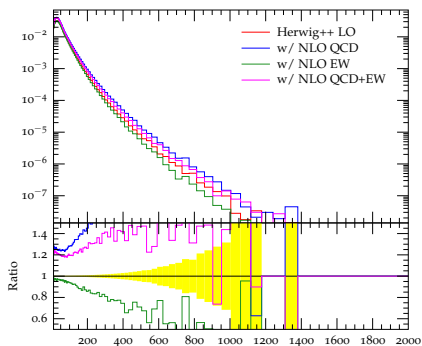
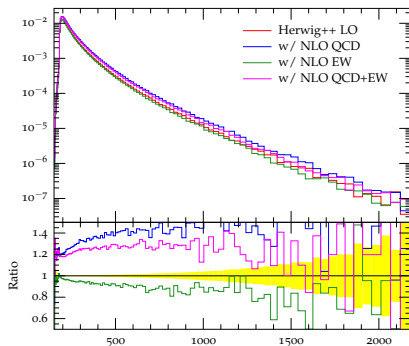
Factorization of EW and QCD corrections:

$$d\sigma_{\text{QCD}\times\text{EW}} = K_{\text{weak}}(\hat{s}, \hat{t}) \times d\sigma_{\text{QCD}}$$

$\sigma_{\text{QCD}}$ : best prediction available for QCD-corrected cross section

- **Assumption:** bulk of EW effects properly described by weak corrections to  $2 \rightarrow 2$  process  $K_{\text{weak}}(\hat{s}, \hat{t})$ .
- **FSR included** in YFS formalism (SOPHTY) [Hamilton, Richardson 2006] (only dressed leptons)
- $K_{\text{weak}}(\hat{s}, \hat{t})$  computed once and for all, data provided as grid files.
- **Some caveats:**
  - factorization assumption only sensible **without additional hard jets**;  
→ EW corrections to ZZ+jet have to be included.
  - Ansatz **does not include** corrections to non-resonant or off-shell contributions

## Simulation for $pp \rightarrow ZZ \rightarrow e^+e^-\mu^+\mu^- + X$ at 8 TeV, $M_{ZZ}$ and $p_{T,Z}$ distributions



- **Standard Herwig++ setup used** (v2.6.2, with simple add-on for EW corrections, 10M events), ZZ at NLO QCD matched with parton showers, hadronization included, underlying event switched off
- **huge QCD corrections at large  $p_{T,Z}$** , factorized ansatz not justified  
 → jet veto, restriction on  $p_{T,ZZ}$

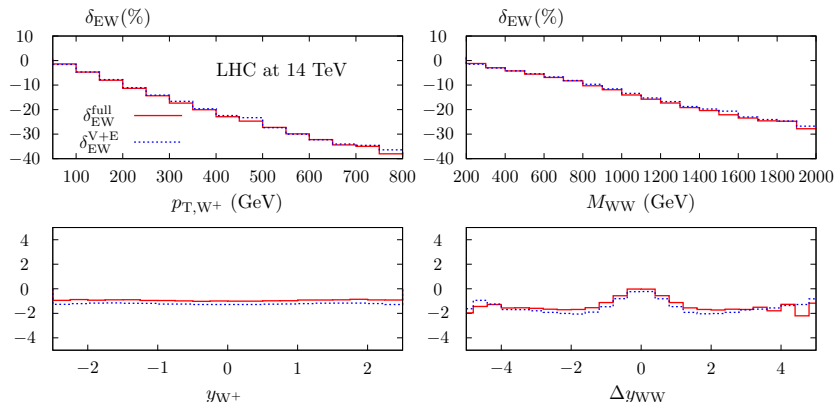
## Problem:

- In WW and WZ production **no gauge-invariant separation** of dominant weak corrections and QED possible
- QED contributions inevitably lead to **IR singularities**
- **Real radiation** has to be included:  
numerical integration has to deal with singular integrands, check cancellation of divergences, check that slicing cuts drop out, . . .
- Finally, QED effects at the level of 1% ( $\alpha/\pi$ ).

## Possible solution:

- **V + E approximation**: Endpoint from subtraction contributions  $\oplus$  virtual corrections gives IR finite result [Dittmaier 1999]
- completely avoid computation of real photon radiation

## On-shell W-Pair production at LHC14, default cuts

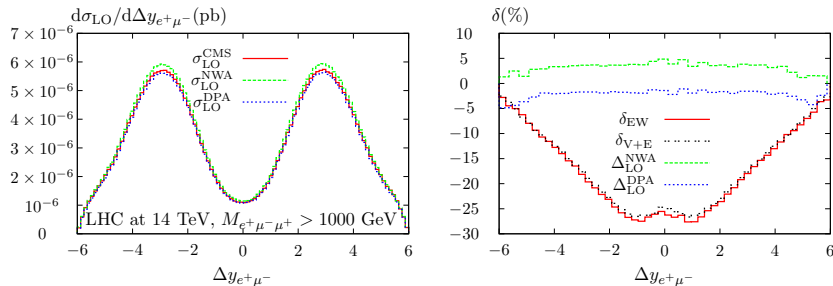


- fantastic approximation of full result (better than 1% in WW, WZ production)
- Approximation works well at high  $p_T$ , high invariant masses and near threshold.
- NNLO EW corrections at the level of 5–10% at high  $p_T$  [Kühn, Metzler, Penin, Uccirati 2011]

**Conclusion:** Corresponding  $K$ -factor should be used for MC implementation.

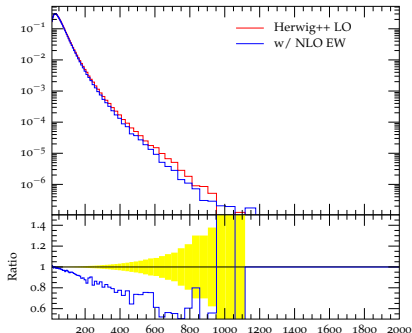
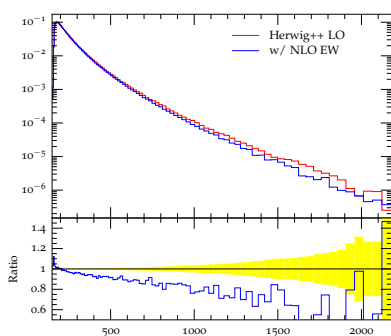
# 4-Lepton Production – Test of our Approach

$pp \rightarrow (W^+ \rightarrow) e^+ \nu_e (Z \rightarrow) \mu^- \mu^+$  at LHC14, standard event-selection cuts  
(Preliminary results!)



