RF Systems

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Outline

 Definitions and basic concepts On modulation Digital Signal Processing • RF System & Control Loops • RF Power Sources • Fields in a Waveguide From Waveguide to Cavity Accelerating Gap • Characterizing a Cavity • Many Gaps Superconducting Cavities Some Examples of RF Systems

Definitions & basic concepts

dB *t*-domain vs. ω-domain phasors

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Decibel (dB)

Convenient logarithmic measure of a power ratio.
A "Bel" (= 10 dB) is defined as a power ratio of 10¹. Consequently, 1 dB is a power ratio of 10^{0.1}≈1.259
If *rdb* denotes the measure in dB, we have:

 $rdb = 10 \text{ dB} \log\left(\frac{P_2}{P_1}\right) = 10 \text{ dB} \log\left(\frac{A_2^2}{A_1^2}\right) = 20 \text{ dB} \log\left(\frac{A_2}{A_1}\right)$

 $\frac{P_2}{P_1} = \frac{A_2^2}{A_1^2} = 10^{rdb/(10 \text{ dB})}$

 $\frac{A_2}{A_1} = 10^{rdb/(20 \, \text{dB})}$

rdb	-30 dB	-20 dB	-10 dB	-6 dB	-3 dB	o dB	3 dB	6 dB	10 dB	20 dB	30 dB
P_{2}/P_{1}	0.001	0.01	0.1	0.25	.50	1	2	3.98	10	100	1000
A_{2}/A_{1}	0.0316	0.1	0.316	0.50	.71	1	1.41	2	3.16	10	31.6

• Related: dBm (relative to 1 mW), dBc (relative to carrier)

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Time domain – frequency domain (1)

- An arbitrary signal g(t) can be expressed in ω -domain using the *Fourier transform* (FT). $g(t) \rightarrow G(\omega) = \frac{1}{\sqrt{2\pi}} \int_{\infty}^{\infty} g(t) e^{j\omega t} dt$
- The inverse transform (IFT) is also referred to as **Fourier Integral** G(ω) ••• $g(t) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} G(\omega) e^{-j\omega t} d\omega$
- The advantage of the ω-domain description is that linear time-invariant (LTI) systems are much easier described.
- The mathematics of the FT requires the extension of the definition of a *function* to allow for infinite values and non-converging integrals.
 - The FT of the signal can be understood at looking at "what frequency components it is composed of".

Time domain – frequency domain (2)

- For *T*-periodic signals, the FT becomes the Fourier-Series, $d\omega$ becomes $2\pi/T$, \int becomes Σ .
- The cousin of the FT is the *Laplace transform*, which uses a complex variable (often s) instead of *j*ω; it has generally a better convergence behaviour.
- Numerical implementations of the FT require discretisation in t (sampling) and in ω. There exist very effective algorithms (FFT).
- In digital signal processing, one often uses the related z-Transform, which uses the variable $z = e^{j\omega\tau}$, where τ is the sampling period. A delay of $k\tau$ becomes z^{-k} .

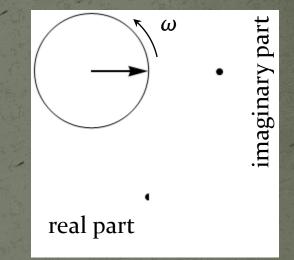
Fixed frequency oscillation (steady state, CW) Definition of phasors

• General: $A\cos(\omega t - \varphi) = A\cos(\omega t)\cos(\varphi) + A\sin(\omega t)\sin(\varphi)$

• This can be interpreted as the projection on the real axis of a circular motion in the complex plane. Re $\{A(\cos(\varphi) + j\sin(\varphi))e^{j\omega t}\}$

 The complex amplitude A is called "phasor".

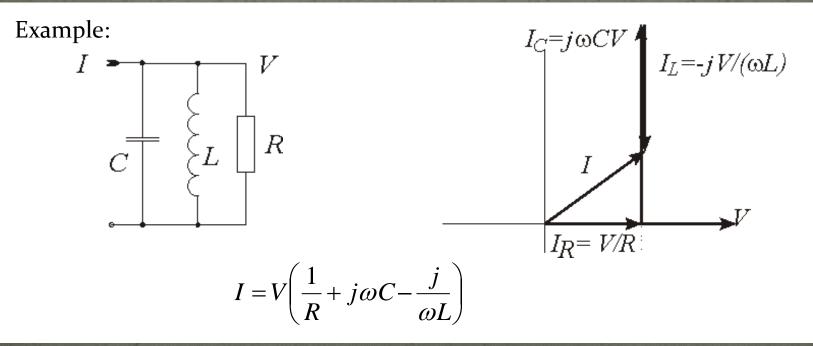
 $\widetilde{A} = A\left(\cos(\varphi) + j\sin(\varphi)\right)$



Calculus with phasors

• Why this seeming "complication"?: Because things become easier!

• Using $\frac{d}{dt} \equiv j\omega$, one may now forget about the rotation with ω and the projection on the real axis, and do the complete analysis making use of complex algebra!



Slowly varying amplitudes

• For band-limited signals, one may conveniently use "slowly varying" phasors and a fixed frequency RF oscillation.

• So-called in-phase (I) and quadrature (Q) "baseband envelopes" of a modulated RF carrier are the real and imaginary part of a slowly varying phasor.

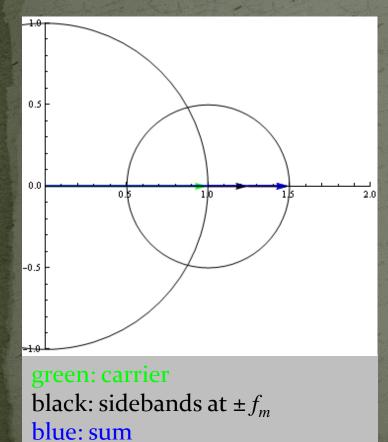
On Modulation

AM PM I-Q

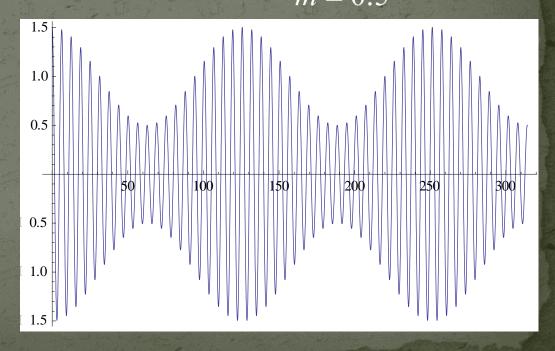
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Amplitude modulation

$$(1+m\cos(\varphi))\cdot\cos(\omega_{c}t) = \operatorname{Re}\left\{\left(1+\frac{m}{2}e^{j\varphi}+\frac{m}{2}e^{-j\varphi}\right)e^{j\omega_{c}t}\right\}$$

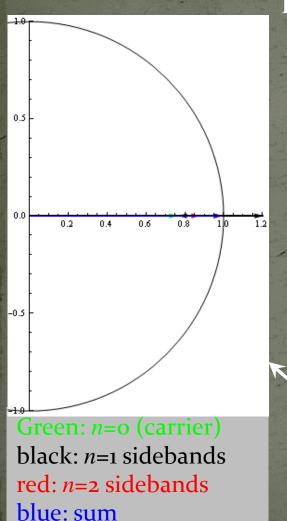


m: modulation index or modulation depth example: $\varphi = \omega_m t = 0.05 \omega_c t$ m = 0.5



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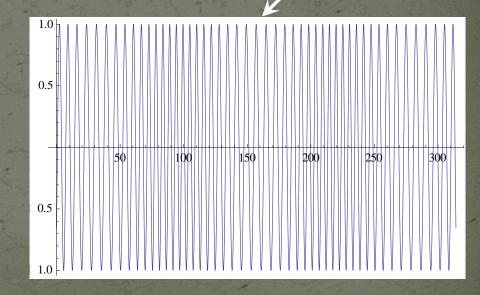
Phase modulation



