

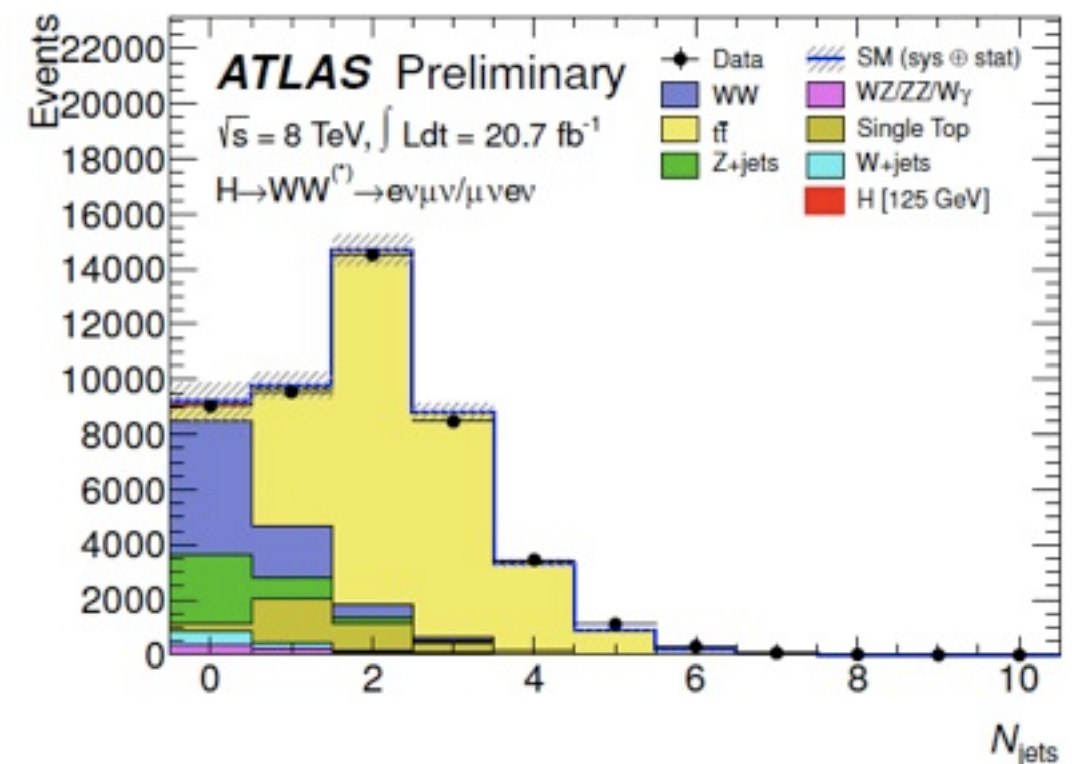
Jet vetoes in Higgs searches at the LHC

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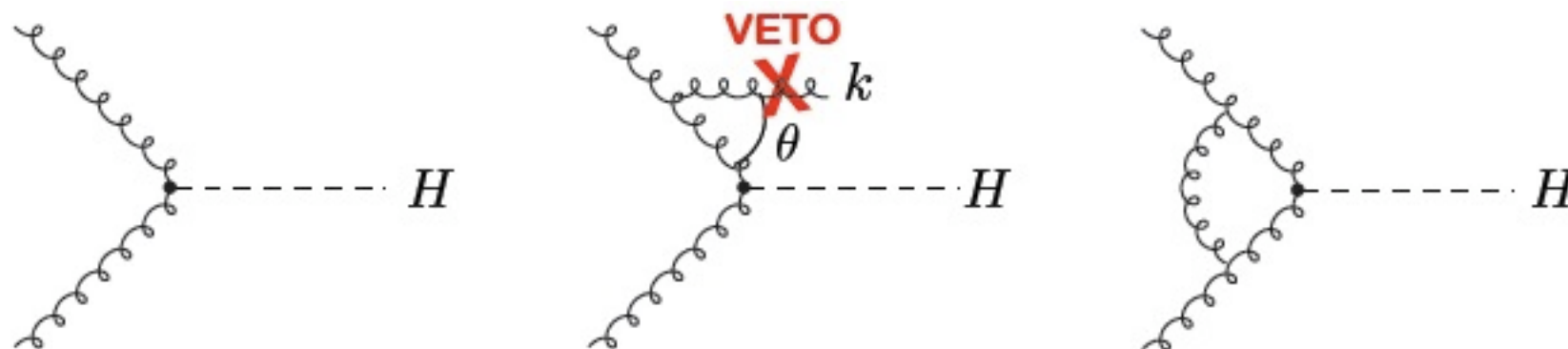
Searches in $H \rightarrow WW$

- ▶ $H \rightarrow W^+W^- \rightarrow l^+\nu^-l^-\nu^+$ relevant for coupling and spin measurements
- ▶ Recent results show a 3.8σ (ATLAS) / 4σ (CMS) excess w.r.t. the background-only hypothesis in good agreement with the SM prediction
- ▶ Main background: WW , $W/Z + \text{jets}$, $t\bar{t}$, ...
- ▶ Categorization according to lepton flavour and jet multiplicity to optimize sensitivity
- ▶ Additional bin-dependent selection cuts for further background reduction



The 0-jet bin

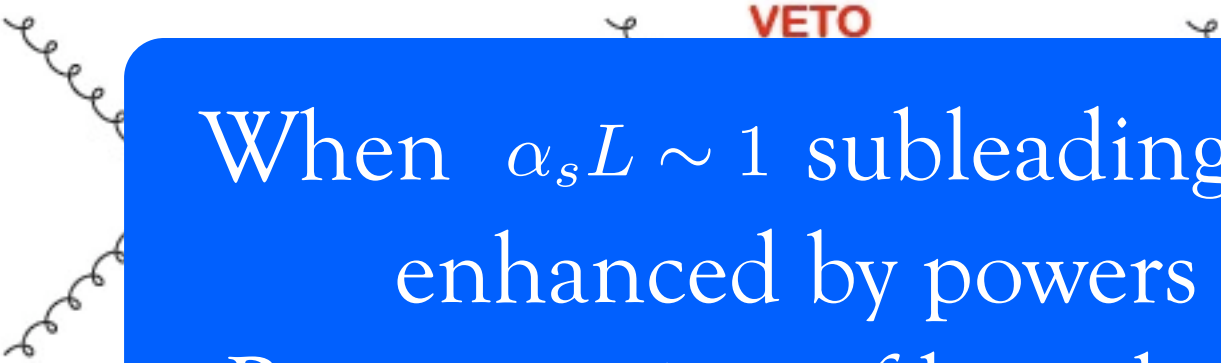
- ▶ 0-jet requirement suppresses high- p_t jets (e.g. b-jets from top decay)
- ▶ To extract couplings, we need to know the fraction of signal events (mainly $gg \rightarrow H$) that survives the veto $p_{t,veto}$ on the ISR
- ▶ Vetoing QCD radiation gives rise to Sudakov logs.
 - ▶ e.g. emission of a soft ($\omega \ll M$) and collinear ($\theta \ll 1$) gluon



$$\sigma_{0-jet} \simeq \sigma_0 \left(1 + C_A \frac{\alpha_s}{\pi} \int \frac{d\omega}{\omega} \frac{d\theta^2}{\theta^2} (\Theta(p_{t,veto} - \omega\theta) - 1) \right) \simeq \sigma_0 \left(1 - 2C_A \frac{\alpha_s}{\pi} \ln^2 \frac{m_H}{p_{t,veto}} + \dots \right)$$

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When $\alpha_s L \sim 1$ subleading terms are enhanced by powers of L .
Resummation of large logs needed

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Theoretical uncertainties in fixed-order

- ▶ LHC experiments choose $p_{t,\text{veto}} \simeq 25 - 30 \text{ GeV}$: over 90% reduction of background
- ▶ For such veto scales, logs. are not dramatically large: $\alpha_s \ln \frac{m_H}{p_{t,\text{veto}}} \sim 0.2$
- ▶ Huge cancellations in $\sigma_{0\text{-jet}}$ between large K-factor (σ_{tot}) and large Sudakov logs ($\sigma_{\geq 1\text{jet}}$)

$$\sigma_{0\text{-jet}} = \sigma_{tot} - \sigma_{\geq 1\text{jet}} \sim \sigma_0 \left(K - 2C_A \frac{\alpha_s}{\pi} \ln^2 \frac{m_H}{p_{t,\text{veto}}} \right)$$