- **LO:** **NWA** and **DPA** work at the level of  $\pm 5\%$
  - **NLO:**
    - $\delta_{EW}$ : Full NLO EW corrections to production process in NWA, spin correlations for decay process included
    - $\delta_{V+E}$ : LO in NWA multiplied with  $K_{EW}(\hat{s}, \hat{t})$  (unpolarized  $K$ -factor used!)
- **Good agreement** at the 1% level for relative corrections
- Spin correlations well reproduced!

**Simulation for  $pp \rightarrow (W^+ \rightarrow)e^+\nu_e (W^- \rightarrow)\mu^-\bar{\nu}_\mu + X$  at 8 TeV,  
 $M_{WW}$  and  $p_{T,W}$  distributions**



- Standard Herwig++ setup used (v2.6.2, with simple add-on for EW corrections, 10M events), ZZ at LO QCD  $\oplus$  parton shower, hadronization included, underlying event switched off
- V+E approximate results consistent with [arXiv:1208.3147](https://arxiv.org/abs/1208.3147)

- We have computed the **full NLO EW corrections** to vector-boson pair production at the LHC, including all mass effects [arXiv:1208.3147, arXiv:1208.3404]
- **Leptonic decays** have been implemented for ZZ, WZ production, including **spin correlations**
- effect of **real W/Z radiation** in general below 5%
- We have proposed a **straight-forward MC implementation** in the HERWIG++ setup, relying on  $2 \rightarrow 2$  *K*-factors.
  - **Claim:** predictions match the “true” NLO EW result at the level of a few %.
  - QCD uncertainties (PDFs, hadronization, missing higher orders, . . .) presumably much larger
  - Approach could easily be applied to  $V$ +jet,  $t\bar{t}$  production in the future.

Thank you!

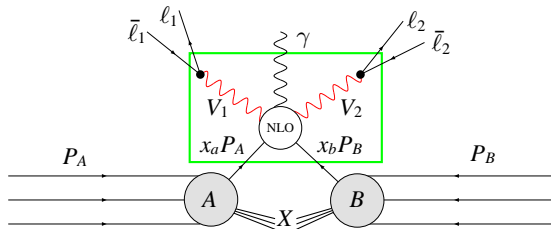


# Reminder: Calculation of Hadronic Cross Sections

## Schematic illustration for

$$pp \rightarrow V_1 V_2 (+\gamma) + X$$

$$\rightarrow \ell_1 \ell_2 \bar{\ell}_1 \bar{\ell}_2 (+\gamma) + X$$



## Hadronic cross sections

$$d\sigma_{AB}(p_A, p_B) = \sum_{a,b} |s|s|s|s| \int_0^1 dx_a \int_0^1 dx_b f_{a/A}(x_a, \mu_F) f_{b/B}(x_b, \mu_F) d\hat{\sigma}_{ab}^{\text{NLO}}(p_a, p_b, \mu_F, \mu_R) \\ \times \mathcal{F}^{(4\ell+\gamma)}(\{\mathcal{O}_{\text{FS}}\}), \quad P_{\{a,b\}}^\mu = x_{\{a,b\}} P_{\{A,B\}}^\mu$$

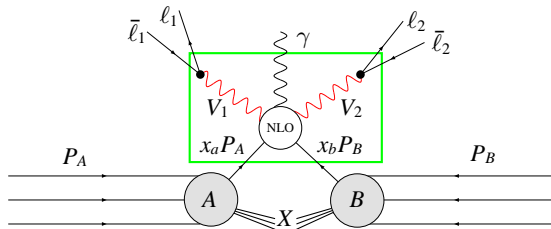
- Dependence on  $\mu_R$ ,  $\mu_F$  reduced by inclusion of higher perturbative orders
- $\mathcal{F}^{(4\ell+\gamma)}$  incorporates definition of observables + phase-space cuts

# Reminder: Calculation of Hadronic Cross Sections

## Schematic illustration for

$$pp \rightarrow V_1 V_2 (+\gamma) + X$$

$$\rightarrow \ell_1 \ell_2 \bar{\ell}_1 \bar{\ell}_2 (+\gamma) + X$$



## Hadronic cross sections

$$d\sigma_{AB}(p_A, p_B) = \sum_{a,b} l_s l_{s'} l_s l_{s'} \int_0^1 dx_a \int_0^1 dx_b f_{a/A}(x_a, \mu_F) f_{b/B}(x_b, \mu_F) d\hat{\sigma}_{ab}^{\text{NLO}}(p_a, p_b, \mu_F, \mu_R)$$

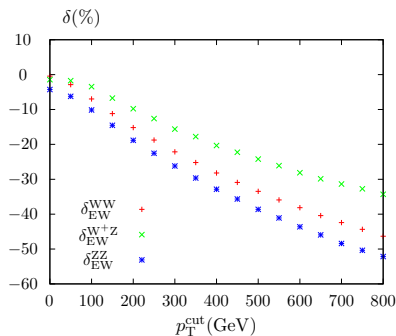
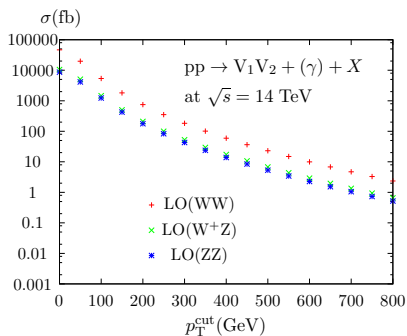
$$\times \mathcal{F}^{(4\ell+\gamma)}(\{\mathcal{O}_{\text{FS}}\}), \quad P_{\{a,b\}}^\mu = x_{\{a,b\}} P_{\{A,B\}}^\mu$$

