

# Anomalous couplings in $\gamma\gamma \rightarrow W^+W^-$ at LHC and ILC

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*in collaboration with*

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# Outline

- 1 Effective Lagrangian approach
- 2 Observables for anomalous couplings in  $\gamma\gamma \rightarrow WW$
- 3 Sensitivities at the LHC
- 4 Sensitivities at the ILC

# Layout

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# The Effective Lagrangian approach

## Anomalous couplings:

- in Standard Model (SM) couplings of  $\gamma$ ,  $W$ ,  $Z$  fixed by:  
gauge invariance & renormalisability
- deviations  $\Rightarrow$  signal for new physics

## Generic descriptions of deviations from SM:

### ① Form Factors

- ▶ allow arbitrary complex couplings for vertices
- ▶ very general, many parameters
- ▶ process specific

### ② Effective Lagrangians

- ▶ add higher dimensional operators
- ▶ real couplings
- ▶ process independent

#### (a) $\mathcal{L}_{\text{eff}}$ after EWSB

- ★ moderate number of couplings for low dim. op.

#### (b) $\mathcal{L}_{\text{eff}}$ before EWSB $\longleftarrow$ here

- ★ few couplings for low dim. op.

# Effective Lagrangian before EWSB

- start from SM Lagrangian (incl. Higgs doublet  $\varphi$ )
- add all higher dim. operators which are
  - ▶ Lorentz-invariant
  - ▶  $SU(3) \times SU(2) \times U(1)$  invariant

$$\Rightarrow \mathcal{L}_{\text{eff}} = \mathcal{L}_0 + \underbrace{\mathcal{L}_1}_{\text{dim 5 op.}} + \underbrace{\mathcal{L}_2}_{\text{dim 6 op.}} + \dots$$

- imposing
  - ▶ equation of motion
  - ▶ lepton and baryon number conservation

$\Rightarrow \mathcal{L}_1$ : none,  $\mathcal{L}_2$ : 80 operators

(*Buchmüller, Wyler 1986*)

# Gauge and gauge-Higgs anomalous couplings

- pure gauge and gauge-Higgs part

$$\mathcal{L}_2 = \frac{1}{v^2} \left( h_W O_W + h_{\tilde{W}} O_{\tilde{W}} + h_{\varphi W} O_{\varphi W} + h_{\varphi \tilde{W}} O_{\varphi \tilde{W}} + h_{\varphi B} O_{\varphi B} + h_{\varphi \tilde{B}} O_{\varphi \tilde{B}} \right. \\ \left. + h_{WB} O_{WB} + h_{\tilde{W}B} O_{\tilde{W}B} + h_\varphi^{(1)} O_\varphi^{(1)} + h_\varphi^{(3)} O_\varphi^{(3)} \right),$$

$$O_W = \epsilon_{ijk} W_\mu^{i\nu} W_\nu^{j\lambda} W_\lambda^{k\mu},$$

$$O_{\tilde{W}} = \epsilon_{ijk} \tilde{W}_\mu^{i\nu} W_\nu^{j\lambda} W_\lambda^{k\mu},$$

$$O_{\varphi W} = \frac{1}{2} (\varphi^\dagger \varphi) W_{\mu\nu}^i W^{i\mu\nu},$$

$$O_{\varphi \tilde{W}} = (\varphi^\dagger \varphi) \tilde{W}_{\mu\nu}^i W^{i\mu\nu},$$

$$O_{\varphi B} = \frac{1}{2} (\varphi^\dagger \varphi) B_{\mu\nu} B^{\mu\nu},$$

$$O_{\varphi \tilde{B}} = (\varphi^\dagger \varphi) \tilde{B}_{\mu\nu} B^{\mu\nu},$$

$$O_{WB} = (\varphi^\dagger \tau^i \varphi) W_{\mu\nu}^i B^{\mu\nu},$$

$$O_{\tilde{W}B} = (\varphi^\dagger \tau^i \varphi) \tilde{W}_{\mu\nu}^i B^{\mu\nu},$$

$$O_\varphi^{(1)} = (\varphi^\dagger \varphi) (\mathcal{D}_\mu \varphi)^\dagger (\mathcal{D}^\mu \varphi),$$

$$O_\varphi^{(3)} = (\varphi^\dagger \mathcal{D}_\mu \varphi)^\dagger (\varphi^\dagger \mathcal{D}^\mu \varphi).$$

