

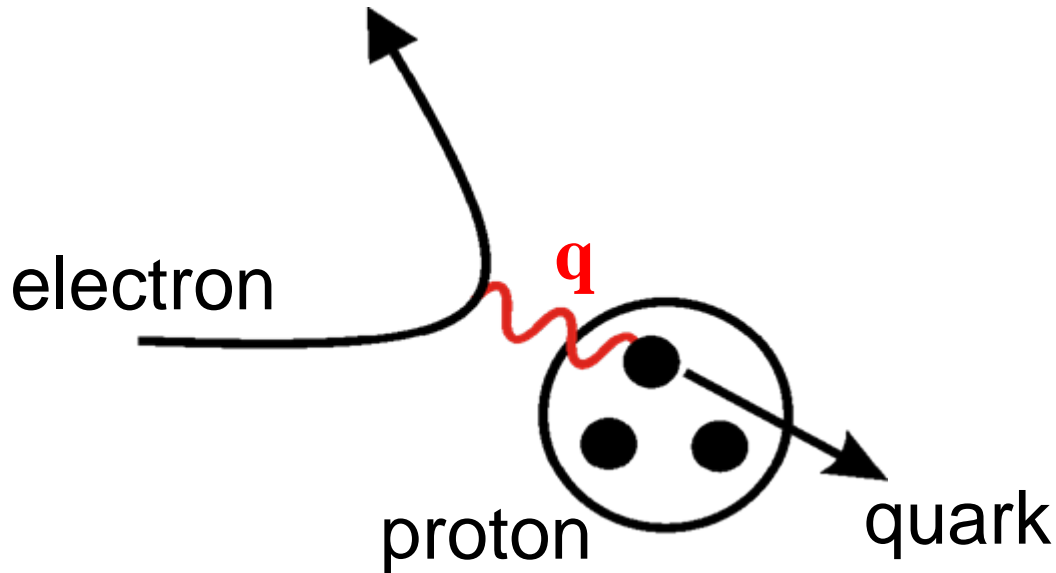
# Impact of HERA on QCD and proton structure

Alan Martin (Durham)

HERA Fest

June 29, 2007

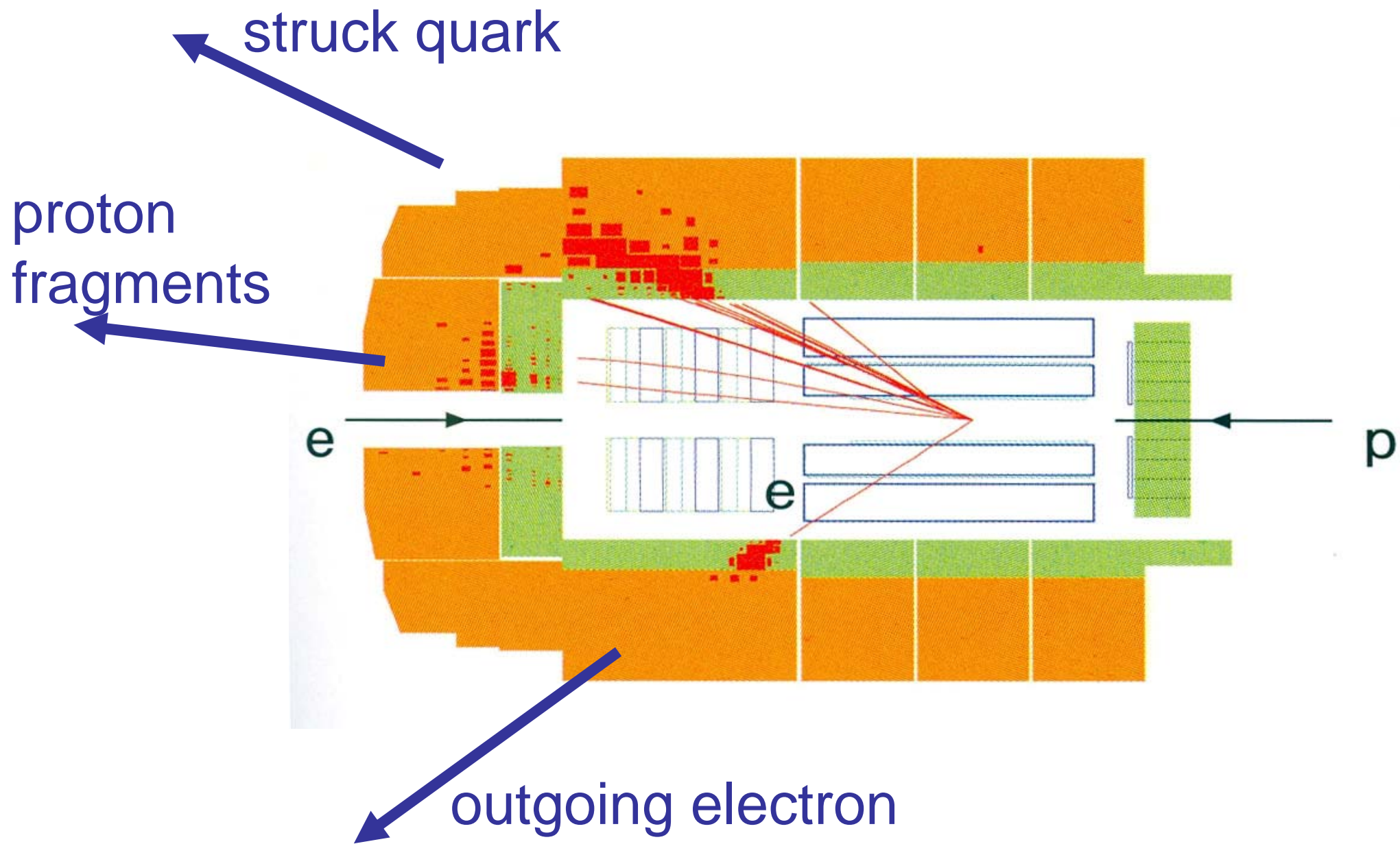
HERA: electron  $\rightarrow$   $\leftarrow$  proton



quark acts as if free,  
yet never seen ?  
big puzzle  $\sim 1970$   
 $\rightarrow$  QCD

virtual photon  $\text{wavy } q$   $Q^2 \equiv -q^2,$   $\lambda = 1/Q$

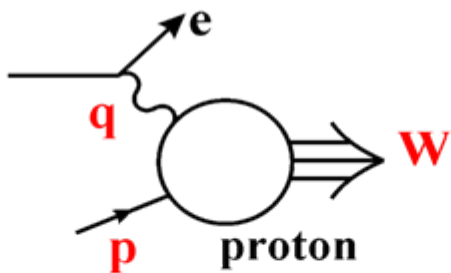
(real particle:  $p^2 = E^2 - \vec{p}^2 = M^2$ )



$$W^2 = (p+q)^2$$

$$= M^2 + 2p \cdot q + q^2$$

$$(Q^2 \equiv -q^2)$$



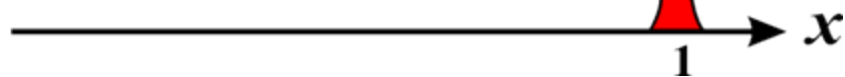
$$\lambda \gg R$$

$$Q^2 R^2 \ll 1$$

elastic  
e-proton  
scatt.

elastic  
W=M

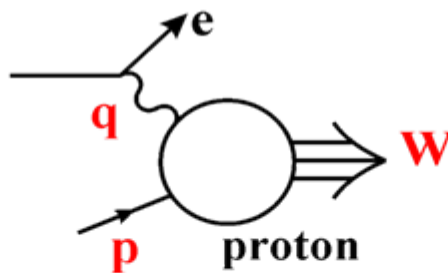
$$x \equiv \frac{Q^2}{2p \cdot q} = 1$$



$$W^2 = (p+q)^2$$

$$= M^2 + 2p \cdot q + q^2$$

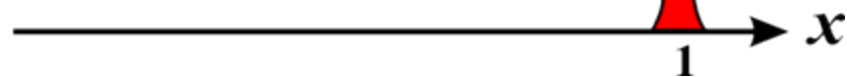
$$(Q^2 \equiv -q^2)$$



$$\lambda \gg R$$

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elastic  
e-proton  
scatt.



elastic  
 $W=M$

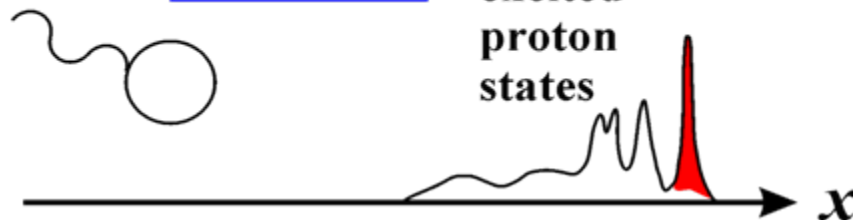
$$x \equiv \frac{Q^2}{2p \cdot q} = 1$$

excit<sup>ns</sup>  
 $W > M$

$$x < 1$$

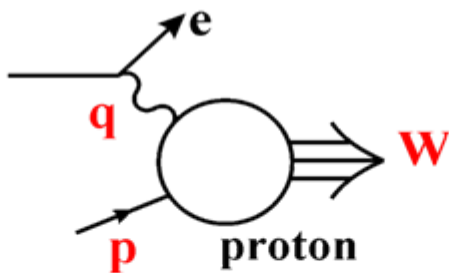
$$Q^2 R^2 \sim 1$$

excited  
proton  
states



$$W^2 = (p+q)^2 = M^2 + 2p \cdot q + q^2$$

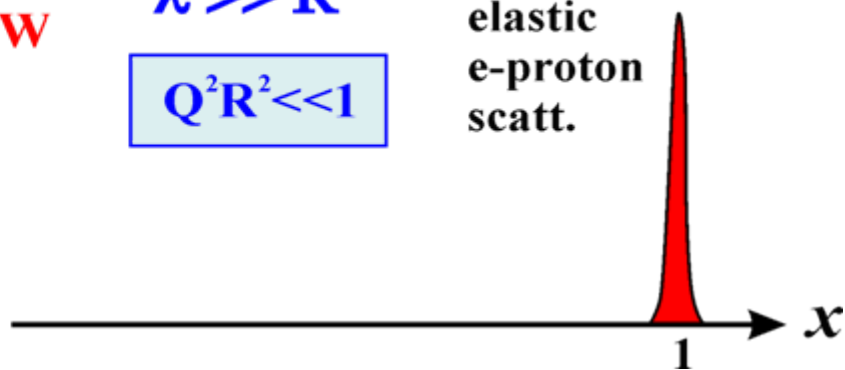
$(Q^2 \equiv -q^2)$



$$\lambda \gg R$$

$$Q^2 R^2 \ll 1$$

elastic  
e-proton  
scatt.



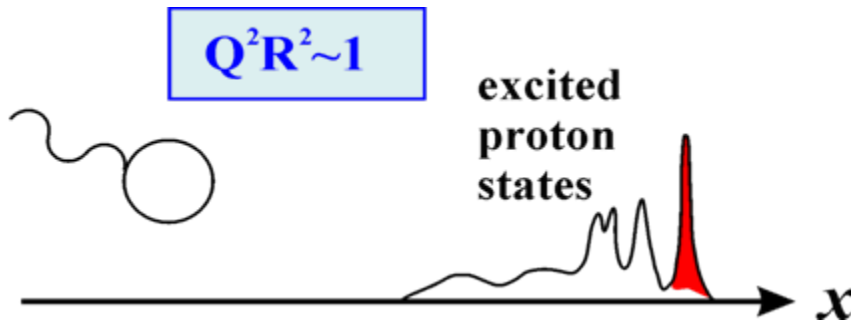
elastic  
 $W=M$

$$x \equiv \frac{Q^2}{2p \cdot q} = 1$$

excit<sup>ns</sup>  
 $W > M$

$$x < 1$$

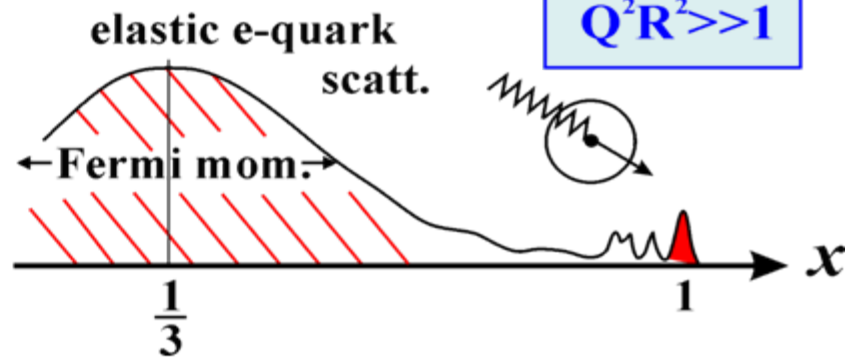
$$Q^2 R^2 \sim 1$$



e-quark  
scatt:

$$x = \frac{1}{3} \left( \frac{Q^2}{2p_q \cdot q} \right) = \frac{1}{3}$$

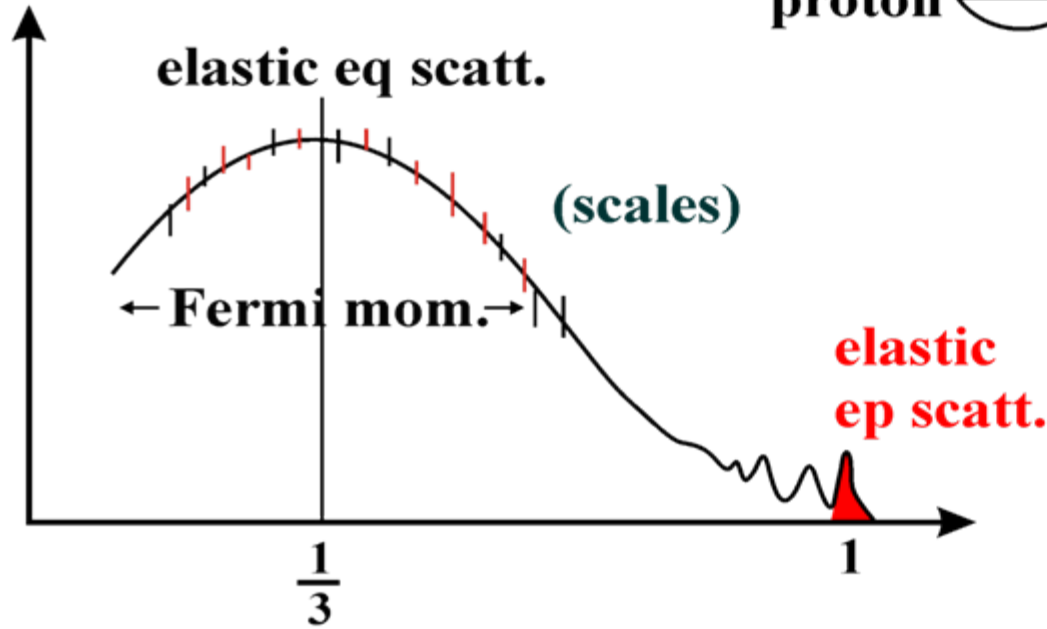
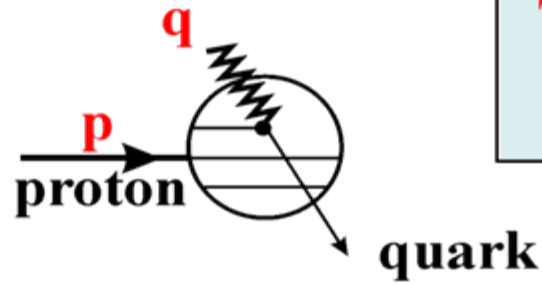
$$Q^2 R^2 \gg 1$$



