

**Entangled glue or collective flow:
a QCD puzzle at the LHC & RHIC**

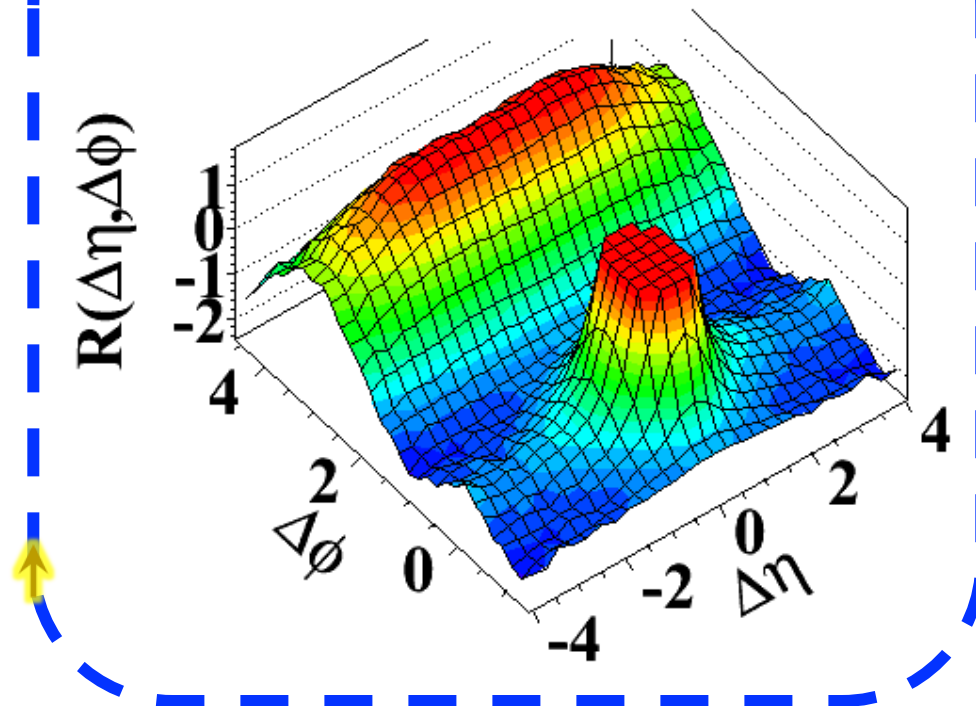
**Raju Venugopalan
Brookhaven National Laboratory**

MIT p+A workshop, May 17-18, 2013

Near side ridge in high multiplicity p+p collisions

“Discovery”

CMS: JHEP 1009, 091 (2010)
(d) $N > 110$, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$





Particles That Flock: Strange Synchronization Behavior at the Large Hadron Collider

Scientific American, February (2011)

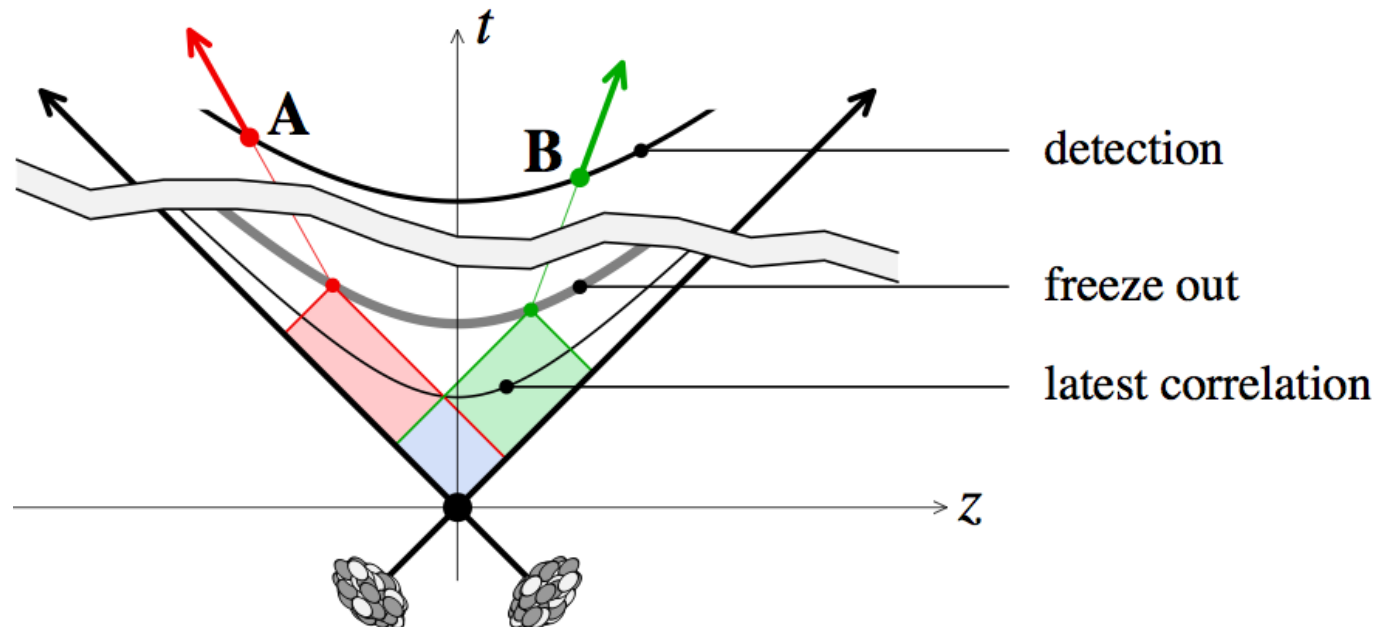
Scientists at the Large Hadron Collider are trying to solve a puzzle of their own making: why particles sometimes fly in sync

The high-energy collisions of protons in the LHC may be uncovering “a new deep internal structure of the initial protons,” says Frank Wilczek of the Massachusetts Institute of Technology, winner of a Nobel Prize

“At these higher energies [of the LHC], one is taking a snapshot of the proton with higher spatial and time resolution than ever before”



Long range rapidity correlations as a chronometer



$$\tau \leq \tau_{\text{frz-out}} \exp \left(-\frac{1}{2} \underbrace{|y_A - y_B|}_{\text{rapidity difference}} \right)$$

- ❖ Long range correlations sensitive to very early time (fractions of a femtometer $\sim 10^{-24}$ seconds) dynamics in collisions



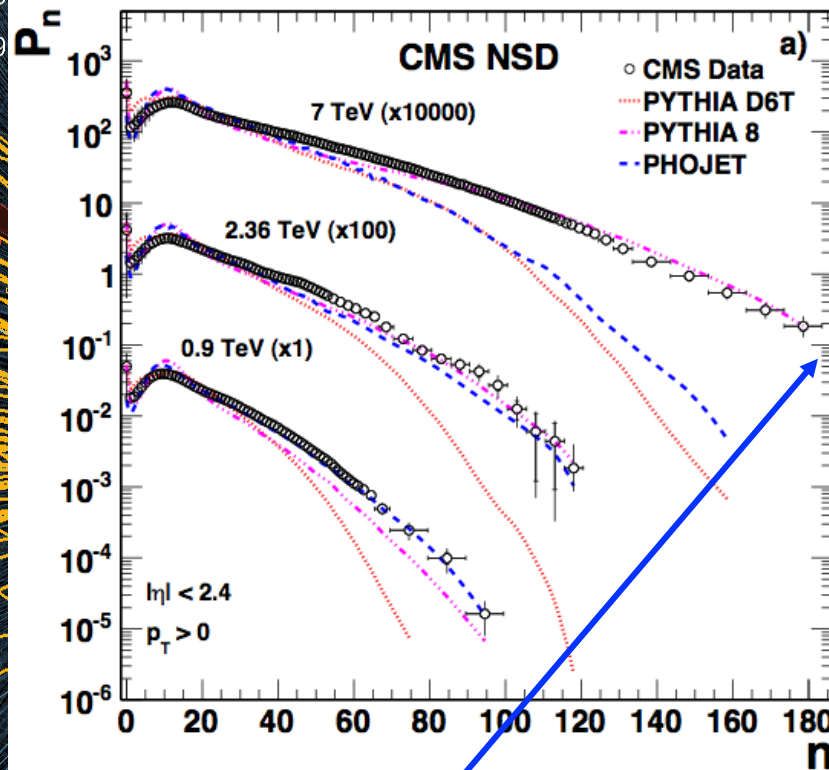
High Multiplicity pp collisions



CMS Experiment High Multiplicity events are rare in nature

Data recorded: 2010-Jul-0

Run / Event: 139779 / 499

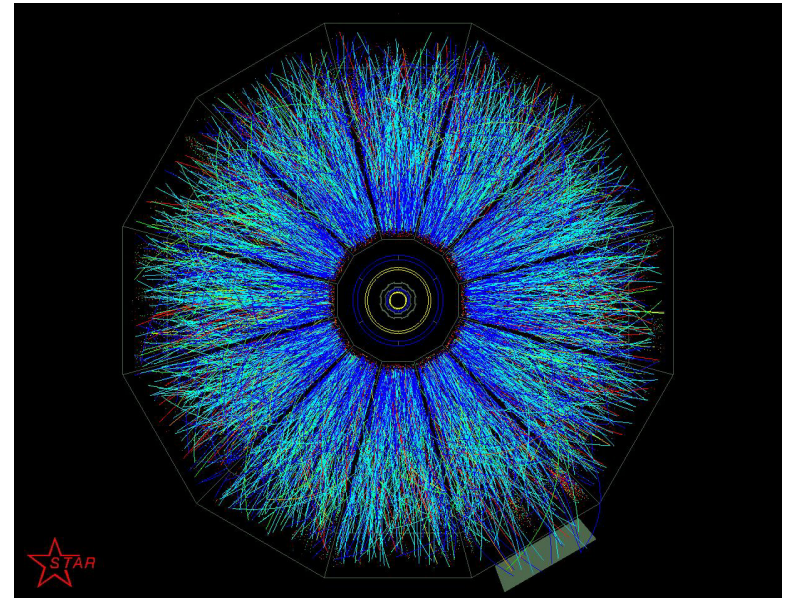


Very high particle density regime
Is there anything peculiar happening there?

(c) Copyright CERN, 2010. For the benefit of the CMS Collaboration.

<http://quana.cern.ch/SPX>

How can we **compute** bulk
multiparticle production
ab initio in QCD ?



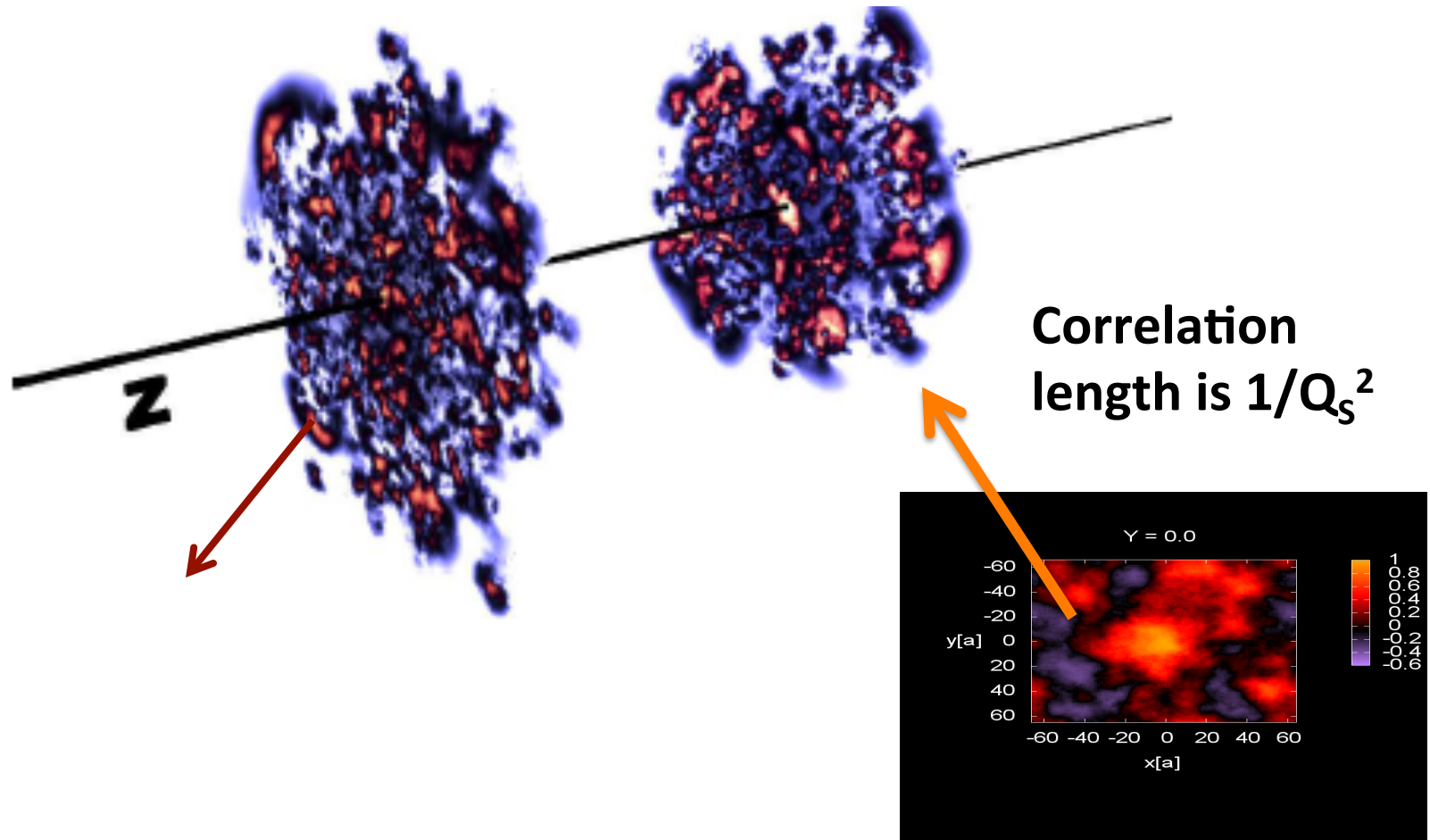
Interesting question:

~~*perturbative VS non-perturbative,*~~

strong coupling VS weak coupling

Always non-perturbative – QFT in strong time dependent fields

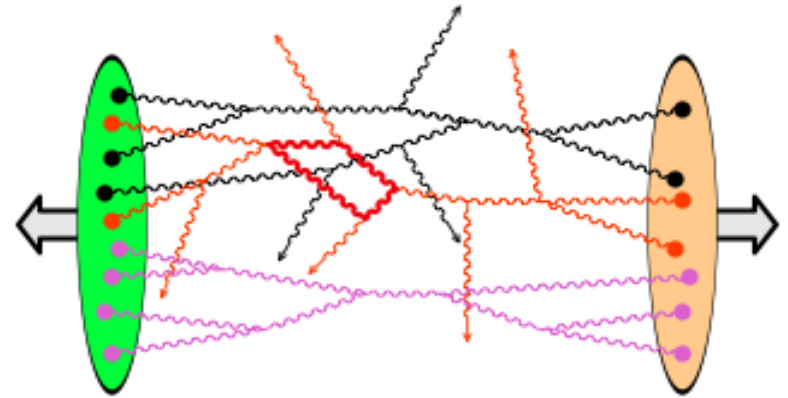
Multiparticle production: high multiplicity events



Weak coupling EFT approach: **Color Glass Condensate**

Highly occupied gluon states of maximal occupancy allowed in **QCD**

Non-perturbative weak coupling QCD
in strong time dependent fields



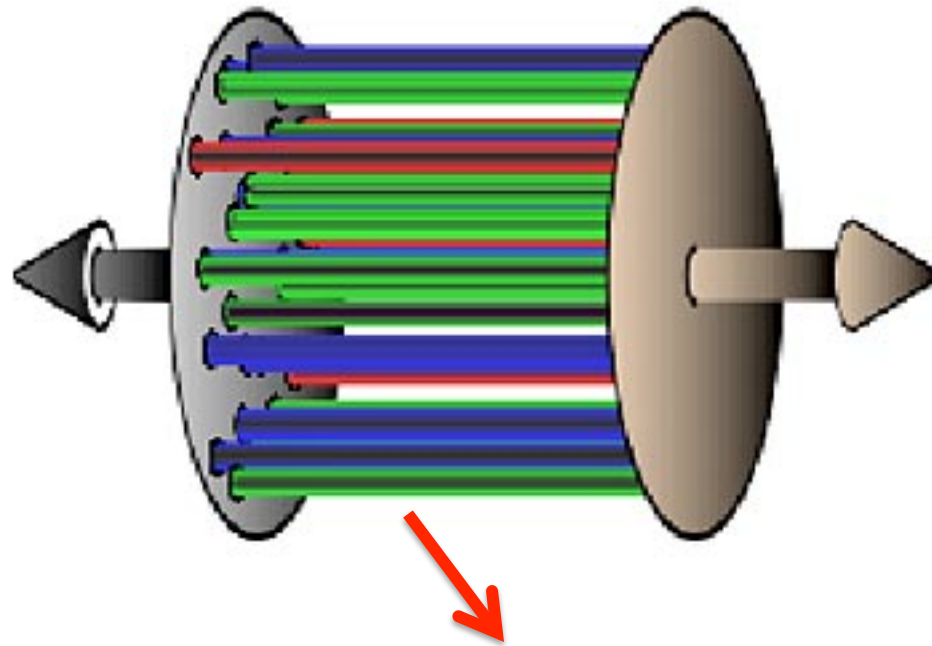
Interesting question:

~~-CGC versus hydro~~

-Initial state dynamics versus final state dynamics

The Glasma: shattering CGCs

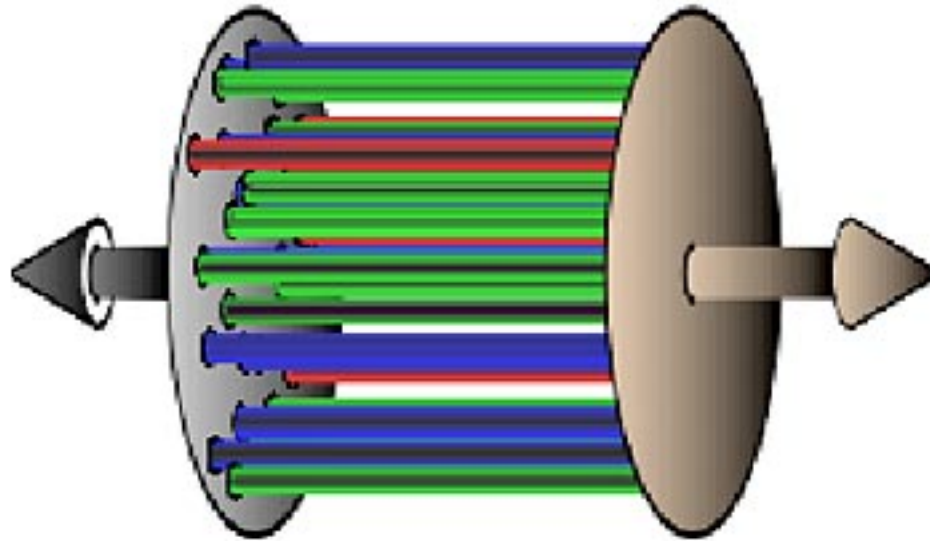
High occupancy=dominance of classical fields



Classical QCD Yang-Mills eqns. demonstrate that each of these color “flux tubes” stretching out in rapidity is of transverse size $1/Q_s \ll 1$ fm

The Glasma: shattering CGCs

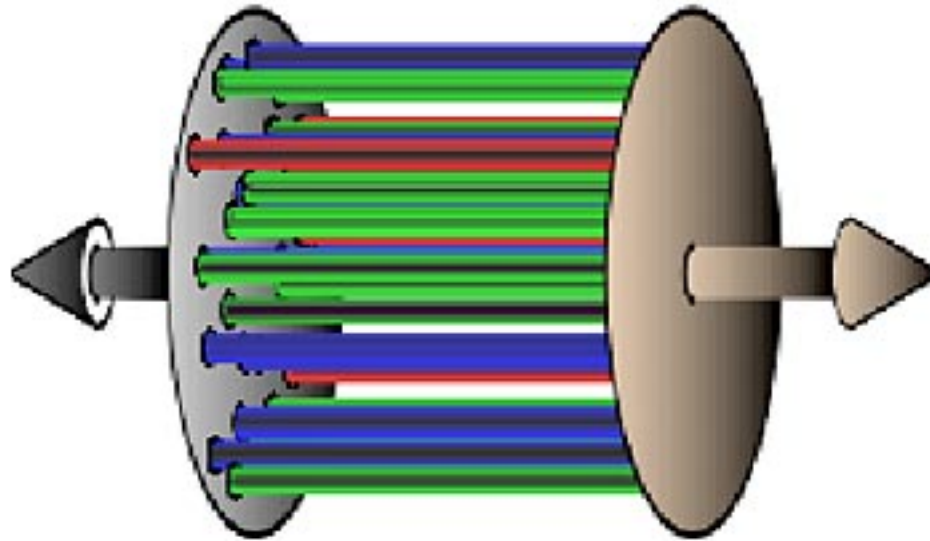
High occupancy=dominance of classical fields



Decay of fields on $t \sim 1/Q_s$ leads to multiparticle dynamics
-- controlled by sub-nucleon QCD scales

The Glasma: shattering CGCs

High occupancy=dominance of classical fields



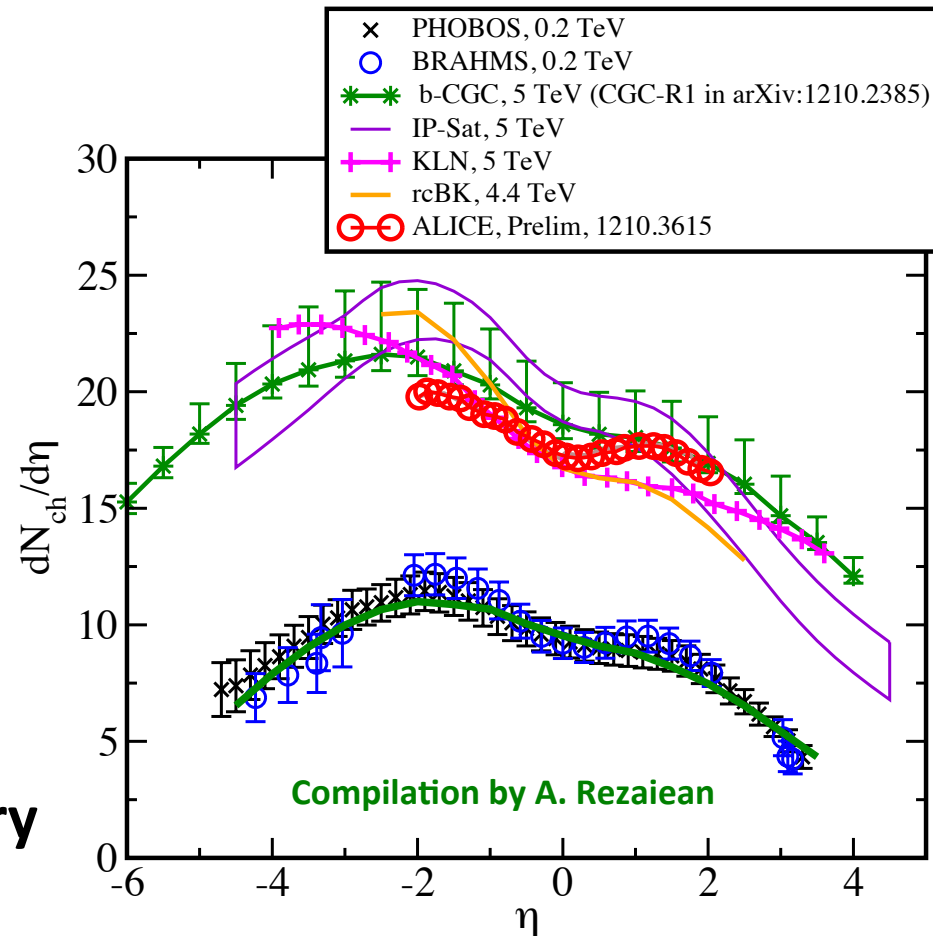
There are $\sim \pi R^2 Q_s^2$ flux tubes – $dn/d\eta \approx \pi R^2 Q_s^2 / \alpha_s$

How do these models do with p+A at the LHC ?

In saturation models

$$\frac{dN}{d\eta} \propto \frac{Q_S^2 S_{\perp}}{\alpha_S(Q_S)}$$

Multiplicities have some sensitivity to “infrared” non-pert. physics/geometry



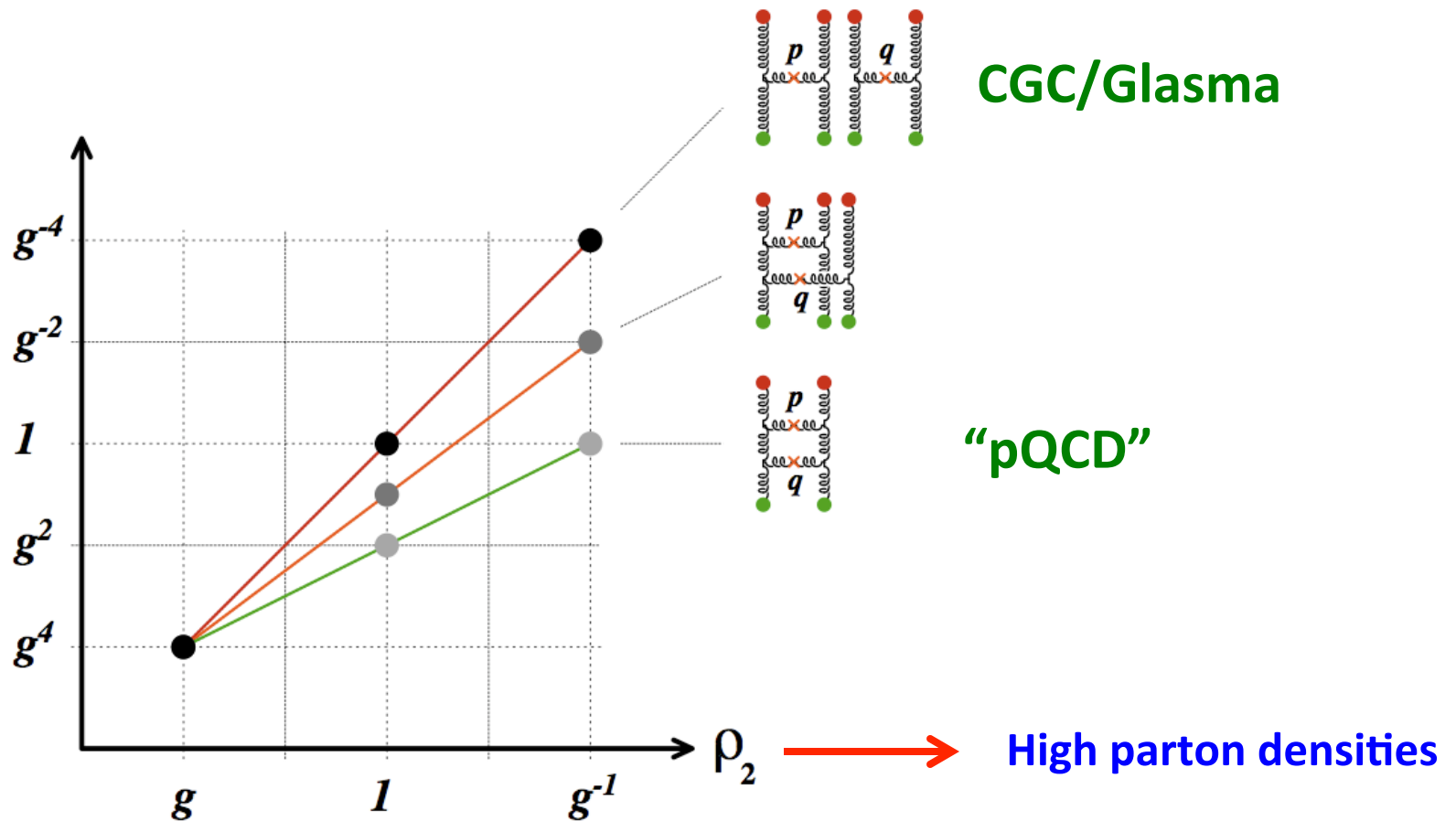
Also describes centrality dependence of multiplicities in A+A