- 10 dimensionless anomalous couplings  $h_i$  with

$$h_i \sim \mathcal{O}\left(v^2/\Lambda^2\right),$$

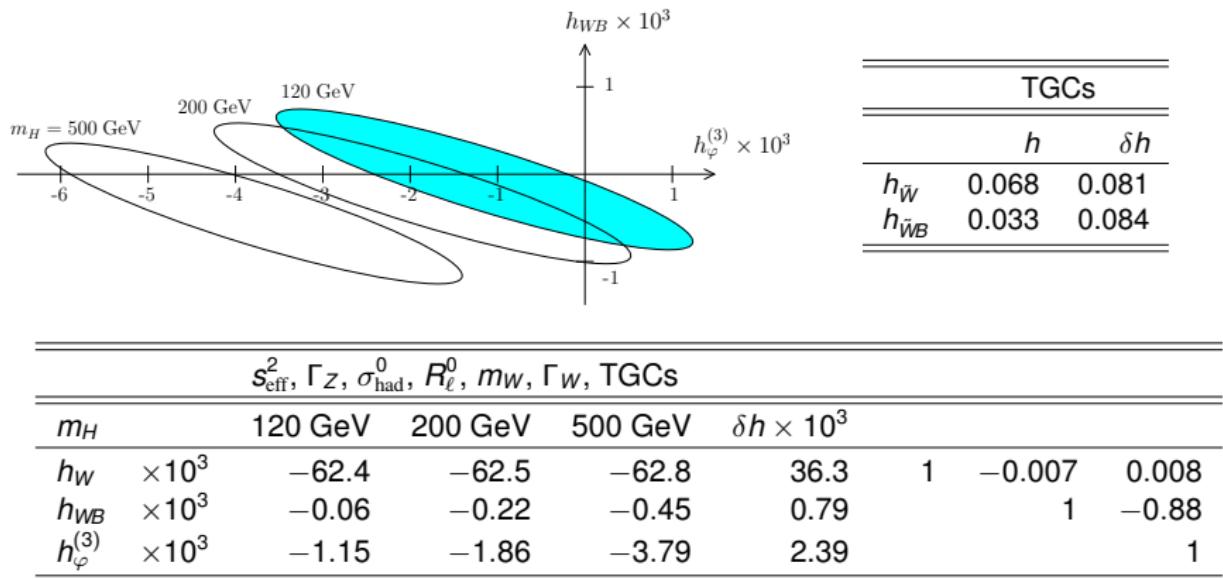
where  $v = 246$  GeV,  $\Lambda$  = new physics scale

- 4 anomalous couplings **CP violating**

# Spontaneous symmetry breaking

- Higgs field  $\varphi$  obtains VEV
- anomalous contrib. to kinetic and mass terms of gauge bosons:
  - ▶ kinetic term:  $h_{\varphi W}$ ,  $h_{\varphi B}$ ,  $h_{WB}$
  - ▶ mass term:  $h_{\varphi}^{(1)}$ ,  $h_{\varphi}^{(3)}$
- get physical  $W^\pm$ ,  $Z$ ,  $\gamma$  fields:
  - ▶ renormalisation of  $W^\pm$
  - ▶ simultaneous diag. of kinetic and mass terms for  $\gamma$ ,  $Z$
- $\Rightarrow$  physical  $W^\pm$ ,  $Z$ ,  $\gamma$  modified wrt. SM
  - ▶ e.g.:  $Z$  decays sensitive to anom. couplings

Present bounds on CP conserving couplings ( $P_Z$ )  
from LEP1, LEP2, SLD, and Tevatron:



## Processes at ILC and LHC

- $e^+e^- \rightarrow Z$  (Giga Z) highly sensitive to ( $P_Z$ ):

$$h_{WB}, h_\varphi^{(3)}$$

- $e^+e^- \rightarrow W^+W^-$  sensitive to ( $P_W$ ):

$$h_W, h_{WB}, h_\varphi^{(3)}, h_{\tilde{W}}, h_{\tilde{WB}}$$

(3 CP conserving, 2 CP violating)

- $\gamma\gamma \rightarrow W^+W^-$  sensitive to ( $P_W$ ):

$$h_W, h_{WB}, h_{\tilde{W}}, h_{\tilde{WB}}, (s_1^2 h_{\varphi W} + c_1^2 h_{\varphi B}), (s_1^2 h_{\varphi \tilde{W}} + c_1^2 h_{\varphi \tilde{B}})$$

(3 CP conserving, 3 CP violating)

- only  $\gamma\gamma$  process allows direct measurement of:

$$h_{\varphi WB} := s_1^2 h_{\varphi W} + c_1^2 h_{\varphi B}$$

$$h_{\varphi \tilde{W}\tilde{B}} := s_1^2 h_{\varphi \tilde{W}} + c_1^2 h_{\varphi \tilde{B}}$$

where  $s_1^2 \equiv \frac{e^2}{4\sqrt{2}G_F m_W^2}$ ,  $c_1^2 \equiv 1 - s_1^2$

- all processes together: 7 out of 10 indep. couplings observable

## Previous work

a lot of excellent work on anomalous couplings in  $\gamma\gamma \rightarrow WW$  exists: e.g. (incomplete)

*Tupper, Samuel (1981),  
Choi, Schrempp (1991),  
Yehudai (1991),  
Bélanger, Boudjema (1992),  
Herrero, Ruiz-Morales (1992),  
Bélanger, Couture (1994),  
Choi, Hagiwara, Baek (1996),  
Baillargeon, Bélanger, Boudjema (1997),  
Piotrzkowski (2001),  
Božović-Jelisavčić, Mönig, Šekarić (2002),  
Bredenstein, Dittmaier, Roth (2004),  
Mönig, Šekarić (2005),  
Nachtmann, Nagel, Pospischil, Utermann (2005),  
de Favereau de Jeneret, Lemaître, Liu, Ovyn, Pierzchała, Piotrzkowski, Rouby, Schul,  
Vander Donckt (in prep.),*

...

see also other talks, in particular by:

