

# An unbroken dark $U(1)$ and phenomenology

["arXiv: 1303.4280" (accepted for JHEP) collaborated with [Seungwon Baek](#) and [Pyungwon Ko](#)]

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# Why is the DM stable?

- Stability is guaranteed by a symmetry.

e.g:  $Z_2$ , R-parity, Topology

- A global symmetry is broken by gravitational effects, allowing interactions like

$$-\mathcal{L}_{\text{int}} = \begin{cases} \lambda \frac{\phi}{M_{\text{P}}} F_{\mu\nu} F^{\mu\nu} & \text{for boson} \\ \lambda \frac{1}{M_{\text{P}}} \bar{\psi} \gamma^\mu D_\mu \ell_{Li} H^\dagger & \text{for fermion} \end{cases}$$

Observation requires [M.Ackermann et al. (LAT Collaboration), PRD 86, 022002 (2012)]

$$\tau_{\text{DM}} \gtrsim 10^{26-30} \text{sec} \Rightarrow \begin{cases} m_\phi \lesssim \mathcal{O}(10) \text{keV} \\ m_\psi \lesssim \mathcal{O}(1) \text{GeV} \end{cases}$$

- Weak scale DM requires a local symmetry.

# Discrete or continuous?

- Discrete symmetry

- The symmetry may be originated from a **spontaneously broken continuous symmetry** (e.g: **local  $Z_2$** -symmetry).
- Dark matter should have **nothing to do with the symmetry breaking**.
- It should be the **lightest odd** particle.

- Continuous symmetry

- It may be from a large gauge group in a UV theory (e.g:  $SO(32)$  or  $E_8 \times E_8' \rightarrow SU(3)_c \times SU(2)_L \times U(1)_Y \times G_{DS}?$ ).
- Dark matter should be the **lightest (dark) charged** particle.

# Unbroken local $U(1)_X$

- **DM self-interaction**

It may solve some puzzles of the collisionless CDM.

- core/cusp problem: [S.-H Oh et al., arXiv:1011.0899]

simulated cusp of DM density profile contrary to the cored one found in the observed LSB galaxies and dSphs

- “too big to fail” problem: [M. Boylan-Kolchin et al., arXiv:1111.2048]

simulated high internal density concentration of the subhalos in the MW-sized halos contrary to the observed brightest MW satellites

- **Massless dark photon**

Contributes to the radiation energy in addition to the one from SM.

$$N_{\text{eff}}^{\text{obs}} = 3.30 \pm 0.27 \text{ at } 68\% \text{ (cf., } N_{\text{eff}}^{\text{SM}} = 3.04)$$

⇒ Fractional contribution of dark photon is still allowed.



# SM-DM communication

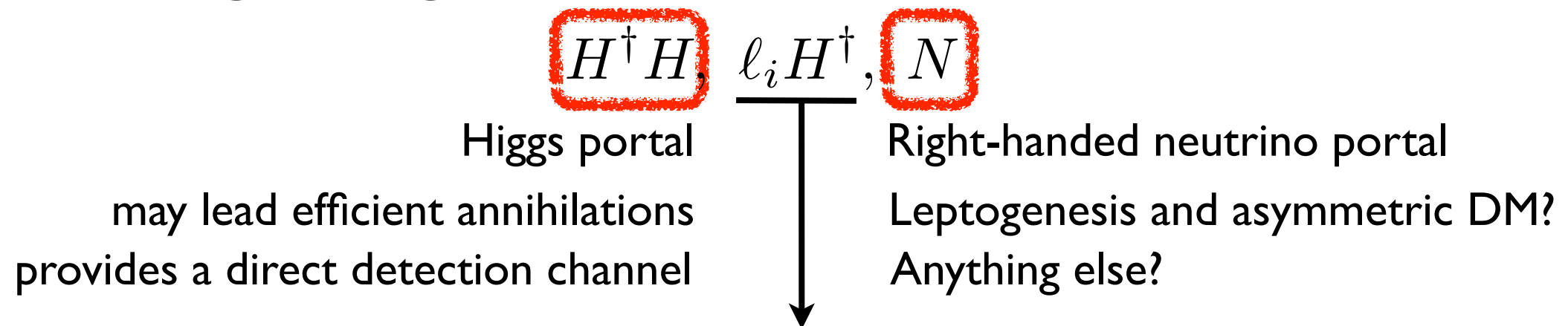
- Kinetic mixing

There could be the kinetic mixing between  $U(1)_X$  and  $U(1)_Y$  of the SM.  
 $\Rightarrow$  DM becomes **mini-charged** under the electromagnetic interaction.

$$\mathcal{L} \supset -\frac{1}{2} \sin \epsilon X_{\mu\nu} B^{\mu\nu} \quad \Rightarrow \quad q_{\text{em}} = -q_X \frac{g_X}{e} \cos W \tan \epsilon$$

$\Rightarrow$  This opens a direct detection channel.

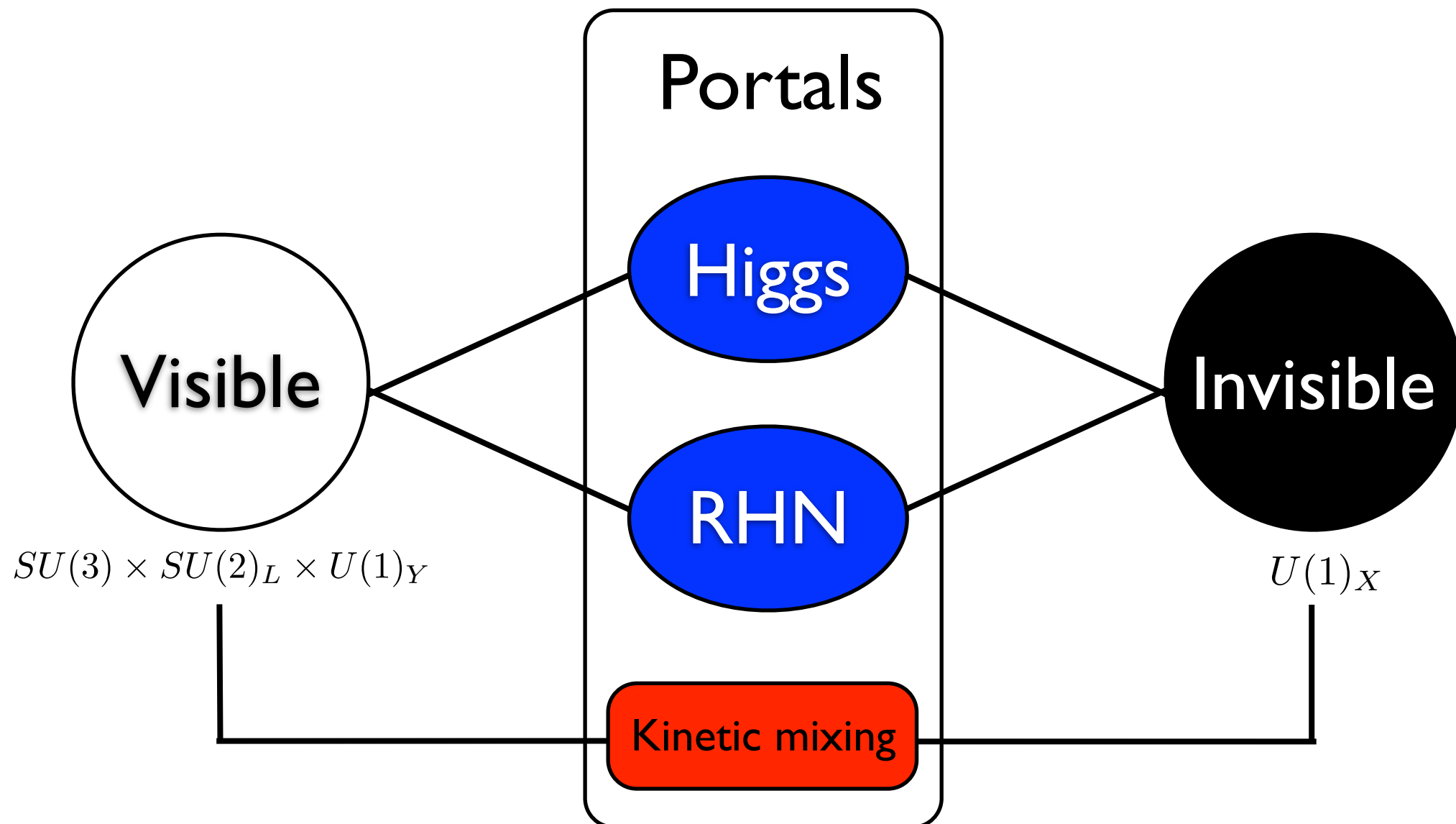
- Gauge-singlets



does not allow renormalizable interactions for a gauge-charged DM

# A minimal(?) model

- The structure of the model



- Symmetry

$$SU(3) \times SU(2)_L \times U(1)_Y \times U(1)_X$$

(SM is neutral under  $U(1)_X$ )

[See also A. Falkowski, J.T. Ruderman & T. Volansky, JHEP1105.016]

