

# ***Neutrinos & Cosmology***

***Pasquale Dario Serpico***

***25th Rencontres de Blois on  
“Particle Physics and Cosmology”***

***30/05/2013***

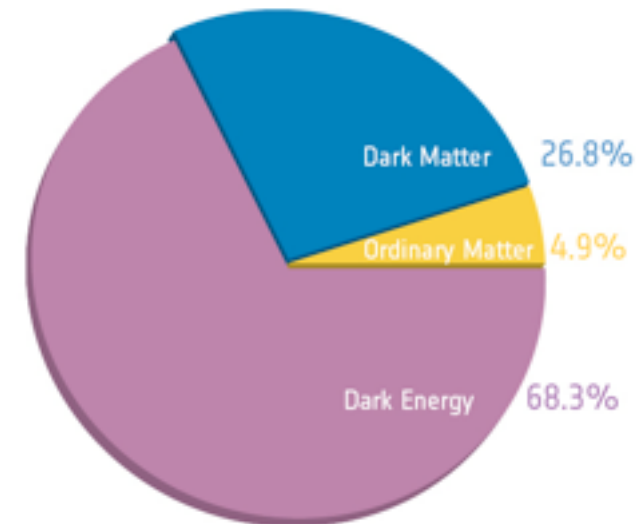


# In a nutshell: why neutrinos matter for cosmology?

- ❖ The energy budget of the Universe is dominated by “dark stuff.”
- ❖ Neutrinos are the only “dark” component (cosmologically stable) present in the standard model
- ❖ We know that they are extremely light... “dark radiation”?
- ❖ The Lab tells us that, nonetheless, they are massive... “dark matter”?
- ❖ The Lab tells us that anomalies might be present in this sector... what would e.g. sterile neutrino imply for cosmology?

## Why does it matter for neutrino physicists?

**Just to tell one:** Basically the only, numerous sample of non-relativistic neutrinos available!  
Via gravitational effects, possible to infer something about their absolute mass scale!



# Outline of the present talk

- ❖ Illustrate the basic physics through which  $\nu$  states are populated in the early universe
- ❖ How they affect observables in BBN, CMB, LSS (“extra radiation” and “extra mass”)
- ❖ Adding sterile states... and some “theoretical caveats”.
- ❖ I will revisit the origin and fate (after Planck) of cosmological “anomalies” and critically examine the extent to which they can be considered to support current hints for sterile  $\nu$

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“anomalies,” and critically examine the extent to which they can be

- ❖ I will revisit the origin and fate (after Planck) of cosmological

# The Birth of cosmological $\nu$ 's

**$T \gg 1 \text{ MeV}$**   
**Neutrinos in equilibrium**

$$f_\nu(p, T) = f_{FD}(p, T) = \frac{1}{e^{p/T} + 1} \quad T_\nu = T_e = T_\gamma$$

Above  $\sim \text{MeV}$ -scale temperatures,  $e^\pm$  pairs  
can be created “Boltzmann unsuppressed”.  
 $\nu$ 's are populated (& reach a thermal distribution)  
via reactions of the kind

$$\nu_a \nu_b \leftrightarrow \bar{\nu}_a \bar{\nu}_b$$

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$$\nu_a \bar{\nu}_a \leftrightarrow e^+ e^-$$

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$$\nu_a e^- \leftrightarrow \bar{\nu}_a e^-$$

***They decouple from the plasma at  $T \sim \mathcal{O}(1) \text{ MeV}$***

*Rate of weak processes*

$$\Gamma_w \approx n \sigma c \approx g a^{-3} G_F^2 E^2 \approx g G_F^2 T^5$$

*Hubble expansion rate*

$$H \approx \sqrt{G_N \rho} \approx \sqrt{g G_N T^2}$$

$$\frac{\Gamma_w}{H} \approx \left( \frac{T}{\text{MeV}} \right)^3$$

After this epoch ( $\sim \mathcal{O}(1)$  s after Big Bang)  $\nu$ 's evolve only due to gravity

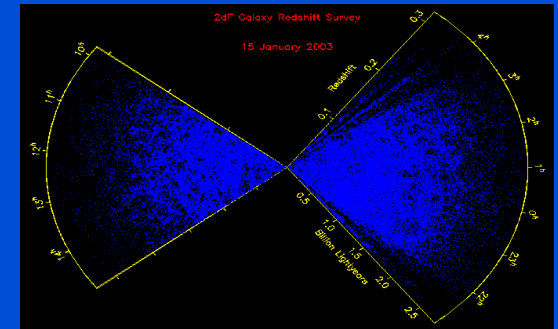
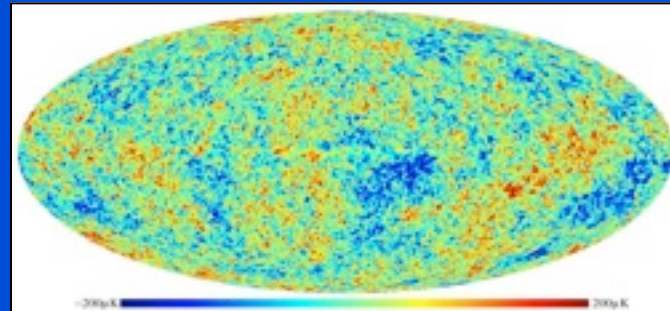
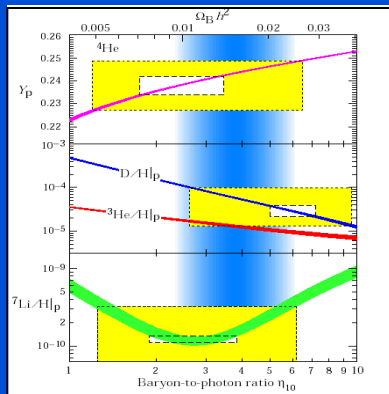
# “Detection” of the CvB

- Pseudo-thermal distribution:  $T_\nu = 1.95 \text{ K}$
- Number density ( $\nu + \bar{\nu}$ ):  $112 \text{ cm}^{-3}/\text{flavour}$
- Mean kinetic energy:  $\ll \text{meV}$

*lower than 2.7 K of CMB due to later  $e^+ e^- \rightarrow \gamma\gamma$  (heating of photons)*

Direct searches hopeless?

Indirect searches: Cosmological observables



**BBN**

$T \sim \text{MeV}$

$\nu_e$  vs.  $\nu_{\mu,\tau}$        $N_{\text{eff}}$

**CMB**

$T \sim \text{eV}$

Gravity only (no flavor discr.)

**LSS**

$N_{\text{eff}}$  &  $m_\nu$

# Neutrinos & BBN: How do $\nu$ 's enter the game?

## Hubble Expansion Law

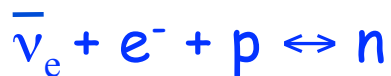
$$H = \frac{\dot{a}}{a} = \left( \frac{8\pi G_N}{3} \right)^{1/2} (\rho_\gamma + \rho_e + \rho_b + \rho_\nu + \rho_X)^{1/2}$$

$$\rho_\nu + \rho_X \rightarrow \frac{7}{8} \frac{4^{1/3}}{11^{1/3}} N_{eff} \rho_\gamma$$

$N_{eff} = 3$   
(SM only & instantaneous decoupling)

*Gravity only, mostly integral quantity, extra relativistic species*

## Weak Rates: $p \leftrightarrow n$ equilibrium



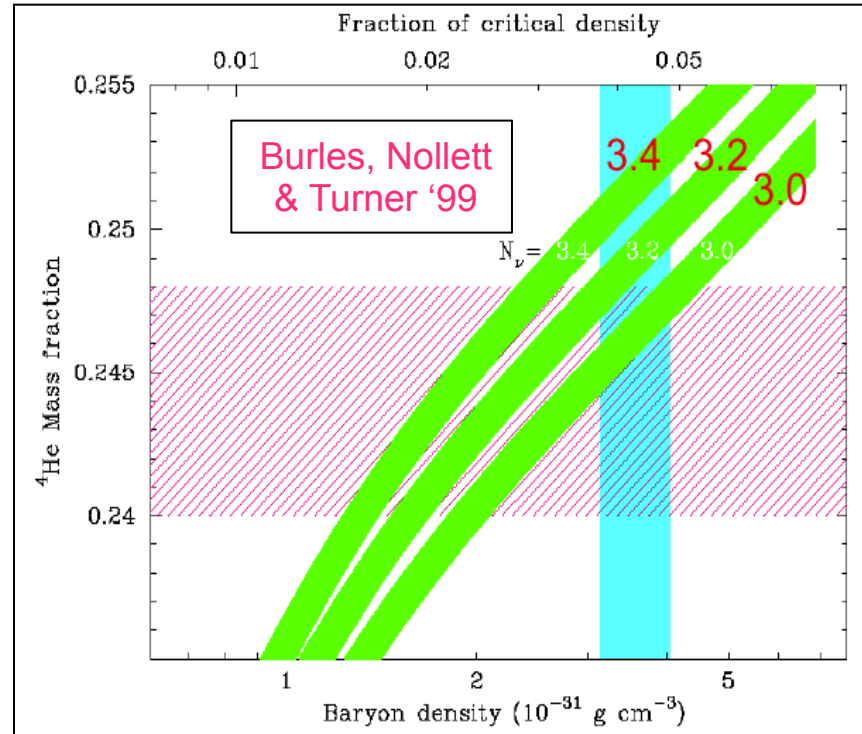
*Very sensitive to weak interactions (only e-flavour matters), energy spectrum.*

Final  $n/p$  (& hence  ${}^4\text{He}$ , where most neutrons are ultimately locked) depends on “when”  $\Gamma_w = H$

For a review, see e.g. F. Iocco et al.

“Primordial Nucleosynthesis: from Precision Cosmology to fundamental physics”  
Phys. Rept. 472, 1 (2009) [arXiv:0809.0631]

# Estimating $^4\text{He}$ response to parameter changes

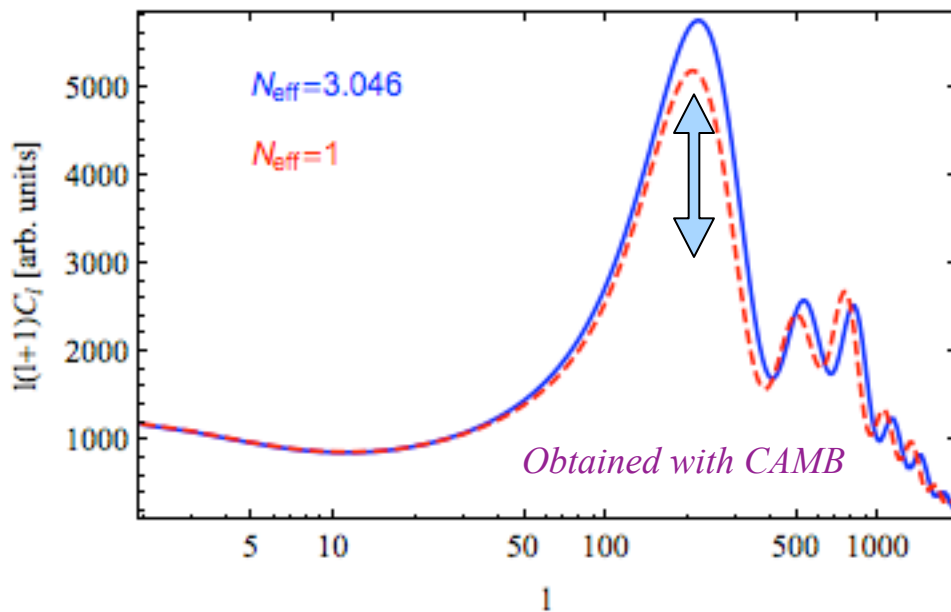


- High  $N_{eff} \rightarrow$  High  $H \rightarrow$  early freeze out ( $\Gamma_{pn} \sim H$  at high  $T$ )  $\rightarrow$  high  $n/p \rightarrow$  high  $Y_p$
- $\nu_e > \bar{\nu}_e \rightarrow \nu_e n \rightarrow e^- p$  favored over  $\bar{\nu}_e p \rightarrow e^+ n \rightarrow$  low  $n/p$  at fr.out  $\rightarrow$  low  $Y_p$   
(chemical potential  $\mu_{\nu_e} > 0$ )
- ...

