

A New Method for Event Reconstruction in Large Cherenkov Detectors

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New Directions in Neutrino Physics

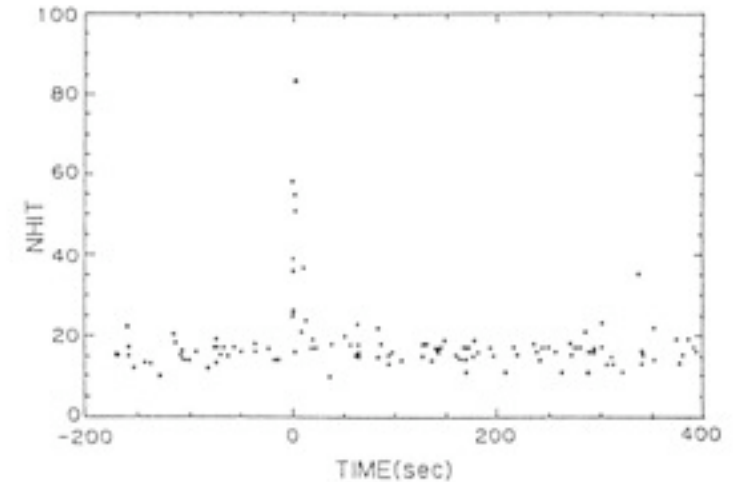
Aspen, CO

4-Feb-2013

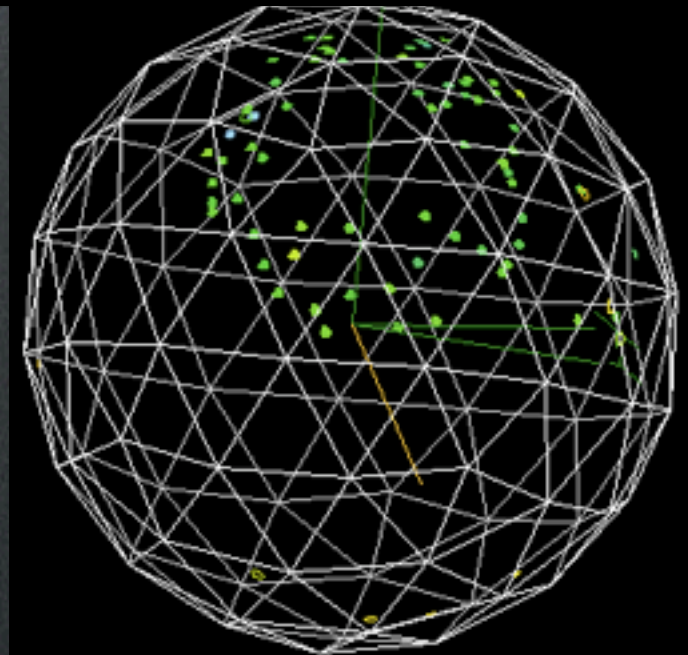
Physics Applications

- Search for proton decay
- Supernovae
 - SN burst
 - Relic SN background
- Neutrino physics
 - Solar neutrinos
 - Atmospheric neutrinos
 - Accelerator neutrinos
 - High-Energy astrophysical neutrinos
 - ...
- Broad physics reach
 - Much to be gained from better utilizing this technology

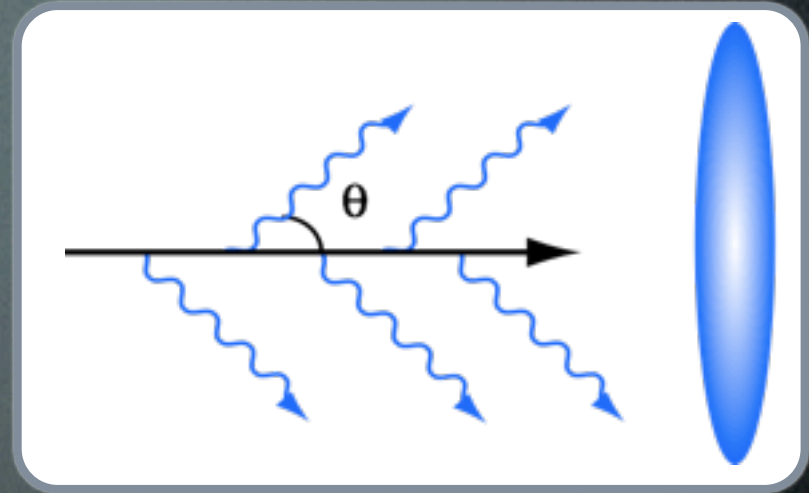
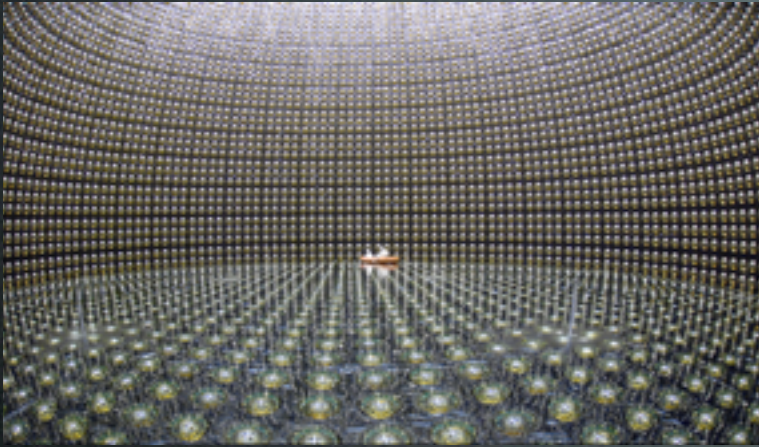
Kamiokande SN 1987a Signal



SNO Single-Electron Event



The Super-K Detector



- 50 kton water Cherenkov detector

- **μ^\pm detection**

- Less scattering \Rightarrow sharp rings

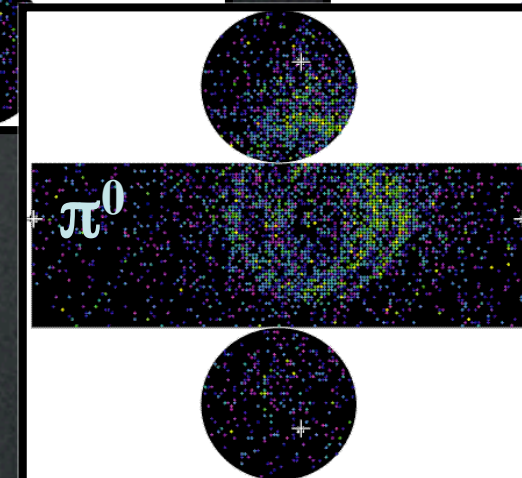
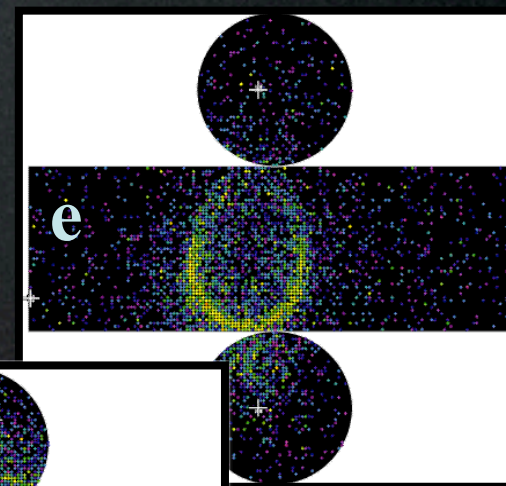
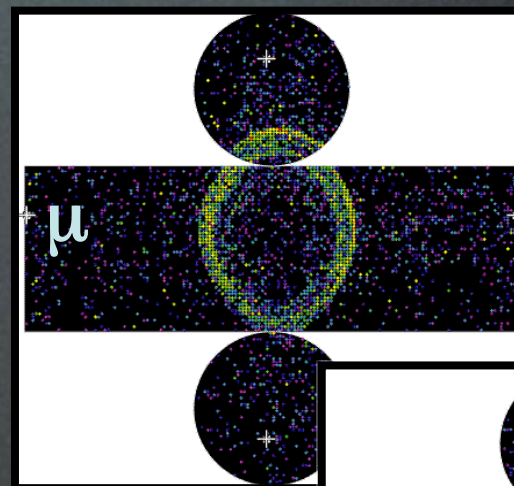
- **e^\pm detection**

- More scattering \Rightarrow fuzzy rings

- **π^0 detection**

- 2 electron rings ($\pi^0 \rightarrow 2\gamma$)

- To separate from electrons, **MUST** detect 2nd ring



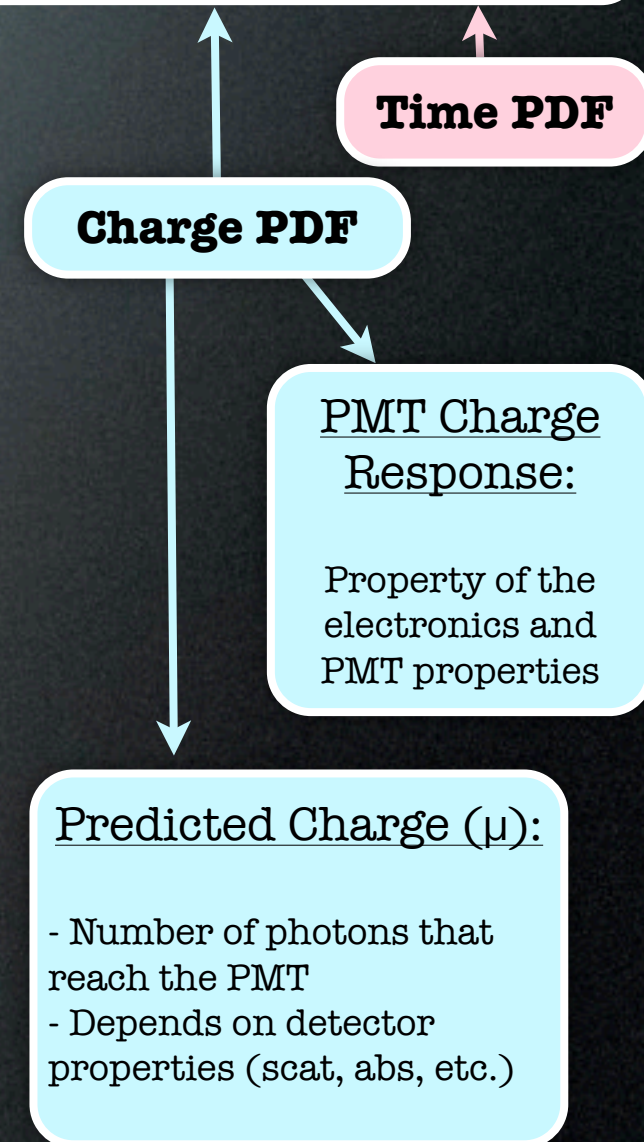
fiTQun: A New Event Reconstruction Algorithm for Super-K

- For each Super-K event we have, for every hit PMT
 - **A measured charge**
 - **A measured time**
- For a given event topology hypothesis, it is possible to produce a **charge and time PDF for each PMT**
 - Based on the likelihood model used by MiniBooNE (NIM A608, 206 (2009))
- Framework can handle **any number of reconstructed tracks**
 - Same fit machinery used for all event topologies (e.g. e^- and π^0)
- Event hypotheses are distinguished by **comparing best-fit likelihoods**
 - electron / π^0
 - electron / muon / π^+ / K^+ / p / ...
 - 1-ring / 2-ring / 3-ring ...

The Likelihood Fit

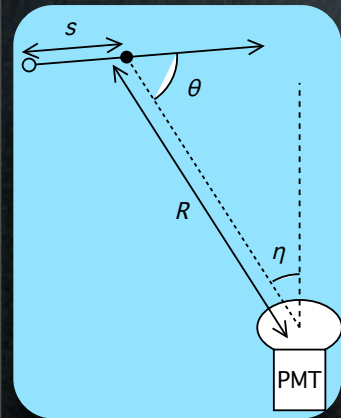
$$L(\mathbf{x}) = \prod_{\text{unhit}} P(i_{\text{unhit}}; \mathbf{x}) \prod_{\text{hit}} P(i_{\text{hit}}; \mathbf{x}) f_q(q_i; \mathbf{x}) f_t(t_i; \mathbf{x})$$

- A single track can be specified by a **particle type**, and **7 kinematic variables** (represented above as the vector \mathbf{x}):
 - A vertex position **(X, Y, Z, T)**
 - A track momentum **(p)**
 - A track direction **(θ, φ)**
- For a given \mathbf{x} , a charge and time PDF is produced for every PMT
- The **charge PDF** is factorized into:
 - Number of photons reaching the PMT
 - **Predicted charge (μ)**
 - PMT & electronics response
- All 7 track parameters **fit simultaneously**



Predicted Charge (μ)

Cherenkov light emission profile



$$\mu^{\text{dir}} = \Phi(p) \int ds g(s, \cos \theta) \Omega(R) T(R) \epsilon(\eta)$$

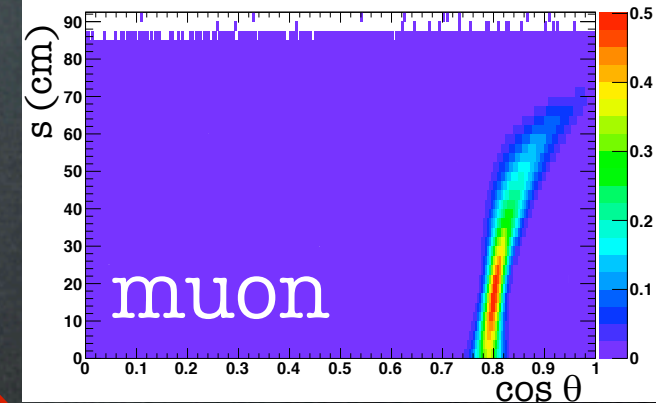
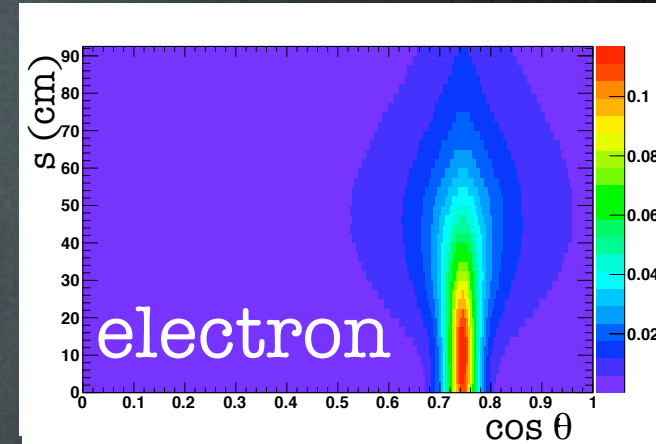
Light Yield

Integral over track length

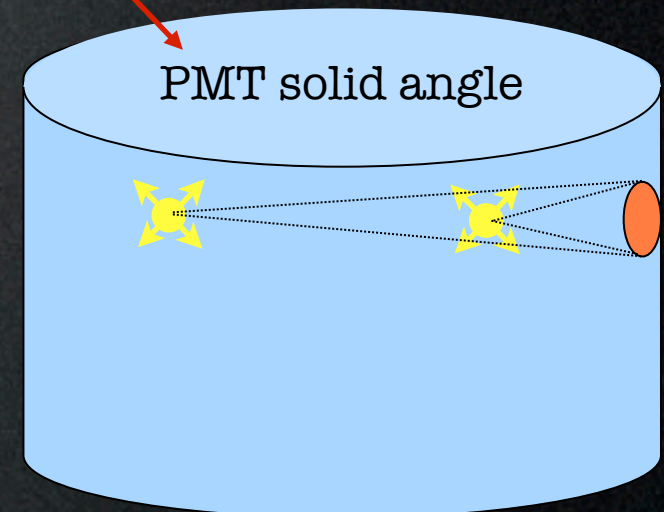
PMT solid angle

Water attenuation

PMT angular response



- ❖ μ^{dir} is the predicted charge due to “direct light” only (scattered light is handled separately)
- ❖ μ is an integral over the length of the track (parameterized by the momentum, p)
- ❖ Cherenkov light emission is characterized by $g(s, \cos \theta)$
 - ❖ These functions must be generated separately for each particle type
 - ❖ All particle ID comes from these distributions
- ❖ Ω , T , and ϵ depend on the geometry and detector properties
 - ❖ Can be used for all particle hypotheses