D. Zeppenfeld, O. Eboli, T. Pierzchała, O. Kepka, and N. Schul

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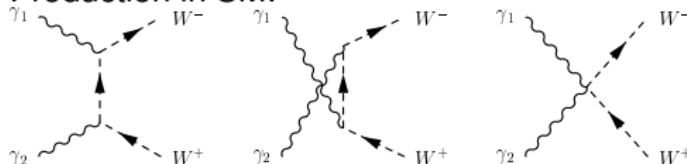
# Feynman diagrams

Consider

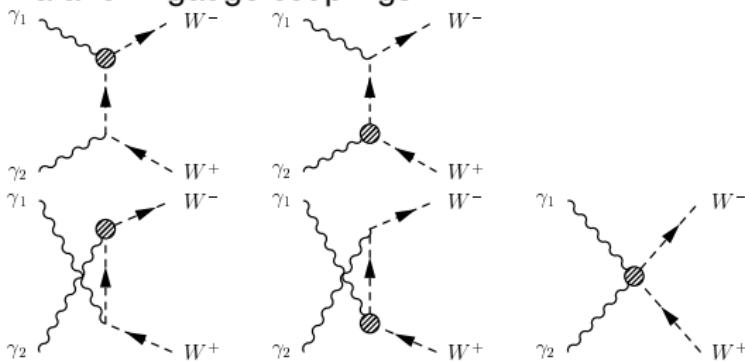
$$\gamma\gamma \rightarrow W^+W^- \rightarrow f\bar{f}f\bar{f}$$

in narrow-width-approximation.

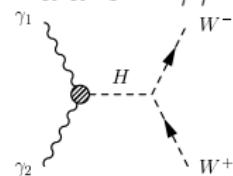
Production in SM:



via anom. gauge couplings:

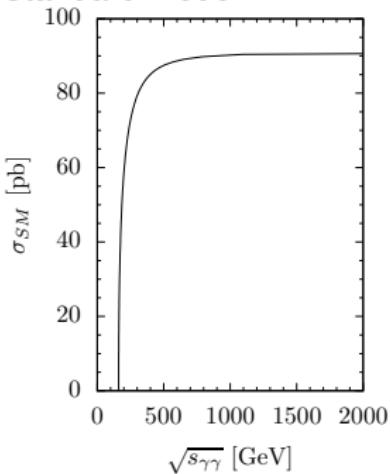


via anom.  $\gamma\gamma H$  coupling:



# Total cross section and energy dependencies

Standard Model:



High energy dependence of leading amplitudes:

$\mathcal{M}_i$	CP even				CP odd		
	SM	$W$	$\varphi W$	$WB$	$\tilde{W}$	$\varphi \tilde{W}$	$\tilde{W}B$
LL	$1^{(*)}$	$\gamma^{-2}$	1	$\gamma^2(\dagger)$	$\gamma^{-2}$	1	$\gamma^2(\dagger)$
TL	$\gamma^{-1}$	$\gamma^{-1}$	0	$\gamma$	$\gamma^{-1}$	0	$\gamma$
TT	1	1	$\gamma^{-2}$	1	1	$\gamma^{-2}$	1

where  $\gamma := \sqrt{s_{\gamma\gamma}}/(2m_W)$ ,

(\*) for  $(\lambda_1 = -\lambda_2)$ ,

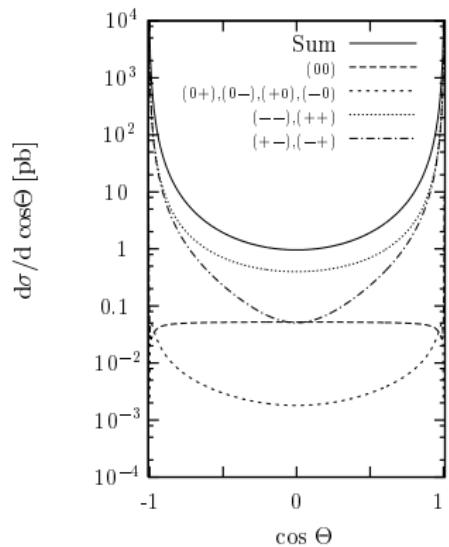
(†) for  $(\lambda_1 = \lambda_2)$ ,

- up to  $\gamma^2$  enhancements for anomalous amplitudes
- CP odd only at quadratic order

diff. cross section:

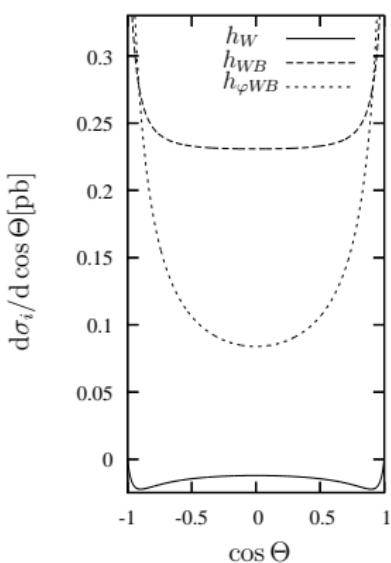
$$\frac{d\sigma}{d \cos \Theta} = \frac{d\sigma_{SM}}{d \cos \Theta} + \sum_i h_i \frac{d\sigma_i}{d \cos \Theta} + \mathcal{O}(h^2)$$