# Neutrinos & CMB

For eV scale neutrinos, both  $m_\nu$  and  $N_{\text{eff}}$  *mostly* affect the time of matter-radiation equality. All the rest fixed:

- Raising  $N_{\text{eff}}$  means more radiation, hence delayed equality.
- Lowering  $m_\nu$  means that part of the total that we call now (dark) matter was behaving as  $\sim$ radiation at CMB formation, hence delayed equality.



*correlation expected!*

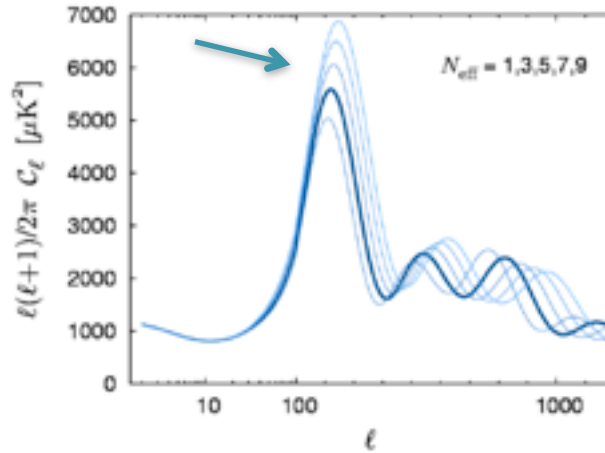
for more details, see e.g.  
J. Lesgourgues & S. Pastor  
Phys.Rept. 429 (2006) 307-379

$$1 + z_{\text{eq}} = \frac{\Omega_m}{\Omega_r} \simeq \frac{\Omega_m}{\Omega_\gamma} \frac{1}{1 + 0.23 N_{\text{eff}}}$$

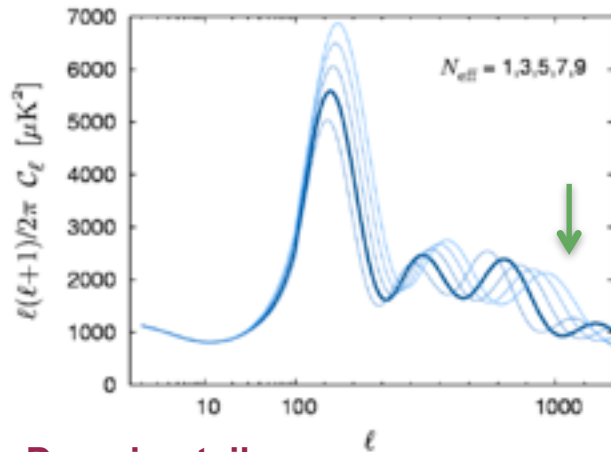
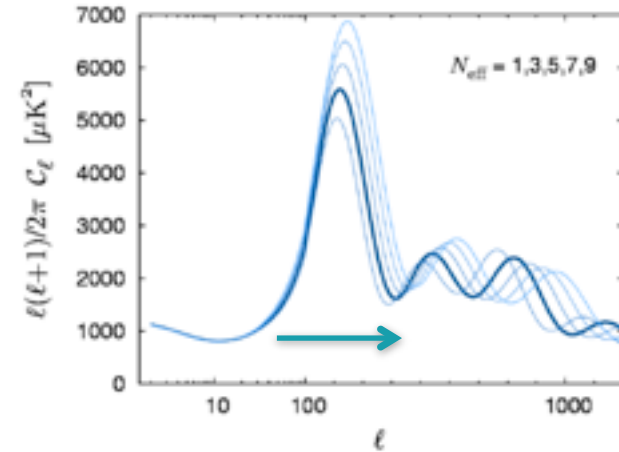
# Beware of degeneracies!

Matter-radiation equality

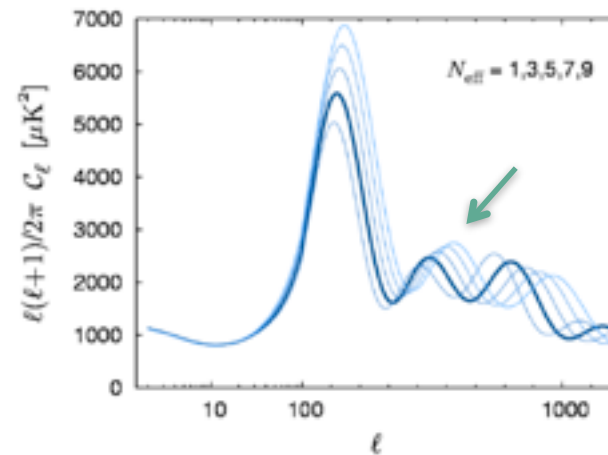
degenerate with  $\Omega_m$



Sound horizon/angular positions of the peaks  
degenerate with  $\Omega_m$  and  $h$



Damping tail  
degenerate with  $Y_p$



Anisotropic stress

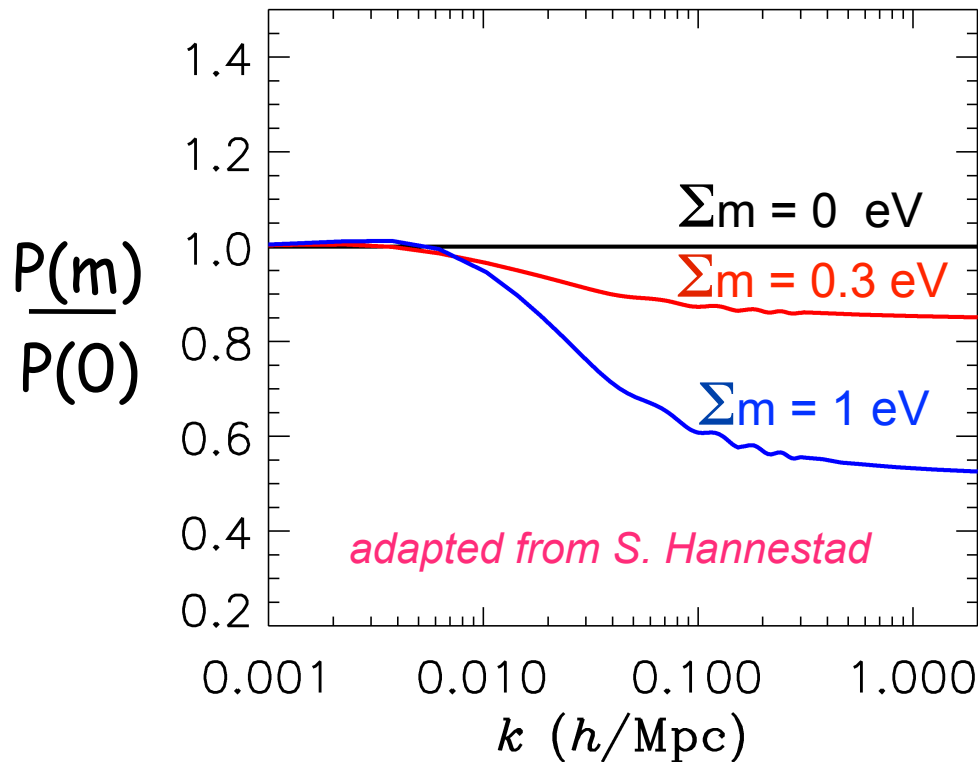
(partially) degenerate  
with  $A_s$  and  $n_s$

adapted from Y. Wong

# Suppression of power-spectrum due to $m_\nu$

Until non-relativistic,  $\nu$ 's do not contribute to gravitational clustering below the free-streaming scale, but they do contribute to the homogeneous expansion. This “unbalance” introduces a peculiar spectral suppression. In linear theory one finds

$$\frac{\Delta P}{P} \approx -8 \frac{\Omega_\nu}{\Omega_m} \approx -0.8 \frac{\sum m_i}{1 \text{ eV}} \frac{0.1}{\Omega_m h^2} \quad @ k > k_{NR}$$
$$\approx 0.015 (\sum m_{eV} \times \Omega_m h^2)^{1/2} \text{ Mpc}^{-1}$$



**This is the key effect used to derive bounds on massive neutrinos from LSS**

Adding sterile states...



# The Quantum Zeno effect (for production via osc.)

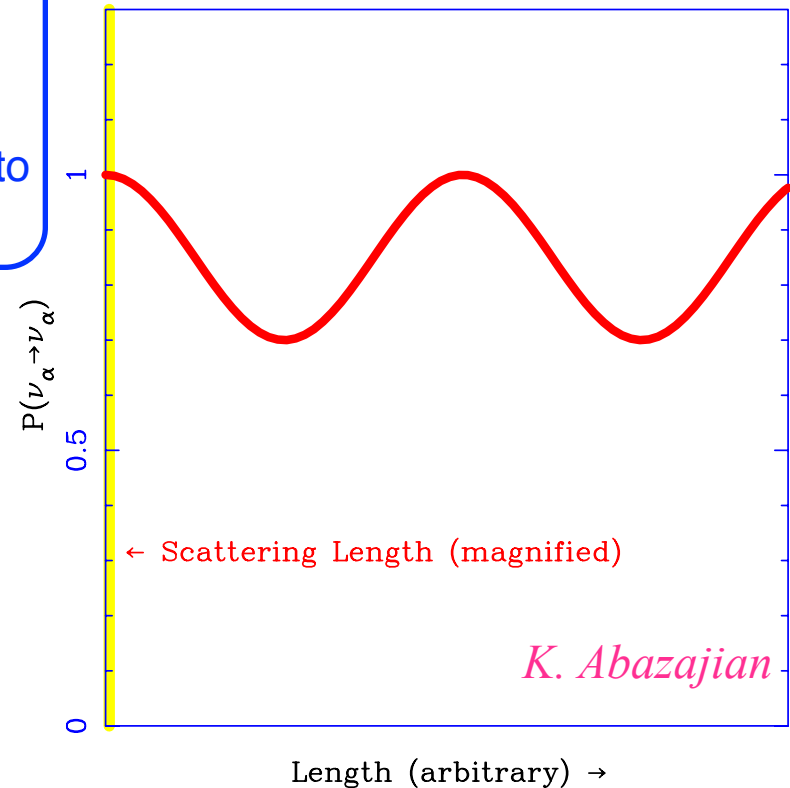
Each scattering of a  $\nu$  acts as a “measurement” of its flavor state. At high temperatures (say,  $T \geq 100$  MeV),  $\lambda_{\text{scatt}}$  is extremely short compared to  $\lambda_{\text{osc}}$ . Therefore, a population of active  $\nu$ 's won't have time to evolve into sterile  $\nu$ 's, but for small amounts.

$$\lambda_{\text{scatt}} = [\sigma n]^{-1} \sim E^{-2} T^{-3} \propto T^{-5}$$

$$\lambda_{\text{osc}} = \frac{4\pi E}{\Delta m^2} (\text{in vacuo}) \propto T$$

$$P_{\alpha\alpha}(\lambda_{\text{scatt}}) = 1 - \sin^2(2\theta) \sin^2\left(\pi \frac{\lambda_{\text{scatt}}}{\lambda_{\text{osc}}}\right)$$