### NLO partonic cross section:

$$\hat{\sigma}_{ab}^{\text{NLO}} = \hat{\sigma}_{ab}^{\text{LO}} + \hat{\sigma}_{ab}^{\text{virt}} + \hat{\sigma}_{ab}^{\text{real}}$$

# Numerical Results for $WW/WZ/ZZ/\gamma\gamma$ Production

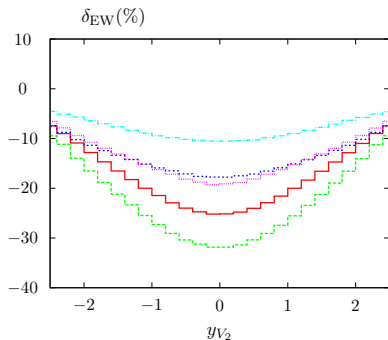
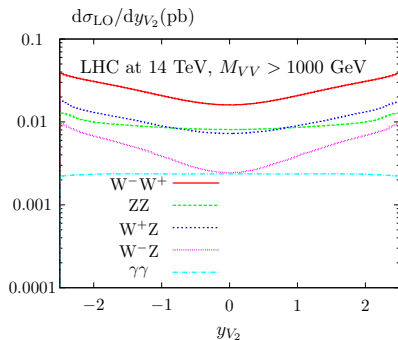
**LHC at 14 TeV, default cuts:**  $p_{T,V} > 15$  GeV,  $|y_V| < 2.5$



- **LO:** Drastically decreasing cross sections for large  $p_T$
- **NLO:**
  - Full result, i.e. virtual, soft, hard, and collinear photons included
  - corrections largest for ZZ, smallest for  $\gamma\gamma$

# Numerical Results (II) for WW/WZ/ZZ/ $\gamma\gamma$ Production

**LHC at 14 TeV, high-energy cuts:**  $p_{T,V} > 15$  GeV,  $|y_V| < 2.5$ ,  $M_{VV} > 1000$  GeV



- significant distortion of rapidity distributions at large invariant masses
- Corrections could be misinterpreted as signal of anomalous couplings.

# Double-Pole Approximation (DPA)

- **Lowest order:** Amplitude given as a product of **on-shell (OS) production amplitude**  $\otimes$  **on-shell decay amplitude**  $\otimes$  **Breit–Wigner:**

$$\mathcal{M}_{\text{Born,DPA}}^{\bar{q}_1 q_2 \rightarrow V_1 V_2 \rightarrow 4f} = \frac{1}{k_1^2 - M_1^2 + iM_1\Gamma_1} \frac{1}{k_2^2 - M_2^2 + iM_2\Gamma_2} \\ \times \sum_{\lambda_1, \lambda_2} \mathcal{M}_{\text{Born}}^{\bar{q}_1 q_2 \rightarrow V_1, \lambda_1 V_2, \lambda_2} \mathcal{M}_{\text{Born}}^{V_1, \lambda_1 \rightarrow f_3 \bar{f}_4} \mathcal{M}_{\text{Born}}^{V_2, \lambda_2 \rightarrow f_5 \bar{f}_6}$$

- Use **OS-projected momenta**  $\hat{\mathbf{k}}$  [Denner, Dittmaier, Roth, Wackerath 2000] in the OS matrix elements:

$$\hat{k}_{1,0} = \frac{1}{2} \sqrt{\hat{s}}, \quad \hat{\mathbf{k}}_1 = \frac{\mathbf{k}_1}{|\mathbf{k}_1|} \beta_W \frac{\sqrt{\hat{s}}}{2}, \quad \dots$$

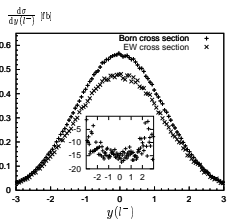
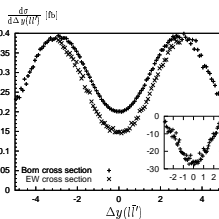
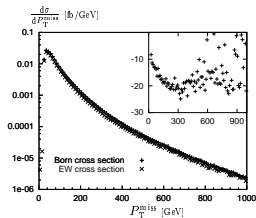
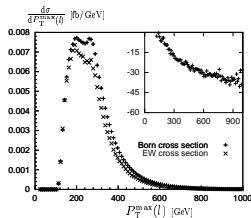
- **NLO:** EW corrections consist of **factorizable** and **non-factorizable** contributions, e.g.

$$\mathcal{M}_{\text{fact}} = \frac{R(k_1, k_2, \theta)}{(k_1^2 - M_1^2 + iM_1\Gamma_1) (k_2^2 - M_2^2 + iM_2\Gamma_2)}$$

**Caution:** Gauge invariance!

# EW corrections to $pp \rightarrow W^+W^- \rightarrow \nu_e e^+ \mu^- \bar{\nu}_\mu$ (DPA)

- Standard LHC event selection cuts applied to final-state leptons and missing transverse momentum; **additionally**  $M_{e^+\mu^-} > 500 \text{ GeV}$  required
- Large negative corrections at large transverse momenta
- Substantial negative corrections to inclusive observables
- Error due to DPA about 10% in the relative corrections
- EW corrections significantly larger than experimental error throughout the whole energy range (for  $L \sim 30 \text{ fb}^{-1}$ )**



[Accomando, Denner, Kaiser: arXiv:0409247 [hep-ph]]