Multi-part. production: systematic power counting

Counting powers of “effective” color charge density $\rho = g n_{\text{occ}}$

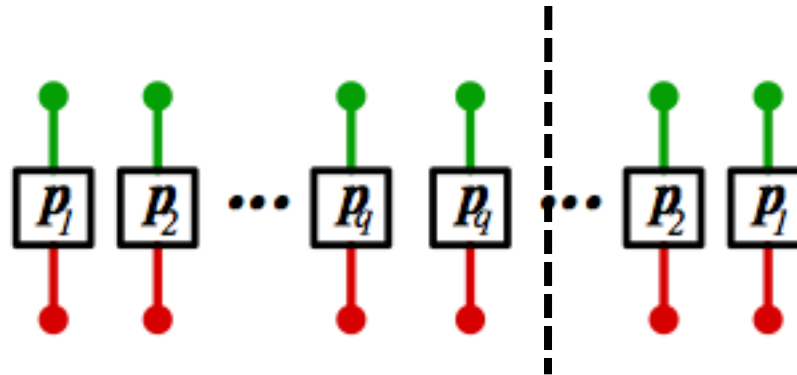
$$k_T \leq Q_S, n_{\text{occ}} = 1/g^2 \Rightarrow \rho \approx 1/g$$

$$k_T \gg Q_S, n_{\text{occ}} = 1 \Rightarrow \rho \approx 1$$

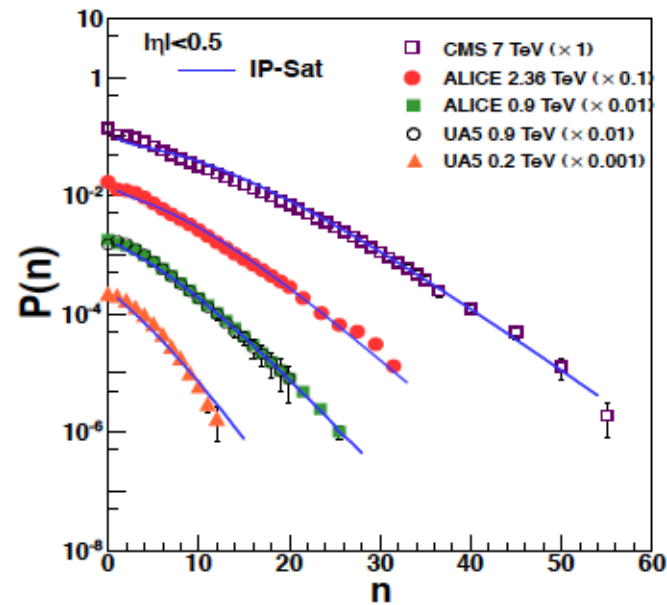


N-particle correlations

Dusling, Fernandez-Fraile, RV
Gelis, Lappi, McLerran



Leading combinatorics gives a negative binomial distribution

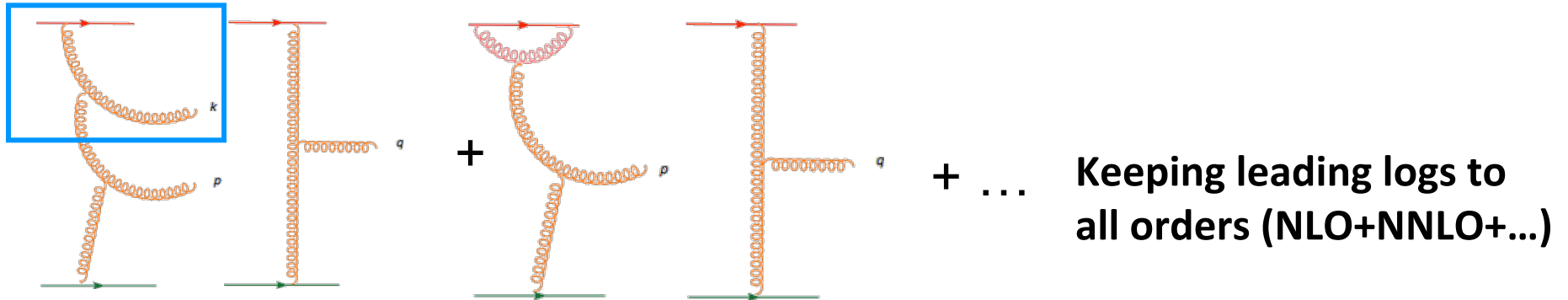


Tribedy, RV
1112.2445

The saturated hadron: Glasma graphs - I

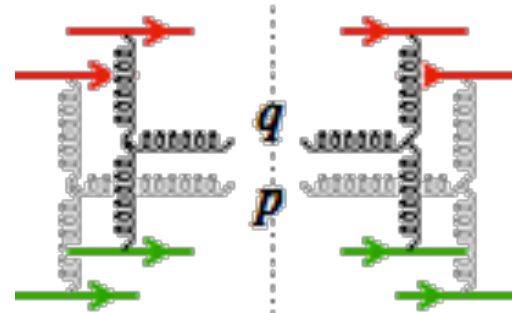
RG evolution:

Dumitru, Gelis, McLerran, RV: 0804.3858
Gelis, Lappi, RV, arXiv: 0807.1306



= LO graph with evolved sources

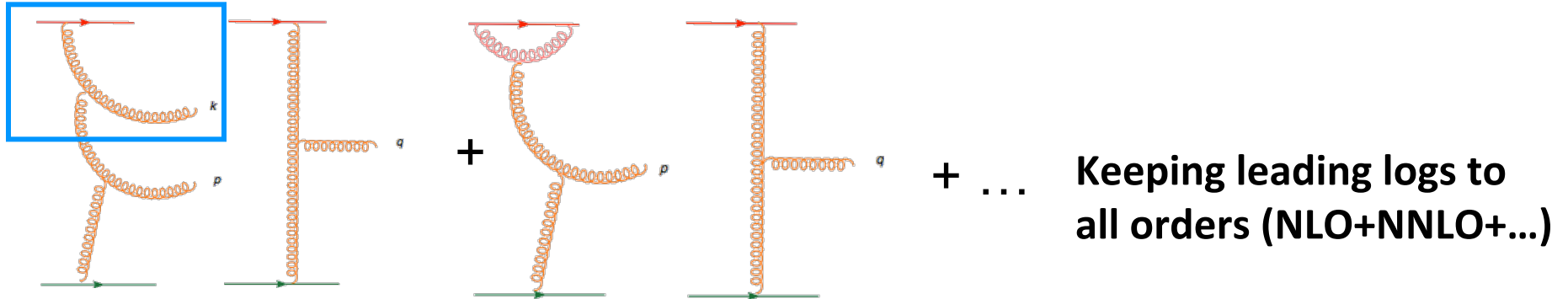
avg. over sources in each event
and over all events gives correlation



The saturated hadron: Glasma graphs - I

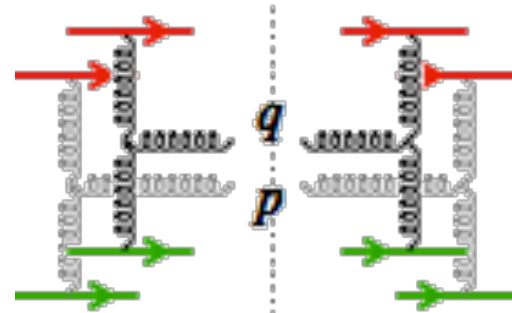
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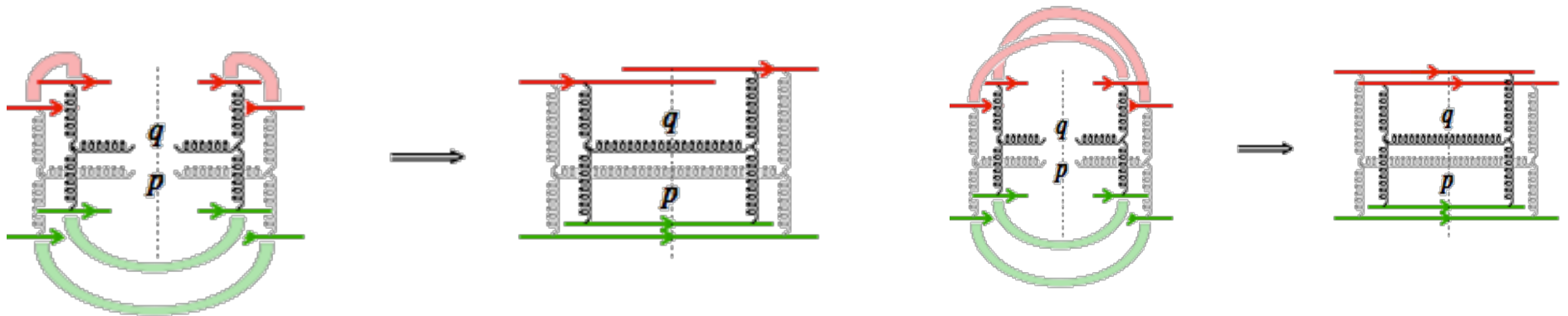


$$\left\langle \frac{dN_2}{d^3p d^3q} \right\rangle_{\text{LLogs}} = \int [d\rho_1][d\rho_2] W_{Y_1}[\rho_1] W_{Y_2}[\rho_2] \frac{dN}{d^3p} \Big|_{\text{LO}} \frac{dN}{d^3q} \Big|_{\text{LO}}$$

From solns. of **Yang-Mills** eqns. with two light cone sources
 Includes all mult. scat. contributions $(g\rho_1)^n$ and $(g\rho_2)^n$

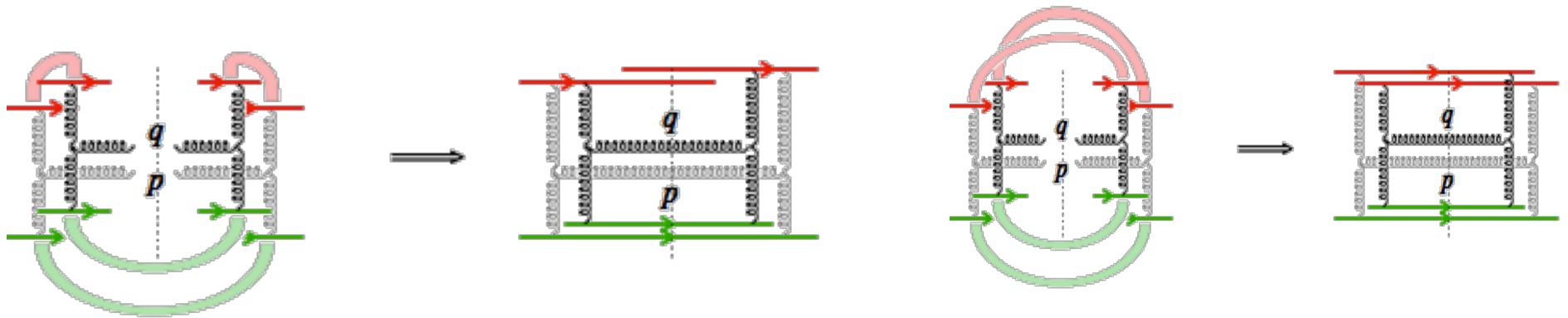
The saturated hadron: Glasma graphs-II

Correlations are induced by color fluctuations that vary event to event – for Gaussian weight functionals in ρ , have **color screening radius** $\sim 1/Q_s$



The saturated hadron: Glasma graphs-II

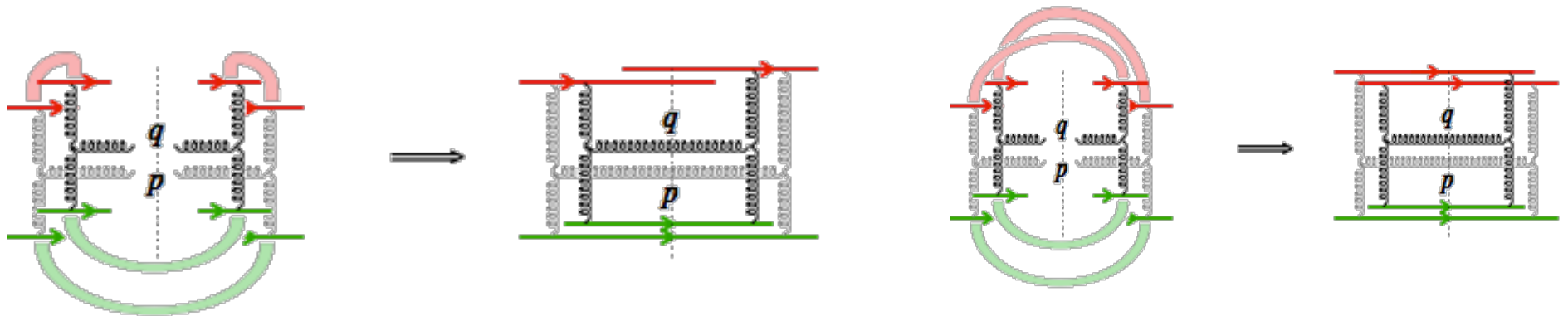
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Glasma graphs generate long range rapidity correlations...

The saturated hadron: Glasma graphs-II

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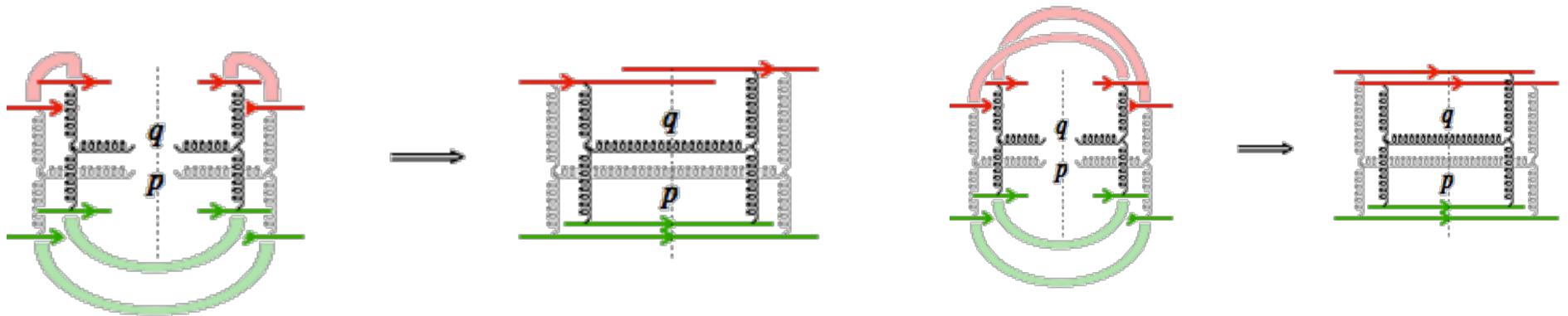


Glasma graphs generate long range rapidity correlations...

Glasma graphs are suppressed relative to “jet” graphs for $Q_s \ll p_T$ by **powers of α_s AND N_C** (At high p_T , large x or large impact parameters)

The saturated hadron: Glasma graphs-II

Correlations are induced by color fluctuations that vary event to event – for Gaussian weight functionals in ρ , have **color screening radius** $\sim 1/Q_s$



Glasma graphs generate long range rapidity correlations...

Suppressed for $Q_s \ll p_T$ by **powers of α_s AND N_c**
(At high p_T , large x or large impact parameters)

Glasma graphs enhanced by $1/\alpha_s^8$ for high occupancy fields (factor of 10^5 !)
(central impact parameters, small x , low p_T , large nuclei)

Nearside collimation: quantum interference of glue

Dumitru, Dusling, Gelis, Jalilian-Marian, Lappi, RV, arXiv:1009.5295

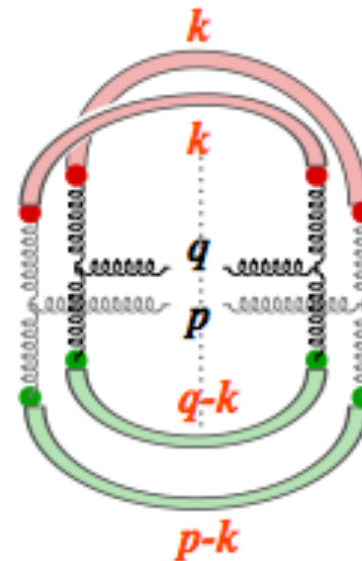
RG evolution of two particle correlations $C(p, q)$ expressed in terms of “unintegrated gluon distributions” in the proton

$$C(\mathbf{p}, \mathbf{q}) \propto \frac{g^4}{\mathbf{p}_\perp^2 \mathbf{q}_\perp^2} \int d^2 \mathbf{k}_{1\perp} \Phi_{A_1}^2(y_p, \mathbf{k}_{1\perp}) \Phi_{A_2}(y_p, \mathbf{p}_\perp - \mathbf{k}_{1\perp}) \Phi_{A_2}(y_q, \mathbf{q}_\perp - \mathbf{k}_{1\perp})$$

+ permutations

Proton 1

Proton 2



These contributions are of order α_s^6/N_c^2 in min. bias events-
in high multiplicity events power counting changes to $1/\alpha_s^2 N_c^2$

Nearside collimation: quantum interference of glue

Dumitru,Dusling,Gelis,Jalilian-Marian,Lappi,RV, arXiv:1009.5295

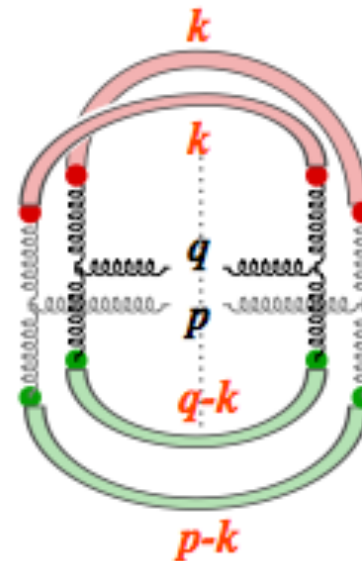
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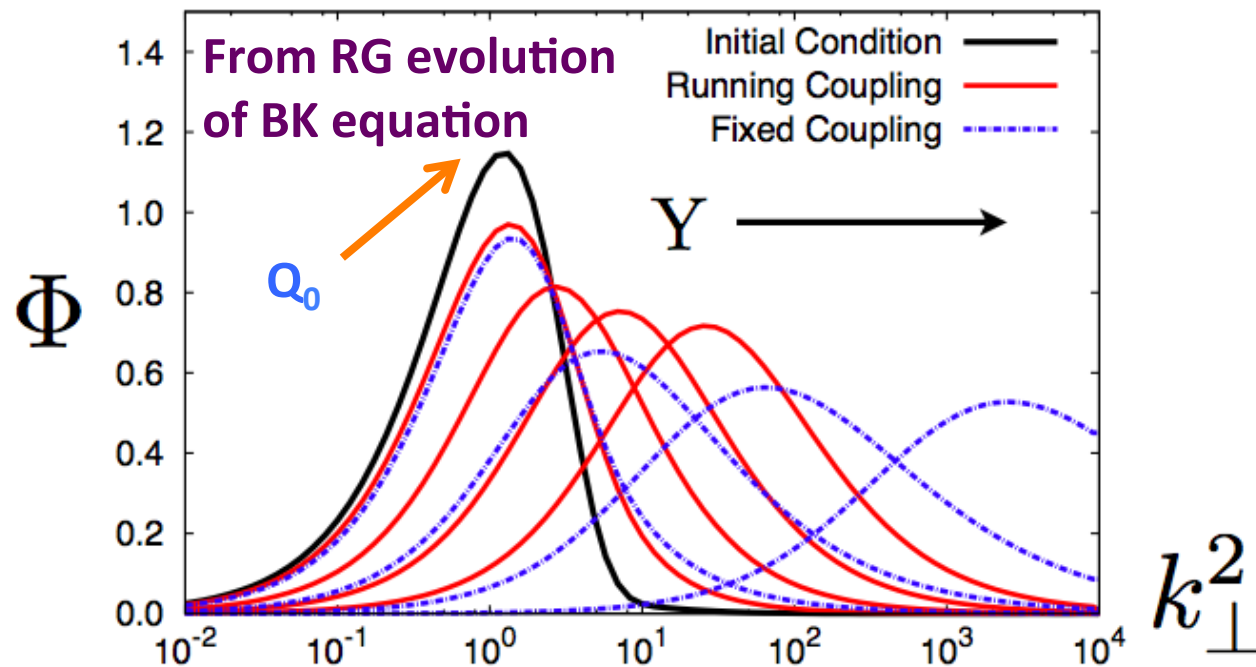


Enhancement of $\sim 10^5$ for $\alpha_s = 0.2$!

Nearside collimation: quantum interference of glue

$$C(\mathbf{p}, \mathbf{q}) \propto \frac{g^4}{\mathbf{p}_\perp^2 \mathbf{q}_\perp^2} \int d^2 \mathbf{k}_{1\perp} \Phi_{A_1}^2(y_p, \mathbf{k}_{1\perp}) \Phi_{A_2}(y_p, \mathbf{p}_\perp - \mathbf{k}_{1\perp}) \Phi_{A_2}(y_q, \mathbf{q}_\perp - \mathbf{k}_{1\perp})$$

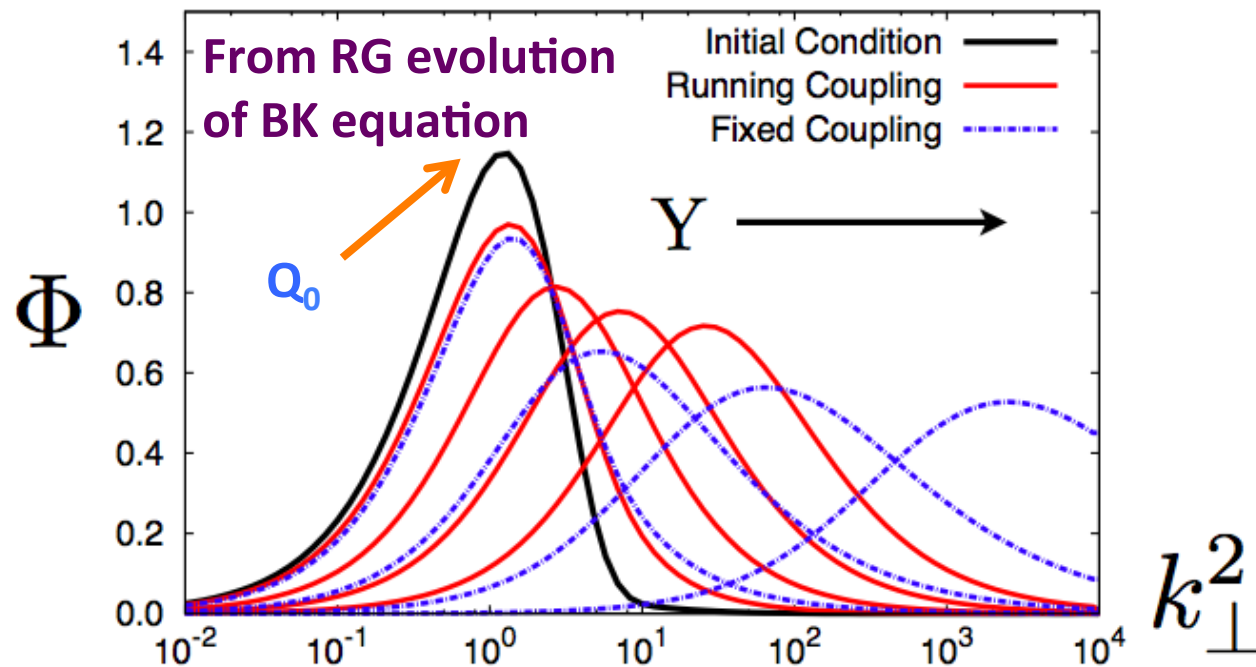
+ permutations



Collimated yield ?

$$C(\mathbf{p}, \mathbf{q}) \propto \frac{g^4}{\mathbf{p}_\perp^2 \mathbf{q}_\perp^2} \int d^2 \mathbf{k}_{1\perp} \Phi_{A_1}^2(y_p, \mathbf{k}_{1\perp}) \Phi_{A_2}(y_p, \mathbf{p}_\perp - \mathbf{k}_{1\perp}) \Phi_{A_2}(y_q, \mathbf{q}_\perp - \mathbf{k}_{1\perp})$$

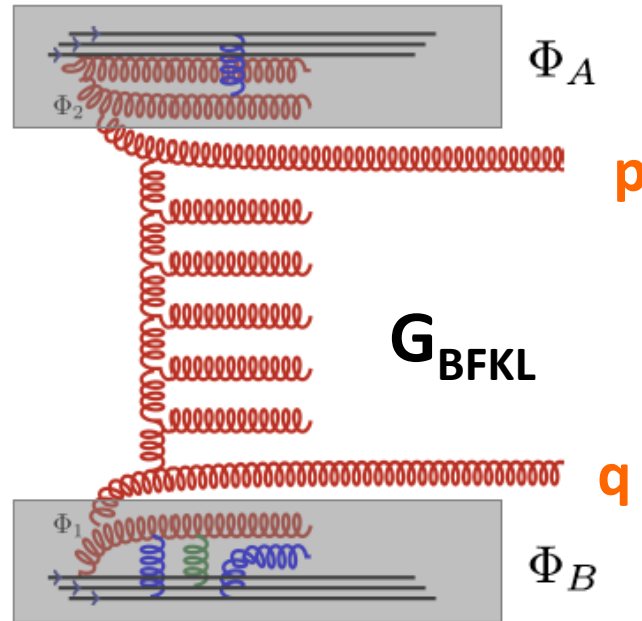
+ permutations



Dominant contribution from $|\mathbf{p}_T - \mathbf{k}_T| \sim |\mathbf{q}_T - \mathbf{k}_T| \sim |\mathbf{k}_T| \sim Q_s$

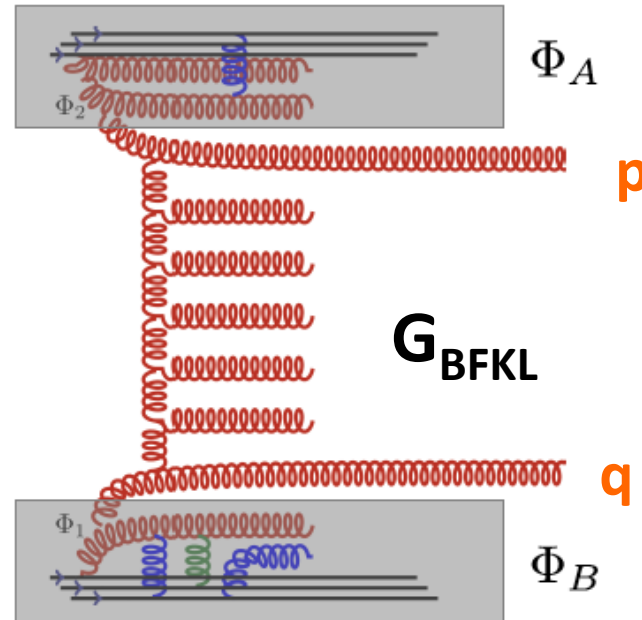
This gives a collimation for $\Delta\Phi \approx 0$ and π

Angular structure from (mini-) Jet radiation



$$C_{\text{dijet}}(\mathbf{p}, \mathbf{q}) \propto \Phi_A \otimes \Phi_B \otimes G_{\text{BFKL}}$$

Angular structure from (mini-) Jet radiation

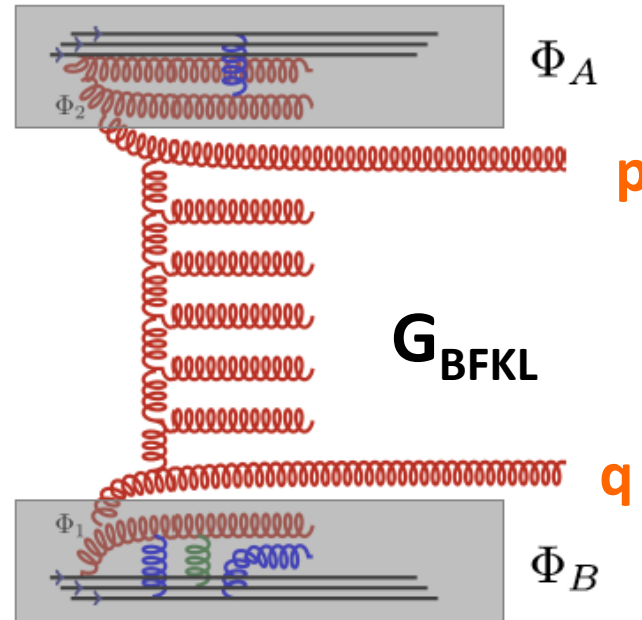


$$C_{\text{dijet}}(\mathbf{p}, \mathbf{q}) \propto \Phi_A \otimes \Phi_B \otimes G_{\text{BFKL}}$$