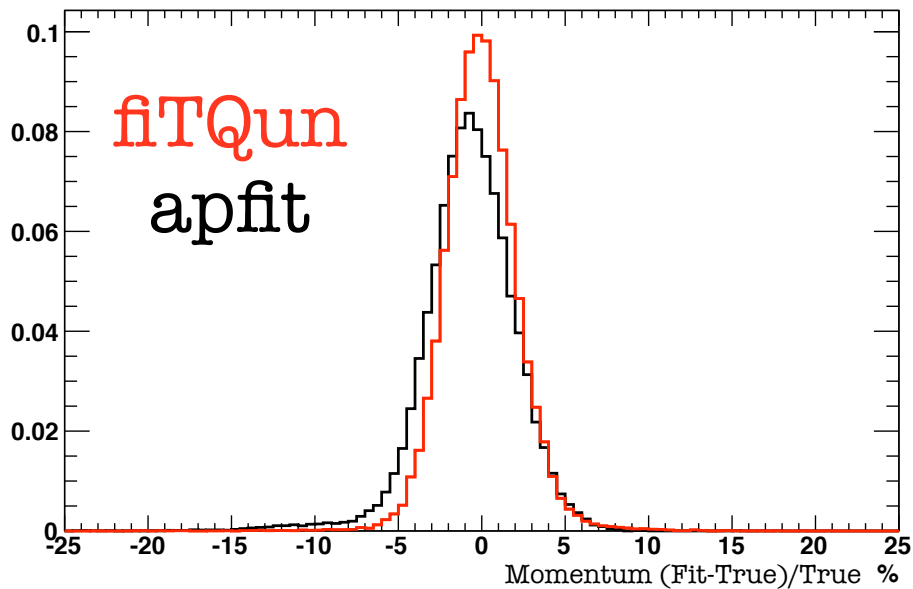


One-Track Fit Performance

Shown with default Super-K
reconstruction, **apfit**, for comparison

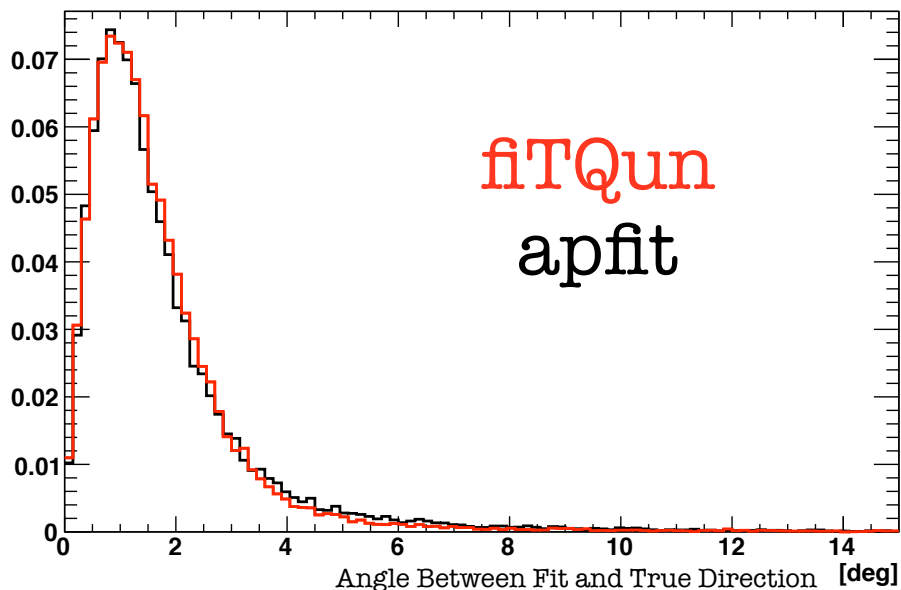
Muons

Momentum

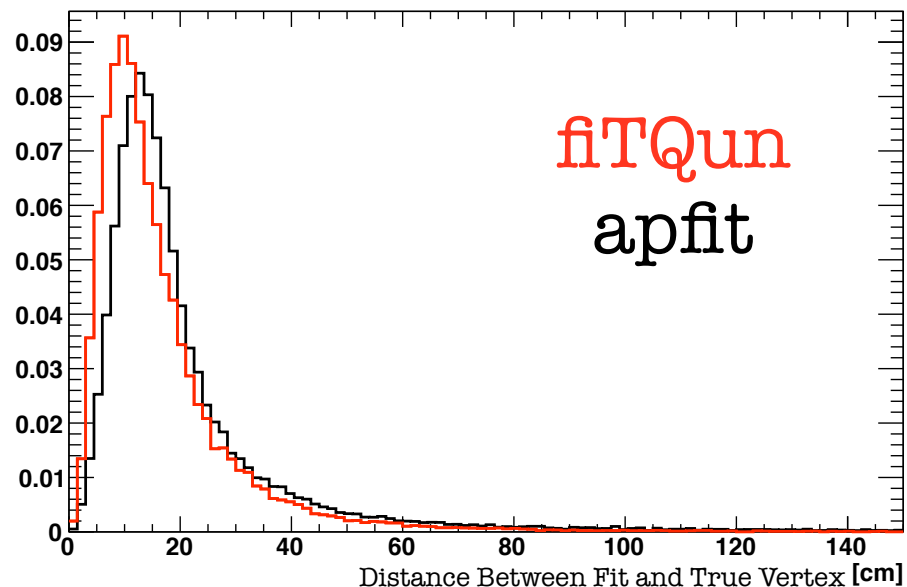


- Tested on a uniform distribution of muons between 0 and 1 GeV/c
- Isotropic & random position (inside FV & charge > 200pe)
- Significant improvements in the vertex and momentum resolution

Angle

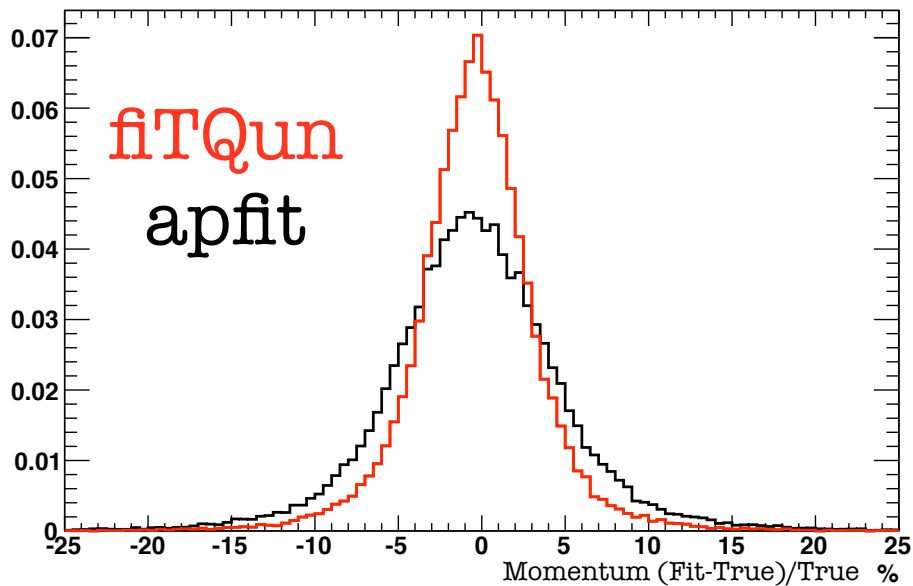


Vertex



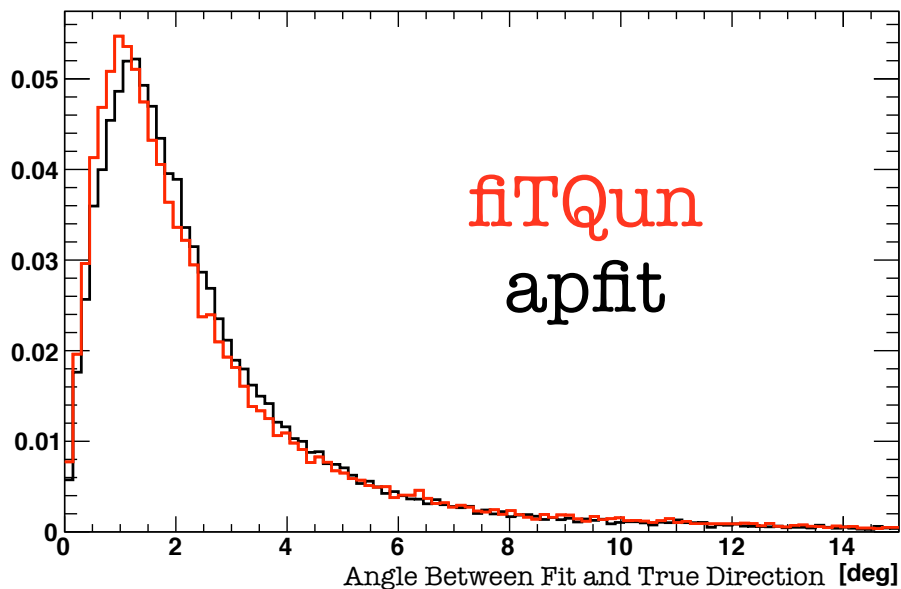
Electrons

Momentum

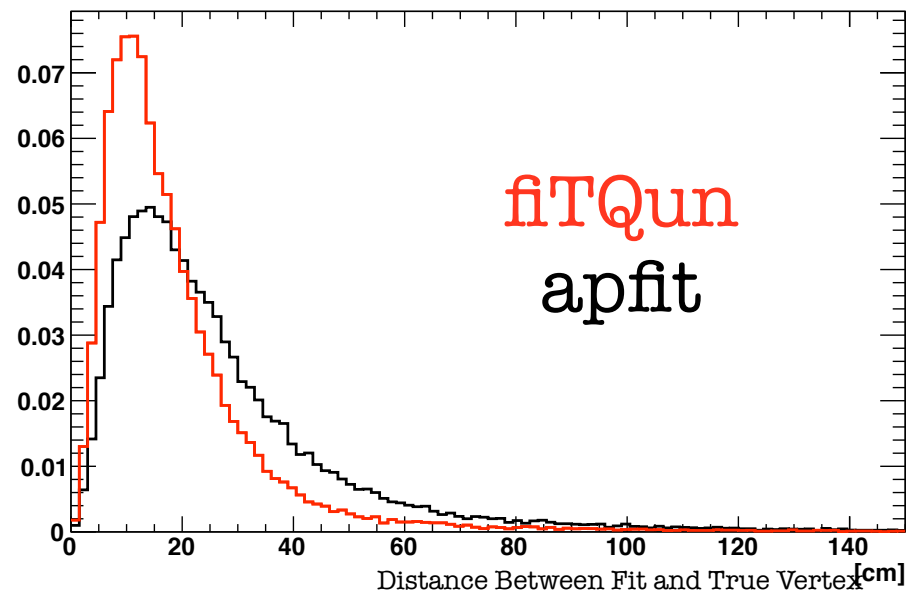


- Tested on a uniform distribution of e^- between 0 and 1 GeV/c
- Isotropic & random position (inside FV & charge > 200pe)
- Significant improvements in the vertex and momentum resolution

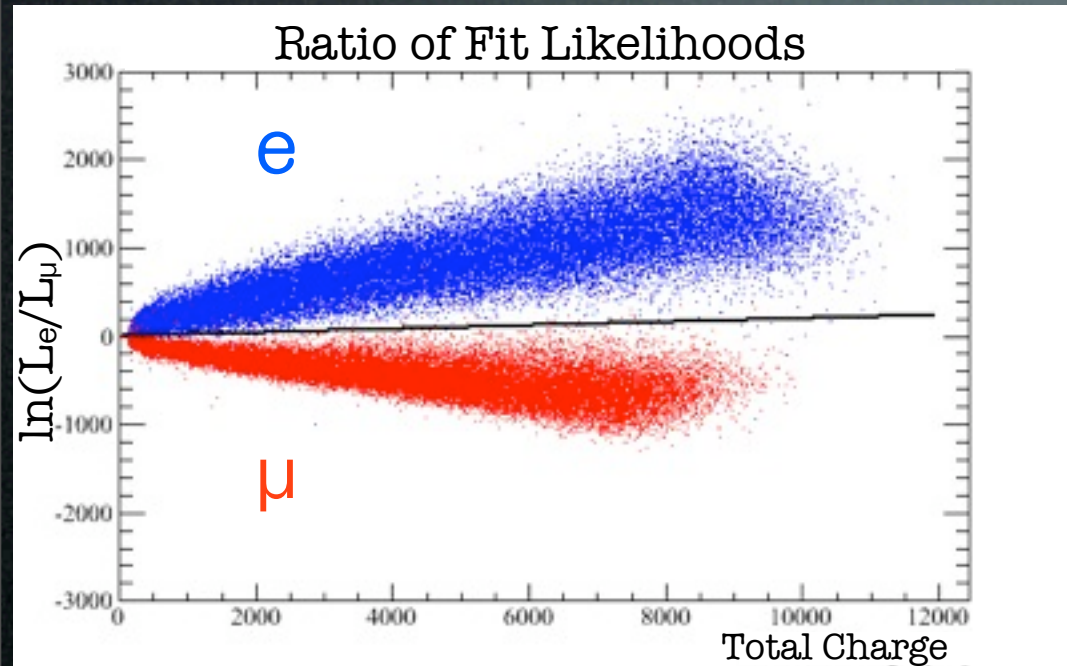
Angle



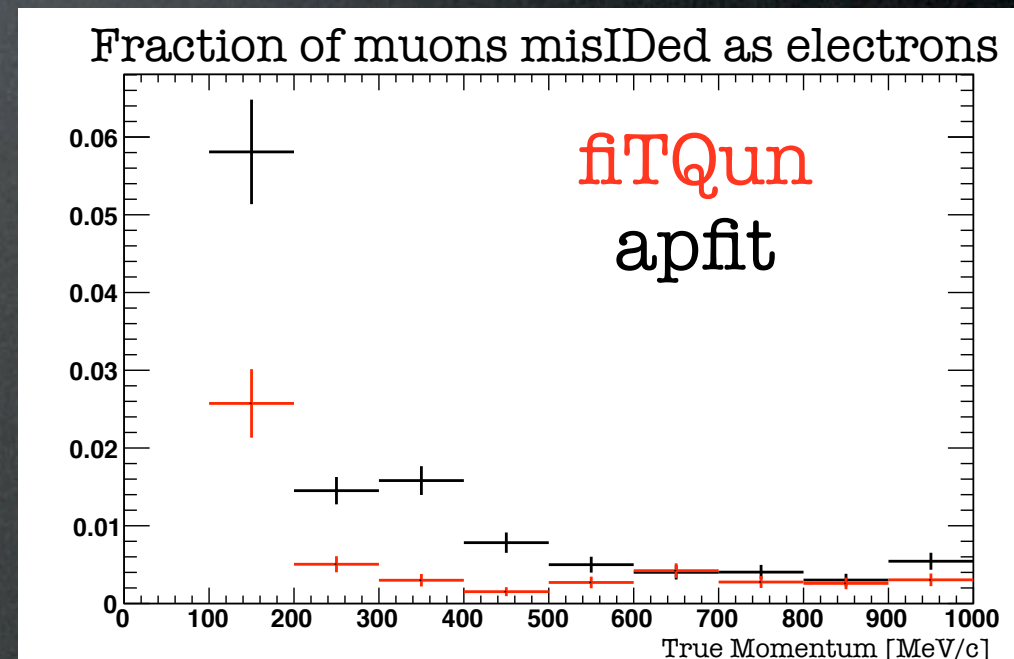
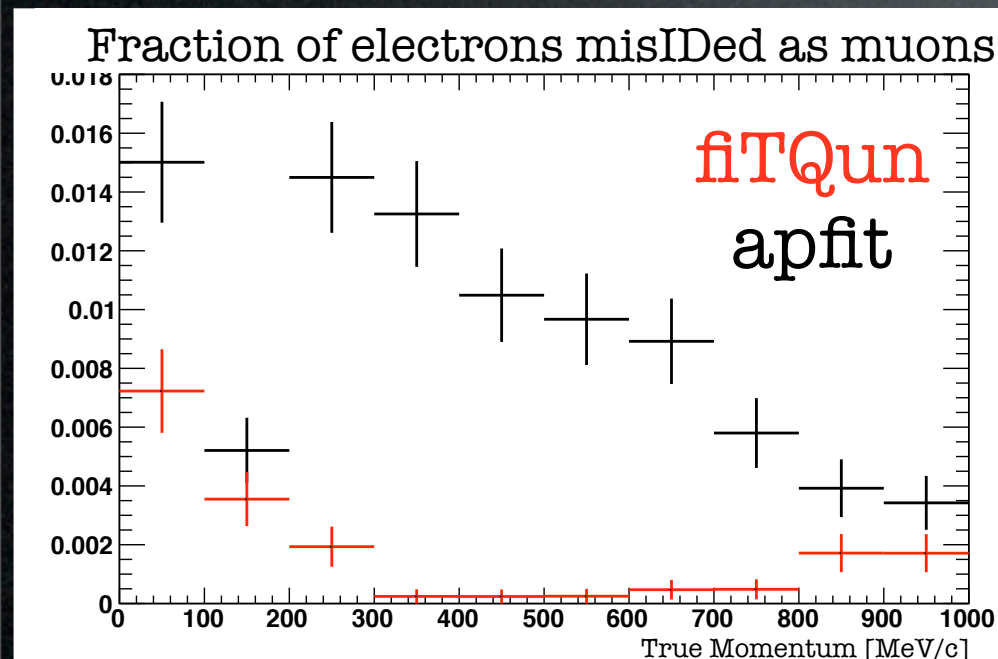
Vertex