 $\operatorname{Re}\left\{e^{j\omega_{c}t+M\sin(\varphi)}\right\} = \operatorname{Re}\left\{\sum_{n=-\infty}^{\infty}J_{n}(M)e^{j(n\varphi+\omega_{c}t)}\right\}$

M: modulation index (= max. phase deviation)

 $\varphi = \omega_m t = 0.05 \,\omega_c t$ M = 4

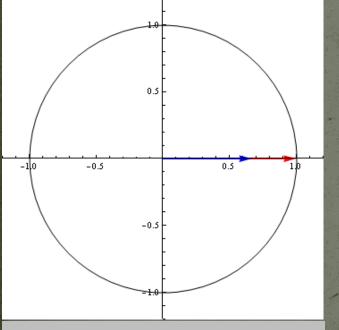


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 $\dot{M} = 1$

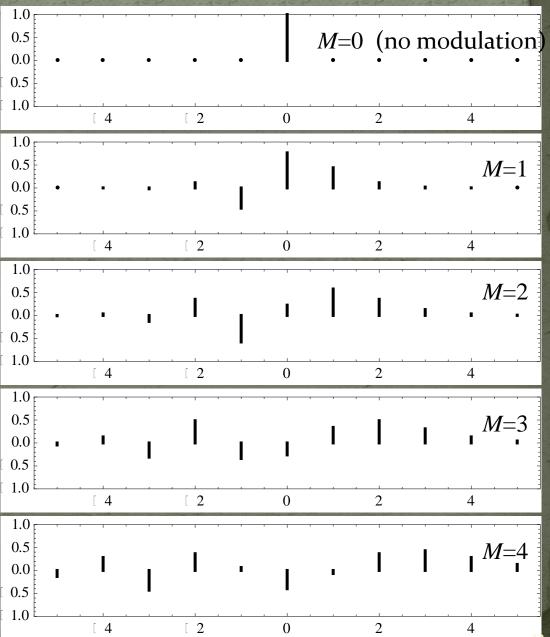
Spectrum of phase modulation

Plotted: spectral lines for sinusoidal PM at f_m Abscissa: $(f-f_c)/f_m$



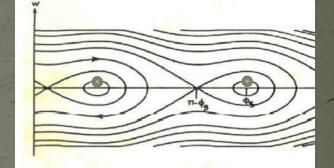
Phase modulation with $M=\pi$: red: real phase modulation blue: sum of sidebands $n \le 3$

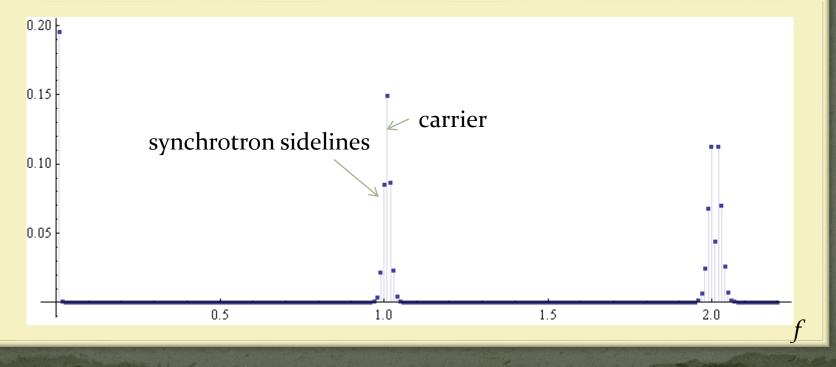
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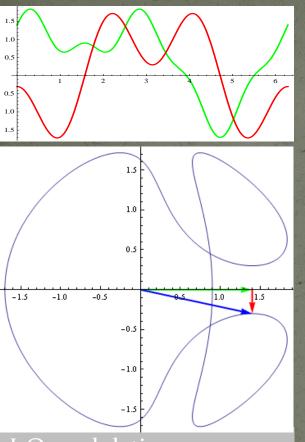
Spectrum of a beam with synchrotron oscillation, M = 1 (=57°)





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Vector (I-Q) modulation



I-Q modulation: green: *I* component red: *Q* component blue: vector-sum More generally, a modulation can have both amplitude and phase modulating components. They can be described as the in-phase (I) and quadrature (Q) components in a chosen reference, $cos(\omega_r t)$. In complex notation, the modulated RF is:

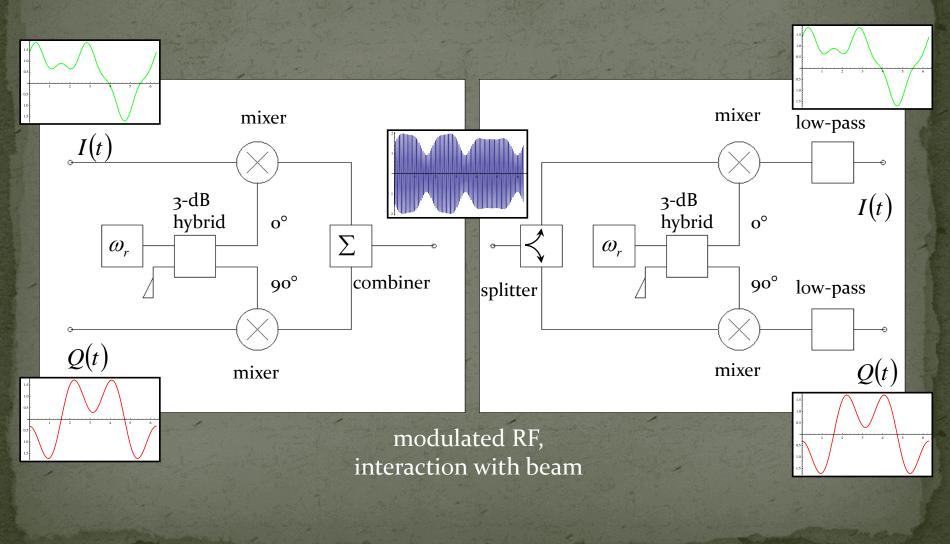
 $\operatorname{Re}\left\{ (I(t) + jQ(t))e^{j\omega_{r}t} \right\} =$ $\operatorname{Re}\left\{ (I(t) + jQ(t))(\cos(\omega_{r}t) + j\sin(\omega_{r}t)) \right\}$ $I(t)\cos(\omega_{r}t) - Q(t)\sin(\omega_{r}t)$

So *I* and *Q* are the cartesian coordinates in the complex "Phasor" plane, where amplitude and phase are the corresponding polar coordinates.