Mini-jets: O (1) in high multiplicity events

- give an angular collimation, albeit only at $\Delta\Phi \cong \pi$

Angular structure from (mini-) Jet radiation



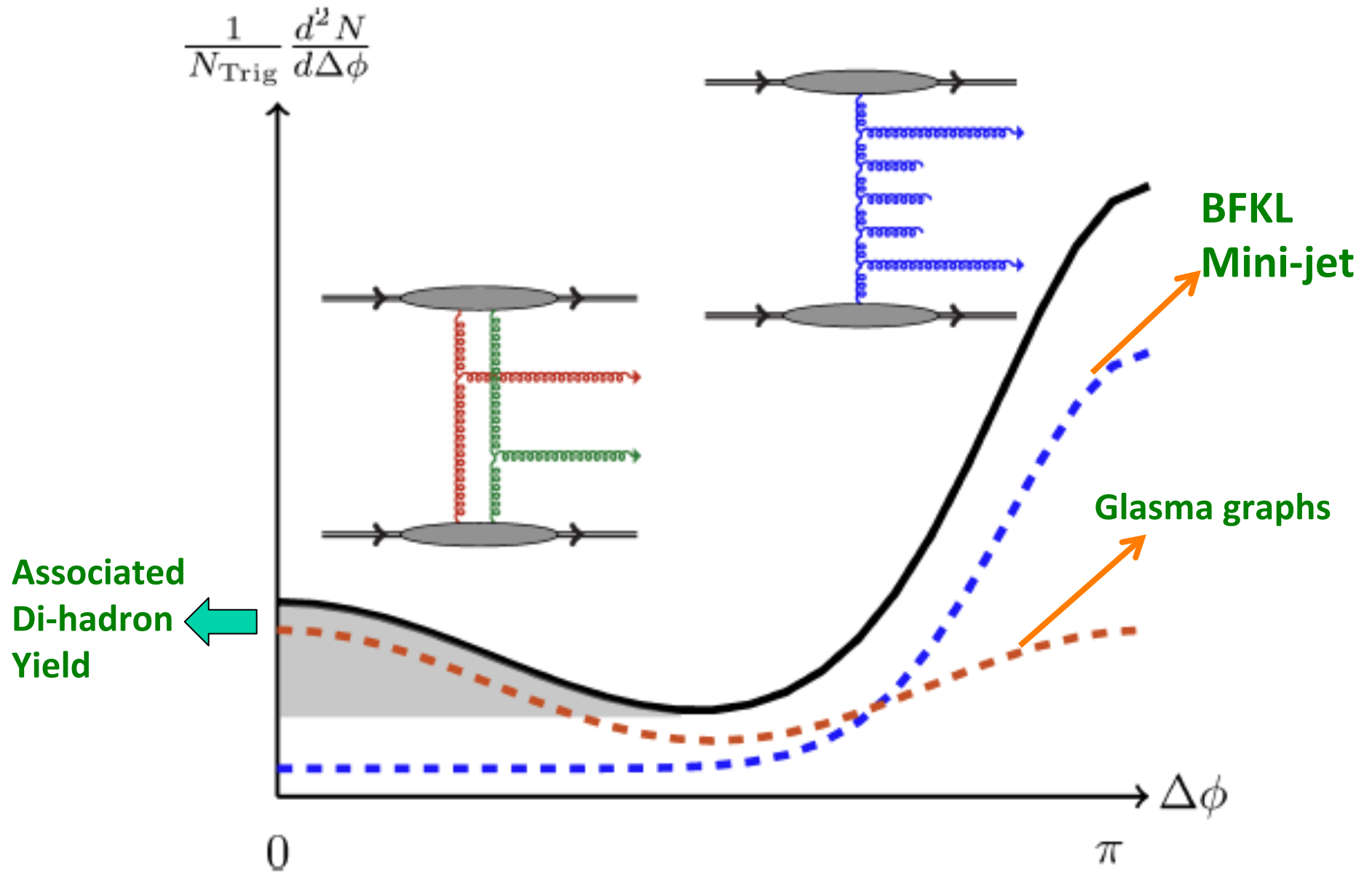
$$C_{\text{dijet}}(\mathbf{p}, \mathbf{q}) \propto \Phi_A \otimes \Phi_B \otimes G_{\text{BFKL}}$$

Mini-jets: $\mathcal{O}(1)$ in high multiplicity events

- give an angular collimation, albeit only at $\Delta\Phi \cong \pi$

LHC p+p & p+A “ridge” results also test the structure of bremsstrahlung radiation between jets

Anatomy of long range collimation yields



Quantitative description of pp ridge

Dusling, RV:PRL108 (2012)262001

$$\begin{aligned}
 \frac{d^2 N}{d\Delta\phi} &= K \int_{-2.4}^{+2.4} d\eta_p d\eta_q \mathcal{A}(\eta_p, \eta_q) \\
 &\times \int_{p_T^{\min}}^{p_T^{\max}} \frac{dp_T^2}{2} \int_{q_T^{\min}}^{q_T^{\max}} \frac{dq_T^2}{2} \int d\phi_p \int d\phi_q \delta(\phi_p - \phi_q - \Delta\phi) \\
 &\times \int_0^1 dz_1 dz_2 \frac{D(z_1)}{z_1^2} \frac{D(z_2)}{z_2^2} \frac{d^2 N_{\text{Glasma}}^{\text{corr.}}}{d^2 \mathbf{p}_T d^2 \mathbf{q}_T d\eta_p d\eta_q} \left(\frac{p_T}{z_1}, \frac{q_T}{z_2}, \Delta\phi \right)
 \end{aligned}
 \tag{6}$$

$$\mathcal{A}(\eta_p, \eta_q) = \theta(|\eta_p - \eta_q| - \Delta\eta_{\min}) \theta(\Delta\eta_{\max} - |\eta_p - \eta_q|)$$

$$N_{\text{trig}} = \int_{-2.4}^{+2.4} d\eta \int_{p_T^{\min}}^{p_T^{\max}} d^2 \mathbf{p}_T \int_0^1 dz \frac{D(z)}{z^2} \frac{dN}{d\eta d^2 \mathbf{p}_T} \left(\frac{p_T}{z} \right)$$

$$\text{Assoc. Yield} = \frac{1}{N_{\text{trig}}} \int_0^{\Delta\phi_{\min.}} d\Delta\phi \frac{d^2 N}{d\Delta\phi} - \frac{d^2 N}{d\Delta\phi} \Big|_{\Delta\phi_{\min.}}$$

Dependence on transverse area cancels in ratio...

Quantitative description of pp ridge

Dusling, RV:PRL108 (2012)262001

$$\frac{d^2 N}{d\Delta\phi} = K \int_{-2.4}^{+2.4} d\eta_p d\eta_q \mathcal{A}(\eta_p, \eta_q) \quad (6)$$

$$\mathcal{A}(\eta_p, \eta_q) = \theta(|\eta_p - \eta_q| - \Delta\eta_{\min}) \theta(\Delta\eta_{\max} - |\eta_p - \eta_q|)$$

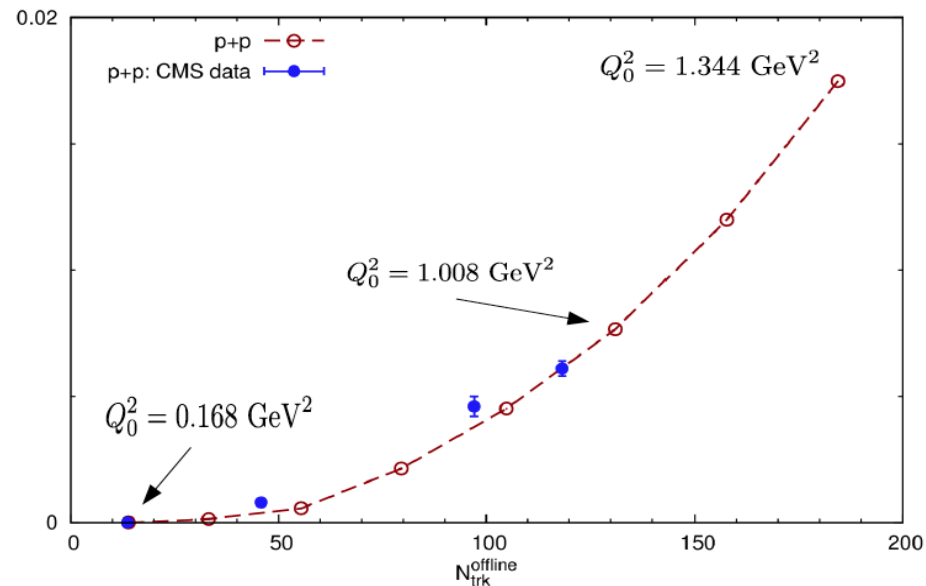
$$\times \int_{p_T^{\min}}^{p_T^{\max}} \frac{dp_T^2}{2} \int_{q_T^{\min}}^{q_T^{\max}} \frac{dq_T^2}{2} \int d\phi_p \int d\phi_q \delta(\phi_p - \phi_q - \Delta\phi)$$

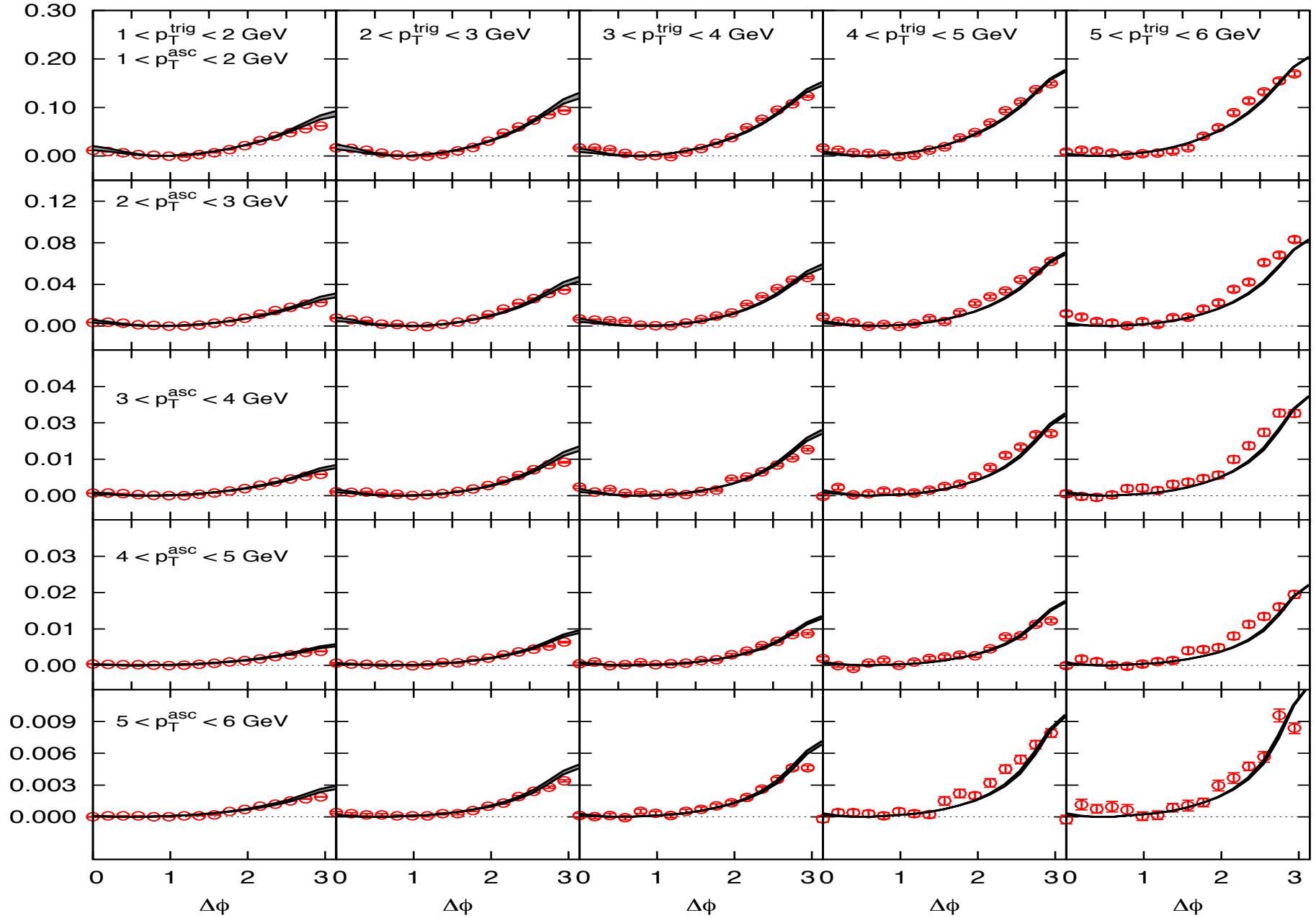
$$\times \int_0^1 dz_1 dz_2 \frac{D(z_1)}{z_1^2} \frac{D(z_2)}{z_2^2} \frac{d^2 N_{\text{Glasma}}^{\text{corr.}}}{d^2 \mathbf{p}_T d^2 \mathbf{q}_T d\eta_p d\eta_q} \left(\frac{p_T}{z_1}, \frac{q_T}{z_2}, \Delta\phi \right) \quad N_{\text{trig}} = \int_{-2.4}^{+2.4} d\eta \int_{p_T^{\min}}^{p_T^{\max}} d^2 \mathbf{p}_T \int_0^1 dz \frac{D(z)}{z^2} \frac{dN}{d\eta d^2 \mathbf{p}_T} \left(\frac{p_T}{z} \right)$$

$$\text{Assoc. Yield} = \frac{1}{N_{\text{trig}}} \int_0^{\Delta\phi_{\min.}} d\Delta\phi \left. \frac{d^2 N}{d\Delta\phi} - \frac{d^2 N}{d\Delta\phi} \right|_{\Delta\phi_{\min.}}$$

Dependence on transverse area cancels in ratio...

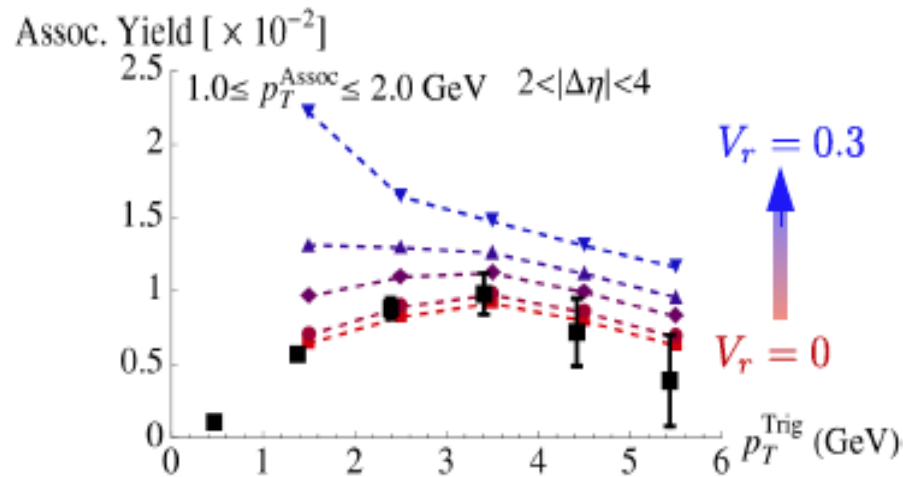
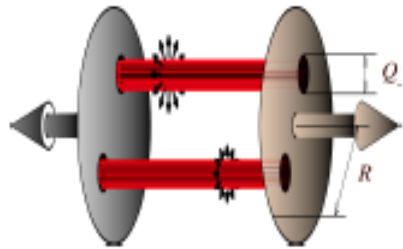
Rarer and rarer
gluon configurations
probed in the proton





p+p

In p+p we are seeing the intrinsic collimation from a single flux tube

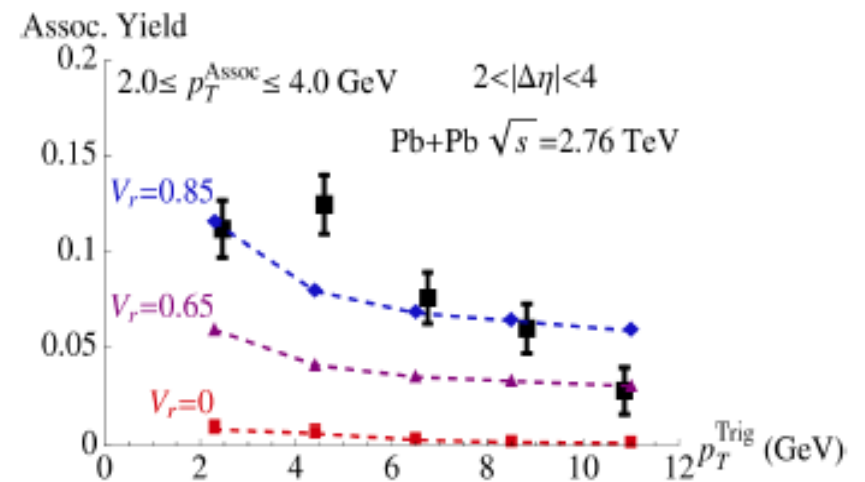
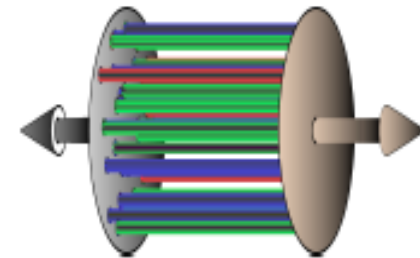


Increasing transverse flow in p+p creates a discrepancy with data.

vs

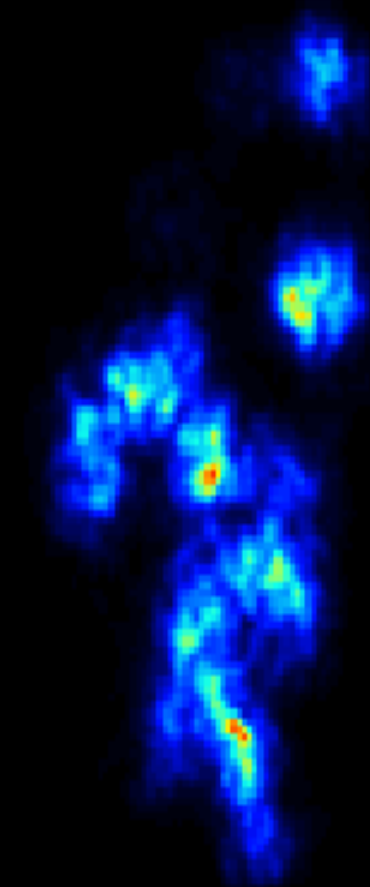
A+A

In A+A there are many such tubes each with an intrinsic correlation enhanced by flow

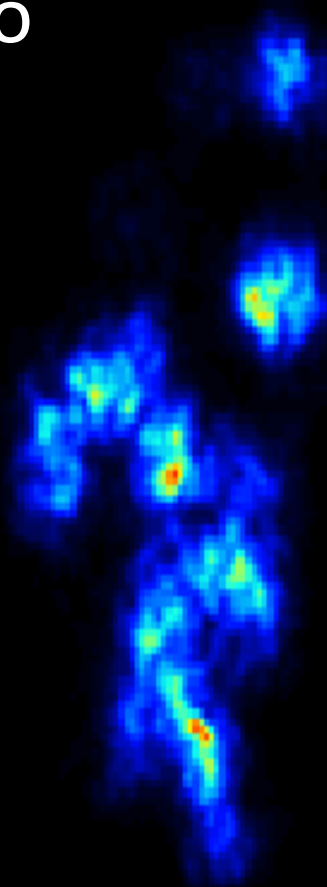


Yet, transverse flow is needed to explain identical measurements in Pb+Pb

IP-Glasma model: match event-by-event Yang-Mills to viscous hydro



2+1-D Yang-Mills



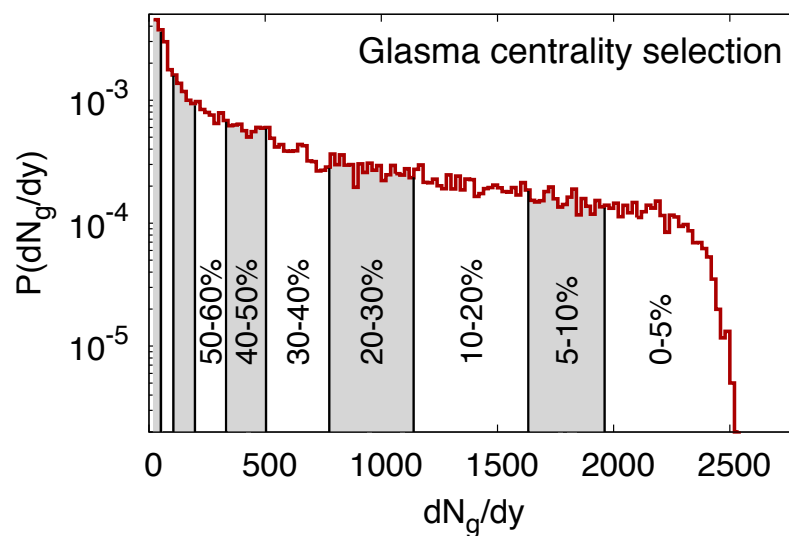
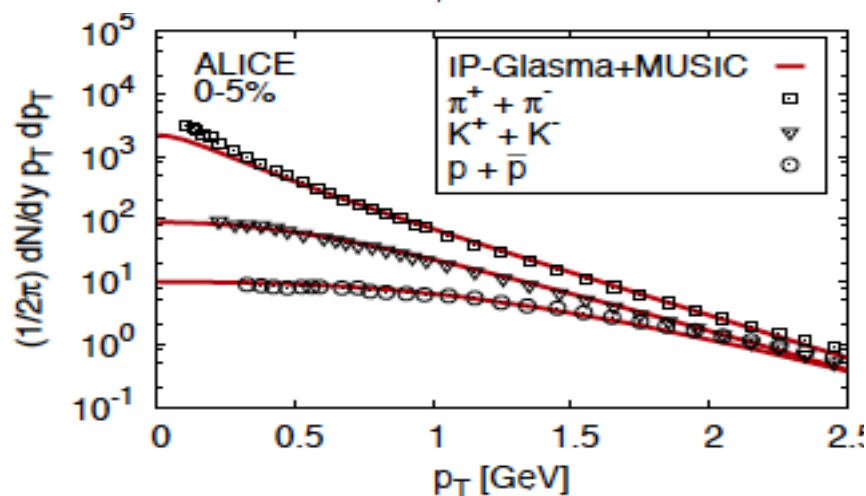
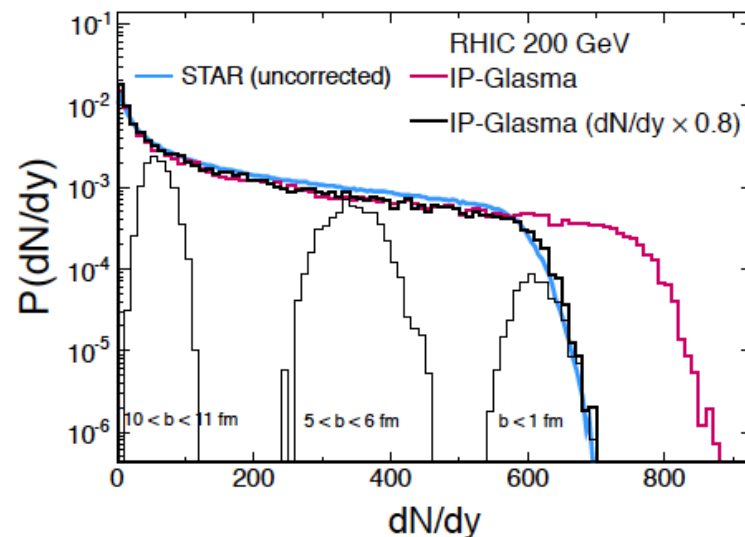
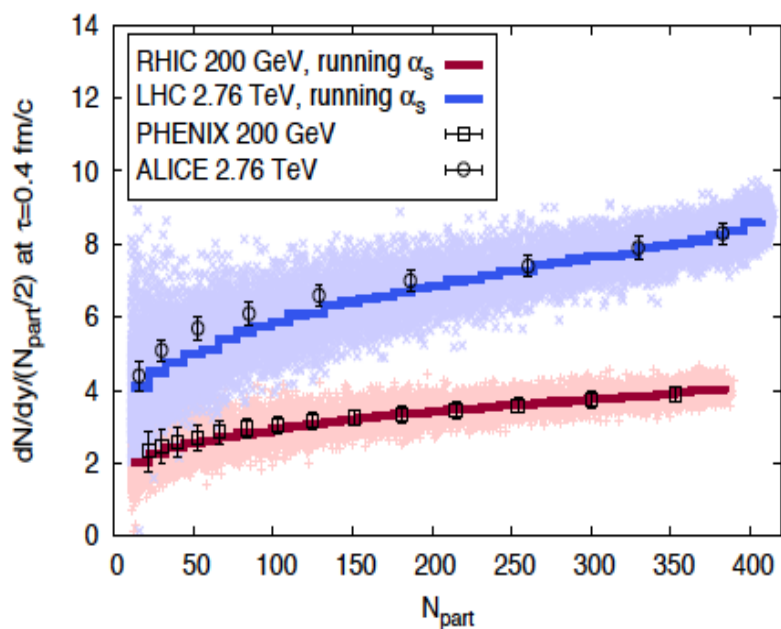
2+1-D Yang-Mills +
2+1-D Viscous hydro

$t = 0.0$ fm/c

Heavy Ion phenomenology: IP-Glasma model

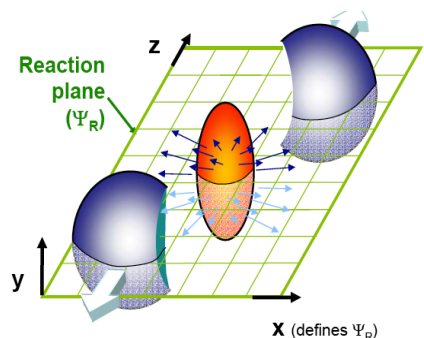
I) Multiplicity distributions

Schenke, Tribedy, RV: PRL108 (2012), 252301; arXiv:1206.6805



IP-Glasma model for A+A

II) Harmonic flow moments (event-by-event 2+1-D CYM + viscous hydro a la MUSIC)

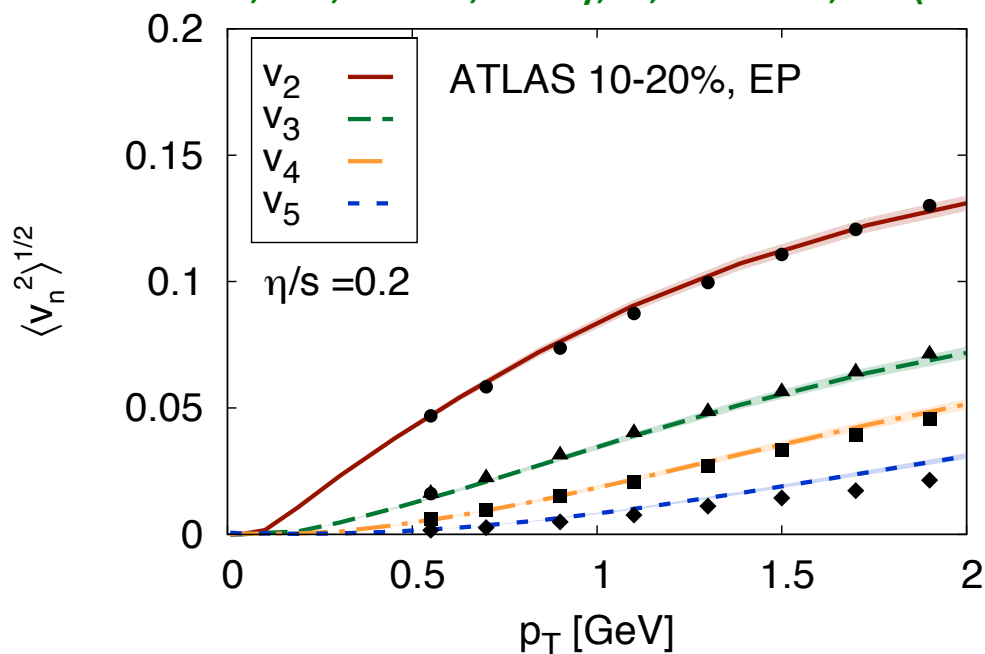
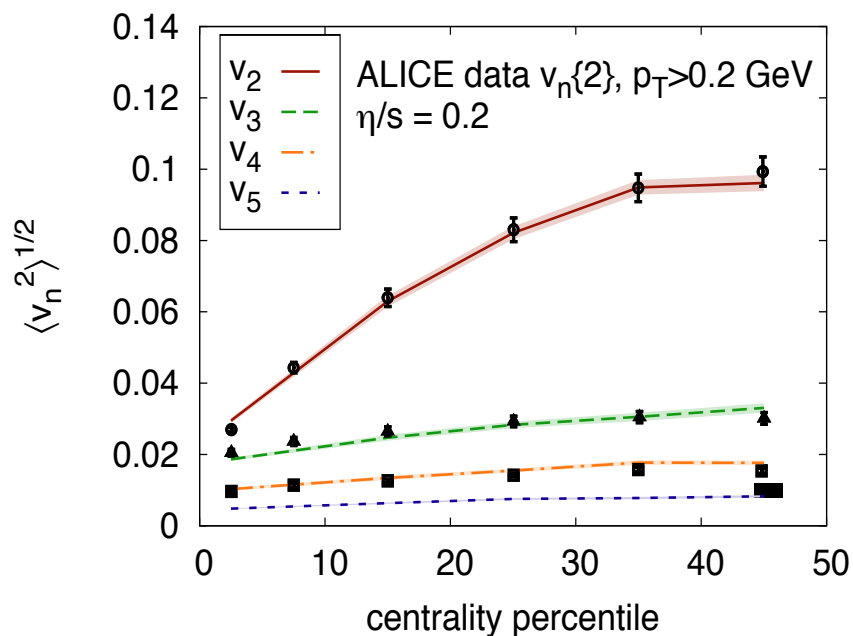


$$v_n = \langle \cos(n(\phi - \psi_n)) \rangle$$

MUSIC:Schenke,Jeon,Gale (2011)