Suppression of  $\nu_s$  Production at Early Times



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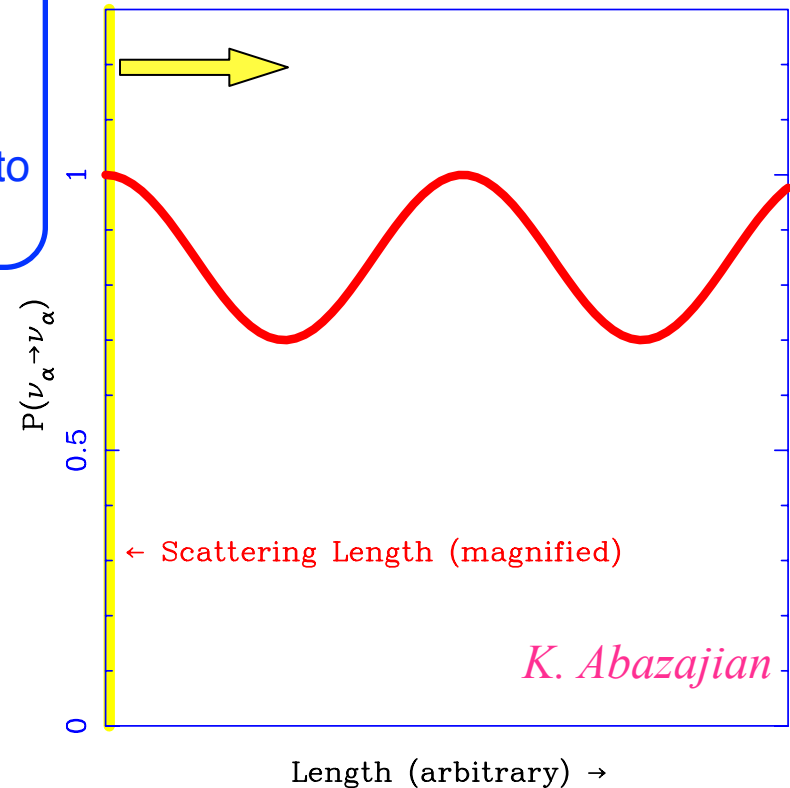
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Suppression of  $\nu_s$  Production at Early Times



As the universe expands, cools & becomes less dense,  $\lambda_{\text{scatt}} \nearrow$ . Then,  $P_{\text{as}} = (1 - P_{\alpha\alpha}) \nearrow$

☞ The larger  $\Delta m^2$ , the faster  $\nu$ 's oscillate, the higher the conversion  $P_{\text{as}}$

☞ Also, the larger  $\theta^2$ , the larger  $P_{\text{as}}$

# Sterile neutrinos are born

- \* If oscillations are effective before decoupling: the additional species can be brought into equilibrium:  $N_{\text{eff}}=4$
- \* If oscillations are effective after decoupling:  $N_{\text{eff}}=3$  but the spectrum of active neutrinos is distorted (direct effect on n/p equilibrium!)

Matter effects are responsible for the hierarchy dependence (resonant vs. non-resonant case) See e.g. Kirilova '03, Dolgov & Villante, NPB 679 (2004)...

In 3+1 fits to anomalies, parameters such that the 4th  $\nu$  always thermalize:  $N_{\text{eff}}\sim 4.05$   
In 3+2 fits, “almost” true,  $N_{\text{eff}}\sim 5$ , although partial thermalization or some spectral *distortions* at BBN times are possible (see e.g. Melchiorri et al. JCAP 01 (2009) 036)

Roughly speaking, in the former models, one new state with  $\sim 1$  eV is needed.  
In the latter models, two states with about 1.5 eV total mass needed.

## Why things may become involved...

**When active neutrinos depart from thermal distributions and sterile population are significant, large non-linearities are present among many modes!**

# Density Matrices

Need to describe of the evolution in time of the flavor content (and p-distribution) of a neutrino system propagating in a medium.

As long as true “many body effects” (higher-order, multi-field correlations) are negligible and the medium is close to homogeneity, density matrices provide an efficient tool

$$\psi(x) = \int d\mathbf{p} [a(\mathbf{p})u_{\mathbf{p}} + b^\dagger(-\mathbf{p})v_{-\mathbf{p}}] e^{i\mathbf{p}\cdot\mathbf{x}}$$

$$\langle a_j^\dagger(\mathbf{p})a_i(\mathbf{p}') \rangle = (2\pi)^3 \delta^{(3)}(\mathbf{p} - \mathbf{p}') \rho_{ij}(\mathbf{p})$$

$$\langle b_i^\dagger(\mathbf{p})b_j(\mathbf{p}') \rangle = (2\pi)^3 \delta^{(3)}(\mathbf{p} - \mathbf{p}') \bar{\rho}_{ij}(\mathbf{p})$$

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**EOM: Liouville eq.  $i\partial_t \rho = [\mathbf{H}, \rho] + \mathbf{C}[\rho]$  (for each neutrino mode)**

Occupation numbers

$$\rho = \begin{pmatrix} \rho_{ee} & \rho_{e\mu} & \rho_{e\tau} \\ \rho_{\mu e} & \rho_{\mu\mu} & \rho_{\mu\tau} \\ \rho_{\tau e} & \rho_{\tau\mu} & \rho_{\tau\tau} \end{pmatrix}$$

“Entanglement”

# EOM for $\nu$ evolution in the Early Universe

Vacuum mixing      Refractive term due to  $e^-e^+$  energy density (Not  $e^-e^+$  difference, less important!)      Self-refraction      Collisions

on total active  $\nu$ 's E-density      on total active  $\nu$ 's # density difference

$$i \frac{d\rho}{dx} = + \frac{x^2}{2m^2 y \overline{H}} [M^2, \rho] + \frac{\sqrt{2} G_F m^2}{x^2 \overline{H}} \left[ \left( -\frac{8 y m^2}{3 x^2 m_W^2} E_\ell - \frac{8 y m^2}{3 x^2 m_Z^2} E_\nu + N_\nu \right), \rho \right] + \frac{x \widehat{C}[\rho]}{m \overline{H}},$$

Eqs. rewritten in terms of (to factor out expansion)

$$x \equiv m a$$

$$y \equiv p a$$

$$z \equiv T_\gamma a$$

(rescaled) Hubble parameter  $\sim x$ -independent

$$\overline{H} \equiv \frac{x^2}{m} H$$

Asymmetric self-refraction term

$$N_\nu = \frac{1}{2\pi^2} \int dy y^2 \{ G_s(\rho(x, y) - \bar{\rho}(x, y)) G_s + G_s \text{Tr} [(\rho(x, y) - \bar{\rho}(x, y)) G_s] \}$$

Symmetric self-refraction term

$$E_\nu = \frac{1}{2\pi^2} \int dy y^3 G_s(\rho(x, y) + \bar{\rho}(x, y)) G_s$$

What does BBN say?



# What do we know about ${}^4\text{He}$ ?

## Main problem

We cannot observe *primordial* abundances:  
Stars have altered the primordial composition.  
For  ${}^4\text{He}$ , stars mostly burn H into He  $\rightarrow Y > Y_p$

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*Observe systems with little chemical processing*

HeII  $\rightarrow$  HeI recombination lines in HII regions  
(about  $\sim 80$  such regions known) of Blue  
Compact Dwarf Galaxies\*



NGC 1705  
from HST

\*small galaxies ( $\sim 1/10$   
MW) containing large  
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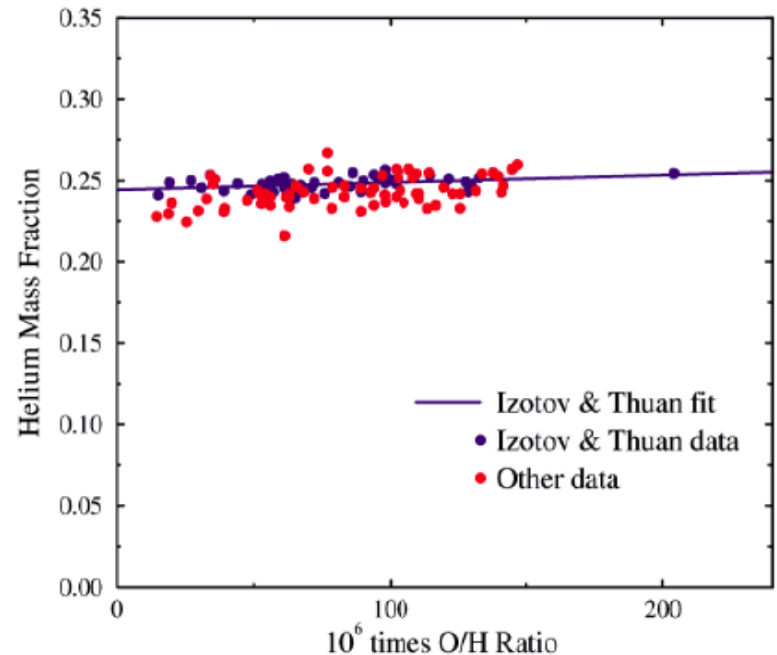
*Correct for chemical evolution*

Extrapolate *linearly* to “zero  
metallicity” in  $Y_p$  vs O/H, N/H plots



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# A simpler strategy (bypass astrophysical ignorance)

## Key Idea

We are not interested in primordial  $^4\text{He}$  abundance.  
We only care about an upper limit on  $N_{\text{eff}}$ .



Take the *observed*  $^4\text{He}$  and just use the qualitative info  $Y > Y_p$  to obtain an upper bound

No need to extrapolate or assume *linearity* in the extrapolation. No need to know Z-evolution as well or to worry about pre-galactic sources of  $^4\text{He}$  (like popIII).

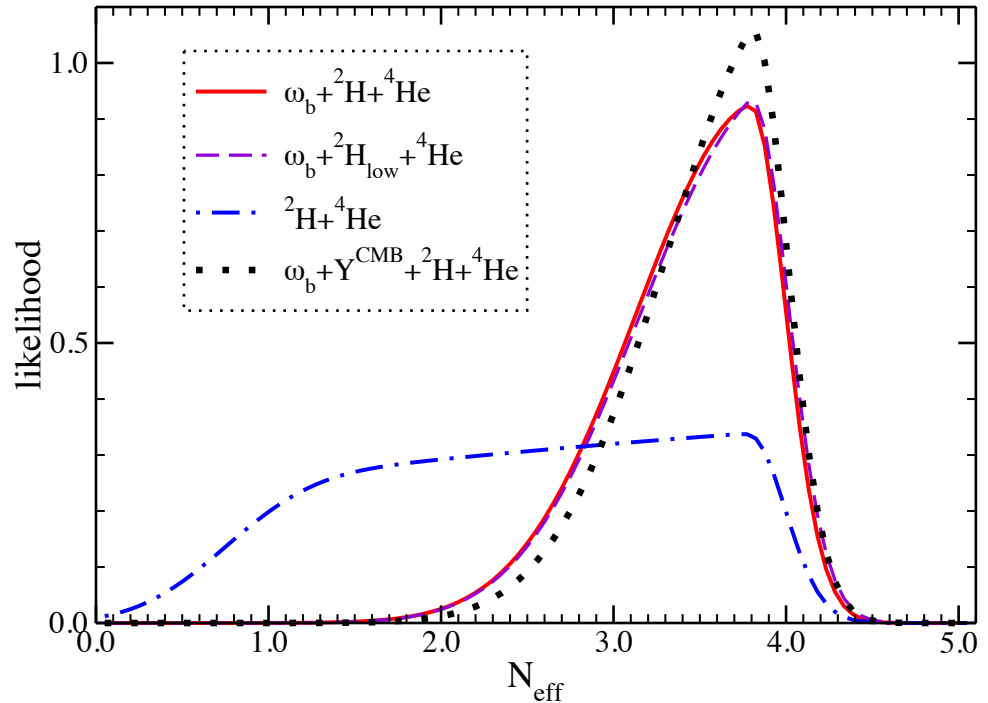
Using the data on 9 metal-poor object with high quality spectra  
of E. Aver, K.A. Olive, E.D. Skillman, arXiv:1012.2385.

$$\langle Y_0 \rangle \pm \sigma_0 = 0.2581 \pm 0.0025 \text{ (68\% C.L.)}$$

$$\ell(Y_p) \propto \Theta(\langle Y_0 \rangle - Y_p) + \Theta(Y_p - \langle Y_0 \rangle) \exp\left[-\frac{(Y_p - \langle Y_0 \rangle)^2}{2\sigma_0^2}\right].$$

# Results: $\Delta N_{\text{eff}} \leq 1$

- ✓ BBN alone (He+D) has no preference for extra dof [blue c.]
- ✓ Adding the CMB prior on  $\omega_b$ , the preference for larger  $N_{\text{eff}}$  is not significant ( $\sim 1\sigma$ ) [red curve]
- ✓ The result doesn't change if observed D used only as lower limit to primordial value [purple curve]
- ✓ Minor change if  $Y_p$  info from CMB is used [black curve]



Datasets	$N_{\text{eff}}^{\text{max}}$	$N_{\text{eff}}^{\text{min}}$	$L(N_{\text{eff}} \leq N_{\text{eff}}^{\text{SM}})$
$\omega_b + {}^2\text{H} + {}^4\text{He}$	4.05	2.56	0.20
$\omega_b + {}^2\text{H}_{\text{low}} + {}^4\text{He}$	4.08	2.57	0.19
${}^2\text{H} + {}^4\text{He}$	3.91	0.80	0.67
$\omega_b + Y_p^{\text{CMB}} + {}^2\text{H} + {}^4\text{He}$	4.08	2.71	0.15

Alternative: avoid  $Y_p$ , take  $\omega_b$  from CMB & “clean” determination of D/H (Nollet, Holder ’11)

$N_{\text{eff}} = 3.0 \pm 0.5$  Pettini & Cooke, MNRAS (1205.3785) but relies on single system...