 $I(t) = A(t) \cdot \cos(\varphi)$ $Q(t) = A(t) \cdot \sin(\varphi)$

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Vector modulator/demodulator



Digital Signal Processing

Just some basics

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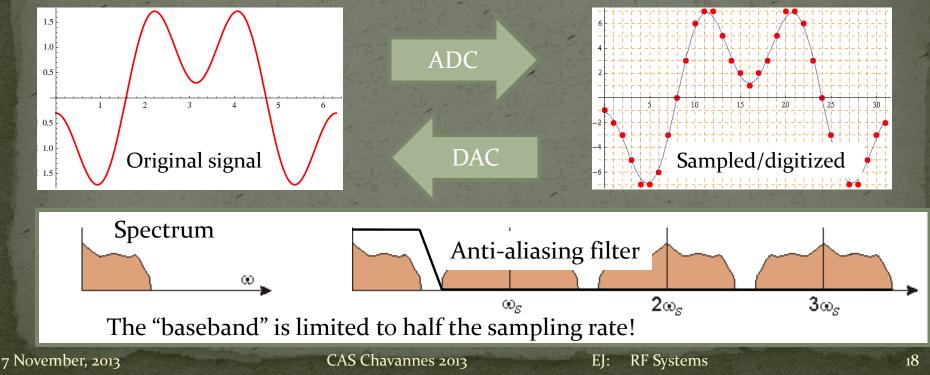
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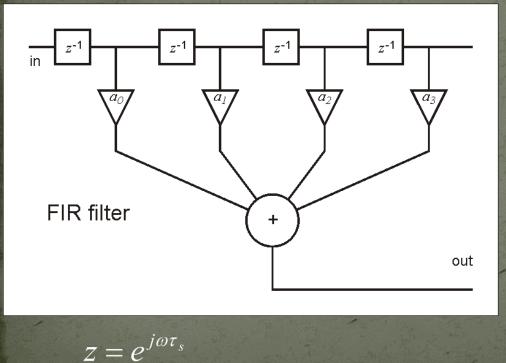
Sampling and quantization

- Digital Signal Processing is very powerful note recent progress in digital audio, video and communication!
- Concepts and modules developed for a huge market; highly sophisticated modules available "off the shelf".
- The "slowly varying" phasors are ideal to be sampled and quantized as needed for digital signal processing.
 - Sampling (at $1/\tau_s$) and quantization (*n* bit data words here 4 bit):



Digital filters (1)

- Once in the digital realm, signal processing becomes "computing"!
- In a "finite impulse response" (FIR) filter, you directly program the coefficients of the impulse response.



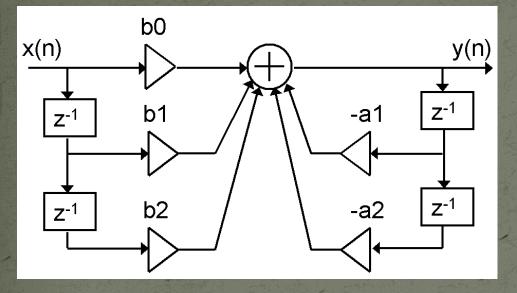
$$a_{0} = \frac{1}{f_{s}} a_{1} = \frac{a_{2}}{a_{3}} a_{4}$$

Fransfer function:
 $a_{1}z^{-1} + a_{2}z^{-2} + a_{3}z^{-3} + a_{4}z^{-3}$

 \boldsymbol{a}

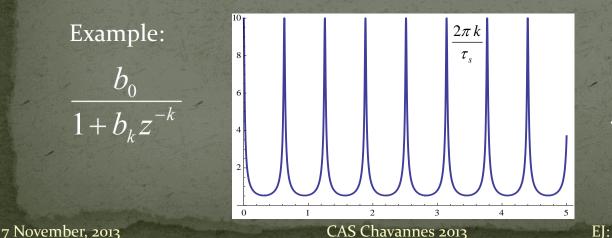
Digital filters (2)

 An "infinite impulse response" (IIR) filter has built-in recursion, e.g. like



Transfer function:

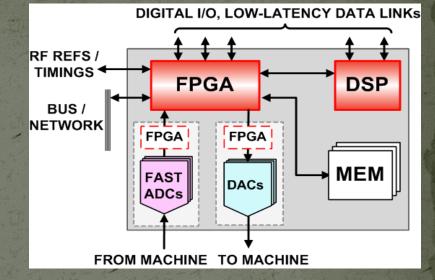
 $\frac{\overline{b_0} + \overline{b_1 z^{-1}} + \overline{b_2 z^{-2}}}{1 + a_1 z^{-1} + a_2 z^{-2}}$



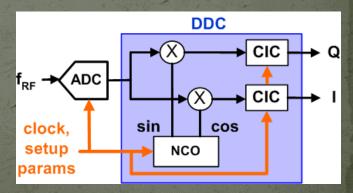
... is a comb filter

Digital LLRF building blocks – examples

 General D-LLRF board:
 modular!
 FPGA: Field-programmable gate array DSP: Digital Signal Processor



 DDC (Digital Down Converter)
 Digital version of the I-Q demodulator
 CIC: cascaded integrator-comb (a special low-pass filter)



RF system & control loops

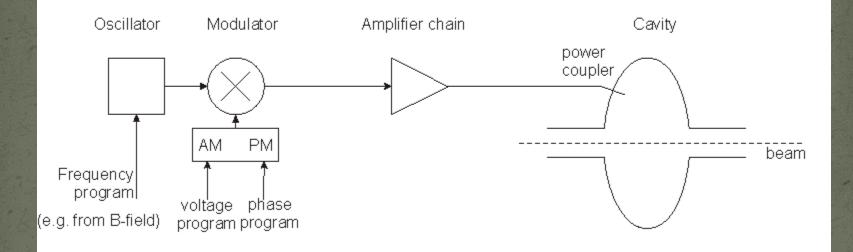
e.g.: ... for a synchrotron: Cavity control loops Beam control loops

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Minimal RF system (of a synchrotron)

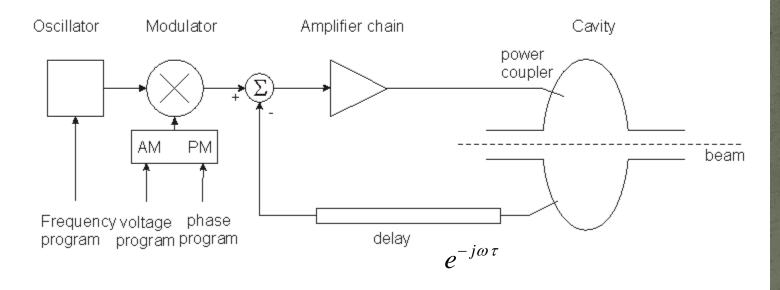
Low-level RF

High-Power RF



- The frequency has to be controlled to follow the magnetic field such that the beam remains in the centre of the vacuum chamber.
- The voltage has to be controlled to allow for capture at injection, a correct bucket area during acceleration, matching before ejection; phase may have to be controlled for transition crossing and for synchronisation before ejection.

Fast RF Feed-back loop



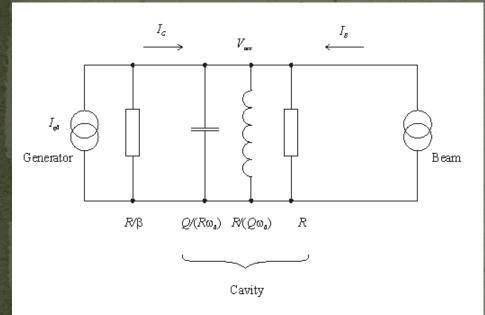
- Compares actual RF voltage and phase with desired and corrects.
- Rapidity limited by total group delay (path lengths) (some 100 ns).
- Unstable if loop gain =1 with total phase shift 180 ° design requires to stay away from this point (stability margin)
- The group delay limits the gain bandwidth product.
- Works also to keep voltage at zero for strong beam loading, i.e. it reduces the beam impedance.

