# Linear Accelerators

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Chavannes 2013

1. 2. 3.

4. 5. Basic concepts Accelerating structures Beam optics Linac architecture RFQ





# 1. Introduction: main concepts, building blocks, synchronicity







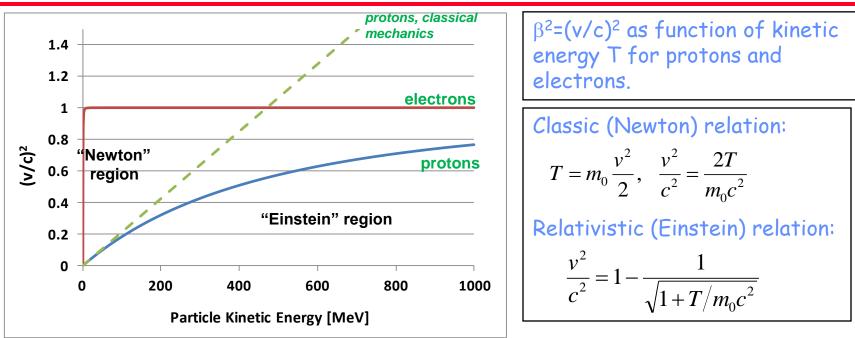
Linear Accelerators are used for:

- 1. <u>Low-Energy acceleration</u> (injectors to synchrotrons or stand-alone): for protons and ions, linacs can be synchronous with the RF fields in the range where velocity increases with energy. When velocity is ~constant, synchrotrons are more efficient (multiple crossings instead of single crossing). Protons :  $\beta = v/c = 0.51$  at 150 MeV, 0.95 at 2 GeV.
- 2. <u>High-Energy acceleration</u> in the case of:
  - Production of <u>high-intensity proton beams</u>, in comparison with synchrotrons, linacs can go to higher repetition rate, are less affected by resonances and instabilities and have more distributed beam losses. Higher injection energy from linacs to synchrotrons leads to lower space charge effects in the synchrotron and allows increasing the beam intensity.
  - High energy linear colliders for leptons, where the main advantage is the absence of synchrotron radiation.

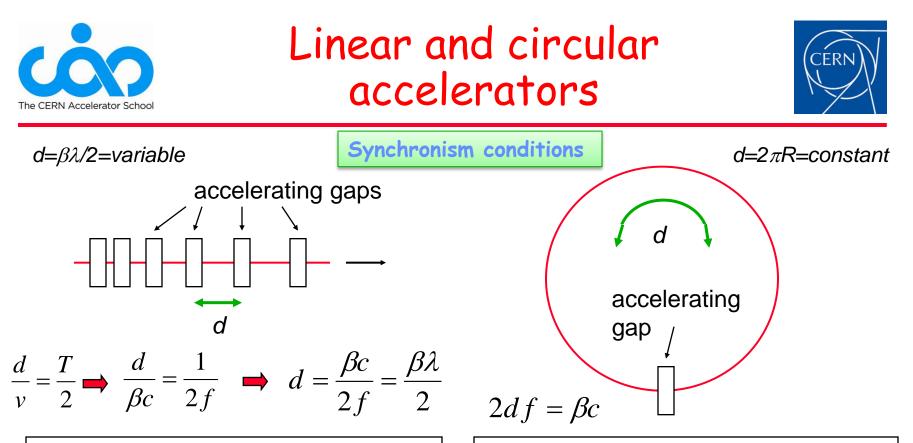


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- → <u>**Protons**</u> (rest energy 938.3 MeV): follow "Newton" mechanics up to some tens of MeV  $(\Delta v/v < 1\%$  for W < 15 MeV) then slowly become relativistic ("Einstein"). From the GeV range velocity is nearly constant (v~0.95c at 2 GeV) → <u>linacs can cope with the increasing particle velocity, synchrotrons cover the range where v nearly constant.</u>
- → <u>Electrons</u> (rest energy 511 keV, 1/1836 of protons): relativistic from the keV range (v~0.1c at 2.5 keV) then increasing velocity up to the MeV range (v~0.95c at 1.1 MeV)  $\rightarrow$  <u>v~c after few meters</u> of acceleration (typical gradient 10 MeV/m). 4



#### Linear accelerator:

Particles accelerated by a sequence of gaps (all at the same RF phase).

Distance between gaps increases proportionally to the particle velocity, to keep synchronicity.

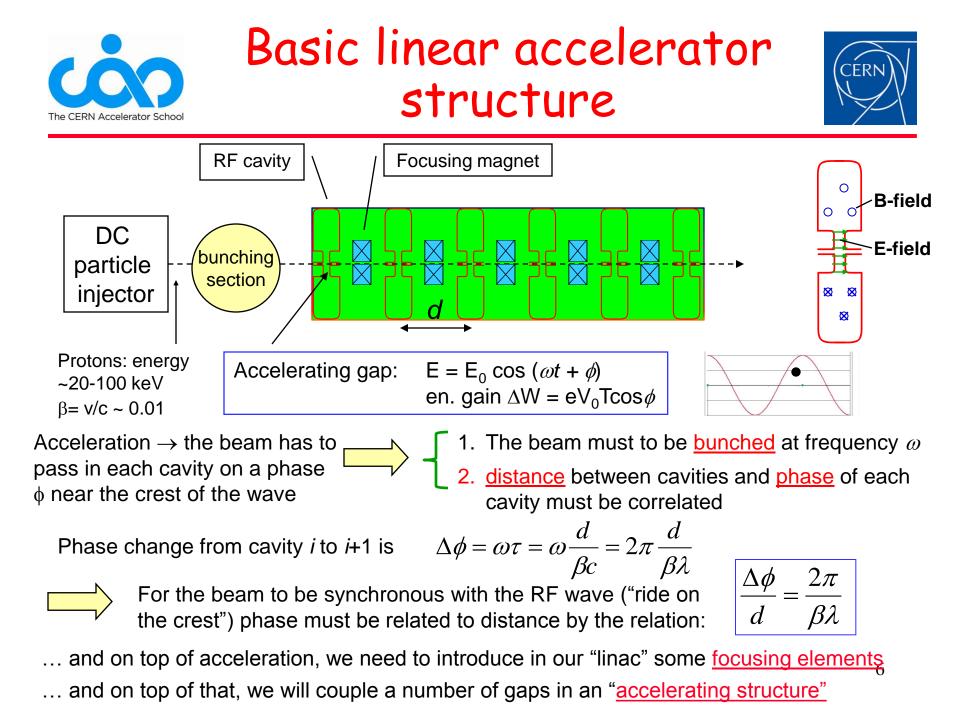
Used in the range where  $\boldsymbol{\beta}$  increases. "Newton" machine

#### Circular accelerator:

Particles accelerated by one (or more) gaps at given positions in the ring.

Distance between gaps is fixed. Synchronicity only for  $\beta$ ~const, or varying (in a limited range!) the RF frequency.