- Lagrangian

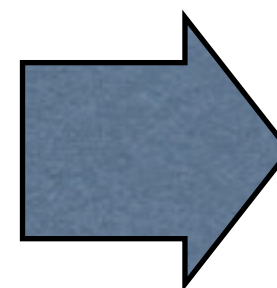
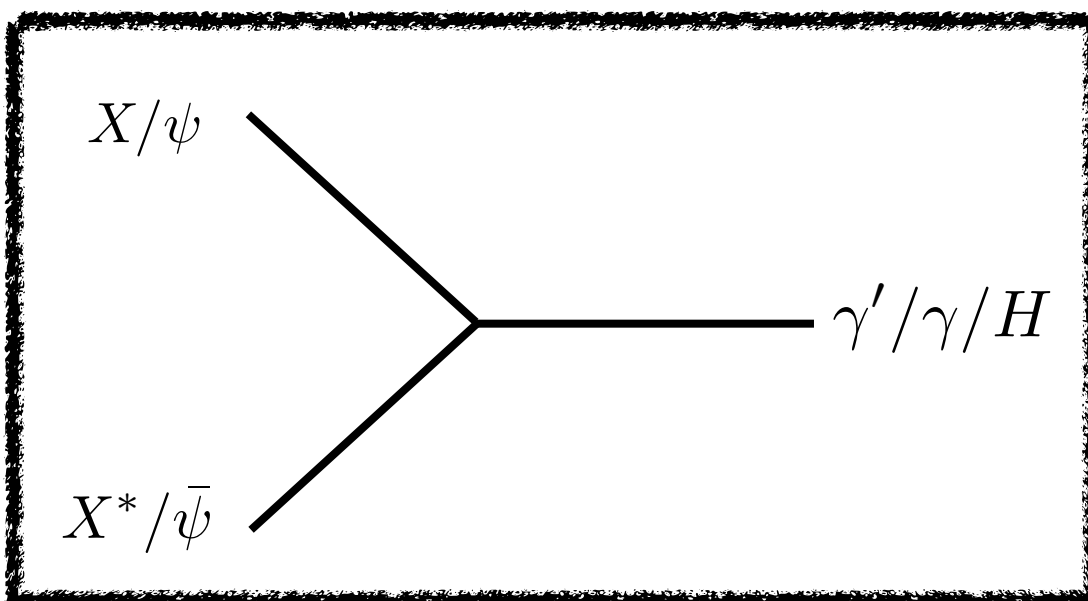
$$\begin{aligned} \mathcal{L} &= \mathcal{L}_{\text{Kinetic}} + \mathcal{L}_{\text{H-portal}} + \mathcal{L}_{\text{RHN-portal}} + \mathcal{L}_{\text{DS}} \\ \mathcal{L}_{\text{Kinetic}} &= i\bar{\psi}\gamma^\mu D_\mu\psi + |D_\mu X|^2 - \frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{1}{2}\sin\epsilon X_{\mu\nu}B^{\mu\nu} \\ -\mathcal{L}_{\text{H-portal}} &= \frac{1}{2}\lambda_{HX}|X|^2 H^\dagger H \\ -\mathcal{L}_{\text{RHN-portal}} &= \frac{1}{2}M_i N_{Ri}^{\bar{C}} N_{Ri} + [Y_\nu^{ij} N_{Ri}^{\bar{C}} \ell_{Lj} H^\dagger + \lambda^i N_{Ri}^{\bar{C}} \psi X^\dagger + \text{H.c.}] \\ -\mathcal{L}_{\text{DS}} &= m_\psi \bar{\psi}\psi + m_X^2 |X|^2 + \frac{1}{4}\lambda_X |X|^4 \end{aligned}$$

$$(q_L, q_X) : N = (1, 0), \psi = (1, 1), X = (0, 1)$$

# ● Interaction vertices of dark particles ( $X, \psi$ )

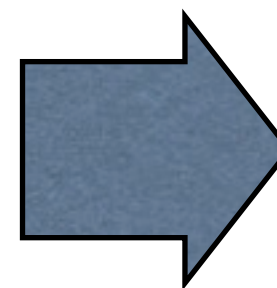
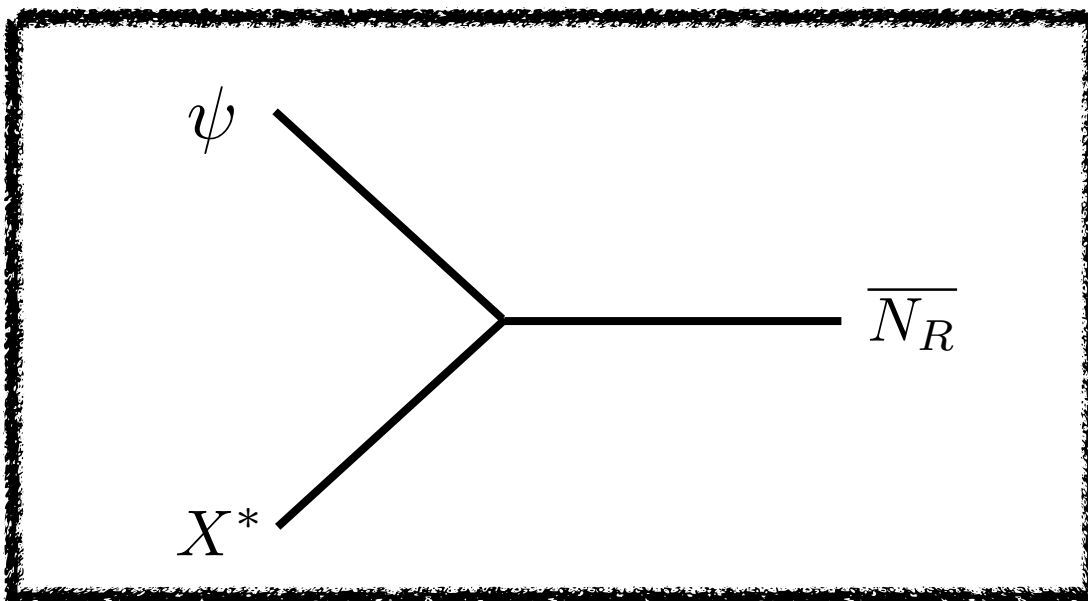
Kinetic term diagonalization: 
$$\begin{pmatrix} \hat{B}^\mu \\ \hat{X}^\mu \end{pmatrix} = \begin{pmatrix} 1/\cos \epsilon & 0 \\ -\tan \epsilon & 1 \end{pmatrix} \begin{pmatrix} B^\mu \\ X^\mu \end{pmatrix}$$

$\Rightarrow \mathcal{L}_{\text{DS-SM}} = g_X q_X t_\epsilon \bar{\psi} \gamma^\mu \psi (c_W A_\mu - s_W Z_\mu) + |[\partial_\mu - ig_X q_X t_\epsilon (c_W A_\mu - s_W Z_\mu)] X|^2$



Annihilation  
or  
scattering

( $\Rightarrow$  Relic density, direct/indirect searches)



Decay of  $N_R$  and  $\psi$  or  $X$   
( $\Rightarrow$  Lepto/darkogenesis?)

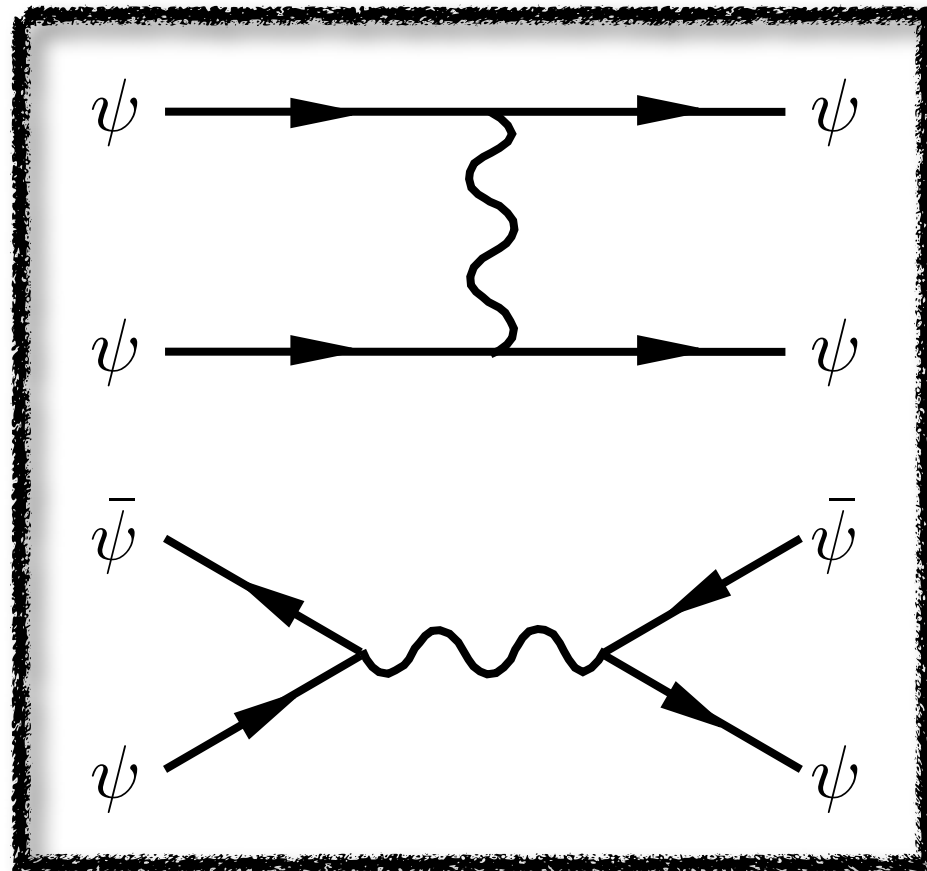
# Phenomenology ( $\approx$ constraints)

Our model can address

- \* Some small scale puzzles of CDM (Dark matter self-interaction) ( $\alpha_X, m_X$ )
- \* CDM relic density (Unbroken dark  $U(1)_X$ ) ( $\lambda, \lambda_{hx}, m_X$ )
- \* Vacuum stability of Higgs potential (Positive scalar loop correction) ( $\lambda_{hx}$ )
- \* Direct detection (Photon and Higgs exchange) ( $\epsilon, \lambda_{hx}$ )
- \* Dark radiation (Massless photon) ( $\alpha_X$ )
- \* Lepto/darkogenesis (Asymmetric origin of dark matter) ( $Y_\nu, \lambda, M_I, m_X$ )
- \* Inflation (Higgs inflation type) ( $\lambda_{hx}, \lambda_X$ )

In other words, the model is highly constrained.