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Fast feedback loop at work



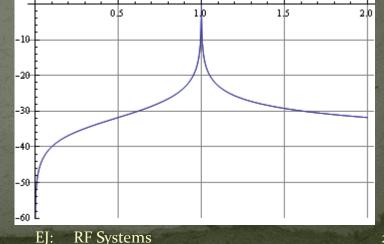
- Gap voltage is stabilised!
- Impedance seen by the beam is reduced by the loop gain!
- Plot on the right: $\frac{1+\beta}{R} \left| \frac{Z(\omega)}{1+G \cdot Z(\omega)} \right|$ vs. ω

with the loop gain varying from 0 to 50 dB

• Without feedback, $V_{acc} = (I_{G0} + I_B) \cdot Z(\omega)$ where $Z(\omega) = \frac{R/(1+\beta)}{1+jQ\left(\frac{\omega}{\omega_0} - \frac{\omega_0}{\omega}\right)}$ • Detect the gap voltage, feed it back to I_{G0} such that $I_{G0} = I_{drive} - G \cdot V_{acc}$

where *G* is the total loop gain (pick-up, cable, amplifier chain ...)
Result: Z(ω)

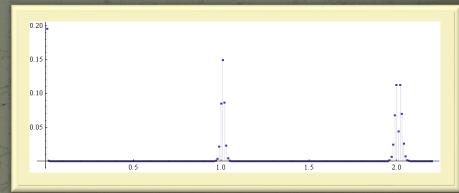
$$V_{acc} = (I_{drive} + I_B) \cdot \frac{Z(\omega)}{1 + G \cdot Z(\omega)}$$

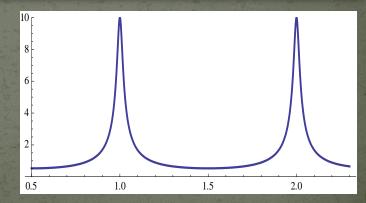


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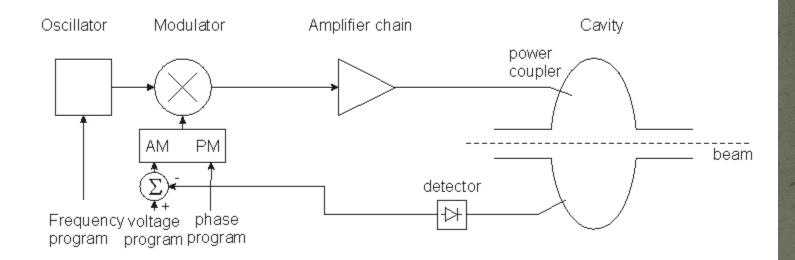
1-turn delay feed-back loop

- The speed of the "fast RF feedback" is limited by the group delay this is typically a significant fraction of the revolution period.
- How to lower the impedance over many harmonics of the revolution frequency?
- Remember: the beam spectrum is limited to relatively narrow bands around the multiples of the revolution frequency!
- Only in these narrow bands the loop gain must be high!
- Install a comb filter! ... and extend the group delay to exactly 1 turn – in this case the loop will have the desired effect and remain stable!





Field amplitude control loop (AVC)



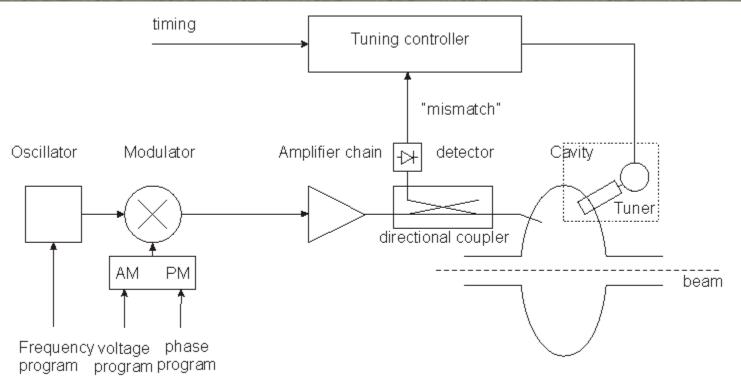
Compares the detected cavity voltage to the voltage program. The error signal serves to correct the amplitude

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Tuning loop



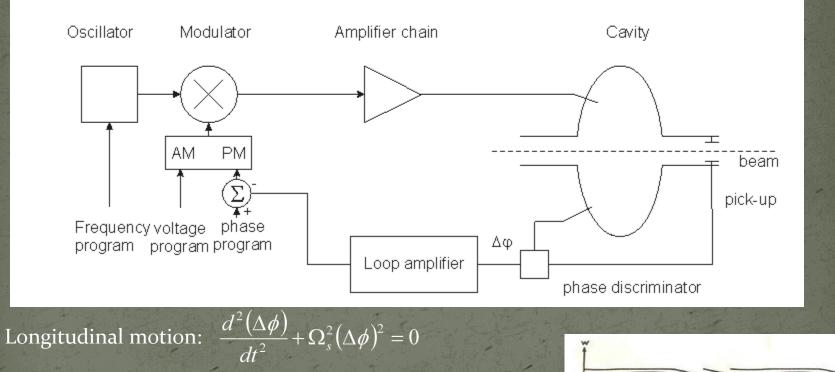
- Tunes the resonance *f* of the cavity to minimize the mismatch of the PA.
- In the presence of beam loading, this may mean $f_r \neq f$.
- In an ion ring accelerator, the tuning range might be > octave!
- For fixed *f* systems, tuners are needed to compensate for slow drifts.
- Examples for tuners:
 - controlled power supply driving ferrite bias (varying μ),
 - stepping motor driven plunger,
 - motorized variable capacitor, ...

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Beam phase loop



Loop amplifier transfer function designed to damp
synchrotron oscillation. Modified equation:

$$\frac{d^2(\Delta\phi)}{dt^2} + \alpha \frac{d(\Delta\phi)}{dt} + \Omega_s^2(\Delta\phi)^2 = 0$$

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Other loops

• Radial loop:

Detect average radial position of the beam,

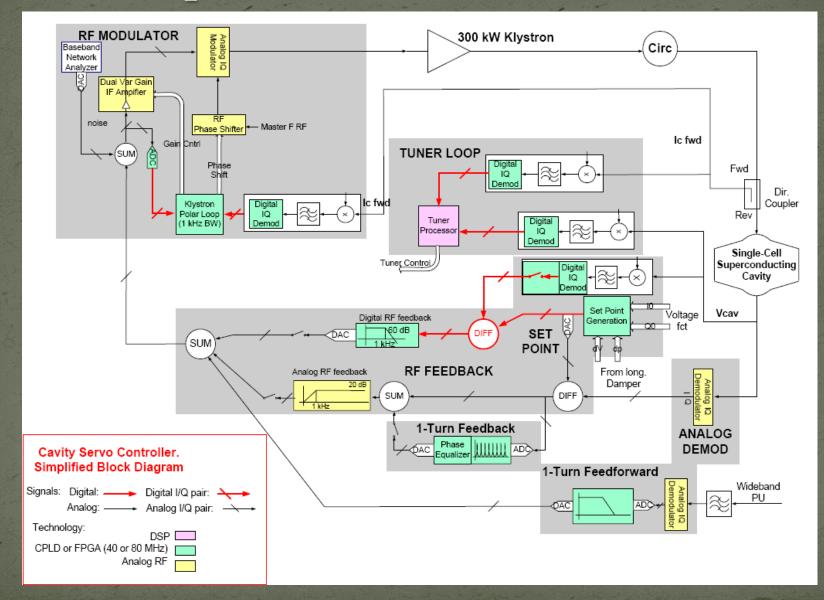
- Compare to a programmed radial position,
- Error signal controls the frequency.

Synchronisation loop:

1st step: Synchronize *f* to an external frequency (will also act on radial position!).