Single Track Particle ID

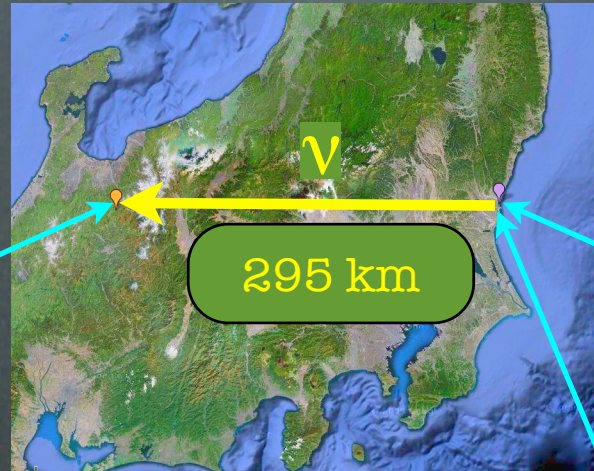
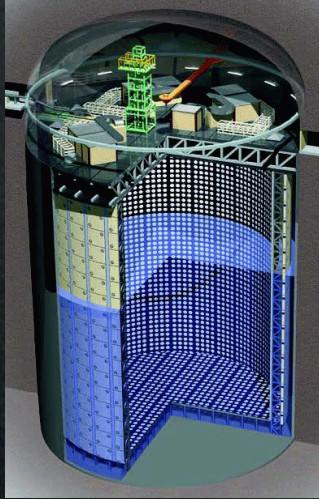


- Simple line cut can be used to separate muons and electrons
- Significantly improved particle ID



Test Case: The T2K Experiment

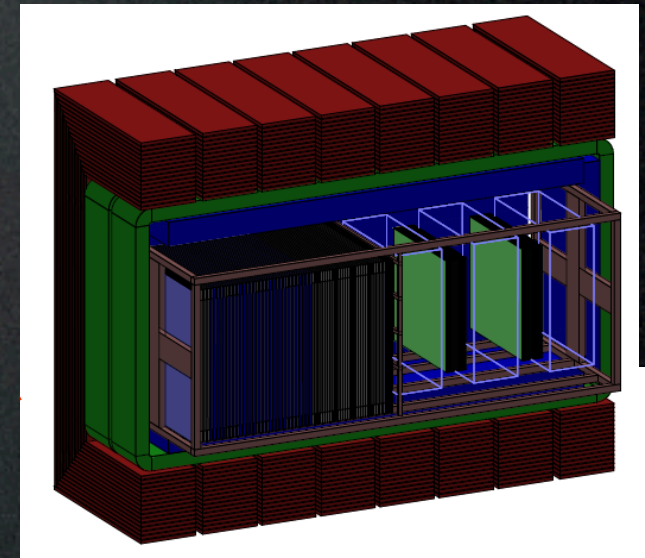
Super-K Detector



J-PARC Accelerator



Near Detector

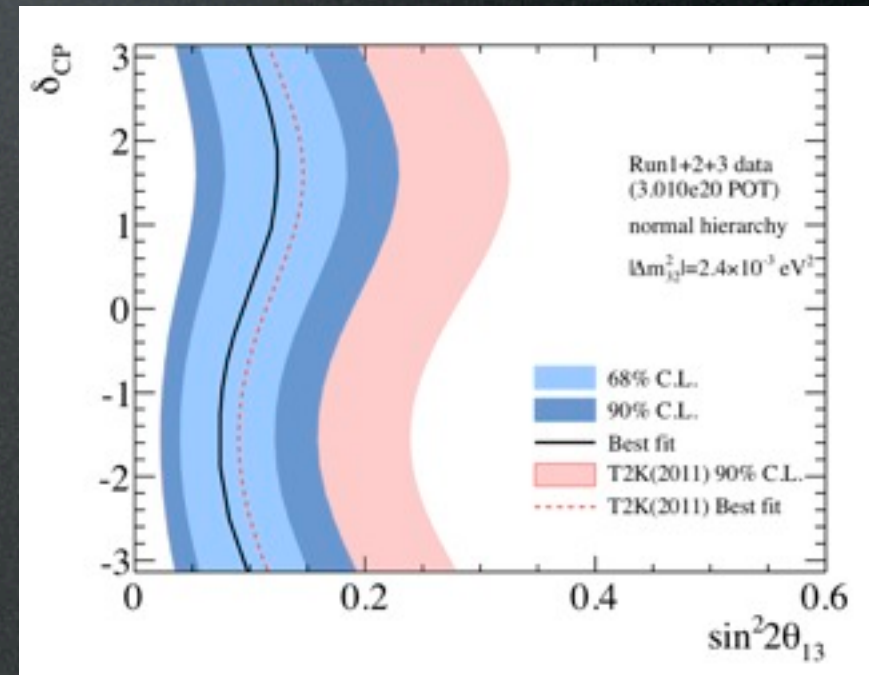
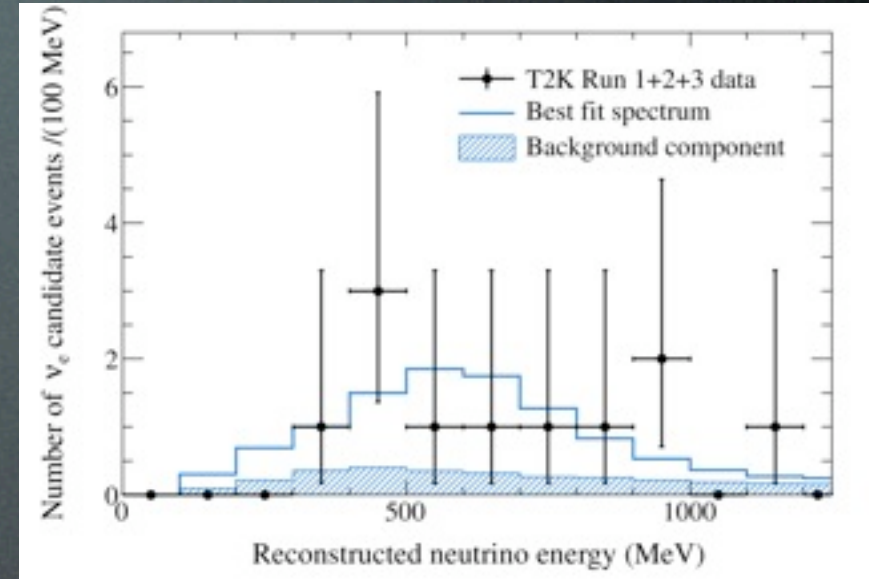


- The T2K experiment searches for neutrino oscillations in a high purity ν_μ beam
- A near detector located 280 m downstream of the target measures the unoscillated neutrino spectrum
- The neutrinos travel 295 km to the Super-Kamiokande water Cherenkov detector
 - For **θ_{13} search**: Super-K looks for the **appearance of ν_e**
 - For **θ_{23} measurement**: The ν_μ at the near and far detectors are compared to search for **ν_μ disappearance**

Latest T2K ν_e Results (2012)

- 11 events observed
- $\sin^2 2\theta_{13} = 0.094^{+0.053}_{-0.040}$
- **3.2 σ** exclusion of $\theta_{13}=0$

- 3.22 ± 0.43 background events
 - 1.56 ± 0.20 **intrinsic beam ν_e**
 - **Irreducible**
 - 1.26 ± 0.35 ν_μ neutral current (**mostly π^0**)
 - **Reducible?**



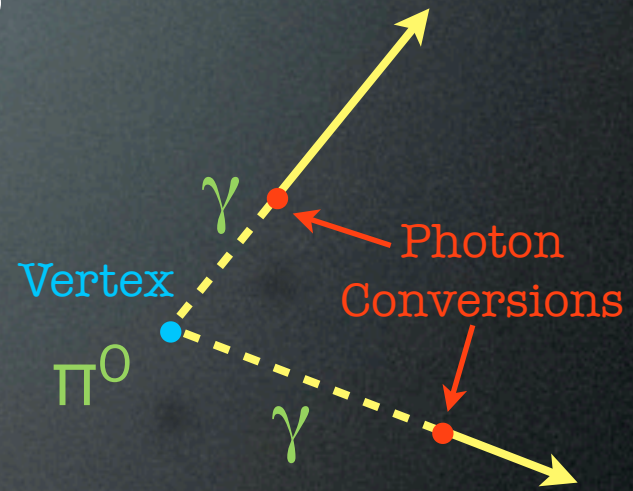
Background Reduction

40% of the ν_e appearance background is from π^0 where the 2nd photon was missed

Can fitQun do better?

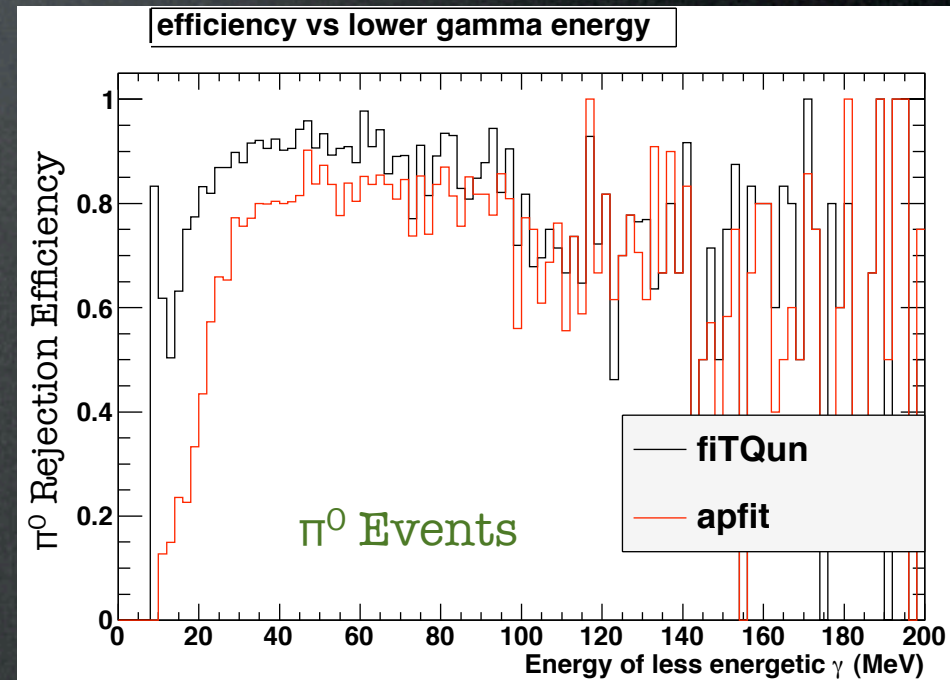
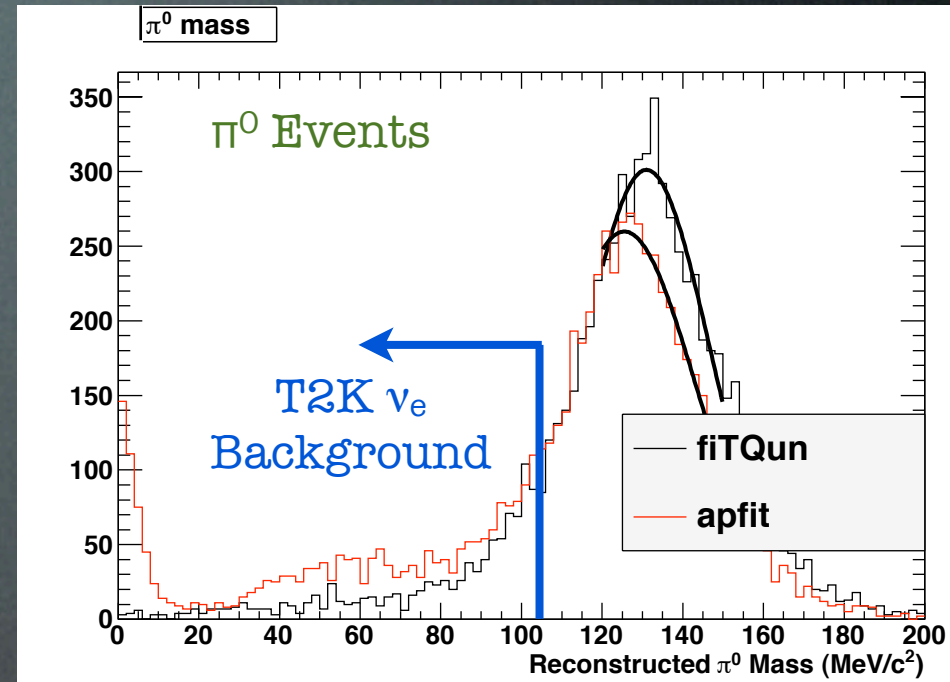
fiTQun π^0 Fitter

- Assumes two electron hypothesis rings produced at a common vertex
- **12 parameters** (single track fit had 7)
 - Vertex (X, Y, Z, T)
 - Directions ($\theta_1, \phi_1, \theta_2, \phi_2$)
 - Momenta (p_1, p_2)
 - Conversion lengths (c_1, c_2)
- **Seeding the fit**
 - Use result of single-track electron fit
 - Scan over various directions with a 50 MeV/c electron and evaluate the likelihood function
 - Choose the direction that yields the best likelihood
 - First, fit while floating only p_1 and p_2
- **Do full 12 parameter fit**



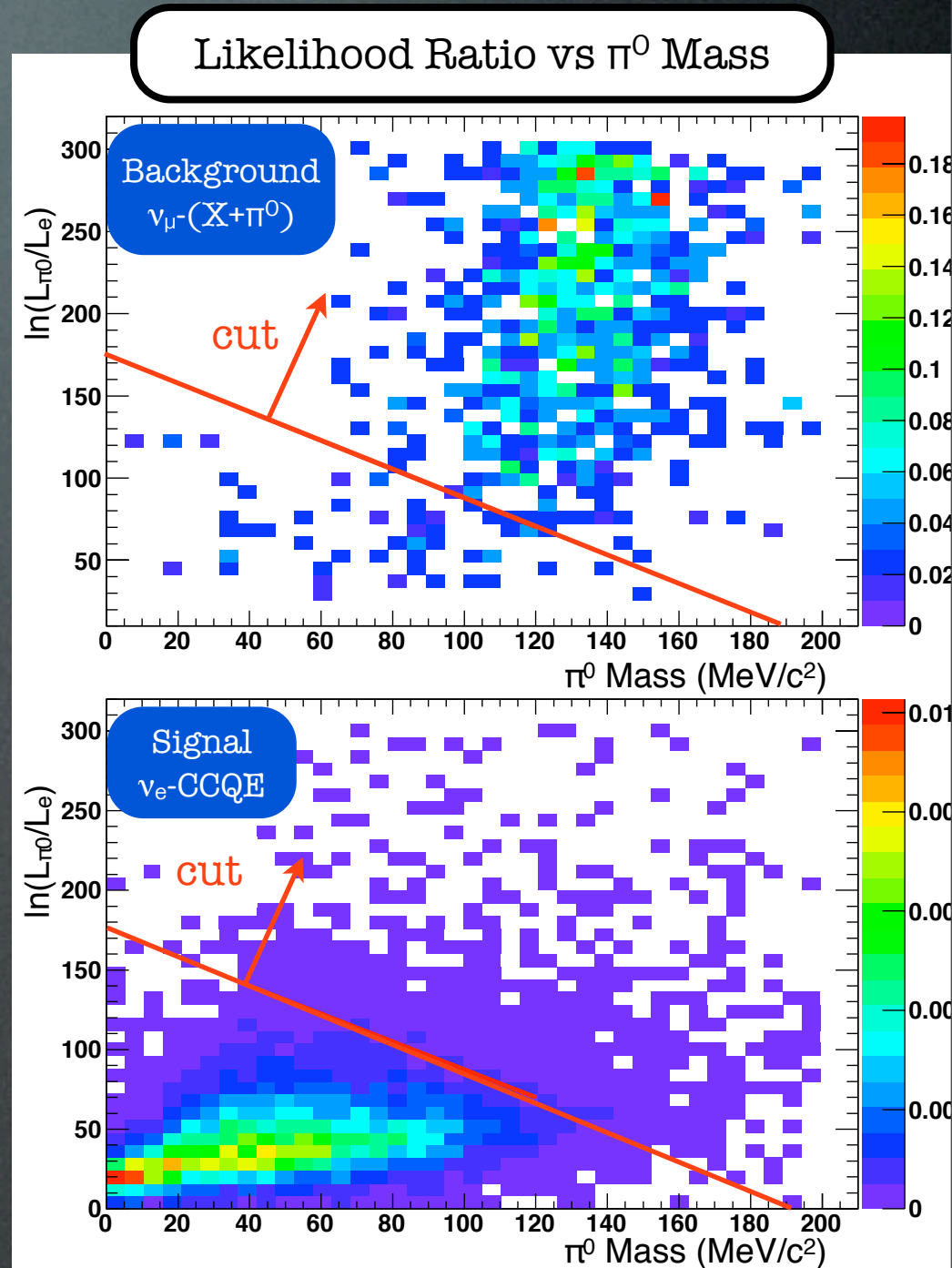
π^0 Performance

- T2K ν_e appearance cut:
 $m_{\pi^0} < 105 \text{ MeV}$
- The π^0 mass tail is much smaller for fiTQun
 - Significant spike at zero mass in standard fitting algorithm (**apfit**)
 - **All events in the spike are background**
 - **fiTQun shows no spike**
- Lower plot:
 π^0 rejection efficiency vs **lower γ energy**
 - fiTQun is more sensitive to lower energy photons