# ● Constraints on dark gauge coupling



$$\Rightarrow \sigma_T \sim \frac{16\pi\alpha_X^2}{m_{X(\psi)}^2} \frac{1}{v^4} \ln \left[ \frac{m_{X(\psi)}^2 v^3}{\sqrt{4\pi\rho_{X(\psi)}}\alpha_X^3} \right]$$

From inner structure and kinematics of dwarf galaxies,

$$\sigma_T^{\max} / m_{\text{dm}} \lesssim 35 \text{ cm}^2 / \text{g}$$

[Vogelsberger, Zavala and Leb, 1201.5892]

$$\Rightarrow \alpha_X \lesssim 5 \times 10^{-5} \left( \frac{m_{X(\psi)}}{300\text{GeV}} \right)^{3/2}$$

☛ If stable,  $\Omega_\psi \sim 10^4 (300\text{GeV}/m_\psi) \gg \Omega_{\text{CDM}}^{\text{obs}} \simeq 0.26$ .

“ $m_\psi > m_X$ ”  $\Rightarrow$   $\Psi$  decays.

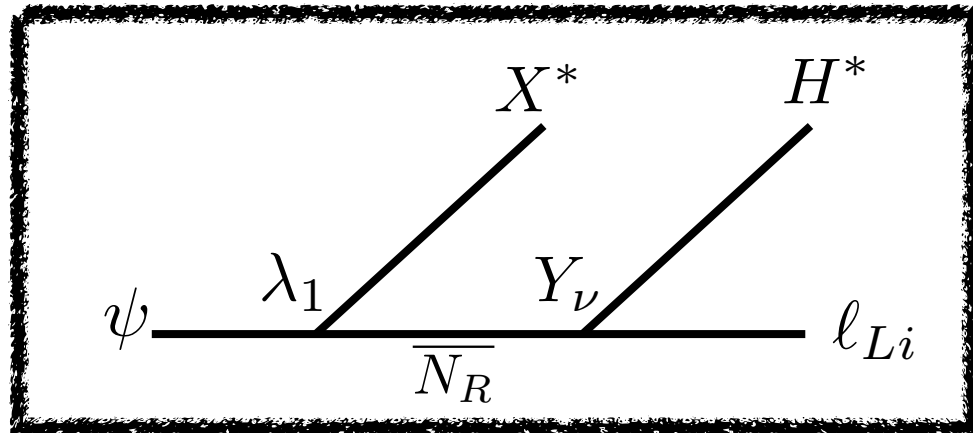
“X”(the scalar dark field) = CDM

☛ For  $\alpha_X$  close to its upper bound,  $X$ - $X^*$  can explain some puzzles of collisionless CDM:

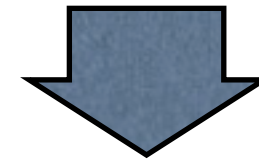
(i) cored profile of dwarf galaxies.

(ii) low concentration of LSB galaxies and dwarf galaxies. [Vogelsberger, Zavala and Leb, 1201.5892]

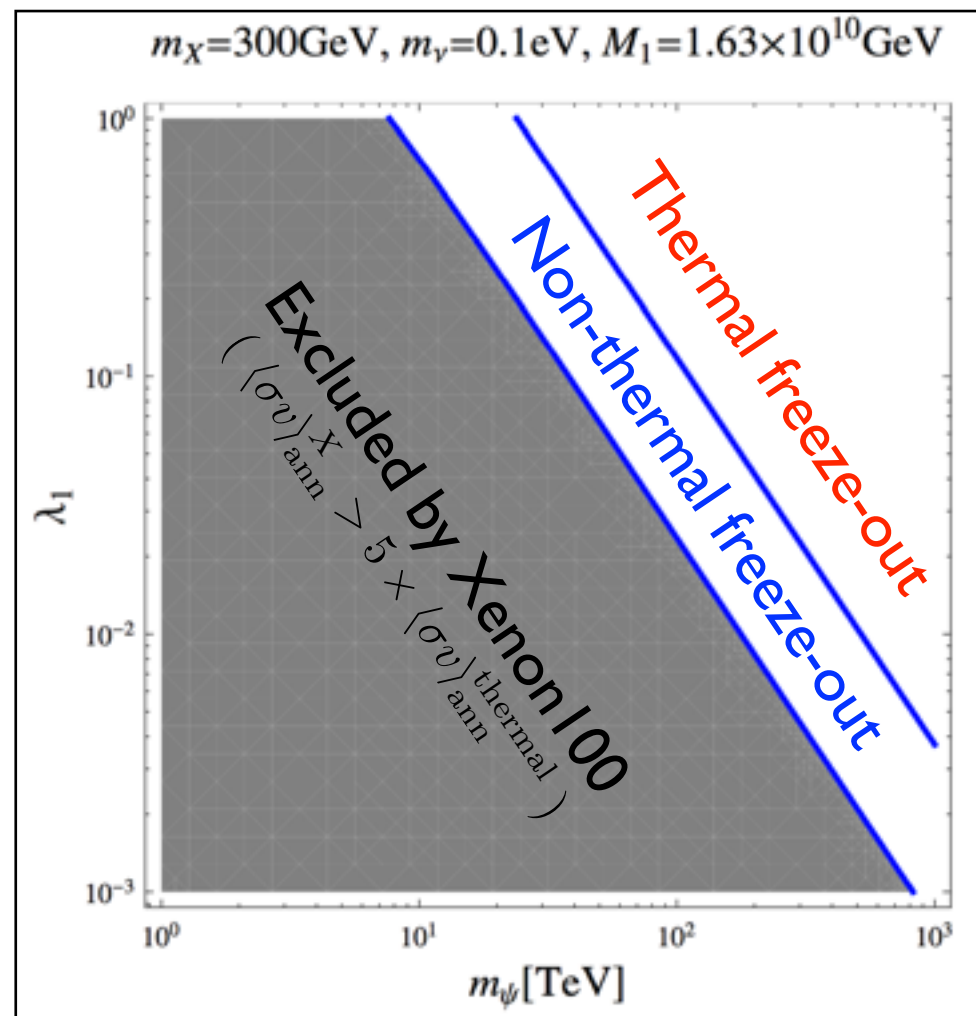
- CDM relic density



The late-time decay of  $\psi$

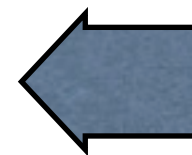


X forms a symmetric DM.  
(Non-) thermal freeze-out of X via Higgs portal



Thermal ( $T_d^\psi > T_{fz}^X$ ) :  $\langle \sigma v \rangle_{\text{ann}}^X = \langle \sigma v \rangle_{\text{ann}}^{\text{thermal}}$

Nonthermal ( $T_d^\psi < T_{fz}^X$ ) :  $\langle \sigma v \rangle_{\text{ann}}^X \sim \Gamma_d^\psi / n_X^{\text{obs}}$



$$\lambda_1 = \lambda_1(m_\psi, \langle \sigma v \rangle_{\text{ann}}^X, \dots)$$