Standard Model:

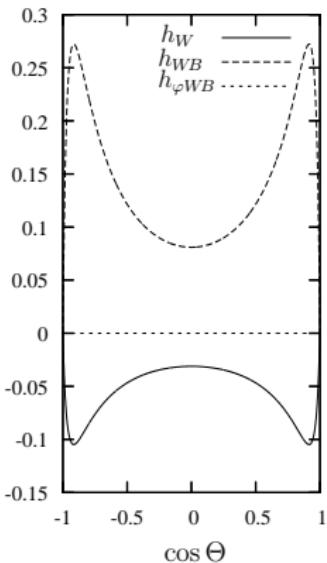


Anomalous CP even:

$$(\lambda_3, \lambda_4) = (0, 0)$$



$$(\lambda_3, \lambda_4) = (0, \pm), (\pm, 0)$$



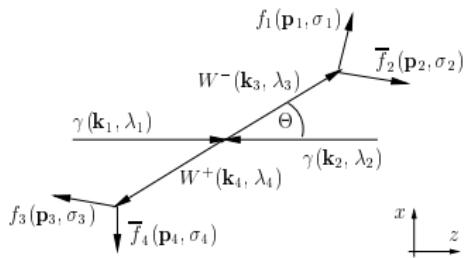
- no CP odd in linear order

Full information: diff. cross section incl.  $W$  decays

$$S(\phi) \equiv \frac{d\sigma}{d \cos \Theta d \cos \vartheta d\varphi d \cos \bar{\vartheta} d\bar{\varphi}} = \frac{3^2 \beta}{2^{11} \pi^3 s} B_{12} B_{34} P_{\lambda'_3 \lambda'_4}^{\lambda_3 \lambda_4} D_{\lambda'_3}^{\lambda_3} \bar{D}_{\lambda'_4}^{\lambda_4}$$

where  $\phi$  = phase space variables

$\Rightarrow$  access to  $\mathcal{O}(h)$  contrib. for all  $h_i$ .



How to measure anom. coupl. with best statistical accuracy ?  $\Rightarrow$  optimal observables

- expand diff. cross section:

$$\frac{d\sigma}{d\phi} = S_0(\phi) + \sum_i h_i S_{1i}(\phi) + \mathcal{O}(h^2) \quad \text{where} \quad \begin{aligned} h_i &= \text{anomalous couplings} \\ \phi &= \text{phase space variables} \end{aligned}$$

- statist. optimal observables for small  $h_i$  (wo/ rate info):

$$\mathcal{O}_i \equiv \frac{S_{1i}(\phi)}{S_0(\phi)}$$

- measure  $\phi_k$  for each event  $k = 1, \dots, N$ , evaluate:

$$\bar{\mathcal{O}}_i = \frac{1}{N} \sum_k \mathcal{O}_i(\phi_k)$$

and calculate  $c_{ij} \equiv \langle (\mathcal{O}_i - \langle \mathcal{O}_i \rangle_0)(\mathcal{O}_j - \langle \mathcal{O}_j \rangle_0) \rangle_0$  with  $\langle \circ \rangle_0 = \frac{\int d\phi S_0(\phi) \circ}{\int d\phi S_0(\phi)}$   
to get estimate of couplings

$$h_i = \sum_j c_{ij}^{-1} (\bar{\mathcal{O}}_j - \langle \mathcal{O} \rangle_0)$$

- covariance matrix for  $h_i$  computable without data

$$V(h) = \frac{1}{N} c_{ij}^{-1}$$

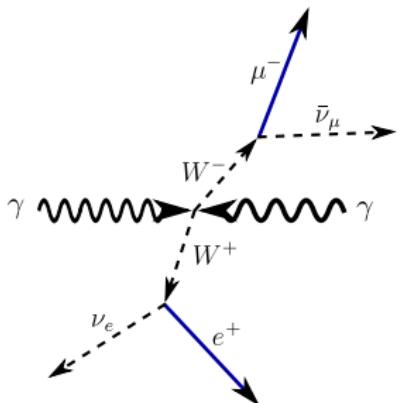
## Choice of final states

- center-of-mass system not fixed in photon production
- loss of kinem. information  $\Rightarrow$  treatable with opt. observ., but: lower sensitivities
- balance: signature, branching ratio, available information

type	signature	branching ratio	kinem. information
leptonic ( $l = e, \mu$ )	++	4/81	-
semi-leptonic ( $l = e, \mu$ )	+	24/81	+
hadronic	-	36/81	(++)

Leptonic final state:

- if CMS known: full reconstruction of final state
- if CMS unknown: no rec. possible



## Choice of final states

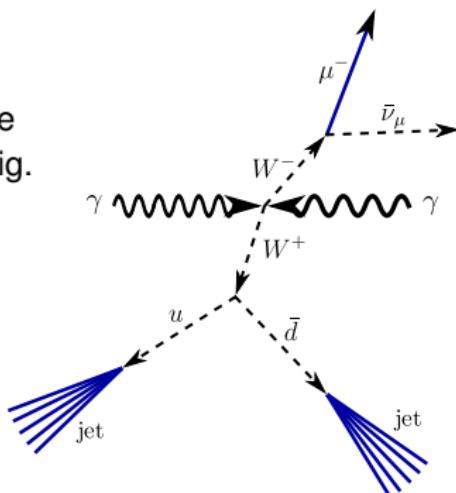
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leptonic ( $l = e, \mu$ )	++	4/81	-
semi-leptonic ( $l = e, \mu$ )	+	24/81	+
hadronic	-	36/81	(++)

Semi-leptonic final state:

- if CMS known: full reconstruction of final state
- if CMS unknown: rec. up to 4-fold discr. ambig.