Even Better π^0 Rejection

- fitQun can also use the **likelihood ratio** to distinguish e^- from π^0
 - Even if 2nd photon is identified, it may be on the tail of the π^0 mass resolution
 - In this case, the 2-ring likelihood will still be preferred
- 2D cut **removes 75% more π^0 background**
 - For the same electron signal efficiency



Effect on ν_e Appearance

- π^0 background has **>30% error (flux + cross section)**
 - Error on **beam ν_e** background is only **$\sim 12\%$**
- Background due to π^0 is reduced by $\sim 75\%$

For 3.01×10^{20} POT	fiTQun	apfit
# π^0 bkgd	0.29	1.13
# Total bkgd	1.94 ± 0.24	2.93 ± 0.46

- Total background is reduced by 33%
 - More importantly, **background error is halved**
 - Significant improvement in $\sin^2 2\theta_{13}$ sensitivity
- Other fiTQun improvements (e.g. e^- PID, ring counting) improve the sensitivity further

Other fitQun Tools: π^+ Fitter

electron tracks



muon tracks

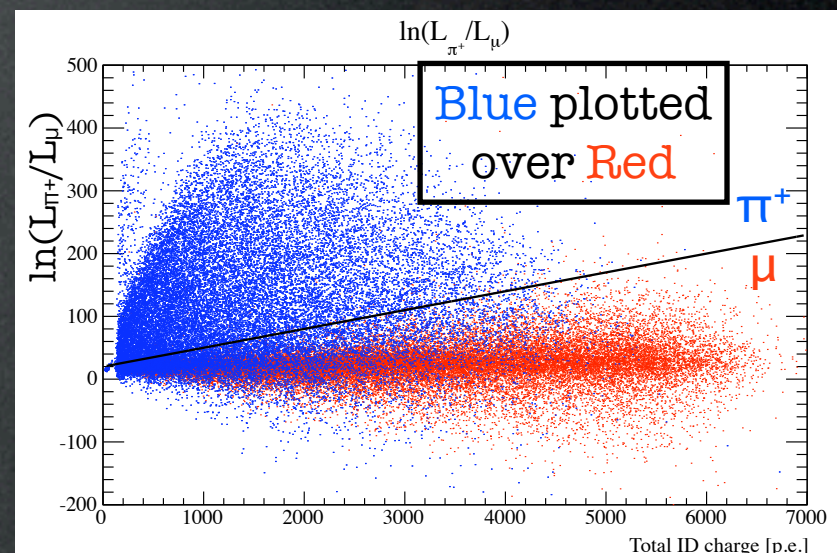
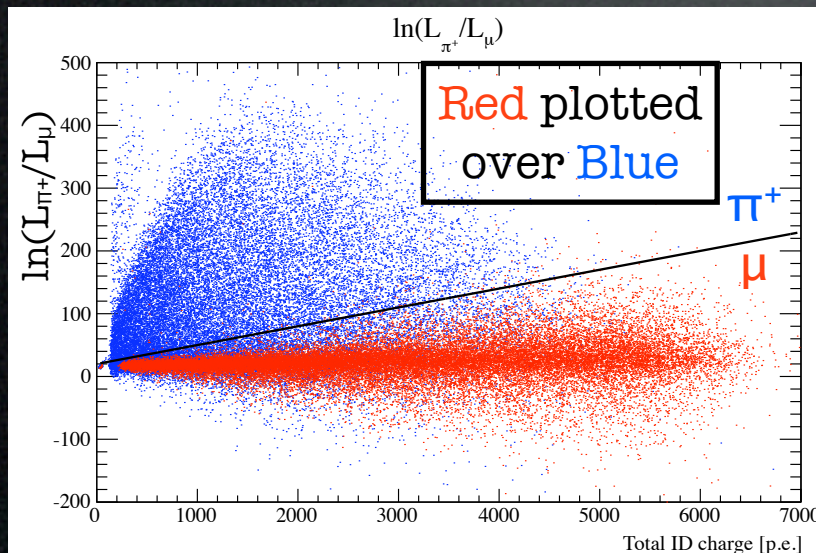


pion tracks



- Pions and muons have **very similar Cherenkov profiles**
 - Main difference is the **hadronic interactions** of pions
- Ring pattern observed is a **“kinked” pion trajectory** (thin ring with the center portion missing)
- π^+ tracks have never been reconstructed before at Super-K

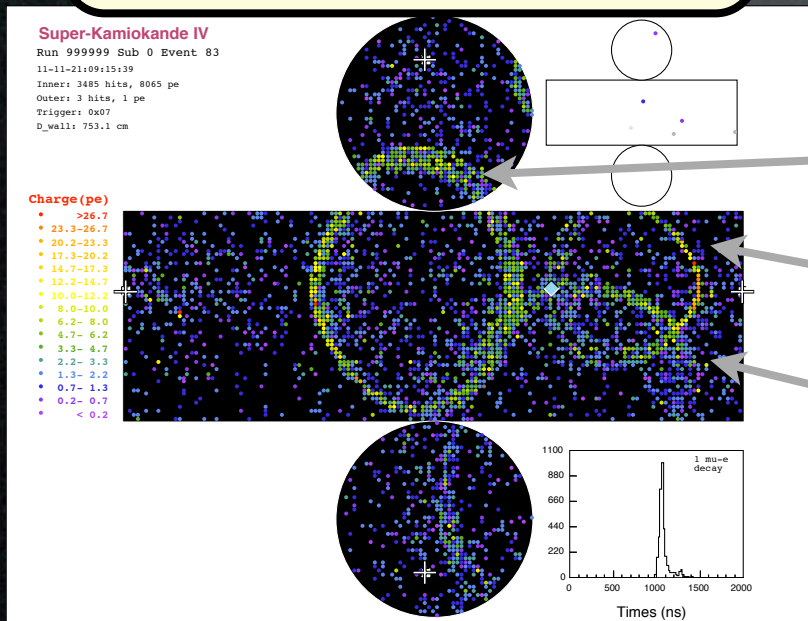
μ & π^+
particle
gun



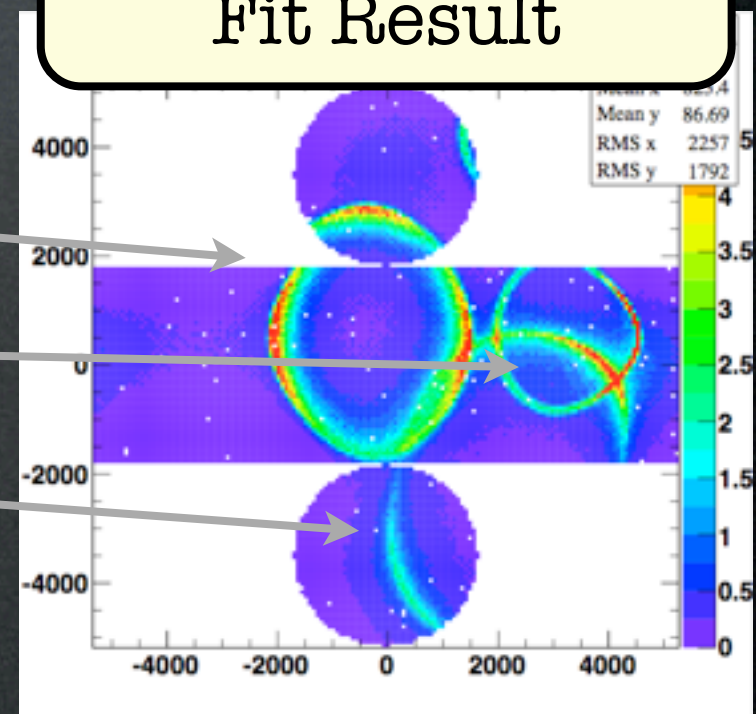
Other Tools: Multi-ring Fitter

- **Fit up to 4 rings** using e & π^+ hypotheses
- 28 fits in total (every possible e/π^+ combination)
- μ hypothesis is a subset of the π^+ hypothesis
- Just need to move the kink point below Cherenkov threshold

Event Display



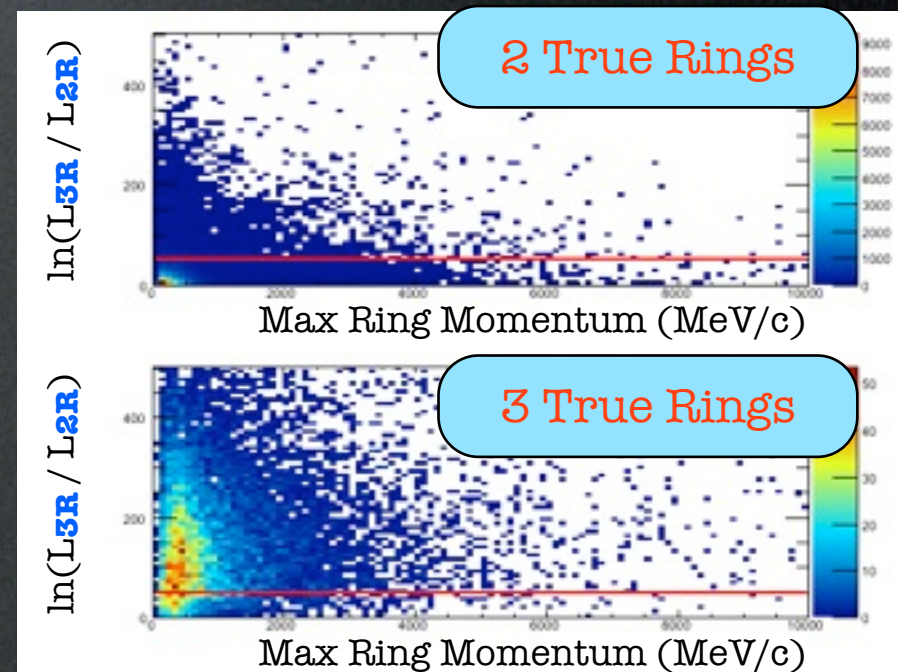
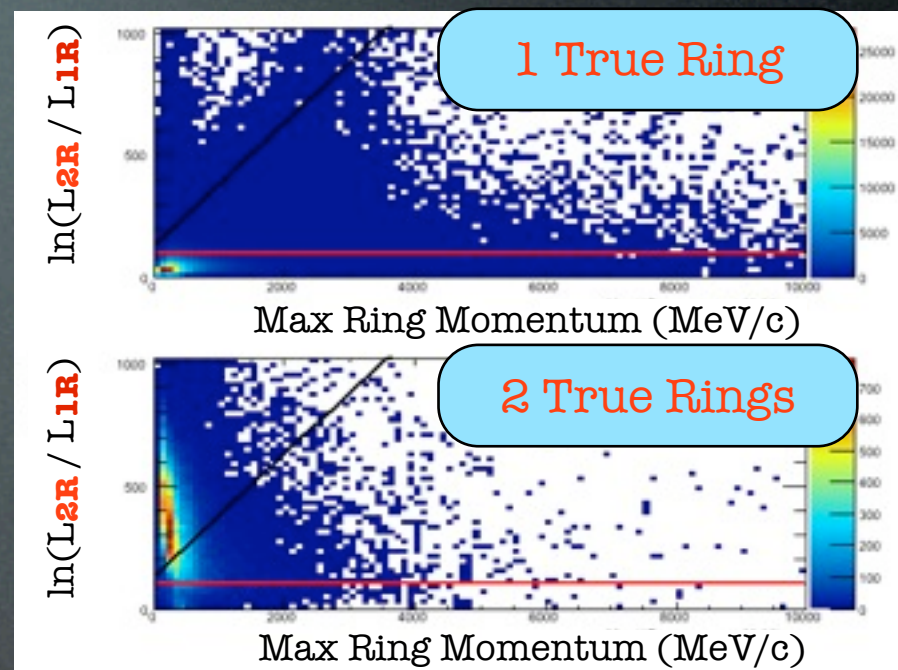
Fit Result



μ
 π^+
 e

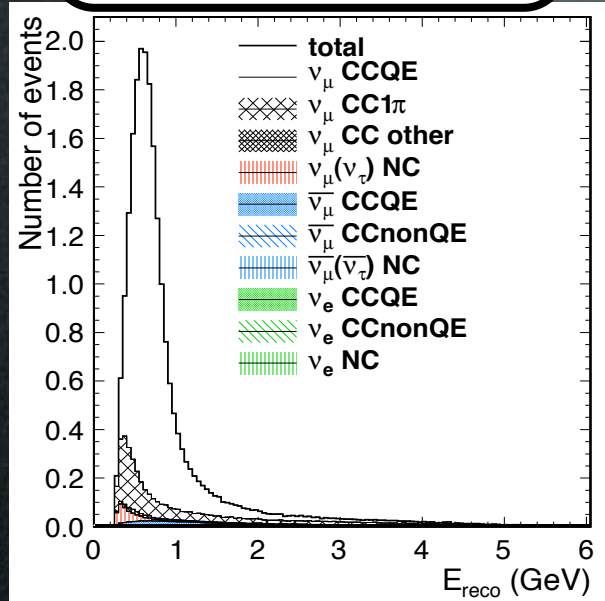
Ring Counting

- Compare best **(n)-ring** likelihood to best **(n+1)-ring** likelihood
 - Ring counting now depends on particle ID
- Can test performance on atmospheric neutrino sample
 - Higher energy neutrinos = **more rings**
 - Define a “true ring”
 - Any particle >10 MeV/c above Cherenkov threshold
- Good performance seen up to 4 rings