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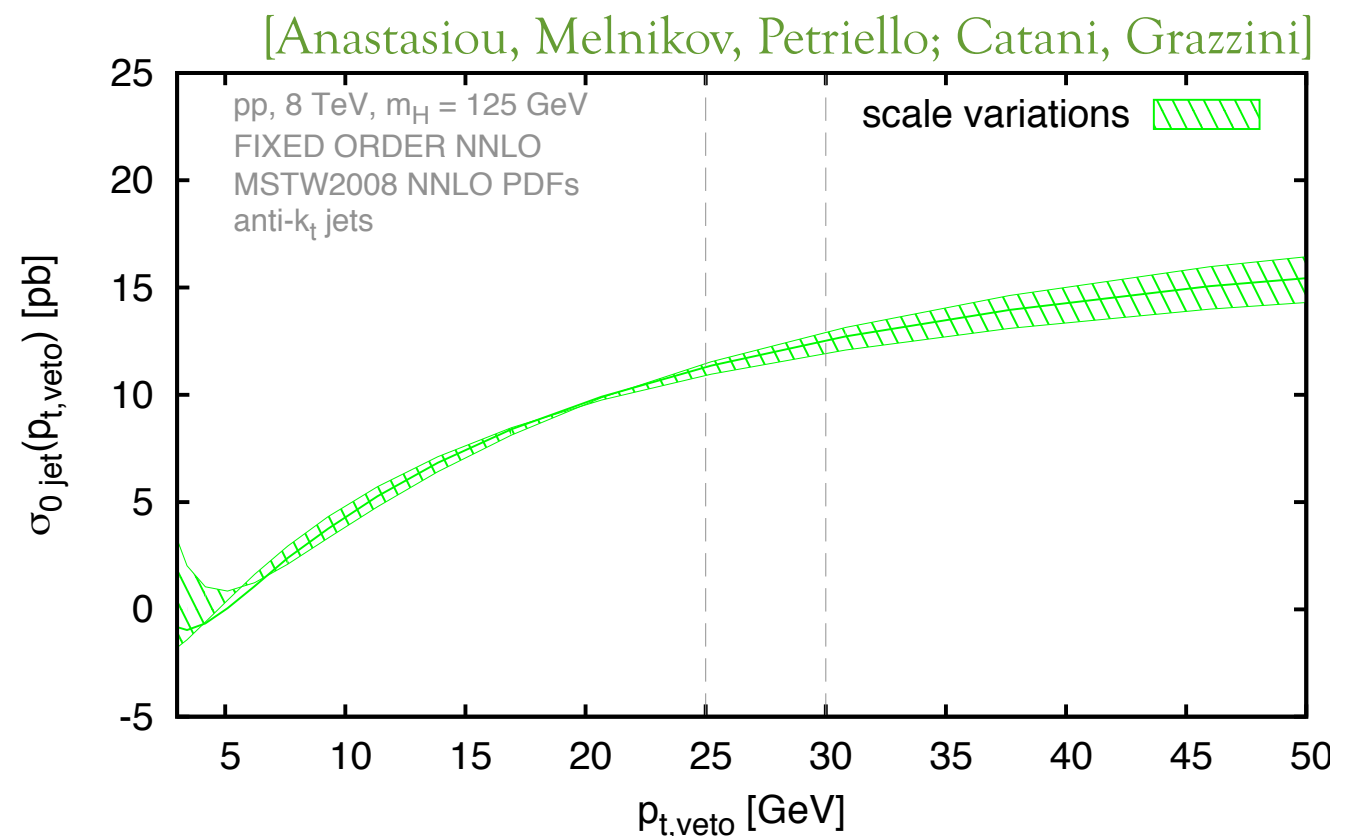
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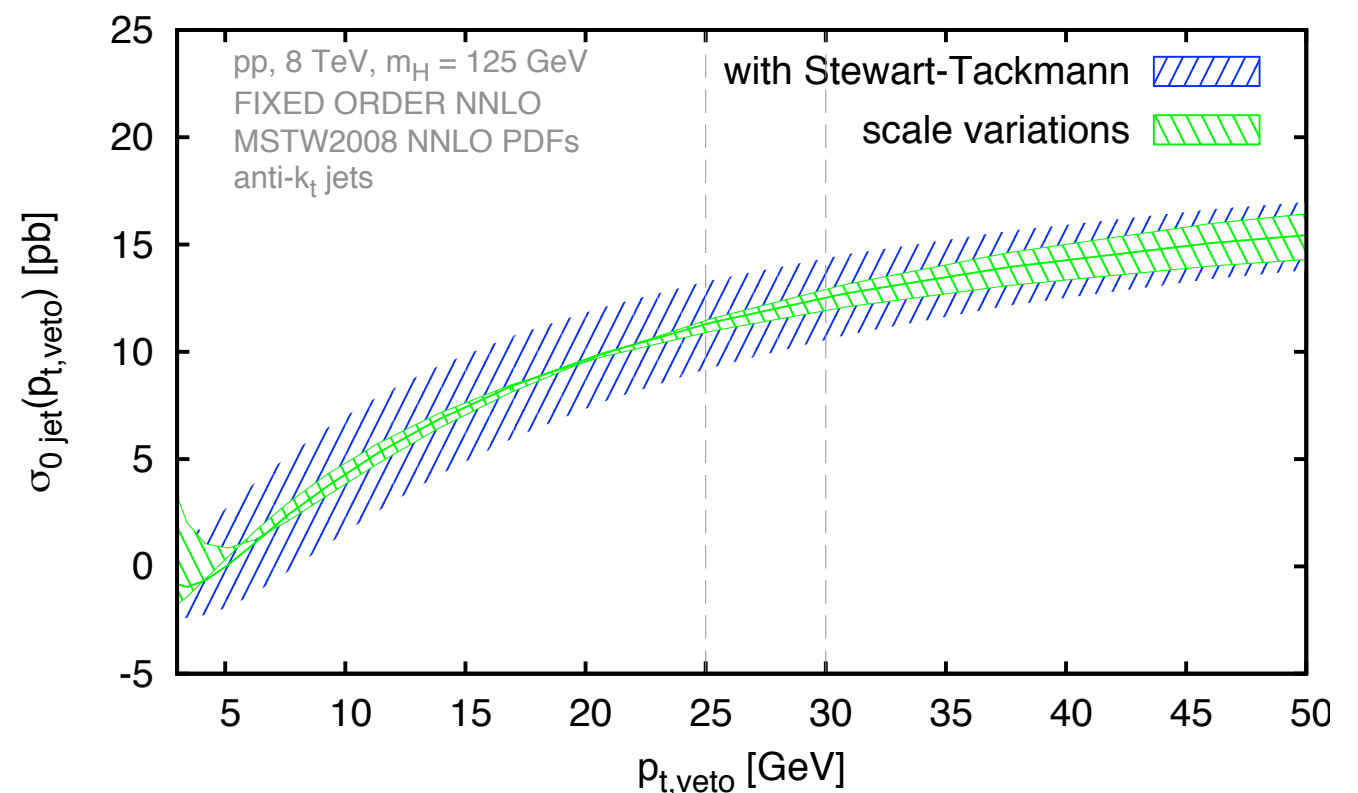


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Can we rely on inclusive uncertainties ?



Theoretical uncertainties in fixed-order

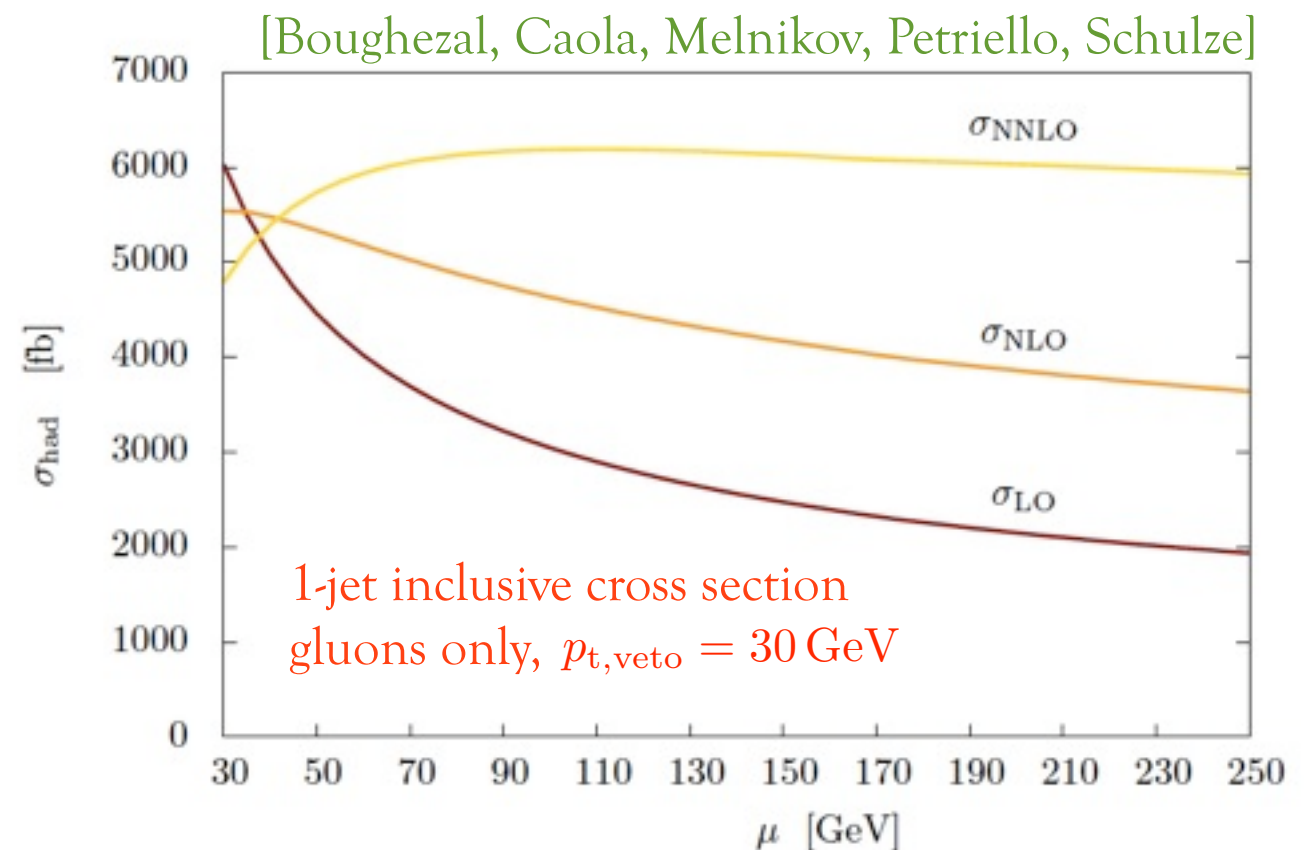
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- ▶ Inclusive cross section $\sigma_{\geq 1jet}$ shows good convergence at low renormalisation scales

e.g.

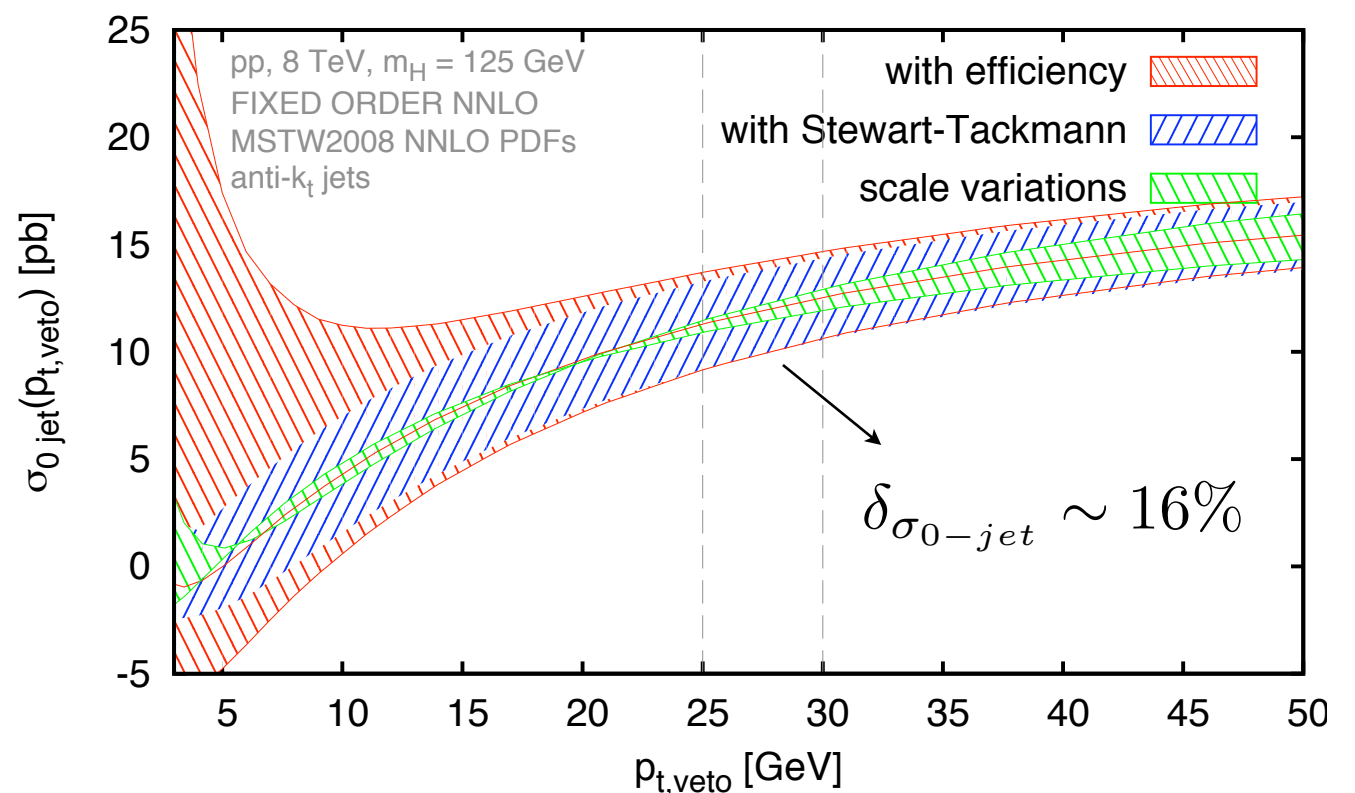
$$\mu \sim m_H/2$$



Theoretical uncertainties in fixed-order

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- ▶ $n + 1$ efficiency schemes are available at N^n LO