Used in the range where  $\beta$  is nearly constant. "Einstein" machine

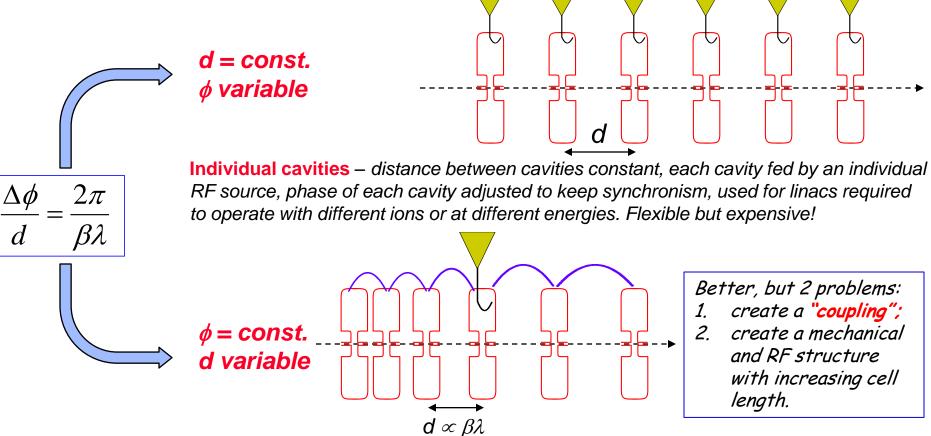




### Accelerating structure architecture



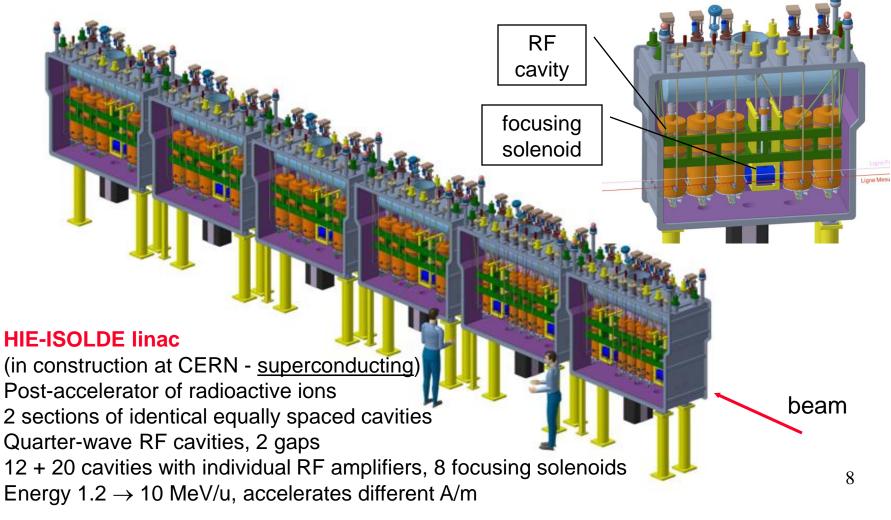
When  $\beta$  increases during acceleration, either the phase difference between cavities  $\Delta \phi$  must decrease or their distance *d* must increase.



**Coupled cell cavities** - a single RF source feeds a large number of cells (up to ~100!) - the phase between adjacent cells is defined by the coupling and the distance between cells increases to keep synchronism . Once the geometry is defined, it can accelerate only one type of ion for a given energy range. Effective but not flexible.



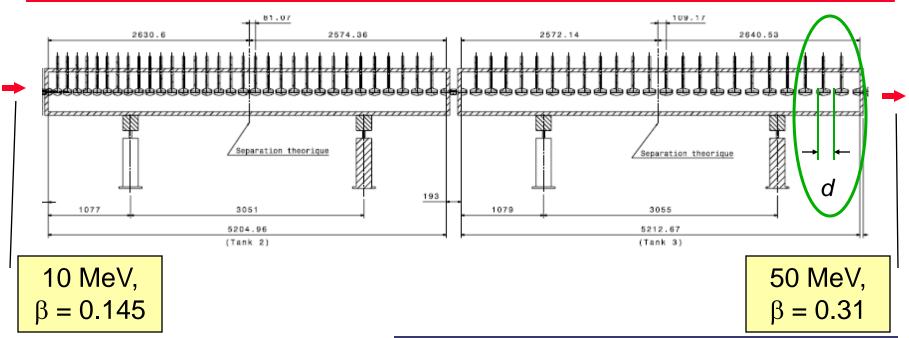
The goal is flexibility: acceleration of different ions (e/m) at different energies $\rightarrow$  need to change phase relation for each ion-energyCryomodule High Beta (5 Cavités Ø320)





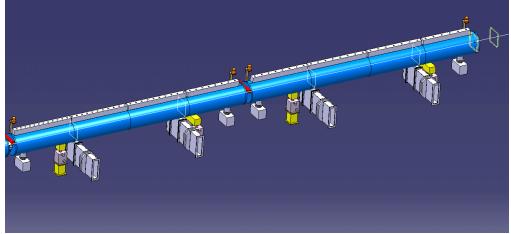






Tank 2 and 3 of the new Linac4 at CERN:

57 coupled accelerating gaps Frequency 352.2 MHz,  $\lambda = 85$  cm Cell length (d= $\beta\lambda$ ) from 12.3 cm to 26.4 cm (factor 2 !).



# Case 3 (intermediate): the Linac4 PIMS structure



Between these 2 "extremes" there are "intermediate" cases: a) single-gap cavities are expensive and b) structures with each cell matched to the beta profile are mechanically complicated  $\rightarrow$  as soon as the increase of beta with energy becomes smaller we can accept a small phase error and allow short sequences of identical cells.

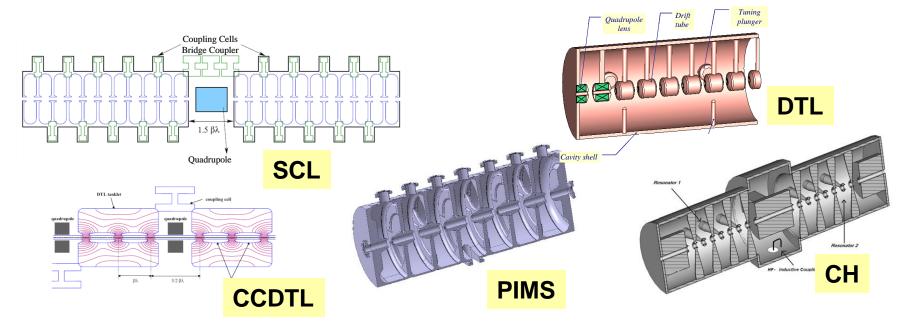
**PIMS**: cells have same length inside a cavity (7 cells) but increase from one cavity to the next. At high energy (>100 MeV) 160 MeV, beta changes slowly and phase error remains small. 155 cm Focusing quadrupoles between cavities 100 MeV, 128 cm (v/c)^2 **PIMS range** 100 200 30( **RF** input Kinetic Energy [Me

## Multi-gap coupled-cell cavities (for protons and ions)



Between the 2 extreme cases (array of independently phased single-gap cavities / single long chain of coupled cells with lengths matching the particle beta) there can be a <u>large number of variations</u> (number of gaps per cavity, length of the cavity, type of coupling) each optimized for a certain <u>range of energy and type of particle</u>.

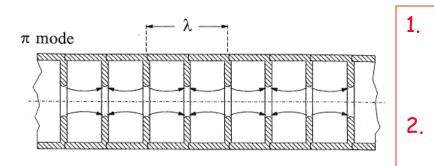
The goal of this lecture is to provide the background to understand the main features of these different structures...