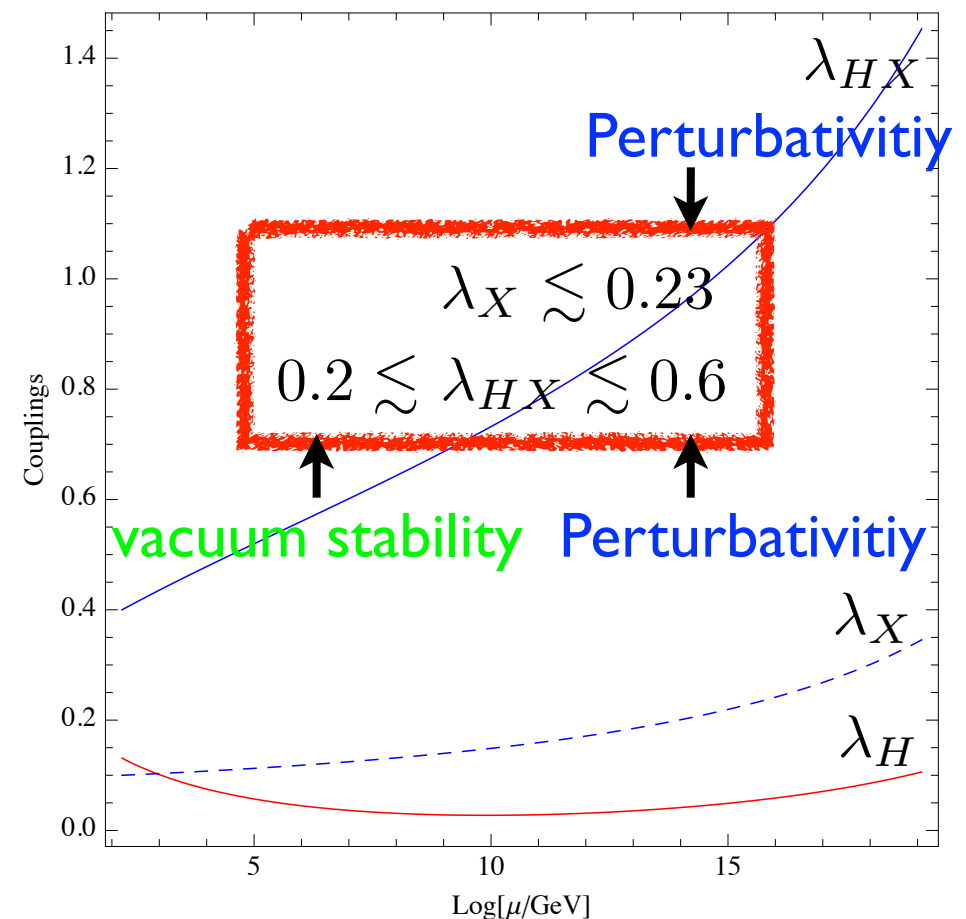
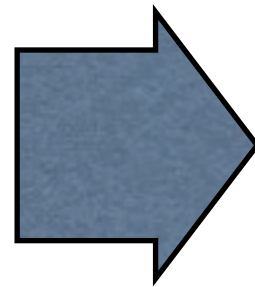
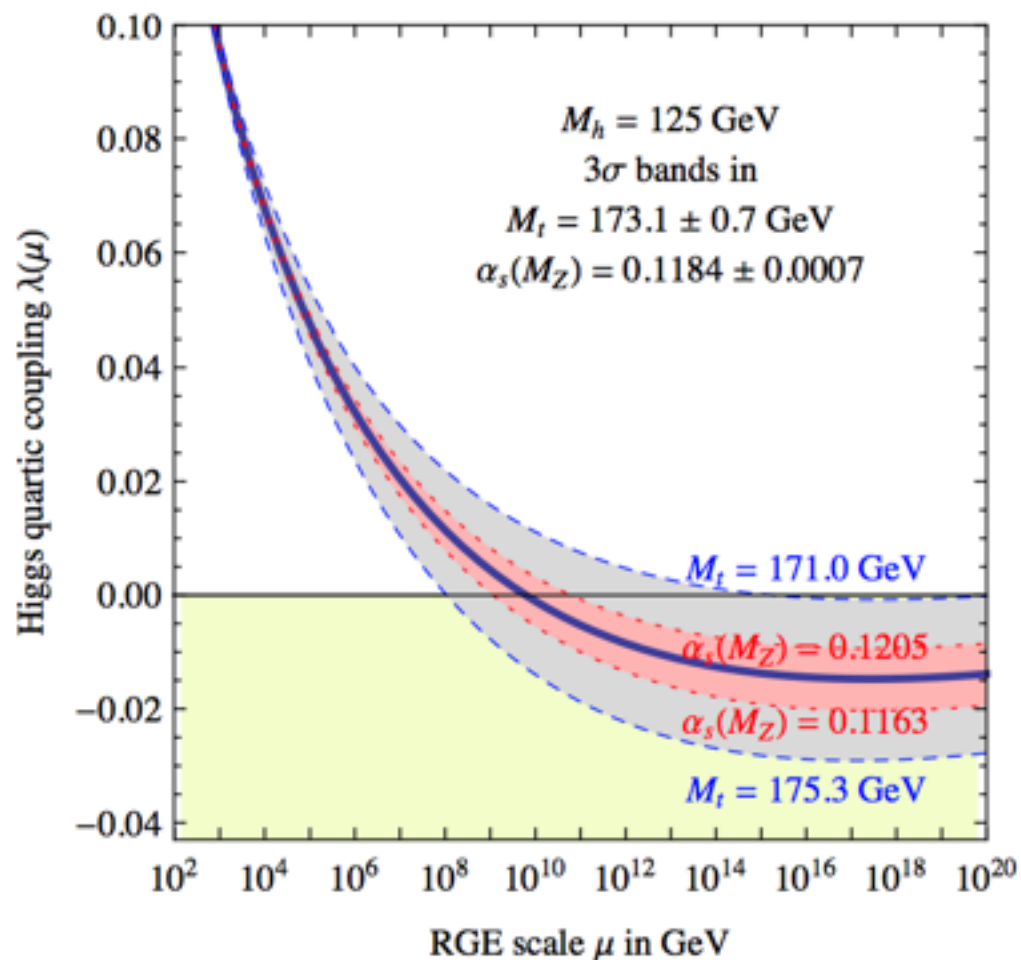
● Vacuum stability ( $\lambda_{HX}$ ) [S. Baek, P. Ko, WIP & E. Senaha, JHEP(2012)]

$$\beta_{\lambda_H}^{(1)} = \frac{1}{16\pi^2} \left[ 24\lambda_H^2 + 12\lambda_H\lambda_t^2 - 6\lambda_t^4 - 3\lambda_H(3g_2^2 + g_1^2) + \frac{3}{8}(2g_2^4 + (g_2^2 + g_1^2)^2) + \frac{1}{2}\lambda_{HS}^2 \right]$$

$$\beta_{\lambda_{HS}}^{(1)} = \frac{\lambda_{HS}}{16\pi^2} \left[ 2(6\lambda_H + 3\lambda_S + 2\lambda_{HS}) - \left( \frac{3}{2}\lambda_H(3g_2^2 + g_1^2) - 6\lambda_t^2 - 4\lambda^2 \right) \right],$$

$$\beta_{\lambda_S}^{(1)} = \frac{1}{16\pi^2} [2\lambda_{HS}^2 + 18\lambda_S^2 + 8\lambda_S\lambda^2 - 8\lambda^4],$$

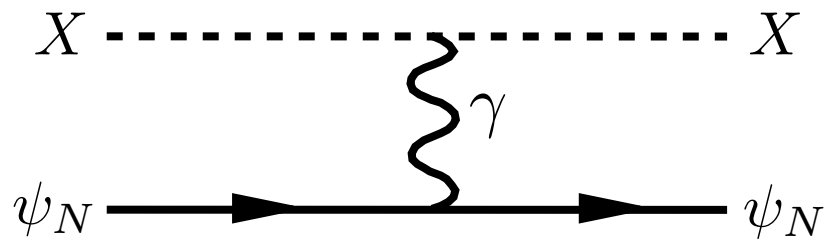
with  $\lambda_{HS} \rightarrow \lambda_{HX}/2$  and  $\lambda_S \rightarrow \lambda_X$



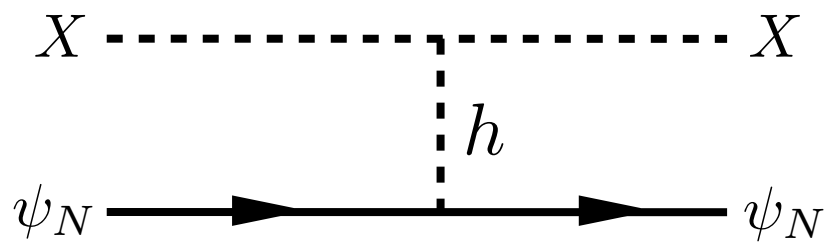
[G. Degrassi et al., 1205.6497]



● DM direct search ( $\epsilon$ ,  $\lambda_{hX}$ ,  $m_X$ )

