

Electromagnetic interactions of neutrinos

(Beyond Standard Model)

"Particle Physics and Cosmology"

XXV Rencontres de Blois
29/05/2013

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&

JINR - Dubna



2013

- *the standard Higgs boson*
(... probably ...)
- *the **Standard Model** experimental status confirmation*

... all people should focus on



*is the only
known*

particle with properties

***B**eyond*

***S**tandard*

***M**odel*

... problem and puzzle




is quite

invisible


particle

 exhibits unexpected properties (puzzles)

W. Pauli, 1930

- neutral “neutron” \Rightarrow  E. Fermi, 1933
- probably $\mu_\nu \neq 0$! ?
...recent claim for new experimental bound on μ_ν (with atomic ionization effect) continue chain of puzzles...
- Pauli himself wrote to Baade:

“Today I did something a physicist should never do. I predicted something which will never be observed experimentally...”



H. Bethe, R. Peierls, «The 'neutrino'»
Nature 133 (1934) 532,

- «There is no practically possible way of observing the neutrino»

... puzzles ...

- ...up to now absolute value

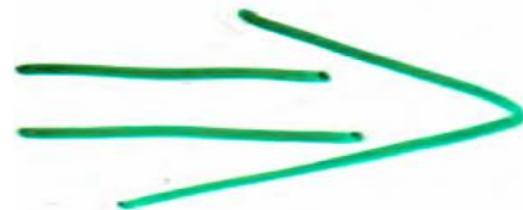
$$m_\nu \neq 0$$

after 80 years left

?



... however ...





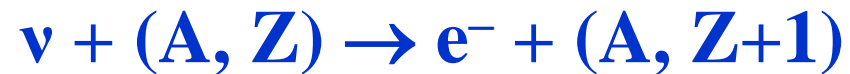
... an optimistic view
on the present
and future of ✓

In 1946
Bruno Pontecorvo:

“... observation of
neutrinos is not out
of question...”

Бруно Понтекорво

1913-1993



August 22, 2013

Centenary of the birth of Bruno Pontecorvo

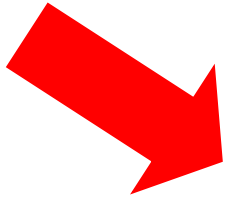
*weak interactions are
indeed weak*

$$L \sim 10^{15} \text{ km}$$

$$\bar{\nu} + p \rightarrow e^+ + n$$

$$E_\nu \sim 3 \text{ MeV}$$

... free path in water... $\sigma \sim 10^{-43} \text{ cm}^2$



*manifests itself most clearly
under the influence of
extreme external conditions:*

- *strong external electromagnetic fields*
and
- *dense background matter*

Outline (1)



*electromagnetic
properties*

(short review)



1

Carlo Giunti, Alexander Studenikin :
"Neutrino electromagnetic properties"
Phys.Atom.Nucl. 73, 2089-2125 (2009)

2

A.Studenikin : "Neutrino magnetic moment: a window to new physics"
Nucl.Phys.B (Proc.Supl.) 188, 220 (2009)

3

C. Giunti, A. Studenikin : "Electromagnetic properties of neutrino"
J.Phys.: Conf.Series. 203 (2010) 012100

4

C.Broggini, C.Giunti, A.Studenikin :
"Electromagnetic properties of neutrinos",
in: Special issue "Neutrino Physics"
(*Adv. iHigh Energy Phys.* 2012 (2012) 459526 (49 pp)
arXiv: 1207.3980 July 17, 2012



5

C.Giunti, A.Studenikin : "Theory and phenomenology
of neutrino electromagnetic properties"
Rev.Mod.Phys. (in preparation)

Outline (II)

- *results of recent experimental searches for upper bound on μ_ν*
(*GEMMA Coll. JINR-ITEP*)
- *our corresponding theoretical studies of ν - e scattering*
 - *proper treatment of “atomic ionization effect”*
- - *new bounds on ν electrical millicharge from μ_ν*

A.Studenikin, arXiv: 1302.1168, May 13, 2013

● “New bounds on neutrino millicharge from limits on magnetic moment”

K.Kouzakov, A.Studenikin,

● “Magnetic neutrino scattering on atomic electrons revisited”

Phys.Lett. B 105 (2011) 061801,

● “Electromagnetic neutrino-atom collisions: The role of electron binding”

Nucl.Phys.B (Proc.Suppl.) 217 (2011) 353

● K.Kouzakov, A.Studenikin, M.Voloshin,

● “Neutrino-impact ionization of atoms in search for neutrino magnetic moment”, Phys.Rev.D 83 (2011) 113001

● “On neutrino-atom scattering in searches for neutrino magnetic

moments” Nucl.Phys.B (Proc.Suppl.) 2011 (Proc. of Neutrino 2010 Conf.)

● “Testing neutrino magnetic moment in ionization of atoms

by neutrino impact”, JETP Lett. 93 (2011) 699

M.Voloshin,

● “Neutrino scattering on atomic electrons in search for neutrino

magnetic moment”

Phys.Rev.Lett. 105 (2010) 201801

Outline (III)

- ν quantum states in magnetized matter (new approach)

Spin Light of ν
in matter

$SL\nu$

1

ν energy
quantization in
rotating
matter

2

ν in matter treated within
«method of exact solutions»
of quantum wave equations for wave function

... basics of ν
electromagnetic properties

$$m_\nu \neq 0$$

... a tool for studying physics
Beyond Standard Model...

$$m_\nu \neq 0$$

Theory (Standard Model with ν_R)

$$\mu_\nu = \frac{3eG_F}{8\sqrt{2}\pi^2} m_\nu \sim 3 \cdot 10^{-19} \mu_B \left(\frac{m_\nu}{1\text{eV}} \right), \quad \mu_B = \frac{e}{2m_e}$$

Lee Shrock, 1977; Fujikawa Shrock, 1980

$$a_e = \frac{\alpha_{QED}}{2\pi} \sim 10^{-3}$$



... much greater values are desired
for astrophysical or cosmology

visualization of μ_ν

• Astrophysical bounds

$$\mu_\nu \leq 3 \cdot 10^{-12} \mu_B$$

G. Raffelt, D. Dearborn,
J. Silk, 1989.

• Theory (Standard Model with ν_R)

$$\mu_e = \frac{3eG_F}{8\sqrt{2}\pi^2} m_{\nu_e} \sim 3 \cdot 10^{-19} \mu_B \left(\frac{m_{\nu_e}}{1 \text{ eV}} \right), \quad \mu_B = \frac{e}{2m_e}$$

Lee Shrock, 1977; Fujikawa Shrock, 1980

• Limits from reactor ν - e scattering experiments

A. Bada et al. (GEMMA Coll.)
(2012):

$$\mu_\nu < 2.9 \times 10^{-11} \mu_B$$

...the present status...

to have visible $\mu \neq 0$

is not an easy task for

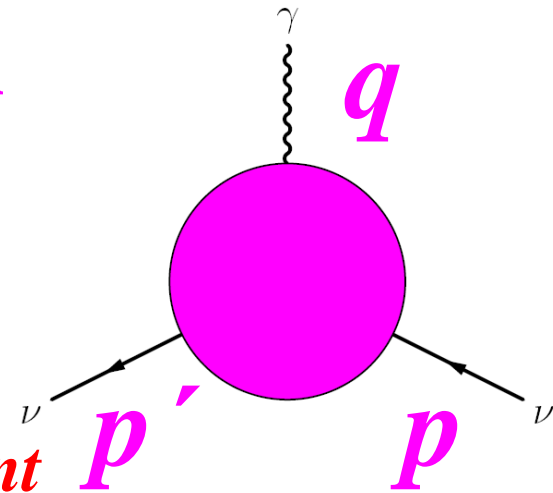
theoreticians

and experimentalists

*... a bit of  electromagnetic
properties theory ...*

✓ electromagnetic vertex function

$$\langle \psi(p') | J_\mu^{EM} | \psi(p) \rangle = \bar{u}(p') \Lambda_\mu(q, l) u(p)$$



Matrix element of **electromagnetic current** is a Lorentz vector

$\Lambda_\mu(q, l)$ should be constructed using

matrices $\hat{1}, \gamma_5, \gamma_\mu, \gamma_5 \gamma_\mu, \sigma_{\mu\nu},$

tensors $g_{\mu\nu}, \epsilon_{\mu\nu\sigma\gamma}$

vectors q_μ and l_μ

$$q_\mu = p'_\mu - p_\mu, \quad l_\mu = p'_\mu + p_\mu$$

Lorentz covariance (1)
and electromagnetic gauge invariance (2)



Matrix element of electromagnetic current between neutrino states

$$\langle \nu(p') | J_\mu^{EM} | \nu(p) \rangle = \bar{u}(p') \Lambda_\mu(q) u(p)$$

where vertex function generally contains 4 form factors

$$\Lambda_\mu(q) = f_Q(q^2) \gamma_\mu + f_M(q^2) i \sigma_{\mu\nu} q^\nu - f_E(q^2) \sigma_{\mu\nu} q^\nu \gamma_5 + f_A(q^2) (q^2 \gamma_\mu - q_\mu \not{q}) \gamma_5$$

1. electric dipole 2. magnetic 3. electric 4. anapole

● Hermiticity and discrete symmetries of EM current J_μ^{EM} put constraints on form factors

Dirac ✓

- 1) CP invariance + hermiticity $\implies f_E = 0$,
- 2) at zero momentum transfer **only** electric charge $f_Q(0)$ and magnetic moment $f_M(0)$ contribute $H_{int} \sim J_\mu^{EM} A^\mu$
- 3) hermiticity **itself** \implies three form factors are real: $Im f_Q = Im f_M = Im f_A = 0$

Majoran ✓

- 1) from CPT invariance (regardless CP or ~~CP~~).

$$f_Q = f_M = f_E = 0$$

...as early as 1939, W.Pauli...

EM properties \implies a way to distinguish **Dirac** and **Majorana** ✓

In general case **matrix element** of J_μ^{EM} can be considered between **different initial** $\psi_i(p)$ **and final** $\psi_j(p')$ **states of different masses**

$$p^2 = m_i^2, \quad p'^2 = m_j^2:$$

$$\langle \psi_j(p') | J_\mu^{EM} | \psi_i(p) \rangle = \bar{u}_j(p') \Lambda_\mu(q) u_i(p)$$

... beyond SM...

and

$$\Lambda_\mu(q) = \left(f_Q(q^2)_{ij} + f_A(q^2)_{ij} \gamma_5 \right) (q^2 \gamma_\mu - q_\mu \not{q}) + f_M(q^2)_{ij} i \sigma_{\mu\nu} q^\nu + f_E(q^2)_{ij} \sigma_{\mu\nu} q^\nu \gamma_5$$

form factors are matrices in \checkmark mass eigenstates space.