$$p_q \sim \frac{1}{3} p$$

**e - proton scatt.**

**Two variables  
 $x, Q^2$**

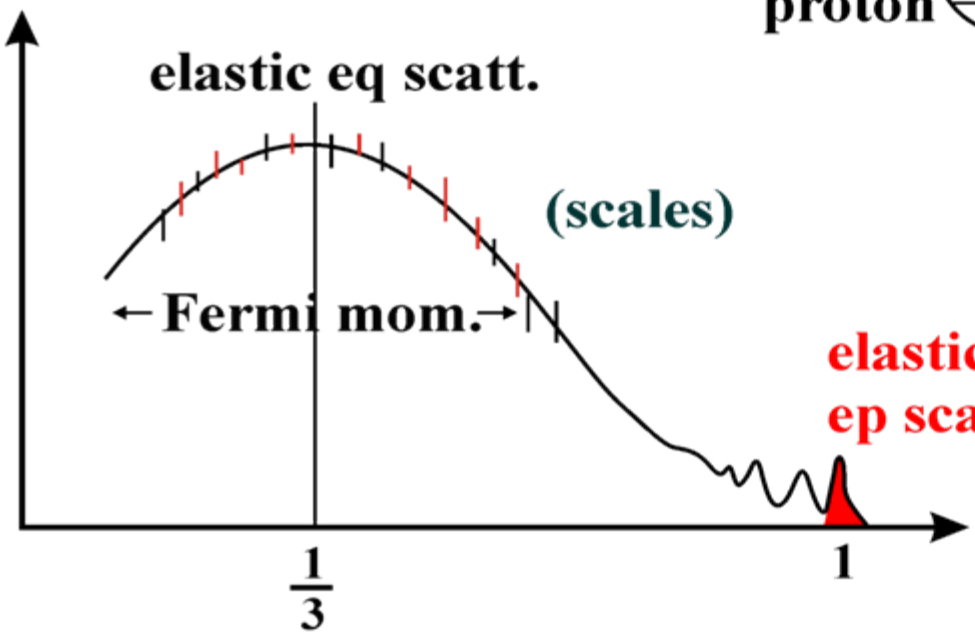
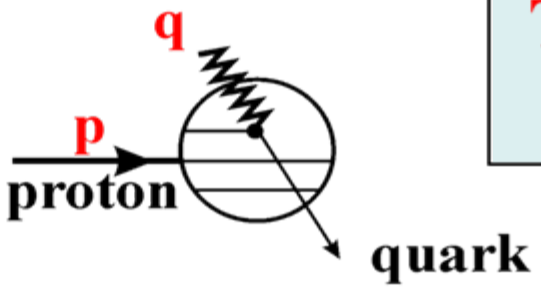


$$x = \frac{Q^2}{2p \cdot q}$$

**Bjorken scaling  
variable**

**e - proton scatt.**

**Two variables  
 $x, Q^2$**



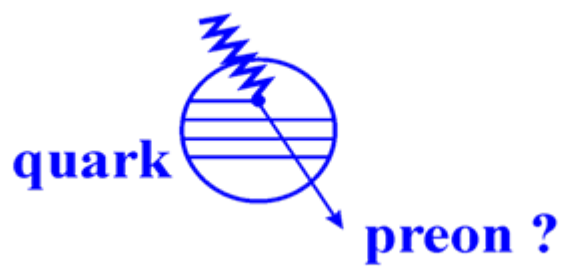
$$x = \frac{Q^2}{2p \cdot q}$$

**Bjorken scaling variable**

**Increase Q further**

**A replay ?**

**peak at  $x = \frac{1}{12}$  ?**



**No evidence of  
q substructure**



Instead of finding  $q$  substructure

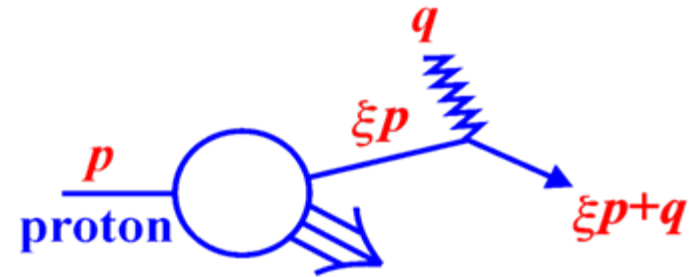
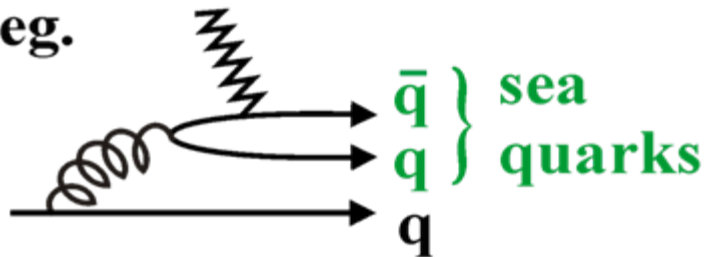


find QCD



(compare QED )

eg.



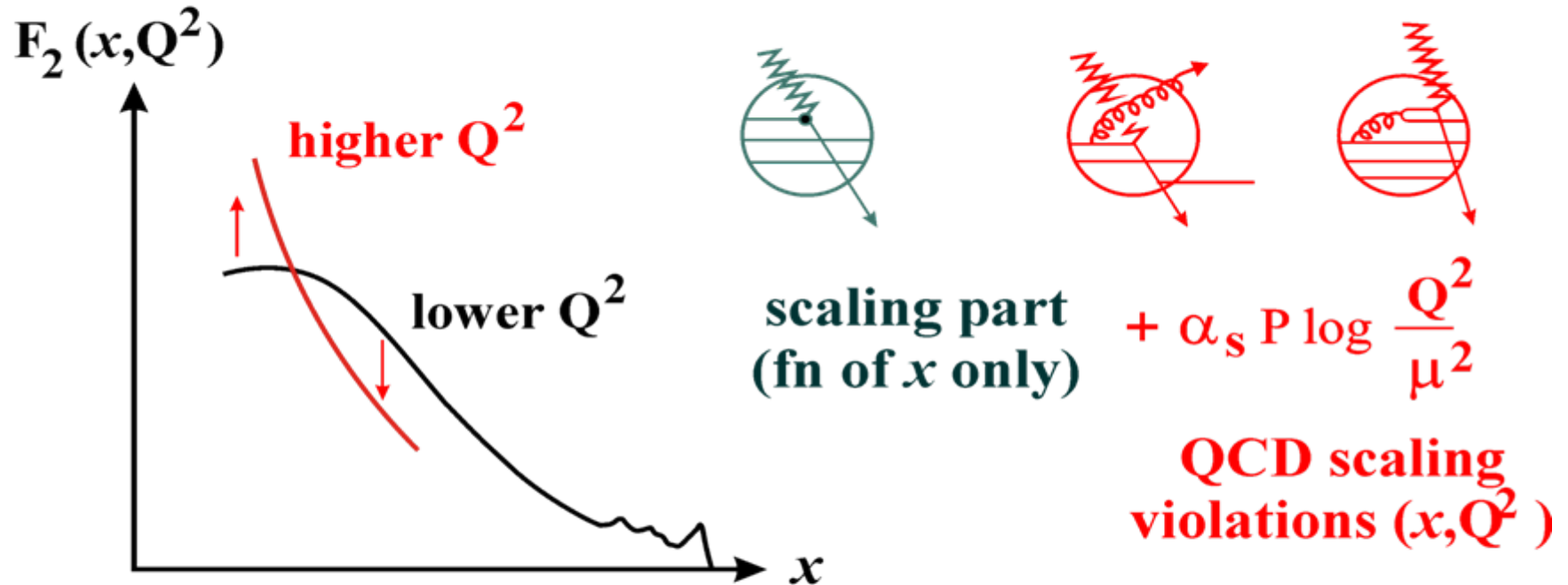
Consequence :  
 as  $Q^2$  increases, more and more partons are involved.  
**Each parton, on average, must have smaller  $x$ .**

$$(\xi p + q)^2 = m_q^2 \simeq 0$$

$$2\xi p \cdot q - Q^2 \simeq 0$$

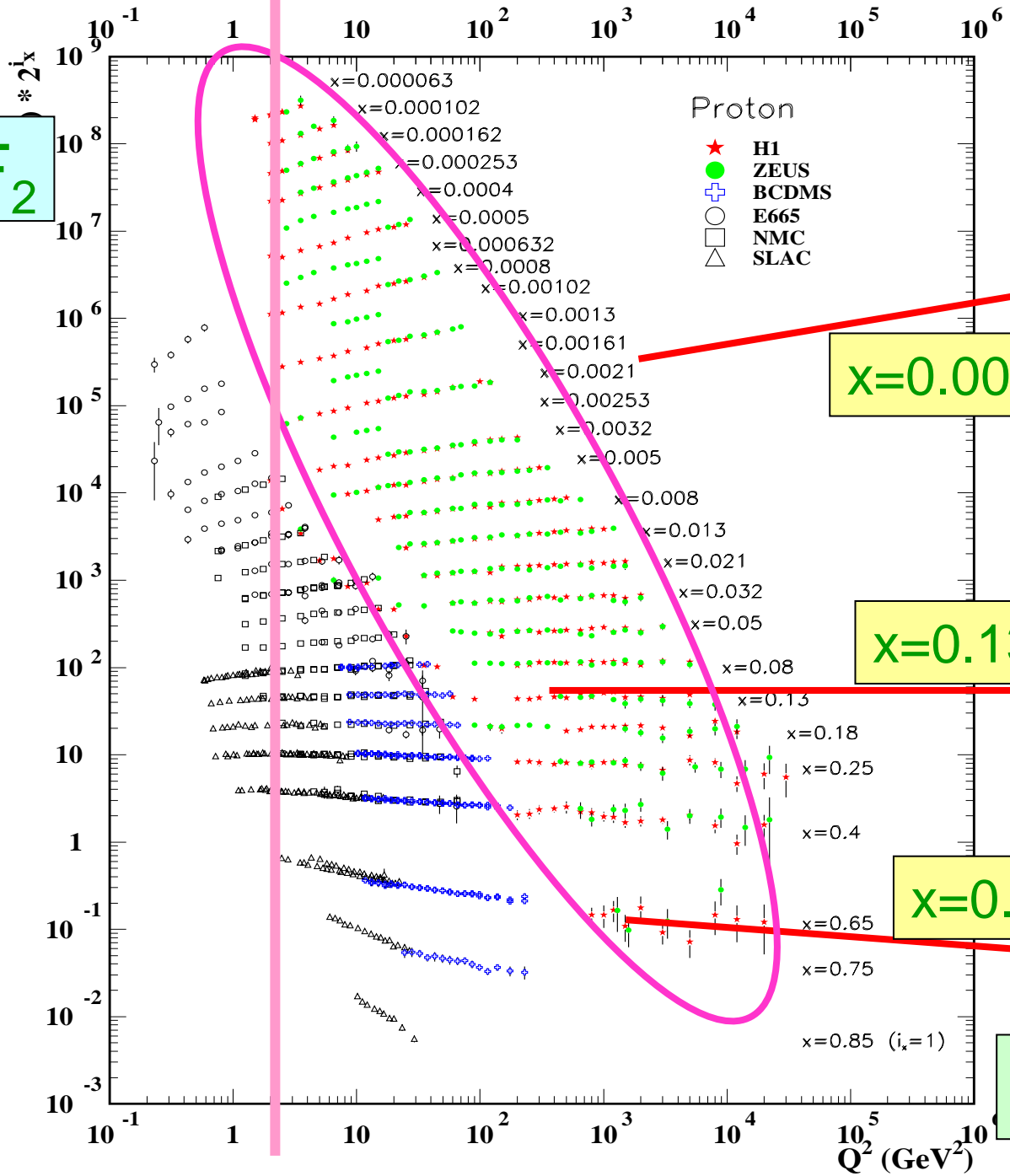
$$\xi = \frac{Q^2}{2p \cdot q} = x$$

As  $Q^2$  increases, each parton has, on average, smaller  $x$



**Famous experimentalist said to Wilczek :  
You expect us to measure logarithms ! ?  
Not in your lifetime, young man !**

$F_2$



Wilczek's QCD  
log  $Q^2$  scaling  
violations

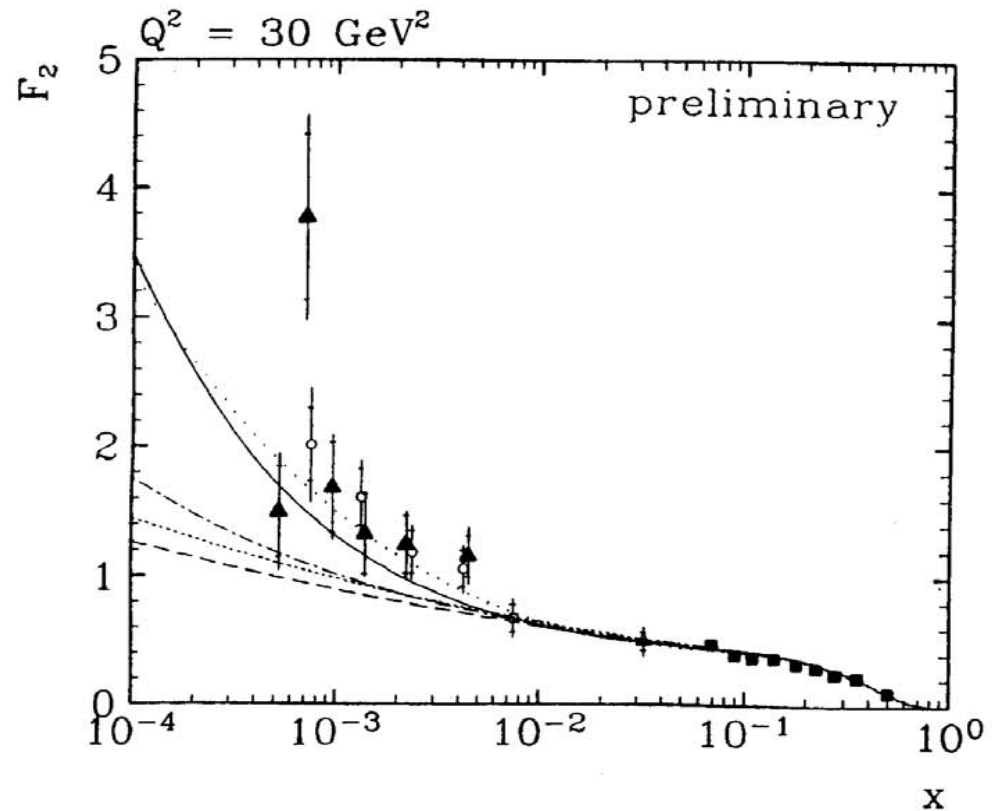
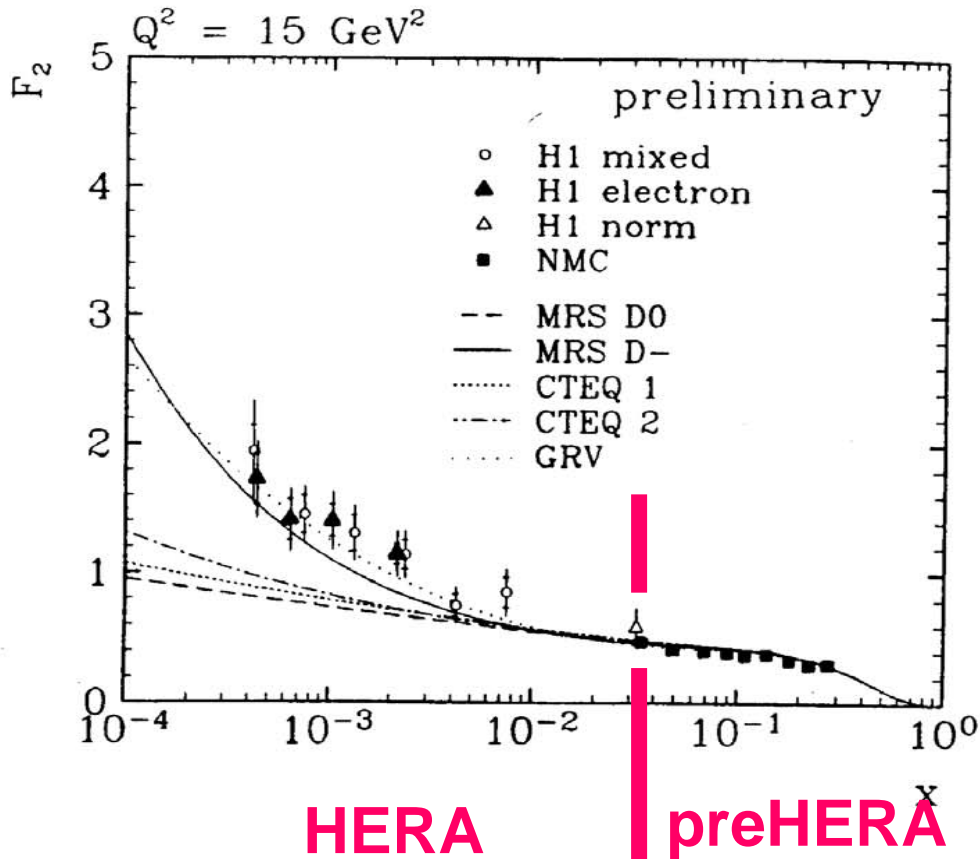
x=0.002

x=0.13

x=0.65

$Q^2$

# Workshop on HERA Durham, March 1993



gain of 100 in reach

From the proc. of “W/S on HERA” (Durham, March 1993)

One of the moments of **high drama** was the presentation of the first measurement of  $F_2$  at **HERA** showing that the structure function did indeed rise quite strongly at low  $x$ .