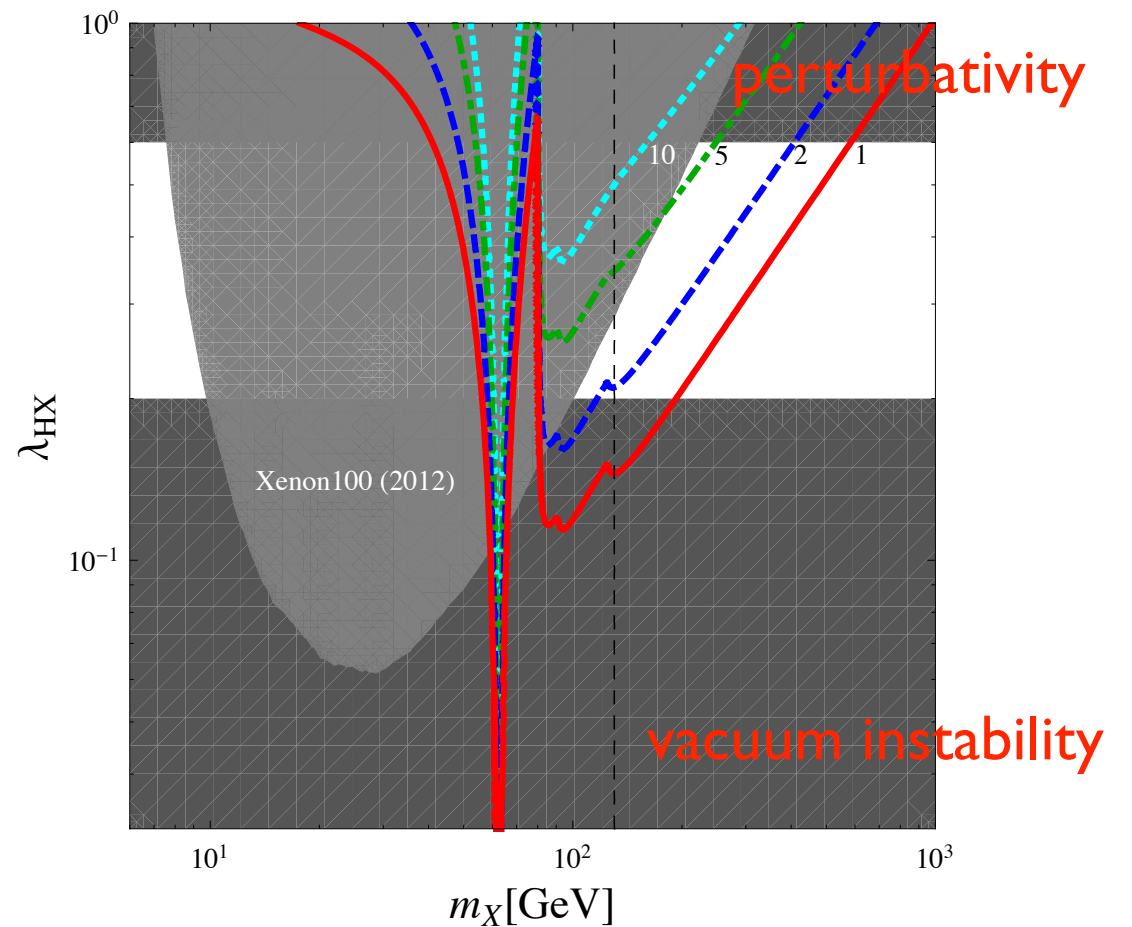
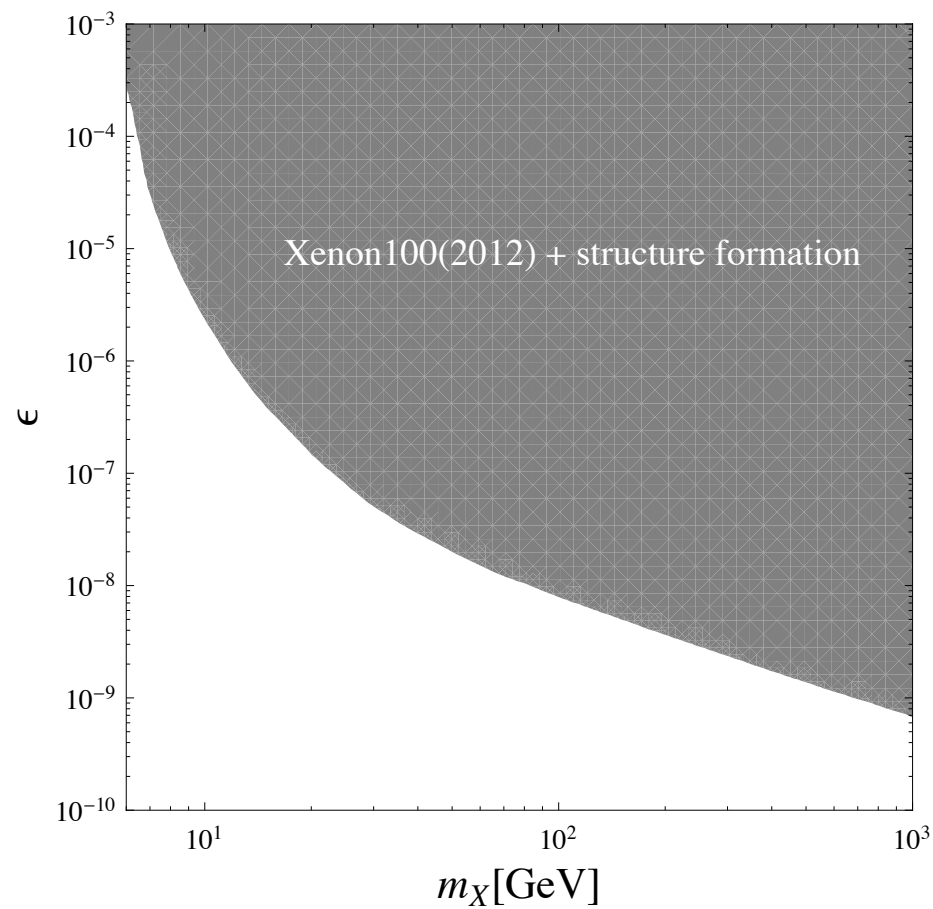


$$\frac{d\sigma_A}{dE_r} = \frac{2\pi\epsilon_e^2\alpha_{em}^2 Z^2}{m_A E_r^2 v^2} \mathcal{F}_A^2(qr_A)$$



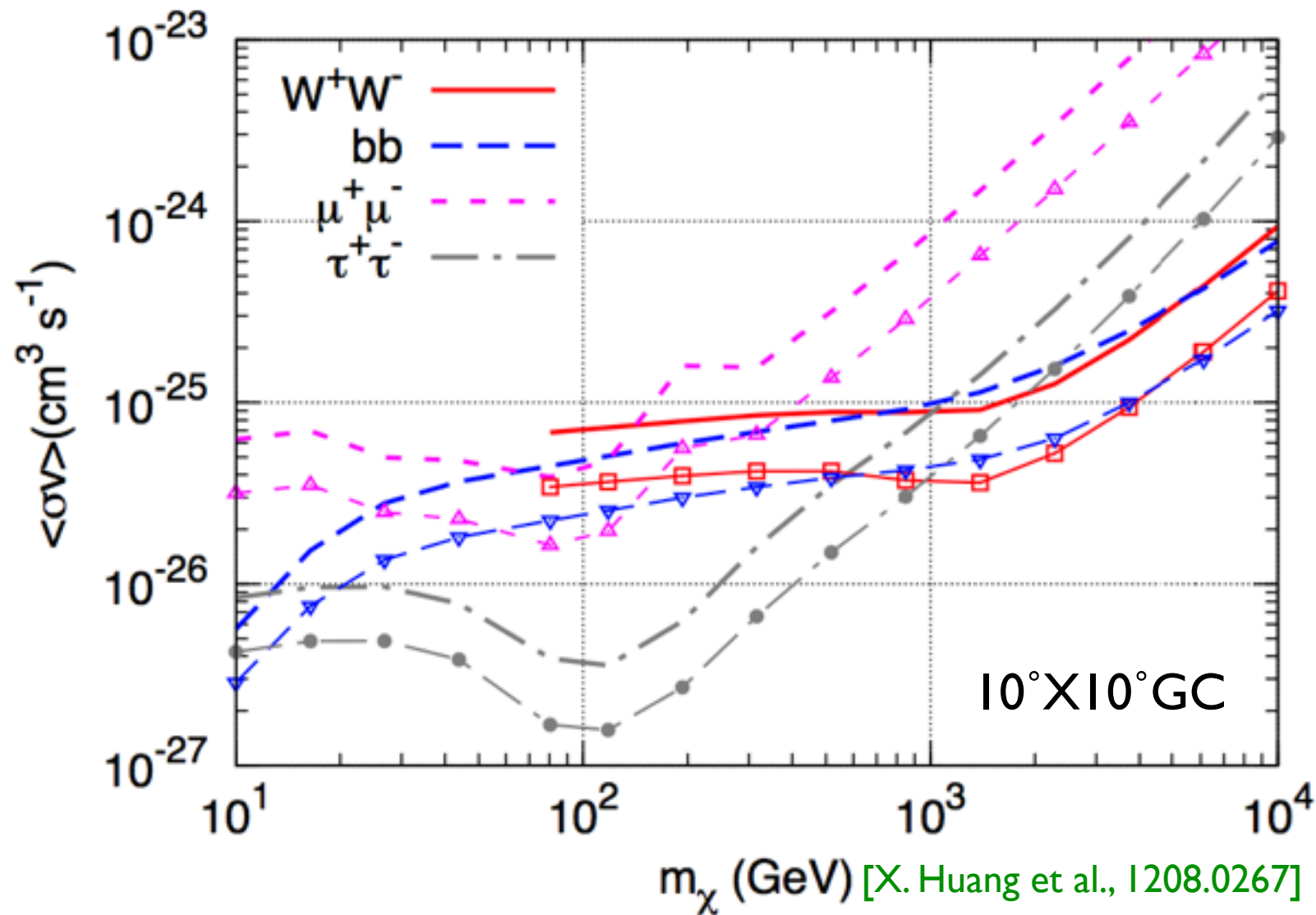
$$\sigma_{N,h}^{SI} = \frac{\lambda_{HX}^2}{64\pi} \frac{m_r^2 m_N^2}{m_X^2 m_h^4} f_{q,h}^2$$

$$\langle\sigma v\rangle_{ann}/\langle\sigma v\rangle_{ann,0}$$



# ● Indirect search ( $\lambda_{hX}, m_X$ )

- DM annihilation via Higgs produces a continuum spectrum of  $\gamma$ -rays
- Fermi-LAT  $\gamma$ -ray search data poses a constraint



In our model,

$$\langle\sigma v\rangle_{XX^\dagger \rightarrow W^+W^-}^{\text{obs}} \lesssim 2 \times 7.4 \times 10^{-26} \text{cm}^3/\text{sec}$$

$$\Rightarrow \langle\sigma v\rangle_{\text{ann}}^X \lesssim \frac{2 \times 7.4 \times 10^{-26} \text{cm}^3/\text{sec}}{\text{Br}(XX^\dagger \rightarrow W^+W^-)}$$

$$\Rightarrow 1 \leq \frac{\langle\sigma v\rangle_{\text{ann}}^X}{\langle\sigma v\rangle_{\text{ann}}^{\text{th}}} \lesssim 5$$

☞ Monochromatic  $\gamma$ -ray spectrum?

$$\langle\sigma v\rangle_{\text{ann}}^{\gamma\gamma} \sim 10^{-4} \langle\sigma v\rangle_{\text{ann}}^X \lesssim 10^{-29} \text{cm}^3/\text{sec}$$

Too weak to be seen!