2nd step: phase loop

A real implementation: LHC LLRF



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RF power sources

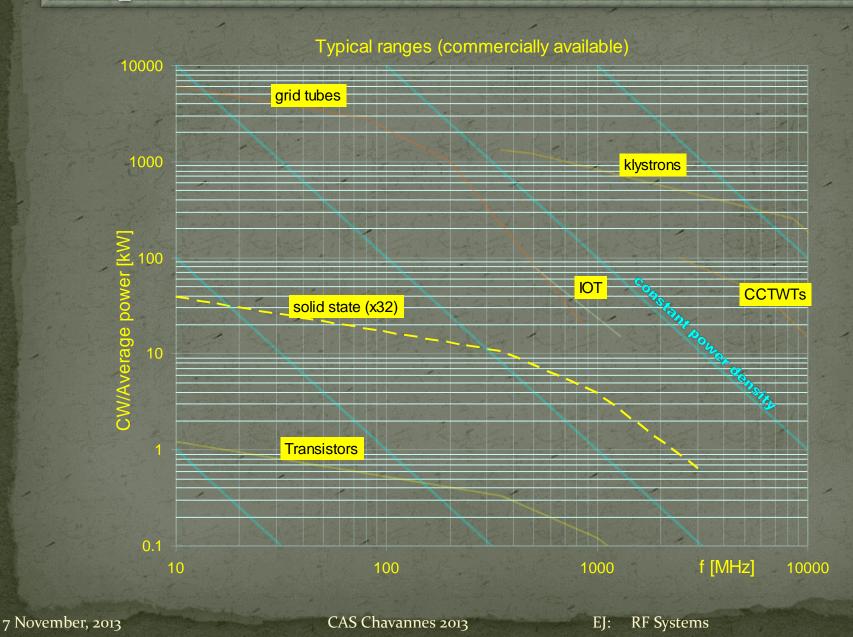
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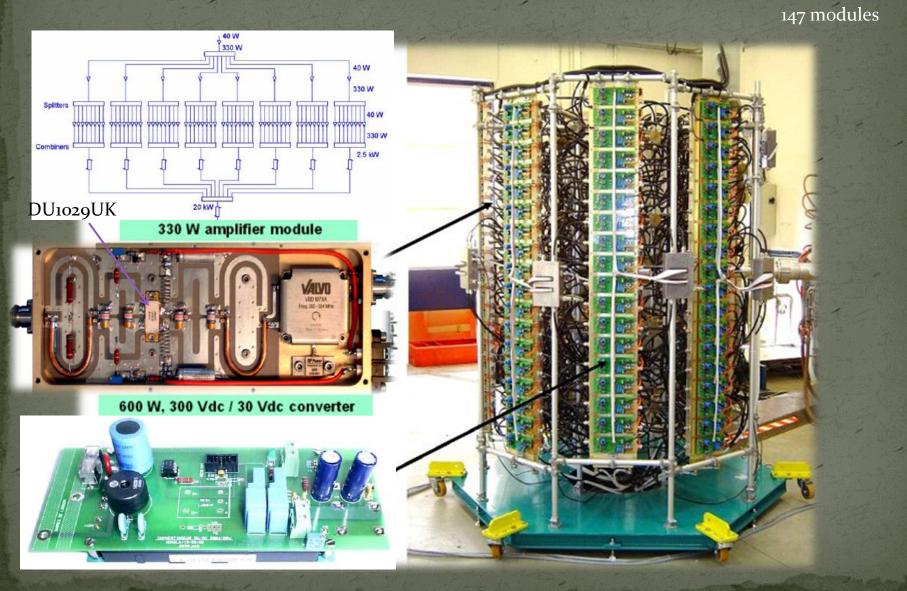
RF power sources



LEIR SSPA, 1 kW, 0.2 – 50 MHz

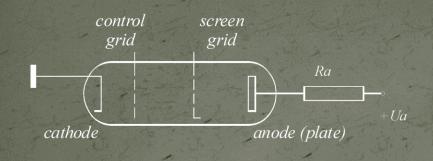


Soleil Booster SSPA, 40 kW, 352 MHz



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Tetrode



potential

4CX250B (Eimac/CPI), < 500 MHz, 600 W (Anode removed)



Ugl

RS 1084 CJ (ex Siemens, now Thales), < 30 MHz, 75 kW

YL1520 (ex Philips, now Richardson), < 260 MHz, 25 kW

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Ia max

High power tetrode amplifier

FINAL 101MHz 350KW J

BERTRONIC

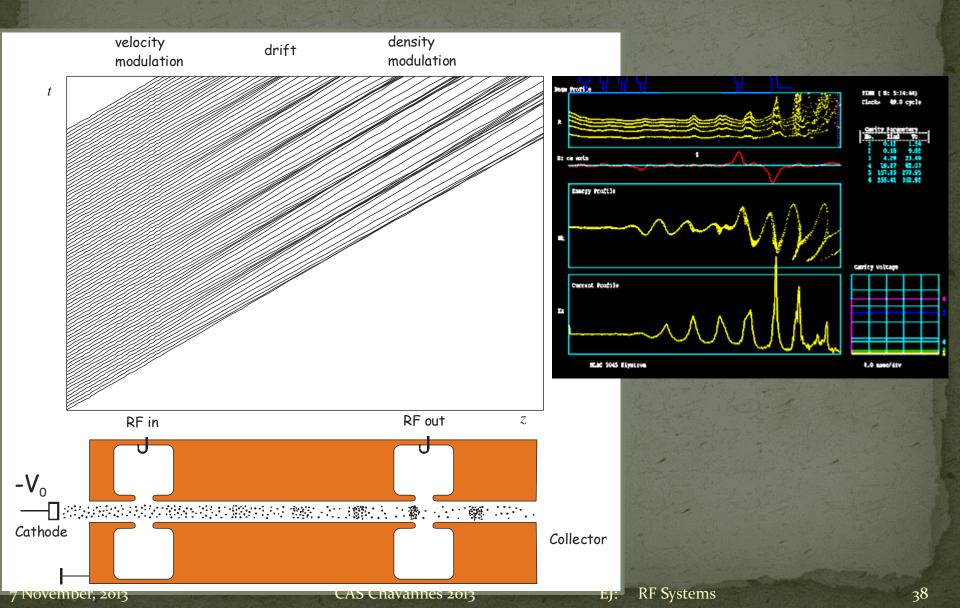
CERN Linac3: 100 MHz, 350 kW 50 kW Driver: TH345, Final: RS 2054 SK

CERN PS: 13-20 MHz, 30 kW Driver: solid state 400 W, Final: RS 1084 CJSC



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Klystron principle



Klystrons

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CERN CTF3 (LIL): 3 GHz, 45 MW, 4.5 μs, 50 Hz, η 45 %

> CERN LHC: 400 MHz, 300 kW, CW, η 62 %



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Fields in a waveguide

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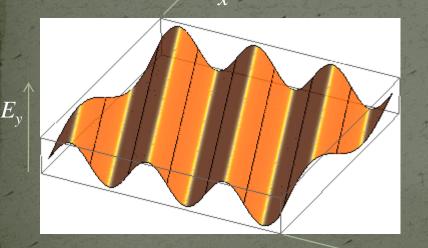
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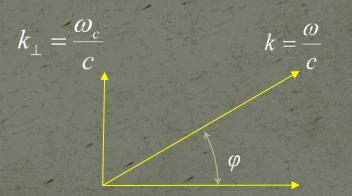
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Homogeneous plane wave

 $\vec{E} \propto \vec{u}_{y} \cos\left(\omega t - \vec{k} \cdot \vec{r}\right)$ $\vec{B} \propto \vec{u}_{x} \cos\left(\omega t - \vec{k} \cdot \vec{r}\right)$ $\vec{k} \cdot \vec{r} = \frac{\omega}{c} \left(\cos(\varphi)z + \sin(\varphi)x\right)$

Wave vector \overline{k} : the direction of \overline{k} is the direction of propagation, the length of \overline{k} is the phase shift per unit length. \overline{k} behaves like a vector.





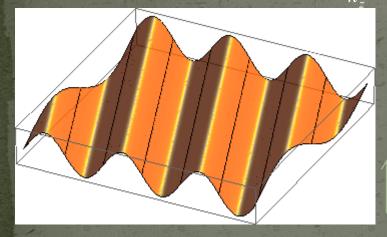
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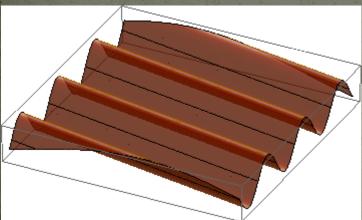
Wave length, phase velocity

• The components of \overline{k} are related to the wavelength in the direction of that component as $\lambda_z = \frac{2\pi}{k}$ etc., to the phase velocity as $v_{\varphi,z} = \frac{\omega}{k} = f \lambda_z$.