- Simple LL ansatz for  $f_{\gamma/p}(x, Q_0^2)$

$$f_{\gamma/p}(x, Q_0^2) = \frac{\alpha}{2\pi} \left[ \frac{4}{9} \ln \left( \frac{Q_0^2}{m_u^2} \right) f_{u/p,v}(x, Q_0^2) + \frac{1}{9} \ln \left( \frac{Q_0^2}{m_d^2} \right) f_{d/p,v}(x, Q_0^2) \right] \otimes \frac{1 + (1-x)^2}{x}$$

- Running of  $f_{q/p}(x, Q^2)$  at  $\mathcal{O}(\alpha)$  affected by photon PDFs!

$$\frac{\partial f_{q/p}(x, \mu^2)}{\partial \ln \mu^2} = \frac{\alpha}{2\pi} \int_x^1 \frac{dy}{y} \left[ P_{qq}(y) Q_q^2 f_{q/p}(x/y, \mu^2) + P_{q\gamma}(y) Q_q^2 f_{\gamma/p}(x/y, \mu^2) \right]$$

- Momentum conservation

$$\int_0^1 dx x \left[ \sum_q f_{q/p}(x, \mu^2) + f_{g/p}(x, \mu^2) + f_{\gamma/p}(x, \mu^2) \right] = 1$$

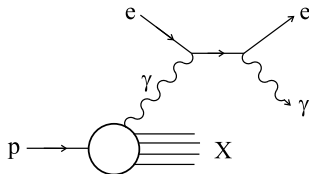
- ⇒ QED effects on  $f_{q/p}(x, \mu^2)$  small!
- ⇒ Still large conceptual uncertainties in  $f_{\gamma,0}$

# Measure Photon PDFs?

Consider the DIS process

$$ep \rightarrow e\gamma + X$$

with high- $p_T$  back-to-back  $e, \gamma$  in the final state



$$\sigma(ep \rightarrow e\gamma + X) = \int dx^\gamma f_{\gamma/p}(x^\gamma, \mu^2) \hat{\sigma}(e\gamma \rightarrow e\gamma),$$

related to Compton scattering

- $x^\gamma = \frac{E_T^\gamma E_e \exp(\eta^\gamma)}{2E_p E_e - E_T^\gamma E_e \exp(-\eta^\gamma)}$
- $f_{\gamma/p}(x^\gamma, \mu^2)$  could be in principle extracted from HERA data!



# EW Input Schemes – Definition of $\alpha$

- $\alpha(0)$ : On-shell definition in the Thomson-limit (zero momentum transfer)

$$\bar{u}(p)\Gamma_{\mu}^{Ae\bar{e}}(p,p)u(p)\Big|_{p^2=m_e^2} = e(0)\bar{u}(p)\gamma_{\mu}u(p), \alpha(0) = e(0)^2/4\pi$$

- $\alpha(M_Z)$  obtained via renormalization-group running from 0 to weak scale  $M_Z$

$$\alpha(M_Z) = \frac{\alpha(0)}{1 - \Delta\alpha(M_Z)}, \quad \Delta\alpha(M_Z) = \Pi_{f\neq t}^{AA}(0) - \text{Re} \Pi_{f\neq t}^{AA}(M_Z^2)$$

- $\alpha_{G_{\mu}}$  defined through the Fermi constant related to the muon lifetime

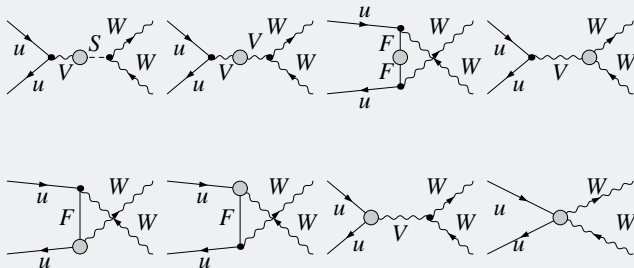
$$\alpha_{G_{\mu}} = \frac{\sqrt{2}G_{\mu}M_W^2s_w^2}{\pi} = \frac{\alpha(0)}{1 - \Delta r}$$

$\Delta r$  includes corrections to muon lifetime not contained in QED-improved Fermi model

- **light-fermion mass logs contained in  $\Pi_{f\neq t}^{AA}(0)$  resummed in effective couplings  $\alpha(M_Z)$  and  $\alpha_{G_{\mu}}$**

# Virtual EW Corrections to $pp \rightarrow W^-W^+ + X$

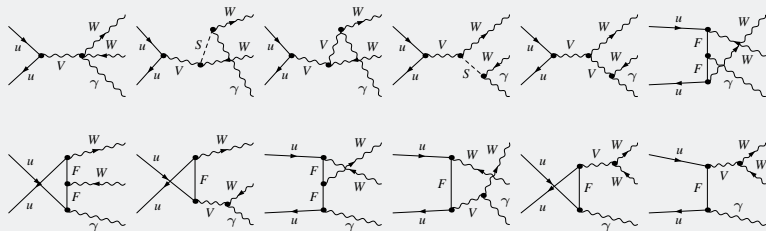
## One-loop contributions at $\mathcal{O}(\alpha^3)$



- On-shell renormalization of SM parameters
- We use the Fermi scheme to calculate the loop corrections.  
 → universal corrections to  $\Delta r$  absorbed in effective LO coupling
- $V_{ij}^{\text{CKM}} = \delta_{ij}$  within the loops → no renormalization of  $V_{ij}^{\text{CKM}}$

# Real EW Corrections – Infrared Singularities

Real photon radiation at  $\mathcal{O}(\alpha^3)$  (generic diagrams):  $q\bar{q} \rightarrow W^-W^+ + \gamma$



- **Soft singularities** due to soft photons
- **Initial-state collinear singularities** due to collinear photon radiation off initial-state quarks  $\rightarrow$  renormalization of PDFs
- Introduce small **quark mass  $m_q$**  and infinitesimal **photon mass  $\lambda$**  to regularize divergences  $\rightarrow$  results exhibit unphysical  $\ln m_q$  and  $\ln \lambda$  terms