Dirac \checkmark (*off-diagonal case* $i \neq j$) Majorana \checkmark

1) ~~hermiticity itself~~ does not apply restrictions on form factors,

1) CP invariance + hermiticity

2) CP invariance + hermiticity

$$\mu_{ij}^M = 2\mu_{ij}^D \quad \text{and} \quad \epsilon_{ij}^M = 0 \quad \text{or}$$

... quite different EM properties ...

$$\mu_{ij}^M = 0 \quad \text{and} \quad \epsilon_{ij}^M = 2\epsilon_{ij}^D$$

$$f_Q(q^2), f_M(q^2), f_E(q^2), f_A(q^2)$$

are relatively real (no relative phases).

... importance of μ_ν studies...

If diagonal $\mu_\nu \neq 0$

were confirmed

then \checkmark Dirac

... for \checkmark Majorana
non-diagonal = transitional
 $\mu_\nu \neq 0$

... progress
in experimental studies of μ_ν \Rightarrow



magnetic moment in experiments

Samuel Ting

*(have written on the wall at Department of
Theoretical Physics of Moscow State University) :*

“Physics is an experimental science”

Studies of ν - e scattering - most sensitive method of experimental investigation of μ_ν

Cross-section:

$$\bullet \quad \frac{d\sigma}{dT}(\nu + e \rightarrow \nu + e) = \left(\frac{d\sigma}{dT}\right)_{\text{SM}} + \left(\frac{d\sigma}{dT}\right)_{\mu_\nu}$$

where the Standard Model contribution

$$\bullet \quad \left(\frac{d\sigma}{dT}\right)_{\text{SM}} = \frac{G_F^2 m_e}{2\pi} \left[(g_V + g_A)^2 + (g_V - g_A)^2 \left(1 - \frac{T}{E_\nu}\right)^2 + (g_A^2 - g_V^2) \frac{m_e T}{E_\nu^2} \right],$$

T is the electron recoil energy and

$$\bullet \quad \left(\frac{d\sigma}{dT}\right)_{\mu_\nu} = \frac{\pi \alpha_{em}^2}{m_e^2} \left[\frac{1 - T/E_\nu}{T} \right] \mu_\nu^2$$

$$\mu_\nu^2 = \sum_{j = \nu_e, \nu_\mu, \nu_\tau} |\mu_{ij} - \epsilon_{ij}|^2$$

$$g_V = \begin{cases} 2 \sin^2 \theta_W + \frac{1}{2} & \text{for } \nu_e, \\ 2 \sin^2 \theta_W - \frac{1}{2} & \text{for } \nu_\mu, \nu_\tau, \end{cases} \quad g_A = \begin{cases} \frac{1}{2} & \text{for } \nu_e, \\ -\frac{1}{2} & \text{for } \nu_\mu, \nu_\tau \end{cases} \quad \text{for anti-neutrinos } g_A \rightarrow -g_A$$

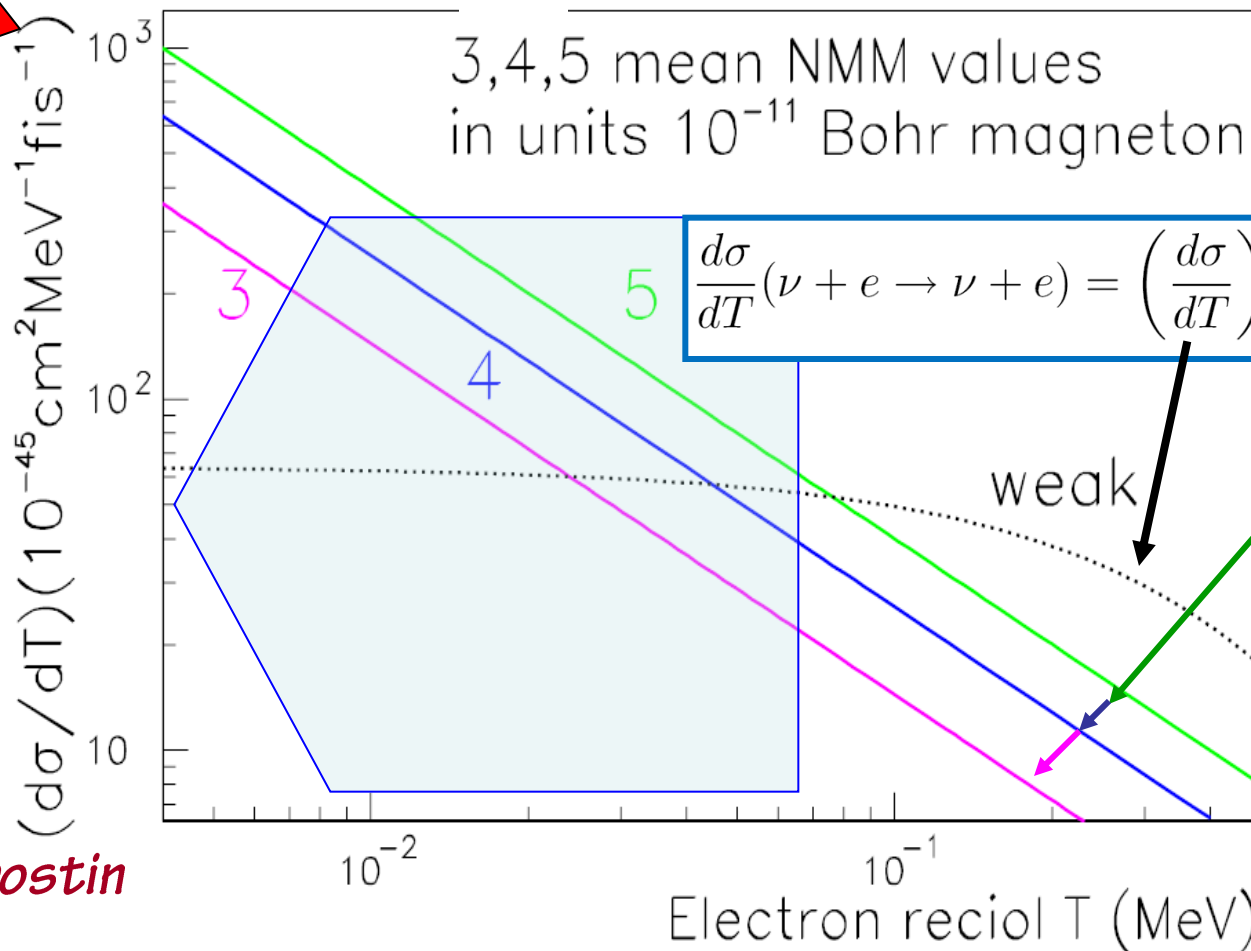
to incorporate charge radius: $g_V \rightarrow g_V + \frac{2}{3} M_W^2 \langle r^2 \rangle \sin^2 \theta_W$

Magnetic moment contribution is dominated at low electron

recoil energies when $\left(\frac{d\sigma}{dT}\right)_{\mu\nu} > \left(\frac{d\sigma}{dT}\right)_{SM}$ and

$$\frac{T}{m_e} < \frac{\pi^2 \alpha_{em}}{G_F^2 m_e^4} \mu_\nu^2$$

... the lower the smallest measurable electron recoil energy is, the smaller values of μ_ν^2 can be probed in scattering experiments ...



from
A. Starostin



MUNU experiment at Bugey reactor (2005)

$$\mu_{\nu} \leq 9 \times 10^{-11} \mu_B$$

TEXONO collaboration at Kuo-Sheng power plant (2006)

$$\mu_{\nu} \leq 7 \times 10^{-11} \mu_B$$

GEMMA (2007)

$$\mu_{\nu} \leq 5.8 \times 10^{-11} \mu_B$$

GEMMA I 2005 - 2007

BOREXINO (2008)

$$\mu_{\nu} \leq 5.4 \times 10^{-11} \mu_B$$

...was considered as the world best constraint...