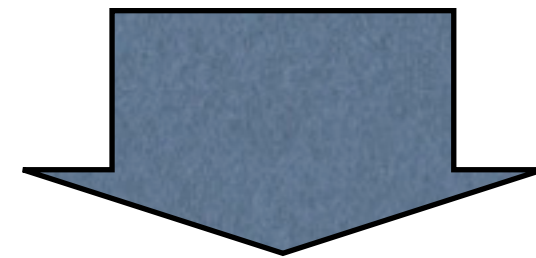
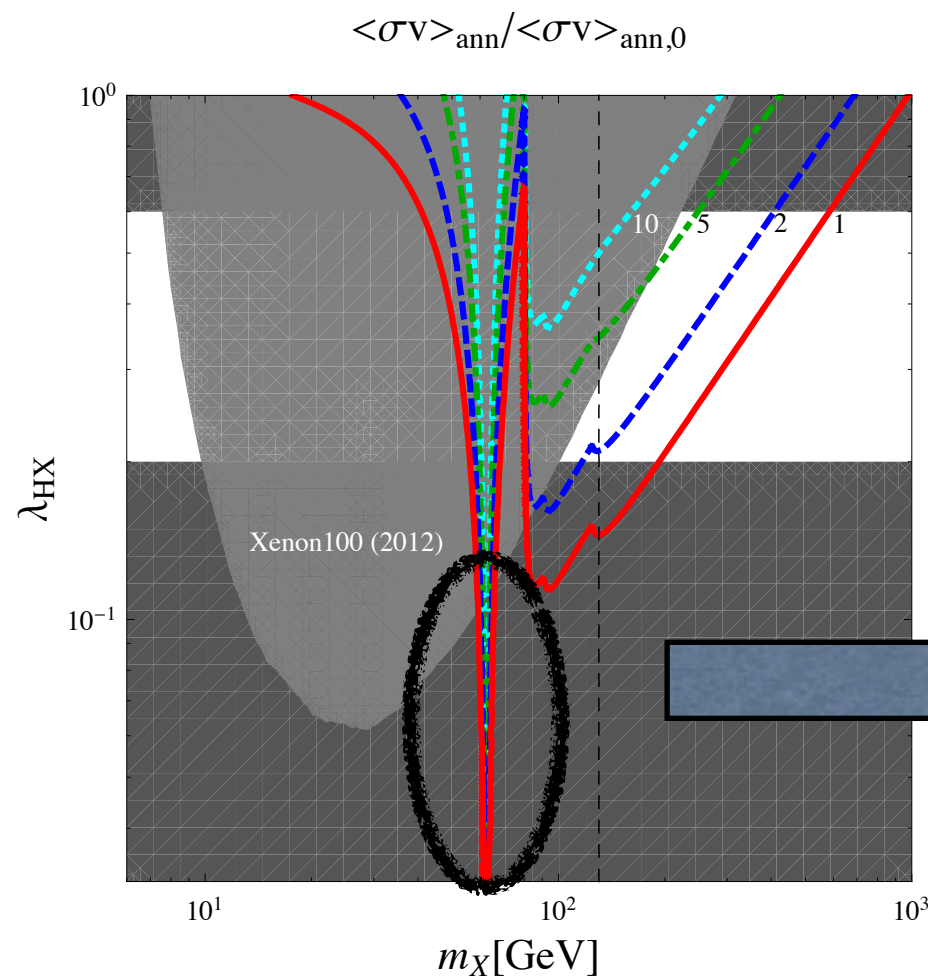
# ● Collider phenomenology ( $\lambda_{hX}, m_X$ )

Invisible decay rate of Higgs is

$$\Gamma_{h \rightarrow XX^\dagger} = \frac{\lambda_{HX}^2 v^2}{128\pi m_h} \left(1 - \frac{4m_X^2}{m_h^2}\right)^{1/2}$$

SM signal strength at collider is

$$\mu = 1 - \frac{\Gamma_{h \rightarrow XX^\dagger}}{\Gamma_h^{\text{tot}}} \quad \left( \begin{array}{l} \text{cf., } \mu_{\text{ATLAS}} = 1.43 \pm 0.21 \quad \text{for } m_h = 125.5 \text{ GeV} \\ \mu_{\text{CMS}} = 0.8 \pm 0.14 \quad \text{for } m_h = 125.7 \text{ GeV} \end{array} \right)$$



We may need  $\text{Br}(h \rightarrow XX^\dagger) \ll \mathcal{O}(10)\%$ , i.e.,

$$\lambda_{HX} \ll 0.1$$

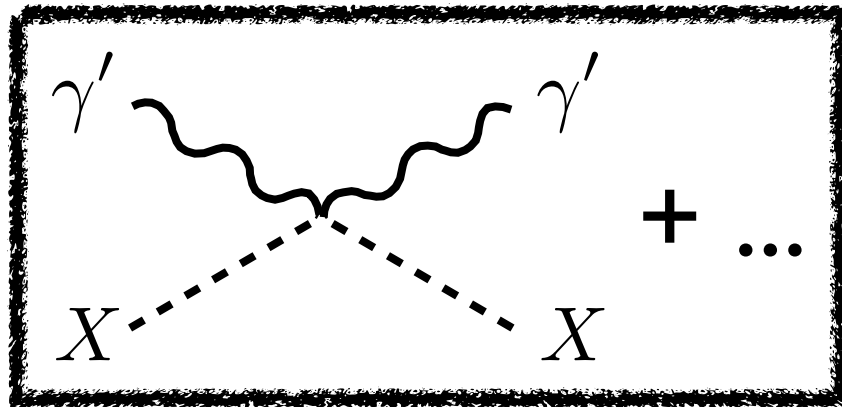
or

$$m_h - 2m_X \lesssim 0.5 \text{ GeV}$$

or kinematically forbidden

- Dark radiation

Decoupling of dark photon



$$\left\{ \begin{array}{l} \Gamma(T_{\gamma'}) = \frac{32\pi^3 \alpha_X^2 T_{\gamma'}^4}{45m_X^3} \Rightarrow T_{\text{dec},\gamma'-X} \gtrsim 16\text{MeV} \\ T_{\text{dec},X-\text{SM}} \sim 1\text{GeV} \Rightarrow T_{\text{dec},\gamma'-\text{SM}} \sim 1\text{GeV} \end{array} \right.$$

# of extra relativistic degree of freedom

$$\Delta N_{\text{eff}} = \frac{\rho_{\gamma'}}{\rho_{\nu}} = \frac{g_{\gamma'}}{(7/8)g_{\nu}} \left( \frac{T_{\gamma,0}}{T_{\nu,0}} \right)^4 \left( \frac{T_{\gamma',\text{dec}}}{T_{\gamma,\text{dec}}} \right)^4 \left( \frac{g_{*S}(T_{\gamma,0})}{g_{*S}(T_{\gamma,\text{dec}})} \right)^{4/3}$$