The **argument over the interpretation began immediately and continued all week**---was it evidence for singular BFKL-type behaviour of the gluon; was it just evidence of the need for a different parametrization; what did it imply for the Pomeron and diffractive scattering ?

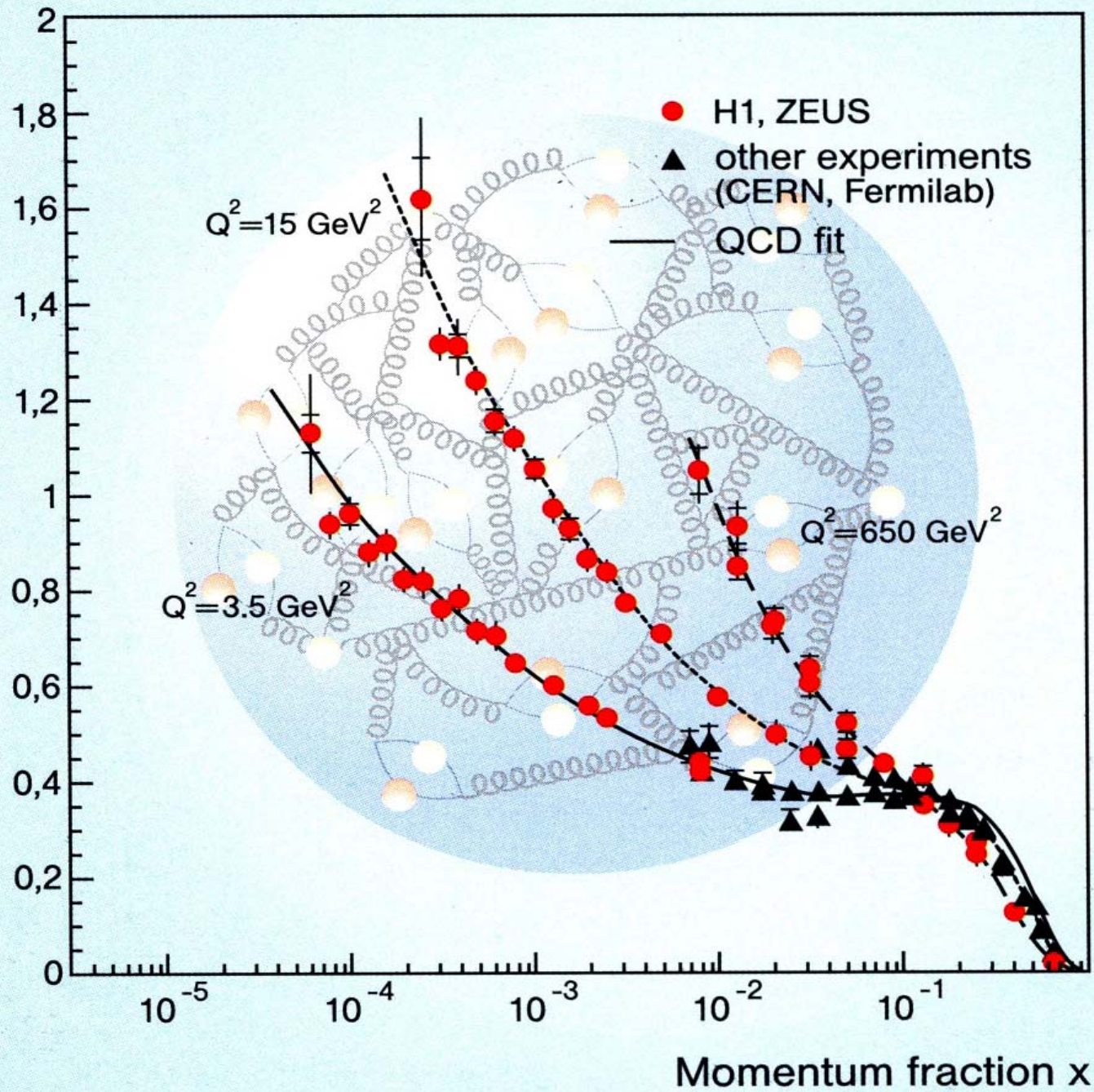
Although the protagonists tried very hard, **it will take a lot more data and quite a few more Workshops to answer all these exciting questions.**

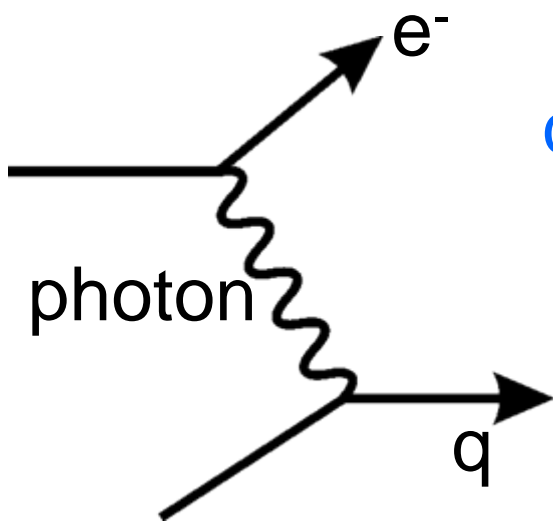
→ led directly to the DIS series of Workshops



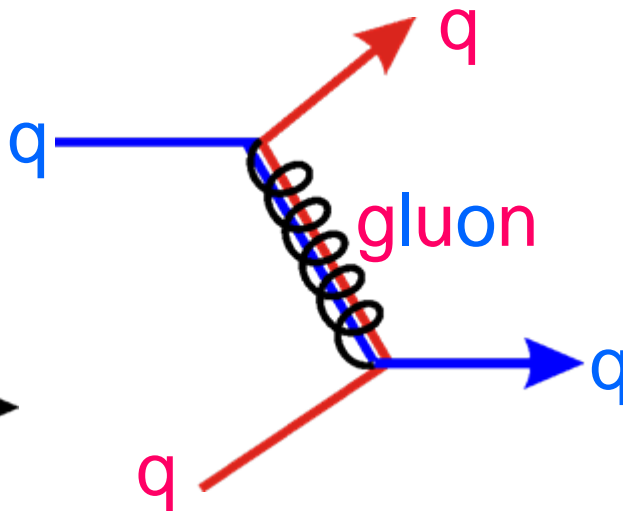
**HERA WORKSHOP  
ST. JOHN'S COLLEGE, DURHAM.  
MARCH 1993**

Proton structure function  $F_2$



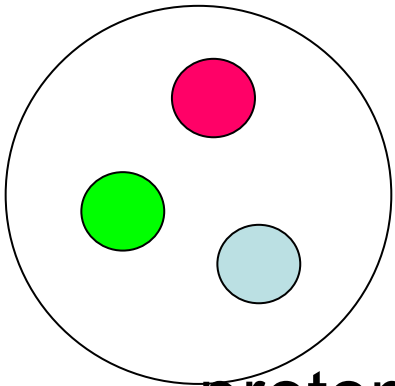


QED: photon does not carry charge



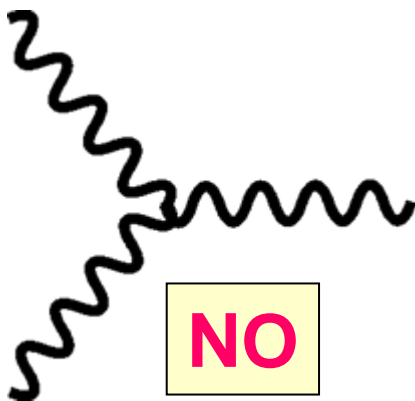
QCD: gluons do carry colour

quarks have colour

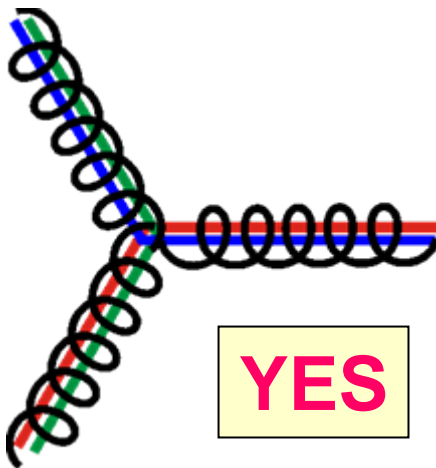


proton

observed pts. are colourless



NO



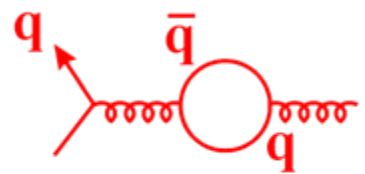
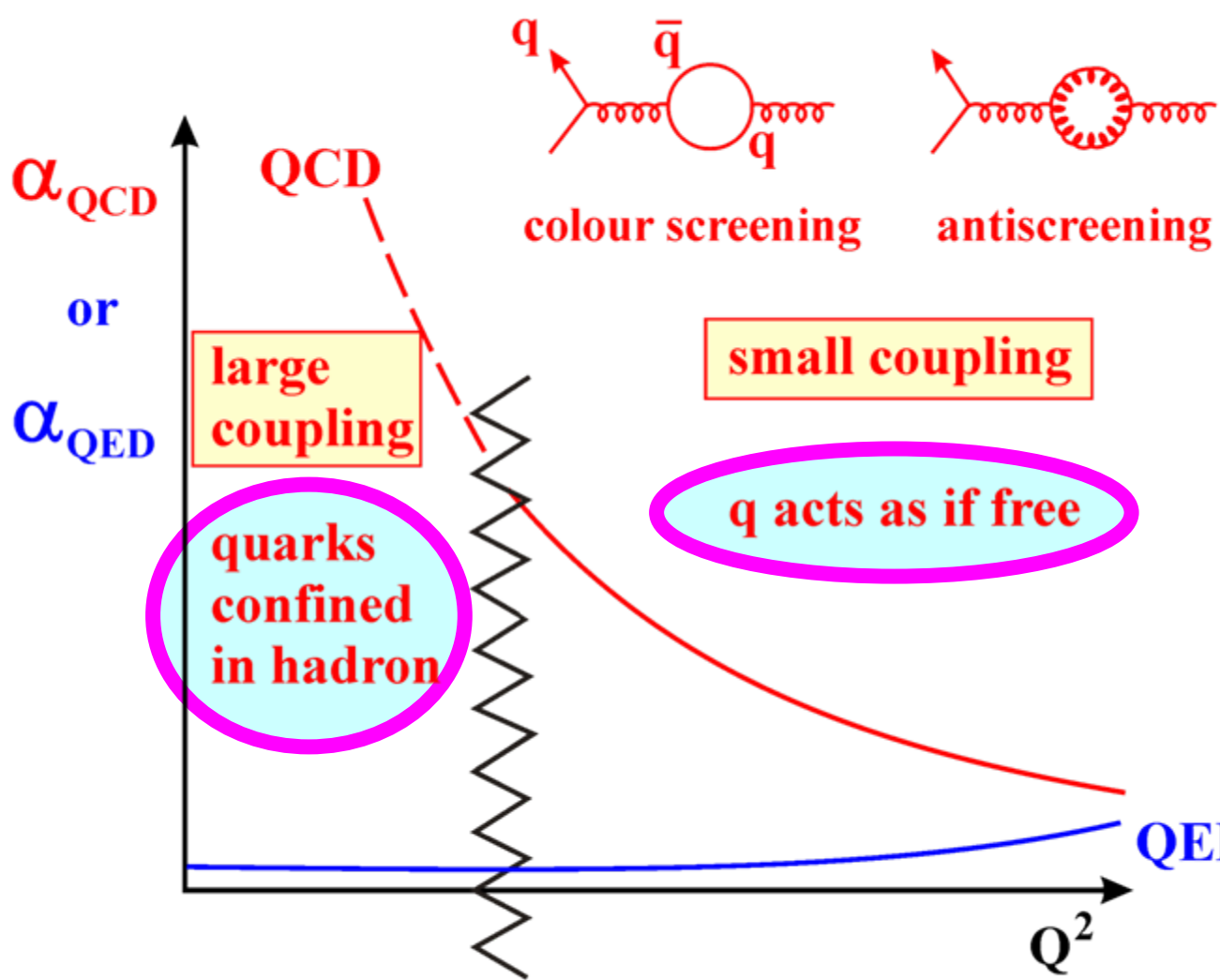
YES



like QED

NEW

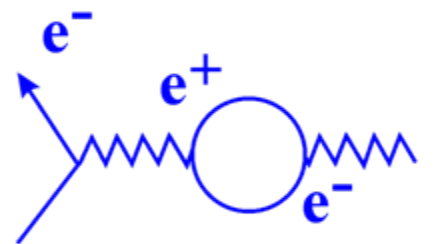
QCD is a 'dream' theory



colour screening



antiscreening

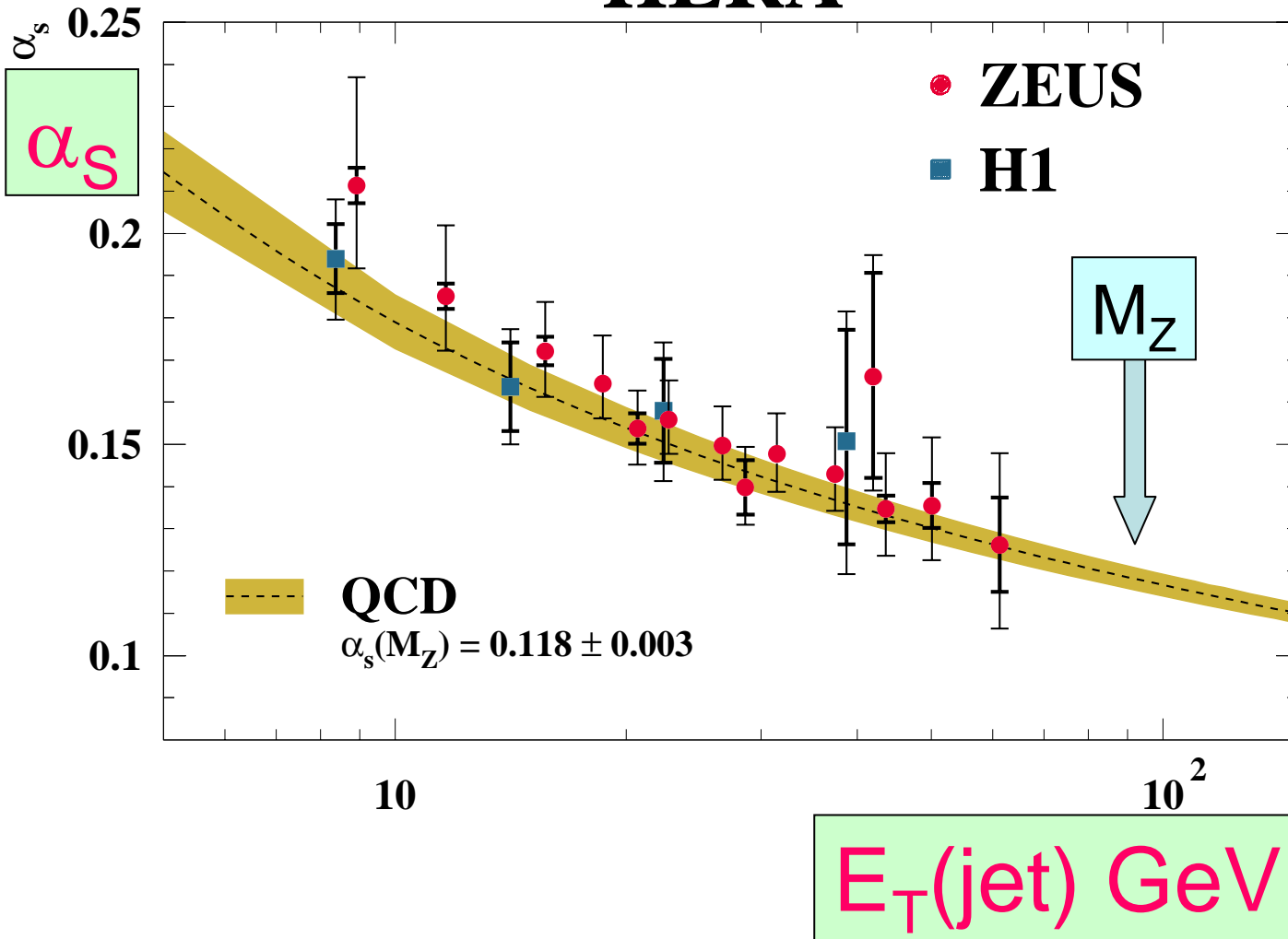


charge screening

(pQCD predicts running, but not absolute value, of  $\alpha_{\text{QCD}}$ )