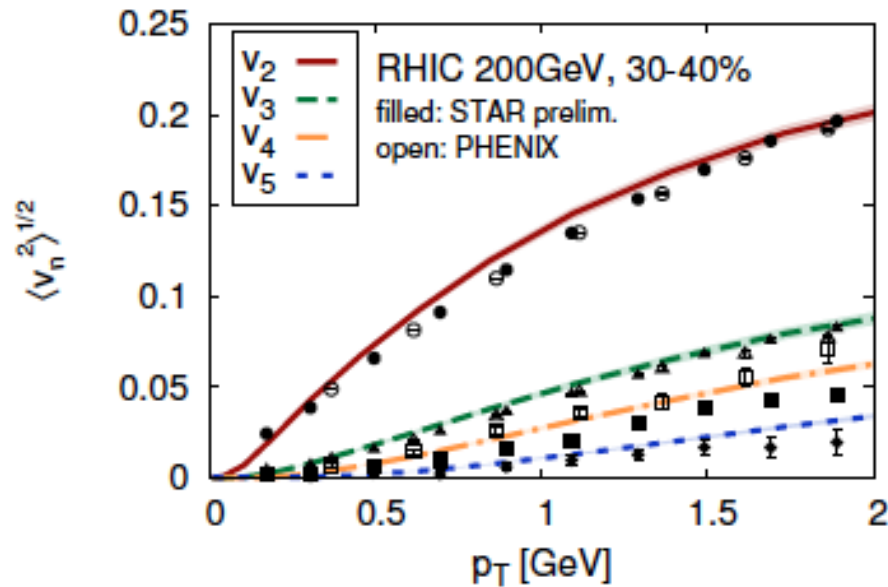
$$\psi_n = \frac{1}{n} \arctan \frac{\langle \sin(n\phi) \rangle}{\langle \cos(n\phi) \rangle}$$

Gale,Jeon,Schenke,Tribedy,RV, 1209.6330, PRL (2013)

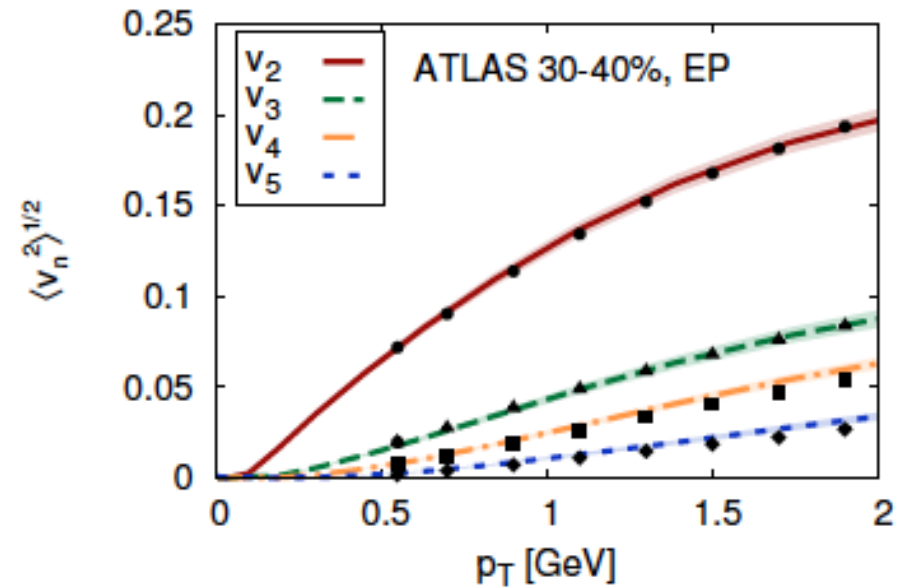


IP-Glasma model for A+A

RHIC $\eta/s = 0.12$

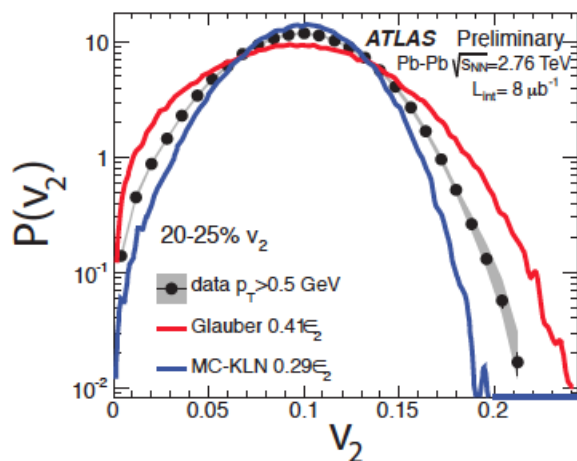


LHC $\eta/s = 0.2$



Initial state Glasma fluctuations + flow describe v_n data for wide range of centrality classes in A+A

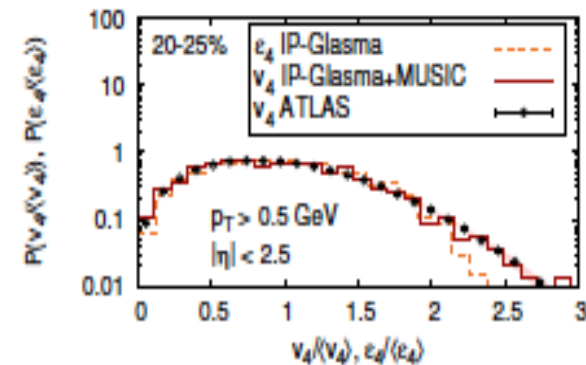
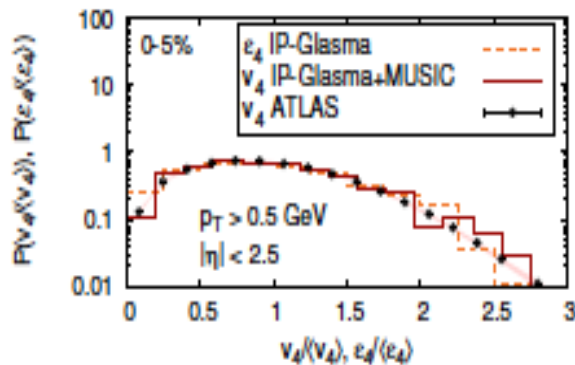
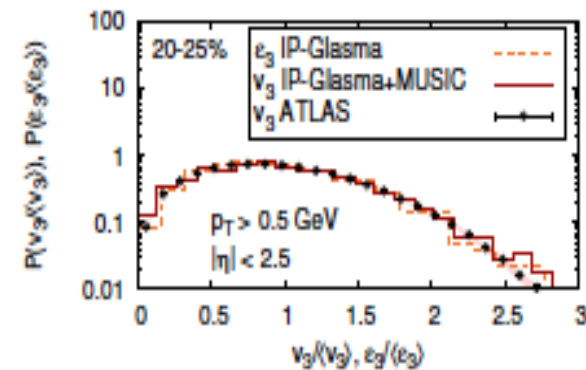
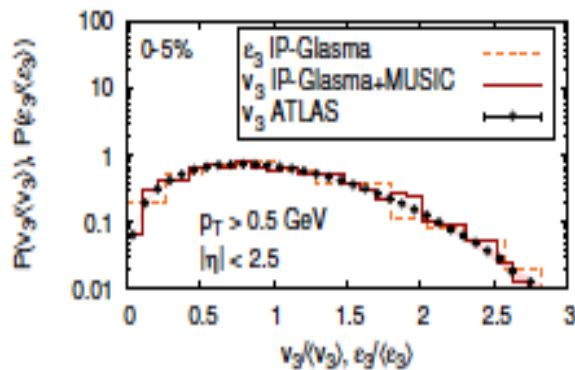
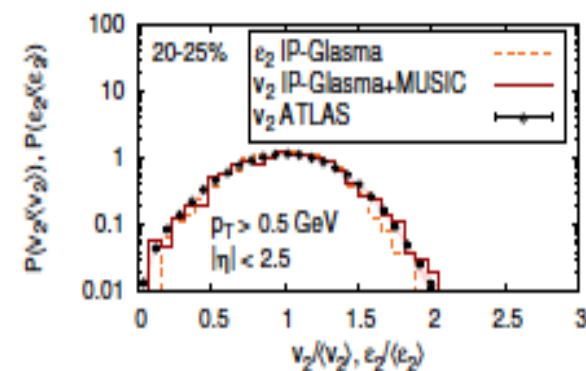
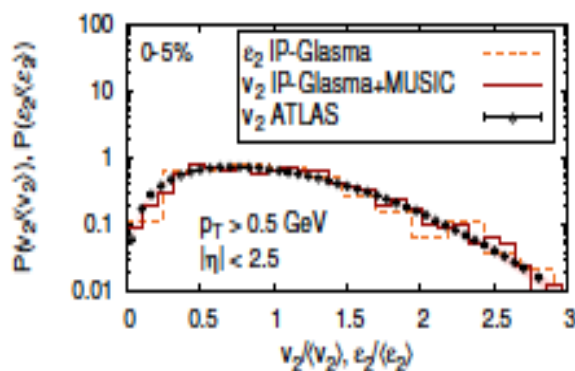
IP-Glasma model for A+A



Event-by-event
flow fluctuations
of v_2, v_3, v_4

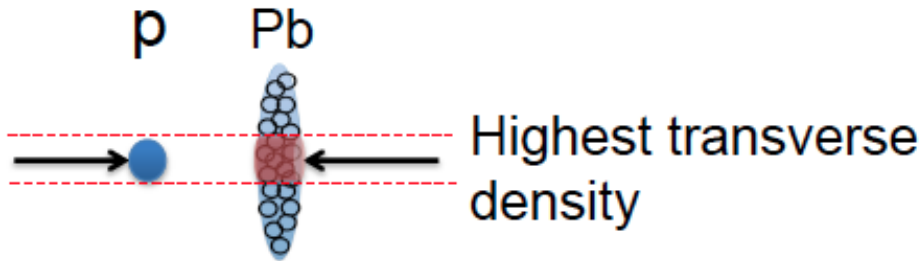
0-5%

20-25%



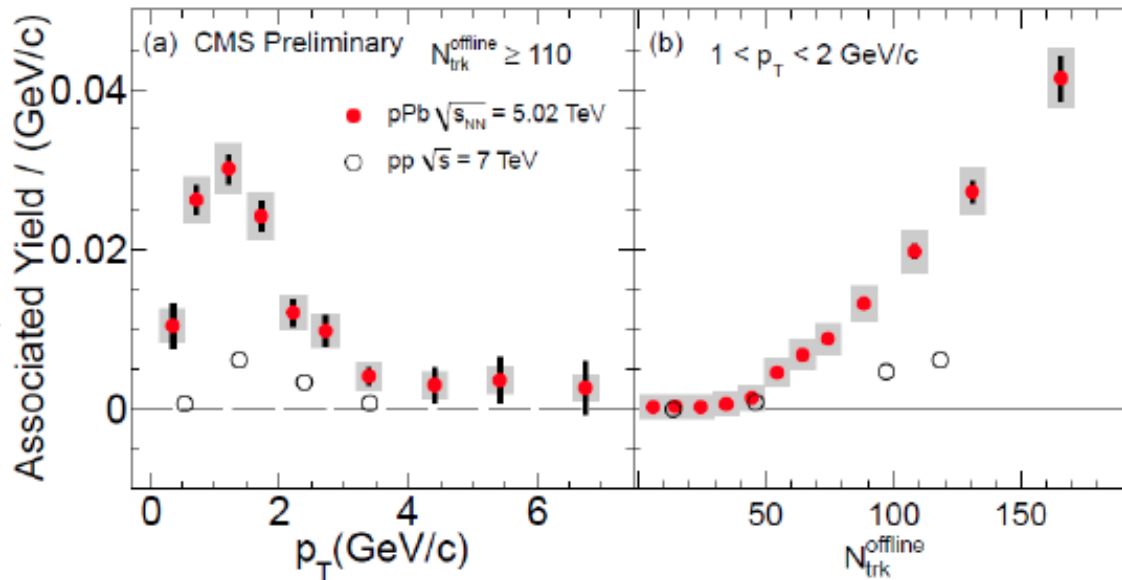
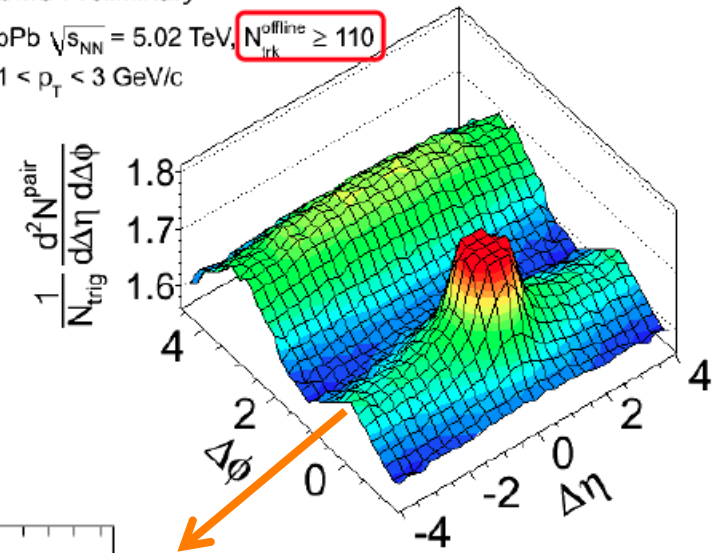
What about p+A ? LHC “pilot” run data

CMS coll. arXiv:1210.5482, Phys. Lett. B



CMS Preliminary

pPb $\sqrt{s_{NN}} = 5.02$ TeV, $N_{trk}^{offline} \geq 110$
 $1 < p_T < 3$ GeV/c



Ridge much bigger than p+p for the same multiplicity !

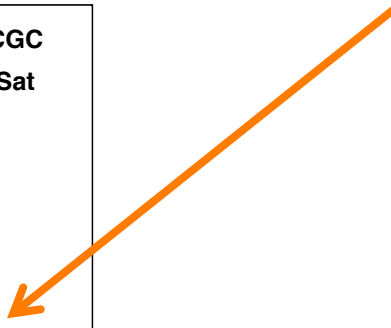
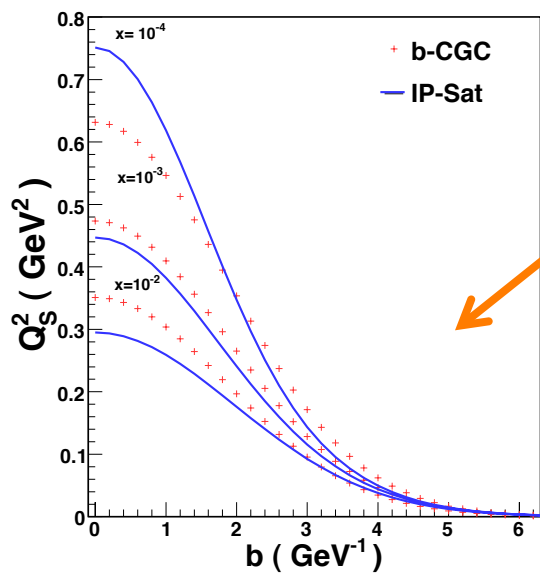
CMS p+Pb pilot run data explained

Dusling, RV: 1302.7018

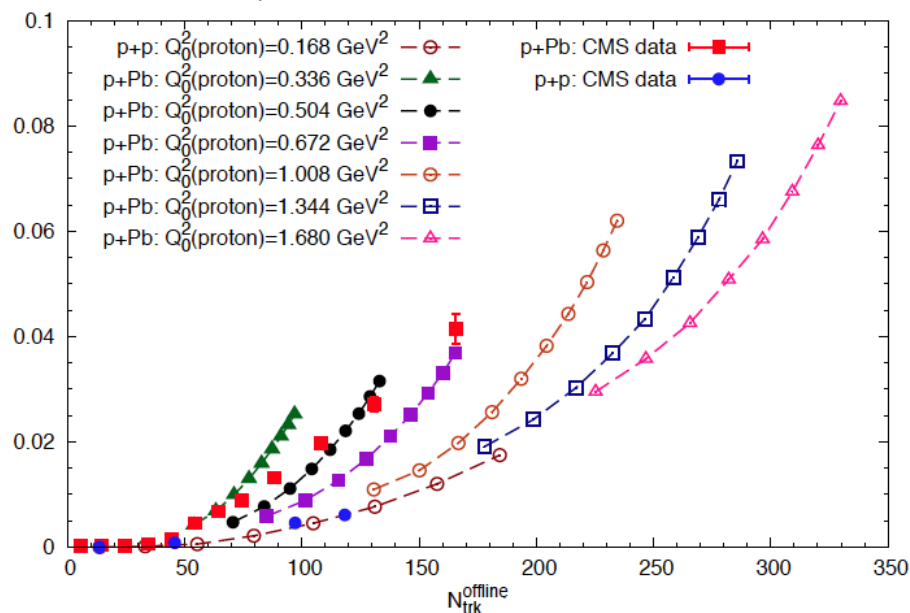
$$Q_0^2(\text{lead}) = N_{\text{part}}^{\text{Pb}} * Q_0^2(\text{proton})$$



of “wounded” nucleons in Lead nucleus



Associated Yield ($1.0 \leq p_T [\text{GeV}] \leq 2.0$)



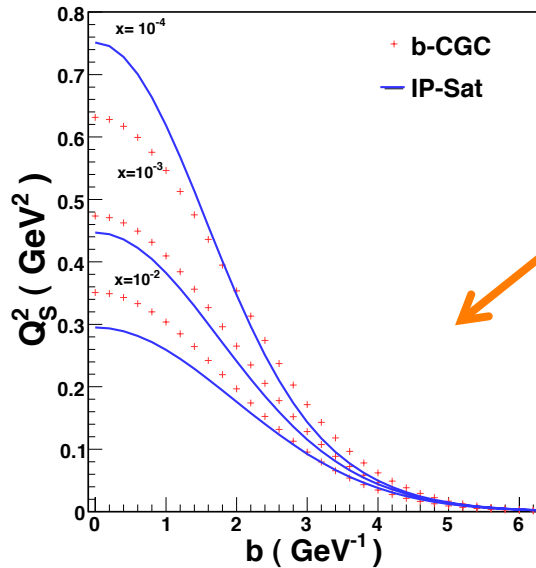
CMS p+Pb pilot data explained

Dusling, RV: 1302.7018

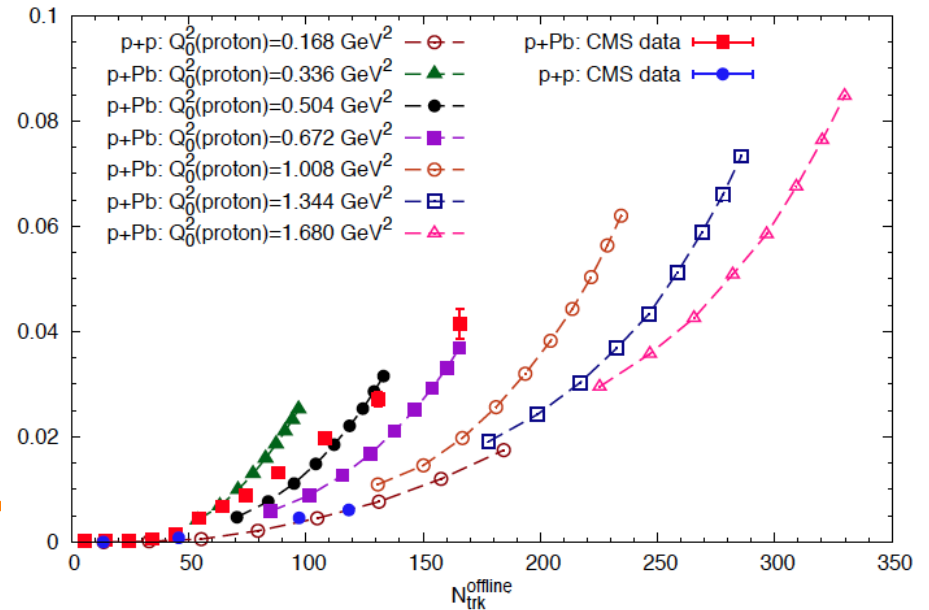
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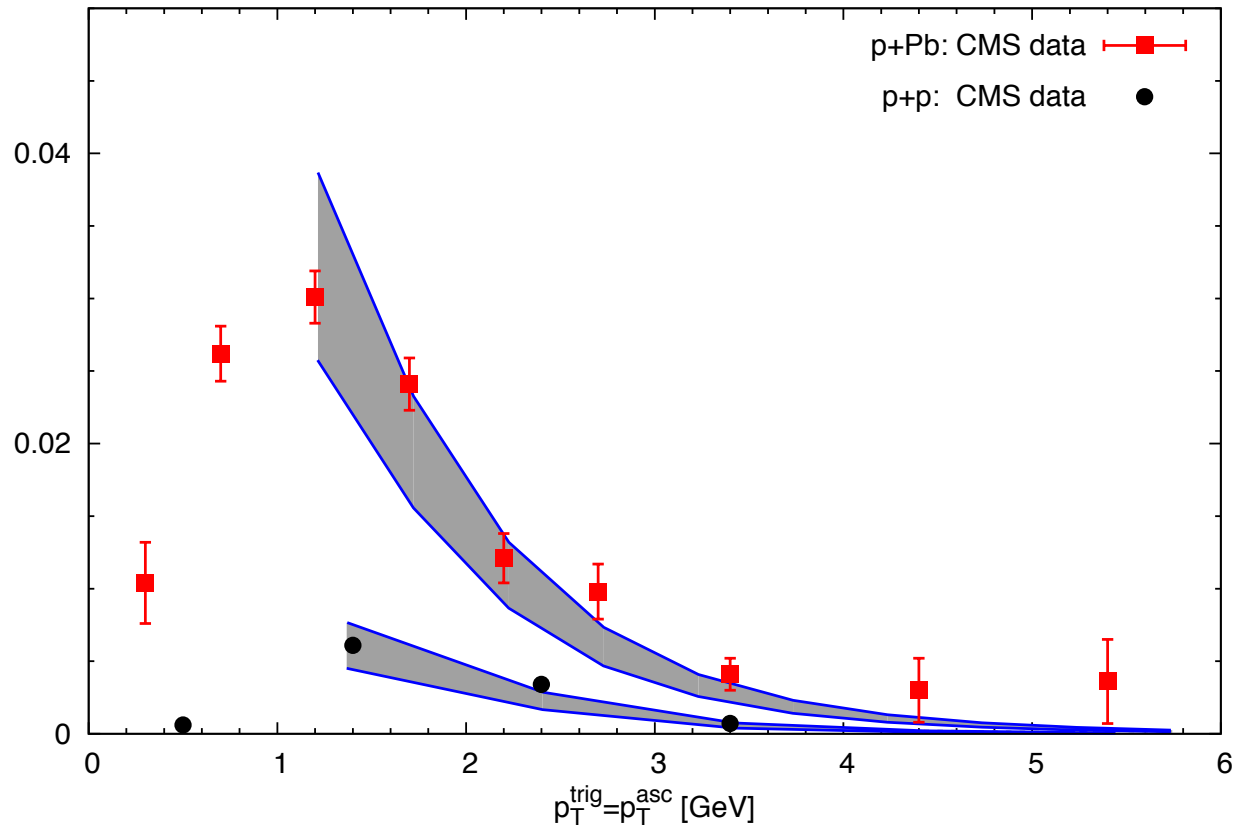
Large “ridge” seen by varying saturation scale in proton and # of wounded nucleons

--rarer and rarer Fock configurations probed in both proton and nucleus

CMS p+Pb pilot data explained

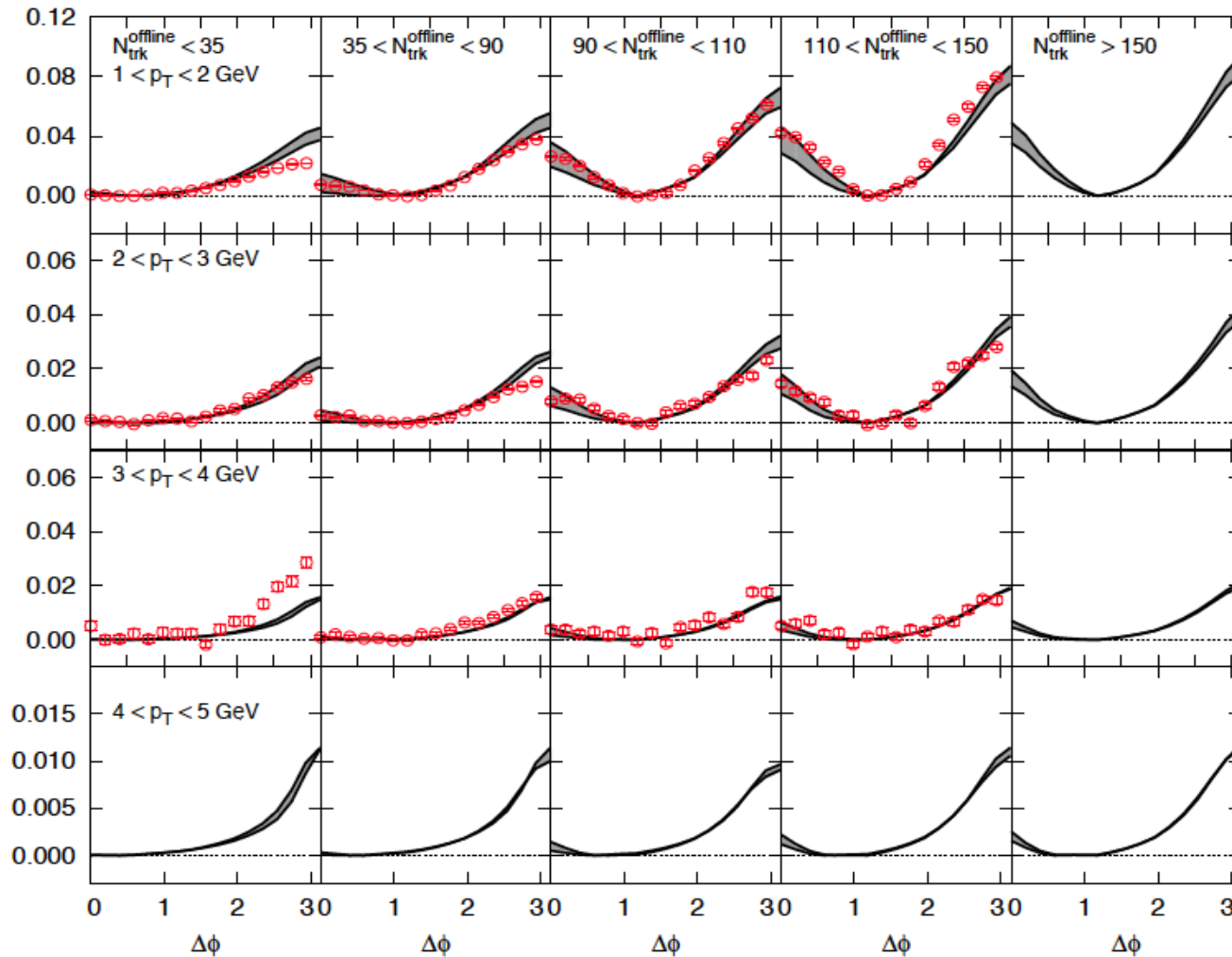
Dusling, RV: 1211.3701
1302.7018

Associated Yield

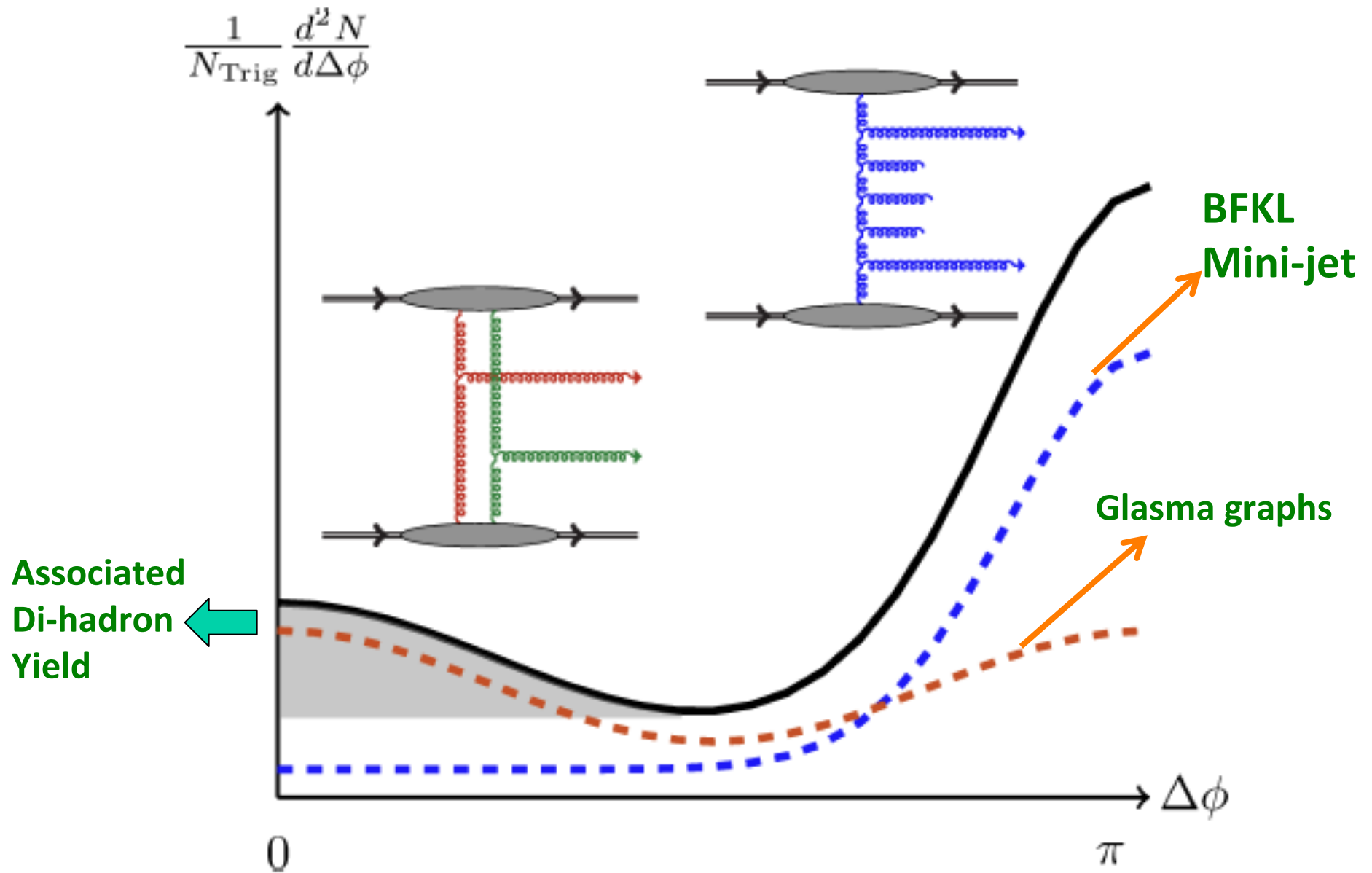


CMS pilot p+Pb data explained

Dusling, RV: 1211.3701
1302.7018



Anatomy of long range di-hadron collimation



ALICE data on the p+Pb ridge

ALICE coll. [arXiv:1212.2001](https://arxiv.org/abs/1212.2001)

Different acceptance ($|\Delta\eta| < 1.8$) than CMS ($2 < |\eta| < 4$) and ATLAS ($2 < |\eta| < 5$).