 $k_{\perp} = \frac{\omega_c}{c}$

 $k_{\perp} = \frac{\omega_c}{c}$





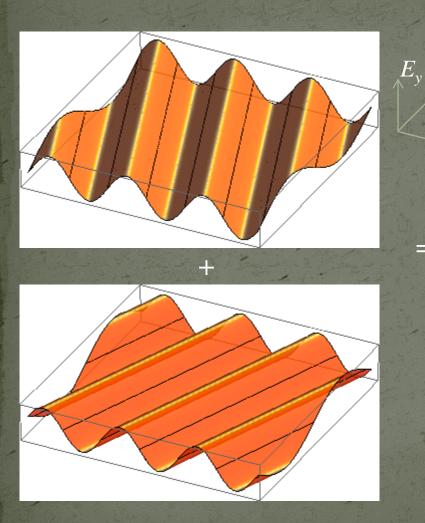
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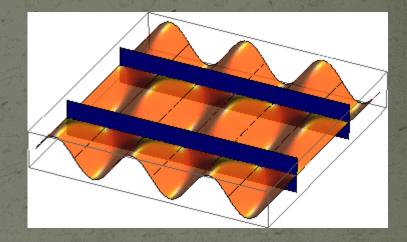
 $\rightarrow k_z = \frac{\omega}{c} \sqrt{1 - \left(\frac{\omega_c}{\omega}\right)^2}$

 $\int k = \frac{\omega}{c}$

 $k = \frac{\omega}{\omega}$

Superposition of 2 homogeneous plane waves





Metallic walls may be inserted where $E_y \equiv 0$ without perturbing the fields. Note the standing wave in *x*-direction!

This way one gets a hollow rectangular waveguide

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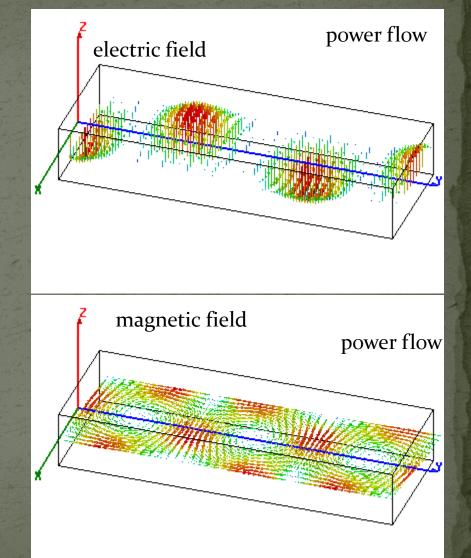
Rectangular waveguide

Fundamental (TE₁₀ or H₁₀) mode in a standard rectangular waveguide. <u>Example:</u> "S-band" : 2.6 GHz ... 3.95 GHz,

Waveguide type WR284 (2.84" wide), dimensions: 72.14 mm x 34.04 mm.

Operated at f = 3 GHz.

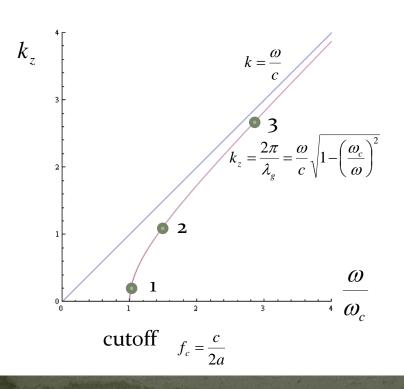
power flow: $\frac{1}{2}$ Re $\{\iint \vec{E} \times \vec{H}^* \cdot d\vec{A}\}$

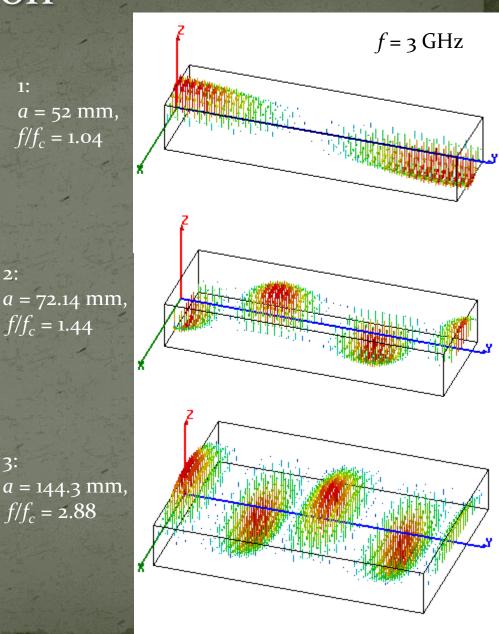


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Waveguide dispersion

What happens with different waveguide dimensions (different width *a*)?





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1:

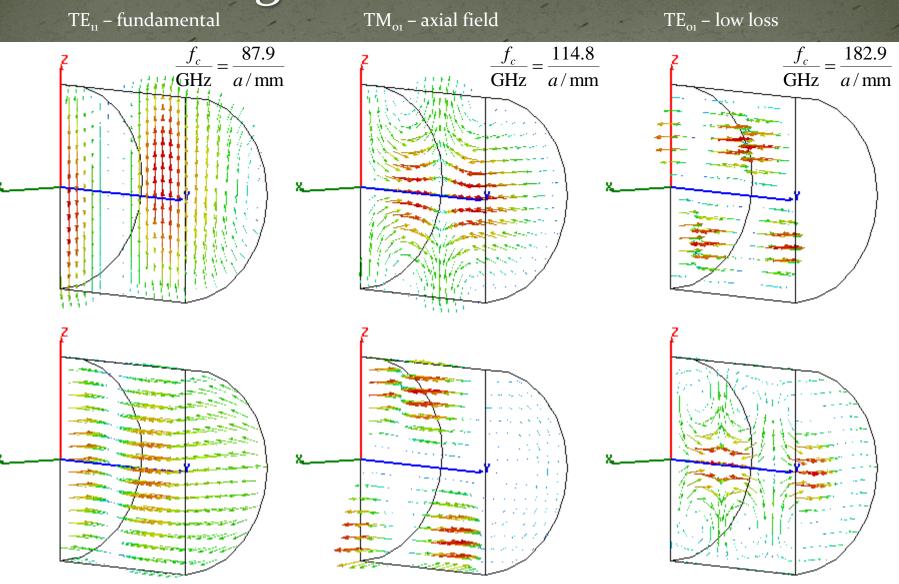
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CJ.

NF Systems

Round waveguide modes



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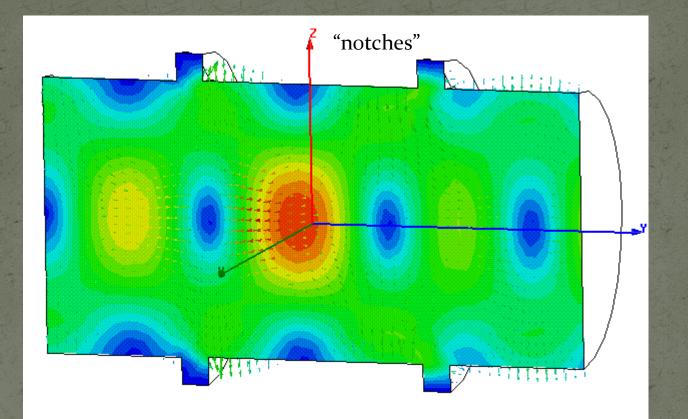
From waveguide to cavity

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Waveguide perturbed by notches

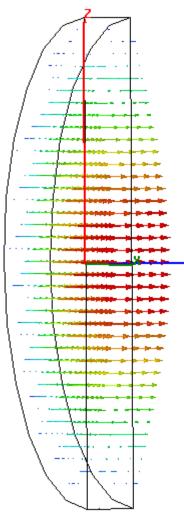


Reflections from notches lead to a superimposed standing wave pattern. "Trapped mode"

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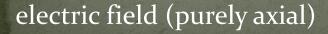
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More drastic than notches: short circuits!