**Apply phase-space slicing for numerically-stable evaluation of phase-space integral**

## Two-cut-off phase-space slicing

- Definition of bremsstrahlung phase space:

$$\sigma_{\text{real}} = \int \text{dPS}(W^- W^+ \gamma) |\mathcal{M}^\gamma|^2$$

- Phase-space decomposition:

$$\sigma_{\text{real}} = \sigma_{\text{hard}} + \sigma_{\text{soft}} + \sigma_{\text{coll}}$$

- **Soft limit:**  $E_\gamma < \Delta E \ll M_W$

$$\sigma_{\text{soft}}(\Delta E) = -\sigma_{\text{LO}} \left[ \frac{e^2}{(2\pi)^3} \int_{|\mathbf{k}_\gamma| < \Delta E} \frac{d^3\mathbf{k}_\gamma}{2\sqrt{\mathbf{k}_\gamma^2 + \lambda^2}} \sum_{ij} \frac{\pm Q_i Q_j (p_i p_j)}{(p_i k_\gamma)(p_j k_\gamma)} \right]$$

- **Collinear limit:**  $\theta_{q\gamma} < \Delta\theta \ll 1$ ,  $E_\gamma > \Delta E$

$$\sigma_{\text{coll},q}(\Delta E, \Delta\theta) = \frac{\alpha Q_q^2}{2\pi} \int_0^{1-2\Delta E/\sqrt{\hat{s}}} dz \frac{(1+z^2)}{1-z} \left( \ln \frac{\hat{s}(\Delta\theta)^2}{4m_q^2} - \frac{2z}{1+z^2} \right) \sigma_{\text{LO}}(z\hat{s})$$

- **Hard bremsstrahlung:**  $\theta_{q\gamma} > \Delta\theta$ ,  $E_\gamma > \Delta E$ ;  
numerical evaluation of  $\sigma_{\text{hard}}(\Delta E, \Delta\theta)$  without regulators
- Numerical result independent of  $\ln \Delta E$  and  $\ln \Delta\theta$

**$\ln m_q$  and  $\ln \lambda$  terms cancel in the sum  $\sigma_{\text{virt}} + \sigma_{\text{soft}} + \sigma_{\text{coll}}$  in infrared-safe observables**

## A problem with unstable particles

Naive implementation of finite width in gauge-boson propagator:

$$\frac{-ig^{\mu\nu}}{q^2 - M_W^2 + i\epsilon} \rightarrow \frac{-ig^{\mu\nu}}{q^2 - M_W^2 + iM_W\Gamma_W}$$

$\Gamma_W$  includes Dyson summation of self energies, mixing of perturbative orders  
→ **might destroy gauge invariance (even at leading order!)**

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→ **might destroy gauge invariance (even at leading order!)**

→ **CMS universal solution that**

- respects gauge invariance
- is valid in all phase-space regions

**Straightforward implementation:**

- **LO:**  $M_V^2 \rightarrow \mu_V^2 = M_V^2 - iM_V\Gamma_V$ ,  $\cos^2 \Theta_W = \frac{\mu_W^2}{\mu_Z^2}$ ,  $V = W, Z$
- **NLO:**
  - Complex renormalization:  $\mathcal{L}_0 \rightarrow \mathcal{L} + \delta\mathcal{L}$ , **bare (real) Lagrangian unchanged!**
  - Evaluate loop integrals with complex masses

# ”Real Radiation” of Massive Vector Bosons

**Low energies:** Phase-space and perturbative suppression of  $pp \rightarrow V_1 V_2 + (W/Z)$   
⇒ contribution below 1%

**High energies:** **Logarithmic enhancement** of additional soft/collinear W- or Z-boson radiation

⇒ Investigation of  $V_1 V_2 + W/Z$  production as background to  $V$  pairs at large  $p_T$ ,  $M_{VV}$

- invisible decay of  $Z \rightarrow \nu\bar{\nu}$
- collinear emission
- ...

**Simplified approach (details depend on experimental analysis),**

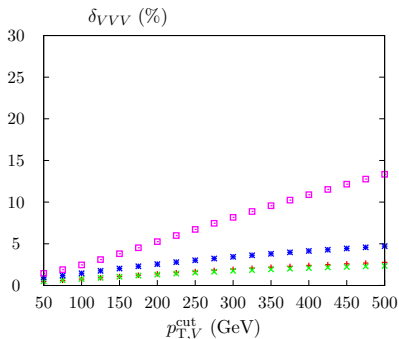
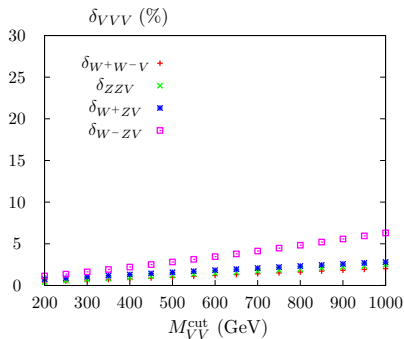
**e.g. W-Pair production:**

- 1 Include  $pp \rightarrow W^- W^+ Z$  with totally inclusive  $Z$
- 2 Include  $pp \rightarrow W^- W^+ W^\pm$ ; treat  $W^\pm$  with lowest  $p_T$  totally inclusively