What does CMB say?

# Pre-PLANCK

*“Precision cosmological data since the WMAP 5-year data release have consistently shown a mild preference for an excess of relativistic energy density.”*

Hint of *dark radiation*?

**Caveat I.** Analyses are **not-independent** (WMAP is always in common,  $H_0$  often in common)

**Caveat II.** It's  $\sim 2 \sigma$ ...

**Caveat III.** Requires combining many **datasets** (errors in quadrature)... chance that systematic errors eventually dominate grows!

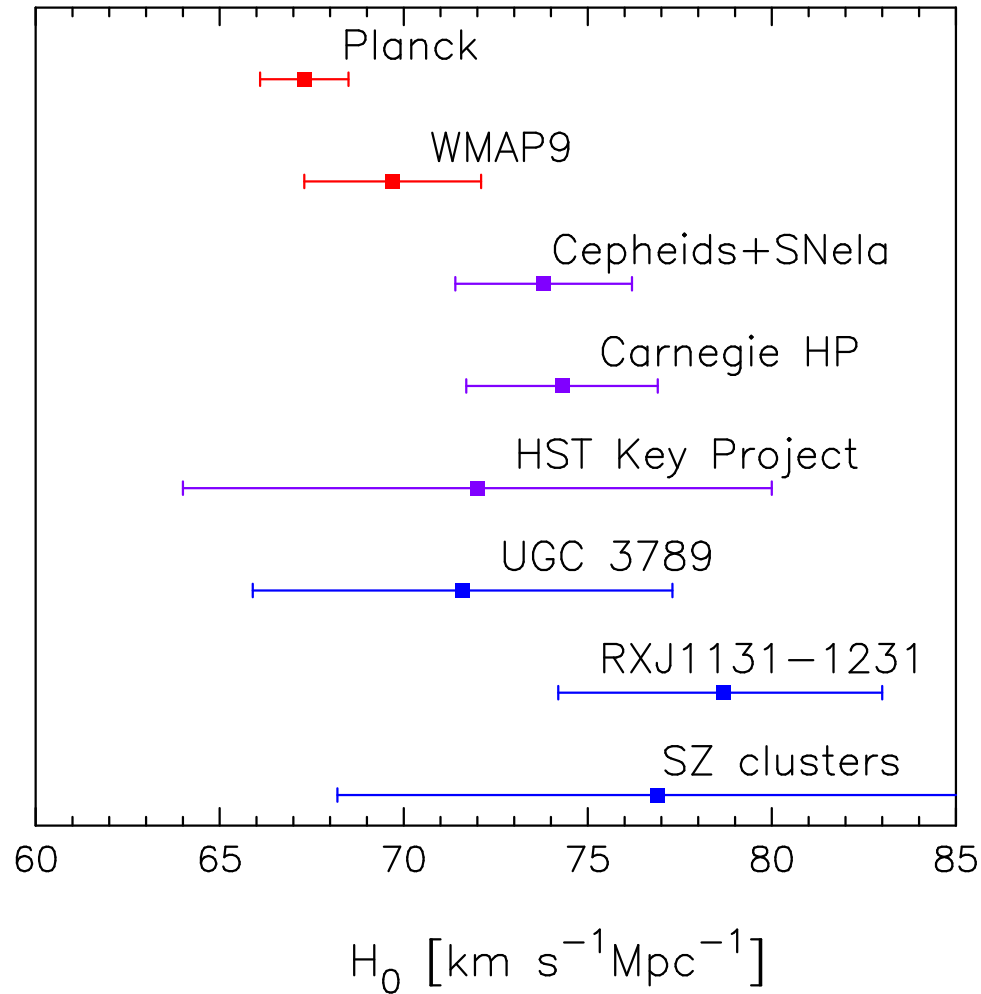
**Caveat IV.** Effect of Priors...

**Caveat V.** Comparing different cosmological models: do we really need adding one parameter wrt  $\Lambda$ CMD? (Bayesian evidence...)

Model	Data	$N_{eff}$	Ref.
$N_{eff}$	W-5+BAO+SN+ $H_0$	$4.13^{+0.87(+1.76)}_{-0.85(-1.63)}$	[346]
	W-5+LRG+ $H_0$	$4.16^{+0.76(+1.60)}_{-0.77(-1.43)}$	[346]
	W-5+CMB+BAO+XLF+ $f_{gas}$ + $H_0$	$3.4^{+0.6}_{-0.5}$	[349]
	W-5+LRG+maxBCG+ $H_0$	$3.77^{+0.67(+1.37)}_{-0.67(-1.24)}$	[346]
	W-7+BAO+ $H_0$	$4.34^{+0.86}_{-0.88}$	[338]
	W-7+LRG+ $H_0$	$4.25^{+0.76}_{-0.80}$	[338]
	W-7+ACT	$5.3 \pm 1.3$	[343]
	W-7+ACT+BAO+ $H_0$	$4.56 \pm 0.75$	[343]
	W-7+SPT	$3.85 \pm 0.62$	[344]
	W-7+SPT+BAO+ $H_0$	$3.85 \pm 0.42$	[344]
	W-7+ACT+SPT+LRG+ $H_0$	$4.08^{(+0.71)}_{(-0.68)}$	[350]
	W-7+ACT+SPT+BAO+ $H_0$	$3.89 \pm 0.41$	[351]
$N_{eff}+f_\nu$	W-7+CMB+BAO+ $H_0$	$4.47^{(+1.82)}_{(-1.74)}$	[352]
	W-7+CMB+LRG+ $H_0$	$4.87^{(+1.86)}_{(-1.75)}$	[352]
$N_{eff}+\Omega_k$	W-7+BAO+ $H_0$	$4.61 \pm 0.96$	[351]
	W-7+ACT+SPT+BAO+ $H_0$	$4.03 \pm 0.45$	[352]
$N_{eff}+\Omega_k+f_\nu$	W-7+ACT+SPT+BAO+ $H_0$	$4.00 \pm 0.43$	[351]
$N_{eff}+f_\nu+w$	W-7+CMB+BAO+ $H_0$	$3.68^{(+1.90)}_{(-1.84)}$	[352]
	W-7+CMB+LRG+ $H_0$	$4.87^{(+2.02)}_{(-2.02)}$	[352]
$N_{eff}+\Omega_k+f_\nu+w$	W-7+CMB+BAO+SN+ $H_0$	$4.2^{+1.10(+2.00)}_{-0.61(-1.14)}$	[353]
	W-7+CMB+LRG+SN+ $H_0$	$4.3^{+1.40(+2.30)}_{-0.54(-1.09)}$	[353]

Tab 3, white paper 1204.5379  
on light sterile neutrinos

# Planck found... Hubble<sub>0</sub> recession (to smaller value)



Planck XVI, 1303.5076

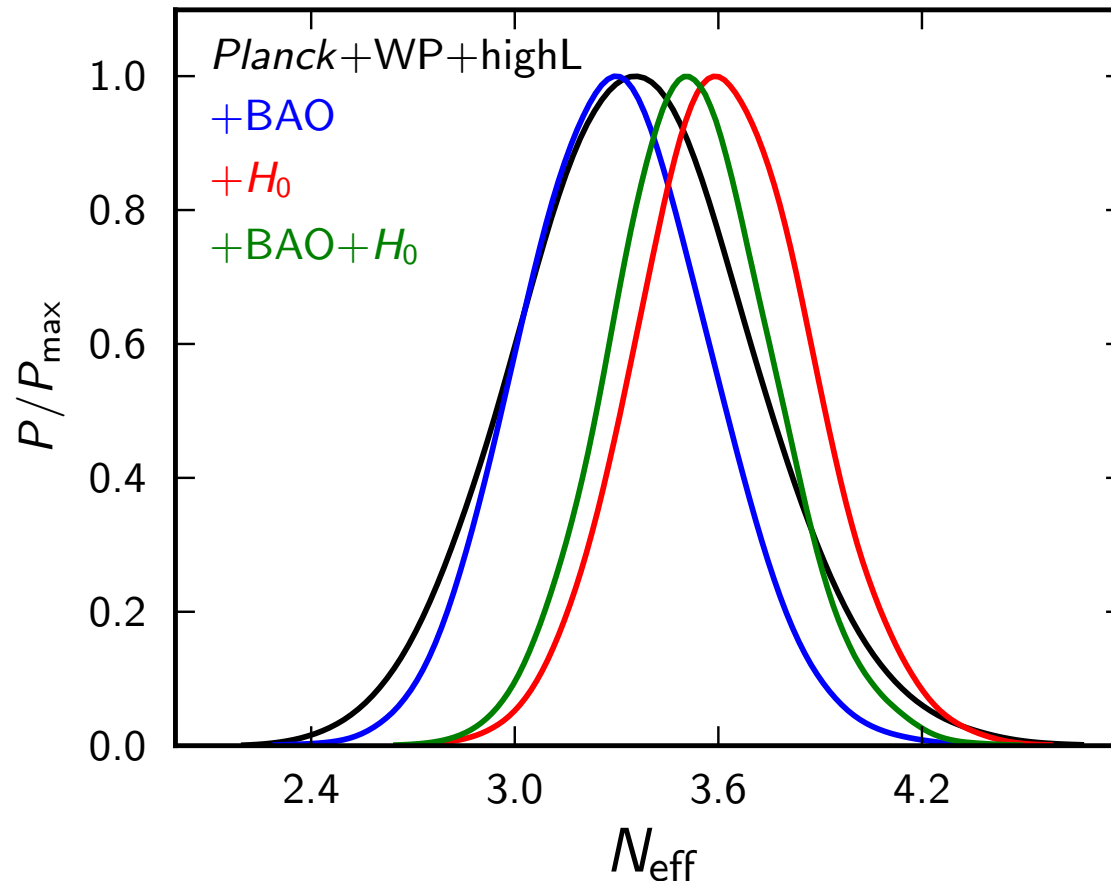
Using BAO and CMB data, we find  **$N_{\text{eff}} = 3.30 \pm 0.27$**  effective number of relativistic degrees of freedom, and an **upper limit of 0.23 eV** for the sum of neutrino masses. [Planck XVI, 2013]