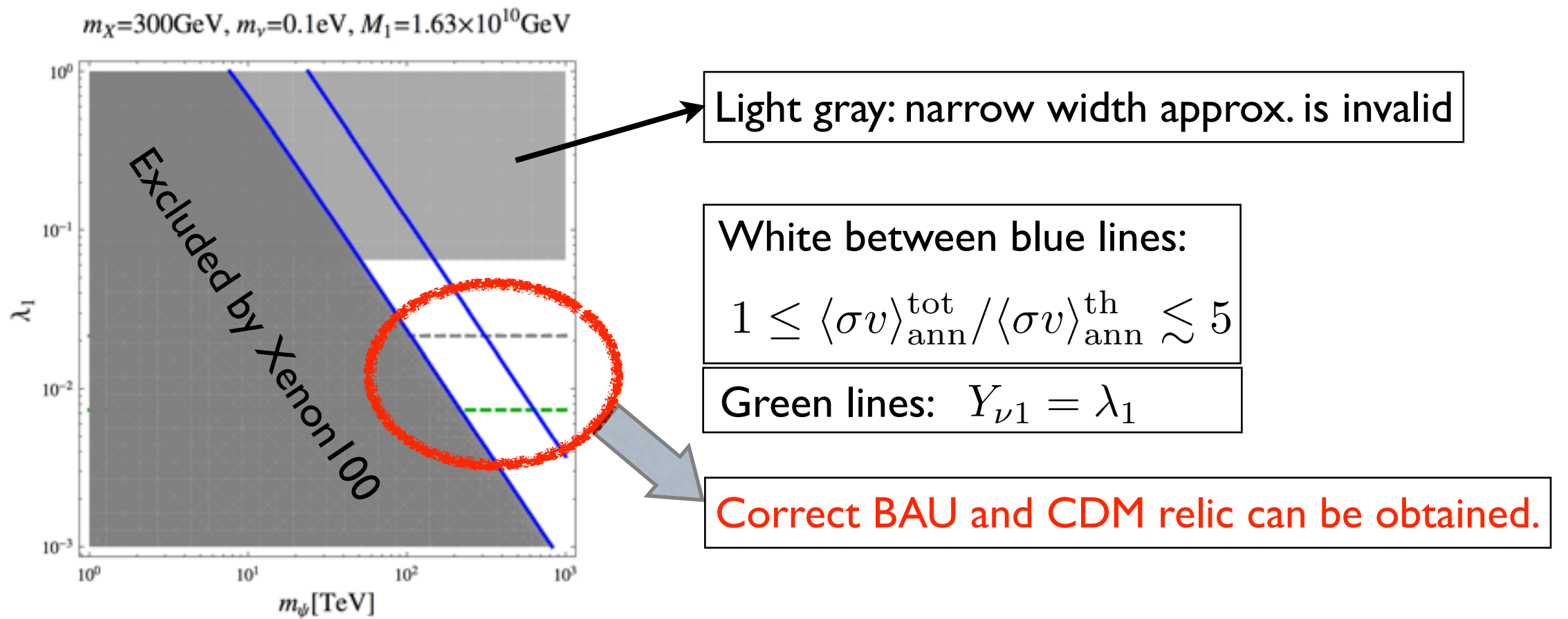
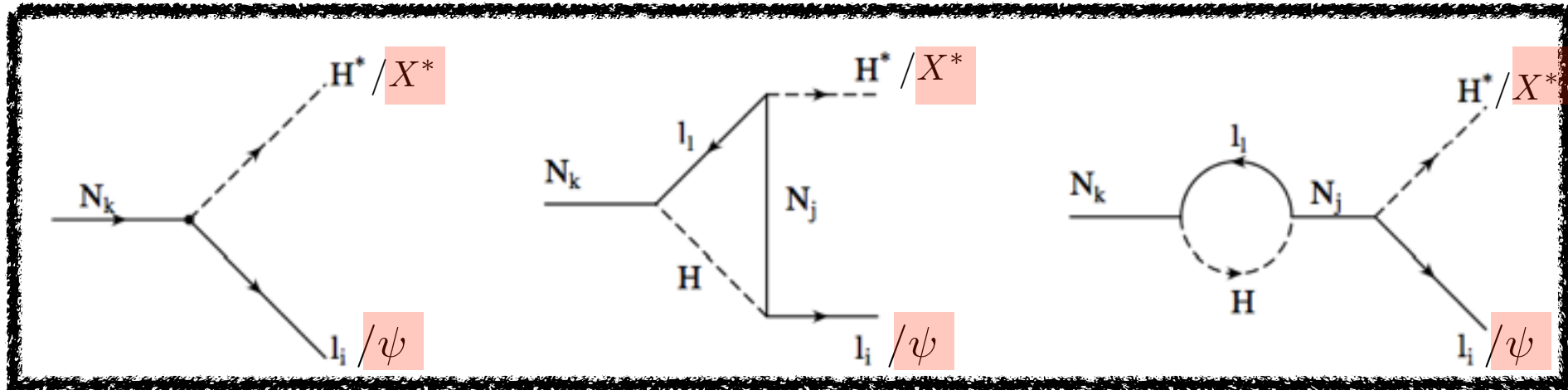
$$\frac{T_{\nu,0}}{T_{\gamma,0}} = \begin{cases} \left(\frac{4}{11}\right)^{1/3} & \text{for } T_{\text{dec}} \gtrsim 1\text{MeV} \\ 1 & \text{for } T_{\text{dec}} \lesssim 1\text{MeV} \end{cases}$$

$$\Delta N_{\text{eff}} = 0.474_{-0.45}^{+0.48} \text{ at 95\% CL (Planck+WP+highL+H}_0\text{+BAO)}$$

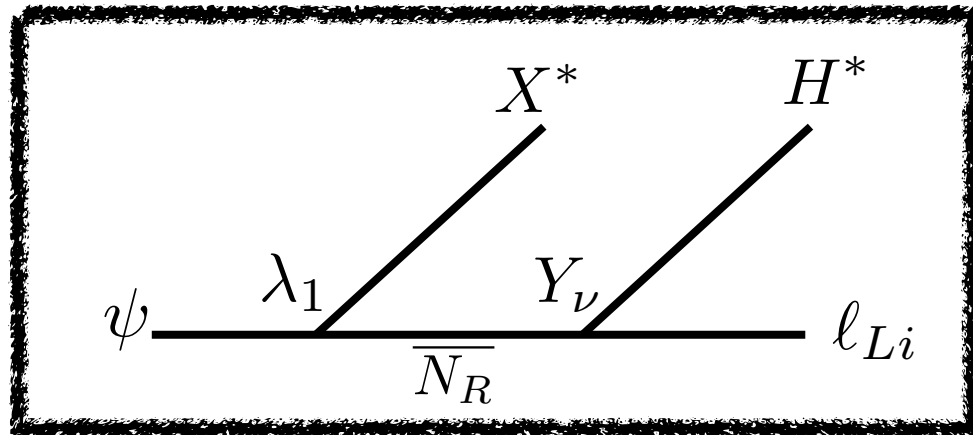
[Planck Collaboration, arXiv:1303.5076]

$$T_{\text{dec},\gamma'-\text{SM}} \sim 1\text{GeV} \Rightarrow \Delta N_{\text{eff}} = \frac{2}{2\frac{7}{8}} \left( \frac{11}{4} \right)^{4/3} \left( \frac{g_{*S}(T_{\gamma,0})}{g_{*S}(T_{\text{dec},X_{\mu}})} \right)^{4/3} \sim 0.06$$

- **Lepto/darkogenesis (1/2)**  
(Genesis from the decay of RHN)



- **Lepto/darkogenesis (2/2)**  
(Genesis from the late-time decay of  $\psi$  &  $\psi$ -bar)



Late-time decay of  $\psi \rightarrow \Delta(Y_{\Delta L}) \neq 0$   
 $T_d^\psi \ll m_\psi \rightarrow$  No wash-out!



$$\underline{\Delta(Y_{\Delta L}) = 2\epsilon_L Y_\psi(T_{\text{fz}}^\psi)}$$

$$Y_\psi(T_{\text{fz}}^\psi) = \frac{3.79 (\sqrt{8\pi})^{-1} g_*^{1/2} / g_* S x_{\text{fz}}^\psi}{m_\psi M_{\text{P}} \langle \sigma v \rangle_{\text{ann}}^\psi} \simeq 0.05 \frac{x_{\text{fz}}^\psi m_\psi}{\alpha_X^2 M_{\text{P}}}$$

$$\Rightarrow \frac{\Delta(Y_{\Delta L})}{Y_{\Delta L}} \simeq 2 \times 10^7 \frac{x_{\text{fz}}^\psi m_\psi}{\alpha_X^2 M_{\text{P}}} \frac{M_1 m_\nu^{\text{max}}}{v_H^2} \times \begin{cases} 1 & \text{for } \text{Br}_L \gg \text{Br}_\psi \\ \sqrt{\lambda_2^2 M_1 / \lambda_1^2 M_2} & \text{for } \text{Br}_L \ll \text{Br}_\psi \end{cases}$$

(e.g :  $\epsilon_L \sim 10^{-7}$ ,  $\alpha_X \sim 10^{-5}$ ,  $m_\psi \sim 10^3 \text{ TeV} \rightarrow \frac{\Delta(Y_{\Delta L})}{Y_{\Delta L}} \sim 0.3$  )

\* Late-time decays of **symmetric  $\psi$  and  $\psi$ -bar** can generate a sizable amount of lepton number asymmetry.