$$\mu_{\nu} \leq 8.5 \times 10^{-11} \mu_B \quad (\nu_{\tau}, \nu_{\mu})$$

*based on first release of
BOREXINO data*

*Montanino,
Picariello,
Pulido, PRD 2008*

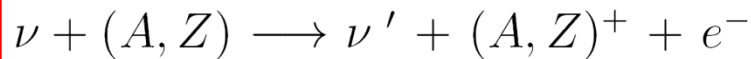
*... attempts to
improve bounds*



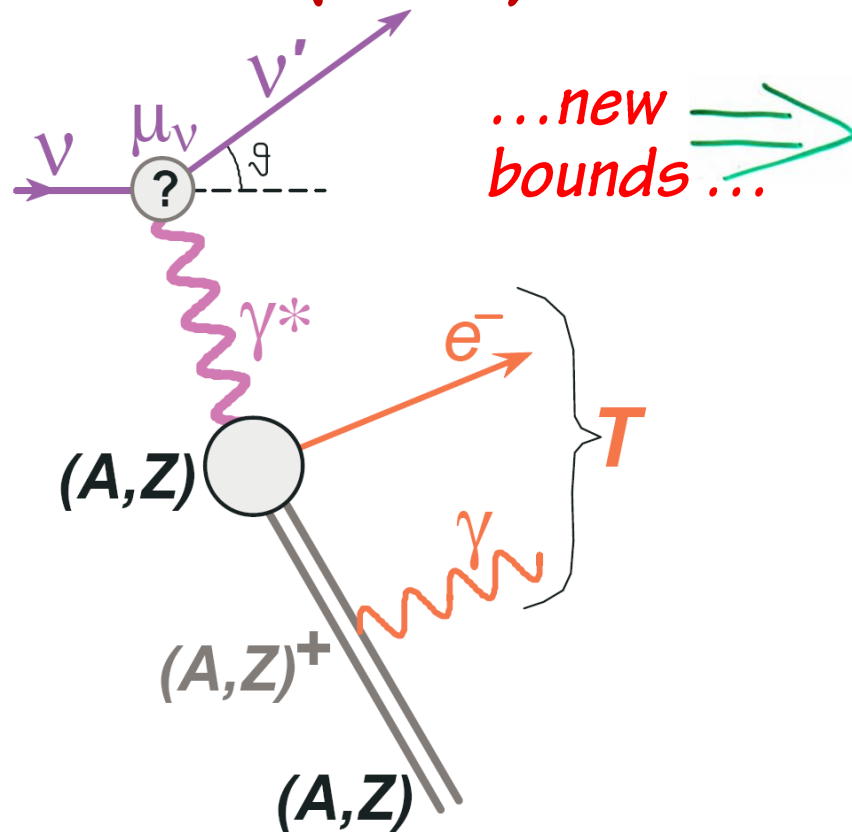
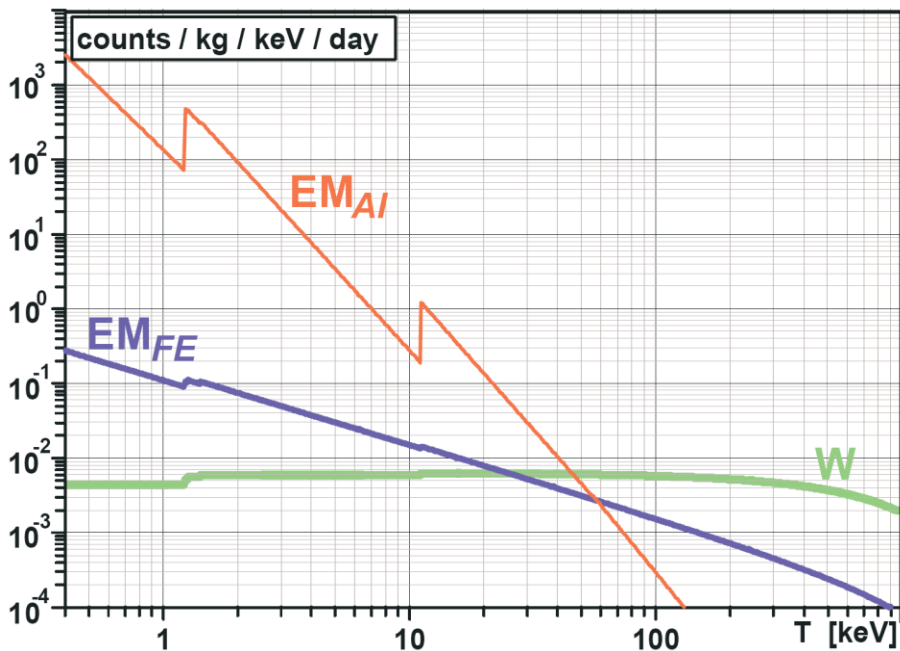
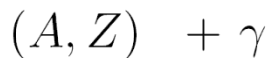
... quite recent *claim*
 that ν - e cross section
 should be increased by
Atomic Ionization effect:



H.Wong et al. (TEXONO Coll.),
 arXiv: 1001.2074,
 13 Jan 2010,
 reported at
 Neutrino 2010 Conference
 (Athens, June 2010),
 PRL 105 (2010) 061801



↓ recombination



...much better limits on ν effective magnetic moment ...


$$\mu_\nu < 1.3 \times 10^{-11} \mu_B$$

?



... atomic ionization effect accounted for ...

H.Wong et al.,
(TEXONO Coll.),
arXiv: 1001.2074,
13 Jan 2010,
PRL 105 (2010)
061801

Neutrino 2010 Conference, Athens

... however ...



$$\mu_\nu < 5.0 \times 10^{-12} \mu_B$$

?



... atomic ionization effect accounted for ...

A.Beda et al.
(GEMMA Coll.),
arXiv: 1005.2736,
16 May 2010

$$\mu_\nu < 3.2 \times 10^{-11} \mu_B$$



... ν - e scattering on free electrons ...
(without atomic ionization)

K.Kouzakov, A.Studenikin,

- “Magnetic neutrino scattering on atomic electrons revisited” ●
Phys.Lett. B 105 (2011) 061801, arXiv: 1011.5847
- “Electromagnetic neutrino-atom collisions: The role of electron binding”
Nucl.Phys.B (Proc.Suppl.) 217 (2011) 353

K.Kouzakov, A.Studenikin, M.Voloshin,

- “Neutrino-impact ionization of atoms in search for neutrino magnetic moment”, **Phys.Rev.D** 83 (2011) 113001
- “On neutrino-atom scattering in searches for neutrino magnetic moments” **Nucl.Phys.B (Proc.Supp.)** 2011 (Proc. of Neutrino 2010 Conf.)
- “Testing neutrino magnetic moment in ionization of atoms by neutrino impact”, **JETP Lett.** 93 (2011) 699

M.Voloshin,

- “Neutrino scattering on atomic electrons in search for neutrino magnetic moment”
Phys.Rev.Lett. 105 (2010) 201801, arXiv: 1008.2171

*No important effect of Atomic Ionization
on cross section in μ , experiments
once all possible final electronic states
accounted for*

... free electron approximation can be used ...

M.Voloshin, 23 Aug 2010;

K.Kouzakov, A.Studenikin, 26 Nov 2010;

H.Wong et al, arXiv: 1001.2074 V3, 28 Nov 2010



GEMMA (2005-2012)

JINR (Dubna) + ITEP (Moscow) at Kalinin Nuclear Power Plant

World best experimental limit

$$\mu_\nu < 2.9 \times 10^{-11} \mu_B$$

June 2012

*A. Beda et al, in: **Special Issue on “Neutrino Physics”**,
Advances in High Energy Physics (2012) 2012,
editors: J.Bernabeu, G. Fogli, A.McDonald, K. Nishikawa*

... quite realistic prospects of the near future

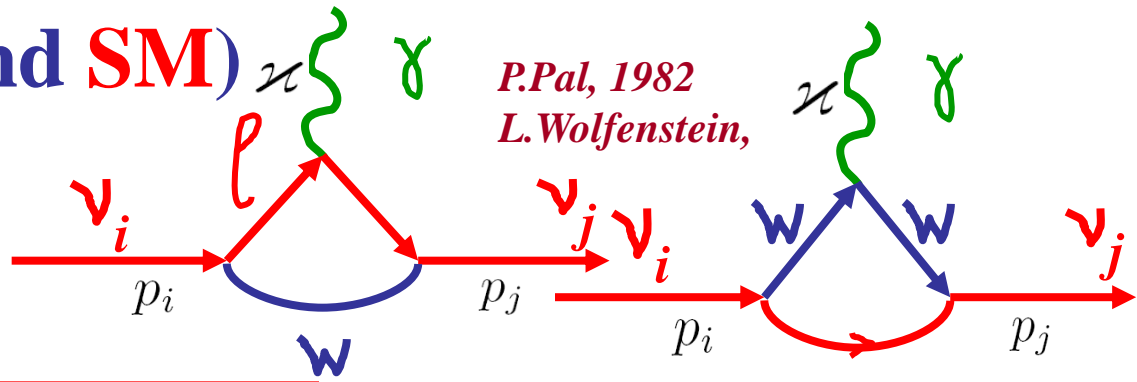
$$\mu_\nu \sim 1 \times 10^{-11} \mu_B$$

*(V.Brudanin,
A.Starostin,
priv. comm.)*

3.5 Neutrino (beyond SM) dipole moments

(+ transition moments)

P.Pal, 1982
L.Wolfenstein,



Dirac neutrino

$$\left. \begin{matrix} \mu_{ij} \\ \epsilon_{ij} \end{matrix} \right\} = \frac{eG_F m_i}{8\sqrt{2}\pi^2} \left(1 \pm \frac{m_j}{m_i}\right) \sum_{l=e, \mu, \tau} f(r_l) U_{lj} U_{li}^*$$

$$r_l = \left(\frac{m_l}{m_W}\right)^2$$

- $m_e = 0.5 \text{ MeV}$
- $m_\mu = 105.7 \text{ MeV}$
- $m_\tau = 1.78 \text{ GeV}$
- $m_W = 80.2 \text{ GeV}$

$m_i, m_j \ll m_l, m_W$

$\Rightarrow f(r_l) \approx \frac{3}{2} \left(1 - \frac{1}{2} r_l\right), r_l \ll 1$

transition moments vanish because unitarity of U implies that its rows or columns represent orthogonal vectors

Majorana neutrino only for

$$i \neq j$$

$$\mu_{ij}^M = 2\mu_{ij}^D \text{ and } \epsilon_{ij}^M = 0$$

or

$$\mu_{ij}^M = 0 \text{ and } \epsilon_{ij}^M = 2\epsilon_{ij}^D$$

transition moments are suppressed, Glashow-Iliopoulos-Maiani cancellation, for diagonal moments there is no GIM cancellation

... depending on relative CP phase of ν_i and ν_j

The first nonzero contribution from **neutrino transition moments**

$$f_{r_l} \rightarrow -\cancel{\frac{3}{2}} + \frac{3}{4} \left(\frac{m_l}{m_W} \right)^2 \ll 1$$

GIM cancellation

$$\left. \begin{matrix} \mu_{ij} \\ \epsilon_{ij} \end{matrix} \right\} = \frac{3eG_F m_i}{32\sqrt{2}\pi^2} \left(1 \pm \frac{m_j}{m_i} \right) \left(\frac{m_\tau}{m_W} \right)^2 \sum_{l=e, \mu, \tau} \left(\frac{m_l}{m_\tau} \right)^2 U_{lj} U_{li}^*$$

$$\mu_B = \frac{e}{2m_e}$$

$$\left. \begin{matrix} \mu_{ij} \\ \epsilon_{ij} \end{matrix} \right\} = 4 \times 10^{-23} \mu_B \left(\frac{m_i \pm m_j}{1 \text{ eV}} \right) \sum_{l=e, \mu, \tau} \left(\frac{m_l}{m_\tau} \right)^2 U_{lj} U_{li}^*$$

... **neutrino radiative decay is very slow**

● **Dirac** \checkmark **diagonal (i=j)** **magnetic moment**

$$\epsilon_{ii}^D = 0 \text{ for } CP\text{-invariant interactions}$$

$$\mu_{ii} = \frac{3eG_F m_i}{8\sqrt{2}\pi^2} \left(1 - \frac{1}{2} \sum_{l=e, \mu, \tau} r_l |U_{li}|^2 \right) \approx 3.2 \times 10^{-19} \left(\frac{m_i}{1 \text{ eV}} \right) \mu_B$$