# Numerical Results (I) – “Real Radiation” of W/Z

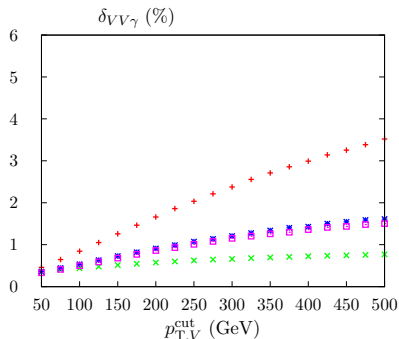
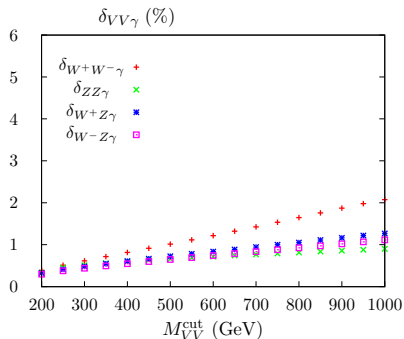
**LHC at 8 TeV, default cuts:**  $p_{T,V} > 15 \text{ GeV}$ ,  $|y_V| < 2.5$



- corrections **below 5%** even for large transverse momenta and invariant masses
- corrections to  $W^-Z$  production enhanced due to  $W^-ZW^+$  final states (PDFs!)

# Numerical Results (II) – Real Radiation of Hard Photons

**LHC at 8 TeV, default cuts:**  $p_{T,V} > 15 \text{ GeV}$ ,  $|y_V| < 2.5$ ,  $p_{T,\gamma} > 15 \text{ GeV}$ ,  $|y_\gamma| < 2.5$



- real radiation of hard photons marginal ( $< 2\%$ )  
→ neglect in MC implementation
- corrections largest for WW production

**Virtual corrections** computed in the `FeynArts/FormCalc/LoopTools (FF)` framework [ (FA): Küblbeck, Böhm, Denner 1990; (FC,LT): Hahn, Pérez Victoria 1999; Hahn 2001; (FF): van Oldenborgh, Vermaseren 1990]

## 1 FeynArts-3.5:

- Automatic generation of diagrams
- Calculation of amplitudes

## 2 FormCalc-6.1:

- Algebraical simplification of amplitudes, introduction of tensor coefficients
- Analytical calculation of squared amplitudes
- Spin-, colour- and polarization sums
- Generation of Fortran code

## 3 LoopTools-2.5:

- Numerical Passarino–Veltman reduction within Fortran
- Numerically-stable evaluation of scalar integrals

**Bremsstrahlung amplitudes** computed with `FeynArts/FeynCalc`  $\oplus$  `Madgraph` [Alwall et al.], numerical phase-space integration within Fortran using the Vegas algorithm

# ZZ Production: Polarizations

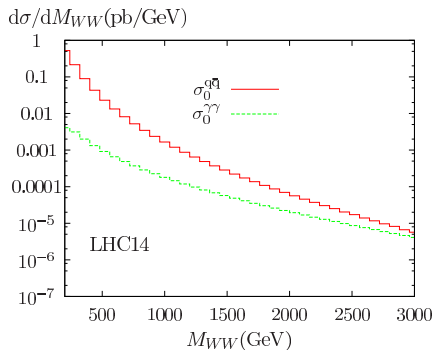
pp $\rightarrow$ ZZ + X					
ZZ polarizations	summed	LL	L+	++	+-
LHC8					
$\sigma_{\text{LO}}/\text{pb}$	3.810	0.223	0.396	$10^{-1} \times [0.559]$	2.676
$\delta\sigma_{\text{weak}}/\text{pb}$	-0.179(-0.155)	-0.009(-0.008)	-0.016(-0.014)	-0.002(-0.002)	-0.134(-0.117)
$p_{T,Z} > 500 \text{ GeV}$					
$\sigma_{\text{LO}}/\text{pb}$	$10^{-2} \times [0.101]$	$10^{-7} \times [0.202]$	$10^{-5} \times [0.779]$	$10^{-8} \times [0.504]$	$10^{-3} \times [0.996]$
$\delta\sigma_{\text{weak}}/\text{pb}$	-0.039(-0.030)	-0.975(+0.748)	-0.204(-0.157)	-0.895(-0.425)	-0.383(-0.293)
$p_{T,Z} > 1000 \text{ GeV}$					
$\sigma_{\text{LO}}/\text{pb}$	$10^{-5} \times [0.919]$	$10^{-10} \times [0.121]$	$10^{-7} \times [0.231]$	$10^{-11} \times [0.303]$	$10^{-5} \times [0.915]$
$\delta\sigma_{\text{weak}}/\text{pb}$	-0.557(-0.387)	-2.599(+14.909)	-0.098(-0.070)	-1.742(+1.043)	-0.555(-0.387)

- **small transverse momenta:** 70% from (+-), similar  $K$ -factors for all polarizations.
- **large transverse momenta:** 99% from (+-), other contributions negligible.
- **Note:** One-loop squared term (given in brackets) contributes at  $\sim 10\%$   
 $\rightarrow$  **large uncertainties** due to missing EW higher orders.

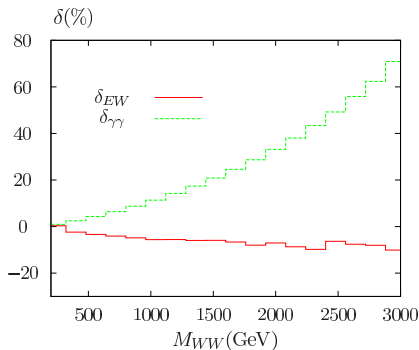
**Conclusion:** One  $K$ -factor sufficient to describe polarized ZZ production

# pp $\rightarrow$ W<sup>-</sup>W<sup>+</sup>( $\gamma$ ) – Numerical Results

## No cuts

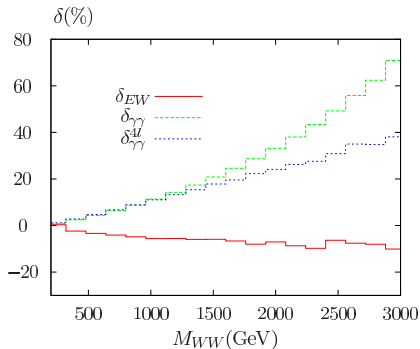
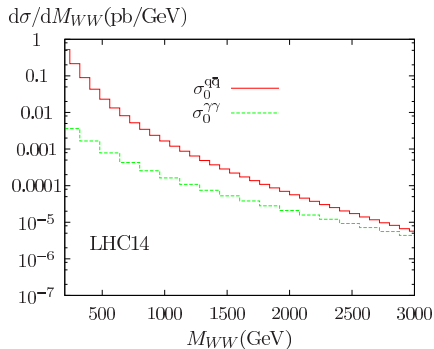


- LO cross section dominated by  $q\bar{q}$  contributions
- Rapid decrease of cross section for increasing invariant masses



- EW corrections small even for large values of  $M_{WW}$
  - Large contributions (+80%!) from  $\gamma\gamma \rightarrow WW$  at high invariant masses
- ⇒ Leptonic decays?