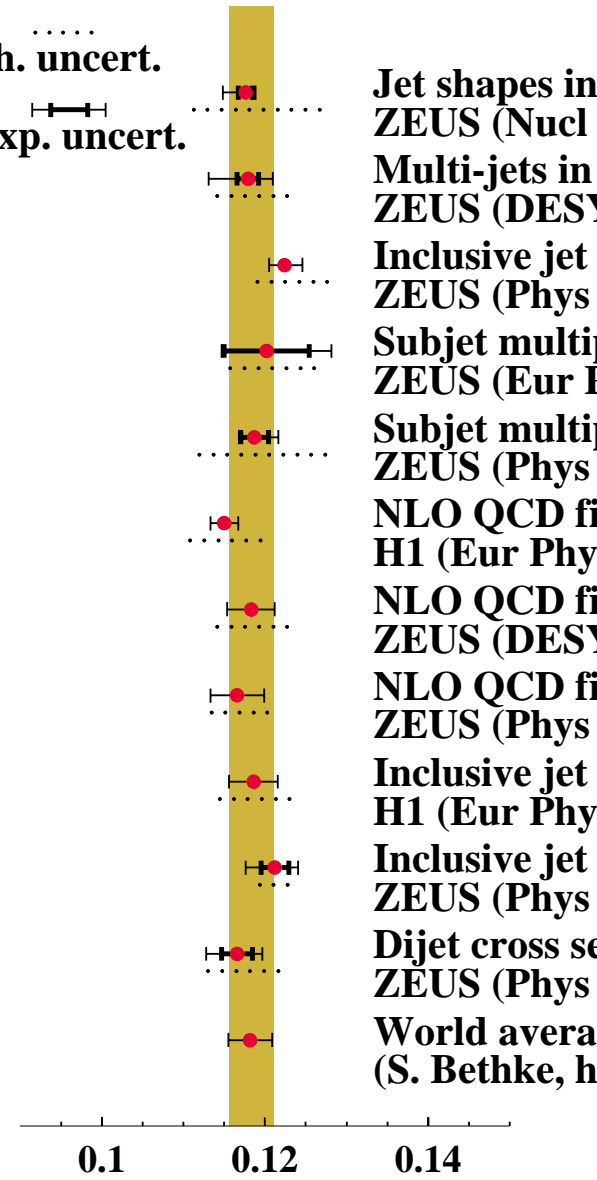
# QCD coupling from inclusive jet data at HERA

## HERA

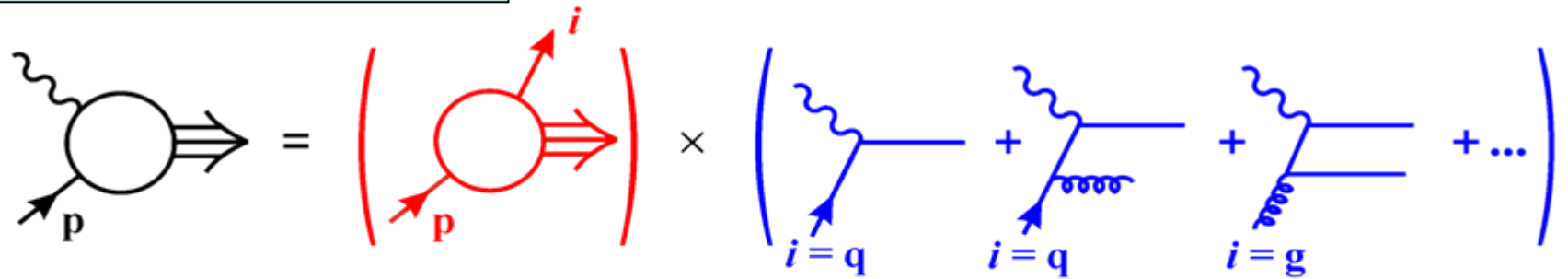


.....  
th. uncert.

—+—+—  
exp. uncert.



## Factorization theorem



$$F_2(x, Q^2) = \sum_{i=q, \bar{q}, g} f_i \otimes C_{2,i}$$

**UNIVERSAL** parton densities  $f_i(x, Q^2)$   
 Q dep. given in pQCD by DGLAP eqs.

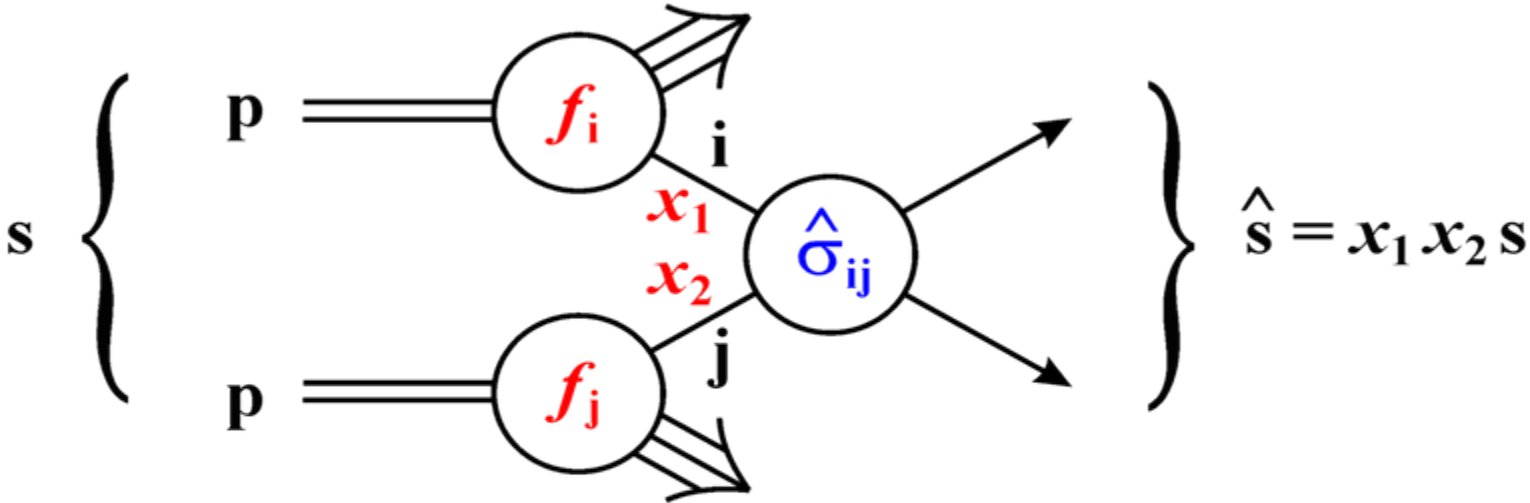
**Coeff. fns,  $C_{a,i}$  KNOWN**  
 from pQCD

$f_i$  and  $C_{2,i}$  are power series in  $\alpha_S$

LO	NLO	NNLO	....
$\alpha_S$	$\alpha_S^2$	$\alpha_S^3$	....

**pp → X LHC**

**(p $\bar{p}$  → X Tevatron)**



$$\sigma = \sum_{i,j} \int dx_1 dx_2 \underbrace{f_i(x_1, Q^2) f_j(x_2, Q^2)}_{\text{same universal parton densities}} \underbrace{\hat{\sigma}_{ij}(x_1 x_2 s, \alpha_S(Q^2))}_{\text{calculable}}$$

# Determination of parton distributions

Parametrise  $x$  dep. at  
low pQCD scale  $Q_0^2$

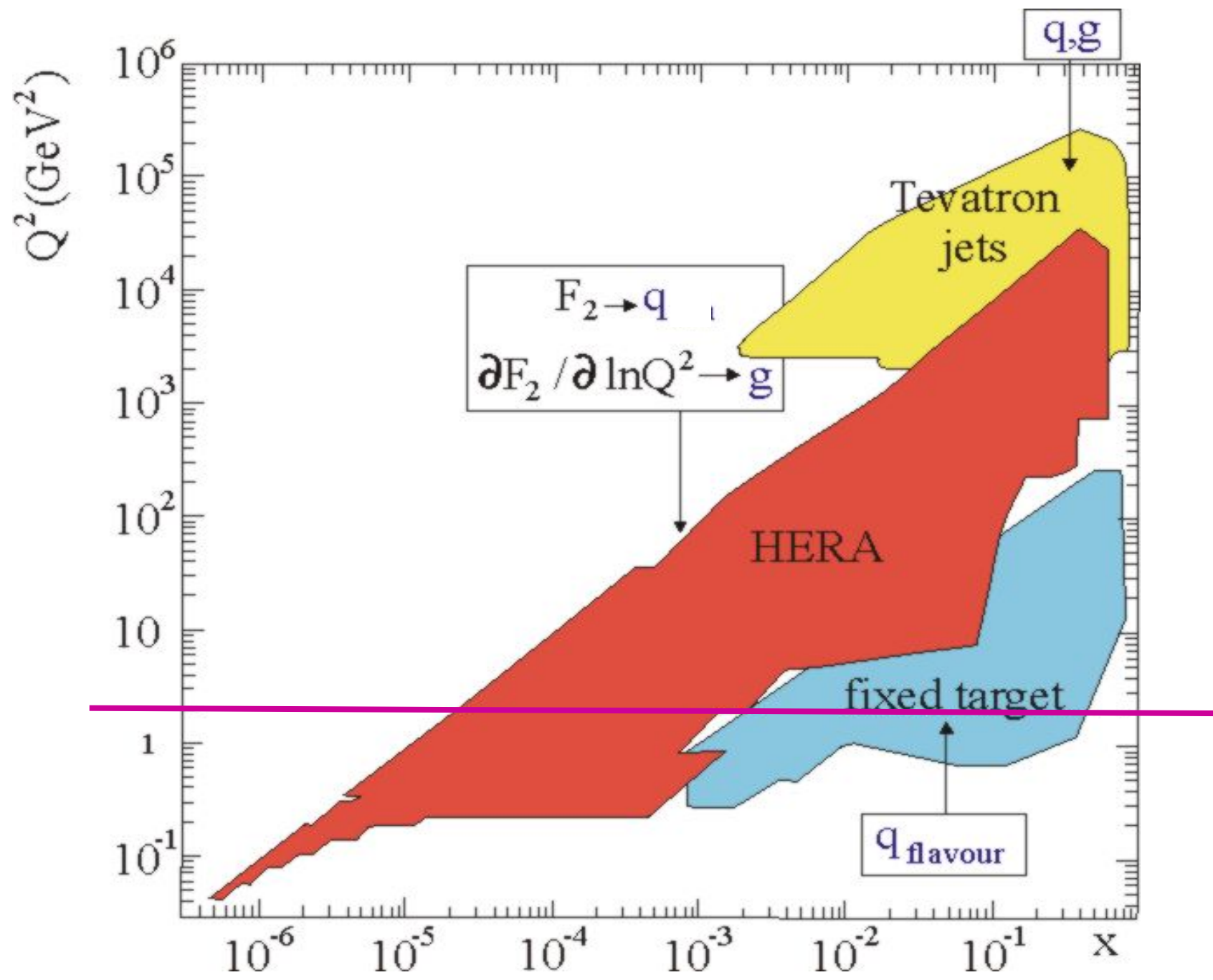
$$\rightarrow f_i(x, Q_0^2)$$

Evolve up in  $Q^2$   
using DGLAP eqs.