# Not surprisingly...

Using BAO and CMB data, we find  **$N_{\text{eff}} = 3.30 \pm 0.27$**

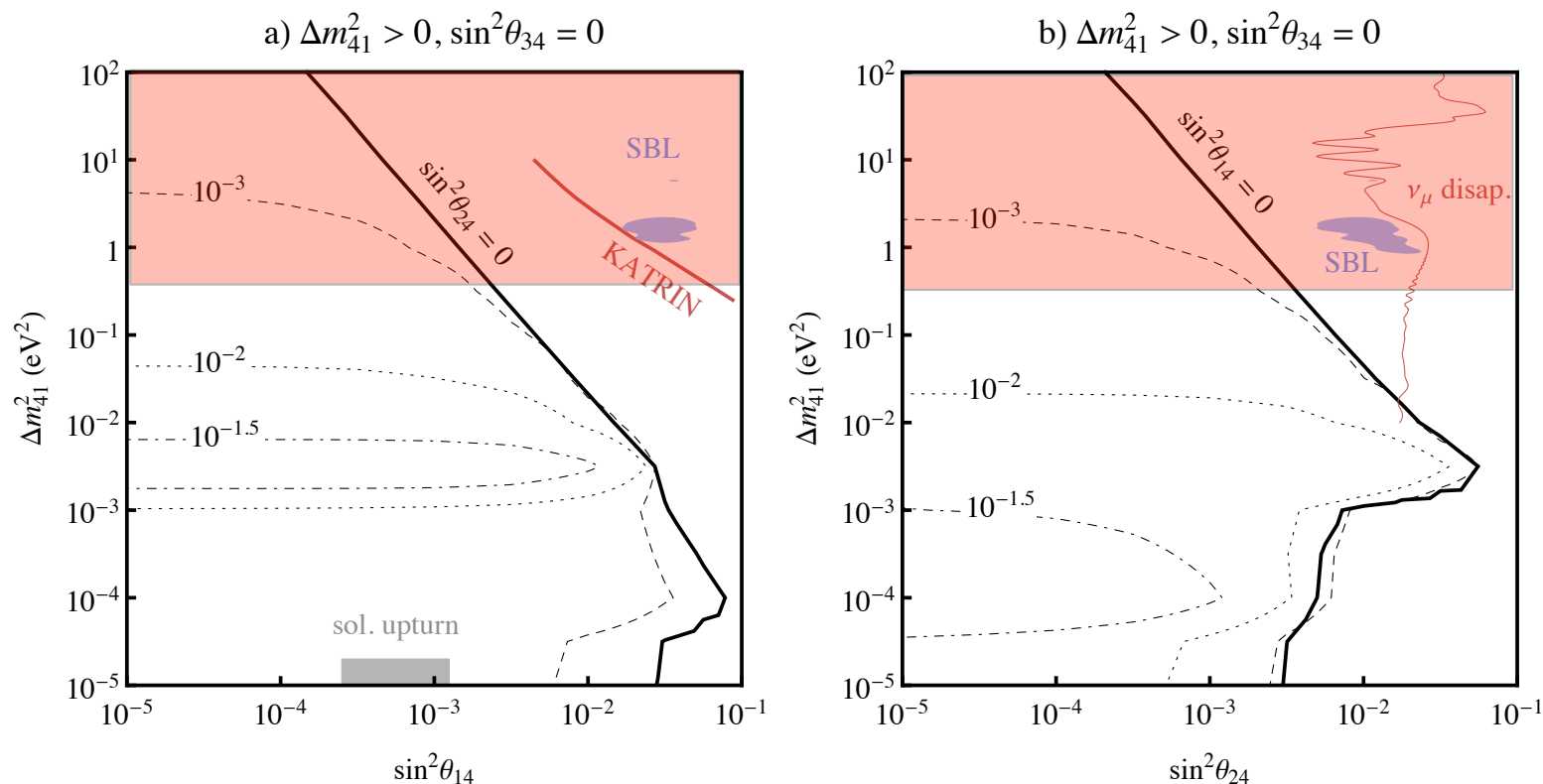
(WP: WMAP low- $l$  polarization)  
(highL: ACT, SPT, ground based)



Our results are in excellent agreement with BBN and the standard value of  $N_{\text{eff}}$

# In the relativistic limit at CMB epoch...

Just by imposing the above-mentioned 95% CL constraint on  $N_{\text{eff}}$ , the limit to the # of relativistic species excludes everything to the right of the curves...

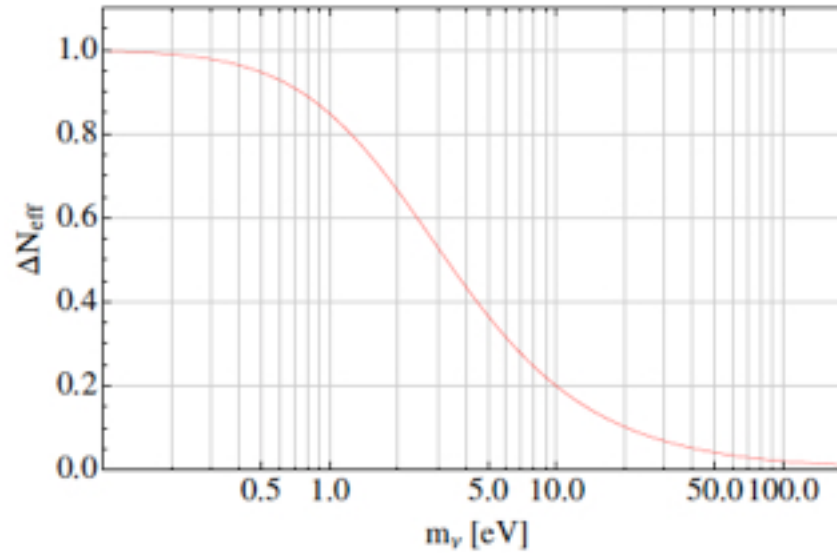


Other non vanishing mixing angles enlarge region where  $\Delta N_{\text{eff}} > 0.8$  is achieved.

**Note:** in the high-mass limit for the sterile, non-relativistic approximation breaks down, but mass constraints become important...

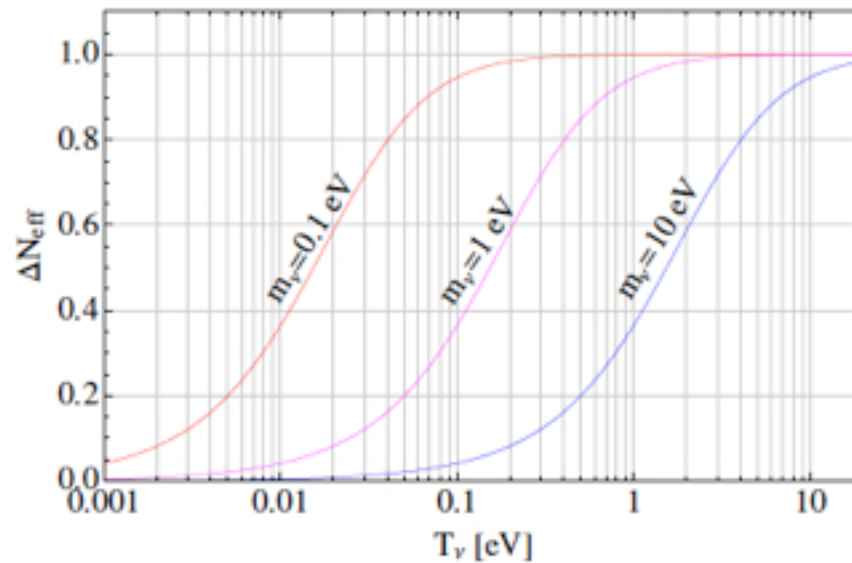
# Transition to non-relativistic

At matter-radiation equality, as function of  $m$



Jacques, Krauss,  
Lunardini  
arXiv:1301.3119

For 3 values of  $m$ , as function of  $T$



# Mass bounds (including Large Scale Structures)

# Before Planck...

Let us take seriously the  $\sim 2$  sigma preference for extra radiation.

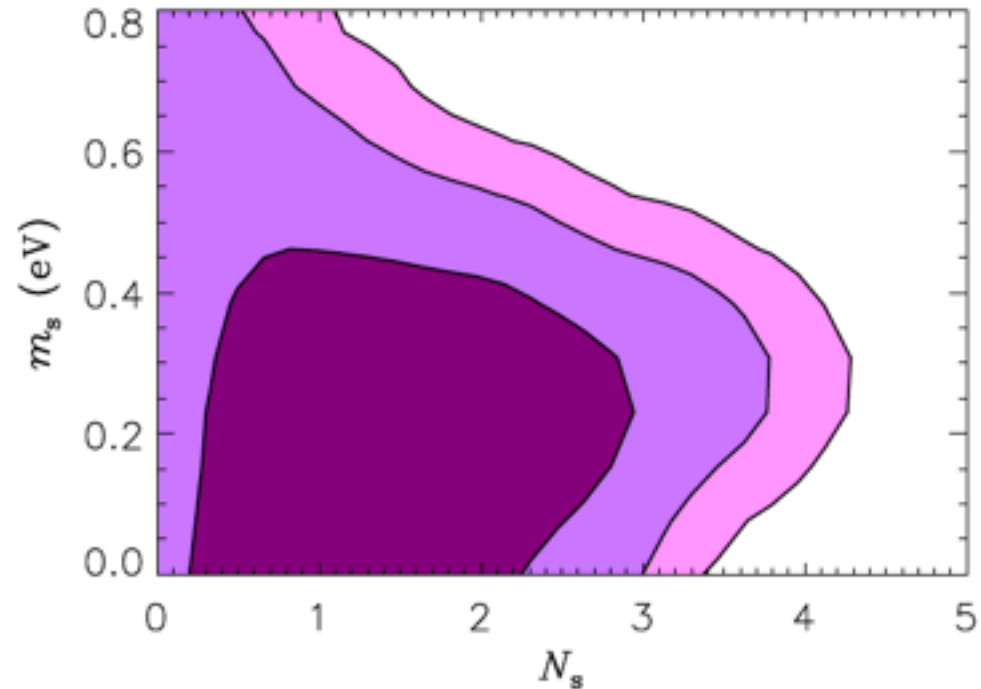
*Was it consistent with a “sterile  $\nu$  interpretation” in the “anomalies-preferred” parameter space?*

**Actually NOT!**

*Why? Because they were already inconsistent with CMB+LSS mass bounds!*

◆ In 3+1 models (fully thermalized)  
 **$m_4 < 0.48$  eV** (95% CL)  
(vs. about 1 eV expected from Lab)

◆ In 3+2 models (fully thermalized)  
 **$m_4 + m_5 < 0.9$  eV**  
(vs about 1.5 expected from Lab)



*J. Hamann et al., PRL 105, 181301 (2010)*

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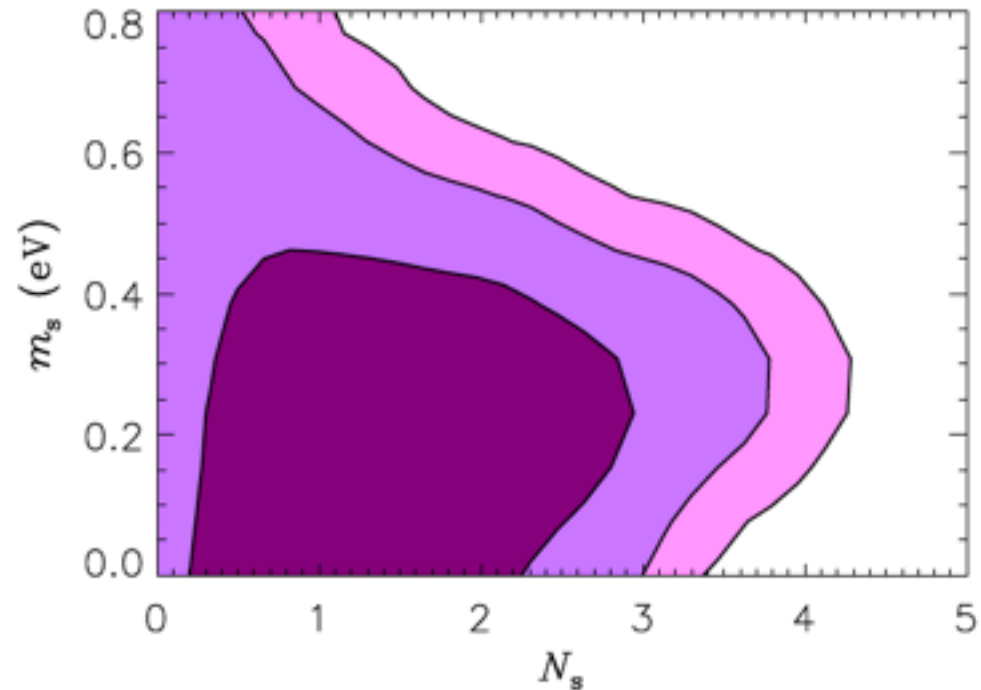
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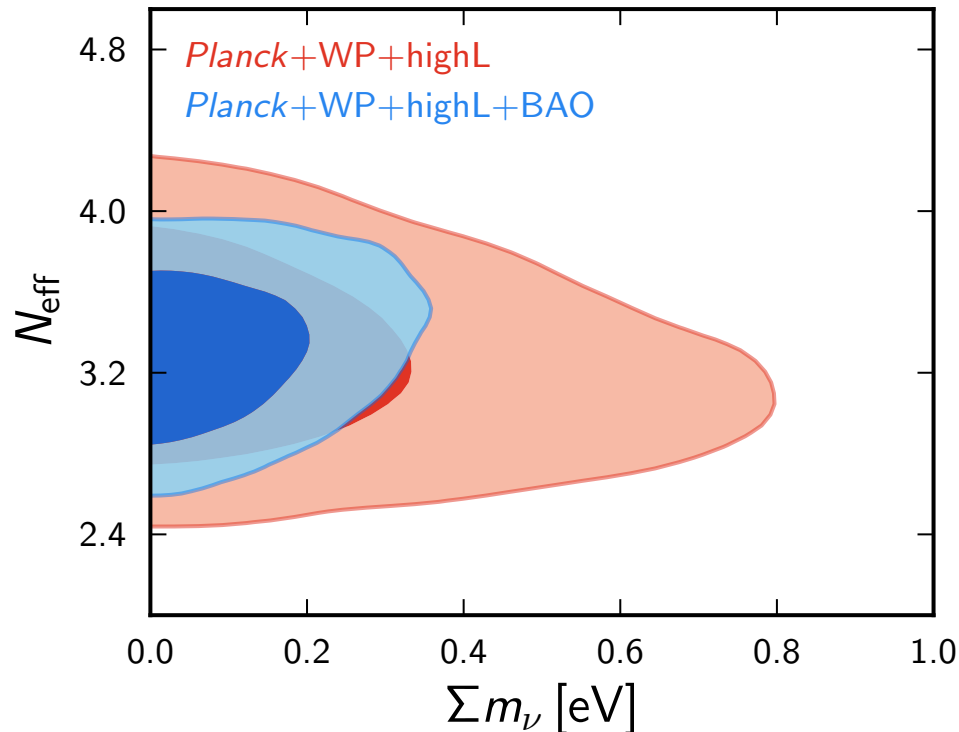
From a pure statistical point of view, adding eV scale massive neutrinos (1 or 2 states) was more disfavoured by cosmology than the weak preference for  $\Delta N_{\text{eff}} > 0$