TM₀₁₀-mode

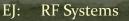
This is called "Pillbox cavity"



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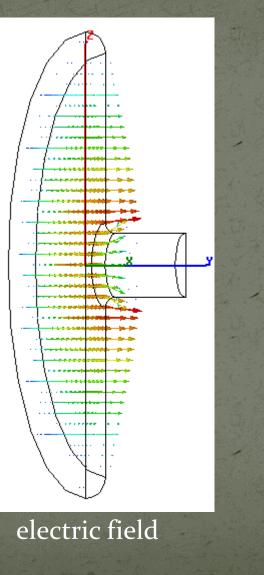
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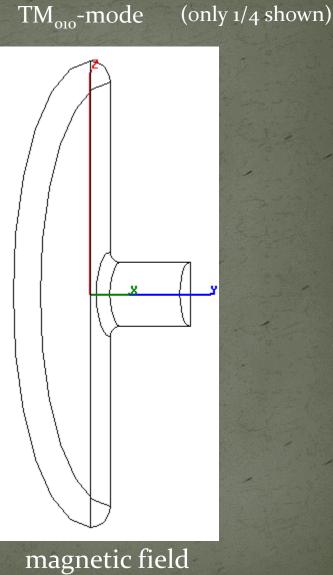
magnetic field (purely azimuthal)



A more practical pillbox cavity

Beam pipe added, sharp edges rounded off





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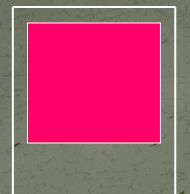
Accelerating gap

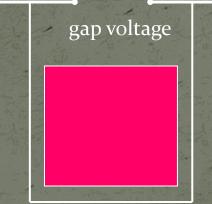
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Accelerating gap





We want a voltage across the gap!

It cannot be DC, since we want the beam tube on ground potential.

Use $\int \vec{E} \cdot d\vec{s} = -\iint \frac{d\vec{B}}{dt} \cdot d\vec{A}$

The "shield" imposes a upper limit of the voltage pulse duration or – equivalently – a lower limit to the usable frequency.

The limit can be extended with a material which acts as "open circuit"!

Materials typically used:

ferrites (depending on *f*-range) magnetic alloys (MA) like Metglas[®], Finemet[®], Vitrovac[®]...

resonantly driven with RF (ferrite loaded cavities) – or with pulses (induction cell)

Ferrite cavity

PS Booster, '98 0.6 - 1.8 MHz, < 10 kV gap NiZn ferrites

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Gap of PS cavity (prototype)

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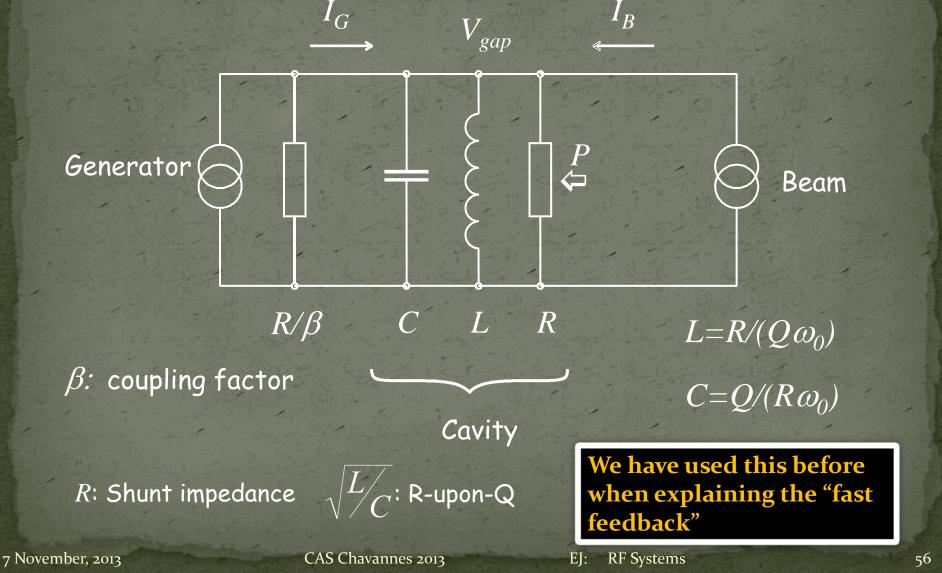
Characterizing a cavity

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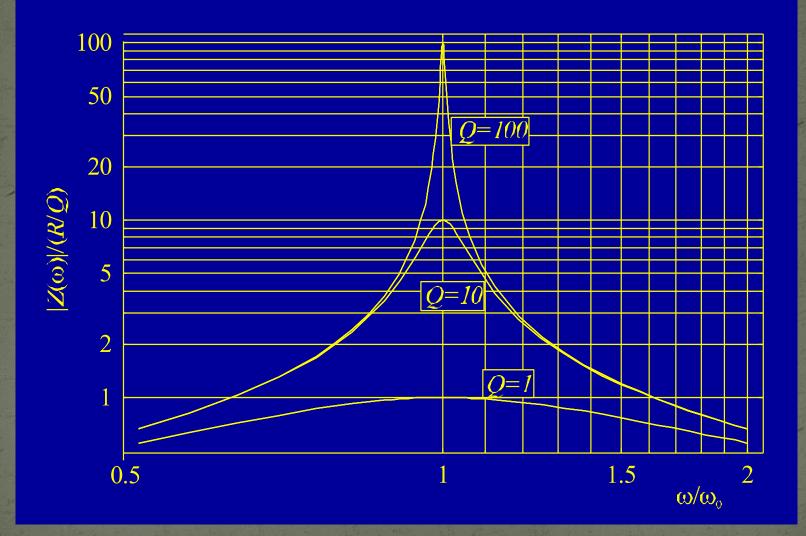
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Cavity resonator – equivalent circuit Simplification: single mode

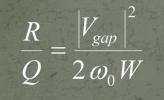


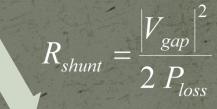
Resonance

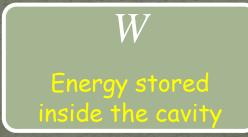


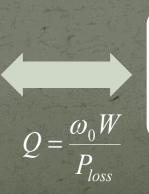
Summary: relations V_{gap}, W, P_{loss}











 P_{loss} Power lost in the cavity walls

Many gaps

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What do you gain with many gaps?

 The *R/Q* of a single gap cavity is limited to some 100 Ω. Now consider to distribute the available power to *n* identical cavities: each will receive *P/n*, thus produce an accelerating voltage of √2 *R P/n*. The total accelerating voltage thus increased, equivalent to

P/n

a total equivalent shunt impedance of nR.