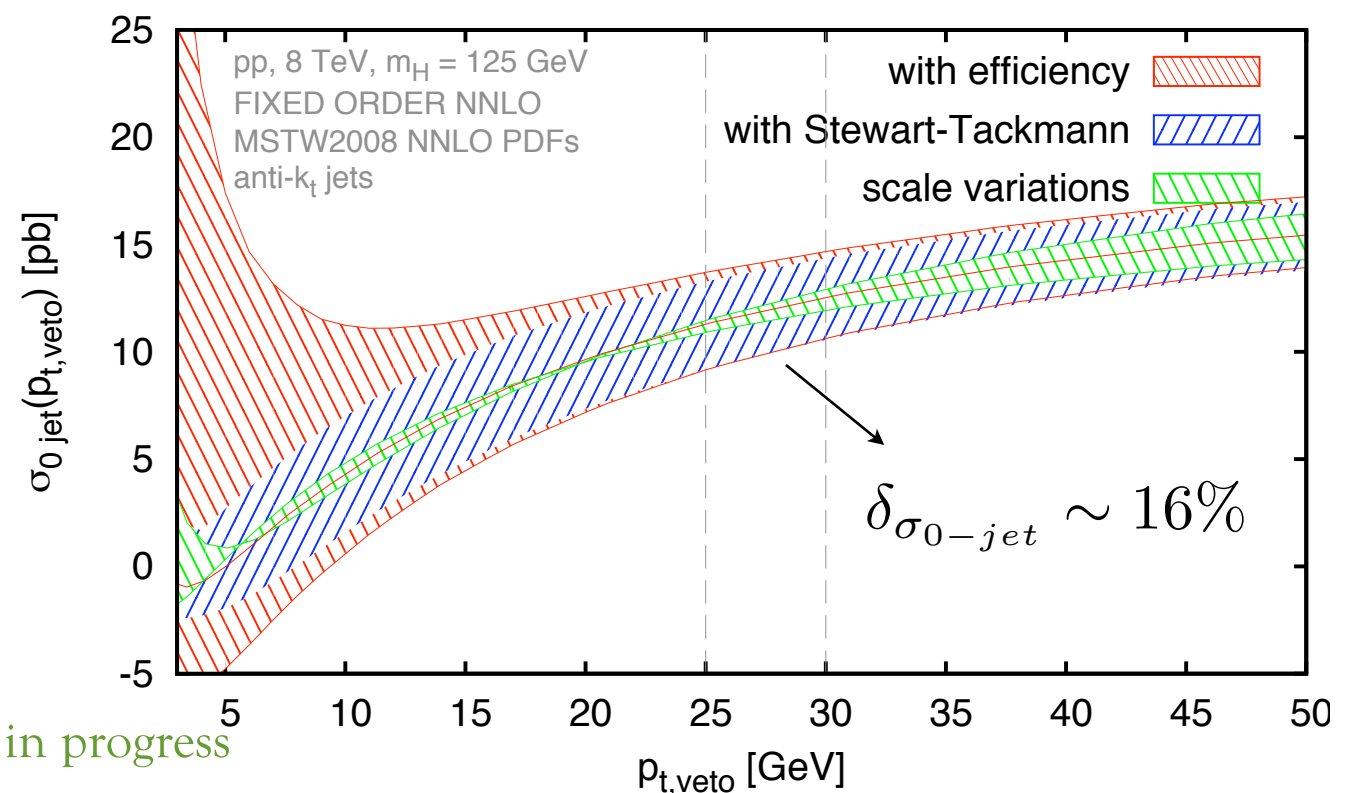


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Resummation of large logs needed to improve error estimate



NLL: Banfi, Salam, Zanderighi '12

NNLL: Banfi, PFM, Salam, Zanderighi;

Becher, Neubert '12; Tackmann, Stewart, Walsh, Zuberi in progress

Resumming large logarithms

- ▶ Automated resummation for a jet observable can be carried out under some applicability conditions (*i.e.* **rIRC safety, continuous globalness**)

[Banfi, Salam, Zanderighi '01/'02]

- ▶ Resummation structure for $\sigma_{0-jet}(p_{t,veto})$ remarkably simple:

$$\sigma_{0-jet}(p_{t,veto}) = |M_B|^2 e^{-R(p_{t,veto})}$$

- ▶ Double logarithms exponentiate: Sudakov factor
 - ▶ Encodes soft-collinear virtual contributions at scales larger than $p_{t,veto}$
 - ▶ Obtained from a single dressed (up to $\mathcal{O}(\alpha_s^3)$) gluon emission
 - ▶ Identical to boson- p_t resummation up to NNLL (not beyond!)

[Bozzi et al. '03; Becher, Neubert '10]

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$$\sigma_{0-jet}(p_{t,veto}) = \mathcal{L}(p_{t,veto}) |M_B|^2 e^{-R(p_{t,veto})}$$

- ▶ Double logarithms exponentiate: Sudakov factor
- ▶ Luminosity pre-factor $\mathcal{L}(p_{t,veto})$ contains:
 - ▶ parton luminosity evaluated at $\mu_F \simeq p_{t,veto}$
 - ▶ hard virtual corrections to the Born up to $\mathcal{O}(\alpha_s(\mu_R))$
 - ▶ collinear coefficient functions up to $\mathcal{O}(\alpha_s(p_{t,veto}))$

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$$\sigma_{0-jet}(p_{t,veto}) = \mathcal{L}(p_{t,veto}) |M_B|^2 e^{-R(p_{t,veto})} \mathcal{F}(R')$$

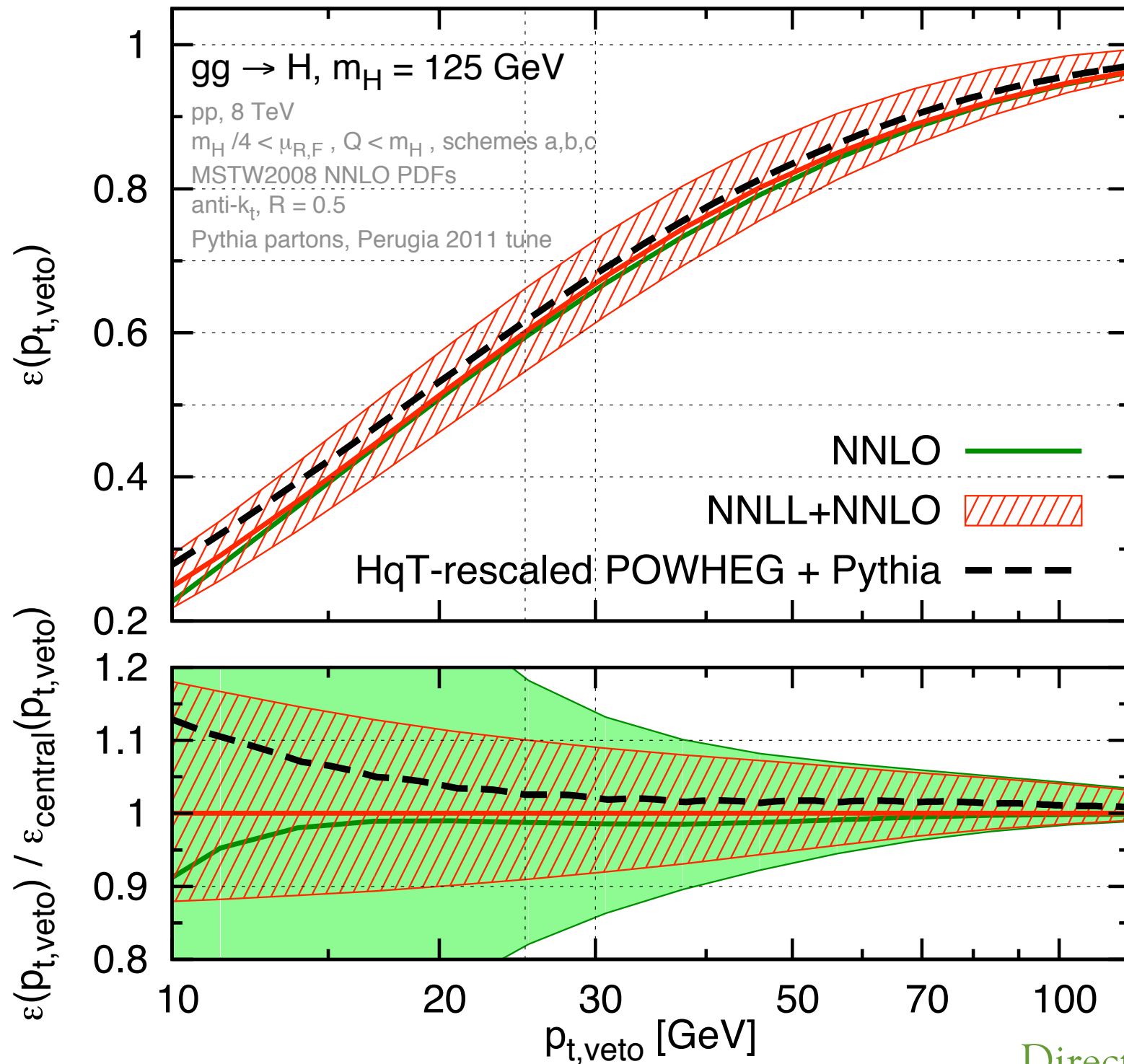
- ▶ Double logarithms exponentiate: Sudakov factor
- ▶ Luminosity pre-factor $\mathcal{L}(p_{t,veto})$
- ▶ Multiple emission function $\mathcal{F}(R')$: encodes the single logarithmic (up to NNLL) contribution from arbitrarily many soft and/or collinear emissions

- ▶ Analytic expression for $\sigma_{0-jet}(p_{t,veto})$. Where $R' = -p_{t,veto} \frac{dR(p_{t,veto})}{dp_{t,veto}}$

Matching to fixed-order

- ▶ Resummation provides a direct handle to estimate the impact of missing Sudakov logarithms (*i.e.* resummation scale variation)
- ▶ Alternatively, one can obtain resummed predictions for the jet-veto efficiency and treat the resulting uncertainty with the efficiency method
 - ▶ Define three matching schemes at NNLL+NNLO in one to one correspondence with the three schemes for the efficiency
 - ▶ The three schemes differ by subleading effects
 - ▶ Varying the scheme leads to an additional systematic uncertainty