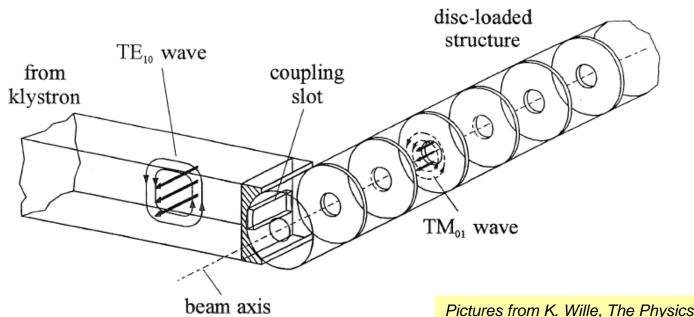


# **Electron linacs**

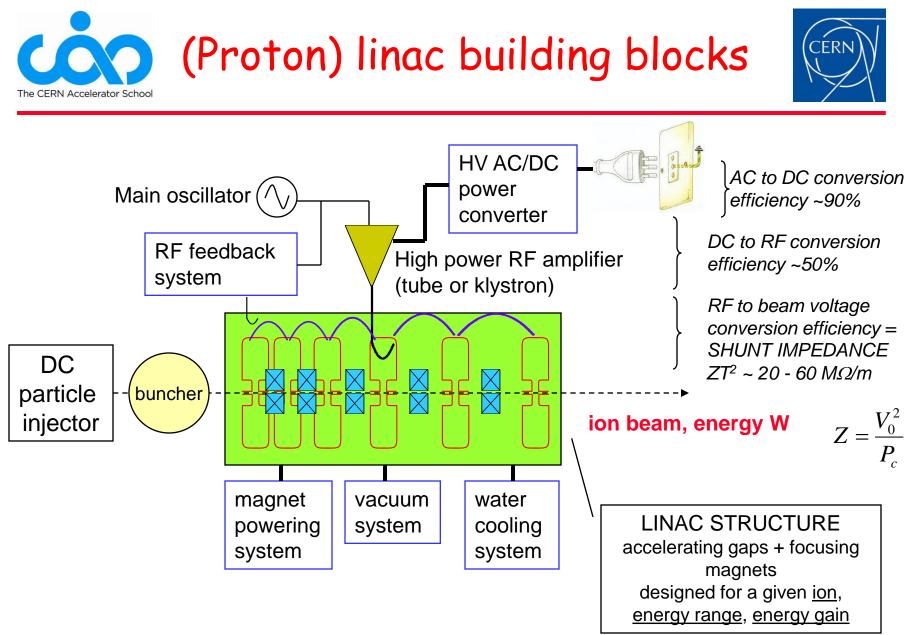




- In an electron linac velocity is ~ constant. To use the fundamental accelerating mode cell length must be d =  $\beta\lambda$  / 2.
- the linac structure will be made of a sequence of identical cells. Because of the limits of the RF source, the cells will be grouped in cavities operating in travelling wave mode.

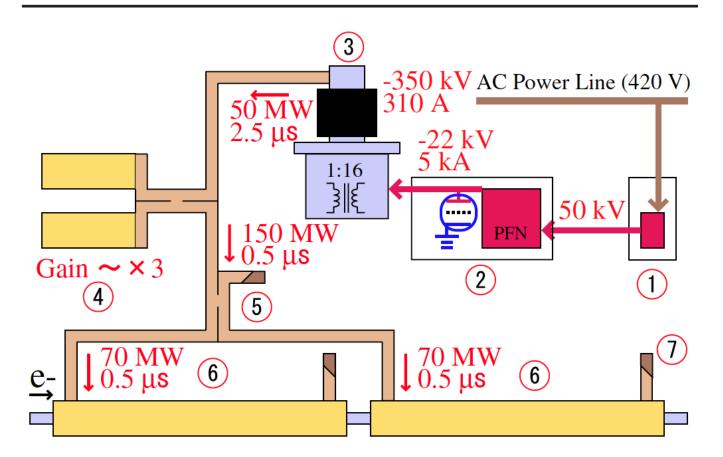


Pictures from K. Wille, The Physics of Particle Accelerators





#### TSUMORU SHINTAKE et al.





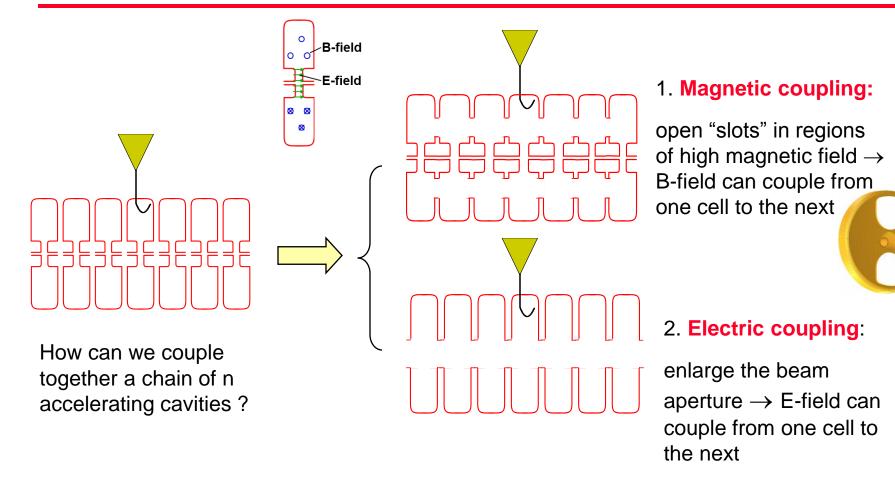


### 2 - Accelerating Structures



# Coupling accelerating cells





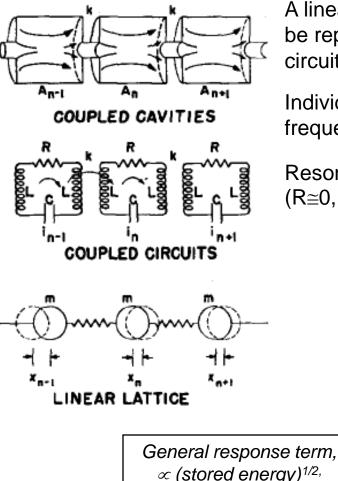
The effect of the coupling is that the cells no longer resonate independently, but will have common resonances with well defined field patterns.



### Linac cavities as chains of coupled resonators



What is the relative phase and amplitude between cells in a chain of coupled cavities?

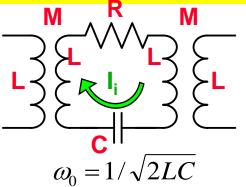


can be voltage, E-field, B-field. etc.

A linear chain of accelerating cells can be represented as a chain of resonant circuits magnetically coupled.

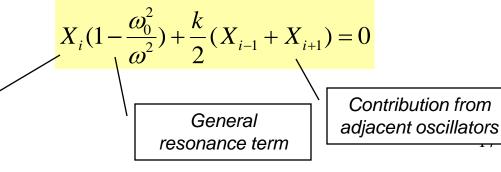
Individual cavity resonating at  $\omega_0 \rightarrow$  frequenci(es) of the coupled system ?