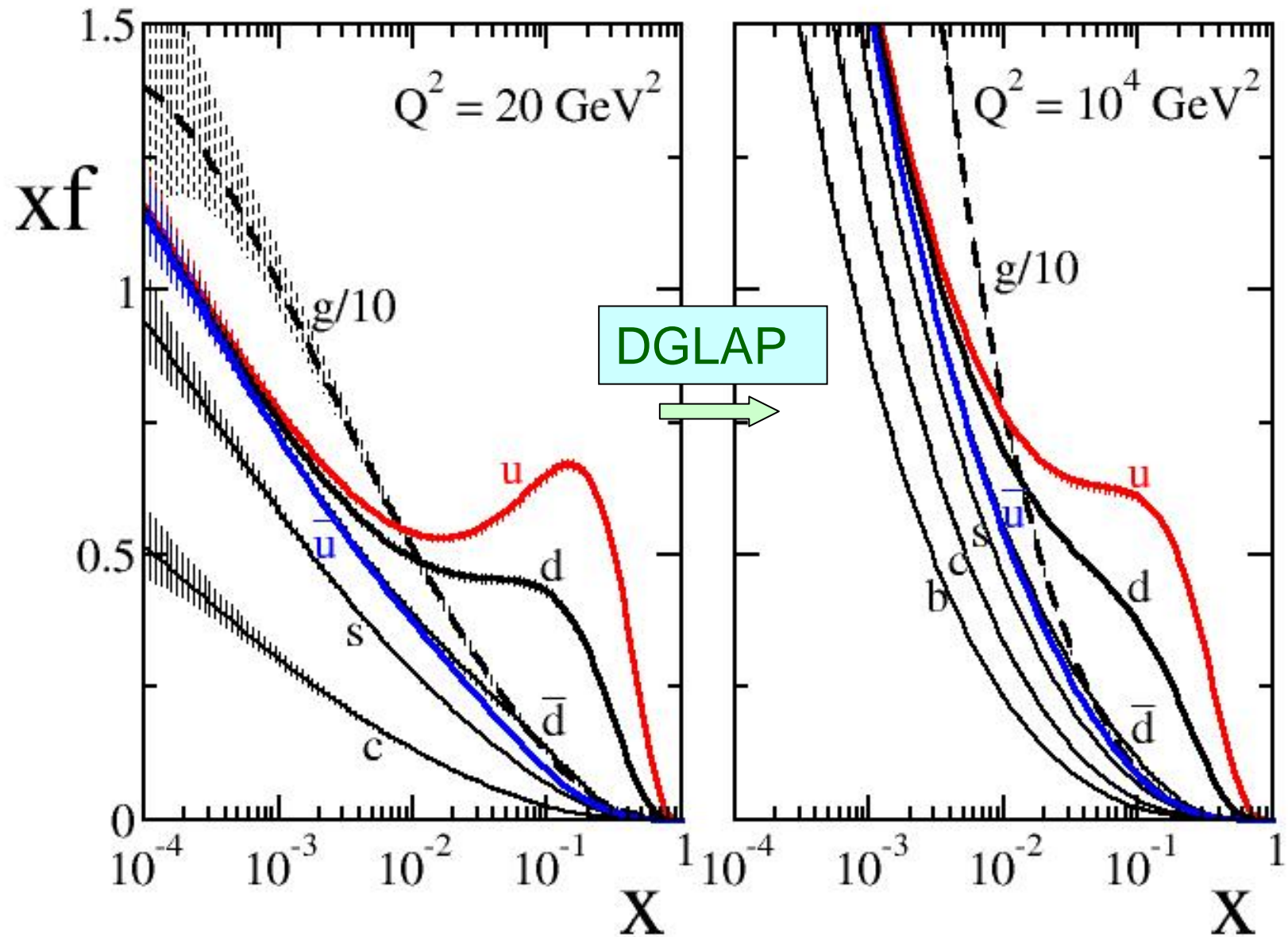
$$\rightarrow f_i(x, Q^2 > Q_0^2)$$

Global fit to **HERA**  
+ all related data

$$\rightarrow f_i\text{'s}$$

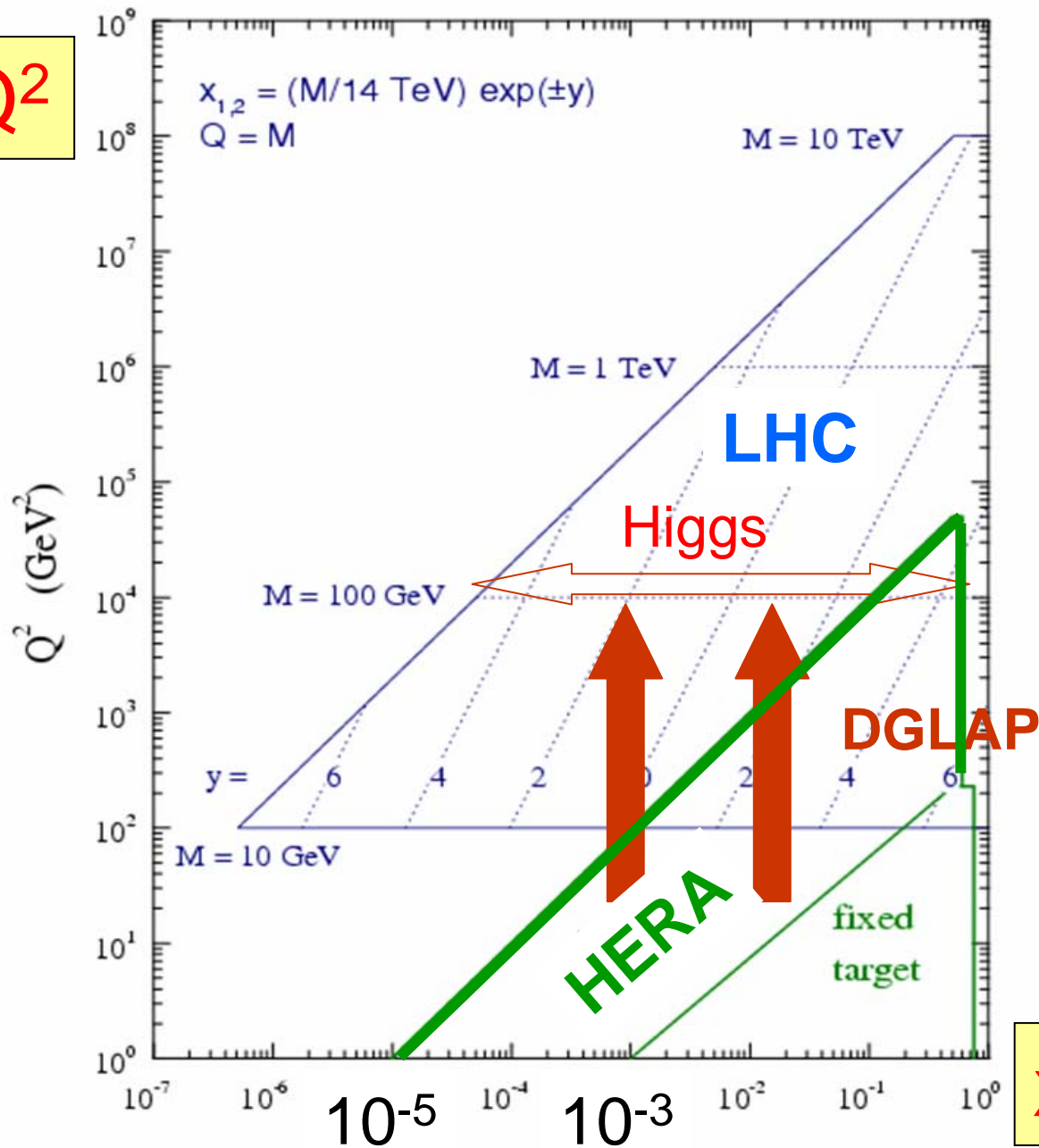


# NNLO Partons (2007)



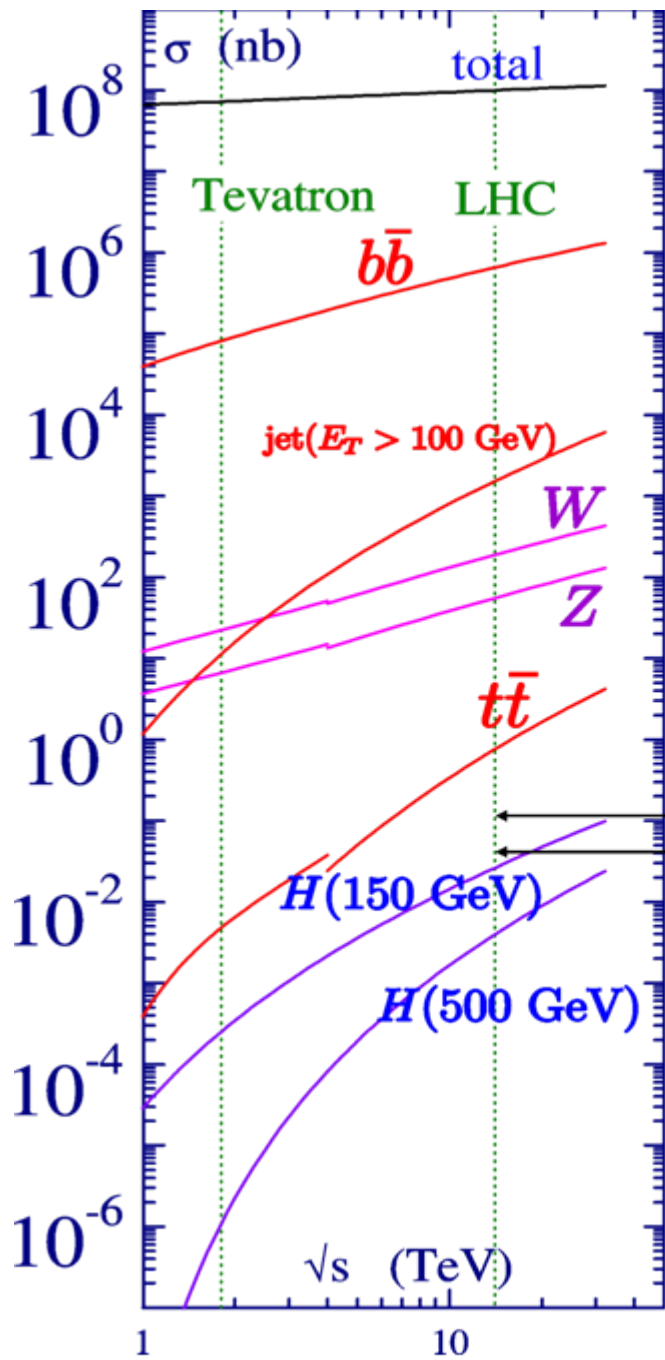
# LHC parton kinematics

$Q^2$



X





events/sec if  $\mathcal{L} = 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

$b\bar{b} \sim 10^6/\text{sec}$  CKM,  
CP violation

$W \rightarrow e\nu \sim 20/\text{s}$   $M_W, \Gamma_W$   
 $Z \rightarrow ee \sim 2/\text{s}$  luminosity

$t\bar{t} \sim 1/\text{s}$   $m_t$

gluino-pair?  
squark-pair?  
Higgs?  
(few/minute) } **discovery?**

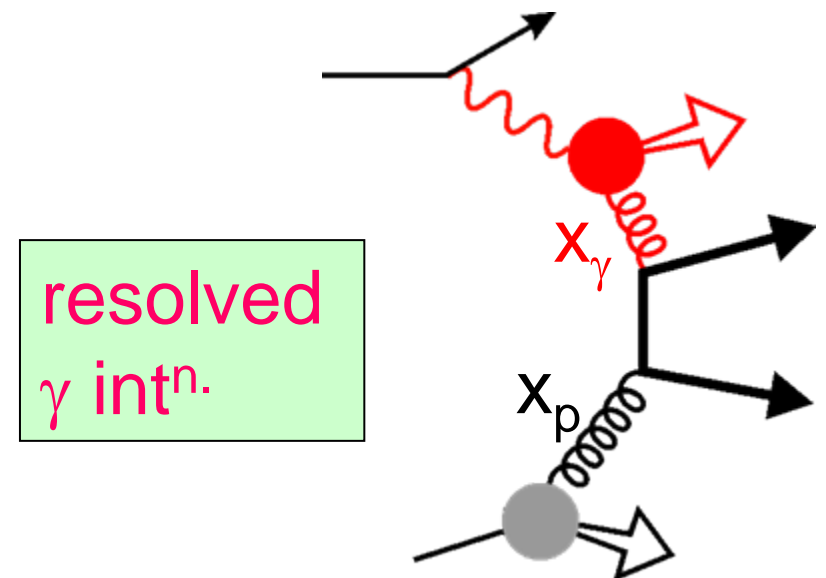
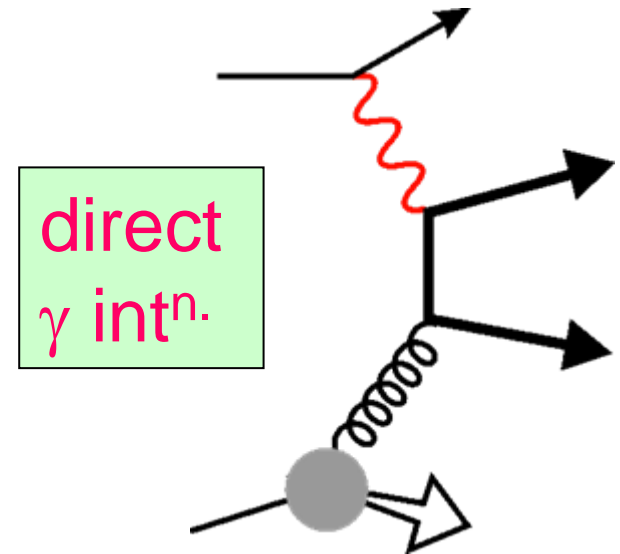
or, more exciting,  
something totally  
unexpected

# Structure of **photon** (and proton) from dijet photoprod. at HERA

Forward dijets give info. on

- 1)  $\gamma$  parton distrib<sup>ns.</sup> (at low  $x_\gamma$ )
- 2) gluon distrib<sup>n.</sup> in proton  
(from direct/high  $x_\gamma$ )

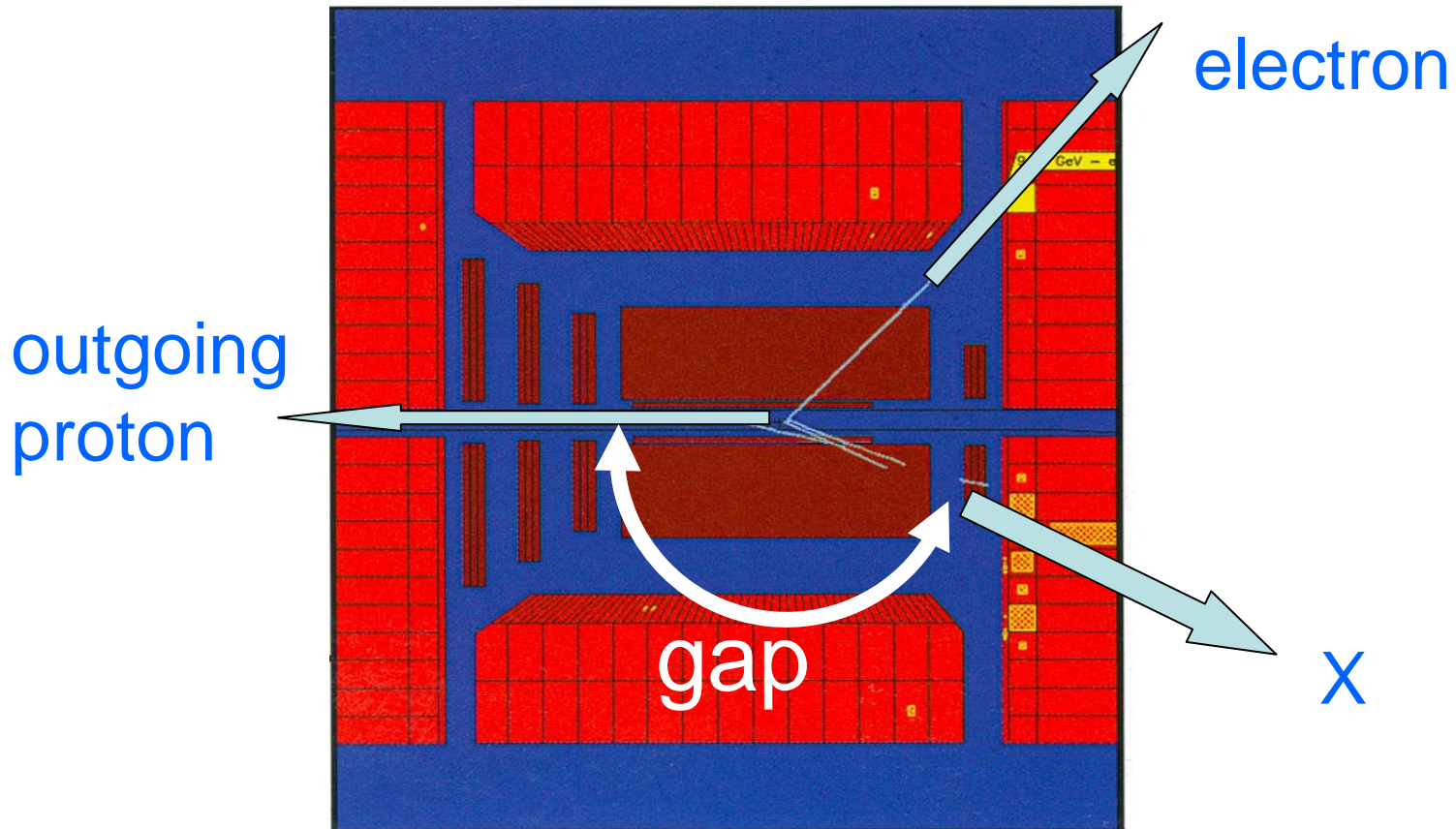
No existing set of photon  
distrib<sup>ns.</sup> gives an adequate  
(NLO) description of  
“resolved” HERA data

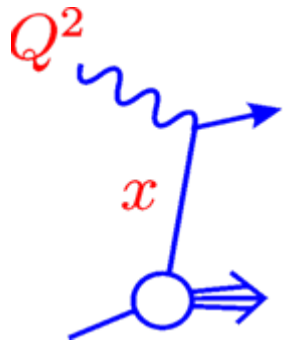


DIS:  $ep \rightarrow eX$  ( $\gamma^* p \rightarrow X$ )

HERA finds that about 10% of these events are

diffractive DIS:  $ep \rightarrow eX+p$  ( $\gamma^* p \rightarrow X+p$ )