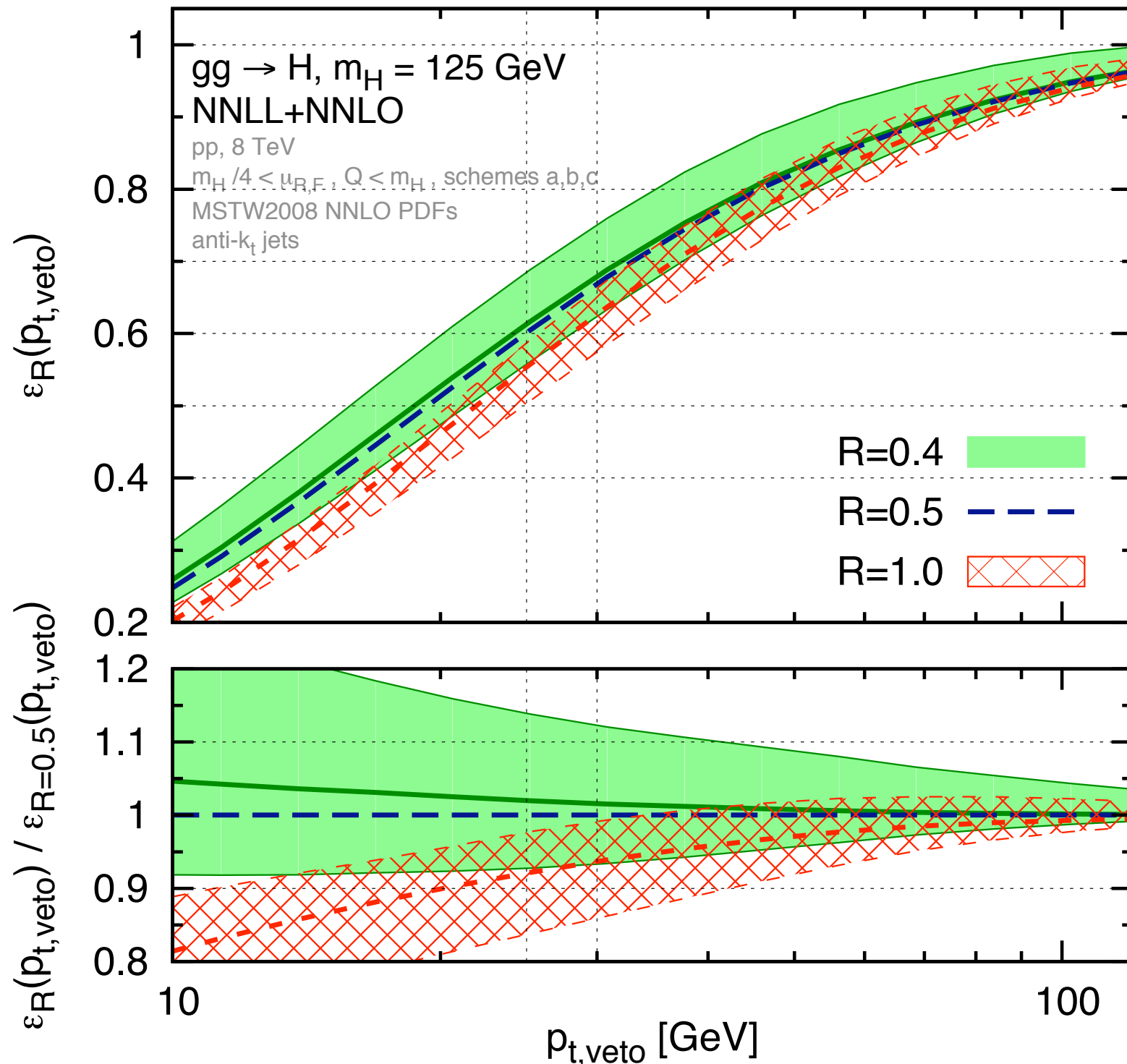
Comparison to MC



- ▶ Good agreement on central values with POWHEG+Pythia reweighted with HqT & HNNLO
- ▶ Uncertainties reduced from $\sim 15\%$ to $\sim 9\%$
- ▶ Hadronisation and UE corrections have a small impact ($\leq 1\%$)
- ▶ Corresponding error in the cross section $\sim 10\% - 11\%$

Direct predictions for the cross section can be also obtained without using the efficiencies

Choice of the jet radius R



- ▶ All-order terms of the form (e.g. $\mathcal{F}(R')$)

$$\alpha_s^n \ln^{n-1} \frac{1}{R}$$

- ▶ For $R \ll 1$ they should be resummed

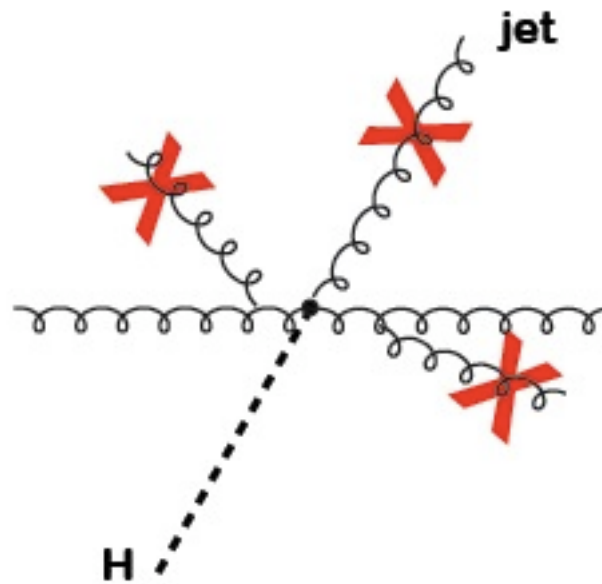
[Tackmann, Walsh, Zuberi '12]

- ▶ Choosing $R \sim 1$ reduces the uncertainties

- ▶ Higher contamination from UE ($\sim R^2$) and pileup ... filtering can be used to reduce it

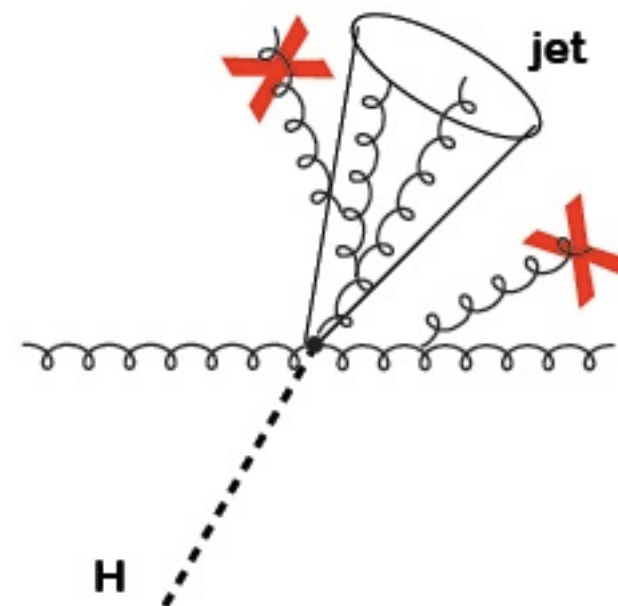
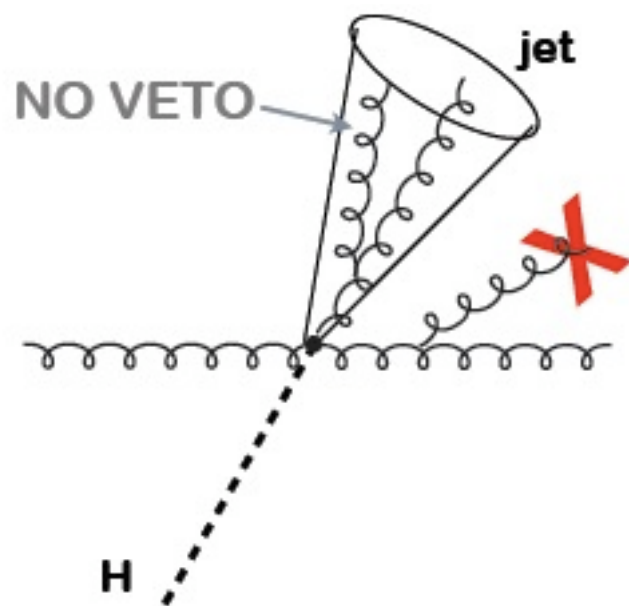
1-jet bin

- ▶ In the 0-jet sample all jets are vetoed. Cross section is sensitive to soft and collinear emissions everywhere in the phase space



1-jet bin

- ▶ In the 0-jet sample all jets are vetoed. Cross section is sensitive to soft and collinear emissions everywhere in the phase space
- ▶ This is not the case if we require to observe n jets. Cross section is insensitive to emissions which take place inside the tagged jets

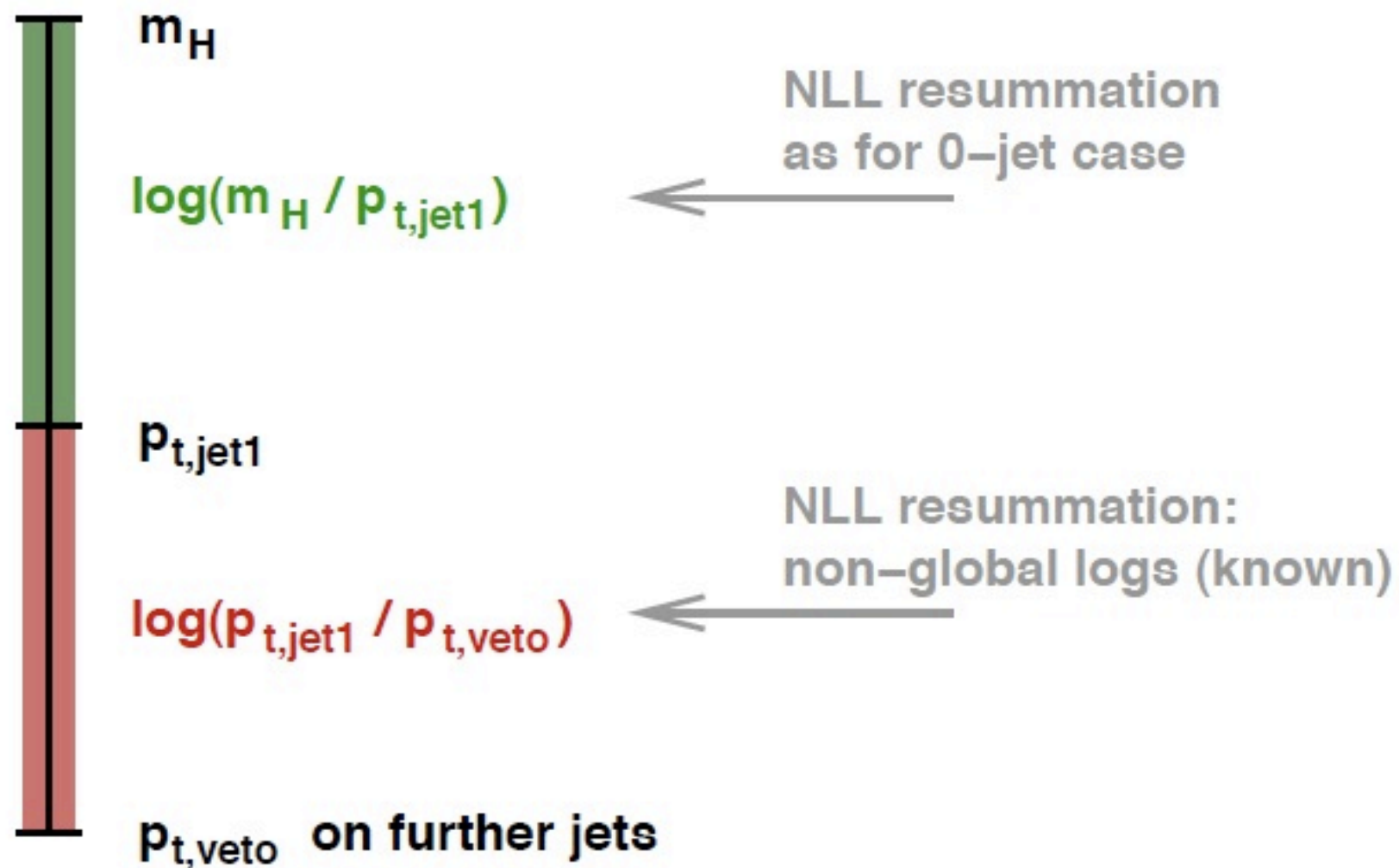


- ▶ A gluon splitting close to the jet boundary gives rise to a new family of large logarithms (non-global single logs) which require all-order treatment