ALICE subtracts away-side “jet” contribution at 60-100% centrality from most central events

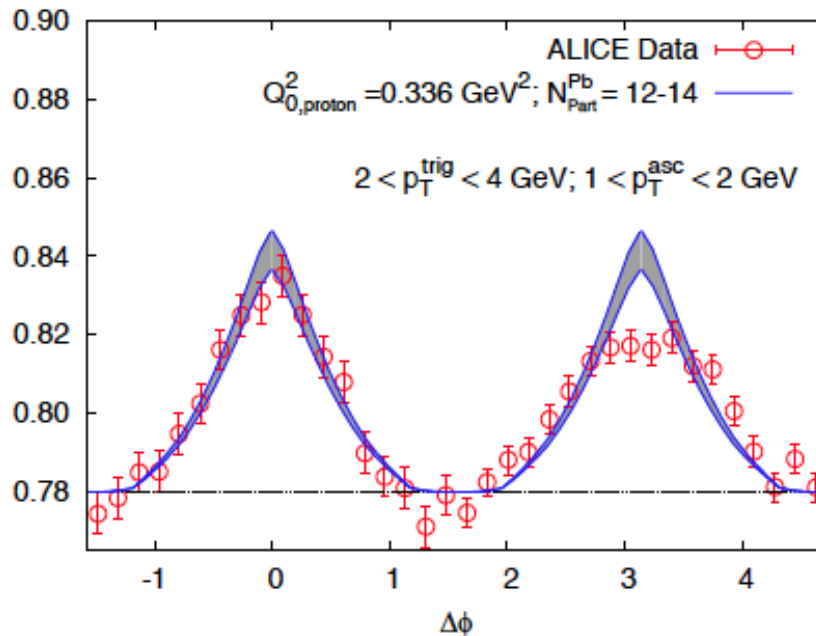
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–this gives dipole shape of correlation



Different analysis technique from CMS/ATLAS

-- same normalization as for CMS/ATLAS

Curves for $Q_{0,proton}^2 = 0.336 \text{ GeV}^2$
& $N_{part}^{Pb} = 12 - 14$

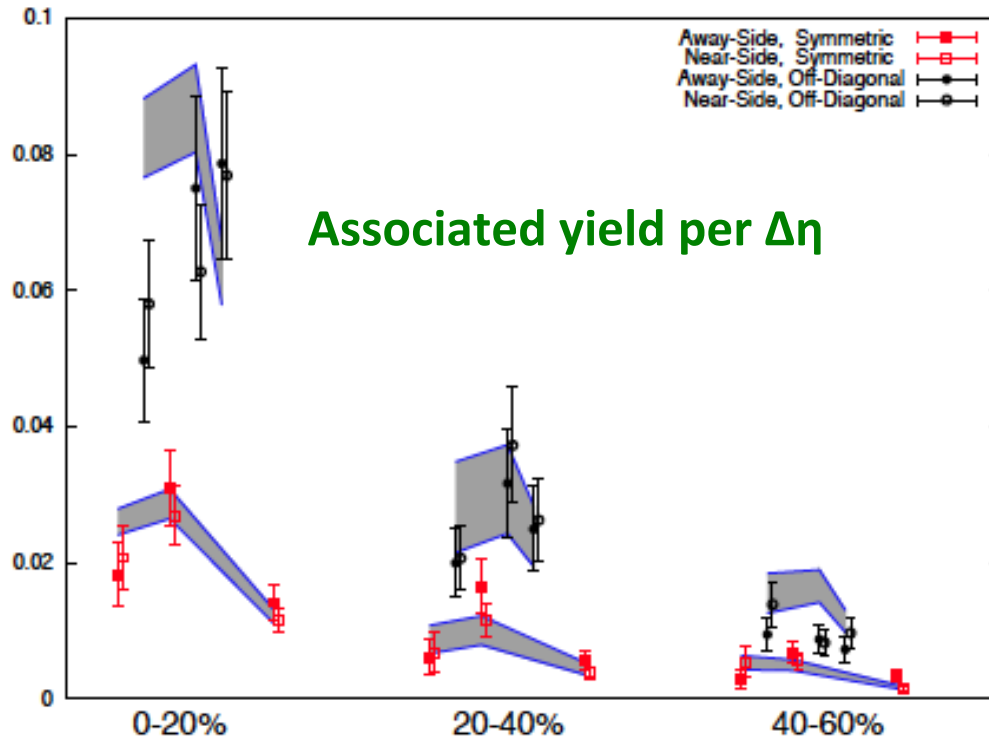
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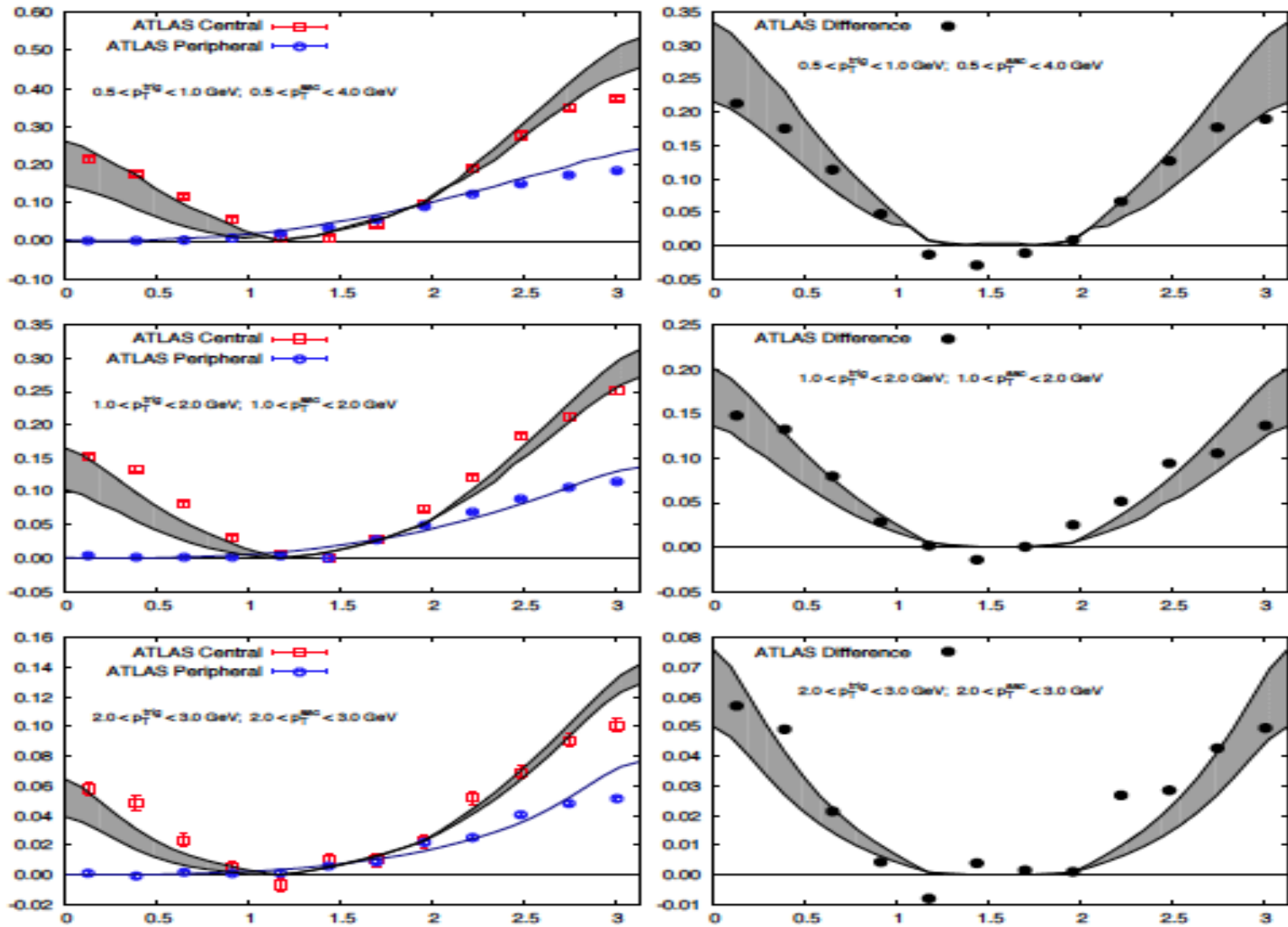
$$0-20\% : Q_{0,\text{proton}}^2 = 0.336 \text{ GeV}^2$$
$$\& N_{\text{part}}^{\text{Pb}} = 12 - 14$$

$$20-40\% : Q_{0,\text{proton}}^2 = 0.336 \text{ GeV}^2$$
$$\& N_{\text{part}}^{\text{Pb}} = 4 - 6$$

$$40-60\% : Q_{0,\text{proton}}^2 = 0.168 \text{ GeV}^2$$
$$\& N_{\text{part}}^{\text{Pb}} = 3-4$$

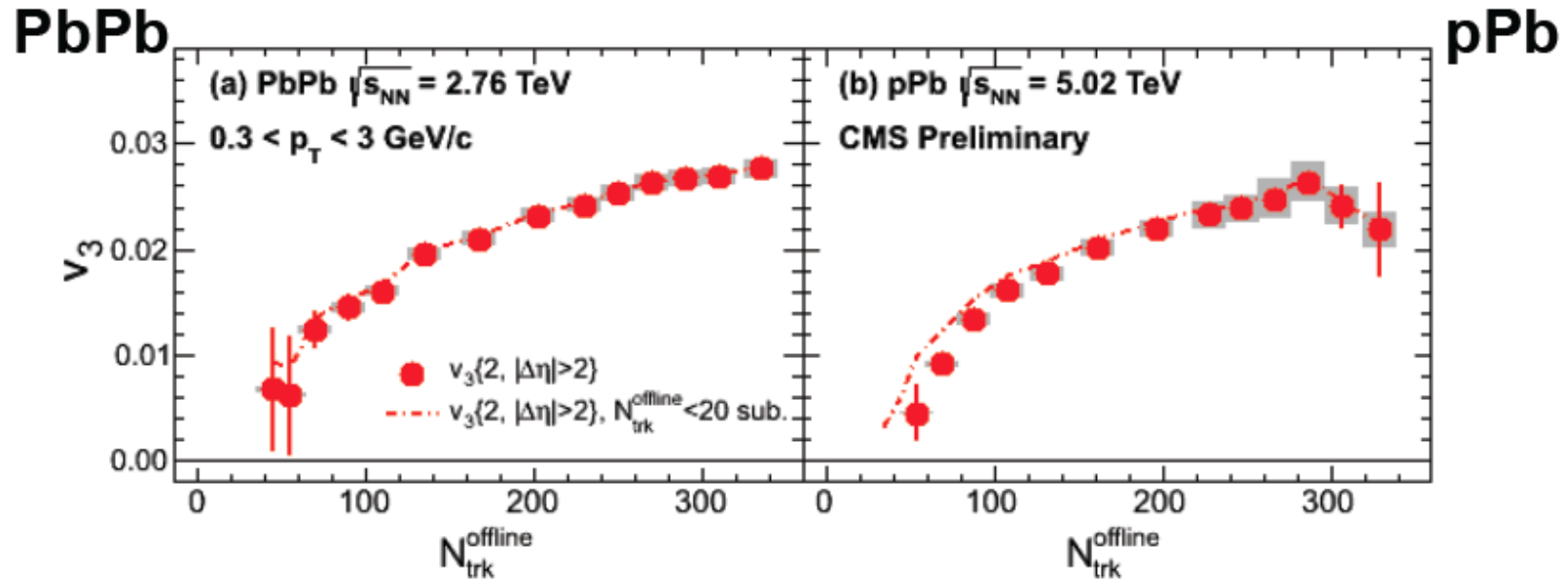
Comparison to ATLAS p+Pb ridge

ATLAS coll. arXiv: 1212.5198



Striking new data presented by CMS

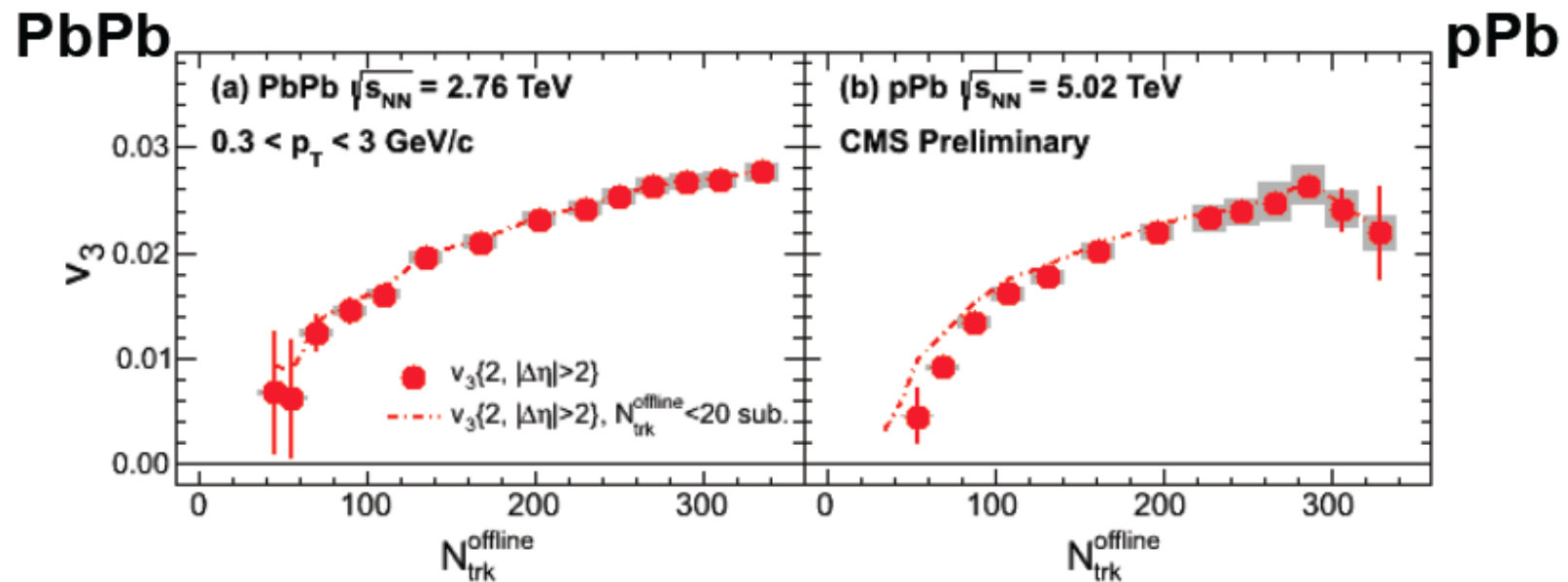
G. Roland, talk at RBRC workshop, BNL, April 16, 2013
CMS 1305.0609



A non-zero v_3 is not obviously obtained from the Glasma graphs, which gives only even moments.

Striking new data presented by CMS

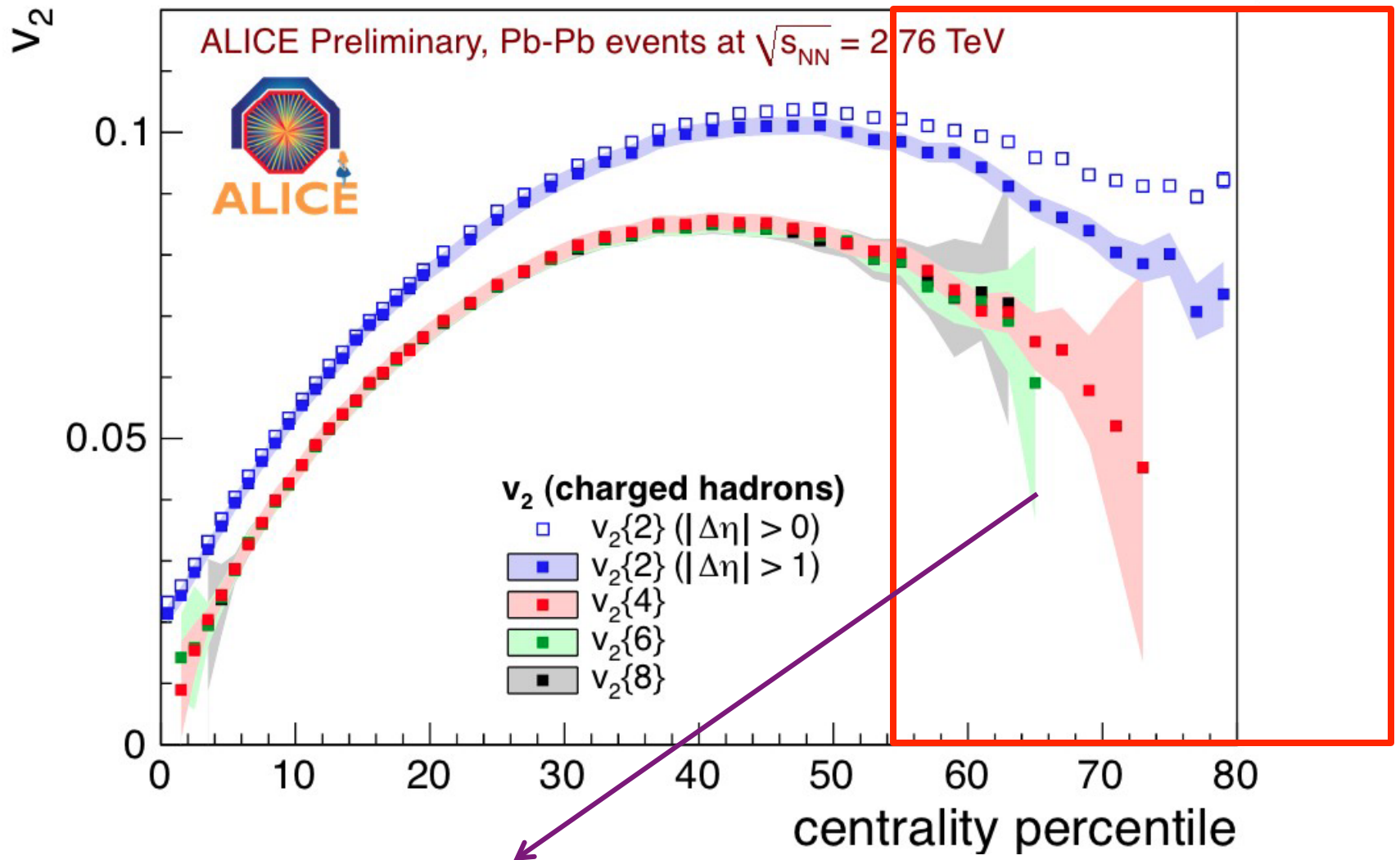
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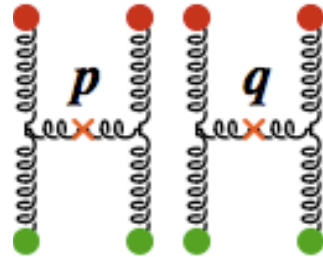
Is it an indication of flow ?

p+Pb versus Pb+Pb

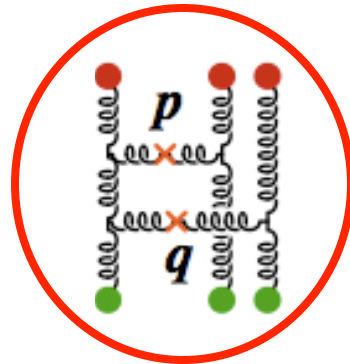


CMS Pb+Pb data comparison is
In 55%-92% centrality range

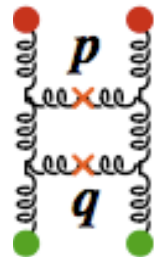
Multi-part. production: systematic power counting



CGC/Glasma yield



Jet/Glasma
interference



"pQCD" jet

Maybe flow ...

but **jet/Glasma interference** term not computed
previously--assumed small. Check if one gets v_3 ...

IP-Glasma+MUSIC model for p+A

Bzdak,Schenke,Tribedy,RV:1304.3403

Initial conditions from IP-Glasma model

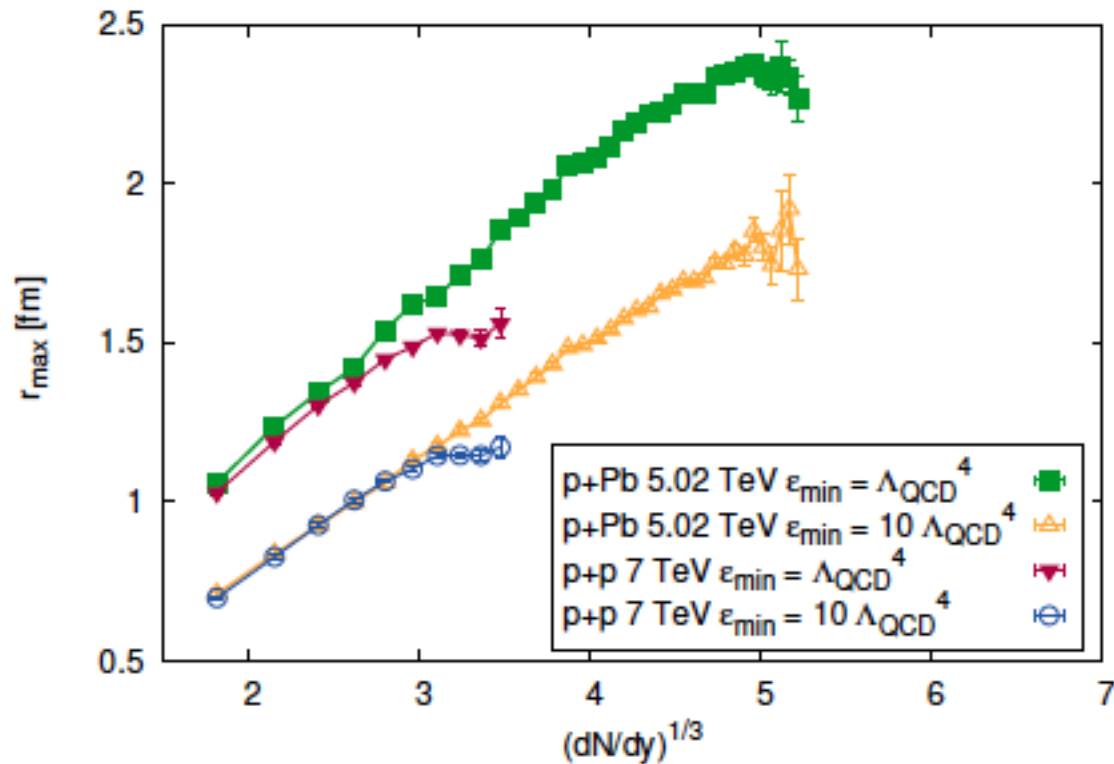
Event-by-event viscous hydro with MUSIC

Flow in p+A: IP-Glasma+MUSIC model

Bzdak,Schenke,Tribedy,RV:1304.3403

CGC initial conditions from IP-Glasma model

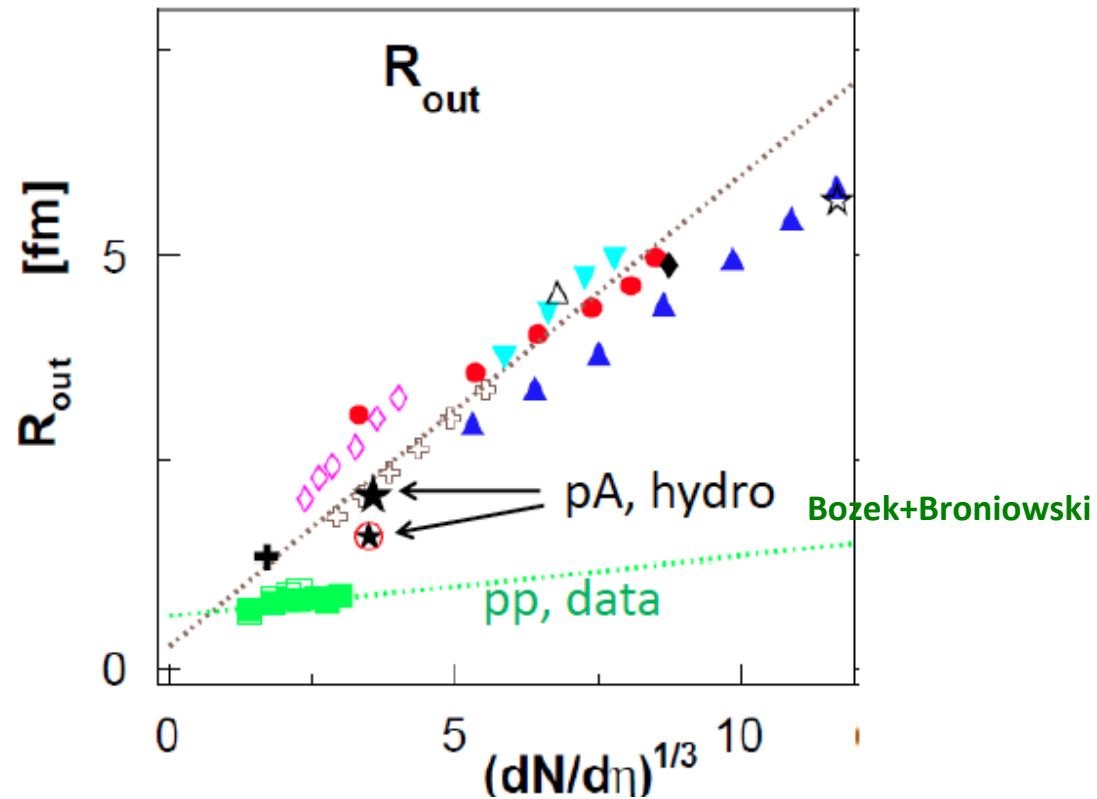
Event-by-event viscous hydro with MUSIC



Initial radii are nearly identical in p+p and p+A

IP-Glasma+MUSIC model for p+A

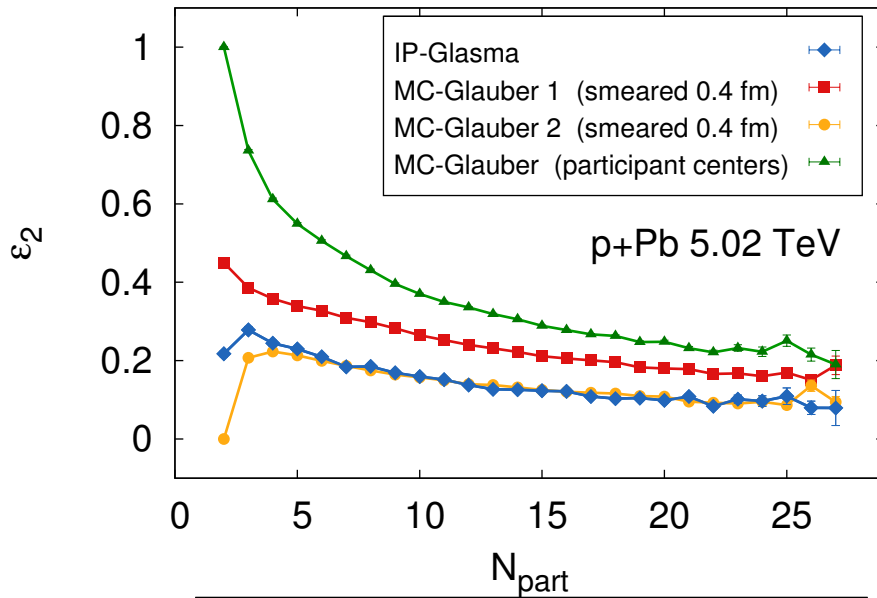
Bzdak,Schenke,Tribedy,RV:1304.3403



Without flow, HBT radii in p+p and p+A will be similar in IP-Glasma

Initial conditions in p+A: IP-Glasma vs “Glauber”