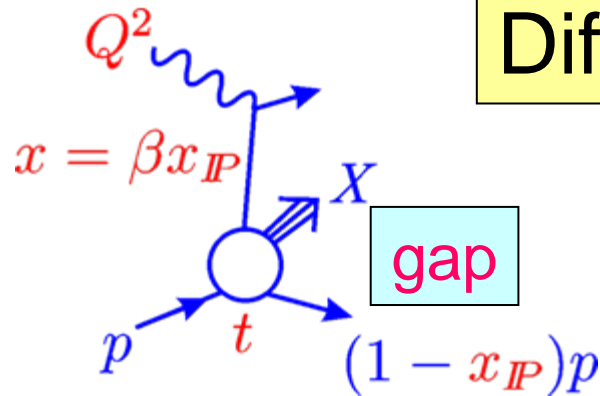
**DIS**

$$F_2(x, Q^2) =$$

$$\sum_{i=q, \bar{q}, g} f_i \otimes C_{2,i}$$

same

**Diffractive DIS**

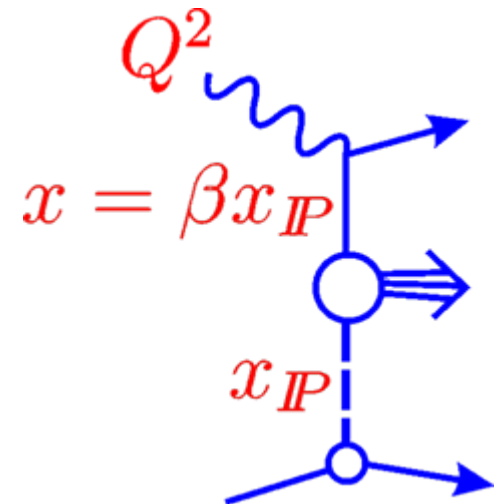


$$F_2^{D(3)}(x_{\mathbb{P}}, \beta, Q^2) =$$

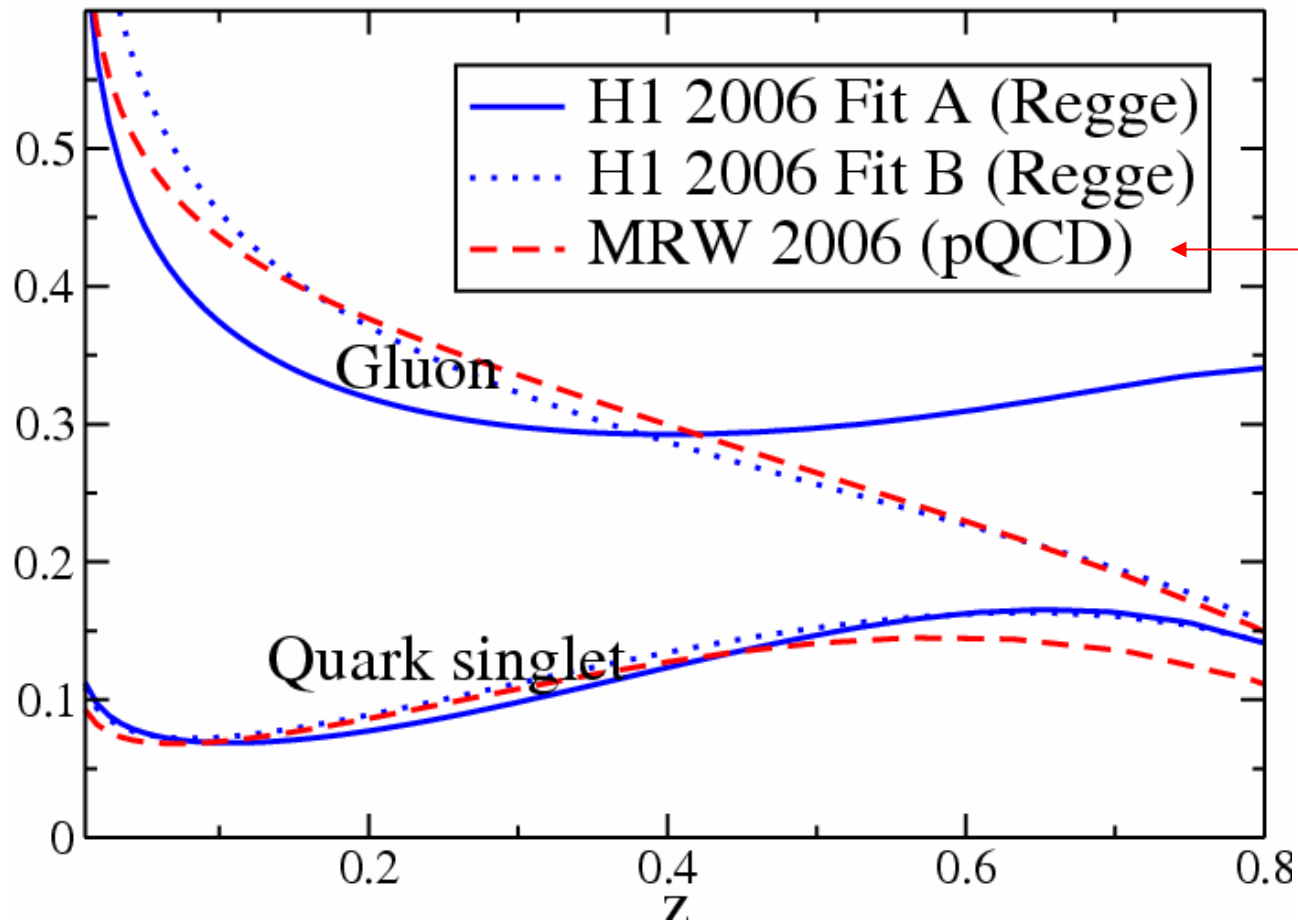
$$\sum_i f_i^D \otimes C_{2,i}$$

If then assume, Regge factorization:

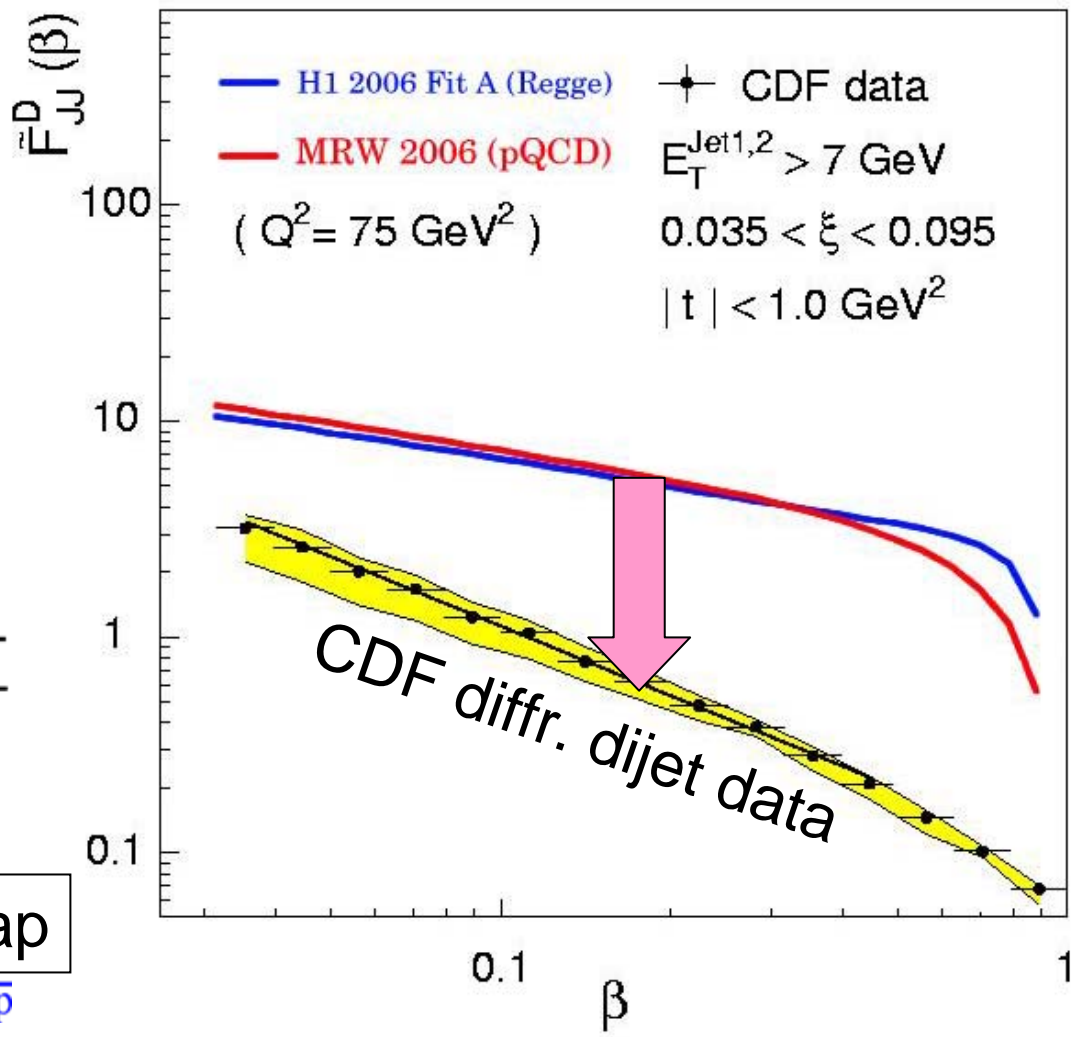
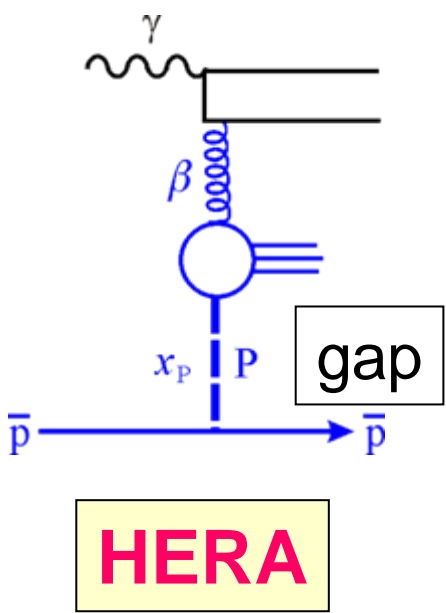
$$f_i^D(x_{\mathbb{P}}, \beta, Q^2) = \text{Flux}(x_{\mathbb{P}}) f_i^{\mathbb{P}}(\beta, Q^2)$$



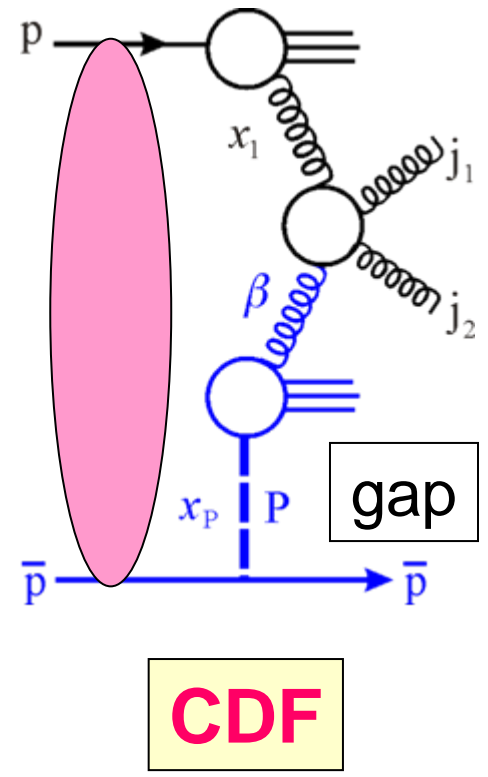
$$x_{\text{IP}} = 0.003, Q^2 = 10 \text{ GeV}^2$$



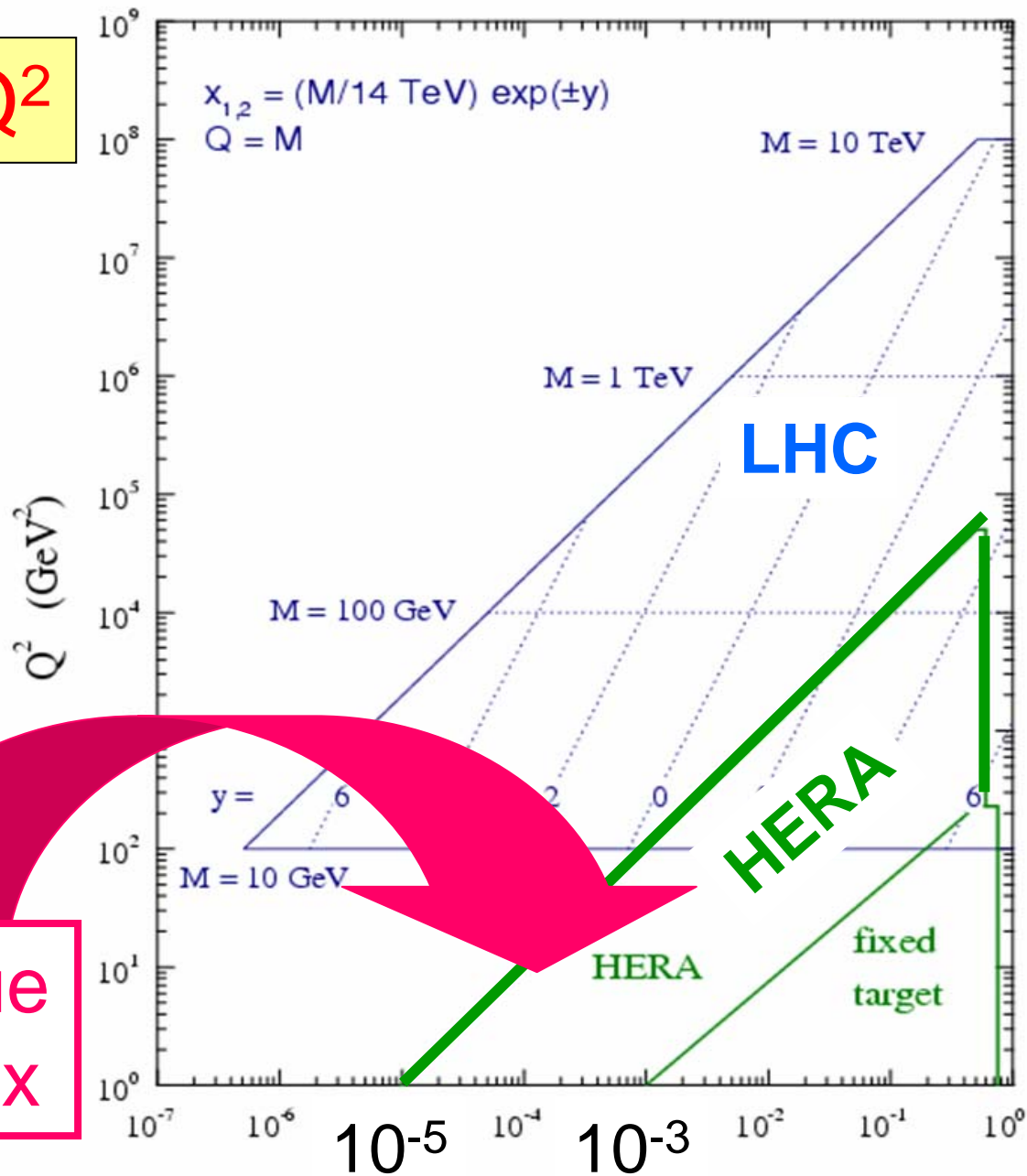
diffractive partons  $g^D, q^D$  can be used to predict diffractive processes with hard scale? Yes, but...



soft rescatt.