[Dasgupta, Salam '01; Appleby, Seymour '02; Banfi, Dasgupta '05]

1-jet bin

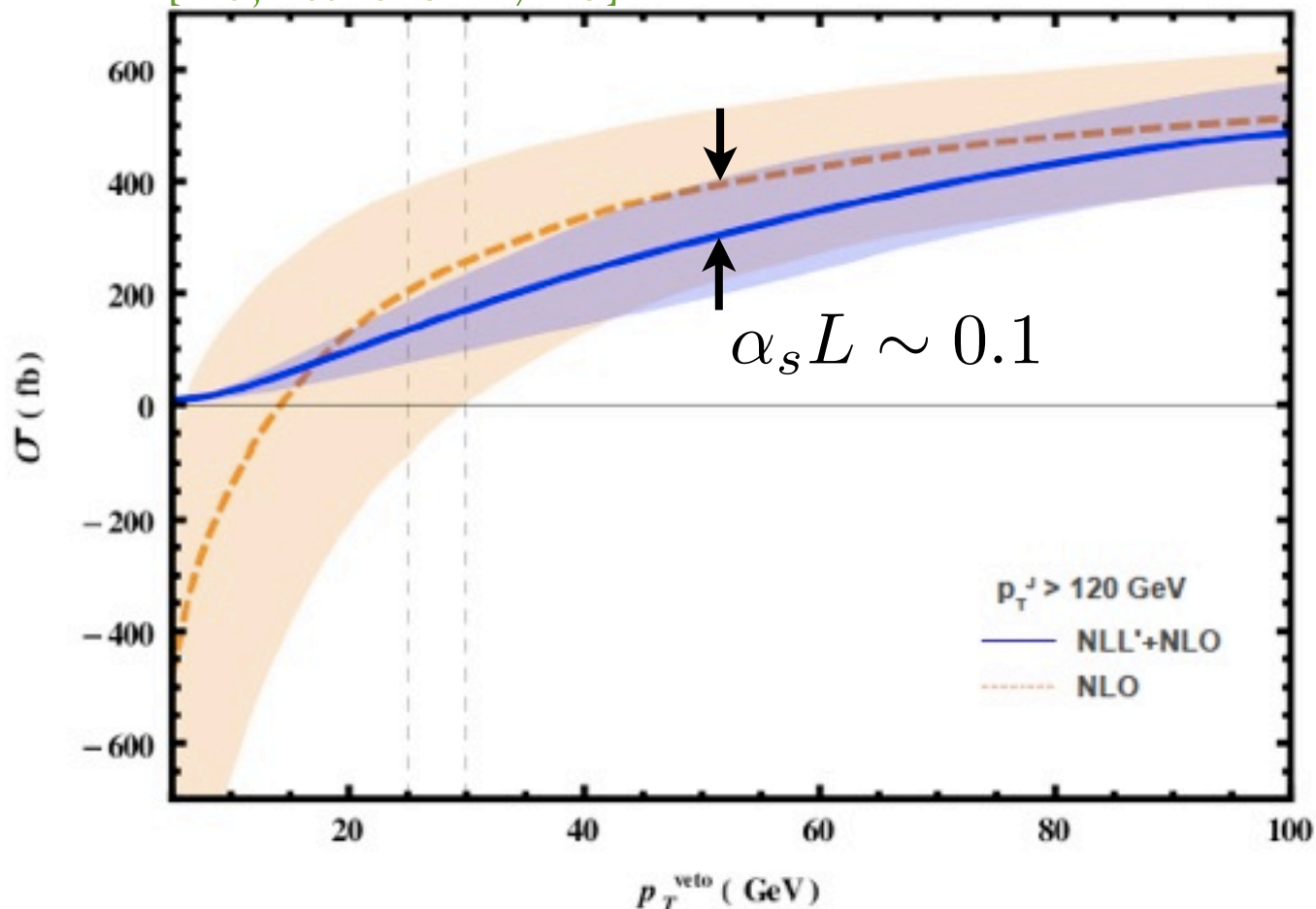
scales for 1-jet bin



- ▶ Three-scale problem
- ▶ More involved log structure
- ▶ Nested resummation required, with $p_{t,jet1}$ integrated from $p_{t,veto}$ to m_H

1-jet bin

[Liu, Petriello '12/'13]



- ▶ Global part of $\ln p_{t,jet}/p_{t,veto}$ recently resummed to NLL in the limit

$$p_{t,veto} \ll p_{t,jet} \sim m_H$$

- ▶ no $\ln \frac{m_H}{p_{t,jet}}$

- ▶ impact of non-global $\ln \frac{p_{t,jet}}{p_{t,veto}}$ estimated to be small

- ▶ Up to $\sim 25\%$ reduction w.r.t. NLO central value ... large subleading corrections or matching effects ?

Fixed-order uncertainty with
Stewart-Tackmann method

2-jet bin

- ▶ In the 2-jet bin VBF production becomes relevant
- ▶ Clean signal, *i.e.* two forward jets widely separated in rapidity and few extra gluon emissions (incoming quarks). VBF selection cuts are applied to isolate it
 - 2-jet bin used in $H \rightarrow WW$ searches
 - But ggF/VFB separation relevant for other channels, *e.g.* $H \rightarrow \gamma\gamma$
- ▶ $\sim 25\%$ contamination from ggF (more radiation in the central region)
- ▶ It can be reduced by imposing a veto on extra (≥ 3) jets, but this makes uncertainties estimate less reliable
- ▶ Resummation desired, but extremely challenging !
 - NLO studies matched to Parton-Showers are available, but hard to assess PS uncertainties
 - [Campbell et al.; Frederix, Frixione]

2-jet bin

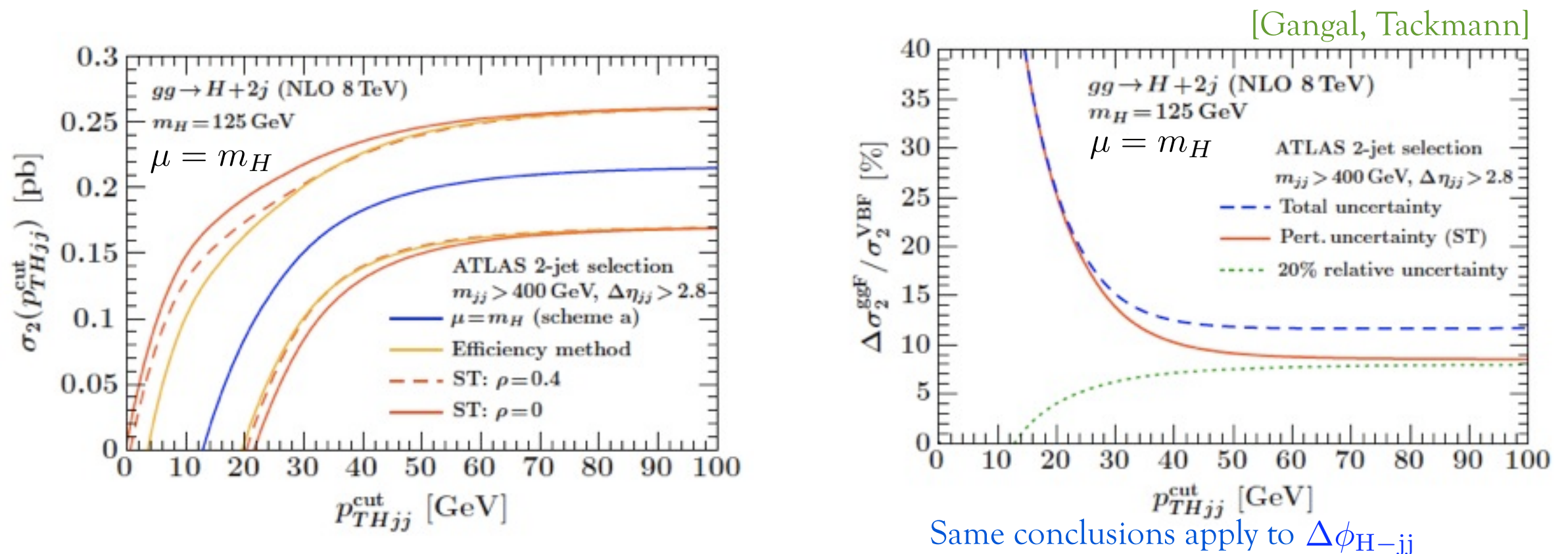
- ▶ Recent analysis for $H \rightarrow \gamma\gamma$ uses $p_{t,Hjj} < 30$ GeV and $\Delta\phi_{H-jj} < 2.6$ rad as jet vetoes
- ▶ Uncertainties with Stewart-Tackmann/Efficiency method

$$\sigma_{2j}(p_{t,Hjj} < p_{t,Hjj}^{\text{cut}}) = \sigma_{\geq 2j} - \sigma_{\geq 3j}(p_{t,Hjj} > p_{t,Hjj}^{\text{cut}})$$

Known @ NLO [Campbell et al.; van Deurzen et al.]

Known @ LO: large relative uncertainty $\sim \mathcal{O}(70\%)$

- ▶ Very large uncertainty on the exclusive 2-jet cross section !



Conclusions

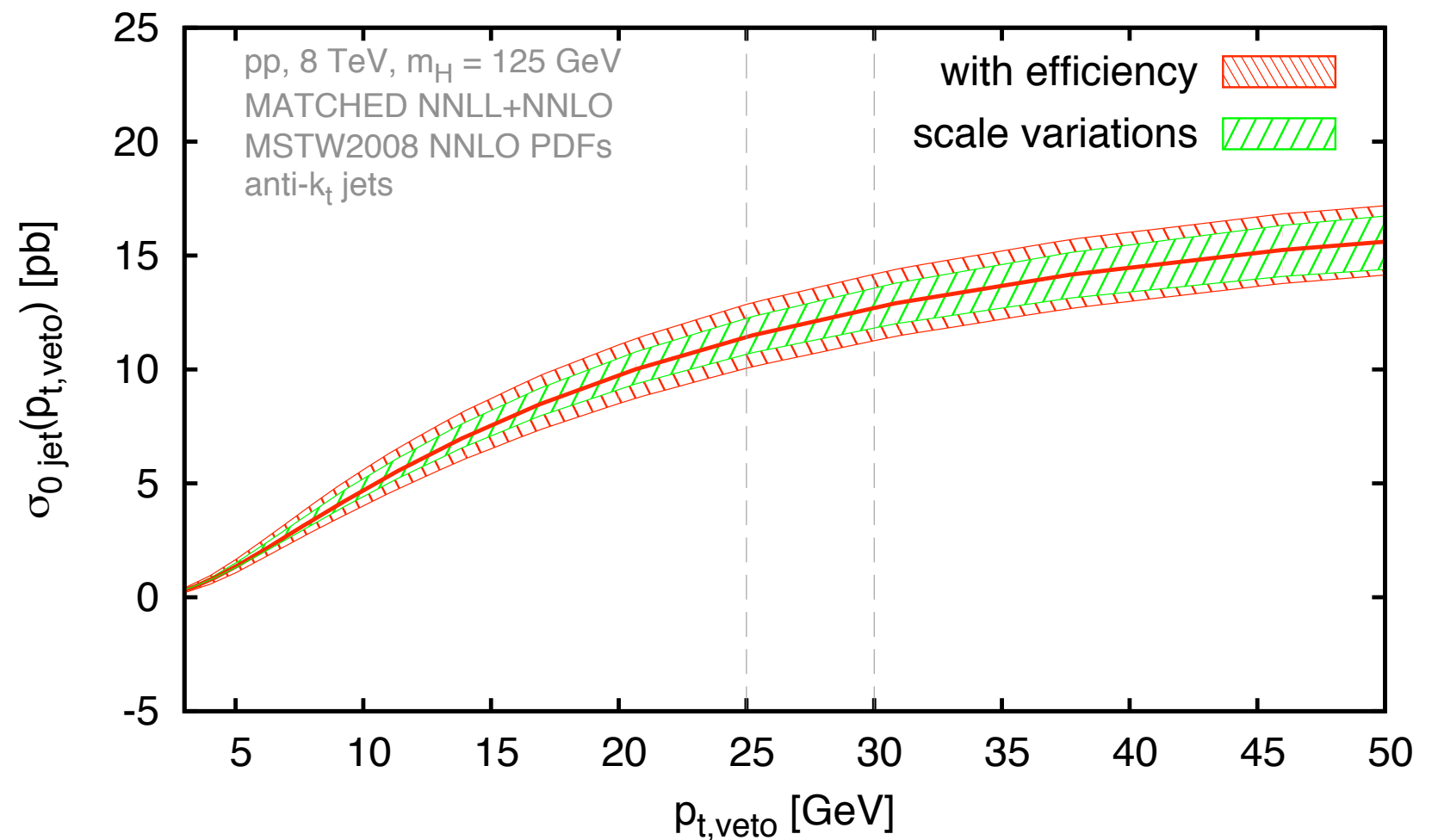
- ▶ Recent progress in resummation of observables involving jets allows for precise assessment of the theory uncertainty (+ efficiency method) in the 0-jet bin. The method can be applied to the production of any colour singlet (e.g. HW, WW, ...)
Public code at: <http://jetvheto.hepforge.org>
 - ▶ Study of all-order small-R structure desirable
- ▶ Recent important progresses for the 1-jet bin. Non-global logarithms and nested resummation are still to be studied in detail
- ▶ The ggF contamination of VBF is still an open issue. H+3j@NLO desirable ?
Several MC analyses currently ongoing using cut-based/multivariate techniques