*J. Hamann et al., PRL 105, 181301 (2010)*

# After Planck

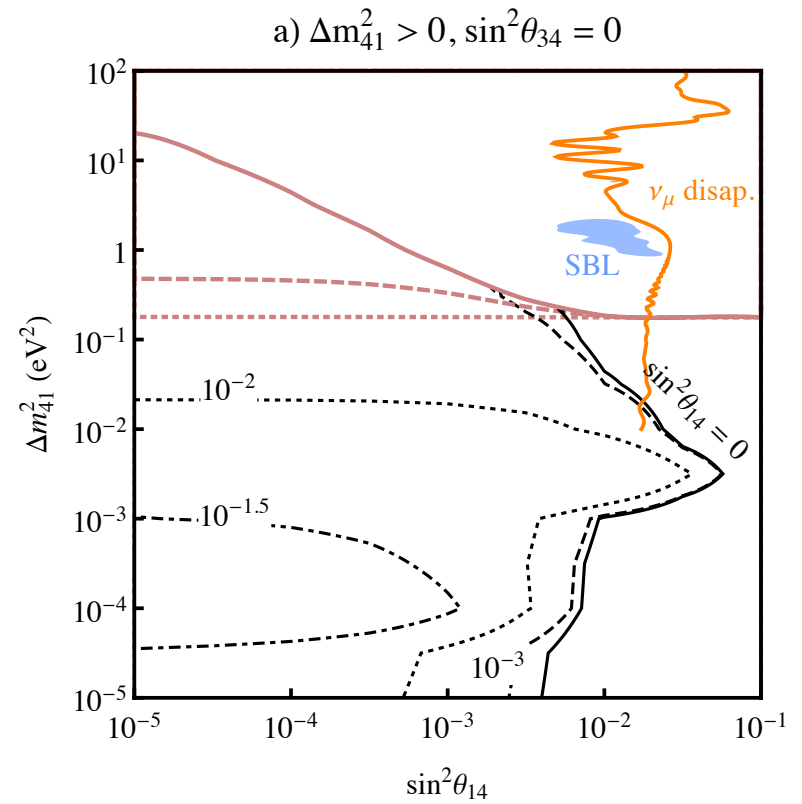
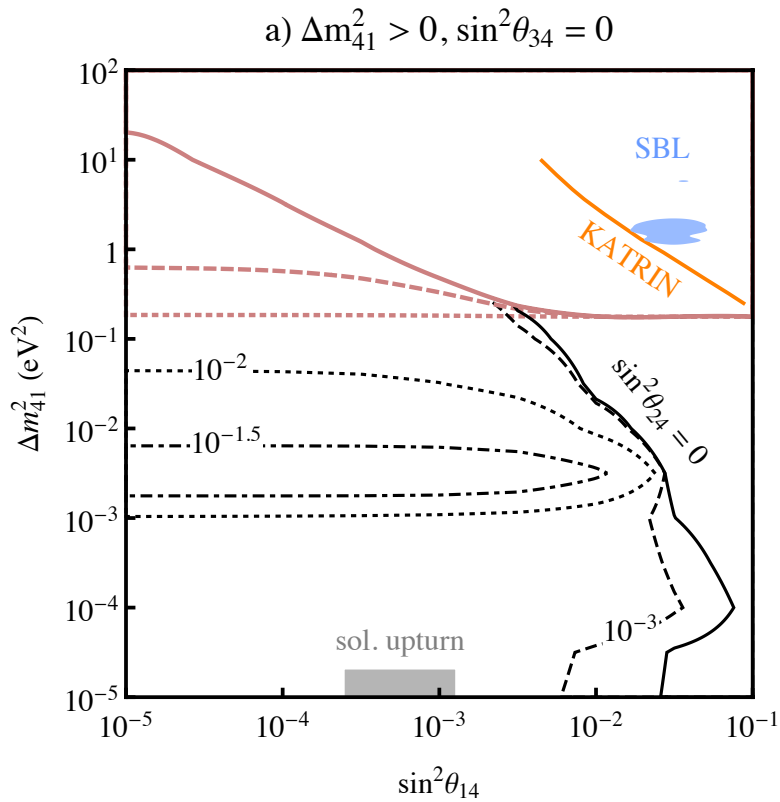
Using BAO and CMB data, we find an **upper limit of 0.23 eV for the sum of neutrino masses**. [Planck XVI, 2013]



here extra  $\nu$ 's are massless,  
active ones massive

Although the “self-consistent” bounds where it is the sterile (and in general non-thermally distributed) neutrino to be massive remain to be published, the obtained improvement suggests that the previous “exclusion” argument holds stronger!

# Preliminary results...



Courtesy A. Mirizzi et al.



# In Summary

BBN is barely consistent with  $N_{\text{eff}} \sim 4$ , but does not prefer significantly  $\Delta N_{\text{eff}} \geq 0$

The only data that somehow preferred (at  $\sim 2 \sigma$  value) a larger  $N_{\text{eff}}$   
were ***CMB in combination with others***

**But:**

LSS already excluded mass values needed to fit lab data

## **After-Planck**

- ✓ the former anomaly seems to be significantly gone
- ✓ Mass constraints are tighter

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## After-Planck

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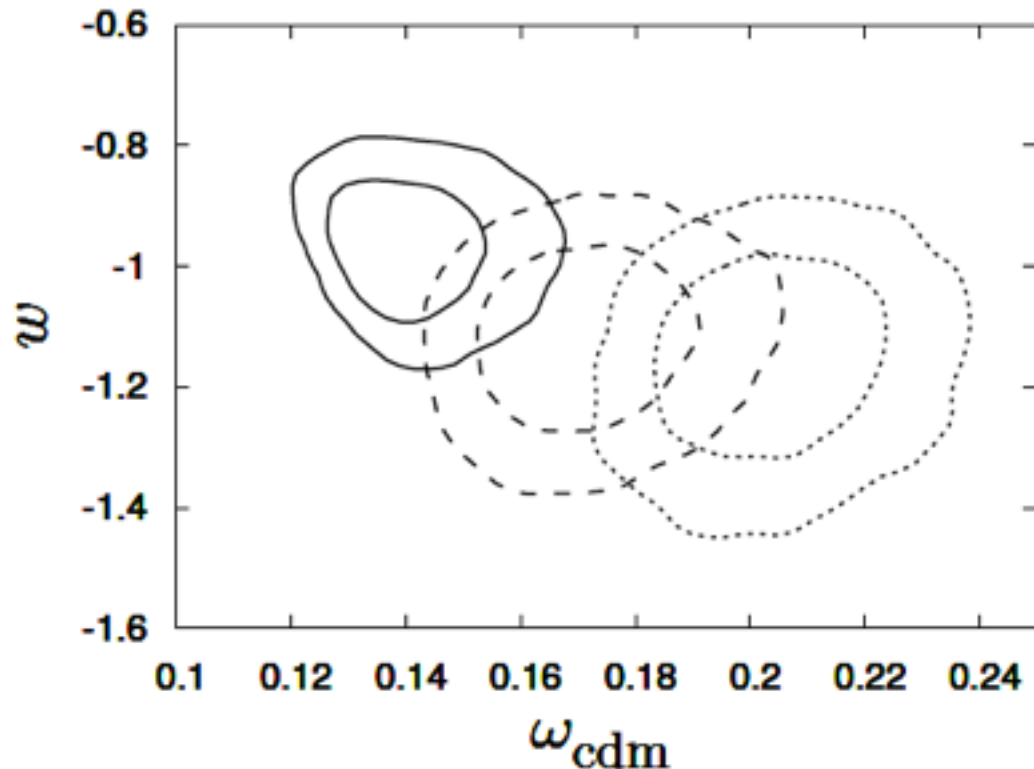
- ➔ Cosmology **does not** support sterile neutrino interpretations of Lab data. Rather, similarly to disappearance experiments, **it disfavors** them
- ➔ Feel free not to trust Cosmology, but **please do not interpret “anomalies” in  $N_{eff}$  (if any) as evidence for eV-scale sterile neutrinos**

# What if Lab confirms eV-scale sterile?

Need to go to contrived (exciting?!) cosmologies

- ✓ Introduce chemical potentials of  $O(0.1)$  to get around BBN (how to generate them?)
- ✓ modify dark energy sector (eg.  $w$ CDM) plus add additional non-massive radiation
- ✓ Explain why cluster determination of DM does not seem to fit (any idea?)

*see e.g. Hamann et al., 1108.4136*



Would be exciting... but unclear if/how well it works!