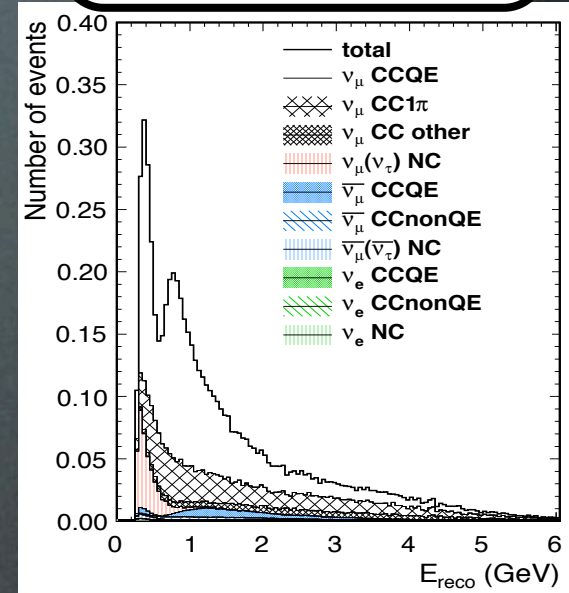
T2K ν_μ Disappearance

Unoscillated Number of events at Super-K



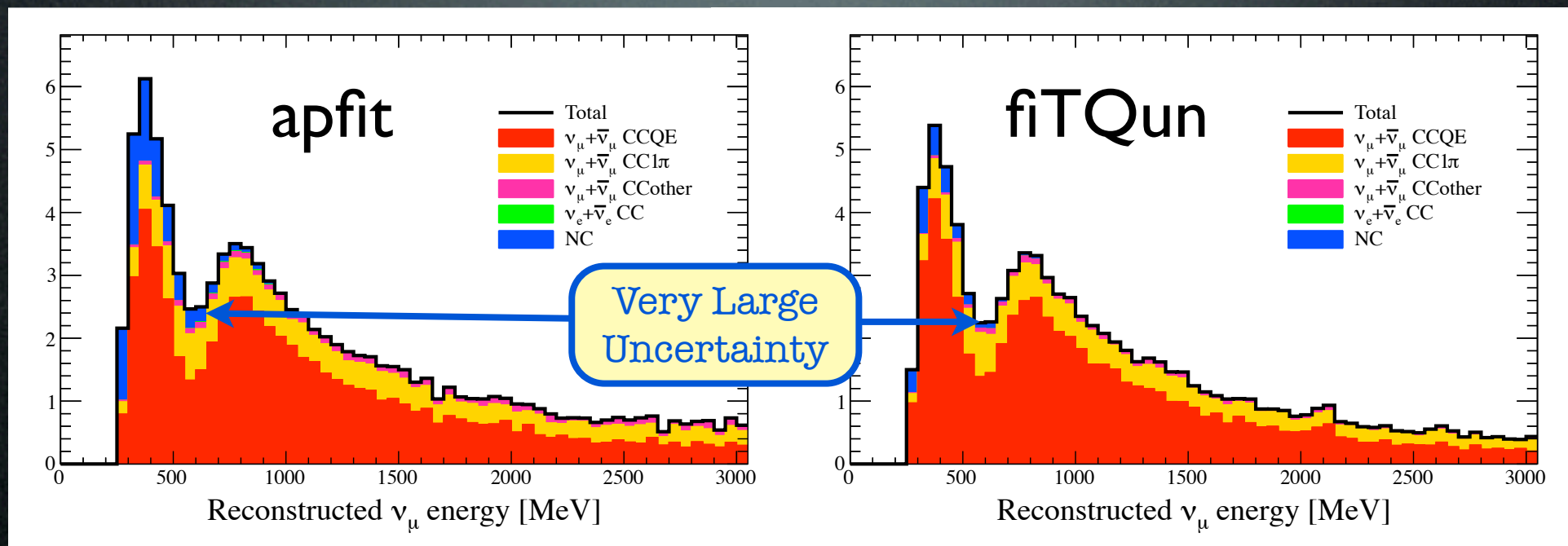
oscillation

$\sin^2(2\theta_{23})=1$
 $\Delta m_{32}^2=2.4 * 10^{-3} \text{ eV}^2/c^4$



- Largest backgrounds are from $\text{CC}\pi^+$ and $\text{NC}\pi^+$
 - **$\text{NC}\pi^+$** : pion is misidentified as a muon
 - Super-K reconstruction **uncertainty on π^+ is large (>100%)**
 - **$\text{CC}\pi^+$** : pion is unobserved
 - The fitQun can now reconstruct π^+
 - If properly reconstructed, **$\text{CC}\pi^+$ can be treated as signal**

ν_μ Selection: fitQun vs apfit



Fraction of apfit selected events removed:

$\nu_\mu + \bar{\nu}_\mu$ CCQE	4.8%
$\nu_\mu + \bar{\nu}_\mu$ CC1 π	21.5%
$\nu_\mu + \bar{\nu}_\mu$ CCothers	53.7%
$\nu_e + \bar{\nu}_e$ CC	92.1%
NC	61.2%

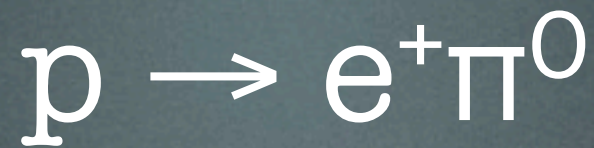
- fitQun signal efficiency is higher below 1 GeV
- Significant reduction of NC background due to π^+ rejection
- **N π^+ background has a very large uncertainty (>100%)**
 - N π^+ piles up near the oscillation dip
- Expect significant enhancement in **θ_{23} and Δm^2_{32} sensitivity**

Other Uses for fiTQun

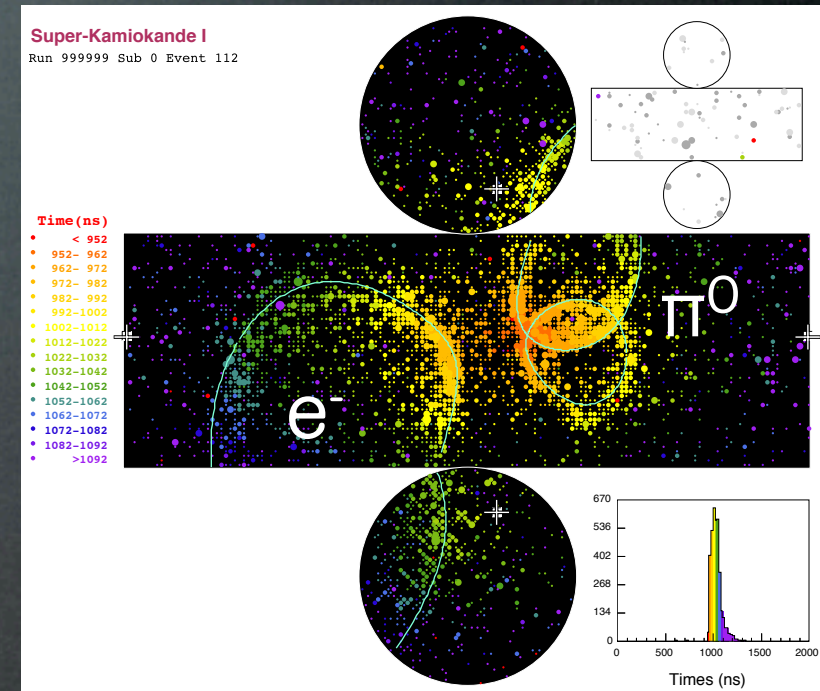
In principle, any Super-K physics analysis can benefit from fiTQun

Particularly, Proton Decay

Reconstruction requirements are very similar to T2K ν_e appearance requirements



- 45% reconstruction efficiency with current Super-K tools
 - Selection allows for 2- or 3-ring reconstructed rings
- fitQun has **improved identification of faint photon rings**
 - Should **improve signal efficiency** (for 3-ring events)
 - Analogous to T2K π^0 search
- Improved electron resolution
 - Better constraints on momentum balance and reconstructed π^0 and p masses
 - Can tighten cuts to improve background rejection

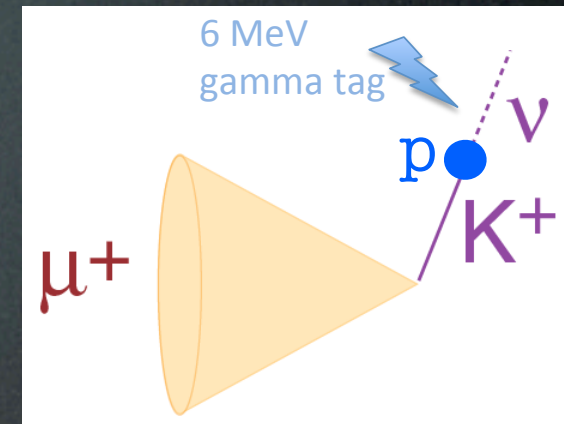




- Search via the largest two K^+ decay channels

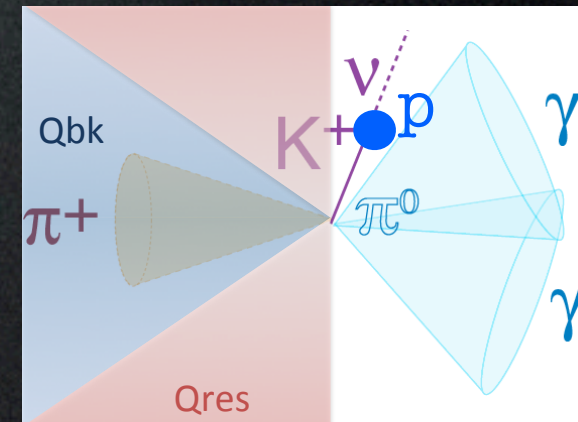
- $K^+ \rightarrow \mu^+ \nu_\mu$**

- Search for a mono-energetic muon
 - fiTQun has improved muon momentum resolution
- Search for **6 MeV photon** from nuclear de-excitation
 - Very low energy \rightarrow current algorithm is very inefficient
 - Only 6.4% efficiency** (44% have a nuclear photon)
 - Large potential improvement** if low-energy photon detection can be improved

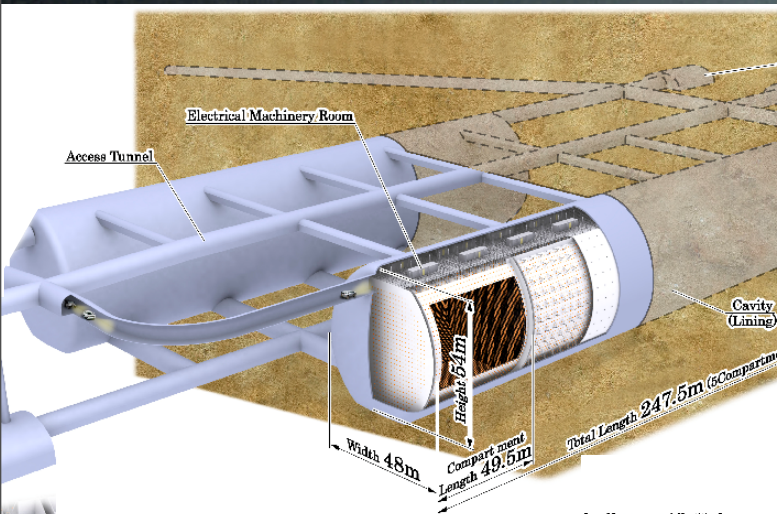


- $K^+ \rightarrow \pi^+ \pi^0$**

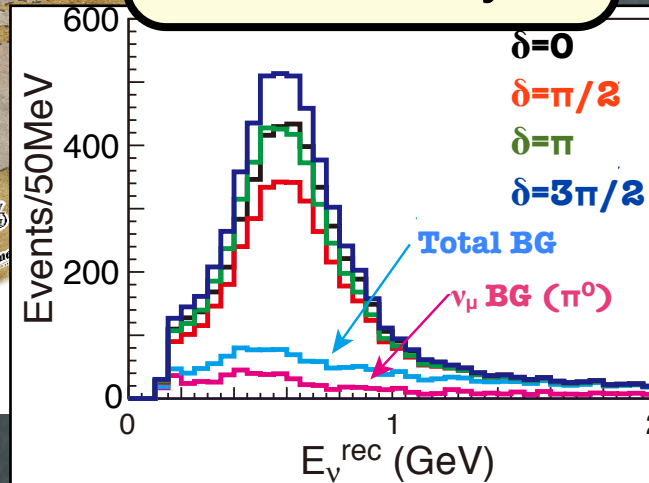
- No previous ability to reconstruct π^+**
 - Instead, sum charge in 40 degree cone opposite the π^0 direction
 - veto on any other charge in the event
- fiTQun can reconstruct charged pions**
 - Can also do **simultaneous $\pi^+ \gamma \gamma$ fit** and compare likelihood with background hypotheses



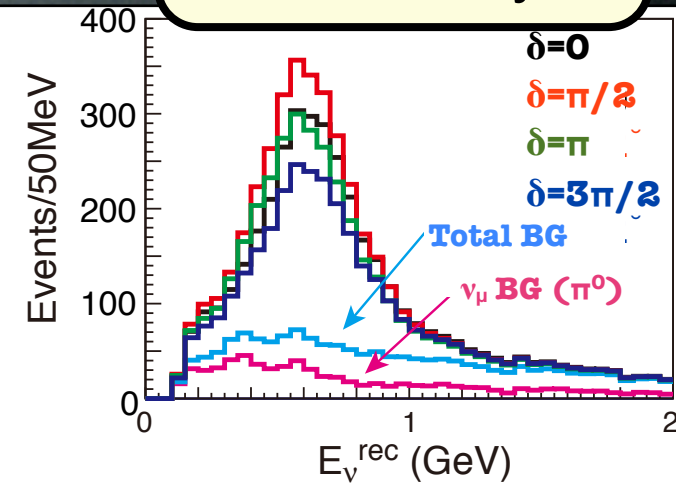
Future Experiments: Hyper-K



ν 0.75M×3yrs



$\bar{\nu}$ 0.75M×7yrs

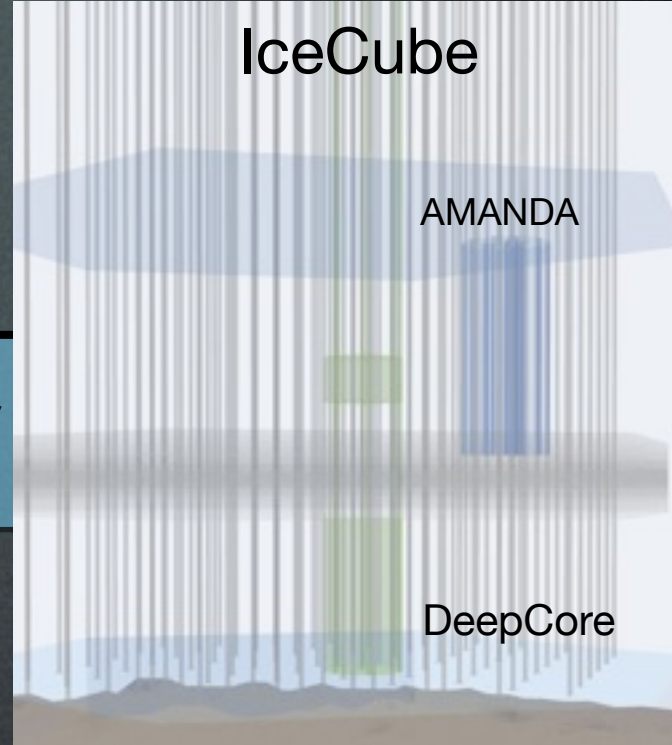


- 0.99 Mton of water ($\sim 25 \times$ Super-K fiducial volume)
- Physics goals include proton decay, δ_{CP} , θ_{23} octant, SN- ν , ...
- Same detector design, neutrino beam, backgrounds, etc. as Super-K/T2K
 - Expect similar improvements in performance
- fiTQun has recently been adapted to the Hyper-K software

IceCube, DeepCore, Pingu, MICA

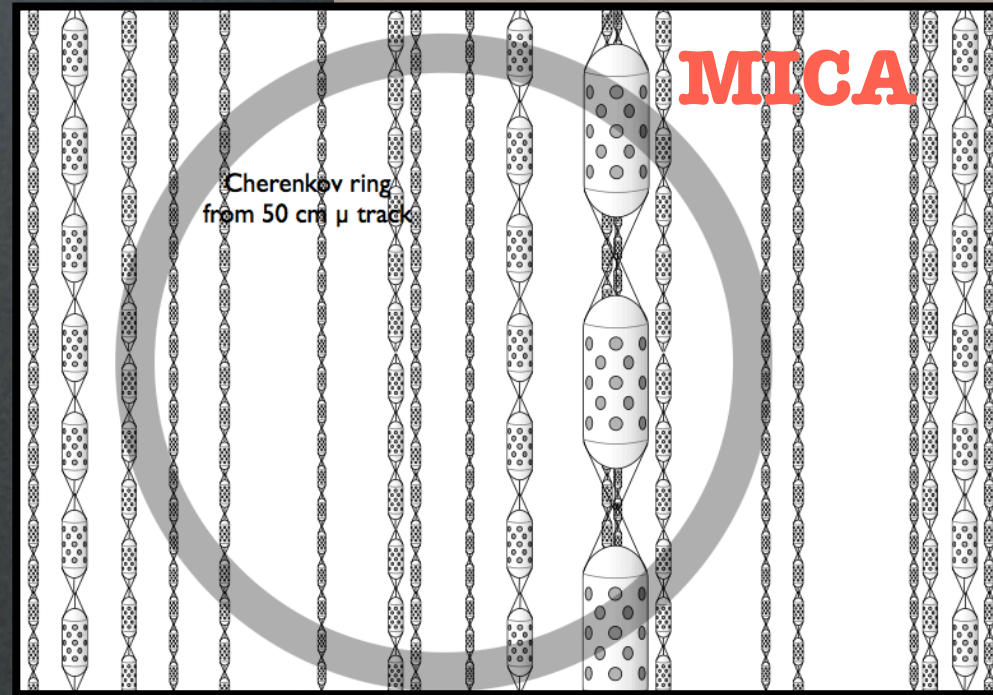


Images from J. Koskinen (see talk on Thursday morning)



- There are plans to increase the number of photo-detectors in the ice
 - See talks Thursday morning
- **This is a problem fitQun is even better suited to solve**
 - Arbitrary phototube locations are naturally accommodated
 - No reflections from tank walls
 - Treatment of non-direct light is greatly simplified
- Proton decay, atmospheric ν , ...