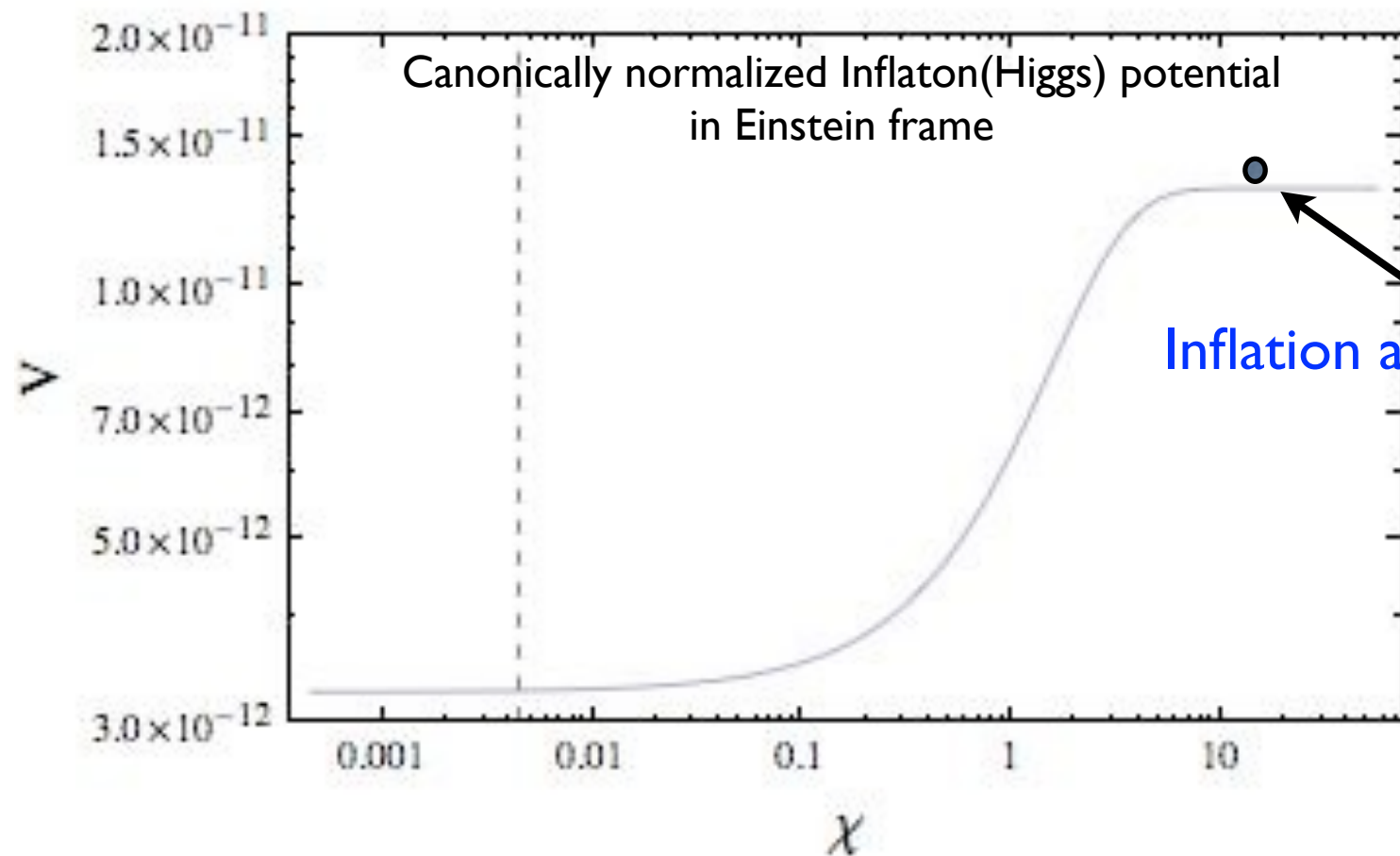


- Higgs inflation in Higgs-singlet system

[Lebedev, 1203.0156]

$$\frac{\mathcal{L}_{\text{scalar}}}{\sqrt{-g}} = -\frac{1}{2}M_{\text{P}}^2 R - \frac{1}{2}(\xi_h h^2 + \xi_x x^2) R + \frac{1}{2}(\partial_\mu h)^2 + \frac{1}{2}(\partial_\mu x)^2 - V(h, x)$$

where  $\xi_h, \xi_x \gg 1$



$$\lambda_X \lesssim 0.23$$

$$0.2 \lesssim \lambda_{HX} \lesssim 0.6$$

# Variations

Assume the decay of Higgs to DMs is forbidden.

Dark sector fields	$U(1)_X$	Messenger	DM	Extra DR	Signal strength $\mu_i$
$\hat{B}'_{\mu\nu}, X, \psi_X$	Unbroken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu}, N_R$	$X$	$\sim 0.06$	1 ( $i = 1$ )
$\hat{B}'_{\mu}, X$	Unbroken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu}$	$X$	$\sim 0.06$	1 ( $i = 1$ )
$\hat{B}'_{\mu}, \psi_X$	Unbroken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu} \textcircled{S}$	$\psi_X$	$\sim 0.06$	$< 1$ ( $i = 1, 2$ )
$\hat{B}'_{\mu}, X, \psi_X, \phi_X$	Broken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu}, N_R$	$X$ or $\psi_X$	$\sim 0$	$< 1$ ( $i = 1, 2$ )
$\hat{B}'_{\mu}, X, \phi_X$	Broken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu}$	$X$	$\sim 0$	$< 1$ ( $i = 1, 2$ )
$\hat{B}'_{\mu}, \psi_X$	Broken	$H^\dagger H, \hat{B}'_{\mu\nu} \hat{B}^{\mu\nu} \textcircled{S}$	$\psi_X$	$\sim 0$	$< 1$ ( $i = 1, 2, 3$ )

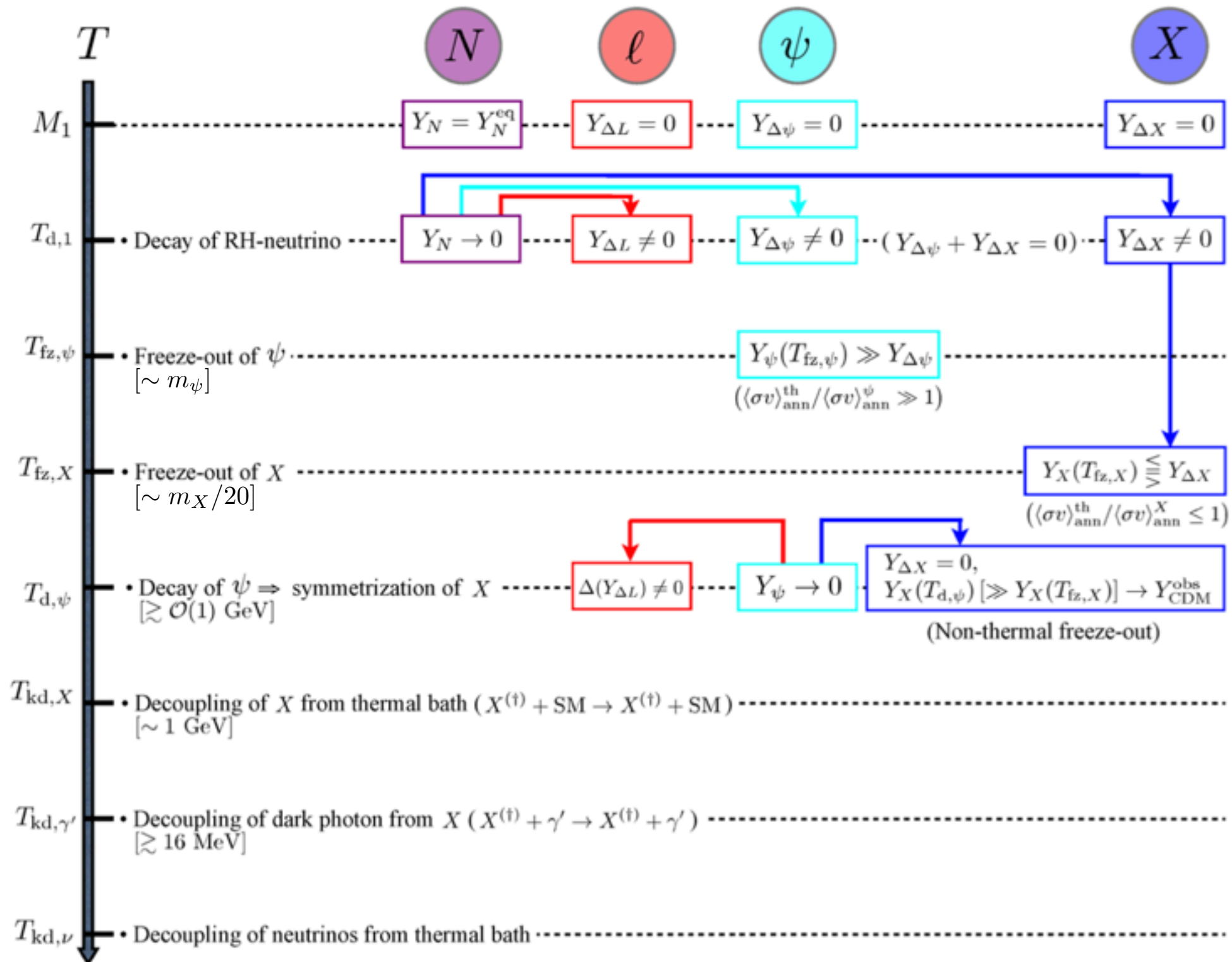
$\textcircled{S}$  = a singlet real scalar

because of mixing in Higgs sector

- \* **Unbroken  $U(1)_X$**  allows a sizable contribution to the **extra radiation**.
- \* **Broken  $U(1)_X$**  or the case of **fermion dark matter** results in “ $\mu_i < 1$ ”.



# Thermal history



# Summary

- Stability of weak scale dark matter requires a local symmetry.
- The simplest extension of SM with a local  $U(1)$  has a unique set of renormalizable interactions.
- The model can address following issues.
  - \* Some small scale puzzles of standard CDM scenario
  - \* Vacuum stability of Higgs potential
  - \* CDM relic density (thermal or non-thermal)
  - \* Dark radiation
  - \* Lepto/darkogenesis
  - \* Inflation (Higgs inflation type)