# Neutrino asymmetries as way out?

Introducing  $L_{\nu_\alpha} = \frac{n_{\nu_\alpha} - n_{\bar{\nu}_\alpha}}{n_\gamma} \simeq 0.7\xi_\alpha$  Suppresses thermalization of sterile  $\nu$ 's  
(Effective  $\nu_a$ - $\nu_s$  mixing reduced by large “matter”  
term  $\propto L$ )

**Caveat:  $L$  can also generate MSW-like resonant flavor conversions among active and sterile neutrinos enhancing their production**

A lot of work has been done in this direction, a non-exhaustive list:

*Enqvist et al., 1990, 1991, 1992; Foot, Thomson & Volkas, 1995; Bell, Volkas & Wong, 1998; Dolgov, Hansen, Pastor & Semikoz, 1999; Di Bari & Foot, 2000; Di Bari, Lipari and Lusignoli, 2000; Kirilova & Chizhov, 2000; Di Bari, Foot, Volkas & Wong, 2001; Dolgov & Villante, 2003; Abazajian, Bell, Fuller, Wong, 2005; Kishimoto, Fuller, Smith, 2006; Chu & Cirelli, 2006; Abazajian & Agrawal, 2008;*

**In a simplified scenario,  $L \sim 10^{-4}$  was found to be enough in order to have a significant reduction of the sterile neutrino abundance**

(and hardly associated to any other signature)

*e.g. Chu & Cirelli, 2006*

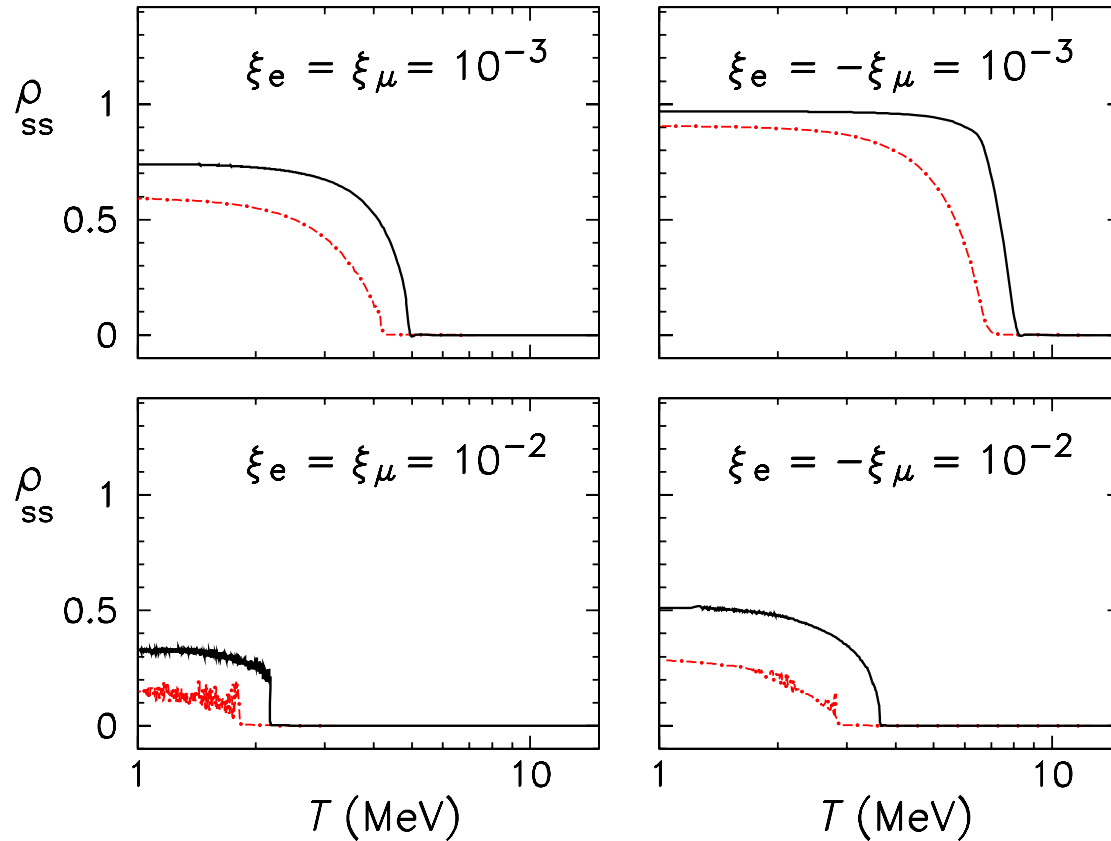
# Not so simple...

In *1206.1046*, *1302.1200* we relaxed many of the previous approximations, accounting for:

- ✓ 3+1, 2+1
- ✓ dynamic asymmetries
- ✓ realistic account of the  $\nu$ - $\nu$  coupling (non-linearities)
- ✓ Explored several scenarios and effects:
  - different and opposite asymmetries
  - CP violation
- ✓ Finally, relaxing the averaged momentum  
(full calculation, but for a specific choice of parameters)

We found that virtually any improvement wrt simplified treatments lead to a less and less effective inhibition of the population

# Results



- ✓ the asymmetry will quickly change sign (populating resonantly both neutrinos and antineutrinos)
- ✓ the asymmetry needed to significantly suppress thermalization is higher ( $\sim 0.01!$ )
- ✓ For such high values  $\rightarrow$  populated *after decoupling*  $\rightarrow$  significant spectral distortions  
 $\rightarrow$  “Large” effects on  $Y_p$ , altered  $Y_p$ - $N_{eff}$  relation (also for CMB analysis)

**Generating large asymmetries theoretically difficult & hard to account for properly: Not an “easy way out”!**

# Final message

- ★ **Cosmology is becoming a precision tool for neutrino physics:  $N_{eff}$  matches SM predictions with 1 sigma (~10% error), neutrino mass detection may be near!**
- ★ **There is a strong tension/exclusion with lab “anomalies”, if interpreted as due to eV scale sterile states...**
- ★ **... an eventual confirmation from the Lab would shake up not only particle physics standard model, but also the “standard cosmological model”, so I wish those looking for it all the best!**

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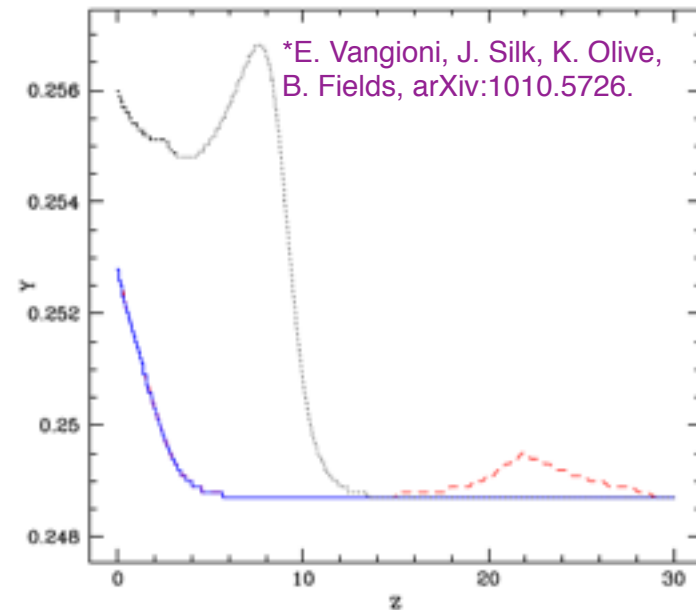
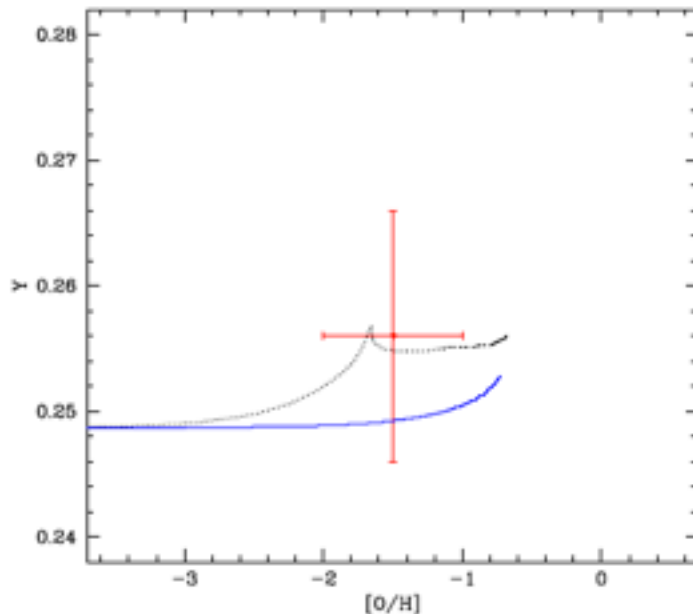
**Thank you for attention!**



Extra Slides

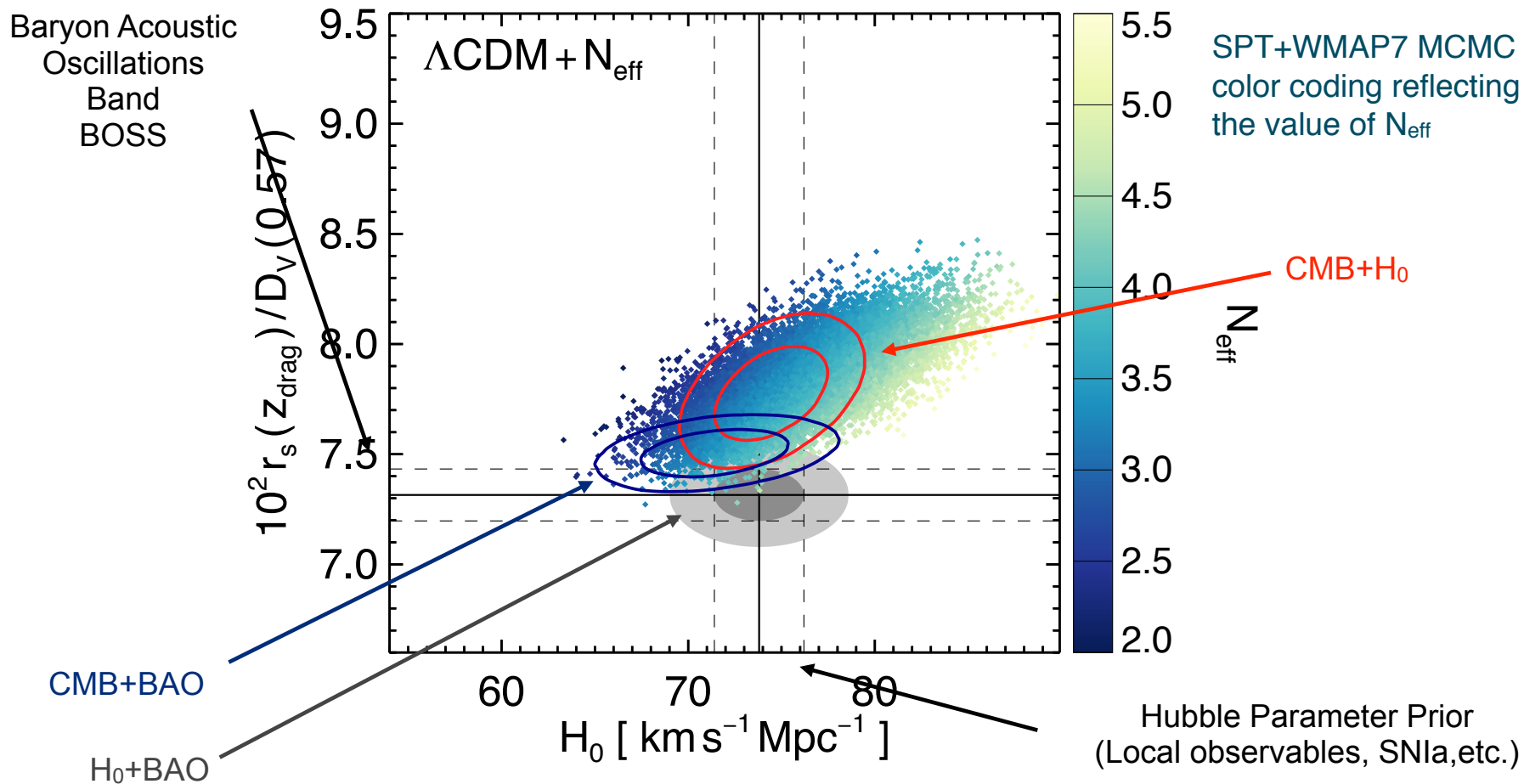
# Conclusions from BBN

- ✓ BBN imposes a conservative upper limit to the extra dof of about  $\Delta N_{\text{eff}} \leq 1$
- ✓ Even in a conservative analysis, there is only a slight preference ( $\sim 1 \sigma$ ) for  $\Delta N_{\text{eff}} \geq 0$
- ✓ Accounting for “astrophysical pollution” (including popII regression and popIII contribution) the upper limit could be converted into a plausible value of  $Y_p$  corresponding to  $\Delta N_{\text{eff}} \approx 0.5$  below what observed\* (almost centered on expectation). This is of course model-dependent, but suggest that there might be no anomaly at all in BBN...



\*See also R. Salvaterra, A. Ferrara, Mon. Not. Roy. Astron. Soc. 340 (2003) L17, astro-ph/0302285.