Resonant circuit equation for circuit *i* (R $\cong$ 0, M=k $\sqrt{L^2}$ ):



$$I_{i}(2j\omega L + \frac{1}{j\omega C}) + j\omega kL(I_{i-1} + I_{i+1}) = 0$$

Dividing both terms by 2j@L:

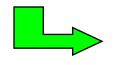


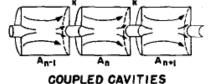
The Coupled-system Matrix The CERN Accelerator School

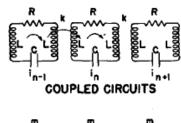


 $X_{i}(1 - \frac{\omega_{0}^{2}}{\omega^{2}}) + \frac{k}{2}(X_{i-1} + X_{i+1}) = 0$ 

$$i = 0, ..., N$$









A chain of N+1 resonators is described by a (N+1)x(N+1) matrix:

$$\begin{vmatrix} 1 - \frac{\omega_0^2}{\omega^2} & \frac{k}{2} & 0 & \cdots \\ \frac{k}{2} & 1 - \frac{\omega_0^2}{\omega^2} & \frac{k}{2} & \cdots \\ \cdots & \cdots & \cdots & \cdots \\ 0 & 0 & \frac{k}{2} & 1 - \frac{\omega_0^2}{\omega^2} \end{vmatrix} | \begin{matrix} X_0 \\ X_2 \\ \cdots \\ X_N \end{matrix} = 0 \quad \text{or} \quad M X = 0$$

This matrix equation has solutions only if  $\det M = 0$ 

Eigenvalue problem!

- 1. System of order (N+1) in  $\omega \rightarrow$  only N+1 frequencies will be solution of the problem ("eigenvalues", corresponding to the resonances)  $\rightarrow$ a system of N coupled oscillators has N resonance frequencies  $\rightarrow$ an *individual resonance opens up into a band of frequencies*.
- 2. At each frequency  $\omega_1$  will correspond a set of relative amplitudes in the different cells ( $X_0, X_2, ..., X_N$ ): the "eigenmodes" or "<u>modes</u>".



## Modes in a linear chain of oscillators



We can find an analytical expression for eigenvalues (frequencies) and eigenvectors (modes):

Frequencies of the coupled system :

$$q^{2} = \frac{\omega_{0}^{2}}{1 + k \cos \frac{\pi q}{N}}, \quad q = 0, ..., N$$

the index q defines the number of the solution  $\rightarrow$  is the "mode index"

→ Each mode is characterized by a phase  $\pi q/N$ . Frequency vs. phase of each mode can be plotted as a "dispersion curve"  $\omega=f(\phi)$ :

 $\omega$ 

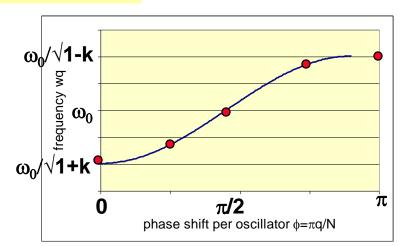
- 1.each mode is a point on a sinusoidal curve.
- 2.modes are equally spaced in phase.

The "eigenvectors = relative amplitude of the field in the cells are:

$$X_i^{(q)} = (const) \cos \frac{\pi q i}{N} e^{j\omega_q t} \quad q = 0, ..., N$$



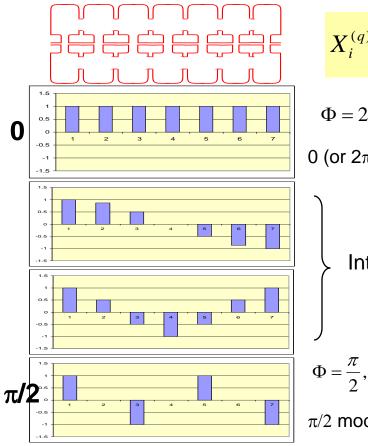
**STANDING WAVE MODES,** defined by a phase  $\pi q/N$  corresponding to the phase shift between an oscillator and the next one  $\rightarrow \pi q/N=\Phi$  is the phase difference 19 between adjacent cells that we have introduces in the 1<sup>st</sup> part of the lecture.





# Example: Acceleration on the normal modes of a 7-cell structure



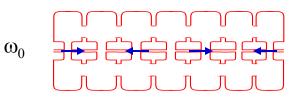


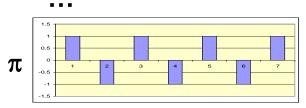
$$\begin{aligned} & \frac{\pi q i}{N} e^{j\omega_q t} \quad q = 0, \dots, N \\ & = 2\pi, \quad 2\pi \frac{d}{\beta\lambda} = 2\pi, \quad d = \beta\lambda \\ & \omega = \omega_0/\sqrt{1+k} \end{aligned}$$

$$\begin{aligned} & = \beta\lambda \end{aligned}$$

Intermediate modes

$$\Phi = \frac{\pi}{2}, \quad 2\pi \frac{d}{\beta \lambda} = \frac{\pi}{2}, \quad d = \frac{\beta \lambda}{4}$$
  
 $\pi/2$  mode, acceleration if  $\mathbf{d} = \frac{\beta \lambda}{4}$ 









### Practical linac accelerating structures



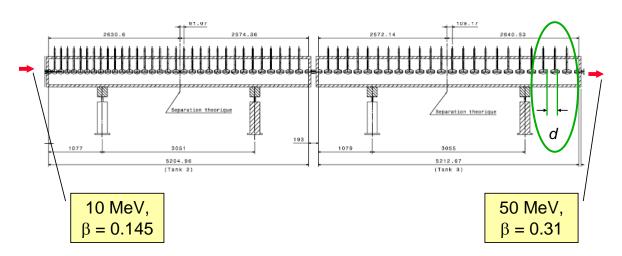
Note: our equations depend only on the cell frequency  $\omega_{0}$ , not on the cell length d !!!

$$\omega_q^2 = \frac{\omega_0^2}{1 + k \cos \frac{\pi q}{N}}, \quad q = 0, \dots, N$$

$$q_n^{(q)} = (const) \cos \frac{\pi q n}{N} e^{j\omega_q t} \quad q = 0, ..., N$$

 $\rightarrow$  As soon as we keep the frequency of each cell constant, we can change the cell length following any acceleration ( $\beta$ ) profile!

X



 $d \Lambda \to (L \Lambda \ , \ C {\downarrow}) \to LC \thicksim const \to \omega_0 \thicksim const$ 

Example:

The Drift Tube Linac (DTL)

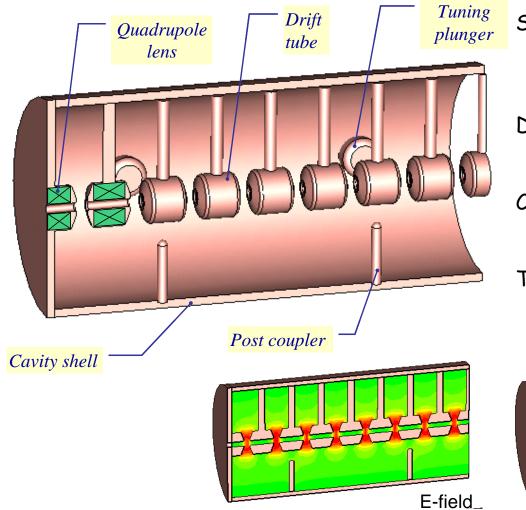
Chain of many (up to 100!) accelerating cells operating in the 0 mode. The ultimate coupling slot: no wall between the cells!