$r_l = \left(\frac{m_l}{m_W} \right)^2$

$$\mu_{ii}^M = \epsilon_{ii}^M = 0$$

Lee, Shrock, Fujikawa, 1977

● **no GIM cancellation**

● μ_{ii}^D - to leading order - **independent on** U_{li} **and** $m_{l=e, \mu, \tau}$

$$\mu_e^2 = \sum_{i=1,2,3} |U_{ie}|^2 \mu_{ii}^2$$

...possibility to measure fundamental μ_{ii}^D

$\mu_{ii}^D = 0$ for **massless** \checkmark (in the absence of **right-handed charged currents**) \rightarrow

3.6 Neutrino magnetic moment in left-right symmetric models

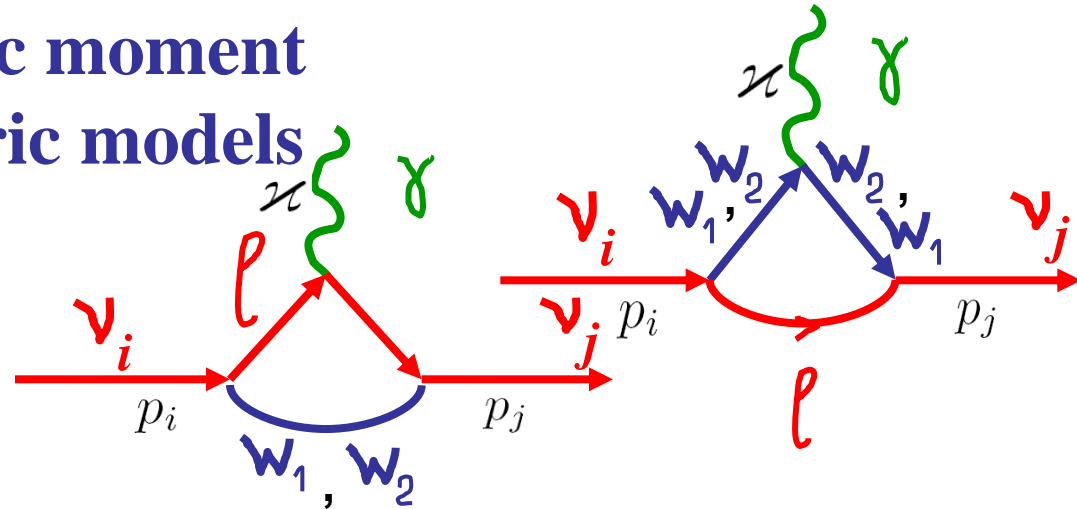
$$SU_L(2) \times SU_R(2) \times U(1)$$

Gauge bosons mass states

$$W_1 = W_L \cos \xi - W_R \sin \xi$$

$$W_2 = W_L \sin \xi + W_R \cos \xi$$

with mixing angle ξ of gauge bosons $W_{L,R}$ with pure $(V \pm A)$ couplings



Kim, 1976; Marciano, Sanda, 1977; Beg, Marciano, Ruderman, 1978

$$\mu_{\nu l} = \frac{eG_F}{2\sqrt{2}\pi^2} \left[m_l \left(1 - \frac{m_{W_1}^2}{m_{W_2}^2} \right) \sin 2\xi + \frac{3}{4} m_{\nu l} \left(1 + \frac{m_{W_1}^2}{m_{W_2}^2} \right) \right]$$

... charged lepton mass ...

... neutrino mass ...

...the present status...

to have visible $\mu \neq 0$

is not an easy task for

theoreticians

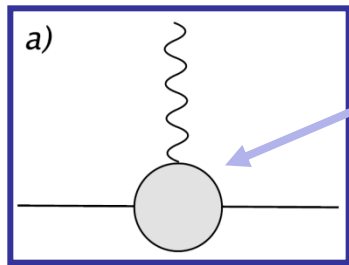
and experimentalists

3.3 Naïve relationship between the size of m_ν and μ_ν

... problem to get large μ_ν and still acceptable m_ν

If μ_ν is generated by physics beyond the SM at energy scale Λ ,

P.Vogel e.a., 2006

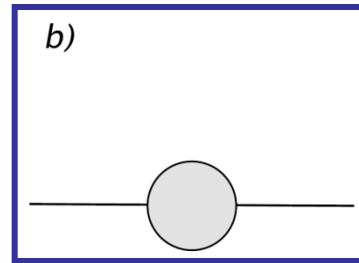


then

$$\mu_\nu \sim \frac{eG}{\Lambda}$$

...combination of constants and loop factors...

contribution to m_ν given by



, then

$$m_\nu \sim G\Lambda$$

$$m_\nu \sim \frac{\Lambda^2}{2m_e} \frac{\mu_\nu}{\mu_B} \sim \frac{\mu_\nu}{10^{-18} \mu_B} [\Lambda(\text{TeV})]^2 \text{ eV}$$

*Voloshin, 1988;
Barr, Freire,
Zee, 1990*

Large magnetic moment

$$\mu_\nu = \bar{\mu}_\nu (m_\nu, m_{e^+}, m_{e^-})$$

- In the L-R symmetric models
($SU(2)_L \times SU(2)_R \times U(1)$)

Kim, 1976
Beg, Marciano,
Ruderman, 1978

- Voloshin, 1988

“On compatibility of small m_ν with large μ_ν of neutrino”,
Sov.J.Nucl.Phys. 48 (1988) 512

... there may be $SU(2)_\nu$ symmetry that forbids m_ν but not μ_ν

- Bar, Freire, Zee, 1990

- supersymmetry
- extra dimensions
- model-independent constraint

considerable enhancement of μ_ν
to experimentally relevant ratios

Bell, Cirigliano,
Ramsey-Musolf,
Vogel,
Wise,
2005

$$\mu_\nu^D \leq 10^{-15} \mu_B$$

$$\mu_\nu^M \leq 10^{-14} \mu_B$$

for BSM ($\Lambda \sim 1 \text{ TeV}$) without fine tuning and
under the assumption that

$$\delta m_\nu \leq 1 \text{ eV}$$

... A remark on electric charge of ν ...

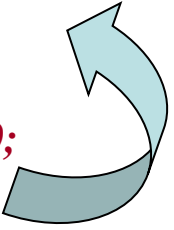
Beyond
Standard
Model...

ν neutrality $Q=0$
is attributed to

gauge invariance
+
anomaly cancellation constraints

imposed in SM of
electroweak
interactions

Foot, Joshi, Lew, Volkas, 1990;
Foot, Lew, Volkas, 1993;
Babu, Mohapatra, 1989, 1990



...General proof:

$$SU(2)_L \times U(1)_Y$$

$$Q = I_3 + \frac{Y}{2}$$

In SM :

In SM (without ν_R) triangle anomalies
cancellation constraints \rightarrow certain relations among particle hypercharges Y ,
that is enough to fix all Y so that they, and consequently Q , are quantized



$$Q=0$$

$Q=0$ is proven also by direct calculation in SM
within different gauges and methods

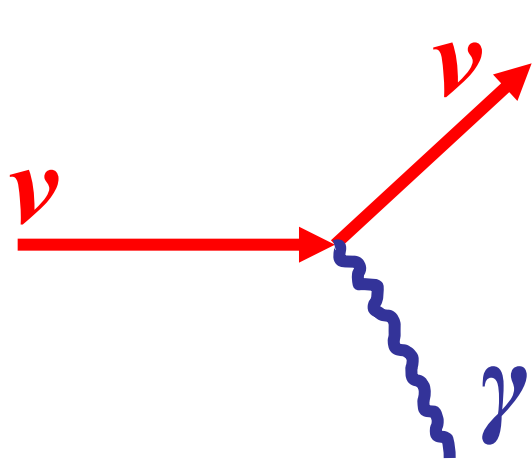
... However, strict requirements for
 Q quantization may disappear in extensions
of standard $SU(2)_L \times U(1)_Y$ EW model if
 ν_R with $Y \neq 0$ are included : in the absence
of Y quantization electric charges Q gets dequantized

Bardeen, Gastmans, Lautrup, 1972;
Cabral-Rosetti, Bernabeu, Vidal, Zepeda, 2000;
Beg, Marciano, Ruderman, 1978;
Marciano, Sirlin, 1980; Sakakibara, 1981;
M.Dvornikov, A.S., 2004 (for extended SM in
one-loop calculations)

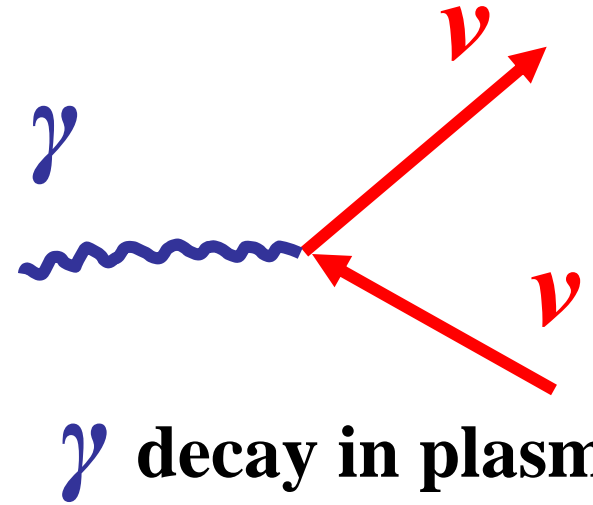


millicharged ν

ν electromagnetic interactions

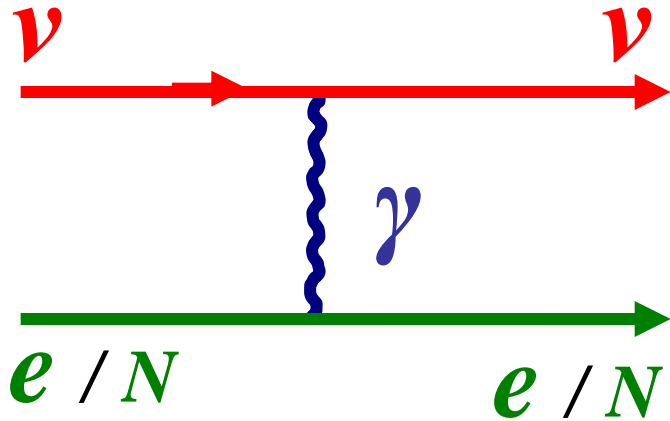


ν decay, Cherenkov radiation

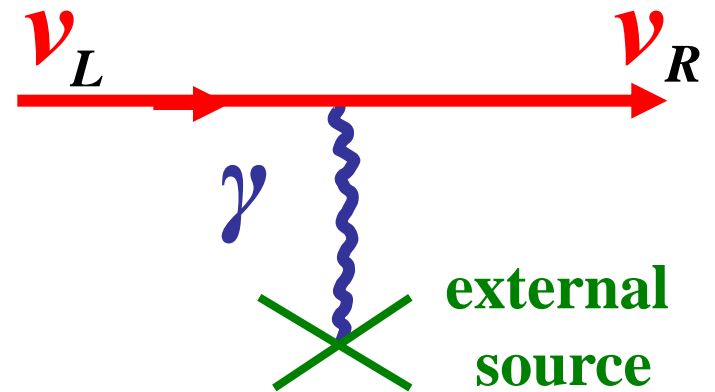


γ decay in plasma

!!!