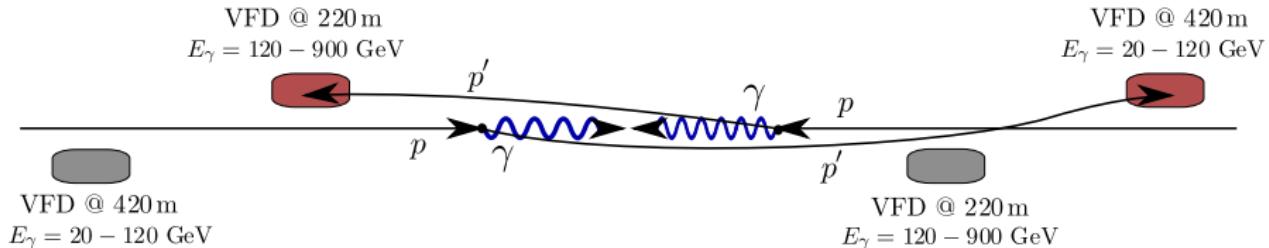
- neutrino momentum unknown
- transverse reconstruction unique
- two-fold ambiguity for neutrino energy  
(for part of phase space)
- two-fold jet ambiguity if  $q$  flavour ID missing
- $\Rightarrow$  reconstruction possible  
up to 4-fold discrete ambiguity



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# High energy photon production at the LHC

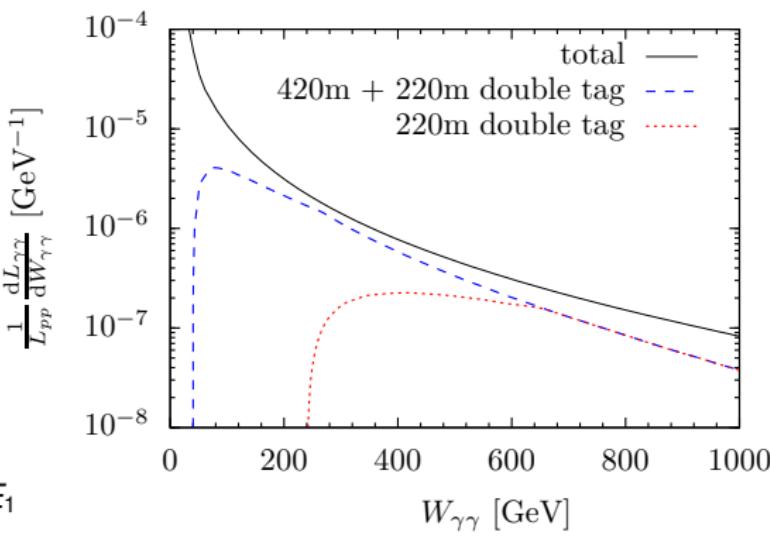


Budnev, Ginzburg, Meledin, Serbo

- almost real photons by elastic radiation off  $p$
- tagging: large rap. gaps or very forward detectors (VFD)
- $d\sigma_{pp} \approx d\sigma_{\gamma\gamma} dN_1 dN_2$  (EPA)

- def. photon luminosity  $L_{\gamma\gamma}$  ( $Q^2$  integrated), then:

$$\begin{aligned}\sigma_{pp} &= \int \sigma_{\gamma\gamma}(W_{\gamma\gamma}, E_1) \times \\ &\times \frac{1}{L_{pp}} \frac{\partial^2 L_{\gamma\gamma}(W_{\gamma\gamma}, E_1)}{\partial W_{\gamma\gamma} \partial E_1} dW_{\gamma\gamma} dE_1\end{aligned}$$



# Parameters, cuts and covariance matrix features

## Choices and assumptions:

- fully leptonic decays  $\Rightarrow$  clean signature
- double tag for both  $p$   $\Rightarrow$  full reconstr. of final state
- $m_{Higgs} = 120$  GeV

## Cuts:

- both charged leptons:  $|\eta| \leq 2.5$
- both charged leptons:  $p_T \geq 10$  GeV
- both photons:
  - ▶  $120 \text{ GeV} \leq E_\gamma \leq 900 \text{ GeV}$  for “VFD 220m”, or
  - ▶  $20 \text{ GeV} \leq E_\gamma \leq 900 \text{ GeV}$  for “VFD 220m + 420m”