Neutrino Telescopes (IceCube, ANTARES, etc.)

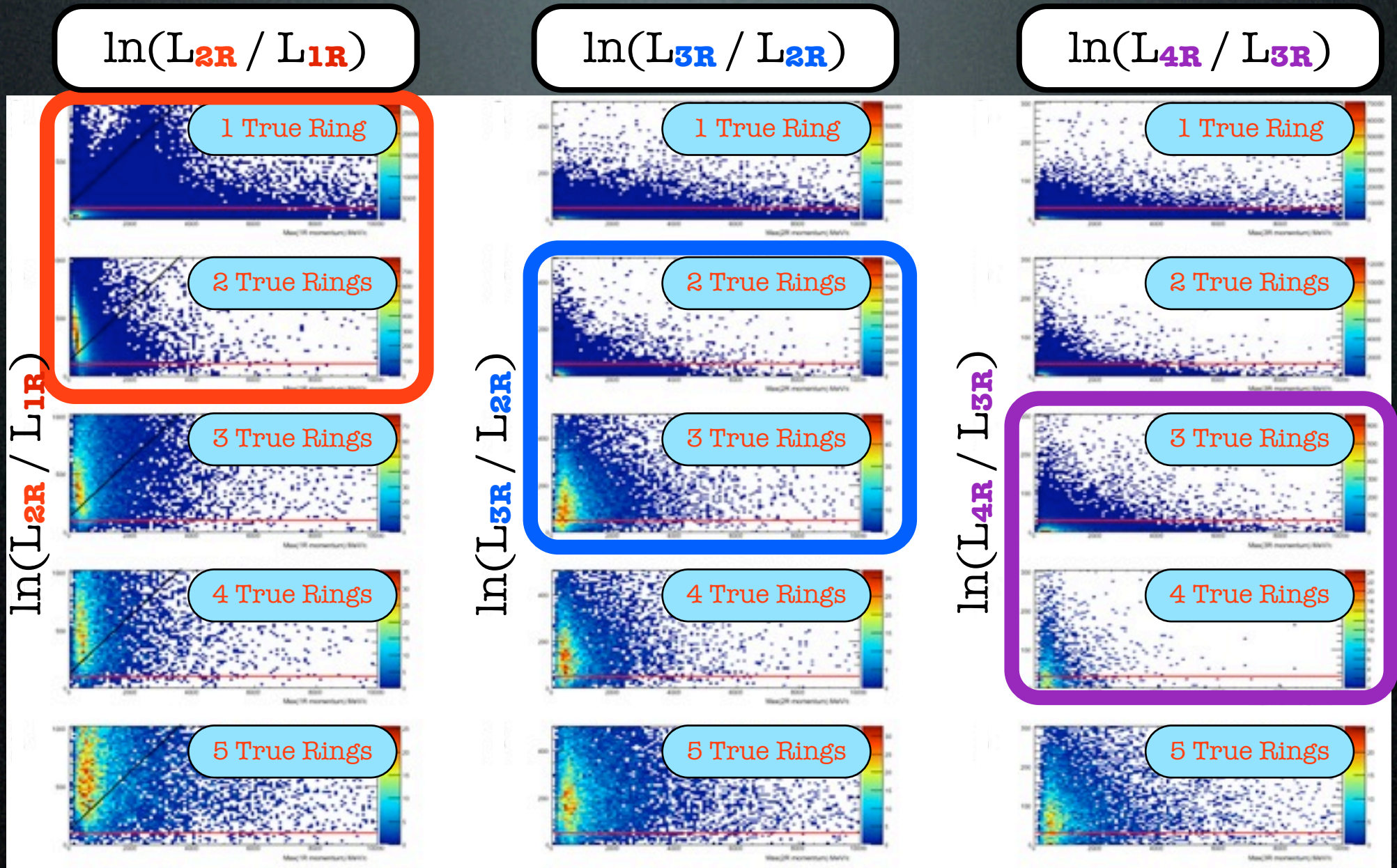


Summary

- fiTQun is a new reconstruction algorithm for large Cherenkov Detectors
- Significant improvements are seen over previously used algorithms
 - Large reductions in poorly understood backgrounds for T2K ν_e appearance and ν_μ disappearance measurements
- fiTQun is beginning to seep into other Super-K analyses
 - Atmospheric neutrinos
 - Proton Decay
- fiTQun can make important contributions to future Cherenkov detectors, such as Hyper-K and PINGU/MICA

Backups

Ring Counting



- Good discrimination seen up to ~ 4 rings

T2K Event Selection

Basic Event Selection

Consistent with Beam Time
No Outer-Detector Activity
Vertex in Fiducial Volume
Minimum Energy Requirements

Single Ring Cut

Select Muon-like Ring

Select Electron-like Ring

1-ring
Candidates

Require:
 ≤ 1 decay e^-

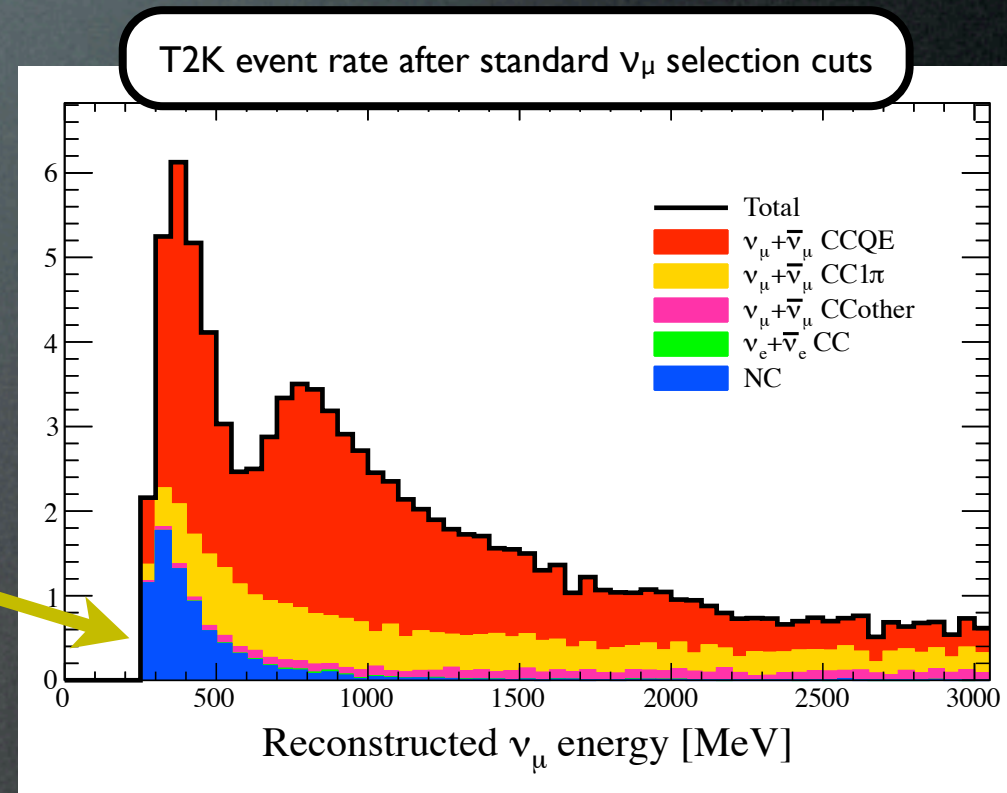
ν_μ Candidates

Require:
no decay e^-
no 2nd π^0 ring
 $E_\nu < 1250$ MeV

ν_e Candidates

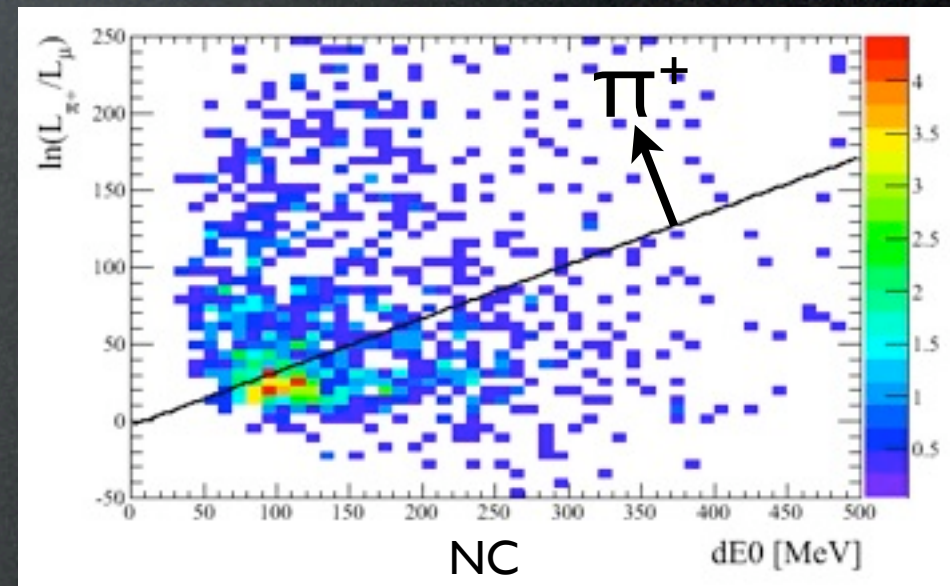
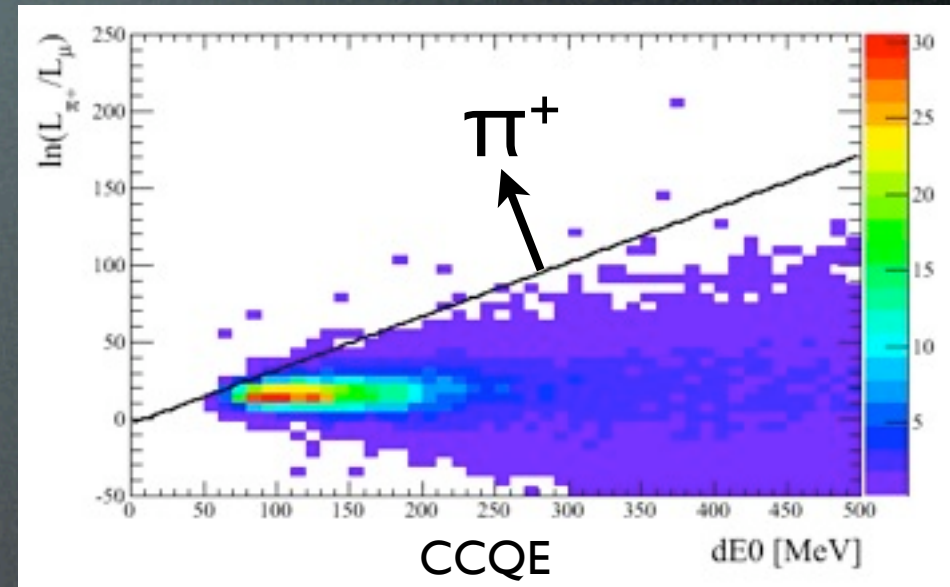
T2K ν_μ Sample

- Large neutral-current (NC) background at low energy
 - Affects the **position (Δm^2)** and **depth ($\sin^2 2\theta$)** of the oscillation dip
- Uncertainty in Super-K π^+ reconstruction is **very large (> 100% error)**
 - No previous algorithm to reconstruct charged pions
- **fiTQun π^+ rejection** can be very helpful

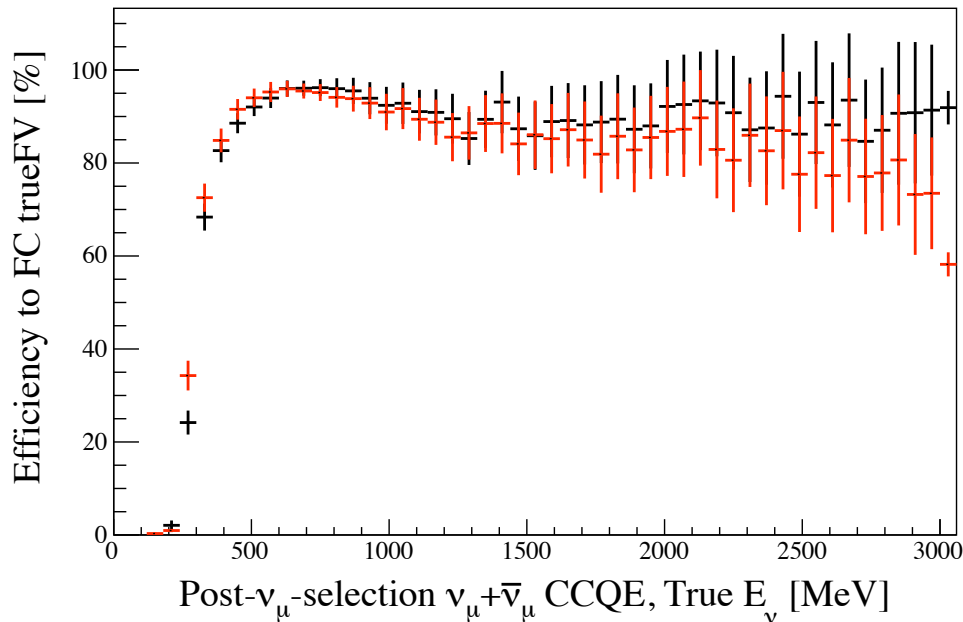
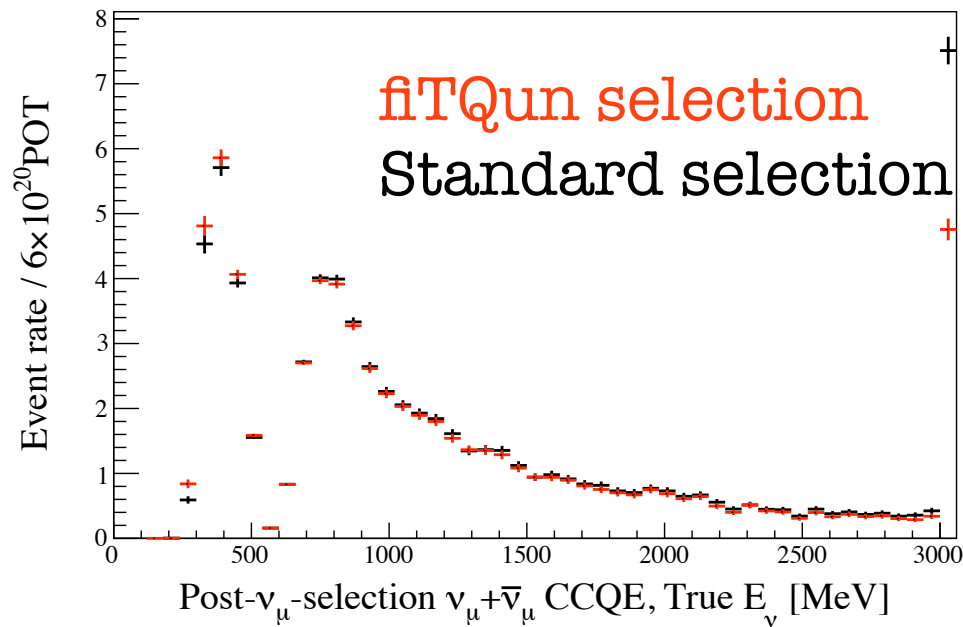


Neutral Current (NC) Rejection

- Use π^+/μ likelihood ratio
- CCQE signal looks muon-like
- A large fraction of the NC background lies above the cut line
- NC background is mostly due to $\text{NC}\pi^+$
- Also a small contribution from NC-proton



ν_μ Signal Efficiency Comparison

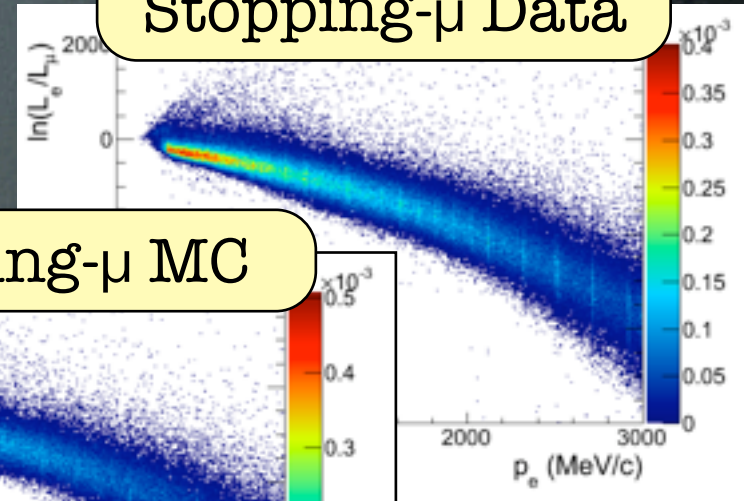


- Around the oscillation dip, fiTQun has higher signal efficiency
- Signal loss by fiTQun selection is mostly in the high-energy tail region ($>3\text{GeV}$)