Each cell has a different length, but the cell frequency remains constant  $\rightarrow$  *"the EM fields don't see that the cell length is changing!"* 21



# The DTL



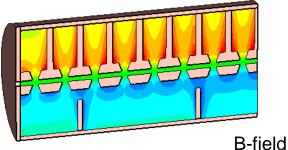


Standing wave linac structure for protons and ions, β=0.1-0.5, f=20-400 MHz

Drift tubes are suspended by stems (no net RF current on stem)

Coupling between cells is maximum (no slot, fully open !)

The O-mode allows a long enough cell  $(d=\beta\lambda)$  to house <u>focusing</u> <u>quadrupoles inside the drift tubes</u>!





# Examples of DTL







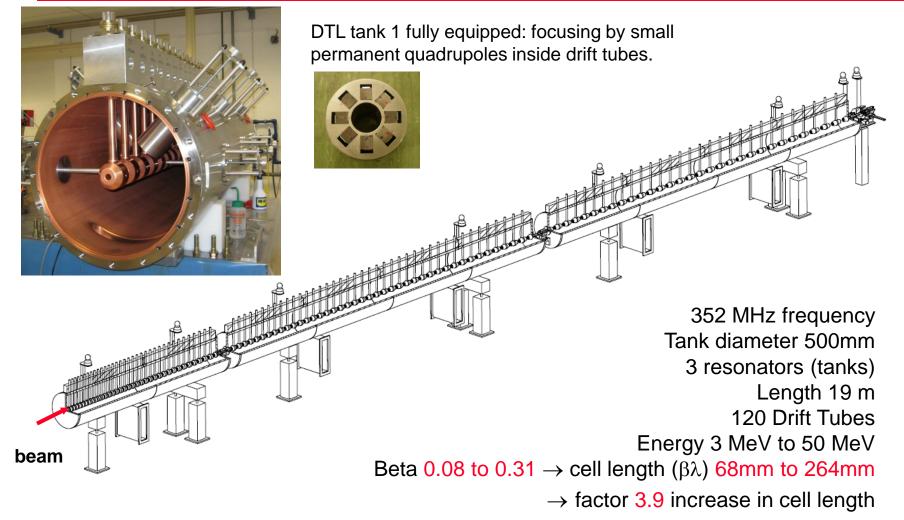
Top; CERN Linac2 Drift Tube Linac: 1978, 202.5 MHz, 3 tanks, final energy 50 MeV, tank diameter 1 meter.

Left: The Drift Tube Linac of the SNS at Oak Ridge (USA): 402.5 MHz, 6 tanks, final energy 87 MeV.



# The Linac4 DTL







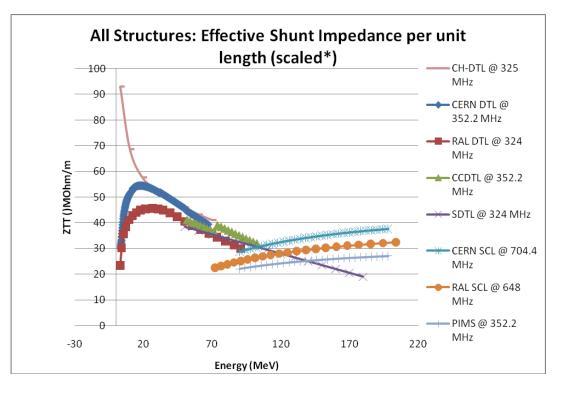
# Shunt impedance

 $Z = \frac{V_0^2}{V_0^2}$ 



How to choose the best linac structure? Main figure of merit is the power efficiency = shunt impedance

Ratio between energy gain (square) and power dissipation, is a measure of the energy efficiency of a structure. Depends on beta, energy and mode of operation.



But the choice of the best accelerating structure for a certain energy range depends as well on **beam dynamics** and on construction **cost**.

Comparison of shuntimpedances for different lowbeta structures done in 2005-08 by the "HIPPI" EU-funded Activity.

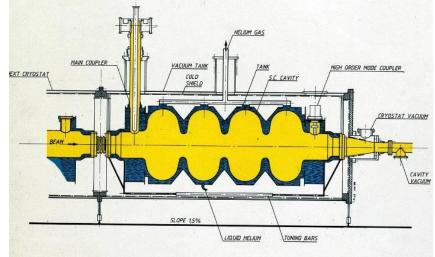
In general terms, a DTL-like structure is preferred at lowenergy, and  $\pi$ -mode structures at high-energy. CH is excellent at very low energies (ions).



### Multi-gap Superconducting linac structures (elliptical)







Standing wave structures for particles at β>0.5-0.7, widely used for protons (SNS, etc.) and electrons (ILC, etc.) f=350-700 MHz (protons), f=350 MHz - 3 GHz (electrons) Chain of cells electrically coupled, large apertures (ZT<sup>2</sup> not a concern).

Operating in  $\pi$ -mode, cell length  $\beta\lambda/2$ Input coupler placed at one end.



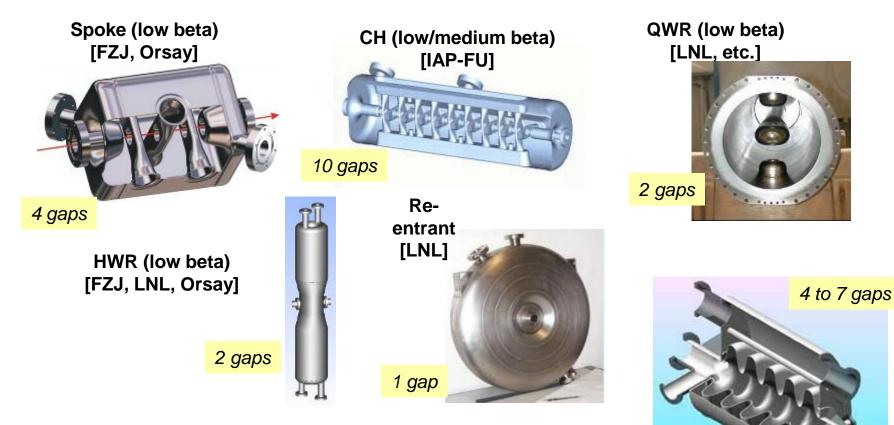


## The superconducting zoo



Elliptical cavities [CEA, INFN-MI, CERN, ...]

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Superconducting structure for linacs can have a small number of gaps  $\rightarrow$  used for low and medium beta.

Elliptical structures with more gaps (4 to 7) are used for medium and high beta.