# Pre-PLANCK

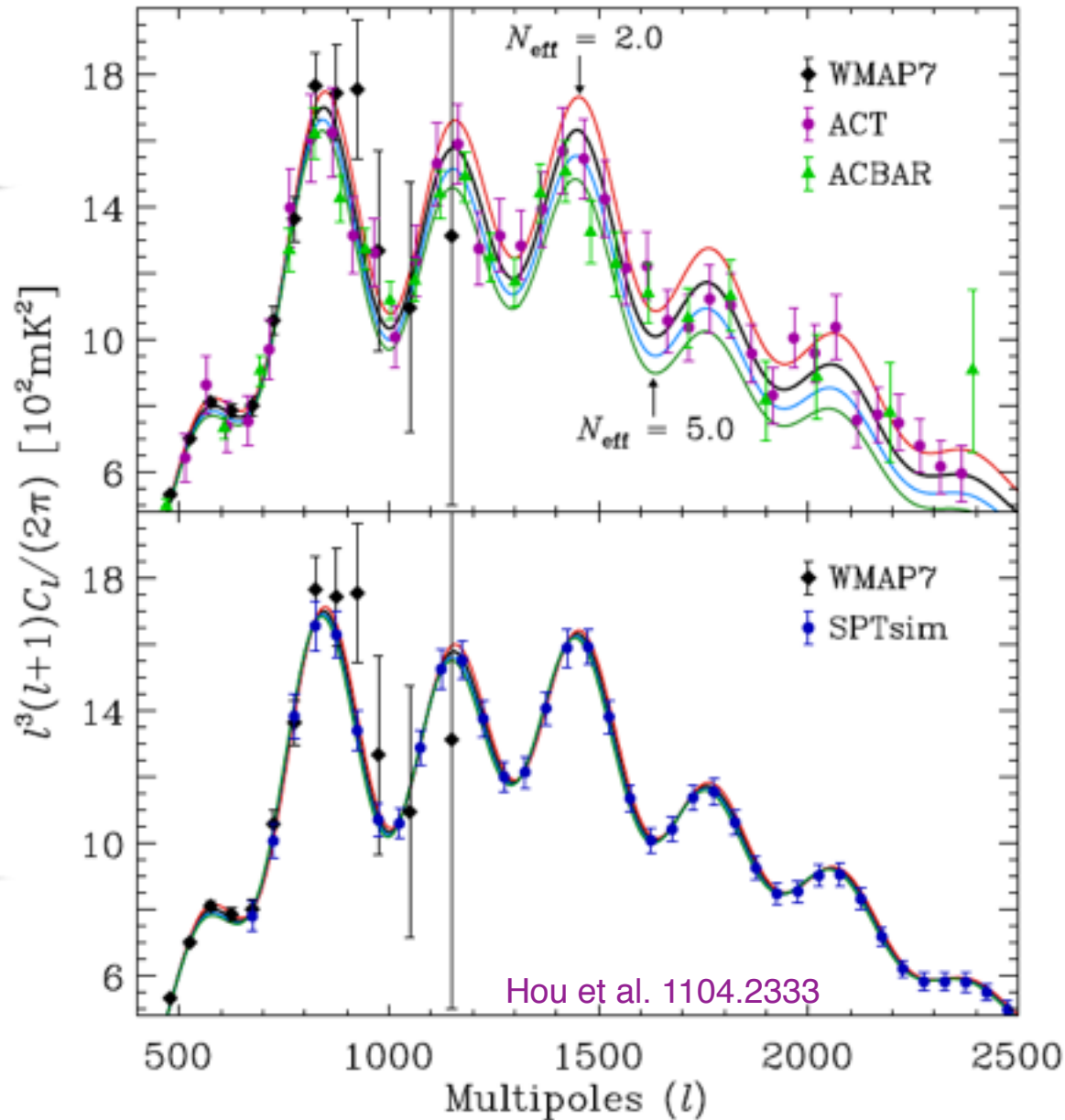


Hou et al., arXiv:1212.6267

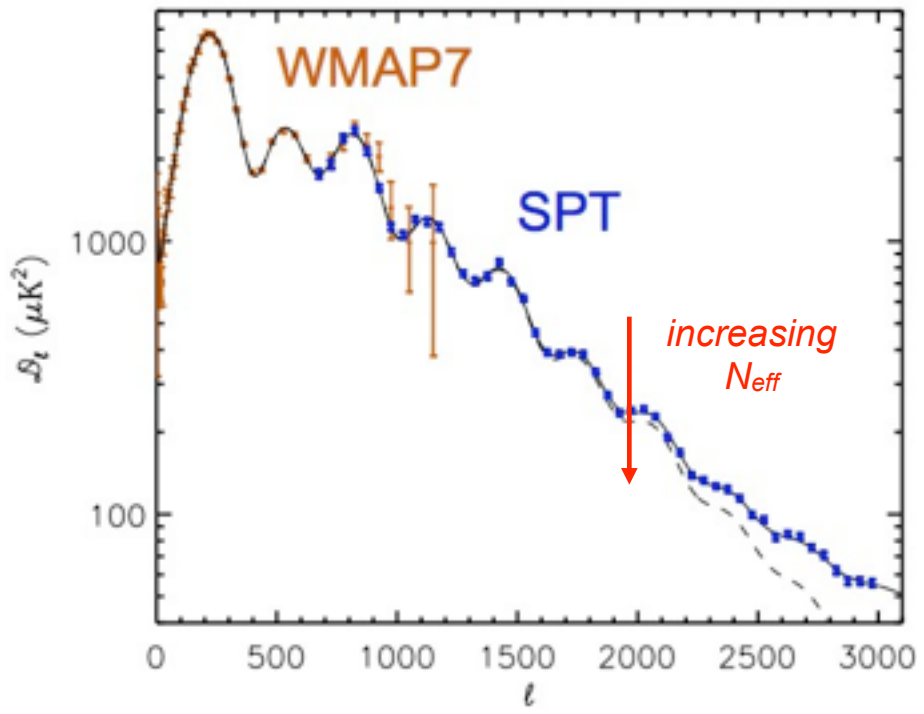
**In Short:** Pre-Planck CMB data alone by itself inconclusive on  $N_{\text{eff}}$  (but for a firm detection of  $N_{\text{eff}} > 0$ )  
It's only the combination with small-scale CMB data,  $H_0$  & BAO that gives  $\sim 2 \sigma$  preference for  $N_{\text{eff}} > 3$

# Alternative explanation of role of CMB damping tail

- ◆ Adjust:
  - Matter-radiation equality
  - Baryon density
  - Sound horizonto agree with WMAP-7 (1<sup>st</sup> peak, invisible in the plot...)
- ◆ Higher  $N_{\text{eff}}$  increases Silk damping at fixed  $z_{\text{eq}}$  (For an explanation see Hou et al. 1104.2333)
- ◆ Different  $N_{\text{eff}}$  visible in the damping tail (probed by ACT, ACBAR, SPT...)
- ◆ It's this tail that made significance higher

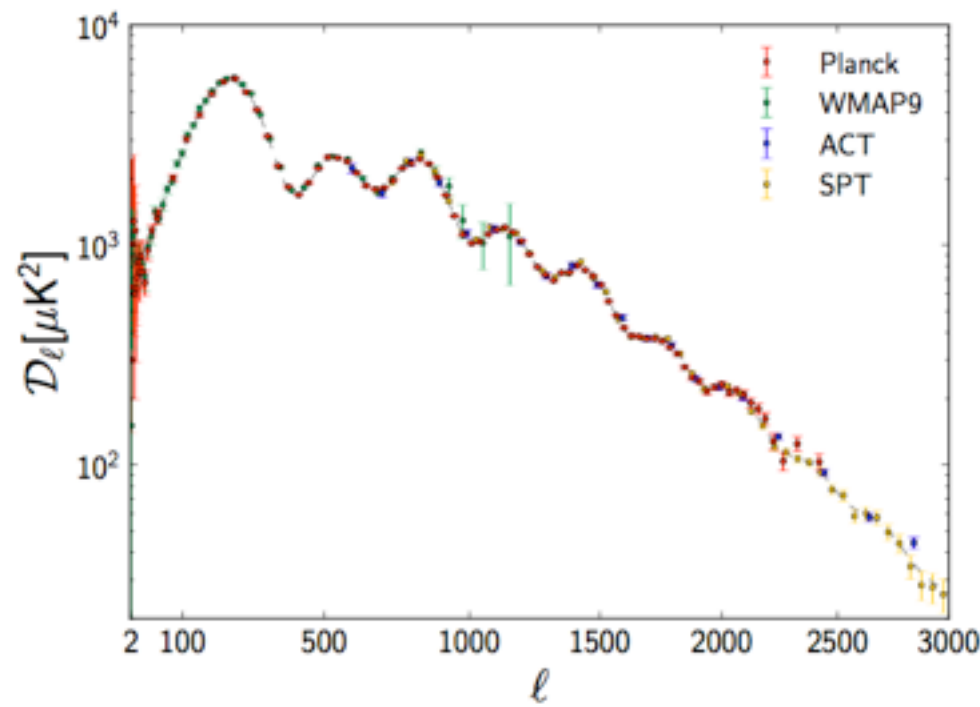


# Pre-Planck: challenging calibration of high- $l$

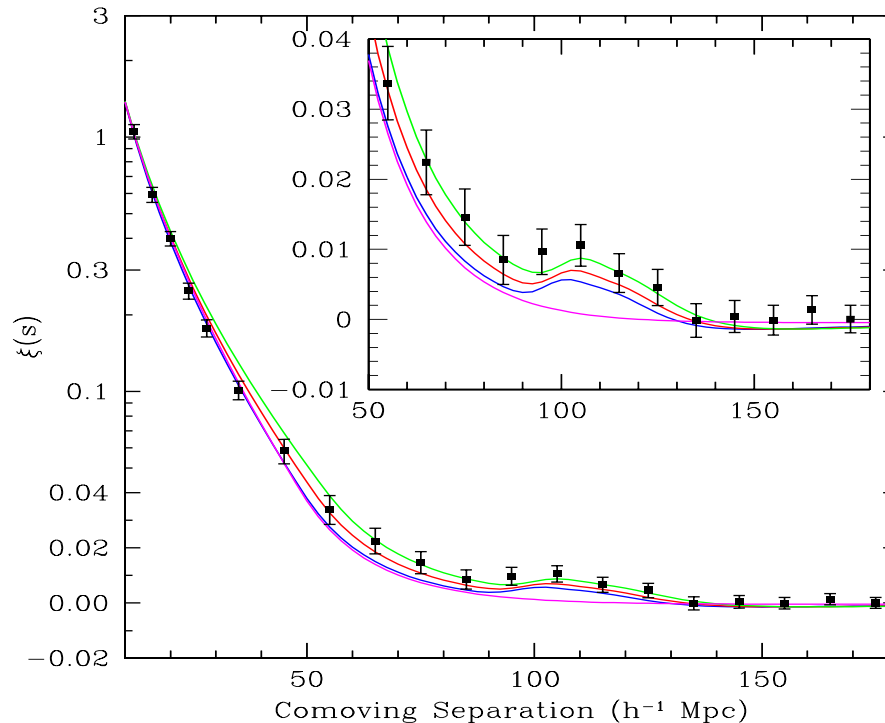


To combine with WMAP, SPT/ACT had to “anchor” at their largest scale (smallest scale for WMAP), with edges of angular range more prone to systematic errors...

Example where gained **resolution** in a **single instrument** does matter!



# what's the BAO



B. A. Bassett and R. Hlozek,  
arXiv:0910.5224

Fig. 1.1. The Baryon Acoustic Peak (BAP) in the correlation function – the BAP is visible in the clustering of the SDSS LRG galaxy sample, and is sensitive to the matter density (shown are models with  $\Omega_m h^2 = 0.12$  (**top**),  $0.13$  (**second**) and  $0.14$  (**third**), all with  $\Omega_b h^2 = 0.024$ ). The bottom line without a BAP is the correlation function in the pure CDM model, with  $\Omega_b = 0$ . From Eisenstein *et al.*, 2005 (52).

Preferred scale in clustering of galaxies, reflecting the acoustic peak of the CMB...  
hence can be used as “standard ruler” → one can make cosmology with it!