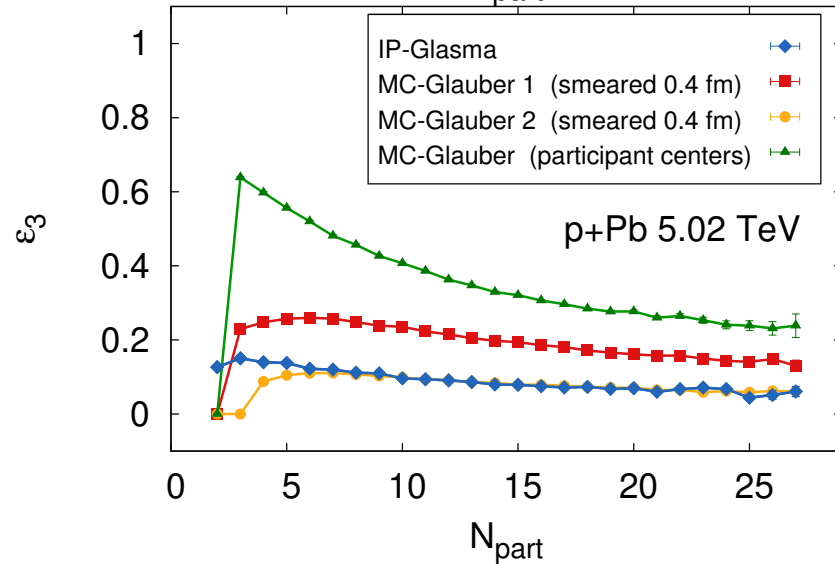
Bzdak,Schenke,Tribedy,RV:1304.3403



MC-Glauber 1

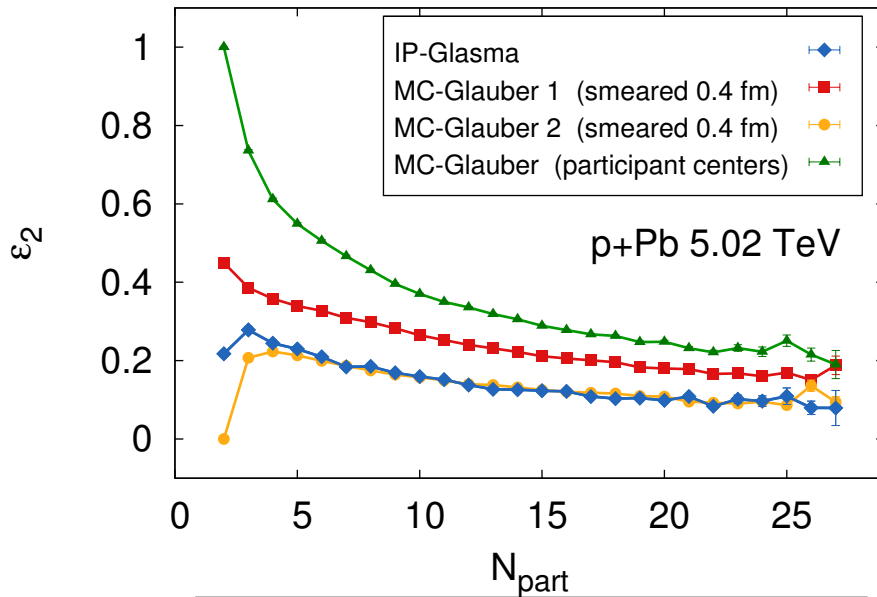


MC-Glauber 2



Initial conditions in p+A: IP-Glasma vs “Glauber”

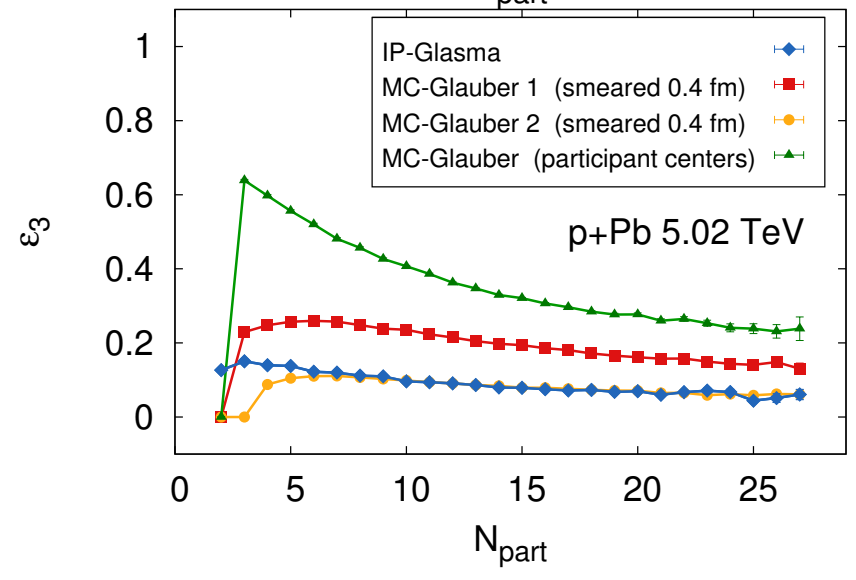
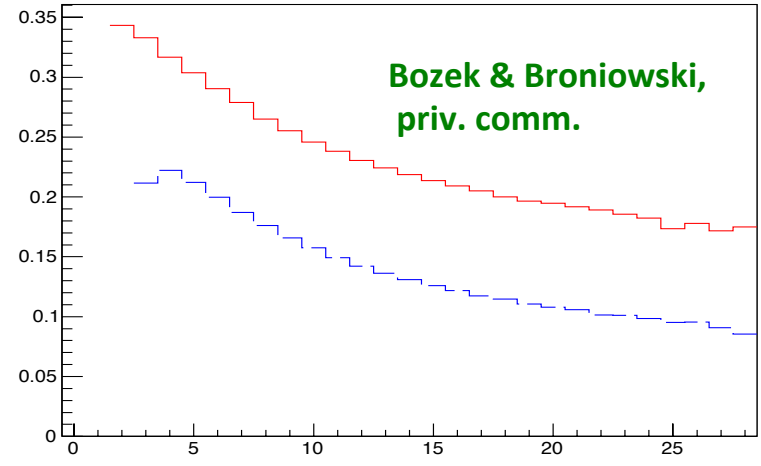
Bzdak, Schenke, Tribedy, RV:1304.3403



MC-Glauber 1

MC-Glauber 2

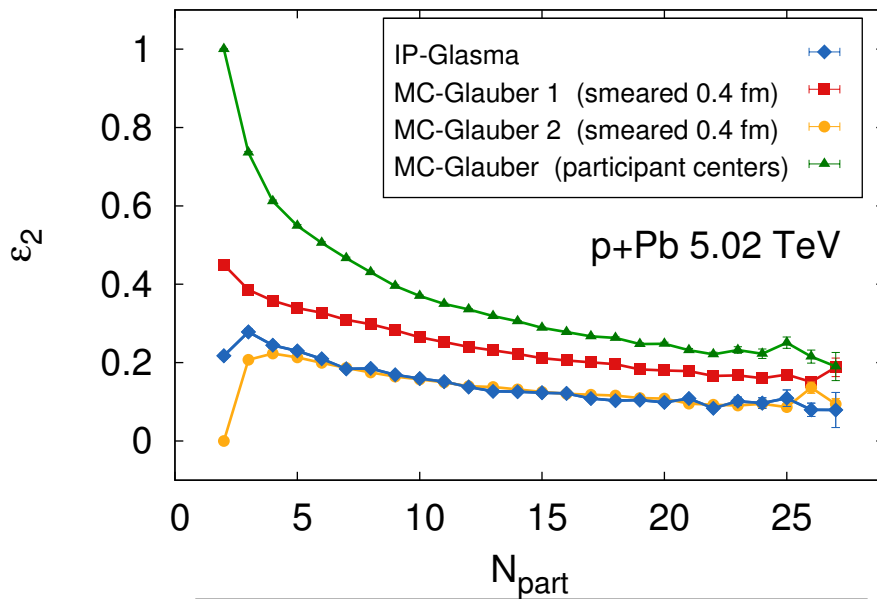
ϵ_2 vs. N_w



In MC Glauber 1, big differences in hard sphere & Gaussian smearing

Initial conditions in p+A: IP-Glasma vs “Glauber”

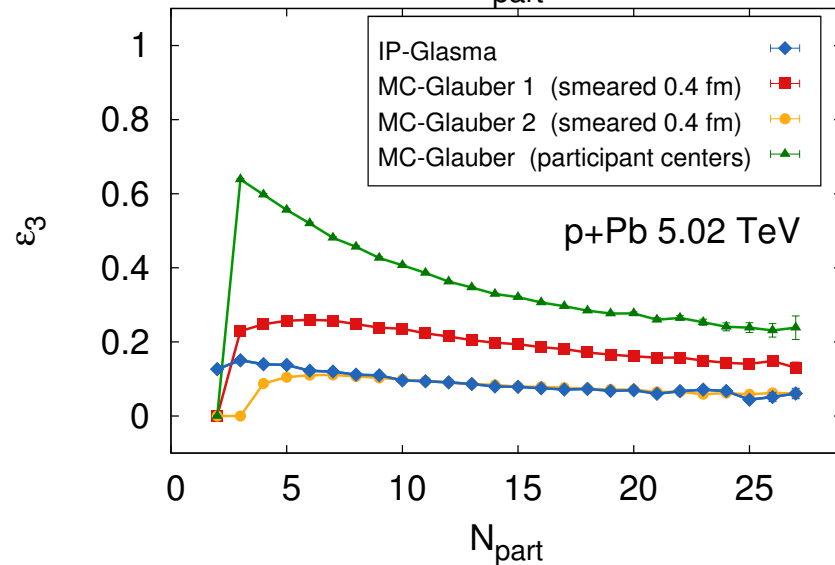
Bzdak,Schenke,Tribedy,RV:1304.3403



MC-Glauber 1



MC-Glauber 2

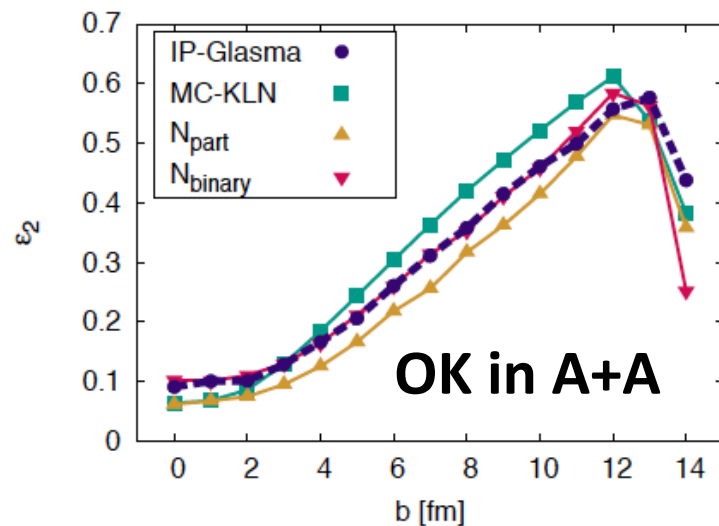
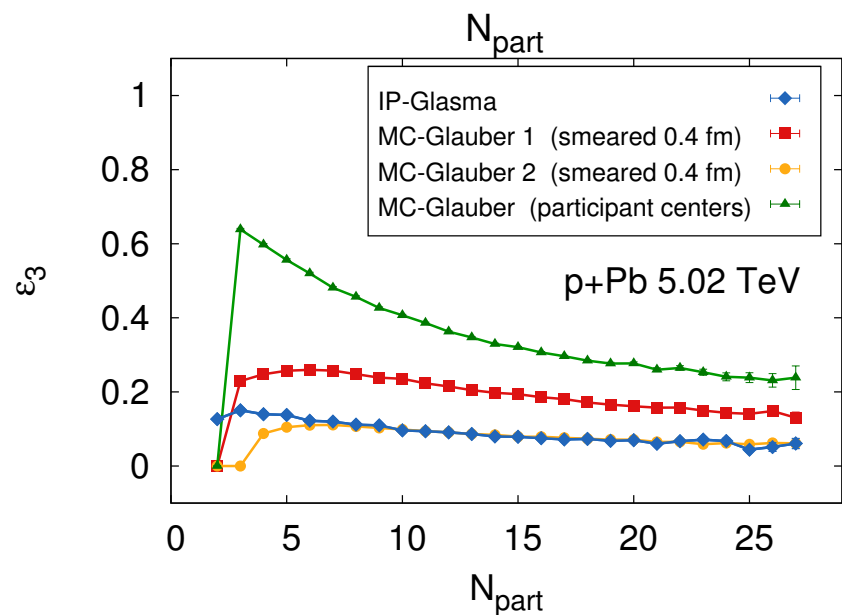
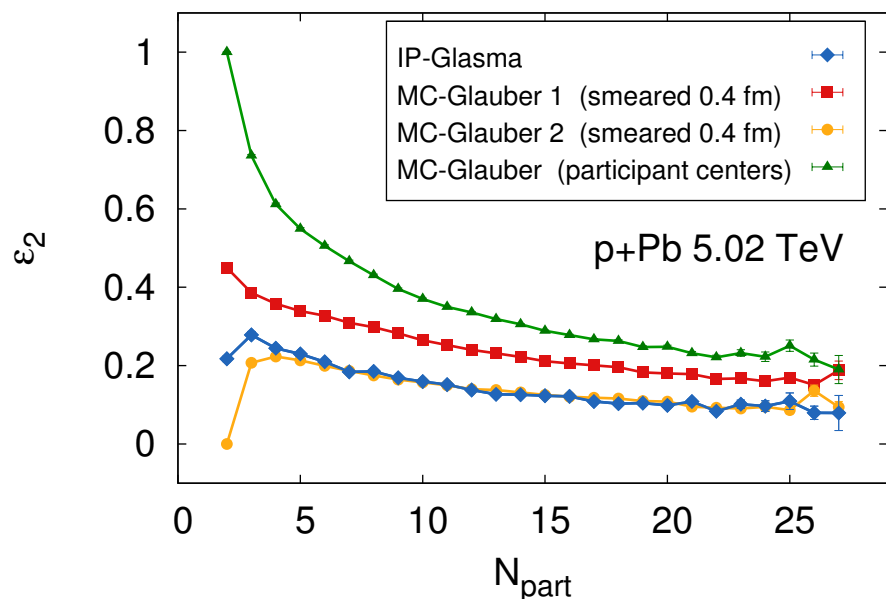


**Lesson: dividing v_2 by ϵ_2
is perilous
for small size systems**

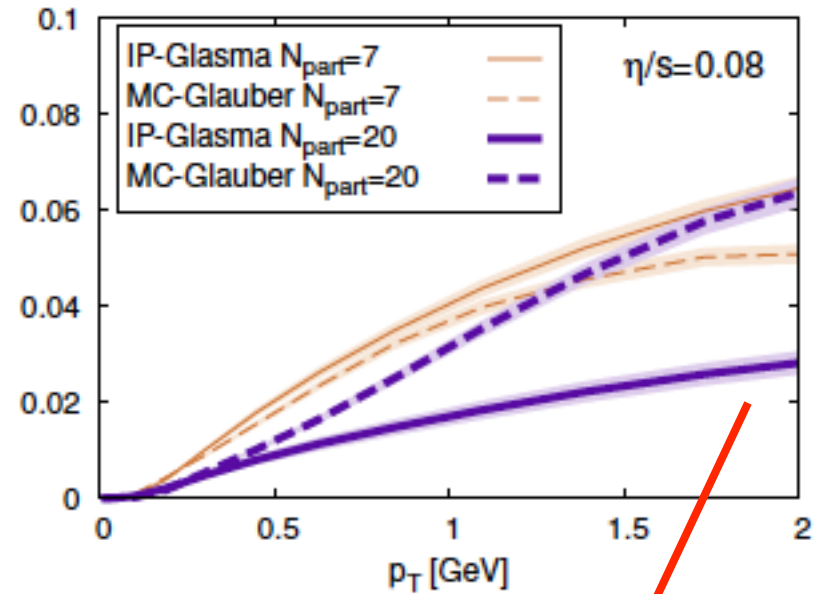
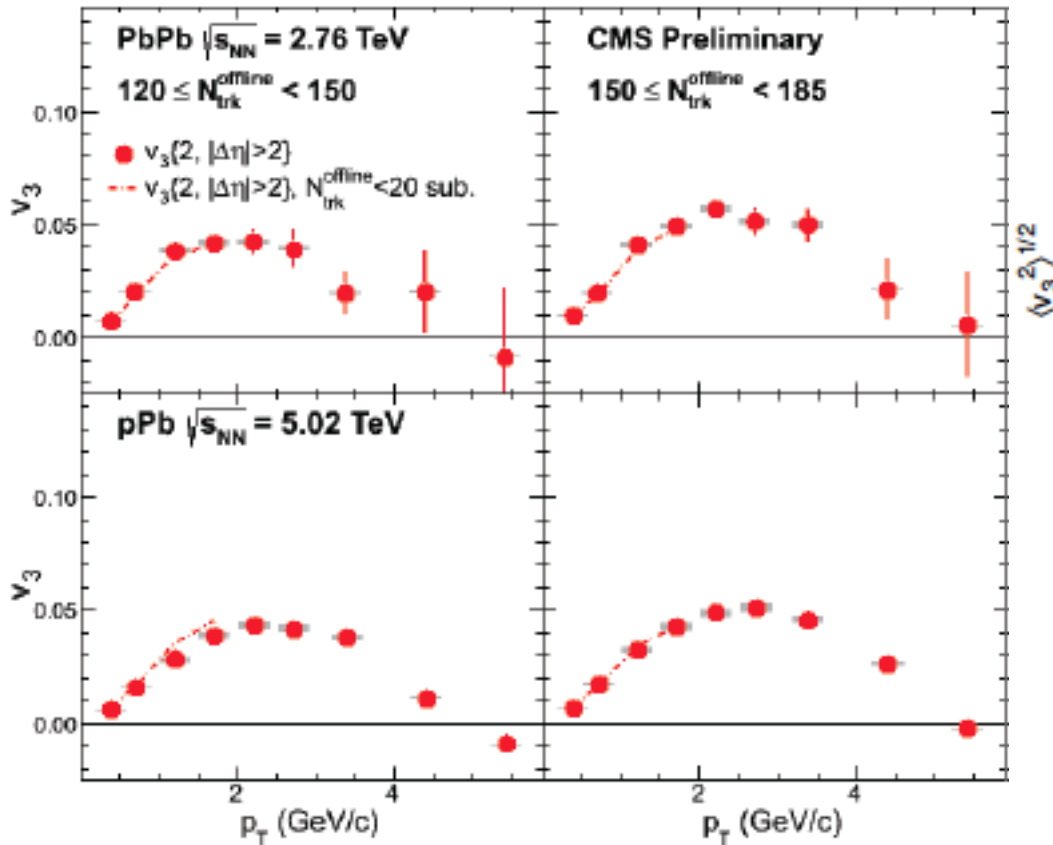
Initial state dynamics matters!

Initial conditions in p+A: IP-Glasma vs “Glauber”

Bzdak, Schenke, Tribedy, RV:1304.3403

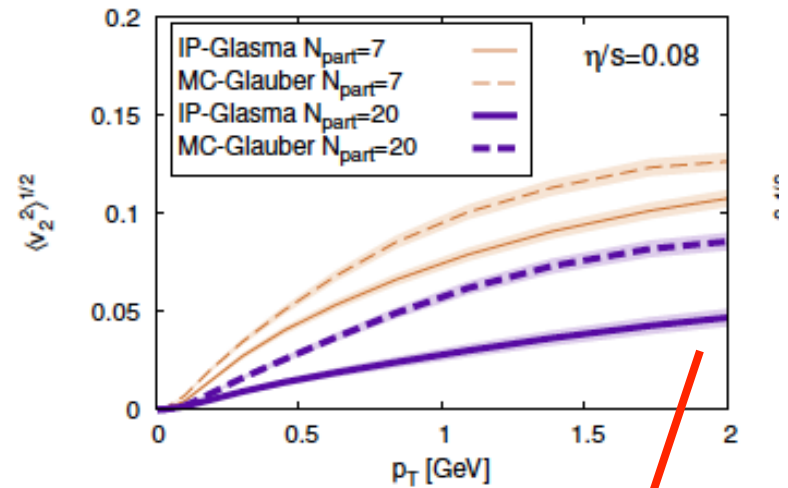
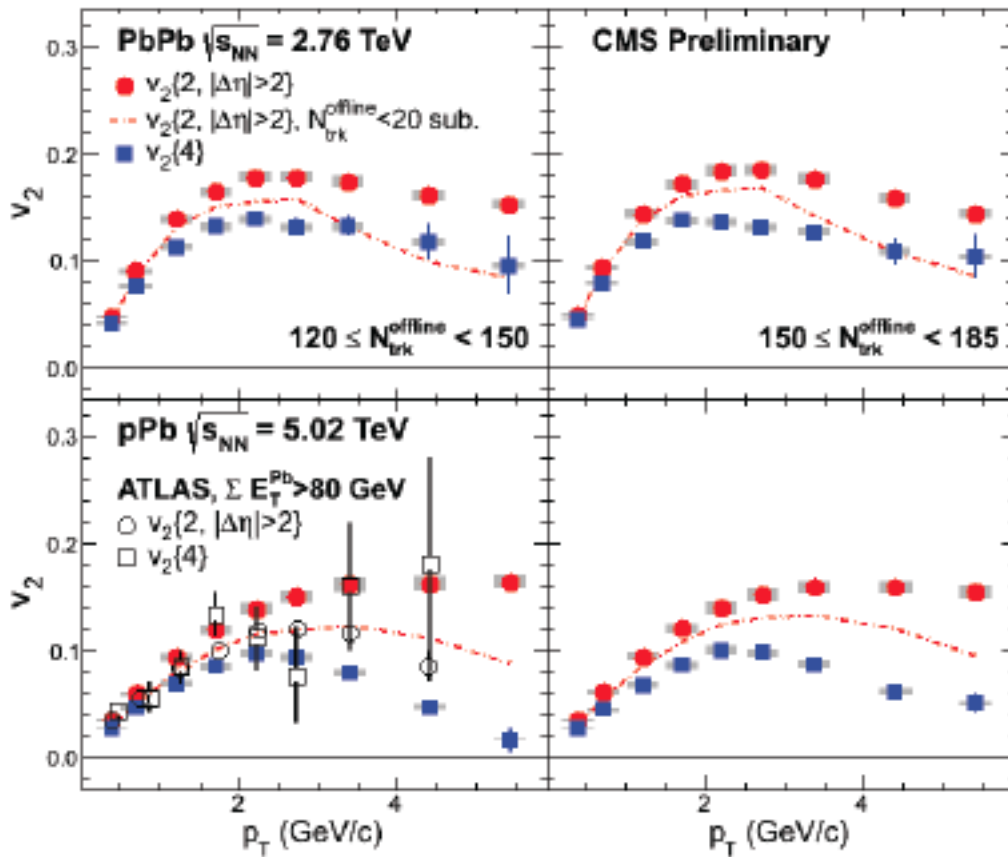


Flow in p+A



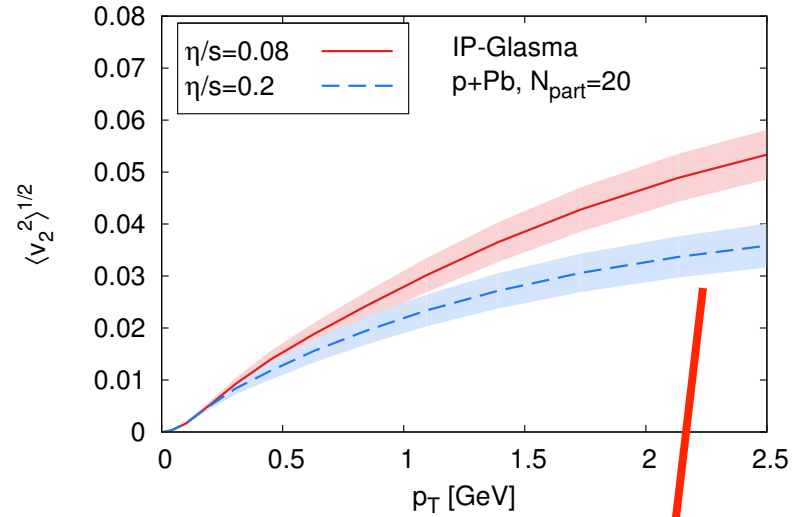
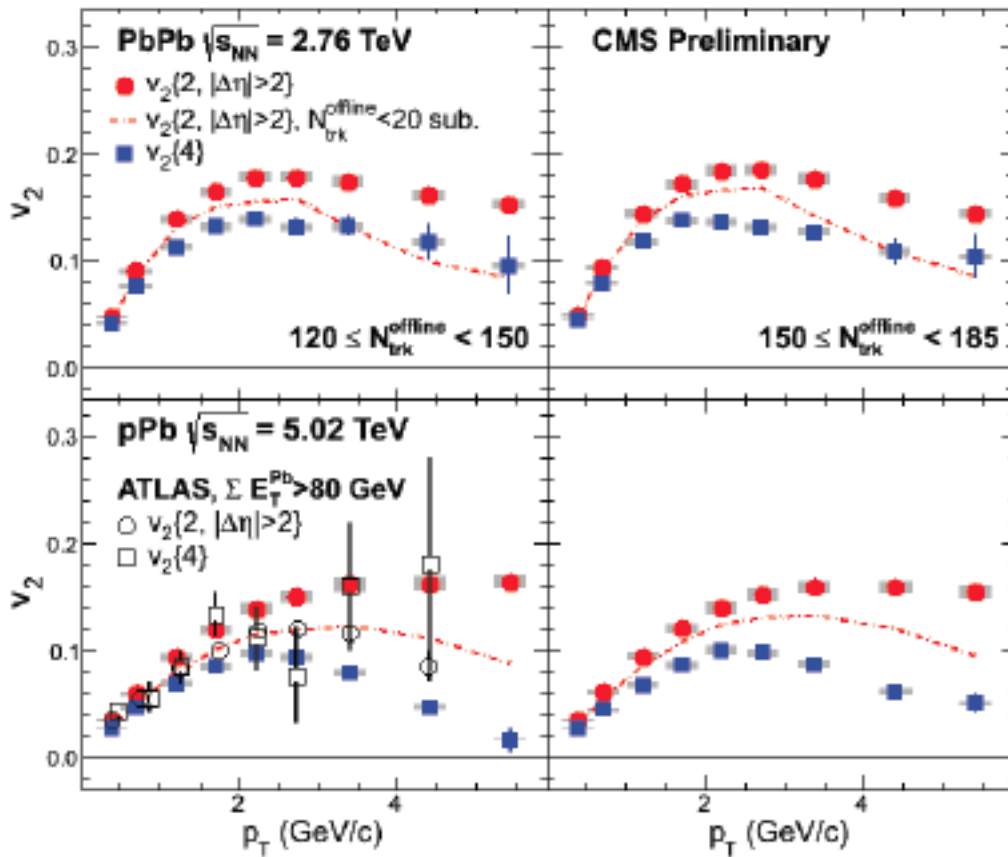
**IP-Glasma result
 2 times smaller than
 data for $\eta/s=0.08$**