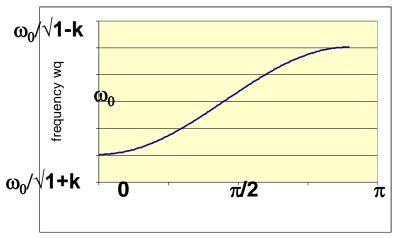
 $X_n^{(q)}$ 

# Traveling wave accelerating structures (electrons)



What happens if we have an infinite chain of oscillators?

$$\omega_q^2 = \frac{\omega_0^2}{1 + k \cos \frac{\pi q}{N}}, \quad q = 0, ..., N \quad \text{becomes } (N \to \infty) \quad \omega^2 = \frac{\omega_0^2}{1 + k \cos \varphi}$$
$$\omega^2 = \frac{\omega_0^2}{1 + k \cos \varphi}$$
$$\omega^2 = \frac{\omega_0^2}{1 + k \cos \varphi}$$
$$\omega^2 = \frac{\omega_0^2}{1 + k \cos \varphi}$$



All modes in the dispersion curve are allowed, the original frequency degenerates into a continuous band. The field is the same in each cell, there are no more standing wave modes  $\rightarrow$  only "traveling wave modes", if we excite the EM field at one end of the structure it will propagate towards the other end.

But: our dispersion curve remains valid, and defines the velocity of propagation of the travelling wave, v\_{\phi} = \omega d/\Phi

For acceleration, the wave must propagate at  $v_{\phi} = c$ 

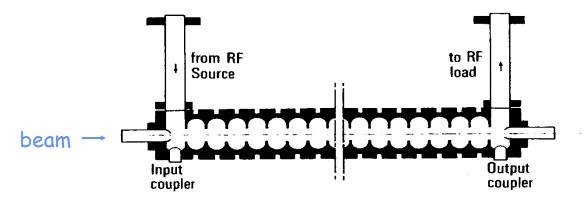
 $\rightarrow$  for each frequency  $\varpi$  and cell length d we can find a phase  $\Phi$  where the apparent velocity of the wave v\_{\_{\!\!\!\!\!\!\!\!\!\!\!\!\!}} is equal to c



# Traveling wave accelerating structures



How to "simulate" an infinite chain of resonators? Instead of a singe input, exciting a standing wave mode, use an input + an output for the RF wave at both ends of the structure.



"Disc-loaded waveguide" or chain of electrically coupled cells characterized by a continuous band of frequencies. In the chain is excited a "traveling wave mode" that has a propagation velocity v<sub>ph</sub> = ω/k given by the dispersion relation.

- For a given frequency  $\omega$ ,  $v_{ph}$  = c and the structure can be used for particles traveling at  $\beta$ =1 The "traveling wave" structure is the standard linac for electrons from  $\beta$ ~1.
- → Can <u>not</u> be used for protons at v<c:</p>
  - 1. constant cell length does not allow synchronism
  - 2. structures are long, without space for transverse focusing





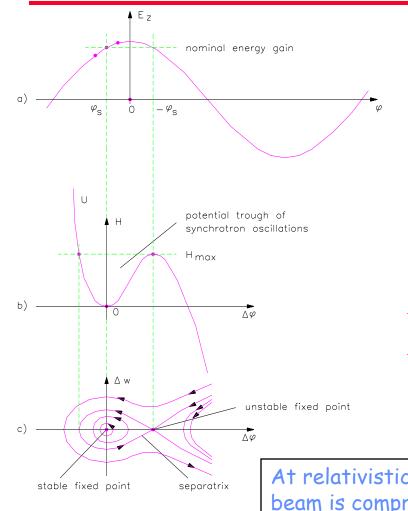
# 3 - Fundamentals of linac beam dynamics



# Longitudinal dynamics



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- Ions are accelerated around a (negative = linac definition) synchronous phase.
  - Particles around the synchronous one perform oscillations in the longitudinal phase space.
- Frequency of small oscillations:

$$\omega_l^2 = \omega_0^2 \frac{qE_0T\sin(-\varphi)\lambda}{2\pi mc^2\beta\gamma^3}$$

- Tends to zero for relativistic particles  $\gamma \gg 1$ .
- → Note phase damping of oscillations:

$$\Delta \varphi = \frac{const}{\left(\beta \gamma\right)^{3/4}} \qquad \Delta W = const \times \left(\beta \gamma\right)^{3/4}$$

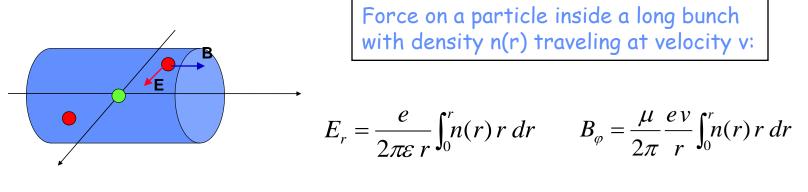
At relativistic velocities phase oscillations stop, and the beam is compressed in phase around the initial phase. The crest of the wave can be used for acceleration.

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- $\rightarrow$  Large numbers of particles per bunch ( ~10<sup>10</sup> ).
- → Coulomb repulsion between particles (space charge) plays an important role and is the main limitation to the maximum current in a linac.
- $\rightarrow$  But space charge forces ~  $1/\gamma^2$  disappear at relativistic velocity

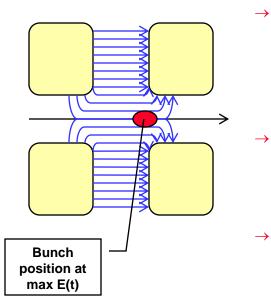


$$F = e(E_r - vB_{\varphi}) = eE_r(1 - \frac{v^2}{c^2}) = eE_r(1 - \beta^2) = \frac{eE_r}{\gamma^2}$$



# Transverse dynamics - RF defocusing





- RF defocusing experienced by particles crossing a gap on a longitudinally stable phase. Increasing field means that the defocusing effect going out of the gap is stronger than the focusing effect going in.
  - In the rest frame of the particle, only electrostatic forces  $\rightarrow$  no stable points (maximum or minimum)  $\rightarrow$  radial defocusing.
  - Lorentz transformation and calculation of radial momentum impulse per period (from electric and magnetic field contribution in the laboratory frame):

$$\Delta p_r = -\frac{\pi e E_0 T L r \sin \varphi}{c \beta^2 \gamma^2 \lambda}$$

→ Transverse defocusing ~  $1/\gamma^2$  disappears at relativistic velocity (transverse magnetic force cancels the transverse RF electric force).





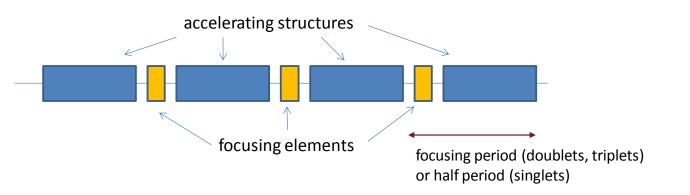


**Defocusing** forces need to be compensated by focusing forces  $\rightarrow$  alternating gradient focusing provided by quadrupoles along the beam line.

A linac alternates accelerating sections with focusing sections. Options are: one quadrupole (singlet focusing), two quadrupoles (doublet focusing) or three quadrupoles (triplet focusing).

Focusing period=length after which the structure is repeated (usually as  $N\beta\lambda$ ).

The accelerating sections have to match the increasing beam velocity  $\rightarrow$  the basic focusing period increases in length (but the beam travel time in a focusing period remains constant). The maximum allowed distance between focusing elements depends on beam energy and current and change in the different linac sections (from only one gap in the DTL to one or more multi-cell cavities at high energies).





### Transverse beam equilibrium in linacs



The equilibrium between external focusing force and internal defocusing forces defines the frequency of beam oscillations.