## Covariance matrix:

- CP even - CP odd correlations vanish

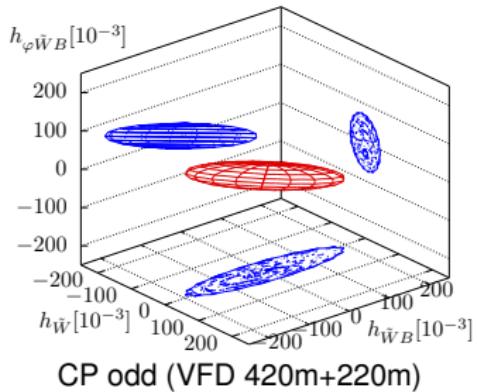
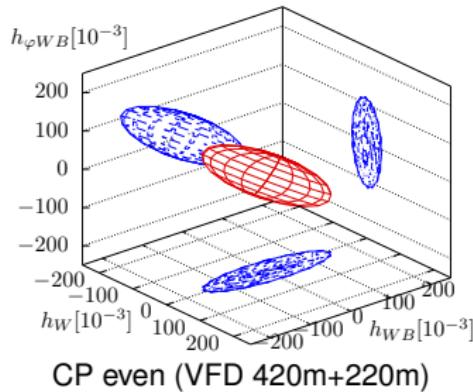
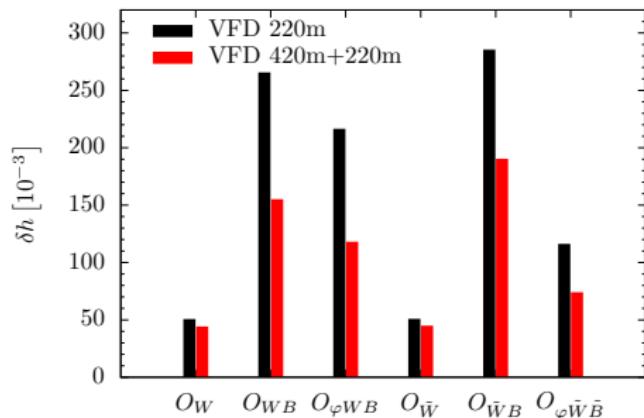
# Results: Sensitivities at the LHC

elastic spectrum, leptonic channels, double tag VFD

preliminary

$$\int L_{pp} = 30 \text{ fb}^{-1},$$

# accept. events =  
 26 (VFD 220m),  
 94 (VFD  
 420m+220m)



# Results: Sensitivities at the LHC

preliminary

elastic spectrum, comparison of channels

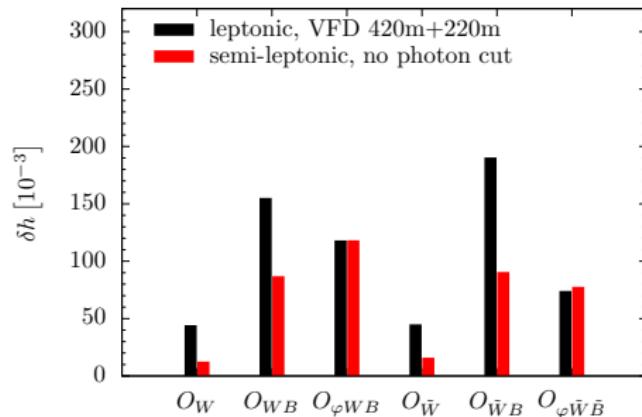
- semi-leptonic measurements more difficult (background)
- but:
  - ▶ VFD tagging not crucial for reconstruction of final state
  - ▶ gain color factor 3 in event rate
- interesting (at low lumi) ?

$$\int L_{pp} = 30 \text{ fb}^{-1};$$

# accept. events =

94 lept. (VFD 420m+220m),  
538 semi-lept. (no photon cut);

jet cuts as for  $I^\pm$



But this means for  $\int L_{pp} = 1 \text{ fb}^{-1}$ :

- only 18 semi-lept. events
- sensitiv. worse by factor of 5.5 wrt. fig.

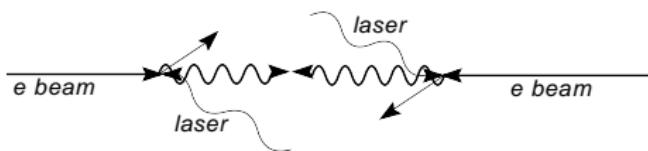
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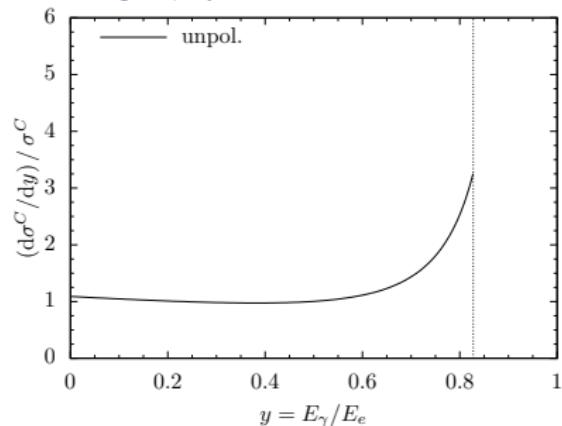
# Unpolarised Compton spectrum