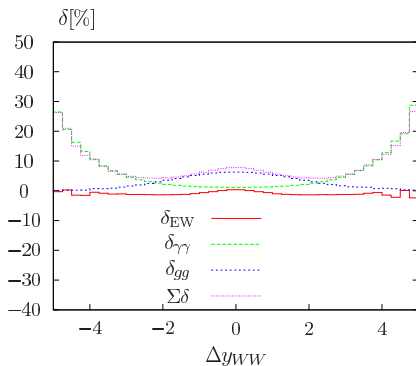
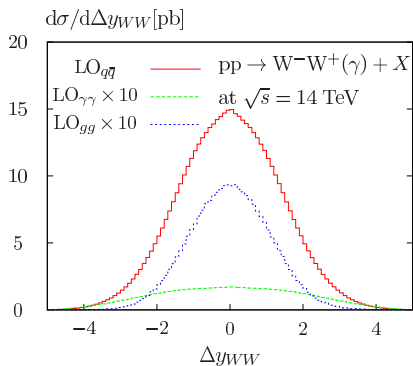
## LHC acceptance cuts



- LO cross section dominated by  $q\bar{q}$  contributions
- Rapid decrease of cross section for increasing invariant masses
- Employ LHC cuts on decay products:  $p_{T,l} > 20$  GeV,  $|y_l| < 3$ ,  $p_{T,miss} > 25$  GeV
- ⇒ relative effect of  $\gamma\gamma \rightarrow WW$  reduced by factor 2 at large  $M_{WW}$

# EW Corrections to $pp \rightarrow W^-W^+ - \text{Numerical Results}$

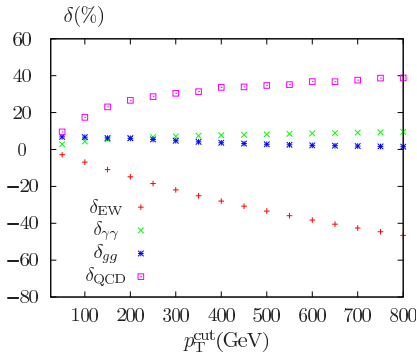
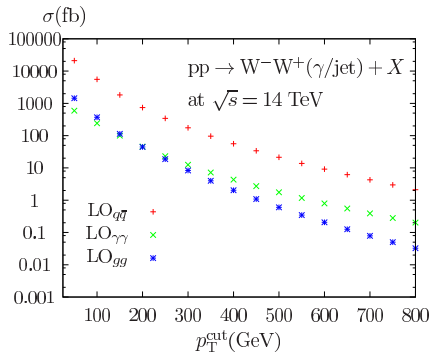
**Default cuts:**  $p_{T,W^\pm} > 15 \text{ GeV}$ ,  $y_{W^\pm} < 2.5$



- WW production dominated by events near threshold, isotropic production at small  $\Delta y_{WW}$
- 5% increase of cross section by gg channel
- EW corrections at the percent level
- Sizable contributions from  $\gamma\gamma$  at large  $|\Delta y_{WW}|$

# pp $\rightarrow$ W<sup>-</sup>W<sup>+</sup>( $\gamma$ ) – Numerical Results

**Default cuts:**  $p_{T,W^\pm} > 15$  GeV,  $|y_{W^\pm}| < 2.5$



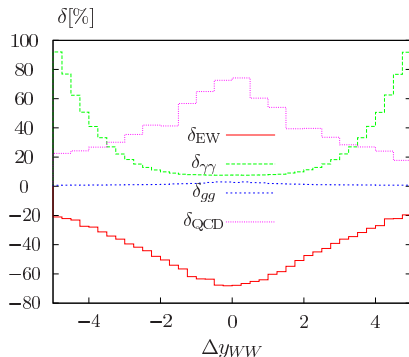
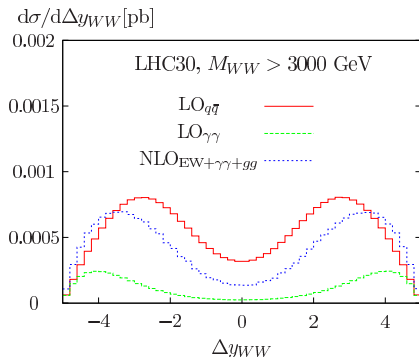
- assume  $\int \mathcal{L} dt = 200 \text{ fb}^{-1}$   
 $\Rightarrow$  1000 WW events with  $p_T > 500$  GeV
- decreasing admixture of gg,  
increasing admixture of  $\gamma\gamma$

- large admixture of  $\gamma\gamma$  (10% !)
- large negative EW corrections (-45%),  
comparable to QCD corrections