Scattering



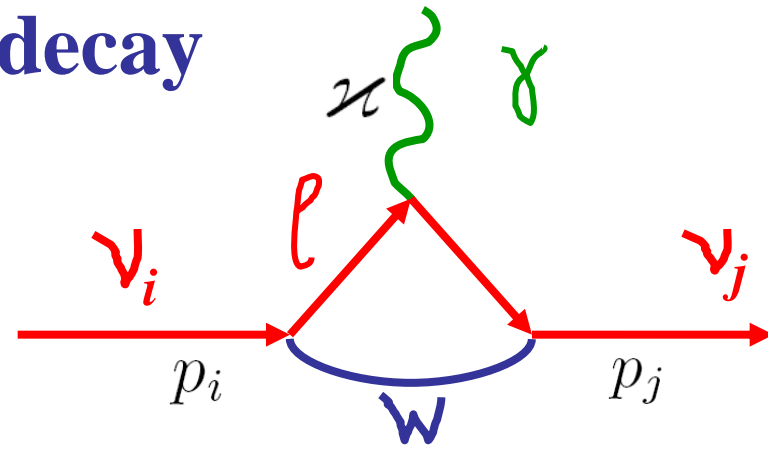
Spin precession

3.7 Neutrino radiative decay

$$\nu_i \longrightarrow \nu_j + \gamma$$

$$m_i > m_j$$

$$L_{int} = \frac{1}{2} \bar{\psi}_i \sigma_{\alpha\beta} (\sigma_{ij} + \epsilon_{ij} \gamma_5) \psi_j F^{\alpha\beta} + h.c.$$



Radiative decay rate

*Petkov 1977; Zatsepin, Smirnov 1978;
Bilenky, Petkov 1987; Pal, Wolfenstein 1982*

$$\Gamma_{\nu_i \rightarrow \nu_j + \gamma} = \frac{\mu_{eff}^2}{8\pi} \left(\frac{m_i^2 - m_j^2}{m_i^2} \right)^3 \approx 5 \left(\frac{\mu_{eff}}{\mu_B} \right)^2 \left(\frac{m_i^2 - m_j^2}{m_i^2} \right)^3 \left(\frac{m_i}{1 \text{ eV}} \right)^3 s^{-1}$$

$$\mu_{eff}^2 = |\mu_{ij}|^2 + |\epsilon_{ij}|^2$$

● Radiative decay has been constrained from absence of decay photons:

- 1) reactor $\bar{\nu}_e$ and solar ν_e fluxes,
- 2) SN 1987A ν burst (all flavours),
- 3) spectral distortion of CMBR

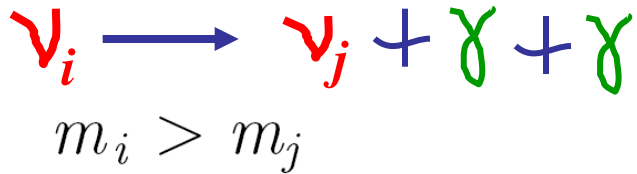
Raffelt 1999

Kolb, Turner 1990;

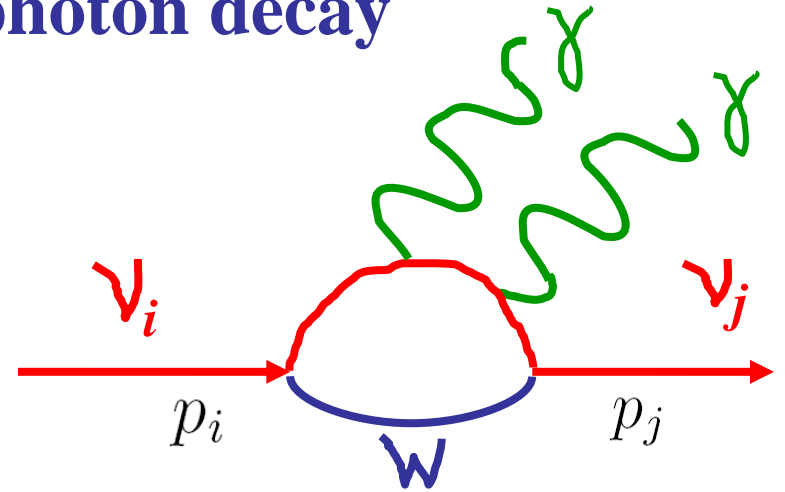
Ressell, Turner 1990

3.8

Neutrino radiative two-photon decay

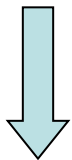


fine structure constant



$$\Gamma_{\nu_i \rightarrow \nu_j + \gamma + \gamma} \sim \frac{\alpha_{QED}}{4\pi} \Gamma_{\nu_i \rightarrow \nu_j + \gamma}$$

... there is no GIM cancellation...



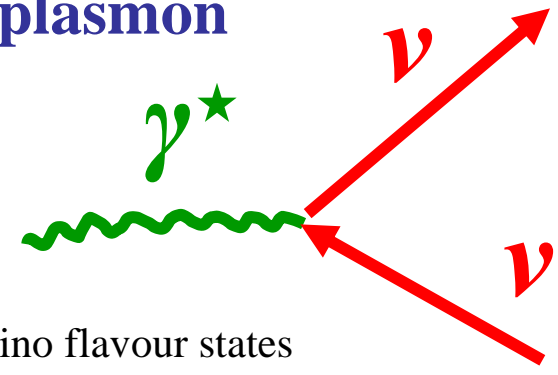
... can be of interest for certain range of ν masses...

$$f(r_l) \approx \frac{3}{2} \left(\cancel{1} - \frac{1}{2} \left(\frac{m_l}{m_W} \right)^2 \right) \rightarrow (m_i/m_l)^2$$

Nieves, 1983; Ghosh, 1984

3.9 The tightest astrophysical bound on μ_{ν}

comes from cooling of **red giant** stars by plasmon decay $\gamma^* \rightarrow \nu \bar{\nu}$



$$L_{int} = \frac{1}{2} \sum_{a,b} \left(\mu_{a,b} \bar{\psi}_a \sigma_{\mu\nu} \psi_b + \epsilon_{a,b} \bar{\psi}_a \sigma_{\mu\nu} \gamma_5 \psi_b \right)$$

neutrino flavour states

Matrix element

$$\epsilon_{\alpha} k^{\alpha} = 0$$

$$|M|^2 = M_{\alpha\beta} p^{\alpha} p^{\beta}, \quad M_{\alpha\beta} = 4\mu^2 (2k_{\alpha} k_{\beta} - 2k^2 \epsilon_{\alpha}^* \epsilon_{\beta} - k^2 g_{\alpha,\beta}),$$

Decay rate

$$\Gamma_{\gamma \rightarrow \nu \bar{\nu}} = \frac{\mu^2 (\omega^2 - k^2)^2}{24\pi \omega}$$

= 0 in vacuum $\omega = k$

In the classical limit γ^* - like a massive particle with $\omega^2 - k^2 = \omega_{pl}^2$

Energy-loss rate per unit volume

$$Q_{\mu} = g \int \frac{d^3k}{(2\pi)^3} \omega f_{BE} \Gamma_{\gamma \rightarrow \nu \bar{\nu}}$$

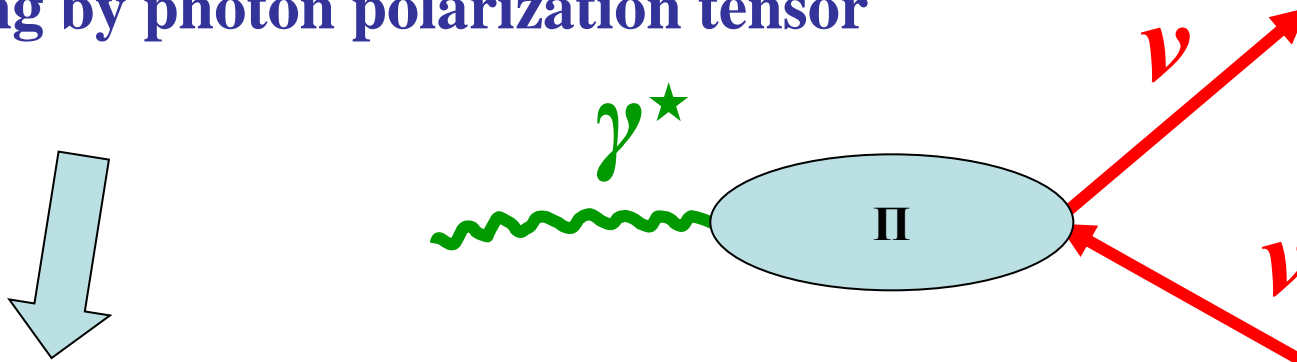
distribution function of plasmons

$$\mu^2 \rightarrow \sum_{a,b} \left(|\mu_{a,b}|^2 + |\epsilon_{a,b}|^2 \right)$$

$$Q_\mu = g \int \frac{d^3k}{(2\pi)^3} \omega f_{BE} \Gamma_{\gamma \rightarrow \nu \bar{\nu}}$$

Energy-loss rate
per unit volume

Magnetic moment **plasmon** decay
enhances the Standard Model photo-neutrino
cooling by photon polarization tensor



more fast cooling of the star.