Oscillations are characterized in terms of *phase advance per focusing period*  $\sigma_t$ or *phase advance per unit length*  $k_t$ .

Ph. advance = Ext. quad focusing - RF defocusing - space charge

$$k_t^2 = \left(\frac{\sigma_t}{N\beta\lambda}\right)^2 = \left(\frac{q\,Gl}{2\,mc\,\beta\gamma}\right)^2 - \frac{\pi\,q\,E_0T\sin(-\varphi)}{mc^2\lambda\,\beta^3\gamma^3} - \frac{3q\,I\,\lambda(1-f)}{8\pi\varepsilon_0\,r_0^3mc^3\beta^2\gamma^3}$$

q=charge G=quad gradient I=length foc. element f=bunch form factor  $r_0$ =bunch radius  $\lambda$ =wavelength

Approximate expression valid for:

FODO lattice, smooth focusing approximation, space charge of a uniform 3D ellipsoidal bunch.

A "low-energy" linac is dominated by space charge and RF defocusing forces !!

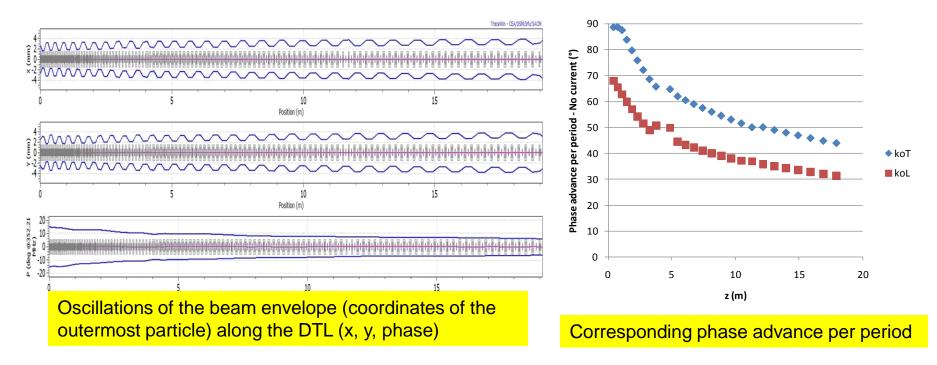
Phase advance per period must stay in reasonable limits (30-80 deg), phase advance per unit length must be continuous (smooth variations)  $\rightarrow$  at low  $\beta$ , we need a strong focusing term to compensate for the defocusing, but the limited space limits the achievable G and I  $\rightarrow$  needs to use short focusing periods N  $\beta\lambda$ .

Note that the RF defocusing term  $\infty f$  sets a higher limit to the basic linac frequency (whereas for shunt impedance considerations we should aim to the highest possible frequency,  $Z \propto \sqrt{f}$ ). <sup>3</sup>35





Beam optics of the Linac4 Drift Tube Linac (DTL): 3 to 50 MeV, 19 m, 108 focusing quadrupoles (permanent magnets).



#### **Design prescriptions:**

- •Tranverse phase advance at zero current always less than 90°.
- Smooth variation of the phase advance.
- Avoid resonnances (see next slide).







Focusing usually provided by quadrupoles.

- Need to keep the phase advance in the good range, with an approximately constant phase advance per unit length → The length of the focusing periods has to change along the linac, going gradually from short periods in the initial part (to compensate for high space charge and RF defocusing) to longer periods at high energy.
- For Protons (high beam current and high space charge), distance between two quadrupoles (=1/2 of a FODO focusing period):
  - $\beta\lambda$  in the DTL, from ~70mm (3 MeV, 352 MHz) to ~250mm (40 MeV),
  - can be increased to 4-10 $\beta\lambda$  at higher energy (>40 MeV).
  - longer focusing periods require special dynamics (example: the IH linac).

For Electrons (no space charge, no RF defocusing): focusing periods up to several meters, depending on the required beam

conditions. Focusing is mainly required to control the emittance. <sup>37</sup>





### 4. Linac architecture



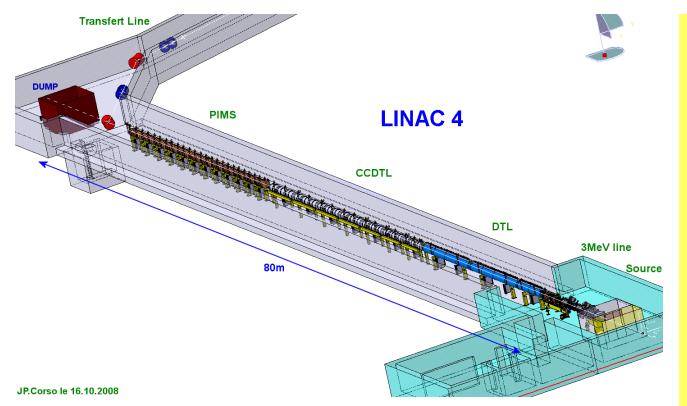


### Architecture: cell length, focusing period



EXAMPLE: the Linac4 project at CERN. H-, 160 MeV energy, 352 MHz. A 3 MeV injector + 22 multi-cell standing wave accelerating structures of 3 types

DTL, 3-50 MeV: every cell is different, focusing quadrupoles in each drift tube, 0-mode CCDTL, 50-100 MeV: sequences of 2 identical cells, quadrupoles every 3 cells, 0 and  $\pi/2$  mode PIMS, 100-160 MeV: sequences of 7 identical cells, quadrupoles every 7 cells,  $\pi/2$  mode



Two basic principles to remember:

1. As beta increases, phase error between cells of identical length becomes small  $\rightarrow$  we can have short sequences of identical cells (lower construction costs).

2. As beta increases, the distance between focusing elements can increase.



# Linac architecture: the frequency



approximate scaling laws for linear accelerators:

- RF defocusing (ion linacs)
- **Cell length (=** $\beta\lambda/2$ **)**
- Peak electric field
- Shunt impedance (power efficiency)
- Accelerating structure dimensions
- Machining tolerances

- ~ frequency
- ~ (frequency)<sup>-1</sup>
- ~ (frequency)<sup>1/2</sup>
- ~ (frequency)<sup>1/2</sup>
- ~ (frequency)<sup>-1</sup>
- ~ (frequency)<sup>-1</sup>
- → Higher frequencies are economically convenient (shorter, less RF power, higher gradients possible) but the limitation comes from mechanical precision required in construction (tight tolerances are expensive!) and beam dynamics for ion linacs.
- → The main limitation to the initial frequency (RFQ) comes from RF defocusing (~  $1/(\lambda\beta^2\gamma^2)$  402 MHz is the maximum achievable so far for currents in the range of tens of mA's.
- → High-energy linacs have one or more frequency jumps (start 200-400 MHz, first jump to 400-800 MHz, possible a 3<sup>rd</sup> jump to 600-1200 MHz): compromise between focusing, cost and size.



### Linac architecture: superconductivity



Advantages of Superconductivity:

- Much smaller RF system (only beam power) → prefer low current/long pulse
- Larger aperture (lower beam loss).
- Lower operating costs (electricity consumption).
- Higher gradients (thanks to cleaning procedures)

### Disadvantages of Superconductivity:



- Need cryogenic system (in pulsed machines, size dominated by static loss  $\rightarrow$  prefer low repetition frequency or CW to minimize filling time/beam time).
- In proton linacs, need cold/warm transitions to accommodate quadrupoles  $\rightarrow$  becomes more expensive at low energy (short focusing periods).
- Individual gradients difficult to predict (large spread)  $\rightarrow$  for protons, need large safety margin in gradient at low energy.