Backup Slides

Uncertainties in the 0-jet cross section

- ▶ Use resummation (with or without efficiencies) to obtain predictions for the exclusive 0-jet cross section

single matching scheme
in green band

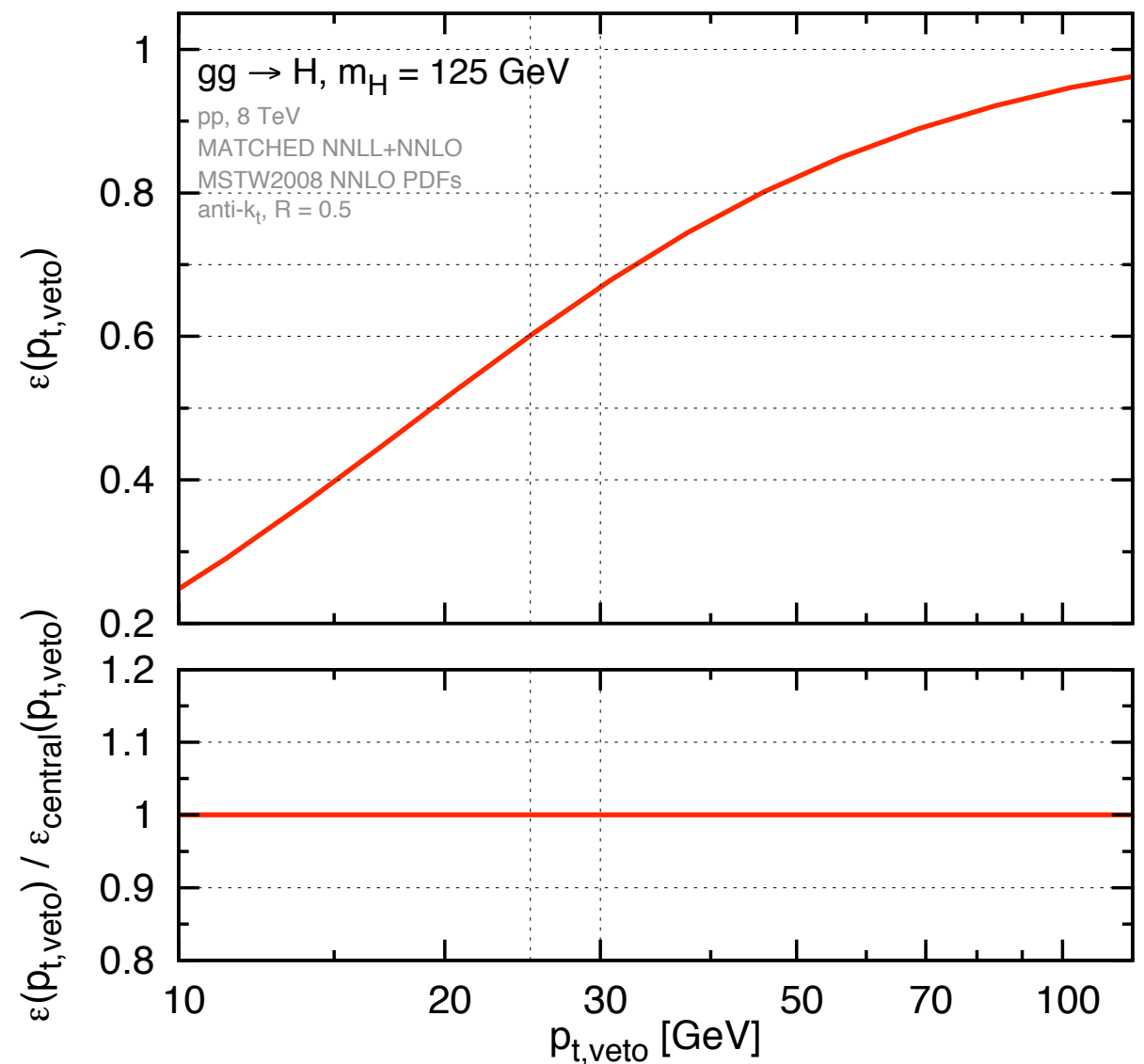


- ▶ Small difference mainly due to matching scheme uncertainty in efficiency method. Robust uncertainty estimate $\sim 10\% - 11\%$

Resummation uncertainties

- ▶ Central value: scheme (a) with

$$\mu_R = \mu_F = Q = M/2$$



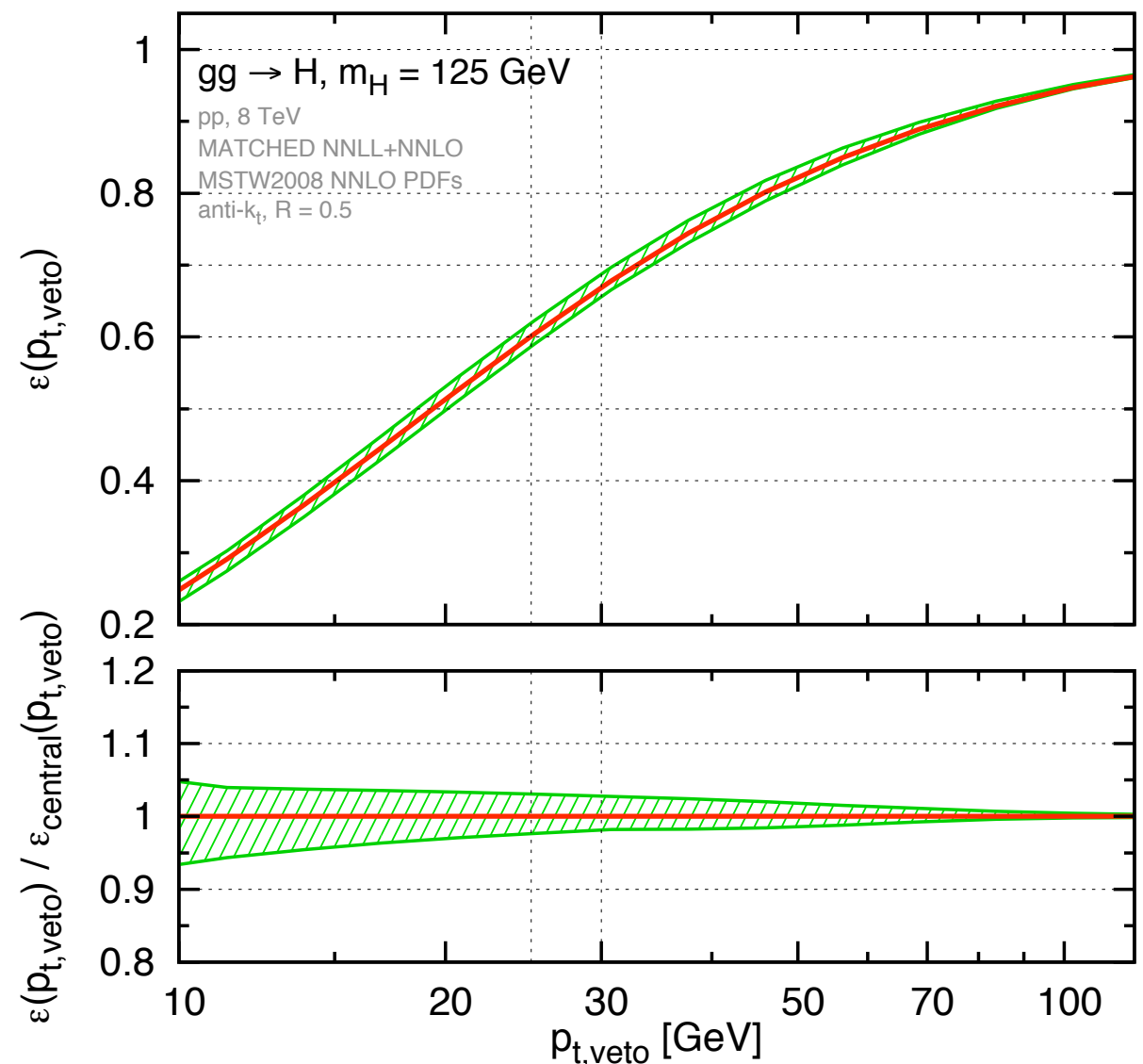
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$$\frac{M}{4} \leq \mu_R, \mu_F \leq M \quad \frac{1}{2} \leq \frac{\mu_R}{\mu_F} \leq 2$$