Flow in p+A



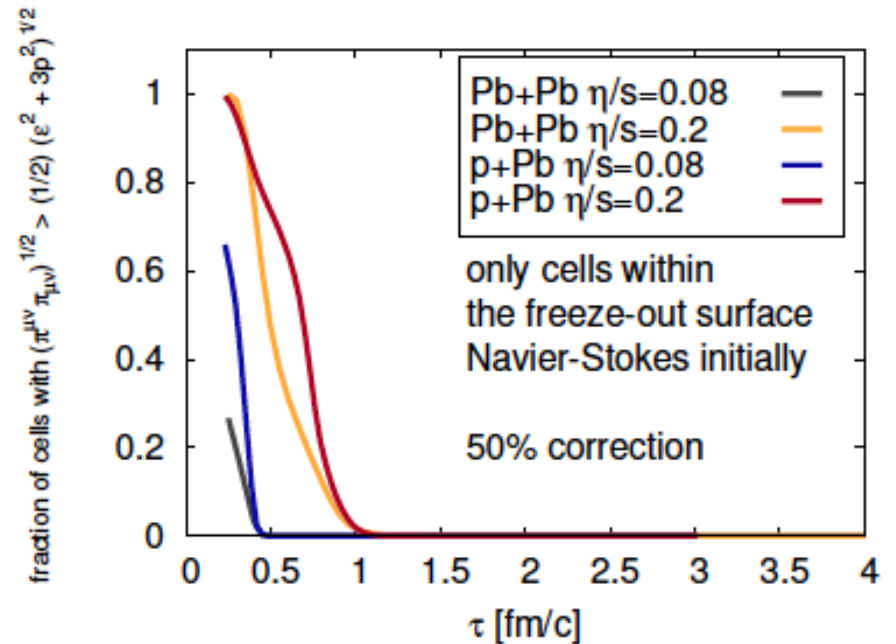
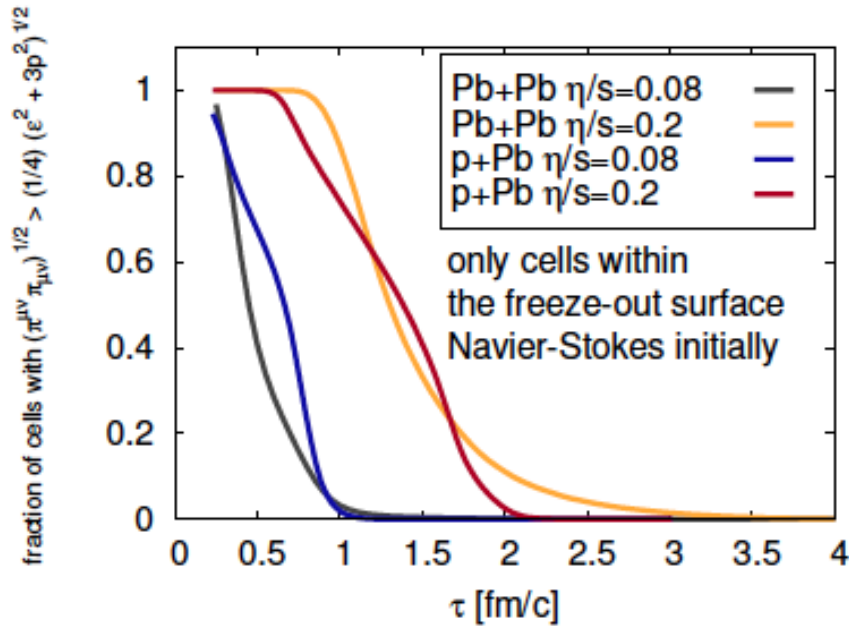
**IP-Glasma result
 2 times smaller than
 data for $\eta/s=0.08$**

Flow in p+A



**IP-Glasma result nearly
3 times smaller than
data for $\eta/s=0.2$**

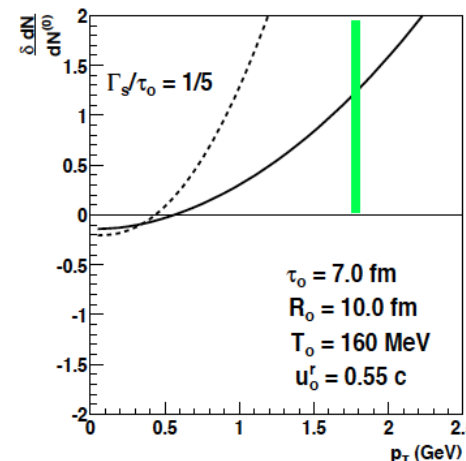
Validity of hydrodynamics for small size systems



◆ Significant viscous corrections at early times for both p+Pb and Pb+Pb but lifetime of Pb+Pb is 5-6 times longer

◆ δf viscous corrections are large in small size systems

$$\frac{\delta N}{N} \propto \frac{\eta}{s} \frac{1}{T\tau_0} \left(\frac{p_T}{T} \right)^2$$



Teaney,
nucl-th/0310099

Conclusions

- ◆ The Glasma framework allows for systematic study of multi-particle production in p+p, p+A and A+A collisions
- ◆ The p+p ridge can be quantitatively understood from gluon saturation enhanced quantum interference
Glasma graphs + BFKL graphs
- ◆ The A+A ridge and v_n moments are quantitatively described in the same framework by
IP-Glasma initial conditions + flow

Conclusions

- ◆ **The p/d+A ridge situation is not completely clear yet**
- but will be clarified soon
- ◆ **2-part corr. data presented thus far**
are described by **Glasma+BFKL dynamics within**
large systematic uncertainties.
Whether v_3 and $v_2\{4\}$ can be generated is under investigation
- ◆ **Flow in p+A is very sensitive to initial conditions.**
In the IP-Glasma framework, v_2 and v_3 are 2-3 times
smaller than data.
A consistent combination of initial and final state dynamics
may be necessary



Annals of Physics

Annals of Physics presents original work in all areas of **basic physics research**. The journal publishes papers on particular topics spanning **theory, methodology, and applications**. Ideas are developed and...

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Editors: V. Gurarie, J. Khoury, J.A. Minahan, R. Venugopalan



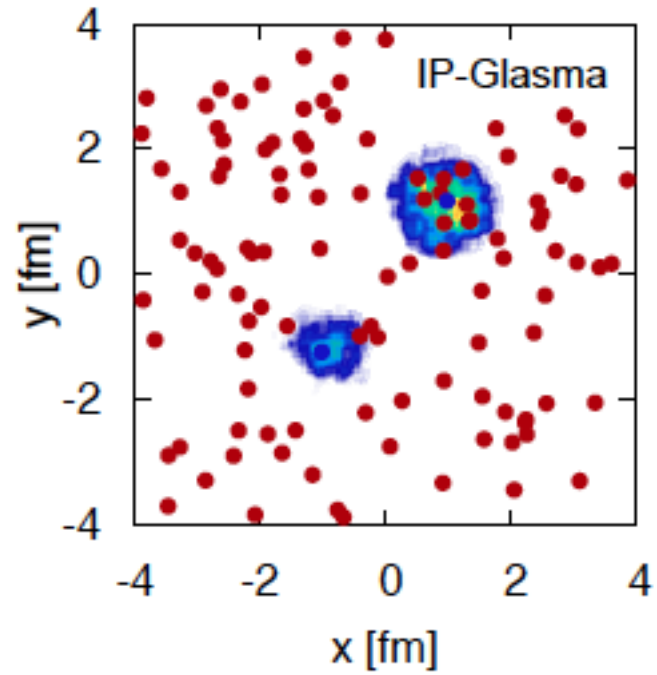
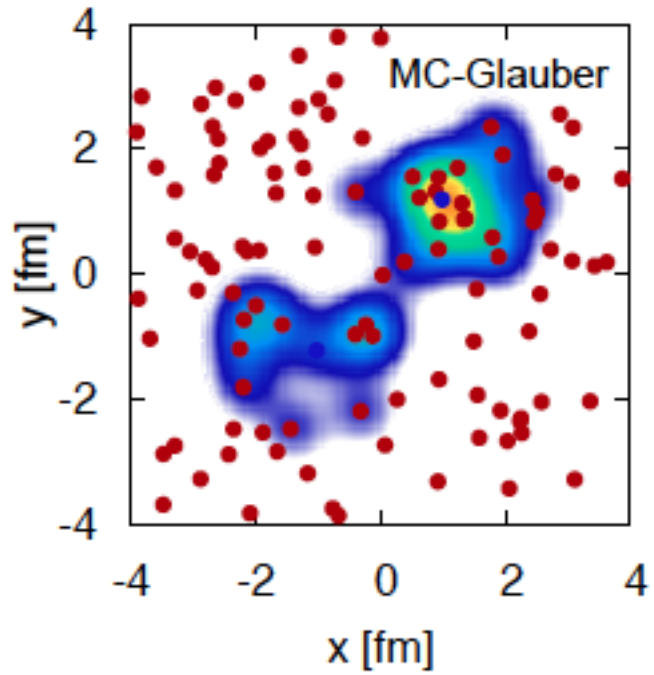
Workshop proceedings will be published as a

Special Issue of Annals of Physics

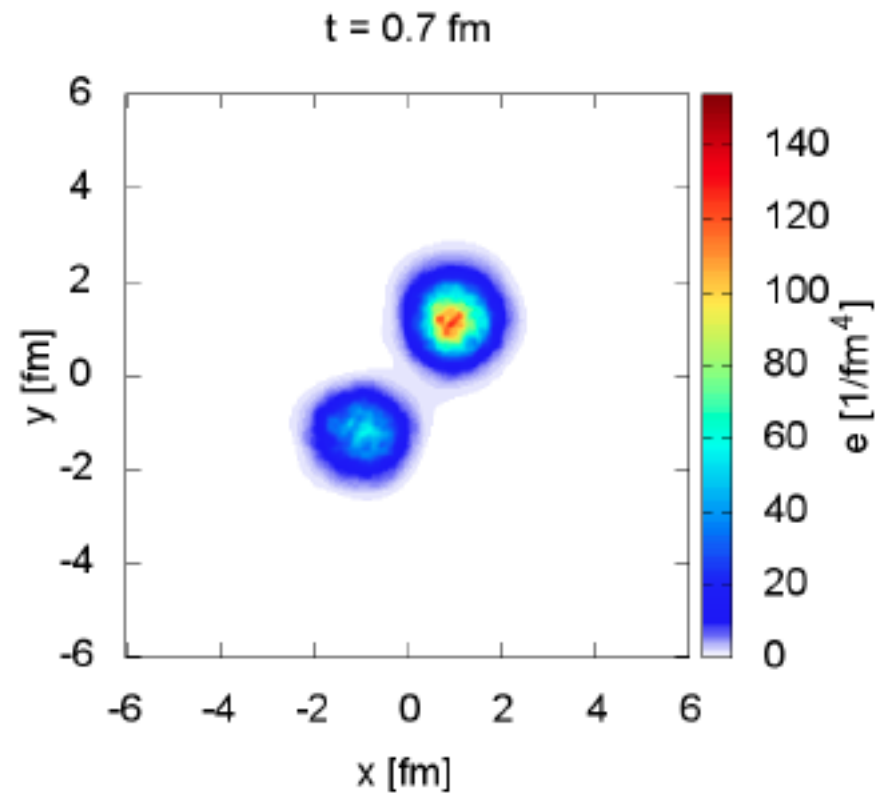
In honor of Prof. Wit Busza's contributions to QCD studies

Guest Editors: the organizers

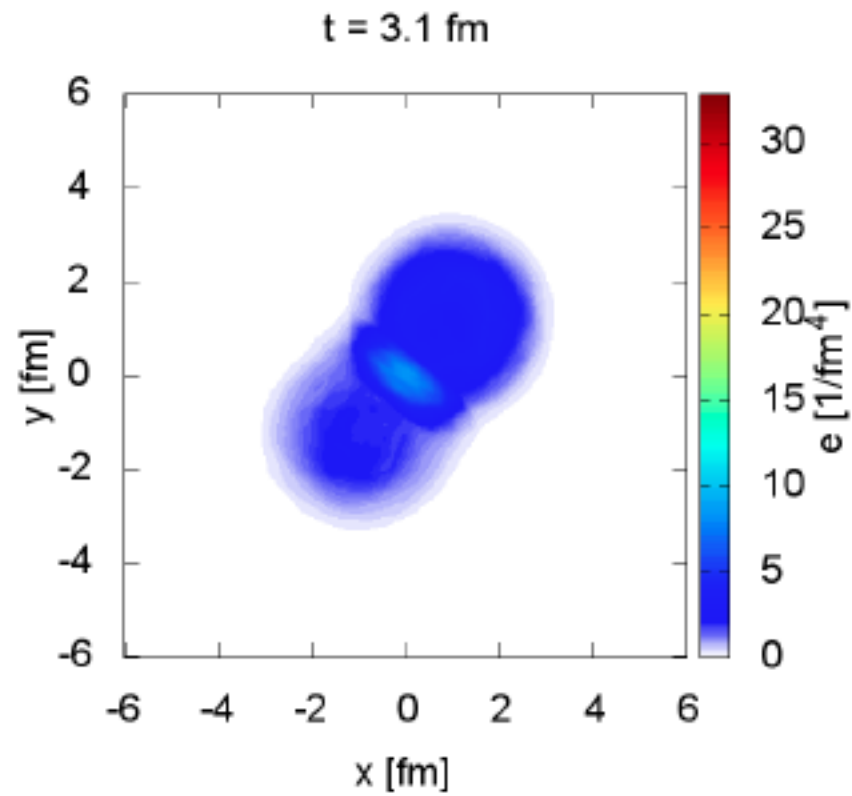
d+Au ridge at RHIC



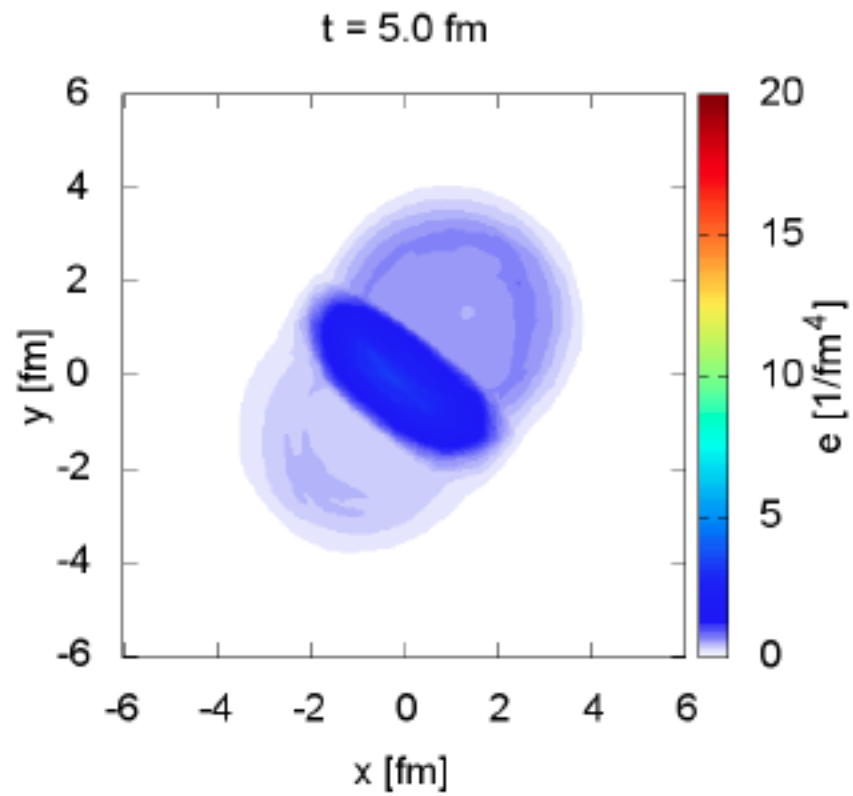
d+Au ridge at RHIC



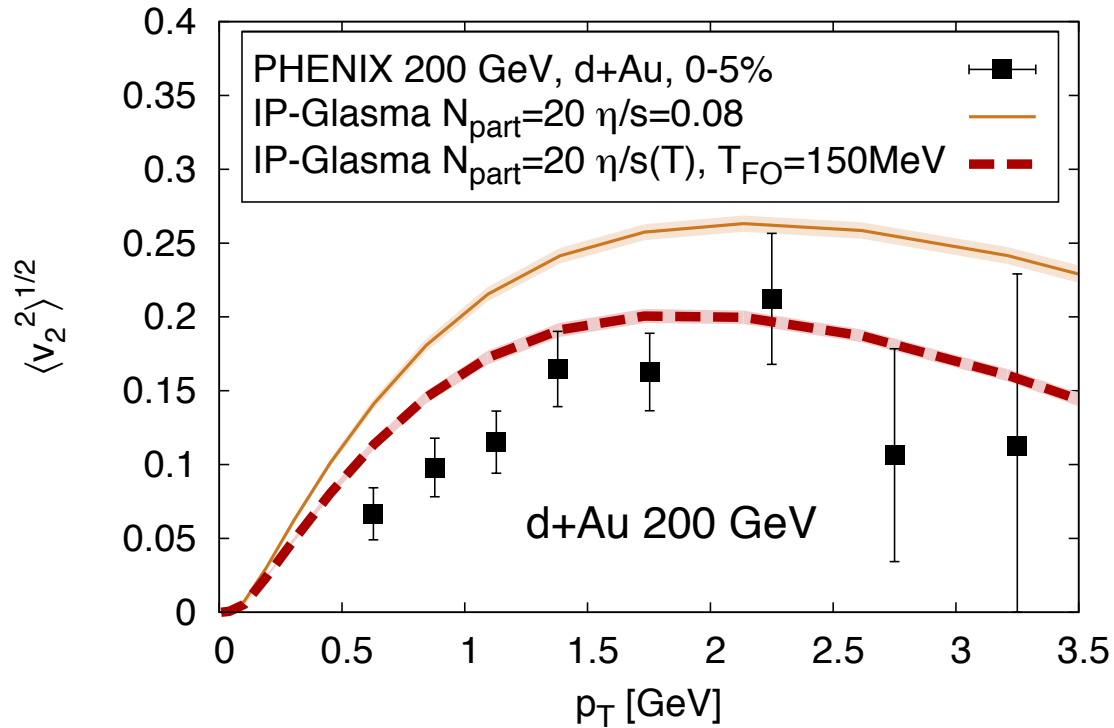
d+Au ridge at RHIC



d+Au ridge at RHIC



d+Au ridge at RHIC

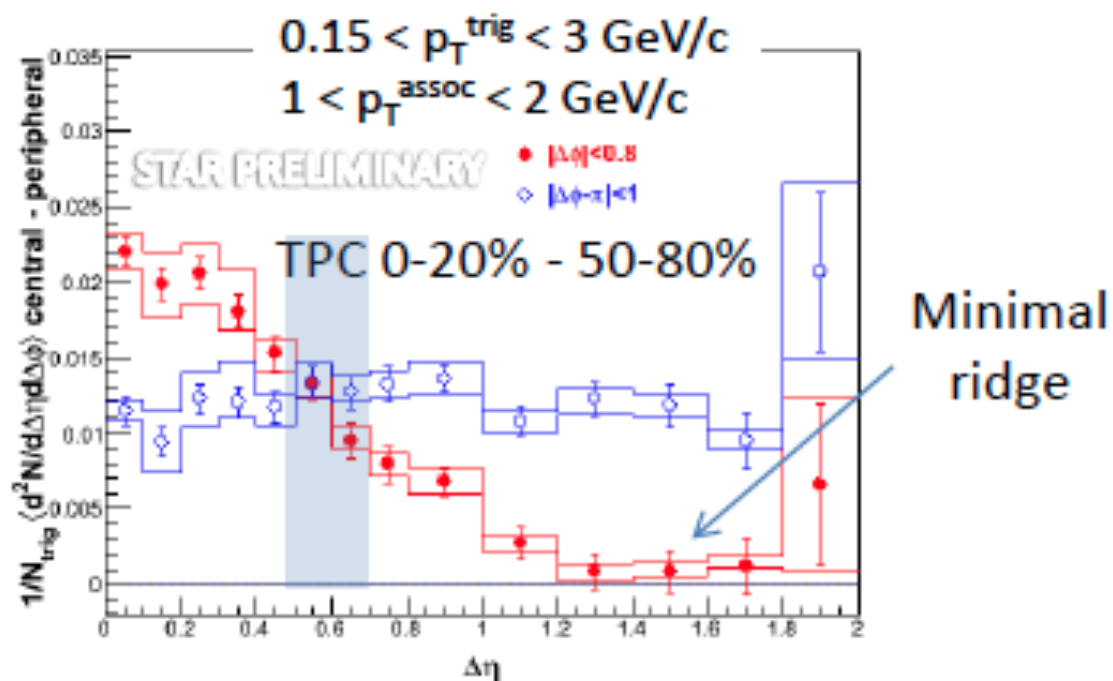


PHENIX, 1303.1794

d+Au ridge at RHIC

But: does a d+Au ridge exist at RHIC ?

Talk by Fuqiang Wang, RBRC workshop, April 15, 2013

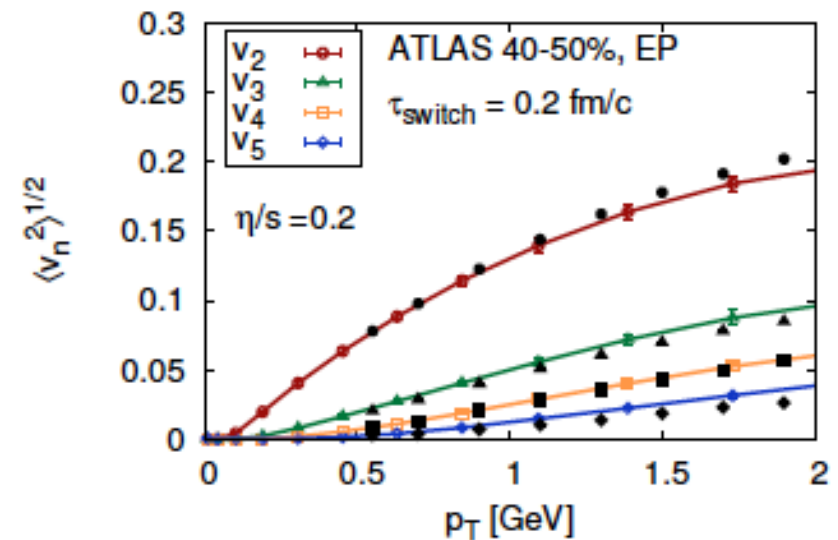
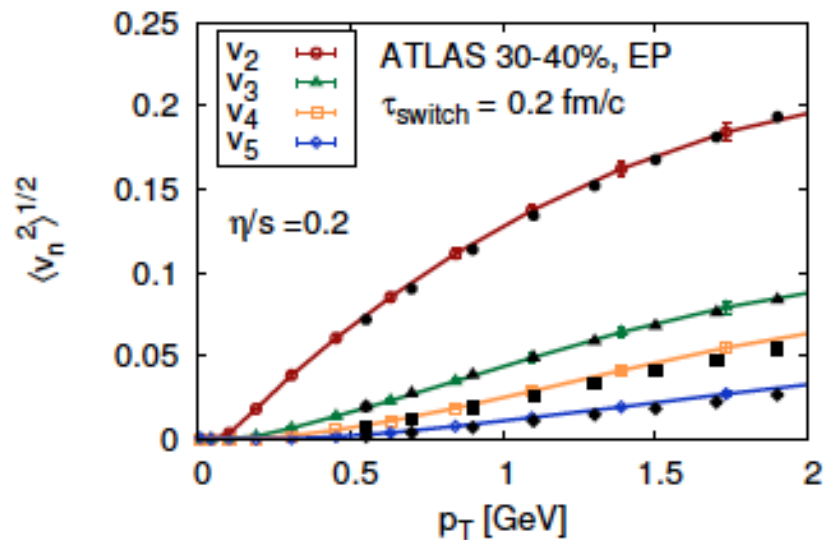
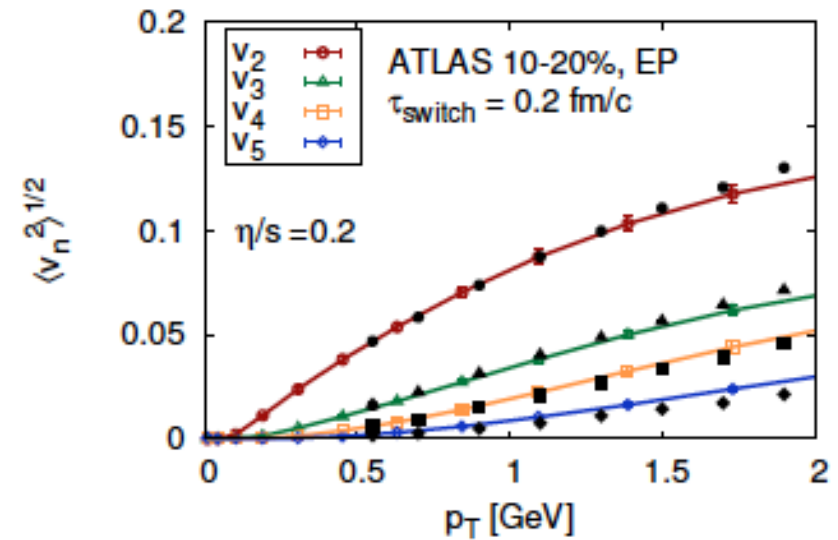
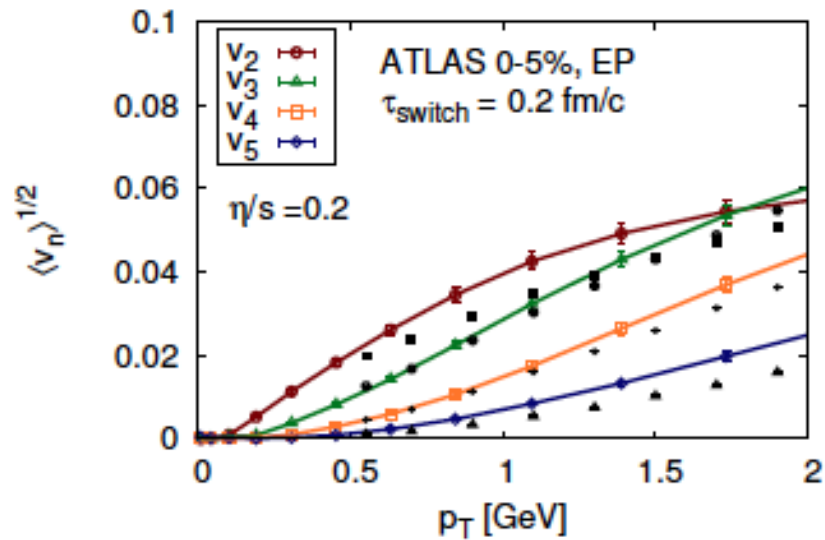


STAR argues nearside ridge goes away with increasing $\Delta\eta$...

Where does this leave the hydro explanation ?

Centrality dependence will be important...