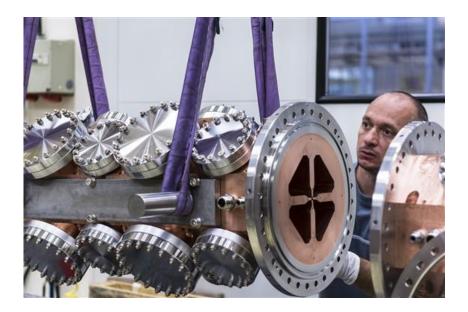
### **Conclusions**:

- 1. Superconductivity gives a large advantage in cost at high energy (protons)/ high duty cycle.
- 2. At low proton energy / low duty cycle superconducting sections are expensive.





# 5. The Radio-Frequency Quadrupole

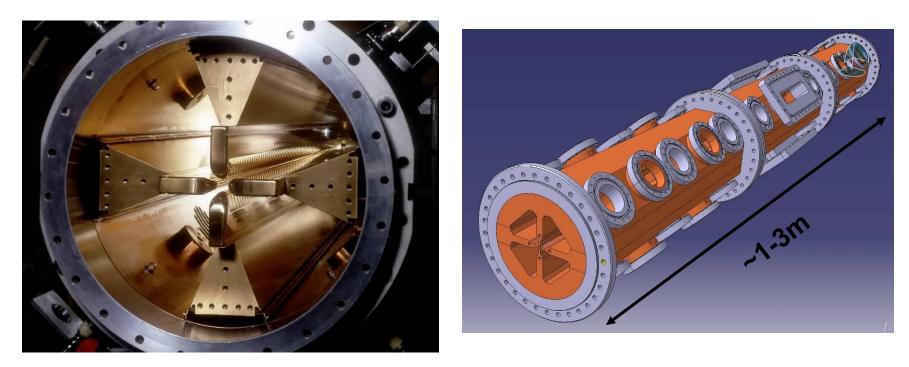




### The Radio Frequency Quadrupole (RFQ)



At low proton (or ion) energies, space charge defocusing is high and quadrupole focusing is not very effective, cell length becomes small  $\rightarrow$  conventional accelerating structures (Drift Tube Linac) are very inefficient  $\rightarrow$  use a (relatively) new structure, the Radio Frequency Quadrupole.



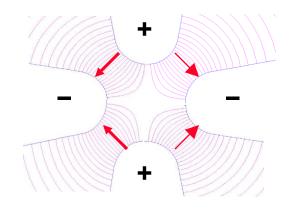
 $\underline{RFQ} = \underline{Electric\ quadrupole\ focusing\ channel + bunching + acceleration} \qquad 43$ 

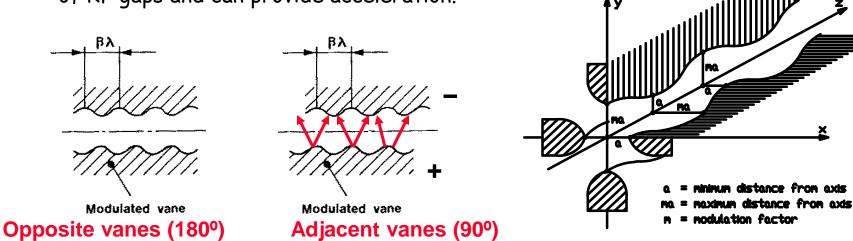


**RFQ** properties - 1



- 1. Four electrodes (vanes) between which we excite an RF Quadrupole mode (TE210)  $\rightarrow$  Electric focusing channel, alternating gradient with the period of the RF. Note that electric focusing does not depend on the velocity (ideal at low  $\beta$ !)
- 2. The vanes have a <u>longitudinal modulation</u> with period =  $\beta\lambda \rightarrow$  this creates a longitudinal component of the electric field. The modulation corresponds exactly to a series of RF gaps and can provide acceleration.





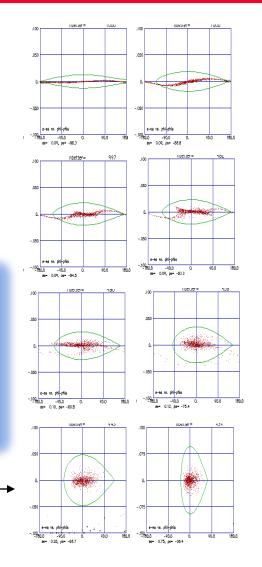






- 3. The <u>modulation period</u> (distance between maxima) can be slightly adjusted to change the phase of the beam inside the RFQ cells, and the <u>amplitude of the modulation</u> can be changed to change the accelerating gradient → we can start at -90° phase (linac) with some bunching cells, progressively bunch the beam (<u>adiabatic bunching channel</u>), and only in the last cells switch on the acceleration.
- An RFQ has 3 basic functions:
- 1. Adiabatically <u>bunching</u> of the beam.
- 2. <u>Focusing</u>, on electric quadrupole.
- 3. <u>Accelerating</u>.

Longitudinal beam profile of a proton beam along the CERN RFQ2: from a continuous beam to a bunched accelerated beam in 300 cells.

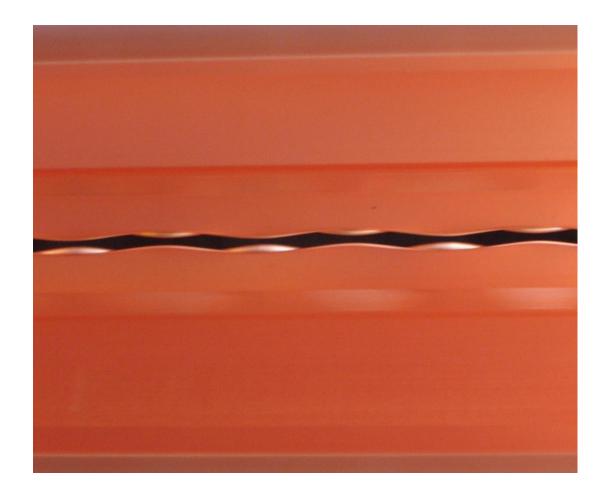


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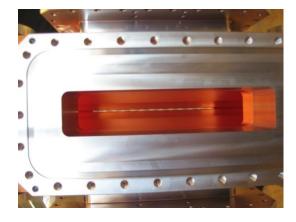


# Peeping into an RFQ...





Looking from the RF port into the new CERN RFQ (Linac4, 2011)

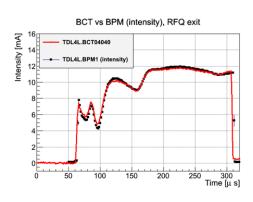




## The Linac4 RFQ



Energy 45 keV – 3 MeV, length 3 m, voltage 78 kV, RF power 700 kW Completed September 2012, beam commissioning on the Test Stand in March 2013 Compact design, aiming at high reliability.



The Linac4 RFQ not only focuses and accelerates the beam as required, but so far it does it in a stable, reliable and reproducible way!





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