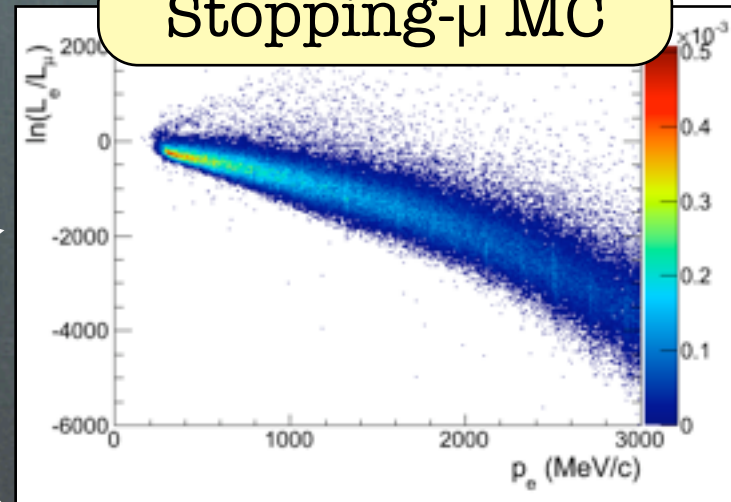
Data Validations

- We have begun a program for data-based fit validation
- Plan to test fitQun over as many data samples as possible
 - Stopping cosmics
 - Electrons from μ -decay
 - Atmospheric neutrinos
 - Detector calibration samples
 - Cone generator
 - Calibration sources (e.g. Nickel ball)

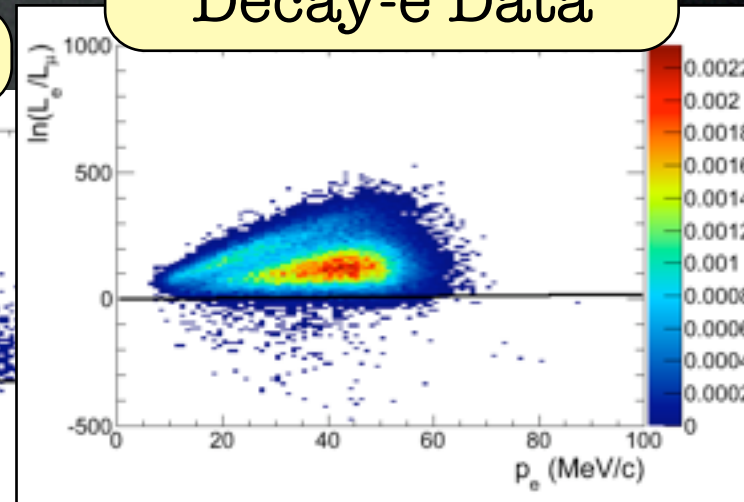
Stopping- μ Data



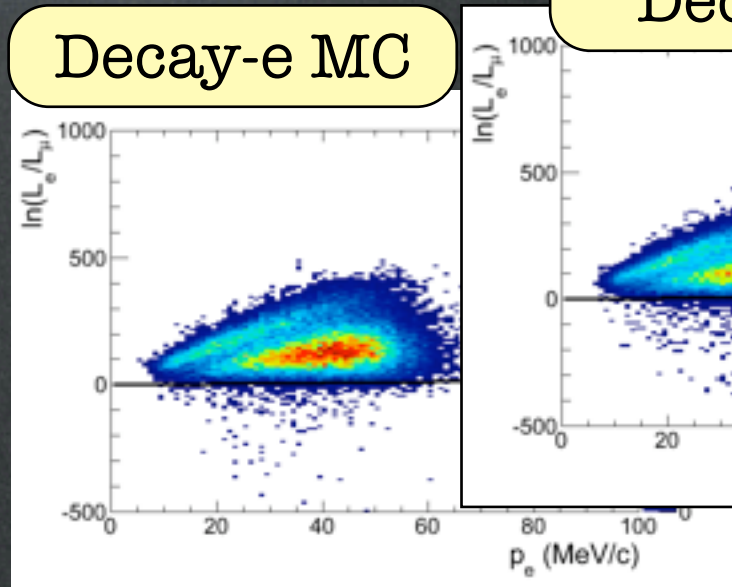
Stopping- μ MC



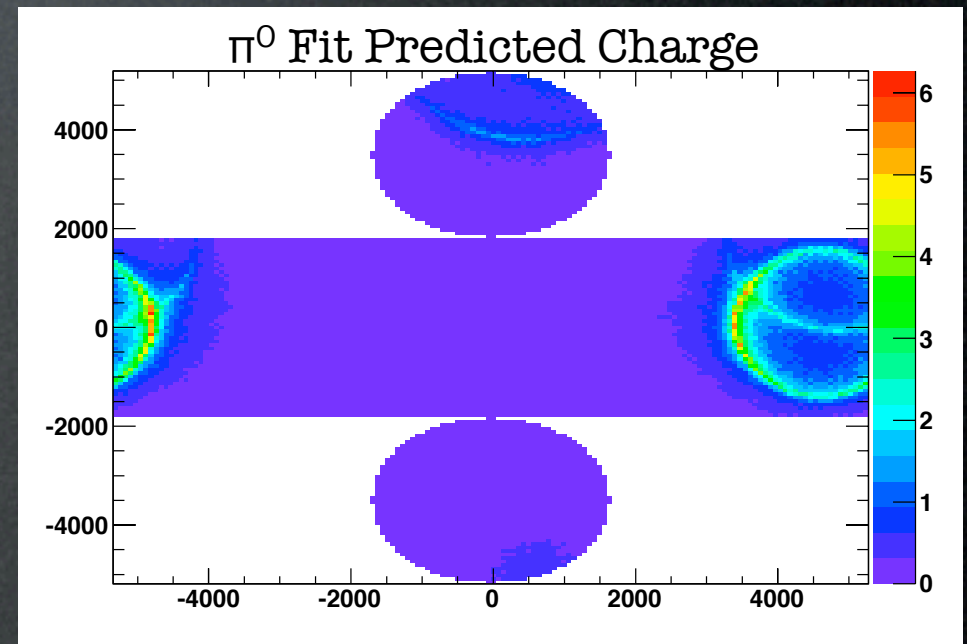
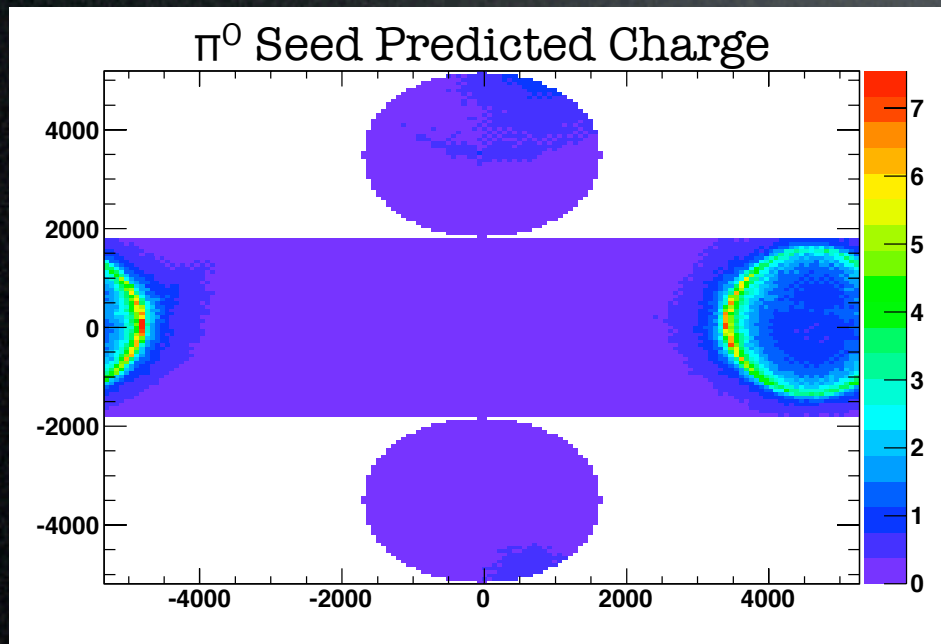
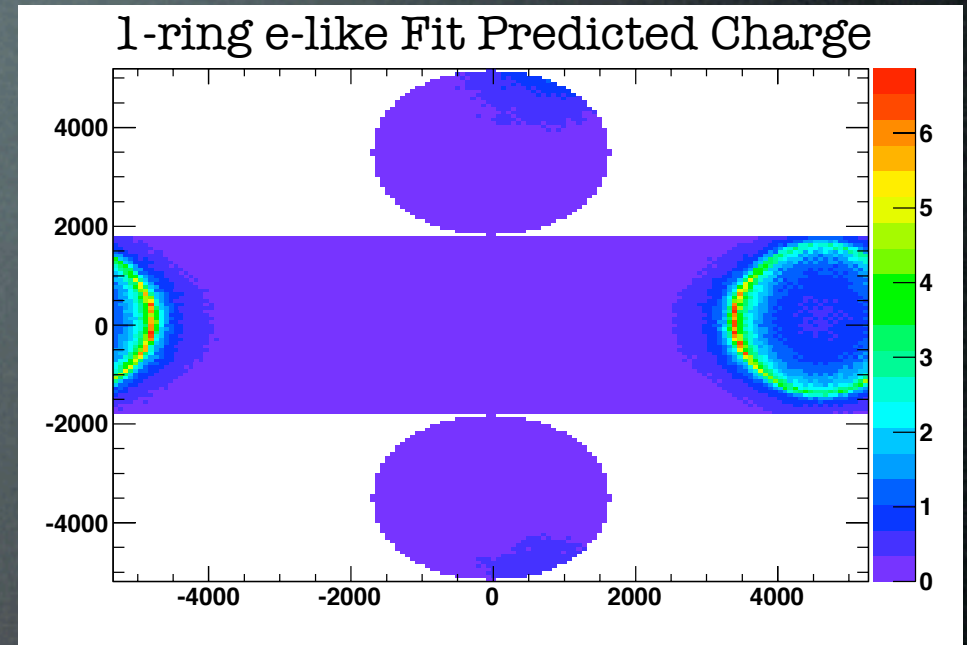
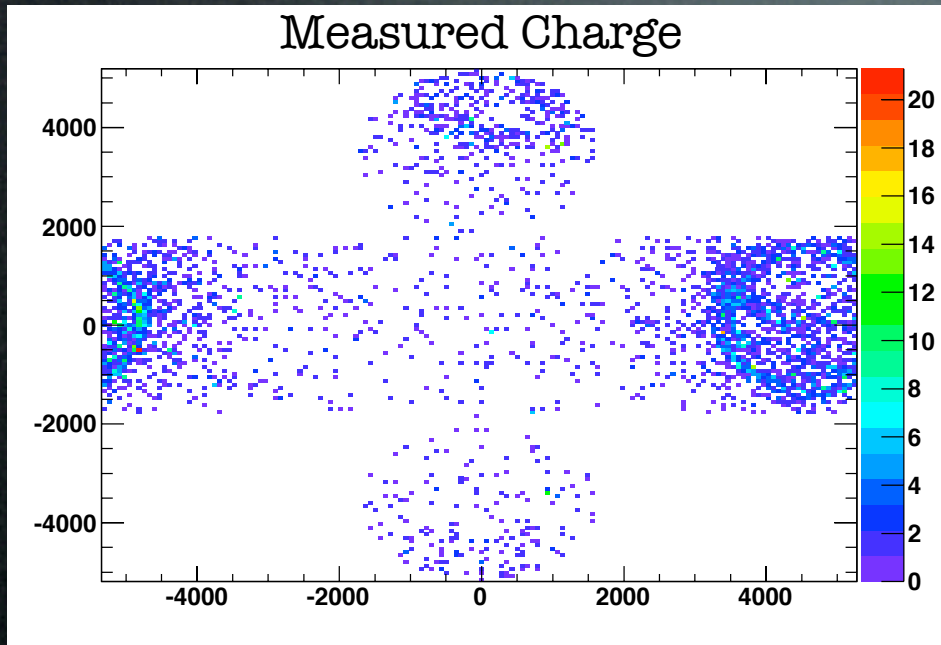
Decay-e Data



Decay-e MC



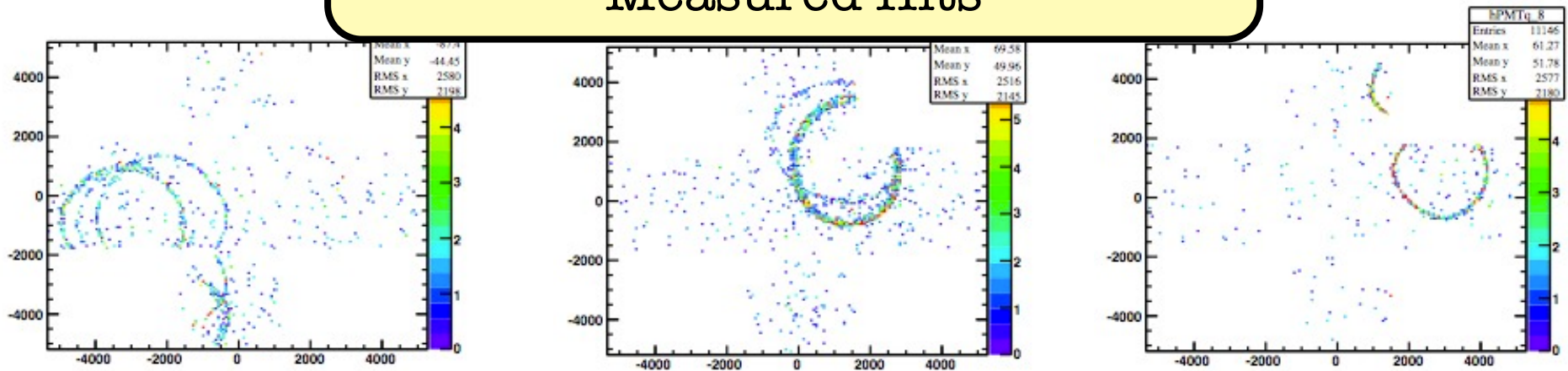
Event Display: π^0 Fit



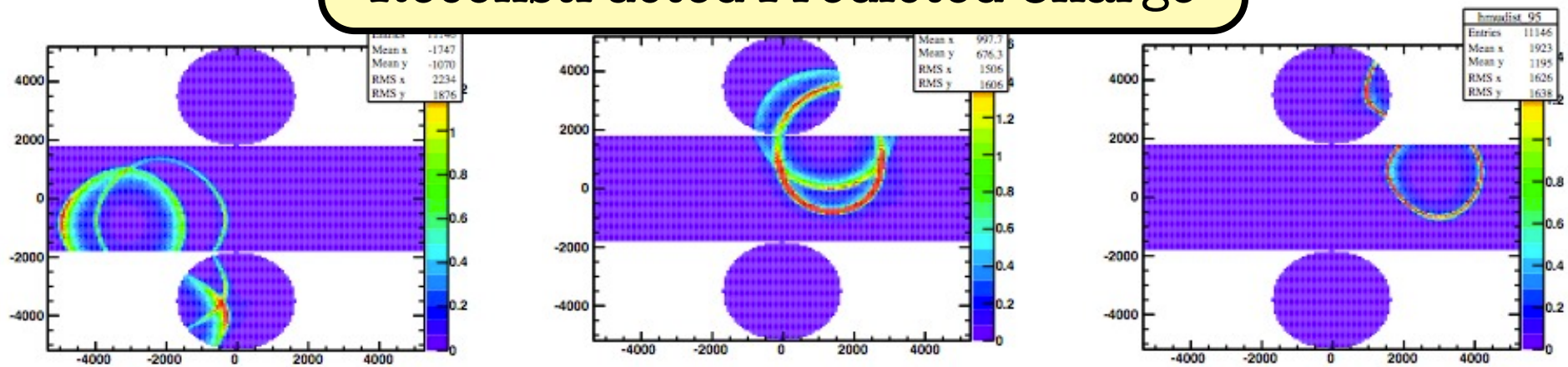
Event Display

Kinked-track π^+ Fitter

Measured Hits

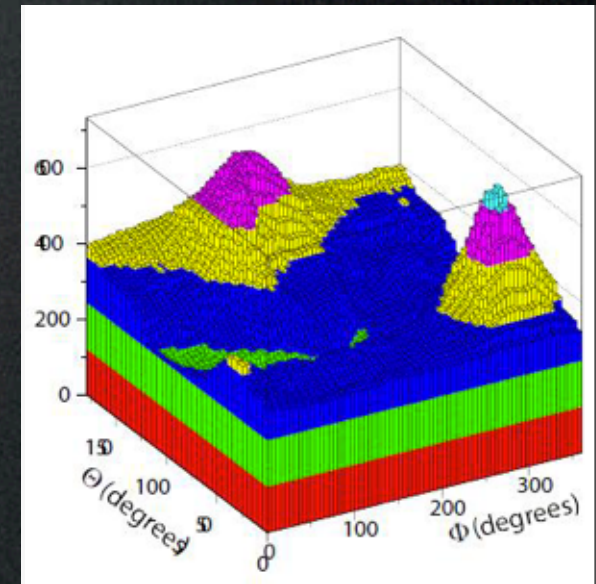
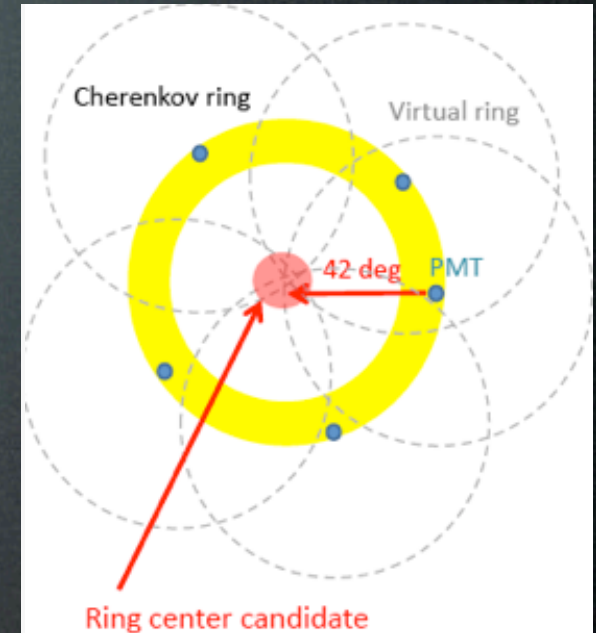