More centrality classes: IP-Glasma + MUSIC



Physics underlying systematics of the ridge

For Glasma graphs

$$d^2 N \propto \int d^2 k_T \Phi_A^2(k_T) \Phi_B(|p_T - k_T|) \Phi_B(|q_T - k_T|)$$

For $|p_T| = |q_T|$, from the Cauchy-Schwarz inequality:

$$\int d^2 k_T \Phi_A^2(k_T) \Phi_B(|p_T - k_T|) \Phi_B(|q_T - k_T|) \leq \int d^2 k_T \Phi_A^2(k_T) \Phi_B^2(|p_T - k_T|)$$

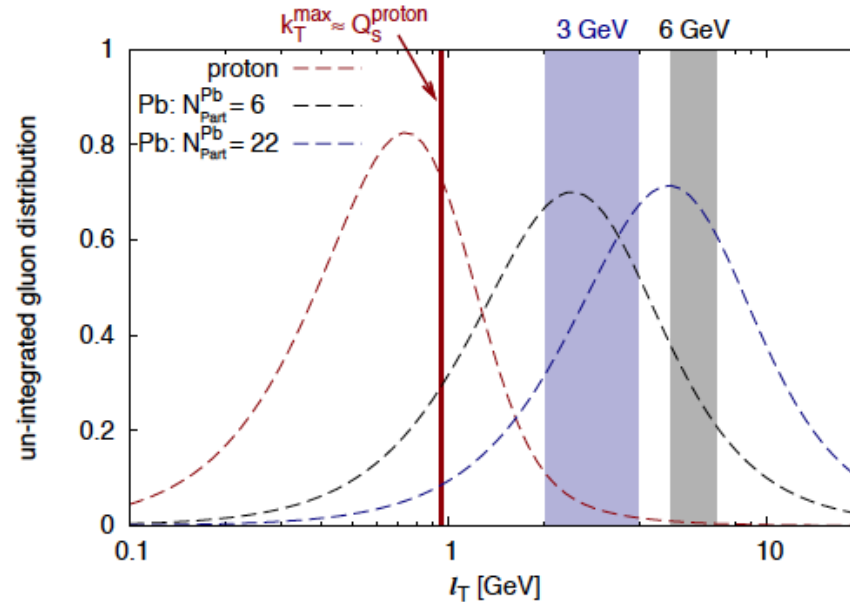
Equality implies no collimation; satisfied only iff $\Phi_B(|p_T - k_T|) \propto \Phi_B(|q_T - k_T|)$

True only if Φ is flat in k_T - for above fns. Else, there must be a collimation

Physics underlying the ridge

Look at ratio of yield at $\Delta\phi_{pq} = 0$ to $\Delta\phi_{pq} = \pi$ for $|p_T| = |q_T|$

$$CY \propto \frac{\int d^2k_T \Phi_A^2(k_T) \Phi_B^2(|p_T - k_T|)}{\int d^2k_T \Phi_A^2(k_T) \Phi_B(|p_T - k_T|) \Phi_B(|p_T + k_T|)}$$

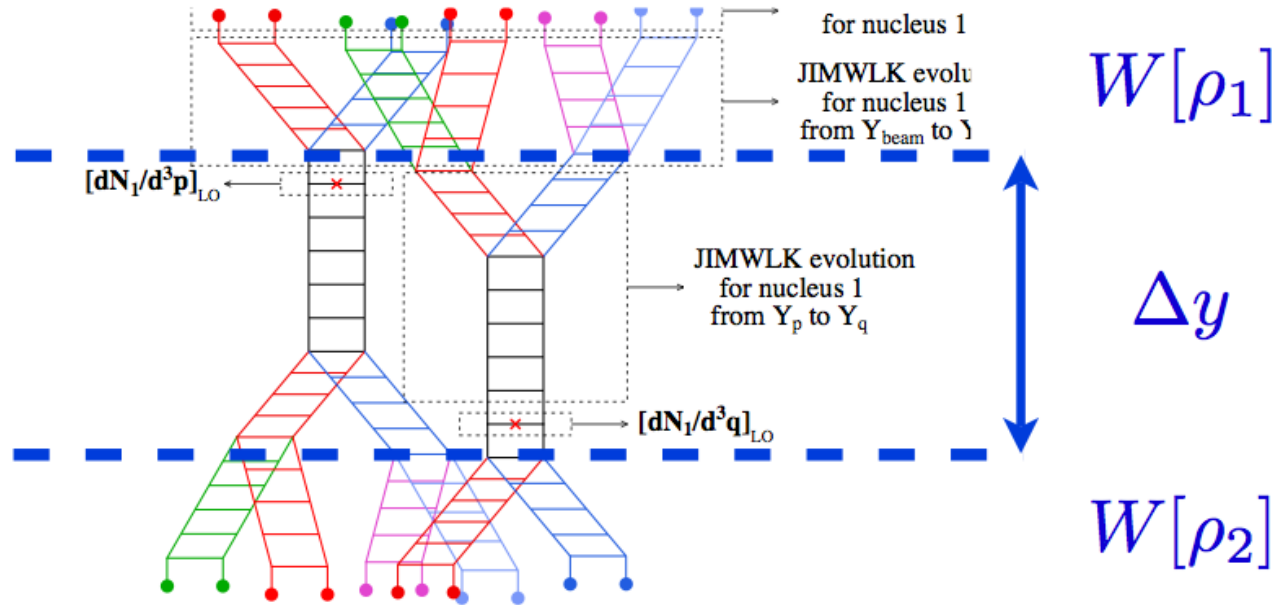


$$CY \propto \frac{\Phi_B(Q_B)}{\Phi_B(\sqrt{2p_T^2 + 2Q_A^2 - Q_B^2})} \propto 1 + \frac{(Q_B - Q_A)^2}{Q_A^2} \sim N_{\text{part}}$$

As seen in the LHC p+Pb data...

Long range di-hadron correlations

Gelis,Lappi,RV (2009)

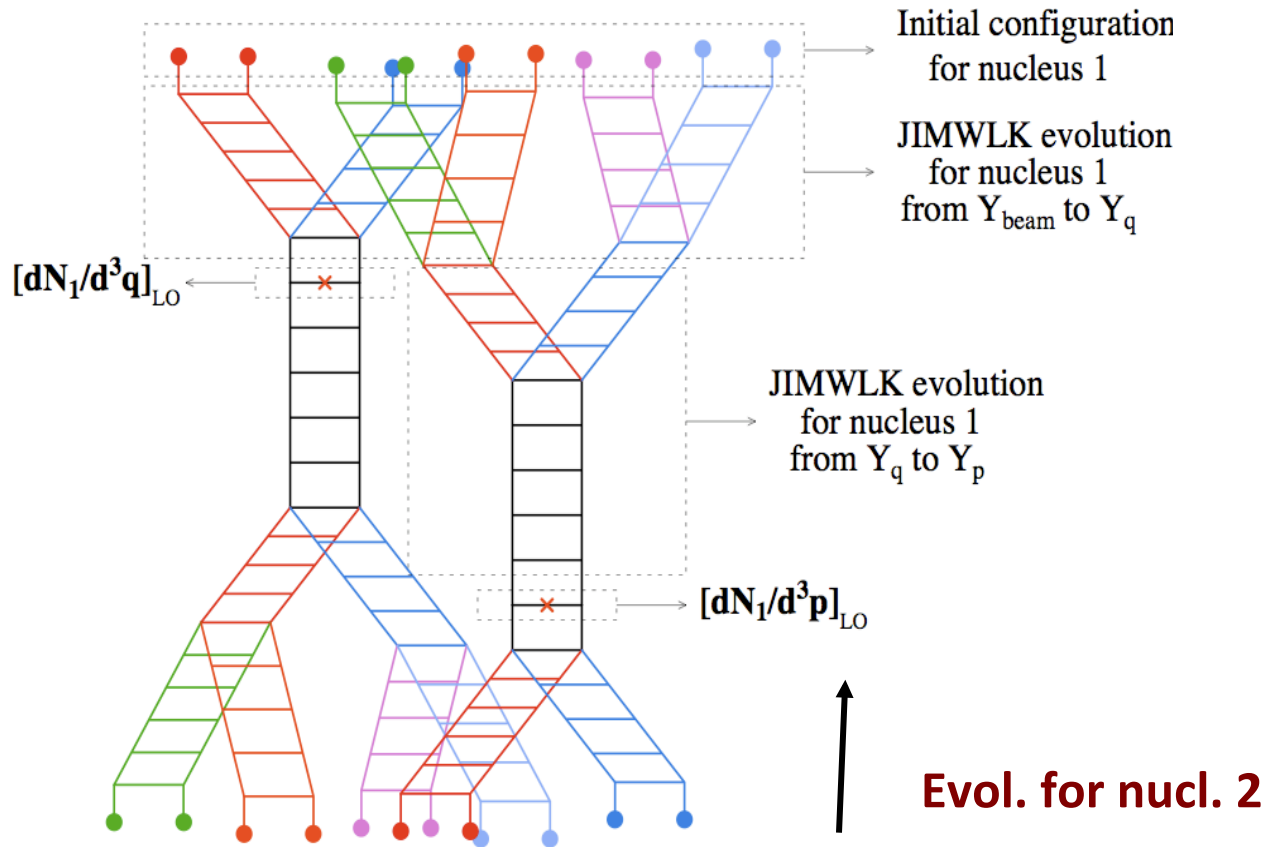


$$\begin{aligned}
 \left\langle \frac{dN_2}{d^2\mathbf{p}_\perp dy_p d^2\mathbf{q}_\perp dy_q} \right\rangle_{\text{LLog}} &= \int [D\rho_1^p(\mathbf{x}_\perp) D\rho_2^p(\mathbf{x}_\perp) D\rho_1^q(\mathbf{x}_\perp) D\rho_2^q(\mathbf{x}_\perp)] \\
 &\times Z_{y_p}[\rho_1^p] G_{y_p, y_q}[\rho_1^p, \rho_1^q] Z_{y_q}[\rho_2^q] G_{y_q, y_p}[\rho_2^q, \rho_2^p] \\
 &\times \left. \frac{dN_1[\rho_1^p, \rho_2^p]}{d^2\mathbf{p}_\perp dy_p} \right|_{\text{LO}} \left. \frac{dN_1[\rho_1^q, \rho_2^q]}{d^2\mathbf{q}_\perp dy_q} \right|_{\text{LO}} .
 \end{aligned}$$

Simplify using “Gaussian truncation” approximation to JIMWLK

Dusling,Gelis,Lappi,RV:0911.2720

High multiplicity events: two particle correlations



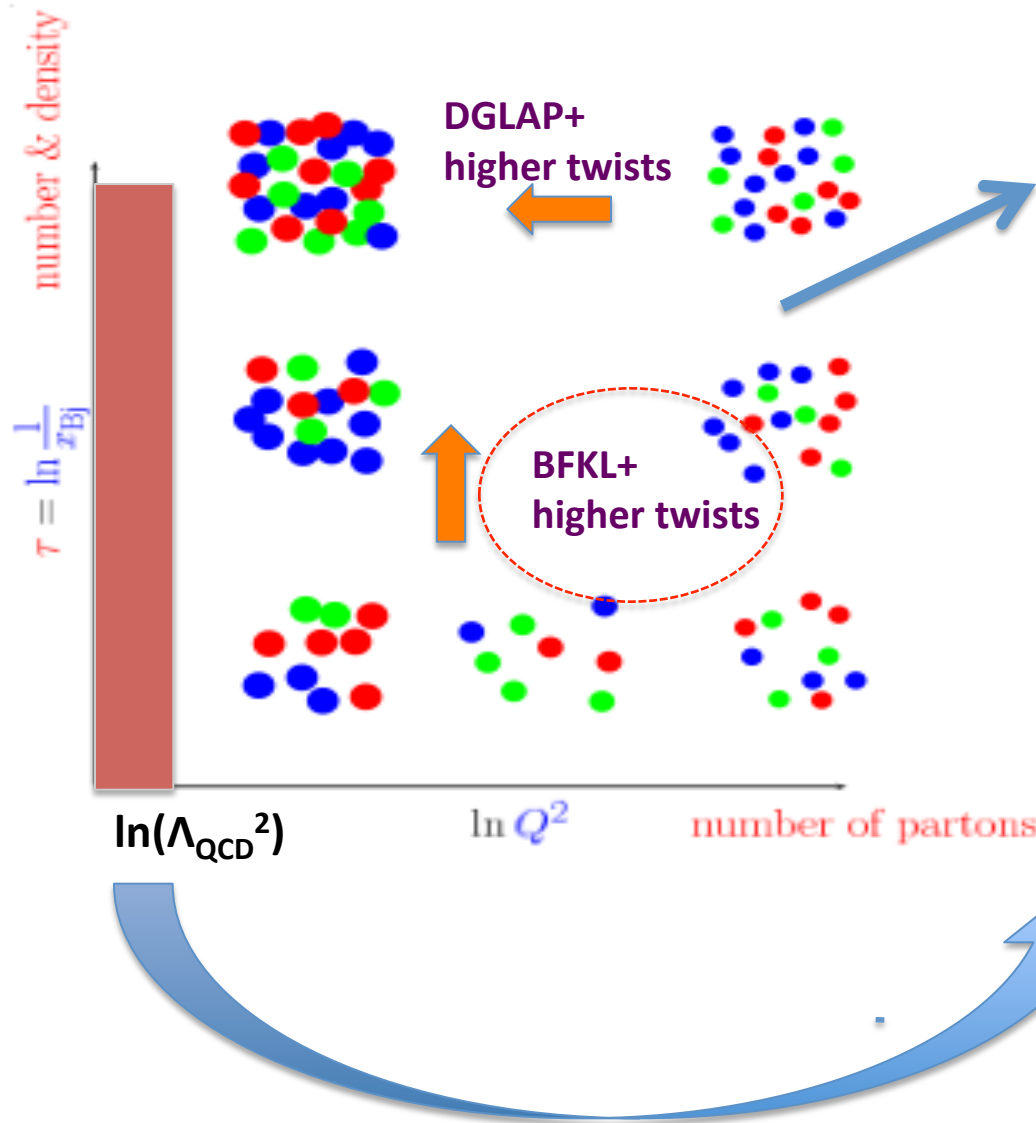
Gelis,Lappi,RV
[arXiv:0804.2630 \[hep-ph\]](https://arxiv.org/abs/0804.2630);
[arXiv:0807.1306 \[hep-ph\]](https://arxiv.org/abs/0807.1306)
[arXiv:0810.4829 \[hep-ph\]](https://arxiv.org/abs/0810.4829)

◆ Full YM+JIMWLK evolution – not available yet Lappi,Schenke,RV in progress

◆ Approximations: BK Gaussian truncation approximation for $k_T \geq Q_s$; YM results for MV model available for all k_T

Dusling,Gelis,Lappi,RV:0911.2720; Lappi,Srednyak,RV:0911.2068; Kovchegov,Wertepny: 1212.1195

Many-body dynamics of universal gluonic matter



How does this happen ? What are the right degrees of freedom ?

How do correlation functions of these evolve ?

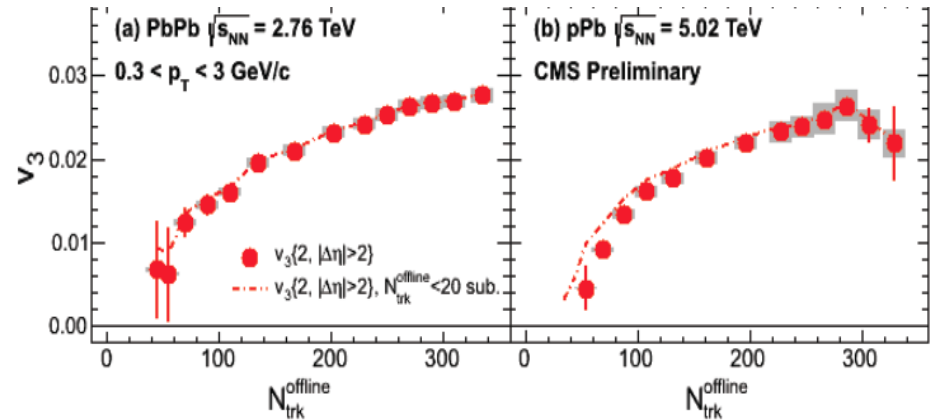
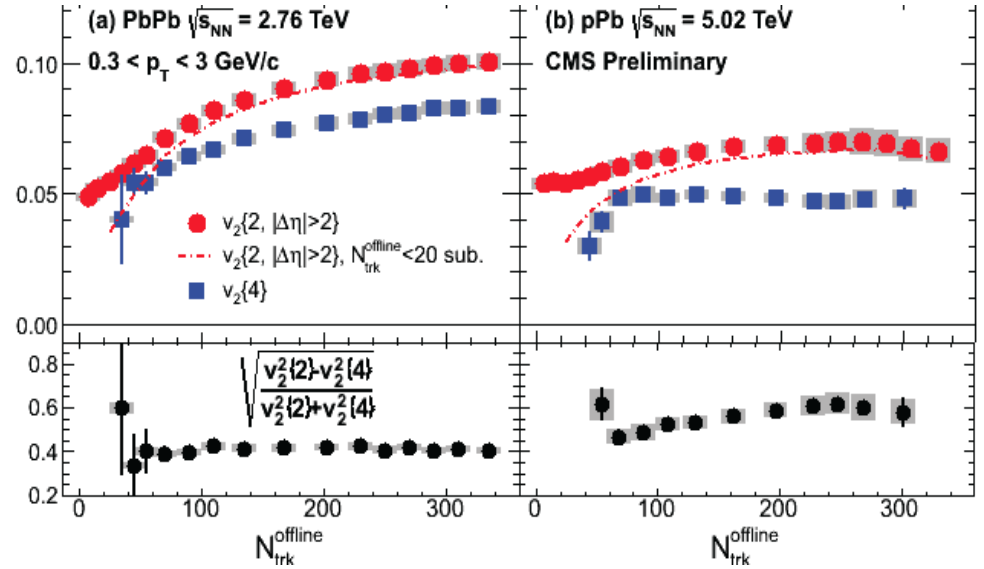
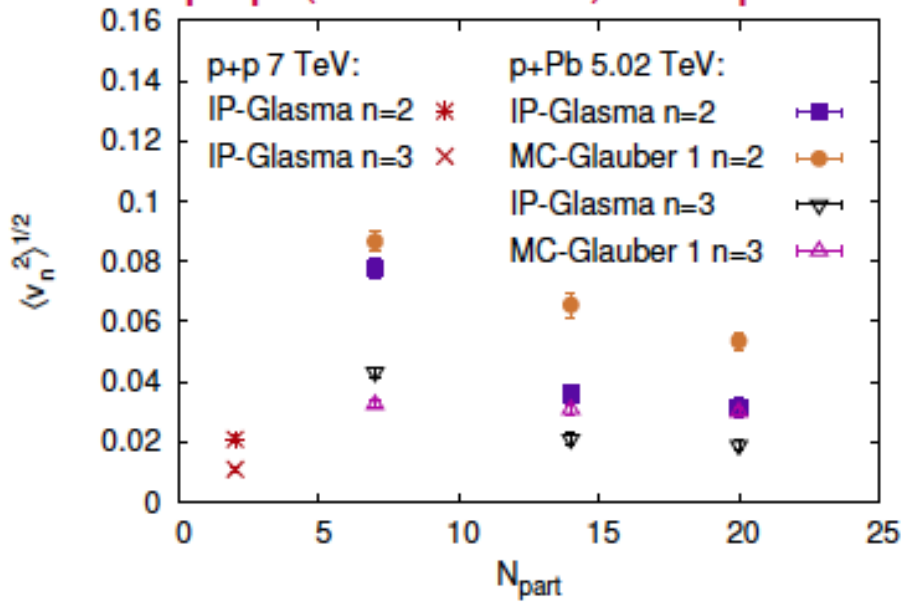
Is there a universal fixed point for the RG evolution of d.o.f

Does the coupling run with Q_s^2 ?

How does saturation transition to chiral symmetry breaking and confinement

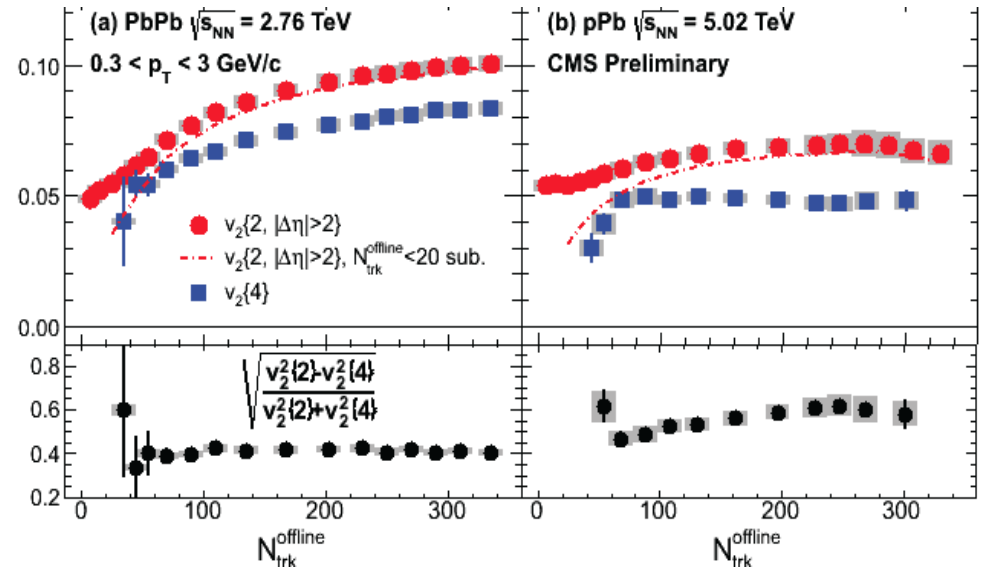
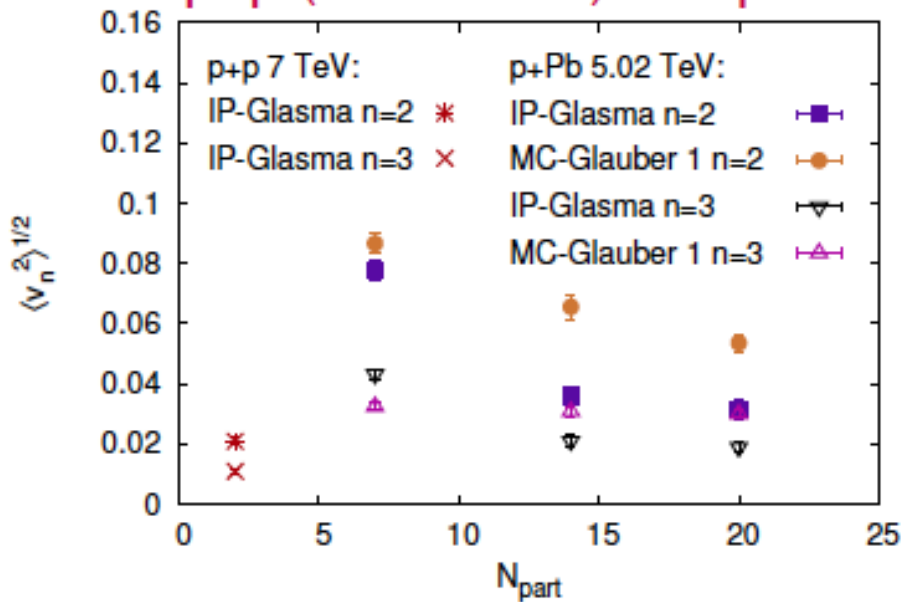
Flow in p+A

p+p (at $b = 0$ fm) and p+Pb



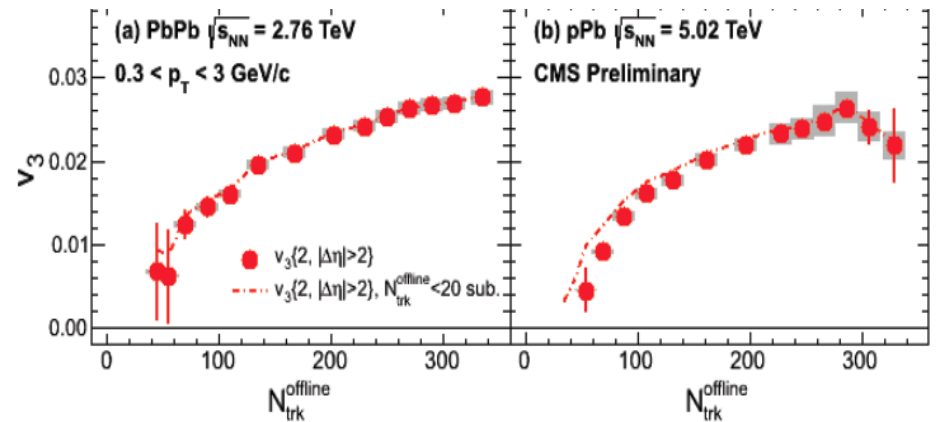
Flow in p+A

p+p (at $b = 0$ fm) and p+Pb



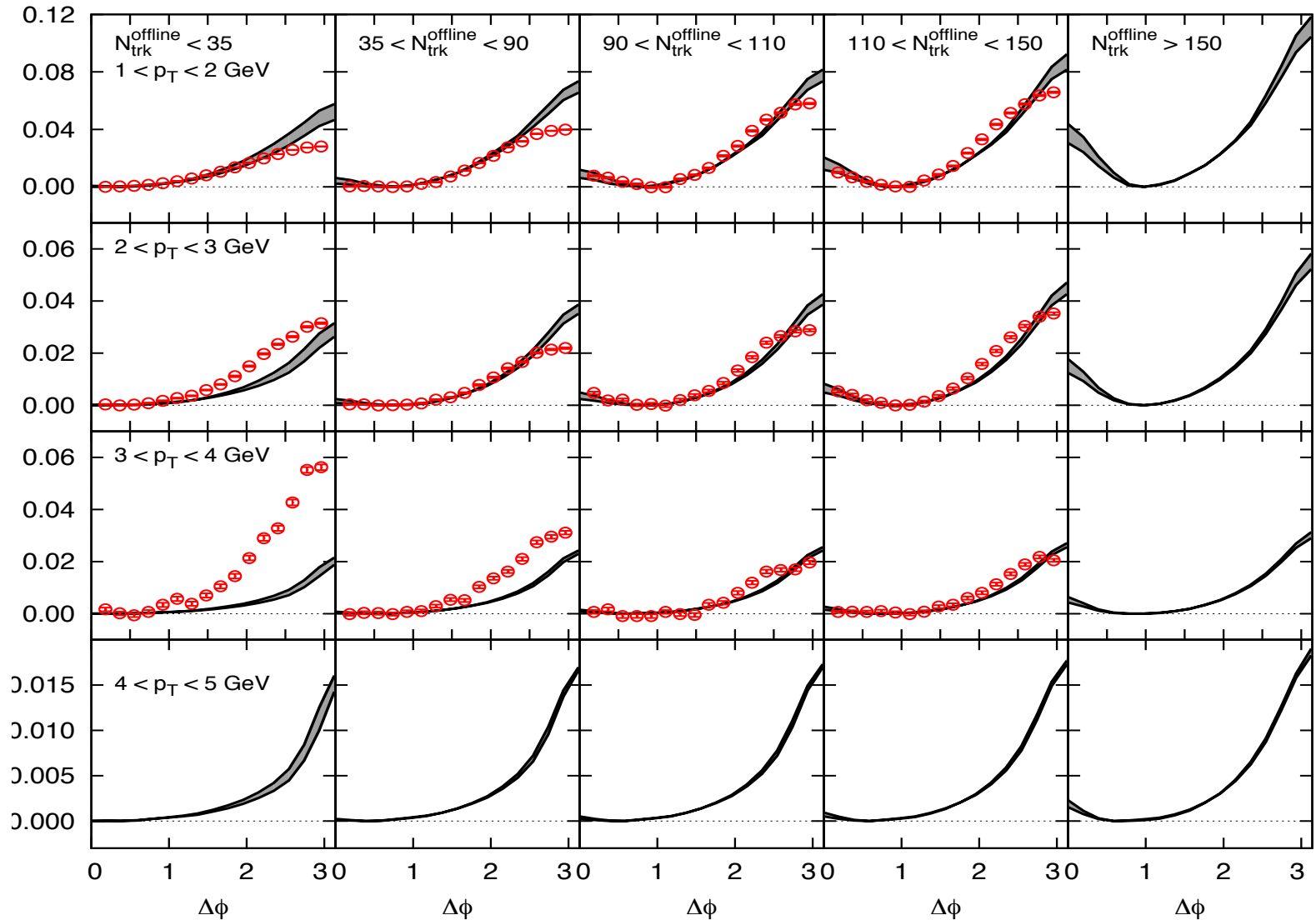
Convert IP-Glasma result to N_{trk} to make direct comparison

Note: result is for $\eta/s=0.08$



CMS data: JHEP 1009, 091 (2010); PLB 718, 795 (2013)

Assoc. yield
per. trig.



$K_{\text{BFKL}} = K_{\text{Glasma}} = 1$
KKP fragmentation

Dusling, RV, PRD 87, 051502 (R) (2013); arXiv:1302.7018, PRD in press