In order not to delay helium ignition ($\leq 5\%$ in Q)

... best
astrophysical
limit on

✓ magnetic moment...

$$\mu \leq 3 \times 10^{-12} \mu_B$$

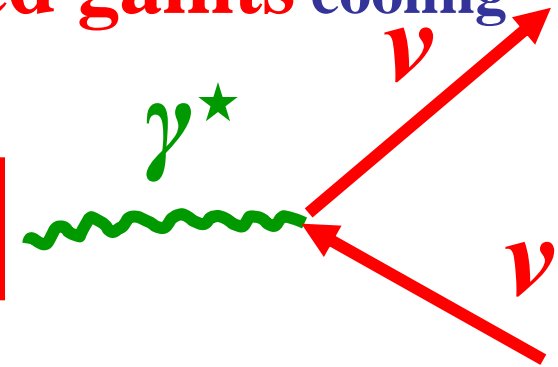
**G.Raffelt,
PRL 1990**

$$\mu^2 \rightarrow \sum_{a,b} \left(|\mu_{a,b}|^2 + |\epsilon_{a,b}|^2 \right)$$

3.10

Dobroliubov, Ignatiev (1990); Babu, Volkas (1992); Mohapatra, Nussinov (1992) ...

● Constraints on neutrino millicharge from red gaints cooling



Interaction Lagrangian

$$L_{int} = -iq_\nu \bar{\psi}_\nu \gamma^\mu \psi_\nu A^\mu$$

millicharge

Decay rate

$$\Gamma_{q_\nu} = \frac{q_\nu^2}{12\pi} \omega_{pl} \left(\frac{\omega_{pl}}{\omega} \right)$$

- $q_\nu \leq 2 \times 10^{-14} e$...to avoid helium ignition in low-mass **red gaints**

Halt, Raffelt, Weiss, PRL 1994

- $q_\nu \leq 3 \times 10^{-17} e$... absence of anomalous energy-dependent dispersion of SN1987A **✓** signal, most model independent

- ... from “charge neutrality” of neutron...

$$q_\nu \leq 3 \times 10^{-21} e$$

Bounds on ν millicharge q_ν from μ_ν

(GEMMA Coll. Data)

A.S.,
arXiv: 1302.1168,
May 13, 2013

ν - e cross-section

$$\left(\frac{d\sigma}{dT}\right)_{\nu-e} = \left(\frac{d\sigma}{dT}\right)_{SM} + \left(\frac{d\sigma}{dT}\right)_{\mu_\nu} + \left(\frac{d\sigma}{dT}\right)_{q_\nu}$$

two not seen contributions:

$$\left(\frac{d\sigma}{dT}\right)_{\mu_\nu^a} \approx \pi\alpha^2 \frac{1}{m_e^2 T} \left(\frac{\mu_\nu^a}{\mu_B}\right)^2$$

$$\left(\frac{d\sigma}{dT}\right)_{q_\nu} \approx 2\pi\alpha \frac{1}{m_e T^2} q_\nu^2$$

Bounds on q_ν from

$$R = \frac{\left(\frac{d\sigma}{dT}\right)_{q_\nu}}{\left(\frac{d\sigma}{dT}\right)_{\mu_\nu^a}} = \frac{2m_e}{T} \frac{\left(\frac{q_\nu}{e_0}\right)^2}{\left(\frac{\mu_\nu^a}{\mu_B}\right)^2} \ll 1$$

... no
observable
effects of
New
Physics

Constraints on μ_ν from GEMMA :

Constraints on q_ν

now $\mu_\nu^a < 2.9 \times 10^{-11} \mu_B$ ($T \sim 2.8$ keV)

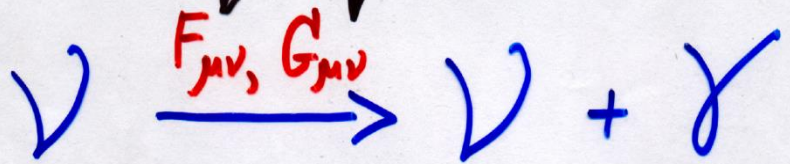
$$|q_\nu| < 1.5 \times 10^{-12} e_0$$

2015 (expected) $\mu_\nu^a \sim 1.5 \times 10^{-11} \mu_B$ ($T = 1.5$ keV) $|q_\nu| < 3.7 \times 10^{-13} e_0$

2017 (expected) $\mu_\nu^a \sim 0.9 \times 10^{-12} \mu_B$ ($T = 400$ eV) $|q_\nu| < 2 \times 10^{-13} e_0$

• New mechanism of electromagnetic radiation

"Spin light of neutrino"
in matter and
electromagnetic fields



A.Lobanov, A.Studenikin,
Phys.Lett. B 564 (2003) 27
Phys.Lett. B 601 (2004) 171

Studenikin, A.Ternov,
Phys.Lett. B 608 (2005) 107

A.Grigoriev, A.S., Ternov,
Phys.Lett. B 622 (2005) 199

Studenikin,

J.Phys.A: Math.Gen. 39 (2006) 6769,
J.Phys.A: Math.Theor. 41 (2008) 16402,

A.Grigoriev, A.Lokhov,
A.Studenikin, A.Ternov,
Nuovo Cim. 35 C (2012) 57,
Phys.lett.B 718 (2012) 512

✓ spin evolution in presence of general external fields

M.Dvornikov, A.Studenikin,
JHEP 09 (2002) 016

General types non-derivative interaction with external fields

$$-\mathcal{L} = g_s s(x) \bar{\nu} \nu + g_p \pi(x) \bar{\nu} \gamma^5 \nu + g_v V^\mu(x) \bar{\nu} \gamma_\mu \nu + g_a A^\mu(x) \bar{\nu} \gamma_\mu \gamma^5 \nu + \frac{g_t}{2} T^{\mu\nu} \bar{\nu} \sigma_{\mu\nu} \nu + \frac{g'_t}{2} \Pi^{\mu\nu} \bar{\nu} \sigma_{\mu\nu} \gamma^5 \nu,$$

scalar, pseudoscalar, vector, axial-vector, tensor and pseudotensor fields:

$$s, \pi, V^\mu = (V^0, \vec{V}), A^\mu = (A^0, \vec{A}), \\ T_{\mu\nu} = (\vec{a}, \vec{b}), \Pi_{\mu\nu} = (\vec{c}, \vec{d})$$

Relativistic (quasiclassical) equation for ✓ spin vector:

$$\dot{\vec{\zeta}}_\nu = 2g_a \left\{ A^0 [\vec{\zeta}_\nu \times \vec{\beta}] - \frac{m_\nu}{E_\nu} [\vec{\zeta}_\nu \times \vec{A}] - \frac{E_\nu}{E_\nu + m_\nu} (\vec{A} \vec{\beta}) [\vec{\zeta}_\nu \times \vec{\beta}] \right\} \\ + 2g_t \left\{ [\vec{\zeta}_\nu \times \vec{b}] - \frac{E_\nu}{E_\nu + m_\nu} (\vec{\beta} \vec{b}) [\vec{\zeta}_\nu \times \vec{\beta}] + [\vec{\zeta}_\nu \times [\vec{a} \times \vec{\beta}]] \right\} + \\ + 2ig'_t \left\{ [\vec{\zeta}_\nu \times \vec{c}] - \frac{E_\nu}{E_\nu + m_\nu} (\vec{\beta} \vec{c}) [\vec{\zeta}_\nu \times \vec{\beta}] - [\vec{\zeta}_\nu \times [\vec{d} \times \vec{\beta}]] \right\}.$$

● Neither s nor π nor V contributes to spin evolution

● Electromagnetic interaction

$$T_{\mu\nu} = F_{\mu\nu} = (\vec{E}, \vec{B})$$

● SM weak interaction

$$G_{\mu\nu} = (-\vec{P}, \vec{M}) \quad \vec{M} = \gamma(A^0 \vec{\beta} - \vec{A}) \\ \vec{P} = -\gamma[\vec{\beta} \times \vec{A}],$$

New mechanism of electromagnetic radiation

?

Why **Spin Light**

of neutrino

$SL\nu$

of electron

SLe

in matter.

Analogies with:

* classical electrodynamics

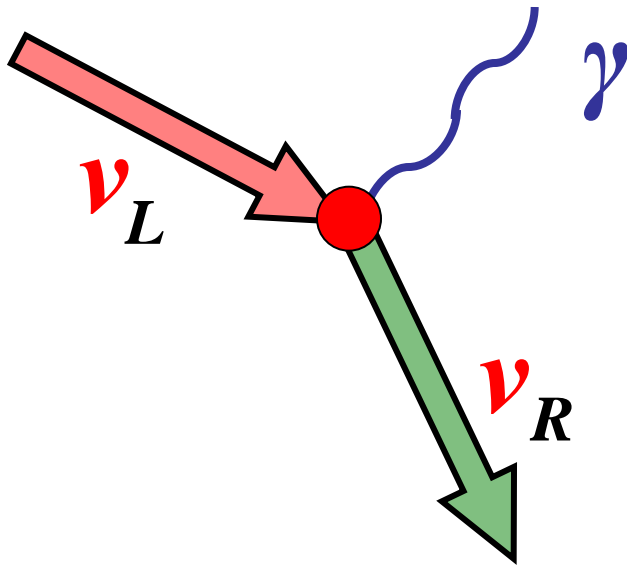
an object with charge $Q=0$ and

magnetic moment $\vec{m} = \frac{1}{2} \sum_i e_i [\vec{r}_i \times \vec{v}_i] \neq 0$

$$\overset{\text{cl. el.}}{I} = \frac{2}{3} \ddot{\vec{m}}^2$$

← magnetic dipole radiation power

Neutrino – photon couplings



*broad neutrino lines
account for interaction
with environment*

“Spin light of neutrino in matter”

SL ν

- ... within the quantum treatment based on method of exact solutions ...