Reconstructed Predicted Charge



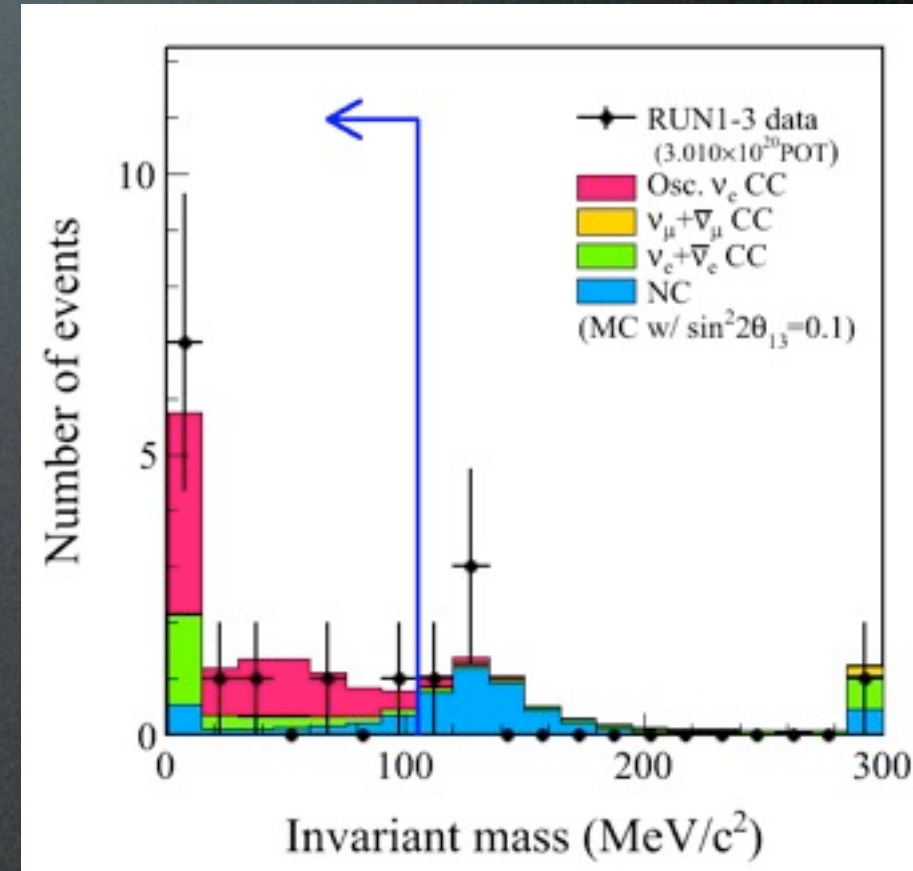
Old Super-K Reconstruction

1. Find the **event vertex** with hit timing information
2. Determine **number & direction** of rings
 - Assume a 42° Cherenkov angle (maximum for water)
 - Use Hough transform to find hits belonging to a common ring
 - Discard dimmer rings if with 15° of another ring
3. Calculate the **particle type for each ring**
 - Use a Gaussian PDF for charge in each PMT based on expected charge pattern
 - Angle can be readjusted to improve fit
4. Sum all charge within 70° cone to **determine the ring momentum**
 - (where rings overlap, try to separate the charge based on expected ring pattern)
- This is a multi-step fitting procedure (**apfit**)



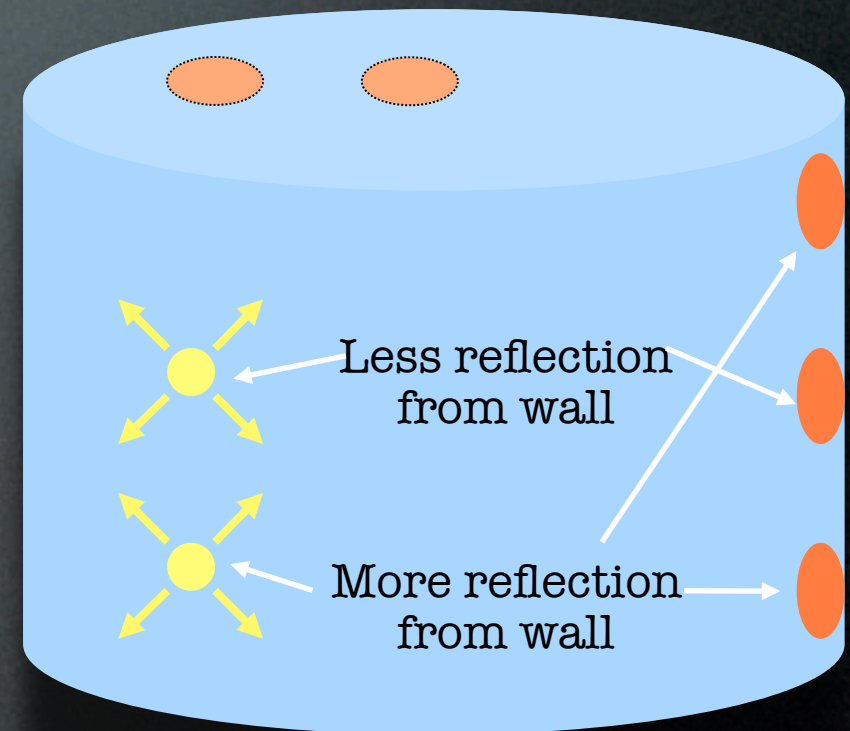
Default π^0 Rejection

- Specialized algorithm is used to **find soft photons**
 - POLFit “Pattern-Of-Light Fit”
 - Finds photons **missed by ring counting** in apfit
- POLFit uses a “fitQun-esqe” predicted-charge fit method
 - **Several approximations are made:**
 - Coarse scattered-light matrix
 - No photon conversion lengths
 - No reflections
 - No time likelihood
- POLFit **always returns a 2nd photon** momentum and direction
 - Cut on reconstructed invariant mass to remove π^0 background



Scattered Light

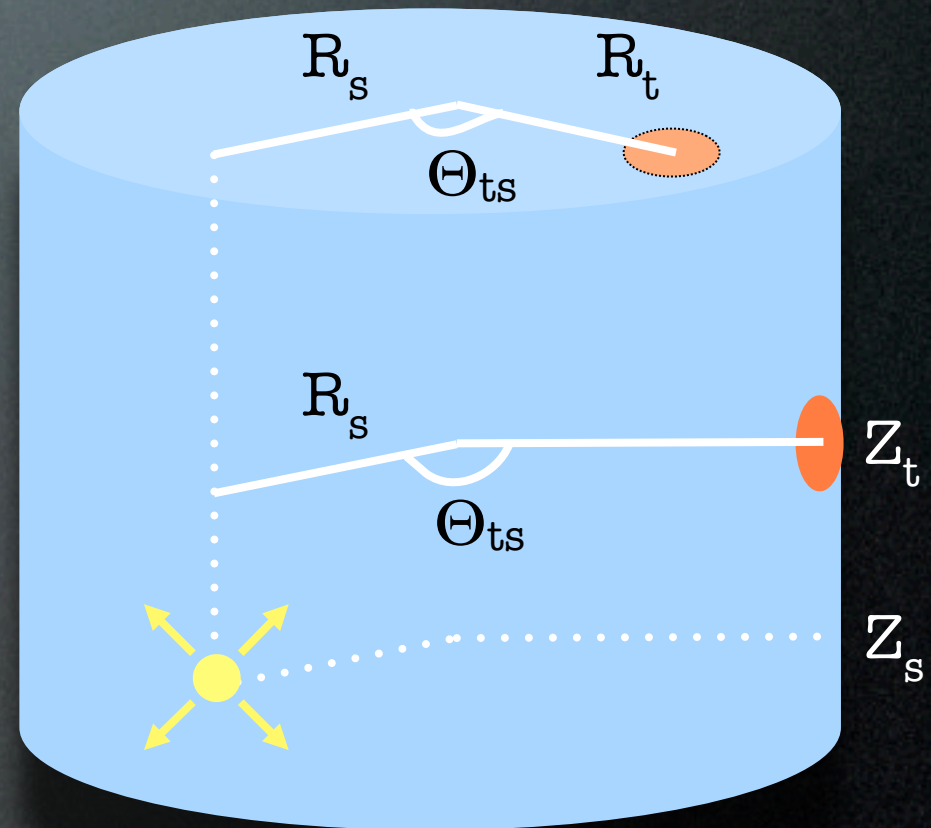
- **More scattered light** is detected for sources that are **close to the wall**
 - The same is true for PMTs near corners
- The scattered light in each PMT depends on:
 - **Light source intensity**
 - **Track direction**
 - **PMT and source geometry**
- Scattered light for each PMT is **normalized to direct light**
 - Accounts for the source intensity
 - Tabulate in advance:
“Scattering Table”, A_{scat}



$$A_{\text{scat}}(\theta_{\text{source}}, \varphi_{\text{source}}, \text{geometric variables}) \equiv \frac{d\mu^{\text{indirect}}}{d\mu^{\text{direct, iso}}}$$

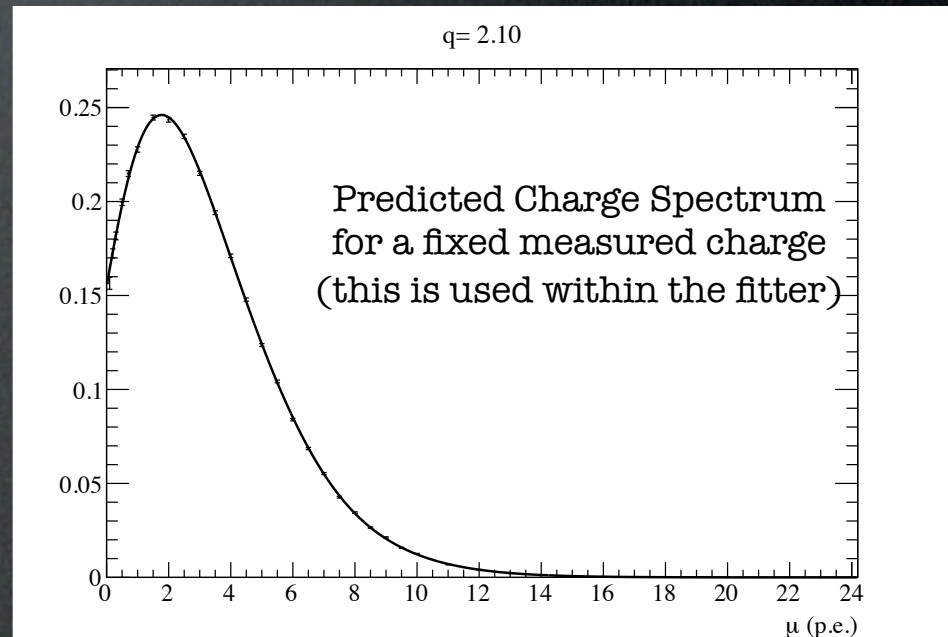
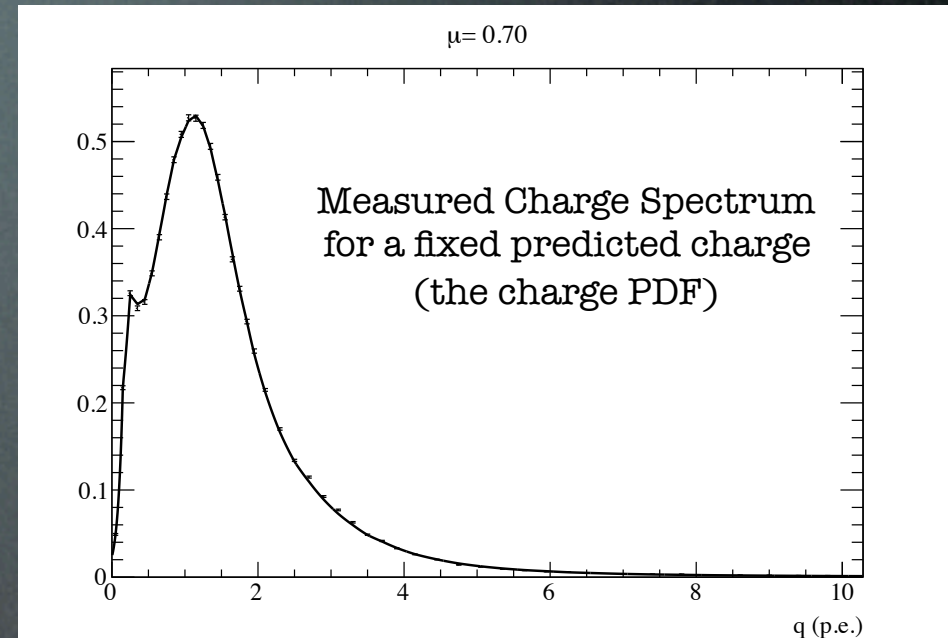
Scattering Tables

- Take advantage of **cylindrical geometry**
- A_{scat} will depend on
 - Source direction (θ_s, ϕ_s)
 - Source position $(\Theta_{ts}, \mathbf{R}_s, \mathbf{Z}_s)$
 - \mathbf{Z}_t for PMTs on the sides
 - $\mathbf{A}_{\text{side}}(\theta_s, \phi_s, \Theta_{ts}, \mathbf{R}_s, \mathbf{Z}_s, \mathbf{Z}_t)$
 - \mathbf{R}_t for PMTs on the ends
 - $\mathbf{A}_{\text{end}}(\theta_s, \phi_s, \Theta_{ts}, \mathbf{R}_s, \mathbf{Z}_s, \mathbf{R}_t)$
- Must tabulate 6-dimensional scattering tables using the detector MC



PMT Charge Response

- For a given predicted charge, μ , we need a PDF for the measured charge, q
- Use skdetsim to generate a Poisson distributed charge in each PMT with mean μ
- This gives a 2D histogram of measured charge vs predicted charge
 - Each bin of measured charge is normalized to 1 (to make proper charge PDF)
 - During the fit, charge is fixed (only predicted charge varies)
 - Use distribution of μ at fixed q
- Use smoothed (i.e. fit) curves to improve minimization performance



Time Likelihood

- For every PMT, we have calculated:
 - Predicted charge from direct light
 - Predicted charge from scattered light
- For a predicted amount of direct light, need a PDF for the first hit arrival time
 - Also need a PDF for scattered light first hit time
- For a given particle hypothesis, particle guns are run at many different momenta
 - Hit times (corrected for time of flight) are recorded in bins of predicted charge and momentum
- Give priority to direct light, since it should reach the PMT first
 - $f_t = P(\text{hit}_{\text{dir}}) * f_{t,\text{dir}}(\mu) + (1 - P(\text{hit}_{\text{dir}})) * f_{t,\text{scat}}(\mu)$
 - If there is a lot of direct light, the time PDF should default to the direct light time PDF