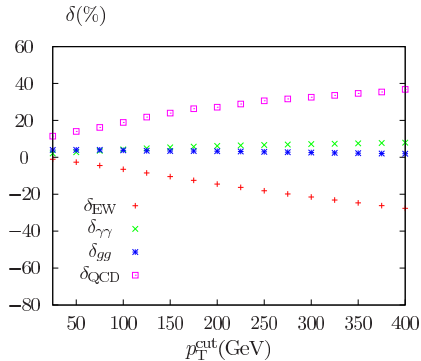
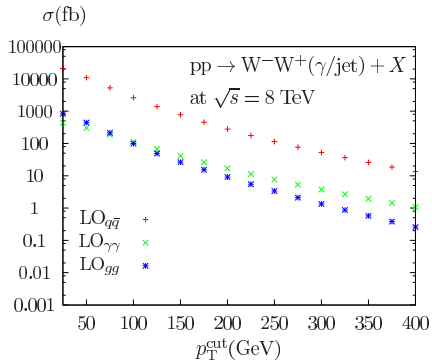
# EW Corrections to $pp \rightarrow W^-W^+$ – Numerical Results

**Very-high-energy cuts:**  $p_{T,W^\pm} > 15$  GeV,  $y_{W^\pm} < 2.5$ ,  $M_{WW} > 3$  TeV

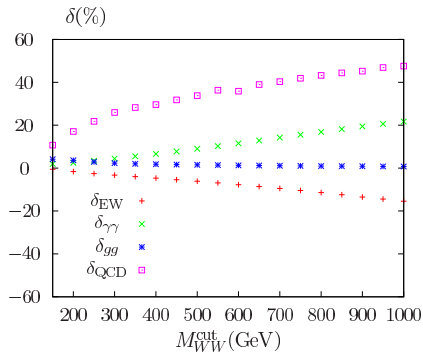
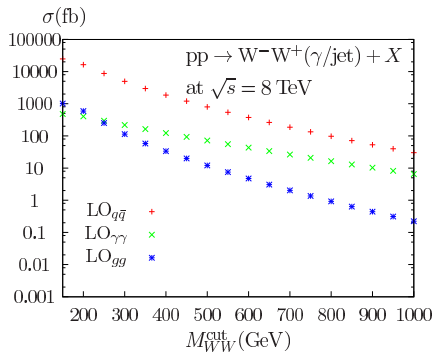


- NLO EW as important as QCD
- extreme distortion due to  $\gamma\gamma$  (**caveat:** high uncertainty in photon PDFs)

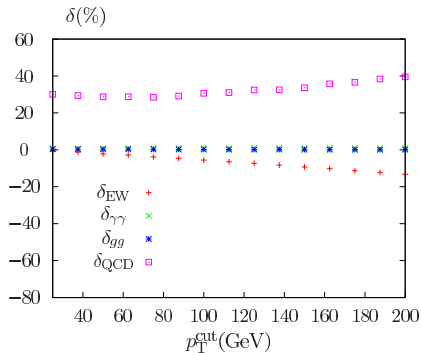
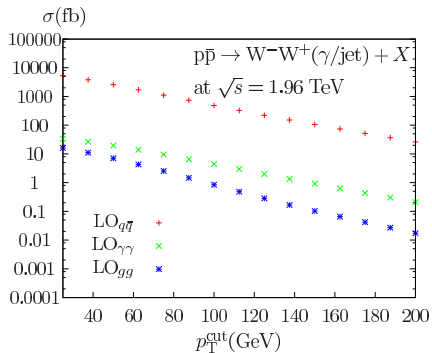
# Transverse-momentum distribution at the LHC8



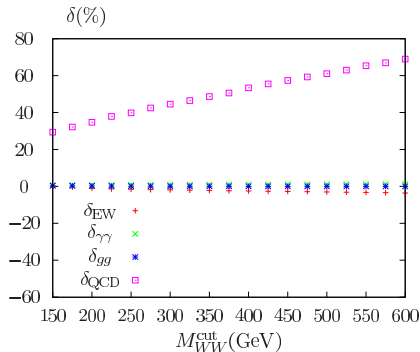
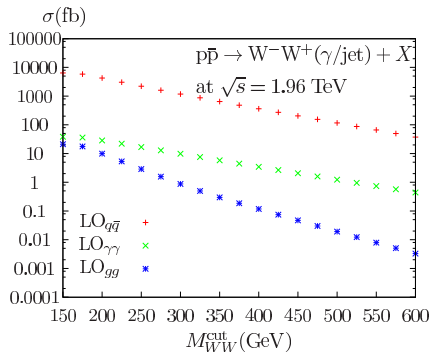
# Invariant-mass distribution at the LHC8



# Transverse-momentum distribution at the Tevatron

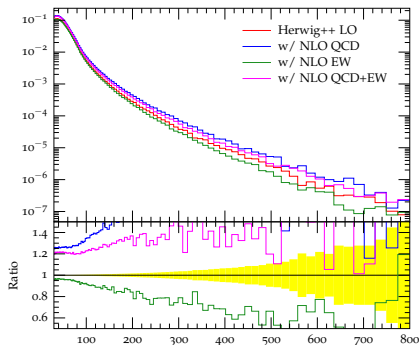
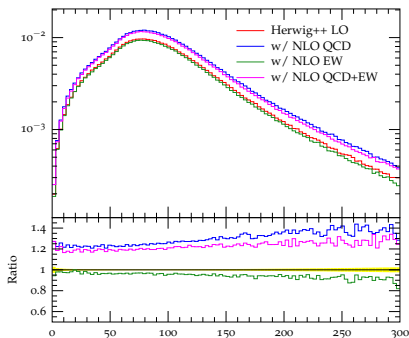


# Invariant-mass distribution at the Tevatron



# HERWIG++ Analysis for ZZ Production (II) – Preliminary!

Simulation for  $pp \rightarrow ZZ \rightarrow e^+e^-\mu^+\mu^- + X$  at 8 TeV,  $M_{e^+\mu^-}$  and  $p_{T,l}$  distributions



- Standard Herwig++ setup used (v2.6.2, with simple add-on for EW corrections, 10M events), ZZ at NLO QCD matched with parton showers, hadronization included, underlying event switched off
- Implementation seems to work fine