«method of exact solutions»

Interaction of particles in external electromagnetic fields (Furry representation in quantum electrodynamics)

Potential of electromagnetic field

$$A_\mu(x) = A_\mu^q(x) + A_\mu^{ext}(x),$$

quantized part
of potential

evolution operator

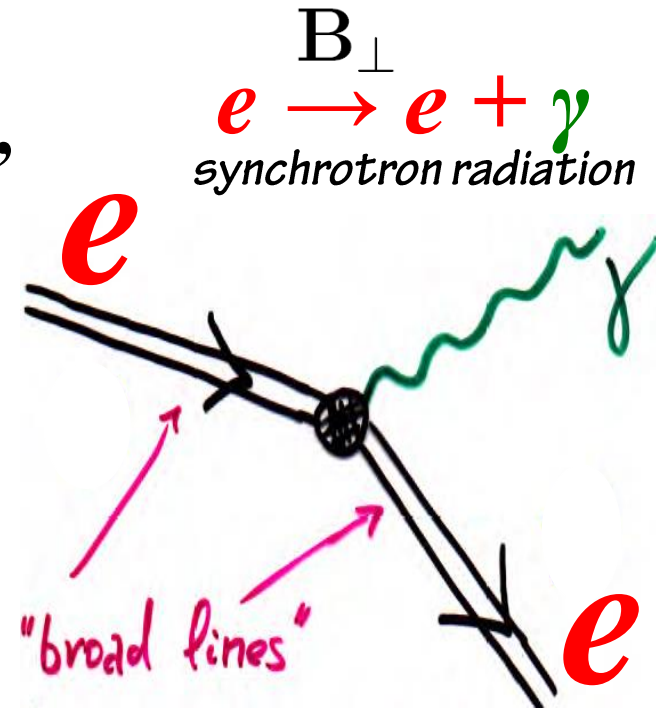
$$U_F(t_1, t_2) = T \exp \left[-i \int_{t_1}^{t_2} j^\mu(x) A_\mu^q(x) dx \right],$$

charged particles current $j_\mu(x) = \frac{e}{2} [\bar{\Psi}_F \gamma_\mu, \Psi_F]$,

Dirac equation in external classical (non-quantized) field $A_\mu^{ext}(x)$

$$\left\{ \gamma^\mu \left(i\partial_\mu - eA_\mu^{ext}(x) \right) - m_e \right\} \Psi_F(x) = 0$$

- ...beyond perturbation series expansion,
strong fields and non linear effects...






and e

in matter treated within
«*method of exact solutions*»
(of quantum wave equations)

A.Studenikin, A.Ternov,
“Neutrino quantum states in
matter”,
Phys.Lett.B 608 (2005) 107;

“Generalized Dirac-Pauli equation
and neutrino quantum states in
matter” hep-ph/0410296,

A.Grigoriev, A.Studenikin,
A.Ternov,
Phys.Lett.B 608 622 (2005)19

●  energy quantization
in rotating matter ...

A.Studenikin, “Method of wave equations
exact solutions in studies of neutrino and
electron interactions in dense matter”,
● J.Phys.A:Math.Theor. 41 (2008) 16402

“Neutrinos and electrons in background
matter: a new approach”,
● Ann. Fond. de Broglie 31 (2006) 289,
● J.Phys.A: Math.Gen.39 (2006) 6769

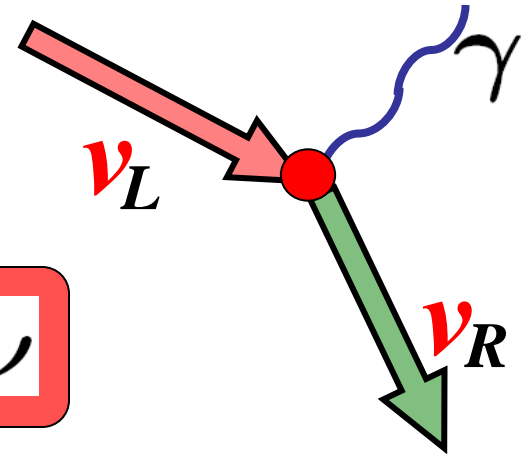
I.Balantsev, Yu.Popov, A.Studenikin,
“On a problem of relativistic particles motion
in a strong magnetic field and dense matter”
● J.Phys.A: Math.Theor.44 (2011)255301

A.Studenikin, I.Tokarev, “Millicharged
neutrino with anomalous magnetic
moment in rotating magnetized matter”,
● arXiv: 1209.3245 v2, May 27, 2013

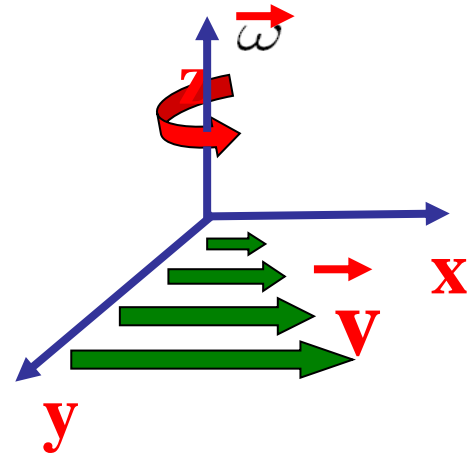
2 problems:

1. Spin Light of ν
in matter

SL ν



2. ν energy quantization
in rotating matter



ν quantum states in matter
New approach to particles in matter

Modified Dirac equation for neutrino in matter

Addition to the vacuum neutrino Lagrangian

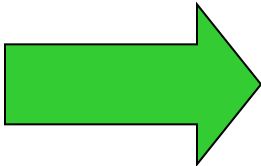
$$\Delta L_{eff} = \Delta L_{eff}^{CC} + \Delta L_{eff}^{NC} = -f^\mu \left(\bar{\nu} \gamma_\mu \frac{1 + \gamma_5}{2} \nu \right)$$

matter
current

where

$$f^\mu = \frac{G_F}{\sqrt{2}} \left((1 + 4 \sin^2 \theta_W) j^\mu - \lambda^\mu \right)$$

matter
polarization



$$\left\{ i \gamma_\mu \partial^\mu - \frac{1}{2} \gamma_\mu (1 + \gamma_5) f^\mu - m \right\} \Psi(x) = 0$$

It is supposed that there is a macroscopic amount of electrons in the scale of a neutrino de Broglie wave length. Therefore, **the interaction of a neutrino with the matter (electrons) is coherent.**

L.Chang, R.Zia, '88; J.Panteleone, '91; K.Kiers, N.Weiss, M.Tytgat, '97-'98; P.Manheim, '88; D.Nötzold, G.Raffelt, '88; J.Nieves, '89; V.Oraevsky, V.Semikoz, Ya.Smorodinsky, '89; W.Naxton, W-M.Zhang '91; M.Kachelriess, '98; A.Kusenko, M.Postma, '02.

**A.Studenikin, A.Ternov, hep-ph/0410297;
Phys.Lett.B 608 (2005) 107**

This is the most general equation of motion of a neutrino in which the effective potential accounts for both the **charged** and **neutral-current** interactions with the background matter and also for the possible effects of the matter **motion** and **polarization.**

Quantum theory of spin light of neutrino (I)

Quantum treatment of *spin light of neutrino* in matter

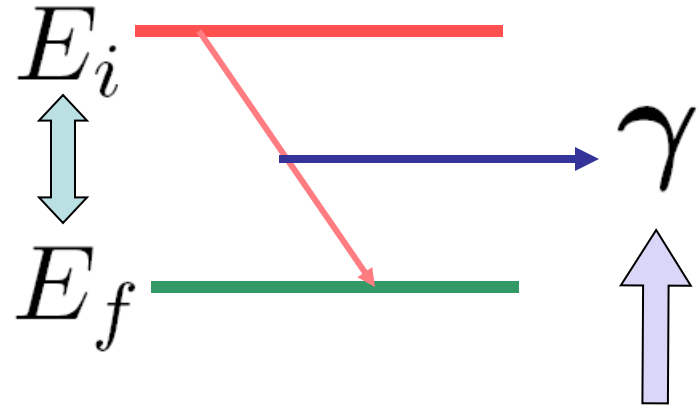
shows that this process originates from the **two subdivided phenomena:**



the **shift** of the neutrino **energy levels** in the presence of the background matter, which is different for the two opposite **neutrino helicity states**,

$$E = \sqrt{\mathbf{p}^2 \left(1 - s\alpha \frac{m}{p}\right)^2 + m^2} + \alpha m$$

$$s = \pm 1$$



the radiation of the photon in the process of the neutrino transition from the **“excited” helicity state** to the **low-lying helicity state** in matter



A.Studenikin, A.Ternov,

Phys.Lett.B 608 (2005) 107;

A.Grigoriev, A.Studenikin, A.Ternov,

Phys.Lett.B 622 (2005) 199;

Grav. & Cosm. 14 (2005) 132;

neutrino-spin self-polarization effect in the matter

A.Lobanov, A.Studenikin, Phys.Lett.B 564 (2003) 27;

Phys.Lett.B 601 (2004) 171

It is possible to have

$$\tau = \frac{1}{\Gamma_{SL\nu}} \ll \text{age of the Universe ?}$$

For ultra-relativistic ✓

with momentum $p \sim 10^{20} eV$

and magnetic moment $\mu \sim 10^{-10} \mu_B$

in very dense matter $n \sim 10^{40} cm^{-3}$

from

$$\Gamma_{SL\nu} = 4\mu^2 \alpha^2 m_\nu^2 p$$

$$p \gg m_{plasmon}$$

also discussed by
A.Kuznetsov,
N.Mikheev, 2007

A.Lobanov, A.S., PLB 2003; PLB 2004

A.Grigoriev, A.S., PLB 2005

A.Grigoriev, A.S., A.Ternov, PLB 2005

$$\alpha m_\nu = \frac{1}{2\sqrt{2}} G_F n (1 + \sin^2 \theta_W)$$

it follows that

$$\tau = \frac{1}{\Gamma_{SL\nu}} = 1.5 \times 10^{-8} s$$

A. Grigoriev, A. Lokhov,
A. Ternov, A. Studenikin

The effect of plasmon mass on spin light of neutrino in dense matter

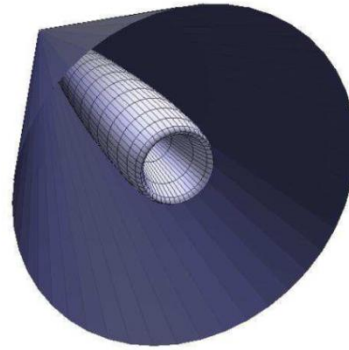


Figure 1: 3D representation of the radiation power distribution.

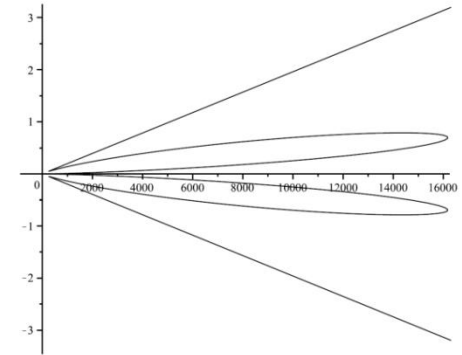


Figure 2: The two-dimensional cut along the symmetry axis. Relative units are used.