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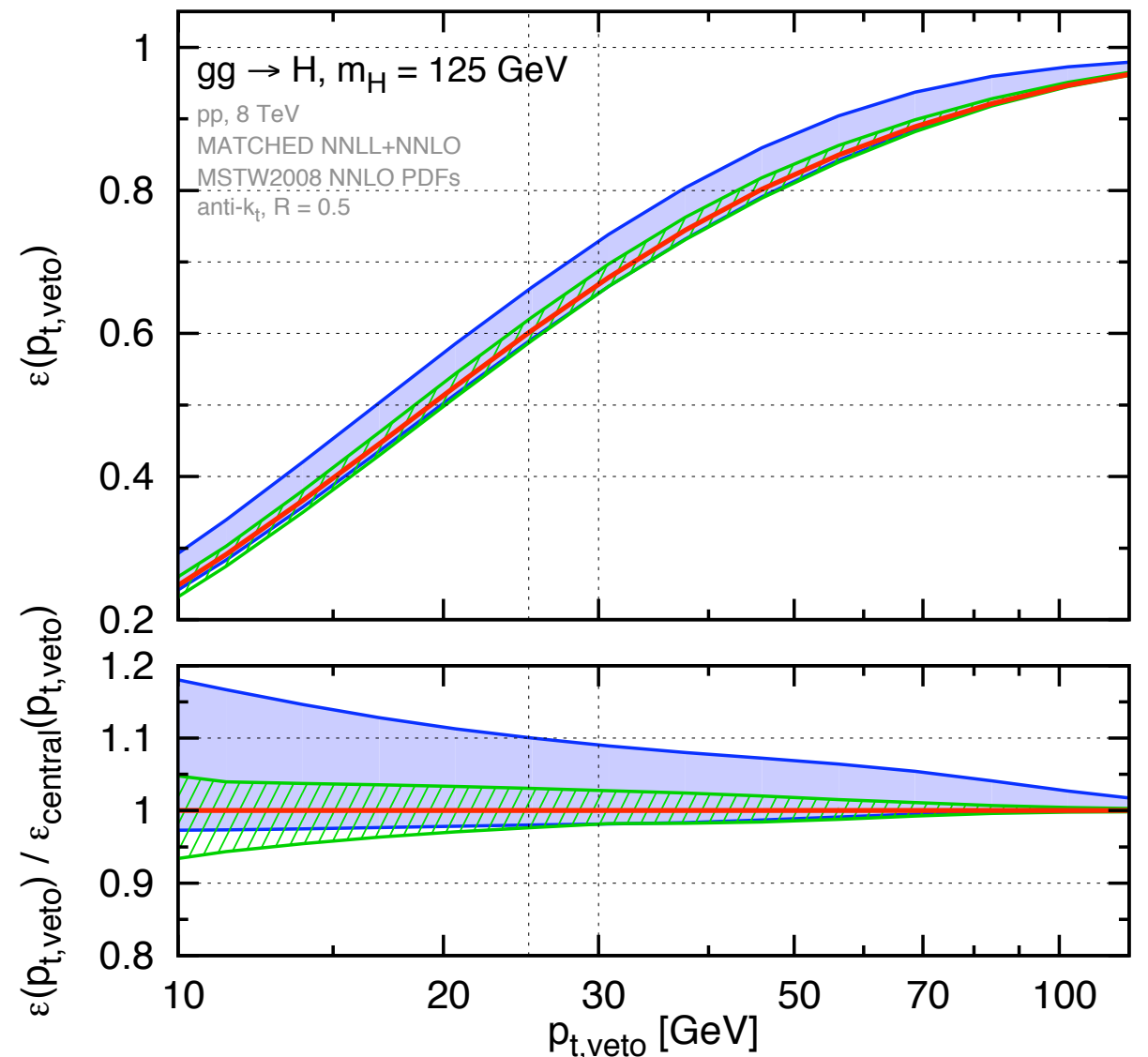
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- ▶ Resummation scale (Q) variation

i.e.

$$\ln \frac{M}{p_{t,\text{veto}}} \rightarrow \ln \frac{Q}{p_{t,\text{veto}}}$$

$$\frac{M}{4} \leq Q \leq M \quad \mu_{R,F} = M/2$$



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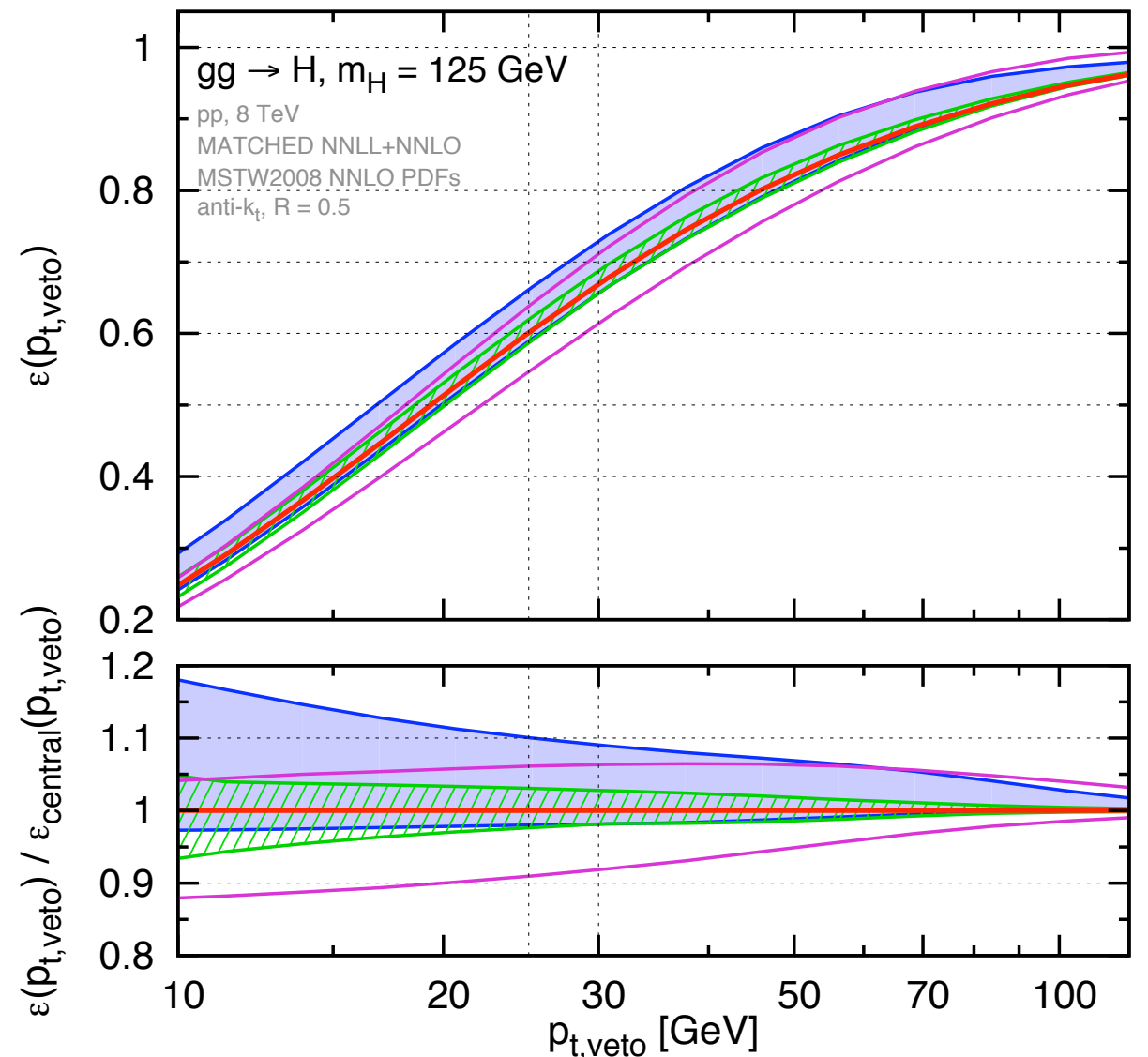
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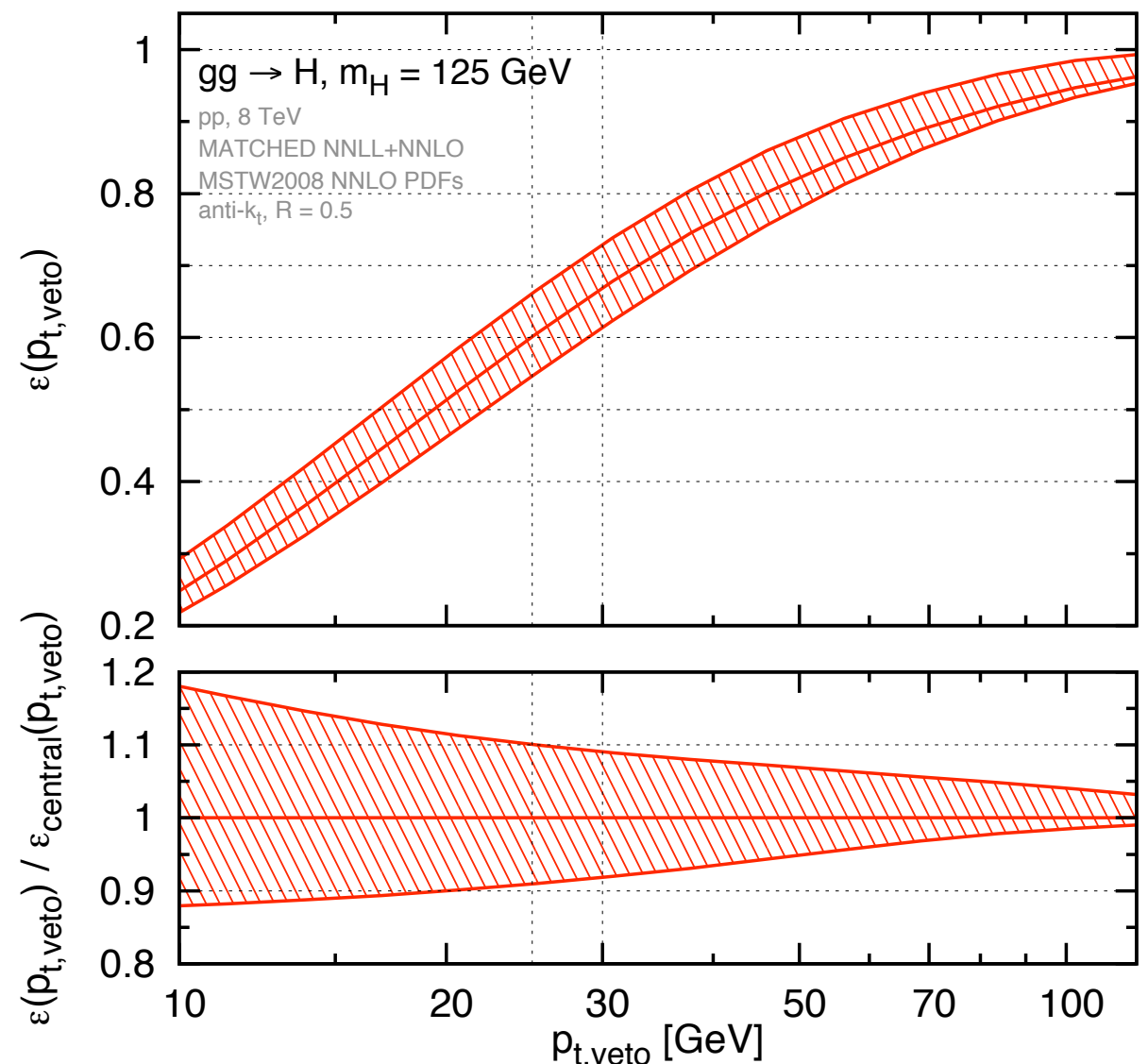
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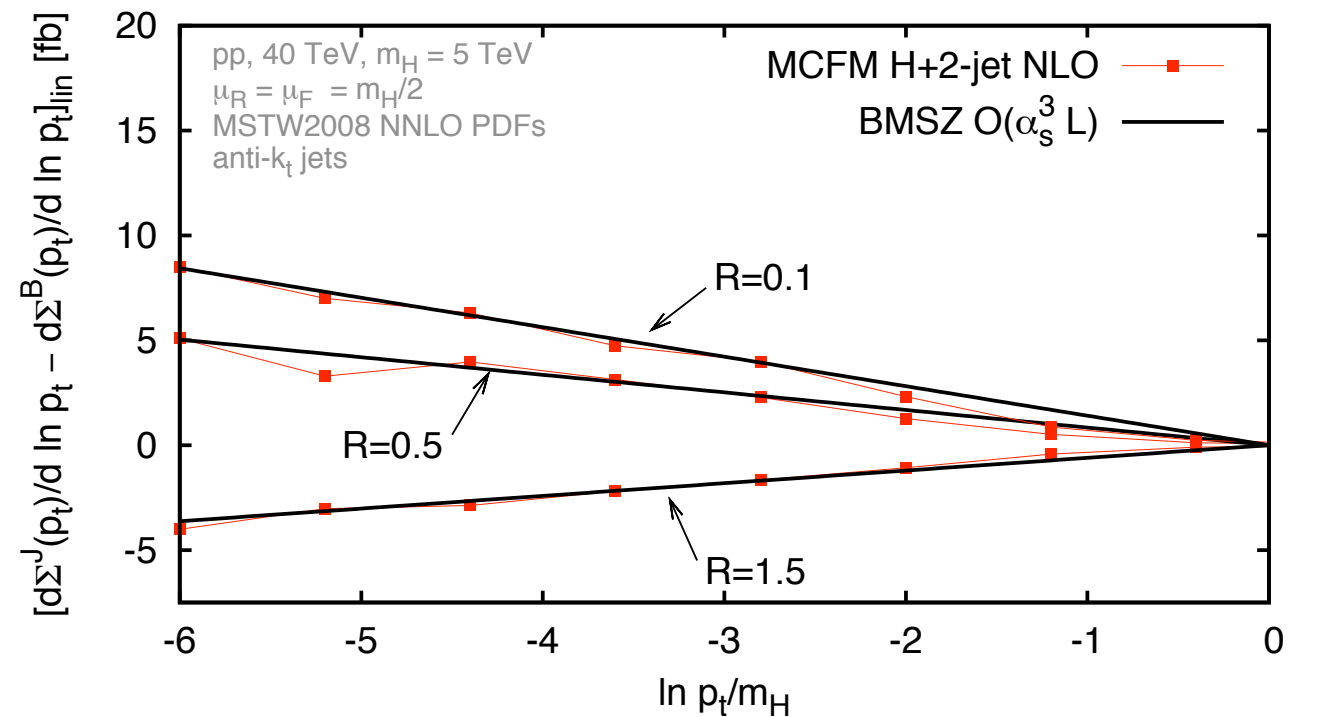
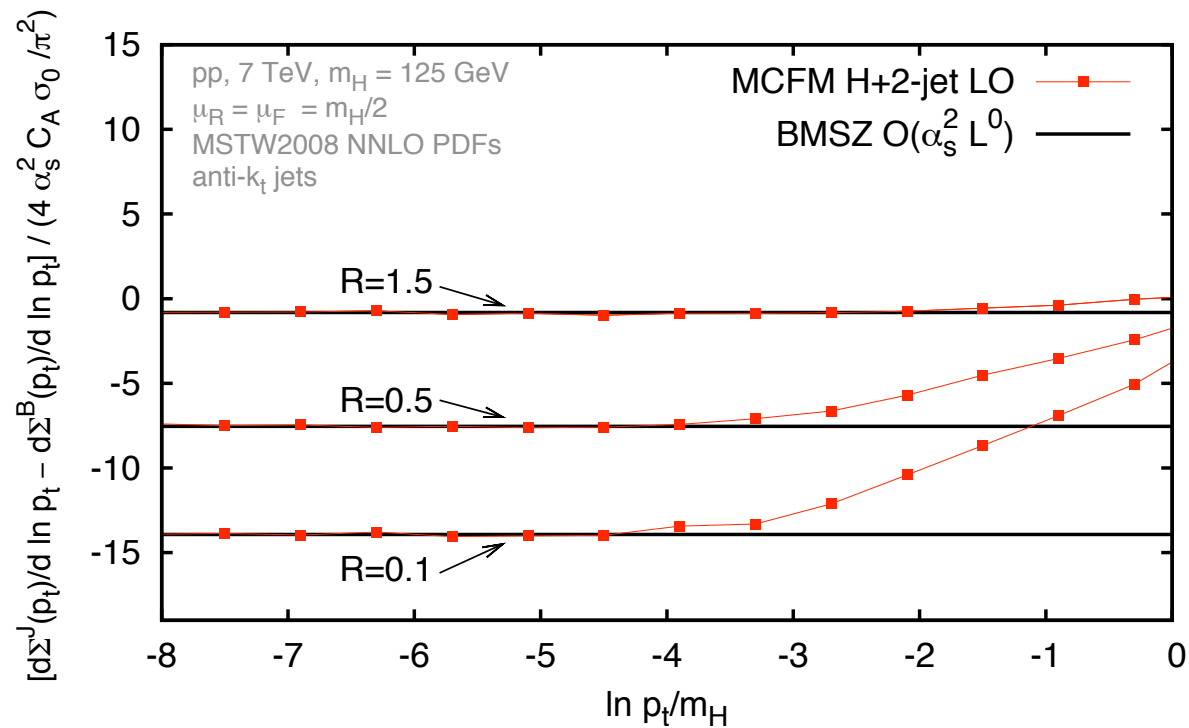
Total uncertainty = envelope