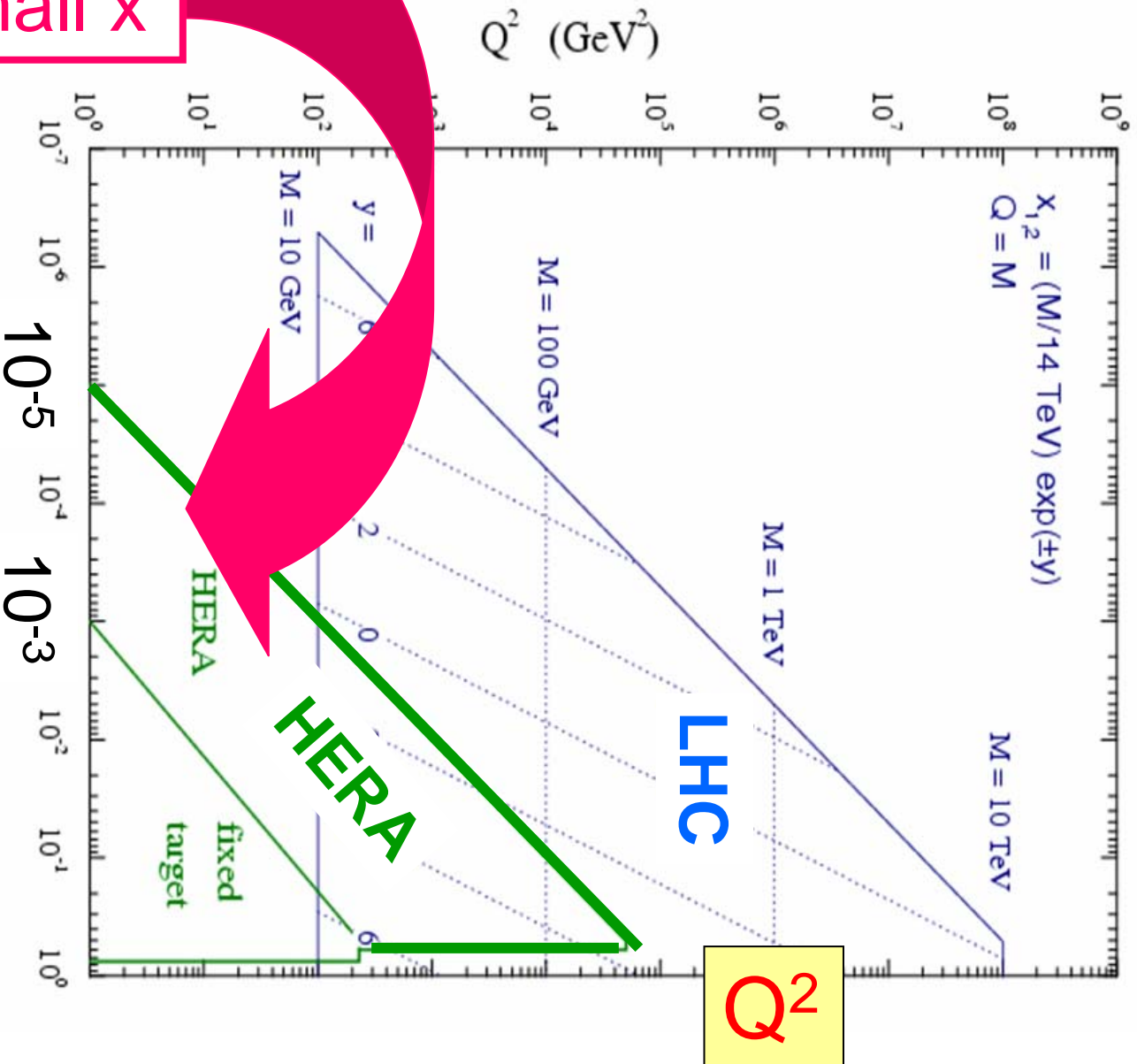
$Q^2$



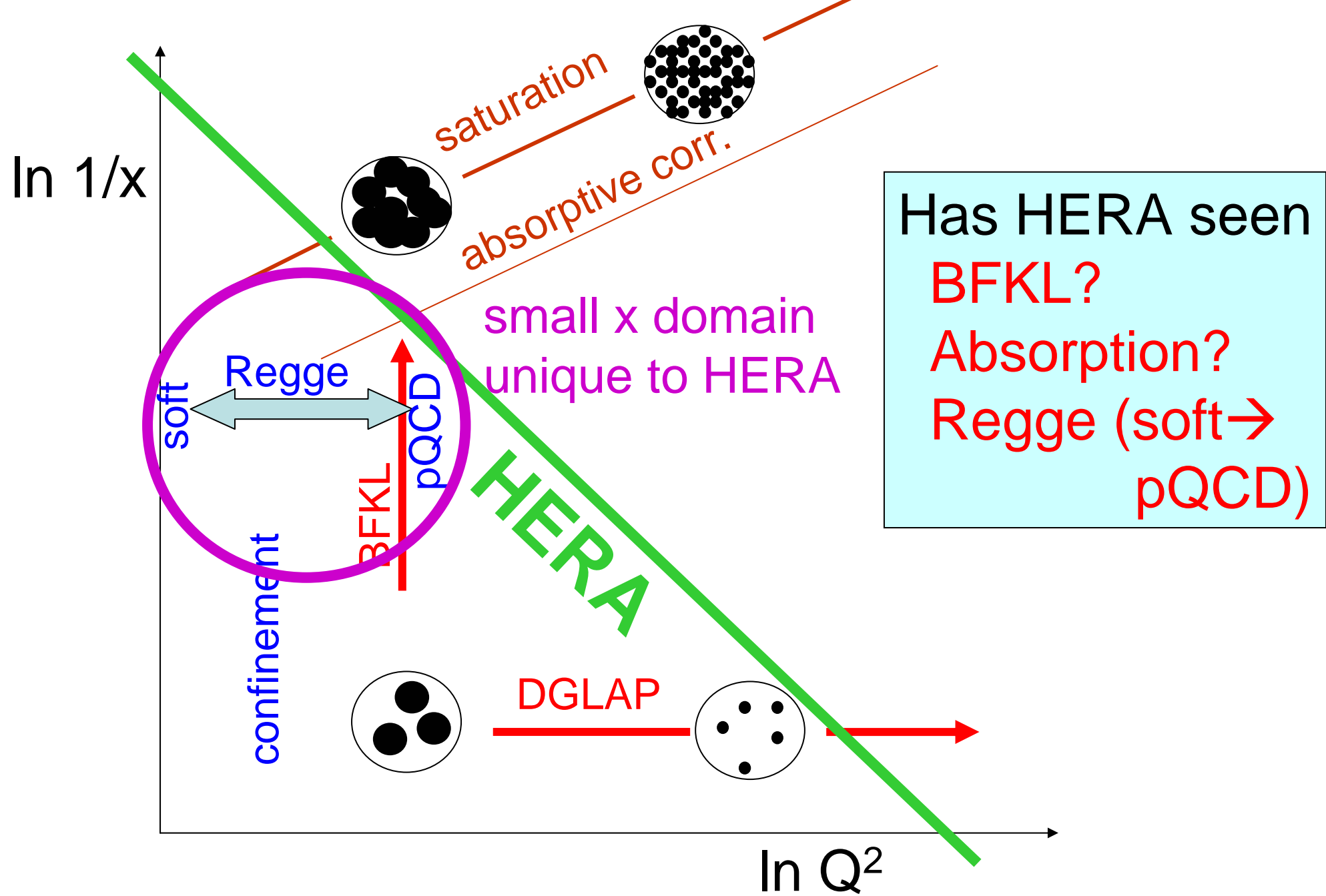
HERA: a unique probe of small  $x$

X

HERA: a unique probe of small x







“soft” – particles go forward – no large scale – no pQCD  
 domain of Regge exchange: at HE Pomeron exchange

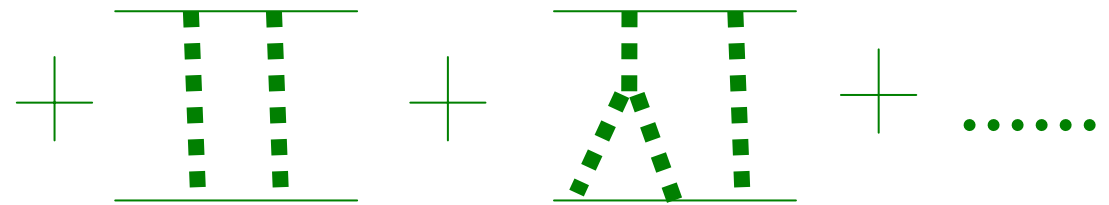
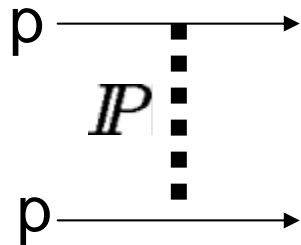
$$A(s, t) \sim f(t) s^{\alpha_{\mathbb{P}}(t)}$$

DL:  $\alpha_{\mathbb{P}}^{\text{eff}}(t) = \alpha_{\mathbb{P}}(0) + \alpha' t$

1.08      0.25

↙      ↘

DL incomplete -- must allow for multi-Pomeron effects



$\sigma_{\text{total}}, \frac{d\sigma_{\text{elastic}}}{dt}$

$s^{\alpha_{\mathbb{P}}(0)-1}$       shrinks

also cause shrinkage  
 also suppress growth of  $\sigma_{\text{total}}$

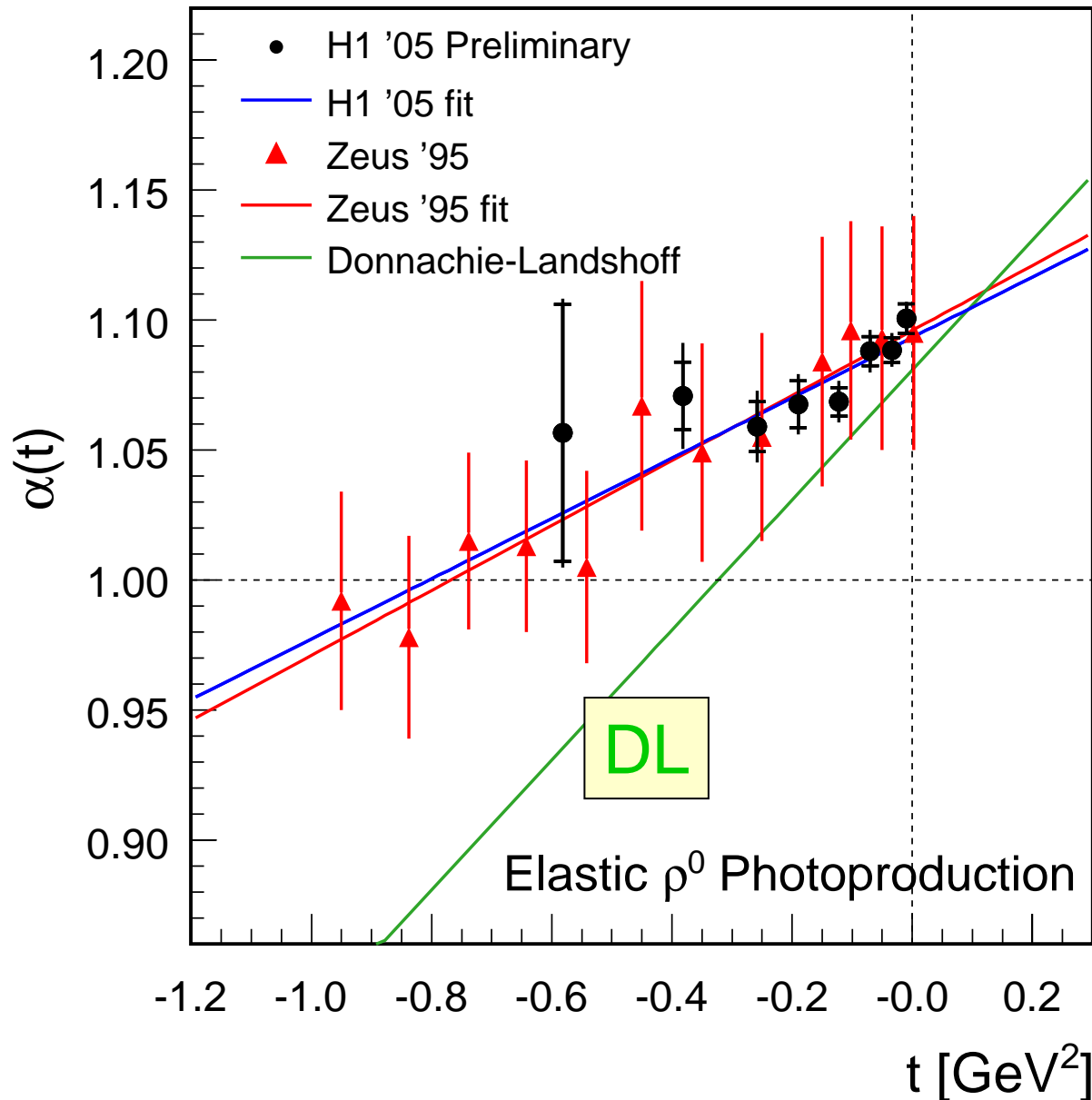
so  $\alpha_{\mathbb{P}}^{\text{bare}}$  has smaller  $\alpha'$ ,  
 larger  $\alpha_{\mathbb{P}}(0)$  to fit same data

$$\alpha_{\mathbb{P}}(t) = \alpha_{\mathbb{P}}(0) + \alpha' t$$

HERA data for



less rescattering  
than  $pp \rightarrow pp$



$\alpha'$  smaller

$\alpha_{\mathbb{P}}(0)$  larger

**BFKL:**

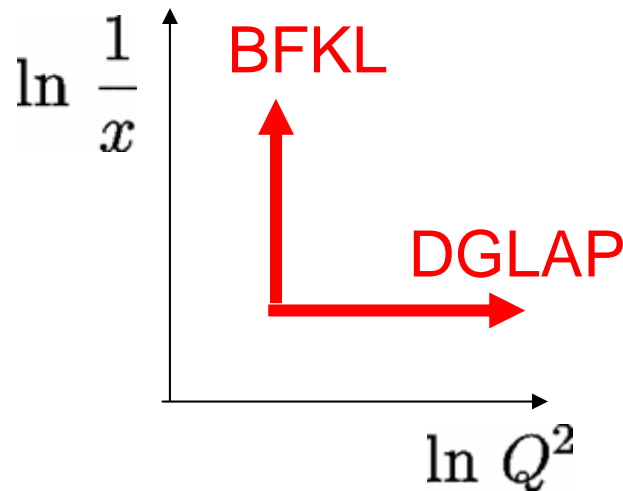
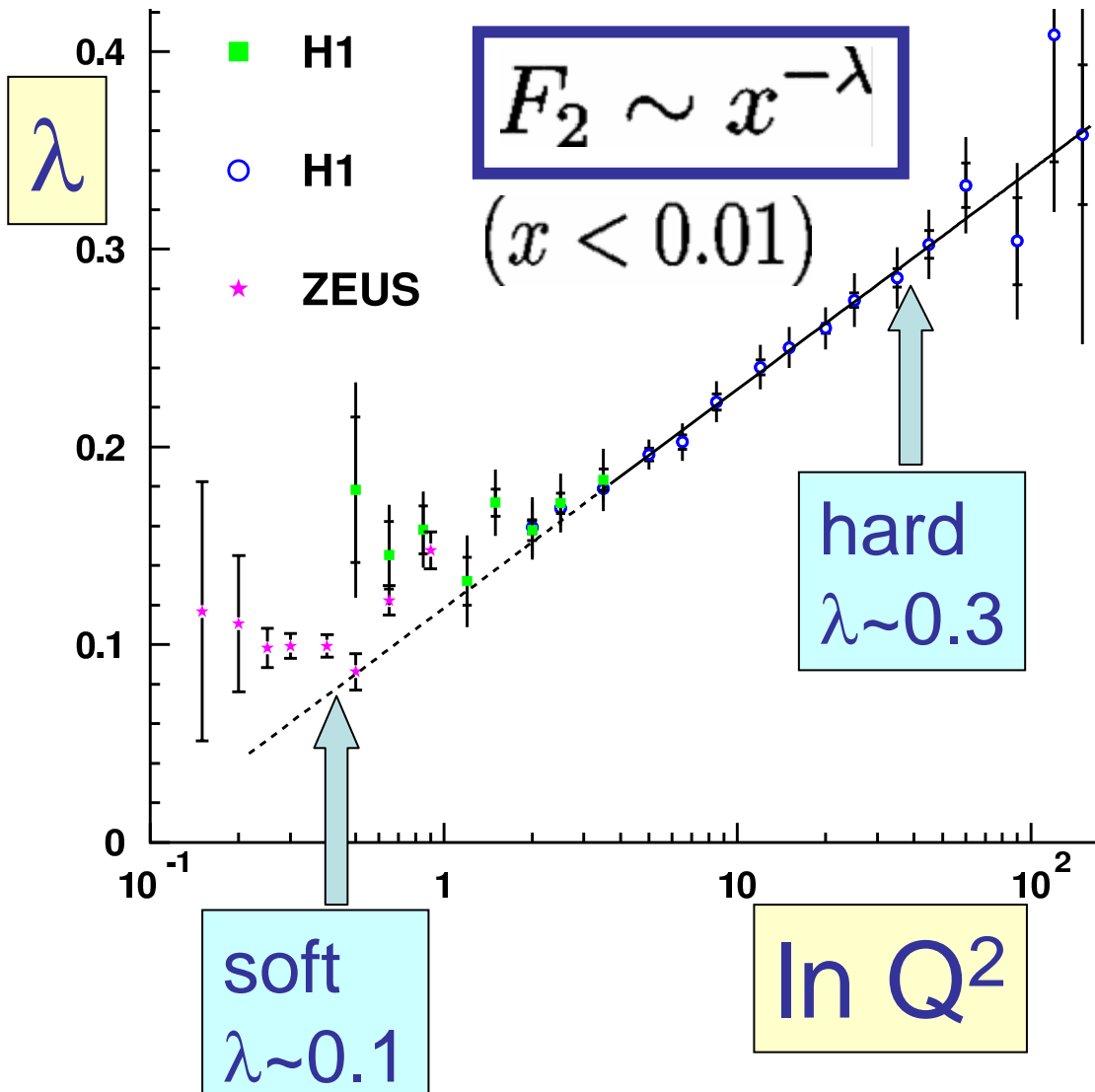
$$\frac{\partial f_g}{\partial \ln(1/x)} = K \otimes f_g = \lambda f_g$$