Phys. Lett. B 718
(2012) 512-515

4. Conclusions

We developed a detailed evaluation of the spin light of neutrino in matter accounting for effects of the emitted plasmon mass. On the base of the exact solution of the modified Dirac equation for the neutrino wave function in the presence of the background matter the appearance of the threshold for the considered process is confirmed. The obtained exact and explicit threshold condition relation exhibit a rather complicated dependence on the matter density and neutrino mass. The dependence of the rate and power on the neutrino energy, matter density and the angular distribution of the $SL\nu$ is investigated in details. It is shown how the rate and power wash out when the threshold parameter $a = m_\gamma^2/4\tilde{n}p$ approaching unity. From the performed detailed analysis it is shown that the $SL\nu$ mechanism is practically insensitive to the emitted plasmon mass for very high densities of matter (even up to $n = 10^{41} \text{ cm}^{-3}$) for ultra-high energy neutrinos for a wide range of energies starting from $E = 1 \text{ TeV}$. This conclusion is of interest for astrophysical applications of $SL\nu$ radiation mechanism in light of the recently reported hints of $1 \div 10 \text{ PeV}$ neutrinos observed by IceCube [17].

✓ energy quantization
in rotating media:
new mechanism for
✓ trapping inside
compact objects

Grigoriev, Savochkin, Studenikin, *Russ.Phys.J.* 50 (2007) 845

Studenikin, *J.Phys. A: Math.Theor.* 41 (2008) 164047

Balantsev, Popov, Studenikin,

J.Phys. A:Math.Theor. 44 (2011) 255301

Balantsev, Studenikin, Tokarev, *Phys.Part.Nucl.* 43 (2012), 727

Phys.Atom.Nucl. 76 (2013) 489

Studenikin, Tokarev, *arXiv: 1209.3245 v 2*, May 28, 2013

Millicharged magnetic ψ in rotating magnetized matter

Balatsev, Tokarev, Studenikin,

Phys.Part.Nucl., 2012,

Phys.Atom.Nucl., Nucl.Phys. B, 2013,

● *Studenikin, Tokarev, arXiv: 1209.3245, V 2, May 27, 2013*

Modified Dirac equation for ψ wave function

$$\left(\gamma_\mu (p^\mu + q_0 A^\mu) - \frac{1}{2} \gamma_\mu (c_l + \gamma_5) f^\mu - \frac{i}{2} \mu \sigma_{\mu\nu} F^{\mu\nu} - m \right) \Psi(x) = 0$$

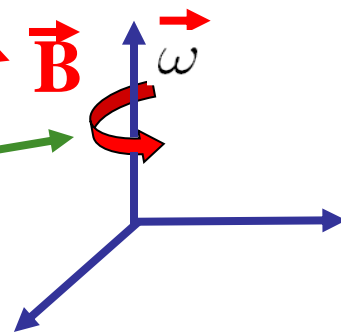
external magnetic field

$$V_m = \frac{1}{2} \gamma_\mu (c_l + \gamma_5) f^\mu$$

matter potential

rotating matter

$$f^\mu = -G n_n (1, -\epsilon y \omega, \epsilon x \omega, 0)$$



✓ wave function (exact solution)

$$\Psi(x) = \Psi_L(x) + \Psi_R(x)$$

$$\psi_1 = \frac{1}{2} \sqrt{\frac{|2Gn_n\omega - \epsilon q_\nu B|}{2\pi L}} \sqrt{1 - \frac{p_3}{p_0^L + Gn_n}} \mathcal{L}_s^{l-1} \left(\frac{|2Gn_n\omega - \epsilon q_\nu B|}{2} r^2 \right) e^{i(l-1)\varphi}$$

$$\psi_2 = \frac{i}{2} \sqrt{\frac{|2Gn_n\omega - \epsilon q_\nu B|}{2\pi L}} \sqrt{1 + \frac{p_3}{p_0^L + Gn_n}} \mathcal{L}_s^l \left(\frac{|2Gn_n\omega - \epsilon q_\nu B|}{2} r^2 \right) e^{il\varphi}.$$

$$\psi_3 = \frac{1}{2} \sqrt{\frac{q_\nu B}{2\pi L}} \sqrt{1 - \frac{p_3}{p_0^R}} \mathcal{L}_s^{l-1} \left(\frac{q_\nu B}{2} r^2 \right) e^{i(l-1)\varphi}$$

$$\psi_4 = \frac{i}{2} \sqrt{\frac{q_\nu B}{2\pi L}} \sqrt{1 + \frac{p_3}{p_0^R}} \mathcal{L}_s^l \left(\frac{q_\nu B}{2} r^2 \right) e^{il\varphi},$$

Laguerre functions
($N = l + s = 0, 1, 2, \dots$)

✓ energy:

$$p_0^R = \sqrt{p_3^2 + 2Nq_\nu B} \quad p_0^L = \sqrt{p_3^2 + 2N|2Gn_n\omega - \epsilon q_\nu B| - Gn_n}$$

$N = 0, 1, 2, \dots$ energy quantization in rotating magnetized matter

✓ energy is **quantized** in
rotating matter

$$G = \frac{G_F}{\sqrt{2}}$$

$$p_0 = \sqrt{p_3^2 + 2N|2Gn_n\omega - \epsilon q_\nu B| + m^2} - Gn_n - q\phi$$

$$N = 0, 1, 2, \dots$$

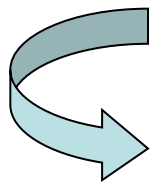
matter rotation
frequency

scalar potential
of **electric field**

Transversal motion of ✓ is **quantized** in **rotating medium**
like **electron motion** is **quantized** in magnetic field
(**Landau energy levels**):

$$p_0^{(e)} = \sqrt{m_e^2 + p_3^2 + 2\gamma N}, \quad \gamma = eB, \quad N = 0, 1, 2, \dots$$

In quasi-classical approach

- 
- ✓ quantum states in rotating matter
 - ✓ motion in circular orbits

$$R = \int_0^\infty \Psi_L^\dagger \mathbf{r} \Psi_L d\mathbf{r} = \sqrt{\frac{2N}{|2Gn_n\omega - \epsilon q_0 B|}}$$

due to *effective Lorentz force*

$$\mathbf{F}_{eff} = q_{eff} \mathbf{E}_{eff} + q_{eff} [\boldsymbol{\beta} \times \mathbf{B}_{eff}]$$

$$q_{eff} \mathbf{E}_{eff} = q_m \mathbf{E}_m + q_0 \mathbf{E} \quad q_{eff} \mathbf{B}_{eff} = |q_m B_m + q_0 B| \mathbf{e}_z$$

where

$$q_m = -G, \quad \mathbf{E}_m = -\nabla n_n, \quad \mathbf{B}_m = 2n_n \boldsymbol{\omega}$$

matter induced “charge”, “electric” and “magnetic” fields

Neutrino *S*tar Turning (ν ST) mechanism

Studenikin, Tokarev,
arXiv:1209.3245

...Due to effective Lorentz force

feedback of neutrinos on rotating star

Escaping ν s move on curved orbits inside rotating star should effect initial rotation of star

... To avoid contradiction between impact ν ST mechanism on pulsar rotation and observational data on pulsars

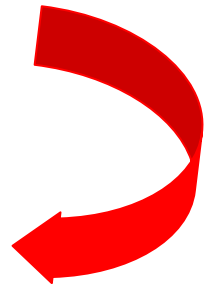
...the shift of rotation frequency (for realistic choice of the star characteristics)

$$\frac{|\Delta\omega_0|}{\omega_0} \simeq 10^{17} \varepsilon \left(\frac{P_0}{10 \text{ s}} \right) \quad \varepsilon = q_\nu / e_0$$

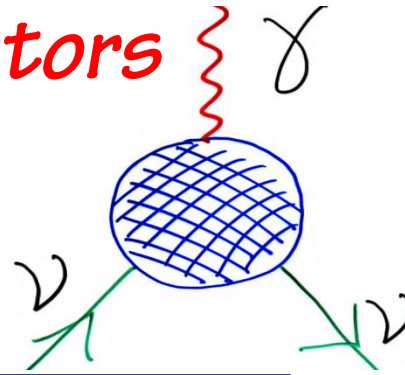
From $|\Delta\omega_0| < \omega_0$ (for slowly rotating stars $P_0 \sim 10 \text{ s}$)

new astrophysical limit

$$q_\nu < 10^{-17} e_0$$



Conclusions

✓ **e.m. vertex function** \Rightarrow **4 form factors** 

charge **dipole** **magnetic** and **electric**

● $\Lambda_\mu(q) = f_Q(q^2)\gamma_\mu + f_M(q^2)i\sigma_{\mu\nu}q^\nu + f_E(q^2)\sigma_{\mu\nu}q^\nu\gamma_5$
 $f_A(q^2)(q^2\gamma_\mu - q_\mu\not{q})\gamma_5$ **anapole**

● **EM properties** \Rightarrow **a way to distinguish Dirac and Majorana** ✓

● **Standard Model with ν_R ($m_\nu \neq 0$):** $\mu_e = \frac{3eG_F}{8\sqrt{2}\pi^2} m_{\nu_e} \sim 3 \cdot 10^{-19} \mu_B \left(\frac{m_{\nu_e}}{1\text{eV}}\right)$

● **In extensions of SM**

enhancement of **magnetic moment** ✓, even **electrically millicharged** ✓

● **Limits from reactor ν -e scattering experiments (2012):**

$\mu_\nu < 2.9 \times 10^{-11} \mu_B$

A.Beda et al. (GEMMA Coll.)

● **Limits from astrophysics, star cooling (1990):**

$\mu_\nu < 3 \times 10^{-12} \mu_B$

G.Raffelt

$|q_\nu| < 1.5 \times 10^{-12} e_0$

$q_\nu < 10^{-17} e_0$

✓ **ST mechanism**

16th Lomonosov
Conference on
Elementary Particle
Physics, www.icas.ru
Moscow State University,
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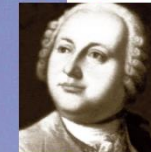
Бруно Понтекорво

1913-1993

centennial anniversary



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