Ginzburg, Kotkin, Panfil, Serbo, Telnov

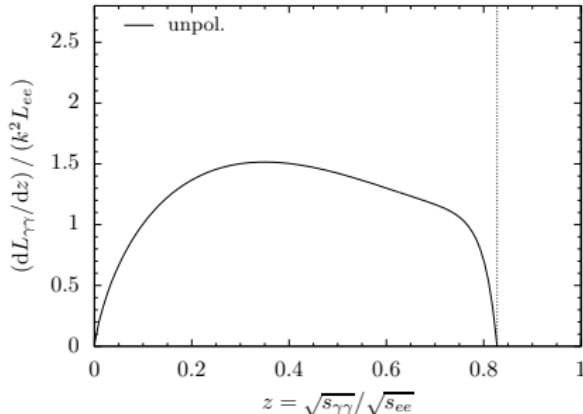
Photons via Compton backscattering of laser on  $e$  beam



norm. single  $\gamma$  spectrum:



norm.  $\gamma\gamma$  luminosity spectrum:



# Parameters, cuts and covariance matrix features

## Parameters and cuts:

- semi-leptonic, no jet id  $\Rightarrow$  discrete ambiguities in reconstr.
- $m_{Higgs} = 120 \text{ GeV}$
- cuts on observed fermions:
  - ▶ fermion energy  $\geq 10 \text{ GeV}$
  - ▶ fermion angle wrt. beam  $\geq 10^\circ$
  - ▶ angle betw. fermions  $\geq 25^\circ$

## Covariance matrix:

- CP even - CP odd correlations vanish
- calculation in presence of ambiguities:
  - ▶ use **Jacobi-weighted** sums over experim. equivalent states
  - ▶ integrate sums over unique phase space

(general discussion: *Nachtmann, Nagel, Pospischil*)

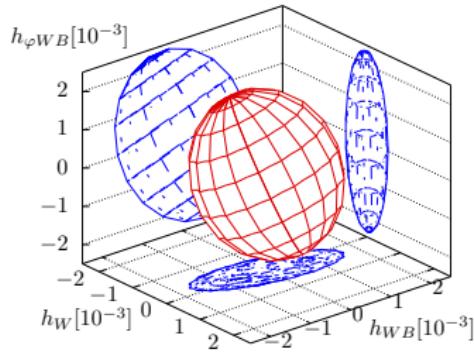
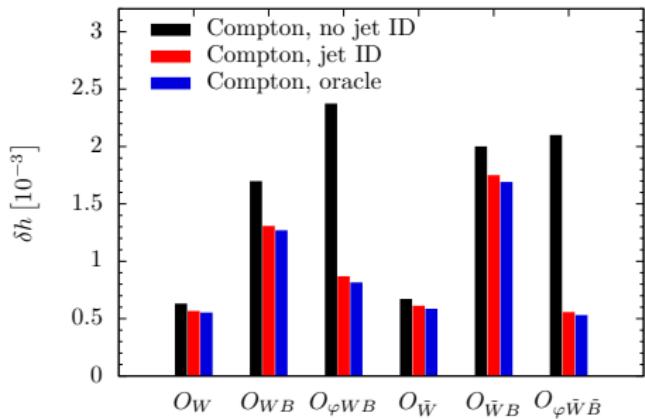
# Results: Sensitivities at the ILC

preliminary

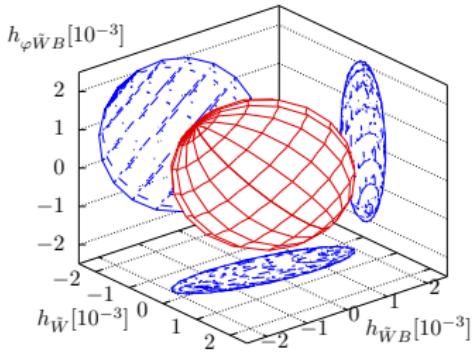
unpolarised Compton spectrum, semi-leptonic channels

$$\int L_{ee} = 500 \text{ fb}^{-1};$$

$$\# \text{ accept. events} = 2.25 \cdot 10^6$$



CP even (Compton, no jet id)



CP odd (Compton, no jet id)

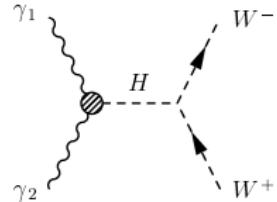
## Possible improvements

Expect higher accuracies from

- higher energies
- polarised  $\gamma\gamma$  initial state

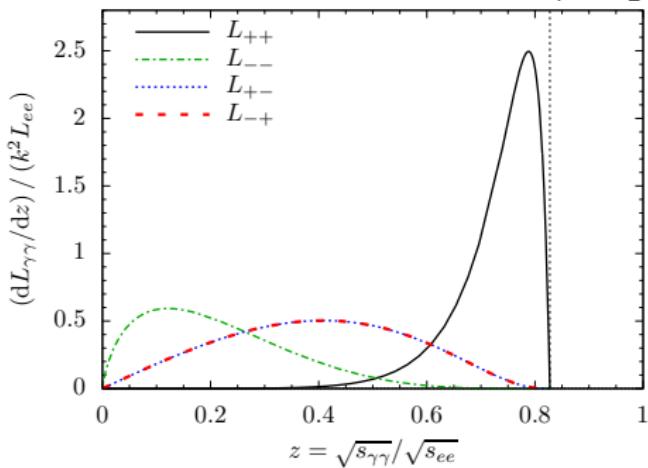
Polarisation ( $\sim$  more information) disentangles different contributions:

- increased differences in angular distributions
- even “switch off terms” completely:  
e.g.: no Higgs production for  $\lambda_1 = -\lambda_2$ , that is  $|J_z| = 2$