$$f_g \sim e^{\lambda \ln(1/x)} \sim x^{-\lambda}$$

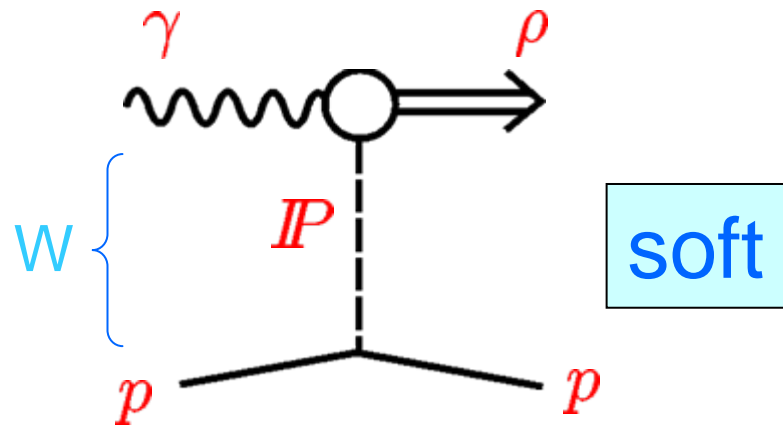
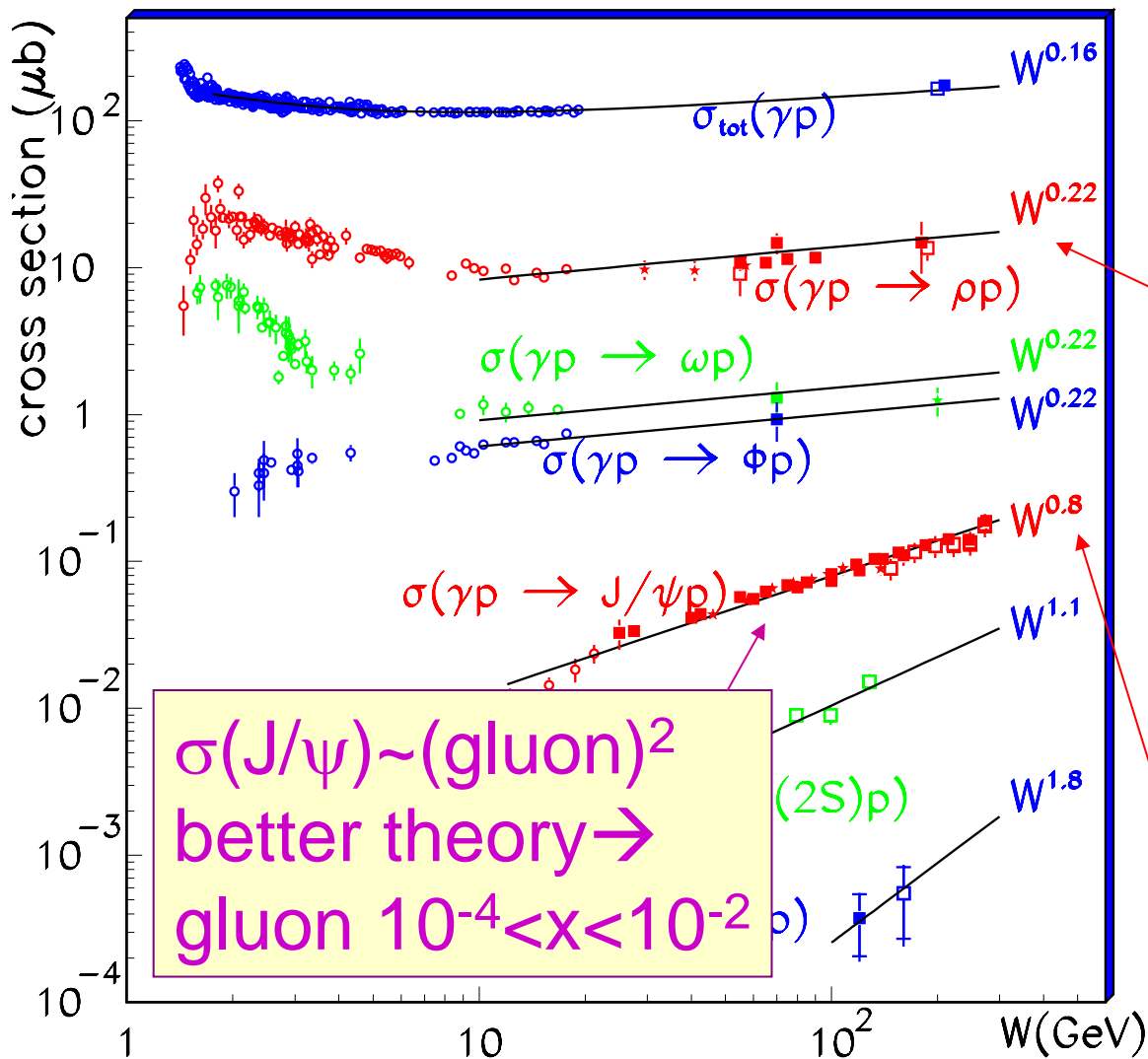
LL+NLL+partial  
all-order resum

$$f_g \sim x^{-0.3}$$

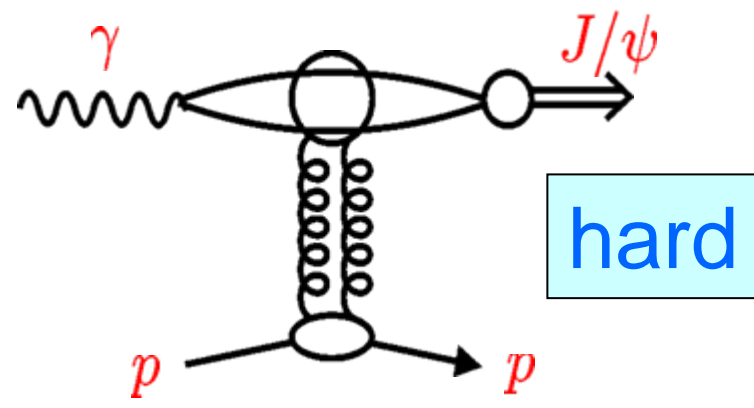
**DGLAP:**  $\frac{\partial g}{\partial \ln Q^2} \sim P \otimes g$



# Photoprod. of vector mesons



$$\sigma \sim W^{4(\alpha_P - 1)} \sim W^{0.2}$$

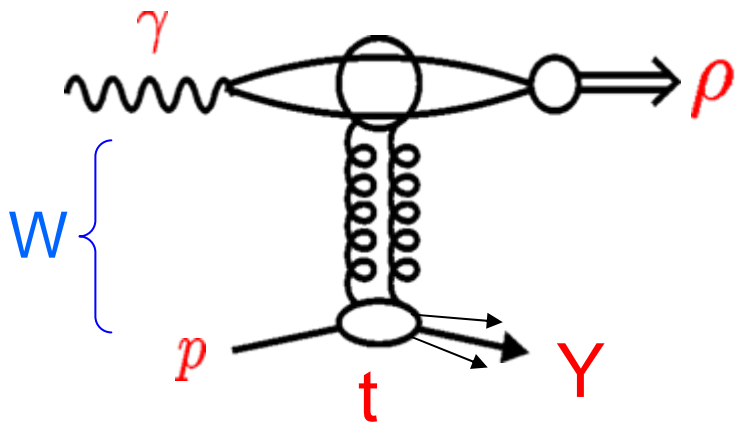
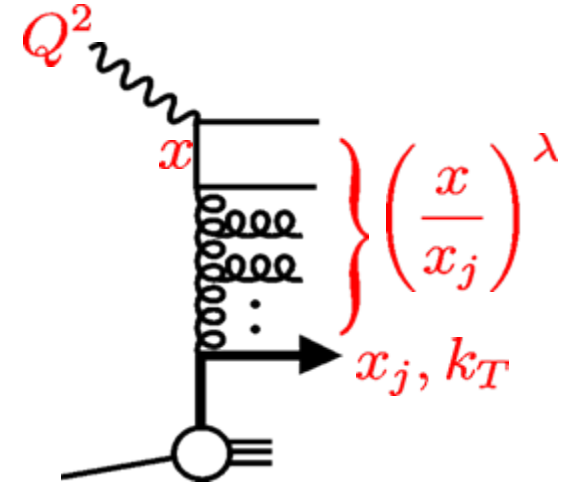


$$\sigma \sim W^{4\lambda(m_c^2)} \sim W^{0.8}$$

# To identify BFKL need to “neutralize” DGLAP

Ex.1: forward jet with  $k_T \sim Q$

choose  $x_j$  as large as possible,  
 $x_j \sim 0.1$ , lose small  $(x/x_j)$  “reach”

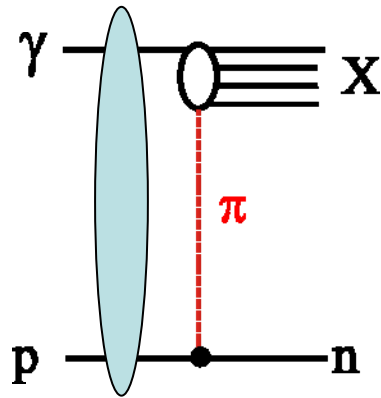


Ex. 2:  $\gamma p \rightarrow \rho Y$  at large  $t$

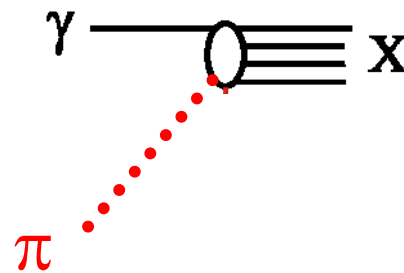
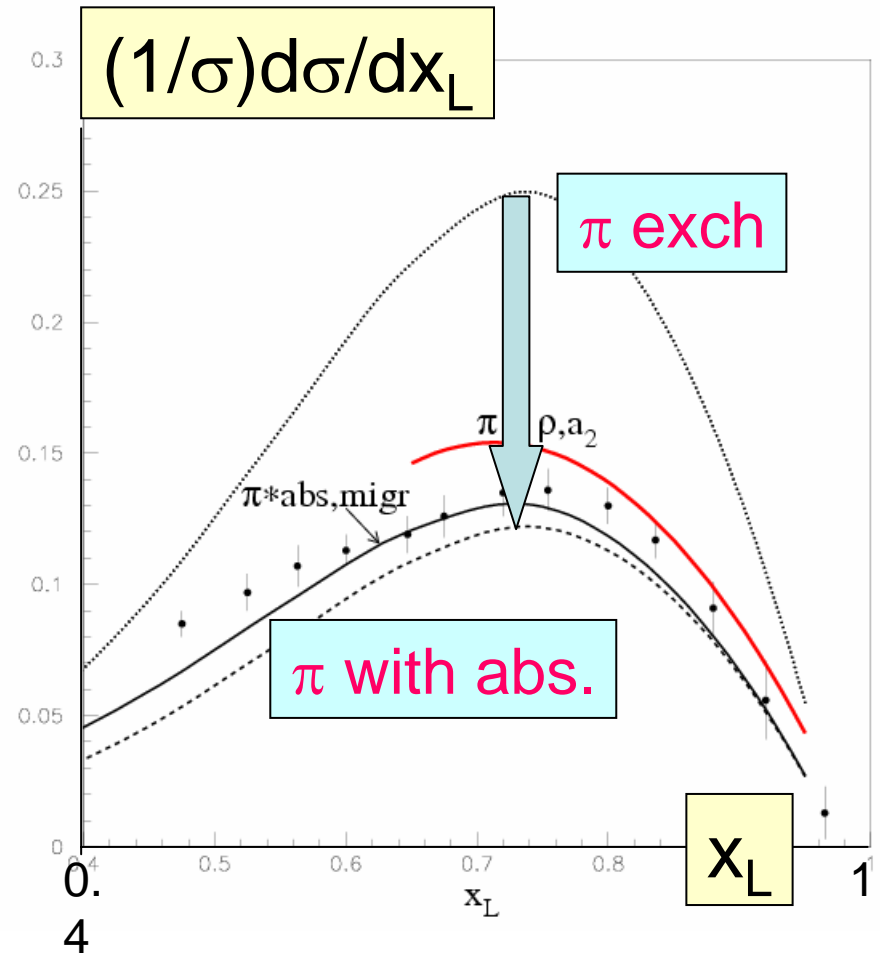
measure  $W$  dependence in a bin at large  $t$  for  $M_Y < 5$  GeV, say

# Evidence of absorptive/rescatt. effects at HERA

1. photoproduced  
**leading neutrons**  
 from ZEUS



DIS leading neutron data reveal information on the **parton distributions of  $\pi$**  in the unexplored small  $x$  domain.



2. Diffractive dijet production at HERA:

Interesting rescattering effects predicted,  
but await the final experimental (H1, ZEUS) verdict.

3. HERA data for  $\gamma p \rightarrow V p$ , with  $V = \rho, J/\psi..$ , gives an effective Pomeron slope,  $\alpha'$ , which decreases as  $Q^2+M^2$  increases --- i.e. rescatt./absorption decreases

4. Impact parameter dep. dipole description, with DGLAP evolution, of vector meson production, DVCS,  $F_2, \dots$  gives evidence of a saturation scale  $Q_s^2 < 1 \text{ GeV}^2$  in the HERA kinematical domain.



**Apologies** for omitting so  
much of HERA physics

particularly the spin and  
flavour physics coming from  
**HERMES and HERAb**

## HERA: an outsider's view

The accelerator and expts have been a tremendous success  
-----have delivered a wealth of new information,  
-----and exceeded the expectations in precision

Greatly illuminates QCD, especially the structure of the  
proton, Pomeron, photon, pion

Unique probe of the important small  $x$  domain

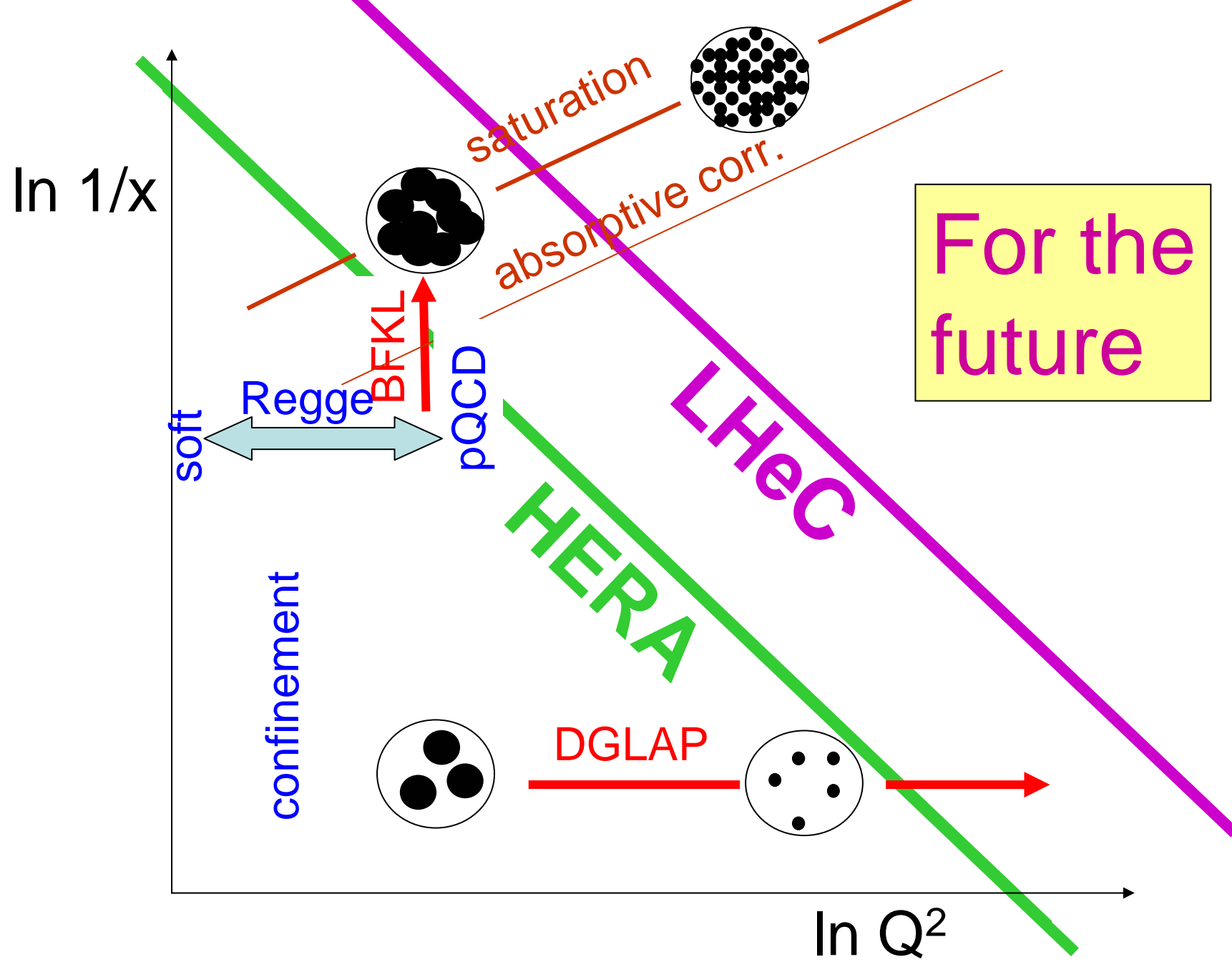
Much of the data is well ahead of theory---much still to be learnt

### Impact for LHC

1. HERA measurements, via parton distributions, essential for predictions of event rates at the LHC.
2. Studies of diffraction at HERA, particularly of the survival probabilities of rapidity gaps, allow rescattering effects to be quantified. Use this to determine these effects at the LHC.



Still lots of HERA data sought after by theorists



Many congratulations to **all**  
who have worked at HERA

**H**ighly  
**E**xceptional  
**R**esearch  
**A**chievement