Check against fixed order

- ▶ Check the difference with boson- p_t distribution by comparing expansion of the resummation to MCFM

[Campbell, Ellis, Williams '10]



- ▶ Difference between log-distributions in $p_{t,\text{Higgs}}$ and $p_{t,\text{veto}}$ at order $\mathcal{O}(\alpha_s^2)$ against MCFM's H+2j@LO

$$\Delta \left(\frac{d\Sigma_2(p_t)}{d \ln p_t} \right) \sim \alpha_s^2 L^0$$

- ▶ Difference between log-distributions in $p_{t,\text{Higgs}}$ and $p_{t,\text{veto}}$ at order $\mathcal{O}(\alpha_s^3)$ against MCFM's H+2j@NLO

$$\Delta \left(\frac{d\Sigma_3(p_t)}{d \ln p_t} \right) \sim \alpha_s^3 L^2 + \alpha_s^3 L + \alpha_s^3 L^0$$

Covariance matrix

- ▶ Stewart-Tackmann: $\sigma_{0\text{-jet}} = \sigma_{\text{tot}} - \sigma_{\geq 1\text{-jet}}$, with σ_{tot} and $\sigma_{\geq 1\text{-jet}}$ uncorrelated, gives the covariance matrix

$$\text{COV}_{\text{ST}}[\sigma_{0\text{-jet}}, \sigma_{\geq 1\text{-jet}}] = \begin{pmatrix} \Delta^2 \sigma_{\text{tot}} + \Delta^2 \sigma_{\geq 1\text{-jet}} & -\Delta^2 \sigma_{\geq 1\text{-jet}} \\ -\Delta^2 \sigma_{\geq 1\text{-jet}} & \Delta^2 \sigma_{\geq 1\text{-jet}} \end{pmatrix}$$

- ▶ Jet-veto efficiency: $\sigma_{0\text{-jet}} = \sigma_{\text{tot}} \epsilon$, with σ_{tot} and ϵ uncorrelated, gives

$$\text{COV}_{\text{BMSZ}}[\sigma_{0\text{-jet}}, \sigma_{\geq 1\text{-jet}}] = \begin{pmatrix} \epsilon^2 \Delta^2 \sigma_{\text{tot}} + \sigma_{\text{tot}}^2 \Delta^2 \epsilon & \epsilon(1 - \epsilon) \Delta^2 \sigma_{\text{tot}} - \sigma_{\text{tot}}^2 \Delta^2 \epsilon \\ \epsilon(1 - \epsilon) \Delta^2 \sigma_{\text{tot}} - \sigma_{\text{tot}}^2 \Delta^2 \epsilon & (1 - \epsilon)^2 \Delta^2 \sigma_{\text{tot}} + \sigma_{\text{tot}}^2 \Delta^2 \epsilon \end{pmatrix}$$

$$\text{COV}_{\text{BMSZ}} = \text{COV}_{\text{ST}} + (1 - \epsilon) \Delta^2 \sigma_{\text{tot}} \begin{pmatrix} 2\epsilon & 1 \\ 1 & 0 \end{pmatrix}$$

- ▶ Consistency with the Stewart-Tackmann procedure in the region where the fixed-order is reliable ($\epsilon \lesssim 1$)

Large R limit

- ▶ As $R \rightarrow \infty$ one would (wrongly) expect to recover the boson- p_t result (whole radiation clustered into a single jet)
- ▶ e.g. NNLL correction at $\mathcal{O}(\alpha_s^2 L)$
 - ▶ $\mathcal{F}_{\text{correl}}$ vanishes smoothly in this limit
 - ▶ subtleties arise with two independent emissions ($\mathcal{F}_{\text{indep}}$)
 - ▶ For $1 \ll R \ll \ln(M/p_{t,\text{veto}})$ (jet-veto case) the first emission's rapidity is bounded by $|y_1| \leq \ln M/k_{t,1}$ while $|\Delta y| \leq R + \mathcal{O}(1/R)$

$$\mathcal{F}_{\text{indep}} = -2C_A^2 \frac{\alpha_s^2}{\pi^2} R \zeta_3 + \mathcal{O}\left(\frac{\alpha_s^2 L}{R}\right) \quad \text{N}^3\text{LL}$$

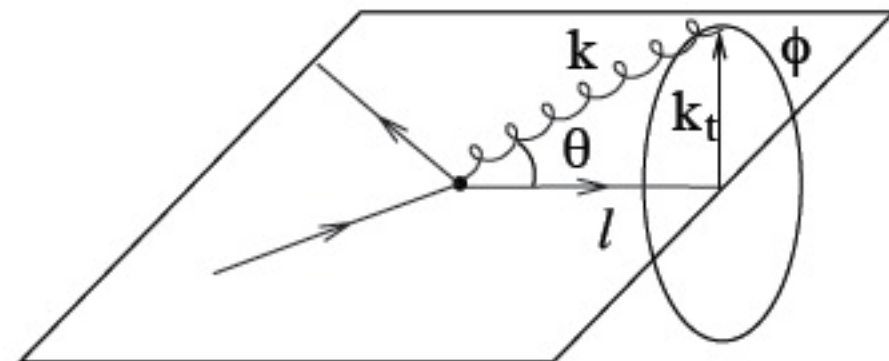
- ▶ For $R \gtrsim \ln(M/p_{t,\text{veto}}) \gg 1$ (boson- p_t) both emissions have $|y_i| \leq \ln \frac{M}{k_{t,1}}$

$$\mathcal{F}_{\text{indep}} = -4C_A^2 \frac{\alpha_s^2}{\pi^2} \zeta_3 \ln \frac{M}{p_t} + \mathcal{O}(\alpha_s^2) \quad \text{NNLL!}$$

Applicability conditions

- ▶ A given observable can be parametrised as follows for a single soft and collinear gluon is emitted off a hard (Born) leg l

$$V(\{p\}, k) = d_l \left(\frac{k_t}{Q} \right)^{a_l} e^{-b_l \eta} g_l(\phi)$$



- ▶ *continuous globalness* : uniform dependence on k_t , independently of the emission direction ($a_1 = a_2 = a_3 = \dots = a$)
- ▶ *recursive Infrared and Collinear (rIRC) safety* : extra emissions do not introduce different soft/collinear scaling

$$\left[\lim_{\bar{v} \rightarrow 0}, \lim_{\zeta \rightarrow 0} \right] \frac{1}{\bar{v}} V(\{p\}, \bar{v}k_1, \bar{v}k_2, \dots, \zeta \bar{v}k_n) = 0$$