## Effective polarisation of hard $\gamma\gamma$

Norm. luminosity spectra for different helicities for choice  $\lambda_1^e = \lambda_2^e = 1/2$ ,  $P_1^C = P_2^C = -1$ :



Polarisation of hard  $\gamma\gamma$ :

- **high energy** enhancement
- polarisation strongly energy dependent  
(multiple scattering destroys pol. at lower energies)

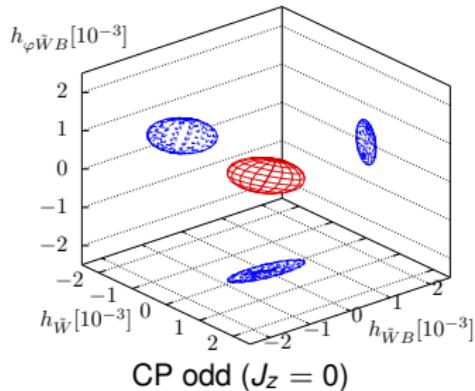
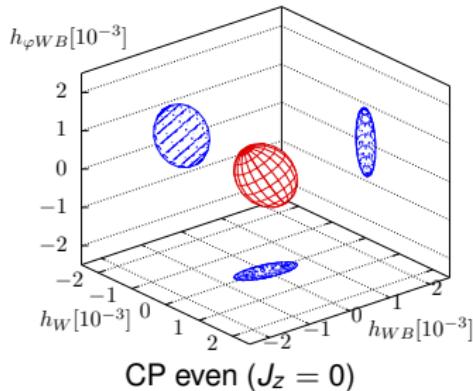
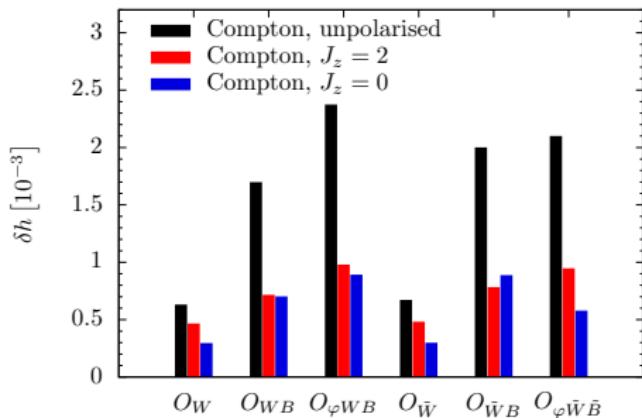
# Results: Sensitivities at the ILC

polarised Compton spectrum, semi-leptonic channels

preliminary

$$\int L_{ee} = 500 \text{ fb}^{-1};$$

# accept. events =  
 $2.25 \cdot 10^6$  (unpol),  
 $2.29 \cdot 10^6$  ( $J_z = 2$ ),  
 $2.61 \cdot 10^6$  ( $J_z = 0$ )



# Comparison of sensitivities

preliminary

present	LHC estimates	ILC estimates
LEP, SLD, Tevatron (*) $h_i [10^{-3}]$	$\gamma\gamma \rightarrow WW$ leptonic $\delta h_i [10^{-3}]$	$ee \rightarrow WW$ (*) $\gamma\gamma \rightarrow WW$ unpolarised $\delta h_i [10^{-3}]$

measurable CP conserving couplings:

$h_W$	$-69 \pm 39$	44	0.3	0.6	0.3
$h_{WB}$	$-0.06 \pm 0.79$	155	0.3	1.7	0.7
$h_{\varphi WB}$	$\times$	118	$\times$	2.4	0.9
$h_{\varphi}^{(3)}$	$-1.15 \pm 2.39$	$\times$	36.4	$\times$	$\times$

measurable CP violating couplings:

$h_{\tilde{W}}$	$68 \pm 81$	45	0.3	0.7	0.3
$h_{\tilde{W}B}$	$33 \pm 84$	190	2.2	2.0	0.9
$h_{\varphi \tilde{W}\tilde{B}}$	$\times$	74	$\times$	2.1	0.6

3 more anomalous couplings unaccessible by these methods:

$$h_{\varphi}^{(1)}, h'_{\varphi WB}, h'_{\varphi \tilde{W}\tilde{B}}$$

(\*) Nachtmann, Nagel, Pospischil

- best for  $h_{WB}, h_{\varphi}^{(3)}$ : Giga Z

## Summary

### Effective Lagrangian approach:

- parametrisation of deviations from SM by new high energy physics
- process independent
- 10 anomalous gauge / gauge-Higgs couplings (6 CP cons., 4 CP viol.)
- LEP, SLD & Tevatron restrict 5 of them
- substantial improvements by  $ee \rightarrow WW$ , Giga-Z at ILC

### Norm. distrib. for $\gamma\gamma \rightarrow WW$ :

- access to 2 new anom. Higgs couplings (not in  $ee \rightarrow WW$ )
- sensitive to 6 anom. couplings
- allows important cross checks with  $ee$  data
- LHC:  
first access to 2 new anom. Higgs coupl.,  
supplements existing data with  $\delta h \approx \mathcal{O}(10^{-1})$
- ILC:  
sensitivities  $\delta h \approx \mathcal{O}(10^{-3})$ ,  
approx. factor 2 better with polarisation