P/n

P/n

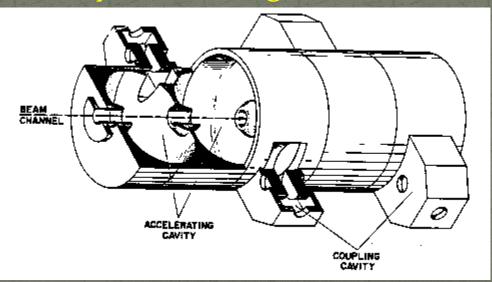
P/n

 $|V_{acc}| = n \left[2R \frac{P}{n} = \sqrt{2(nR)P} \right]$

Standing wave multicell cavity

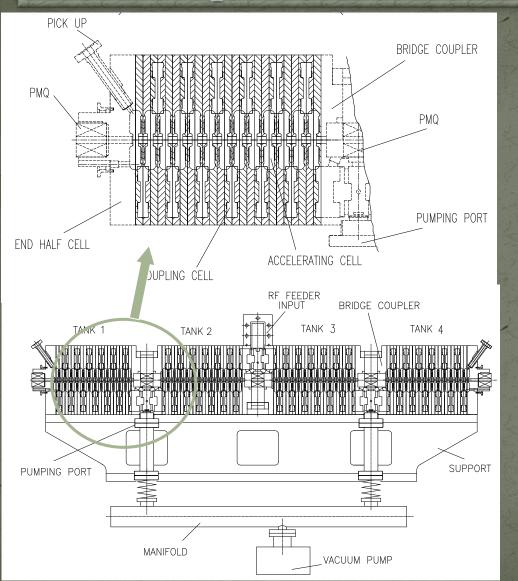
 Instead of distributing the power from the amplifier, one might as well couple the cavities, such that the power automatically distributes, or have a cavity with many gaps (e.g. drift tube linac).

Coupled cavity accelerating structure (side coupled)



The phase relation between gaps is important!

Side Coupled Structure : example LIBO



A 3 GHz Side Coupled Structure to accelerate protons out of cyclotrons from 62 MeV to 200 MeV

Medical application: treatment of tumours.

Prototype of Module 1 built at CERN (2000)

Collaboration CERN/INFN/ Tera Foundation

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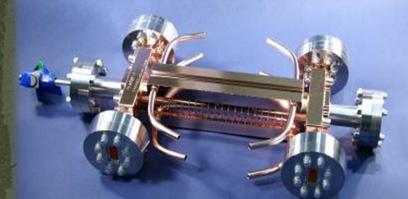
LIBO prototype



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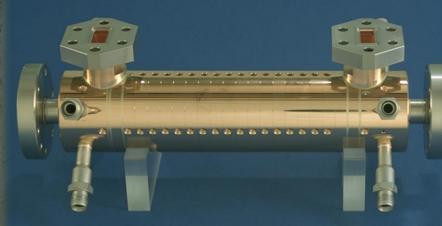
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CLIC travelling wave structures (12 & 30 GHz)



"T18" reached 105 MV/m!

"HDS" – novel fabrication technique



Superconducting Cavities

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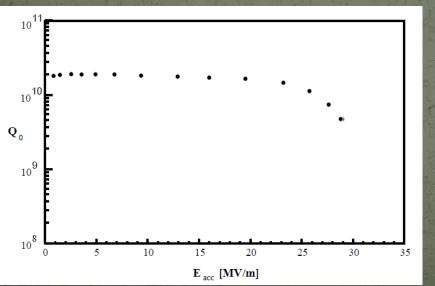
RF Superconductivity

- Best described by BCS (Bardeen-Cooper-Schrieffer) Theory
- $R_{BCS} \propto \frac{\omega^2}{T} \exp\left(-1.76 \frac{T_c}{T}\right)$
- Surface resistance $R = R_{BCS} + R_{res}$.
- *R* is not zero Q_0 is finite.

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• Good values are some 10¹⁰.

Typical performance plot of a SC cavity:



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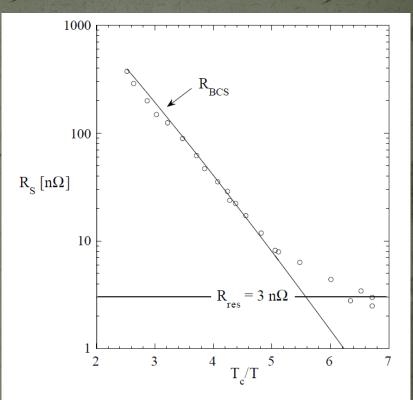


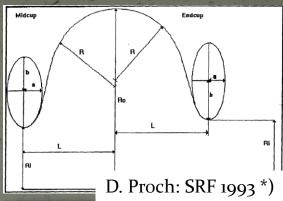
FIG. 1. The surface resistance of a 9-cell TESLA cavity plotted as a function of T_c/T . The residual resistance of 3 n Ω corresponds to a quality factor of $Q_0 = 10^{11}$.

From prst-ab.aps.org/abstract/PRSTAB/v3/i9/e092001

"Elliptical" multi-cell cavities

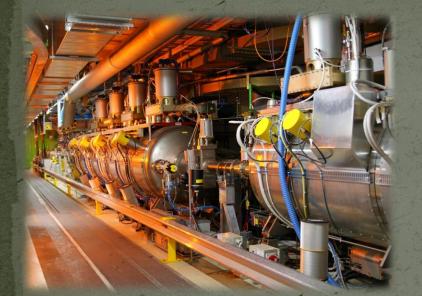
- The elliptical shape was found as optimum compromise between
 - maximum gradient (*E_{acc}/E_{surf}*)
 - suppression of multipactor
 - mode purity
 - machinability
- Operated in π -mode, i.e. cell length is exactly $\beta\lambda/2$.
- It has become de facto standard, used for ions and leptons! E.g.:
 - ILC/X-FEL: 1.3 GHz, 9-cell cavity
 - SNS (805 MHz)
 - SPL/ESS (704 MHz)
 - LHC (400 MHz^{*)})

*): accelconf.web.cern.ch/accelconf/SRF93/papers/srf93g01.pdf 7 November, 2013 CAS Chavannes 2013



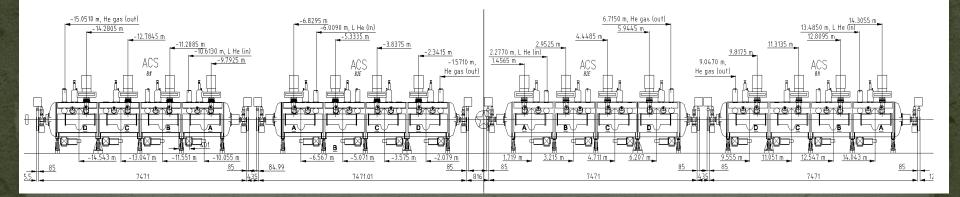


LHC SC RF, 4 cavity module, 400 MHz



installed in LHC IP4, 2 MV/cavity

LHC spare module stored in CERN's SM18

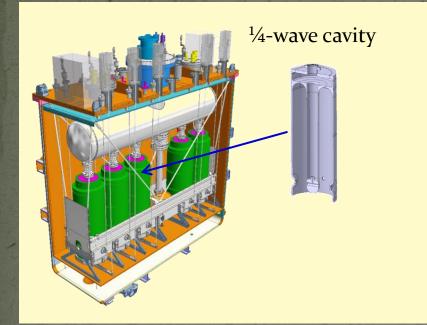


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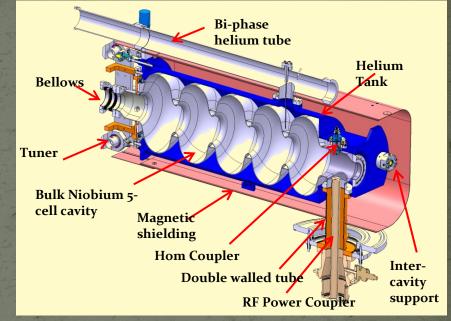
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SC Cavity Cryomodules (examples)

HIE-ISOLDE (radioactive isotopes postaccelerator), 101 MHz, 5-cavity CM



SPL/ESS 704 MHz CM (partial view)



ILC/X-FEL 1.3 GHz, 8 cavity CM



Some examples of RF Systems

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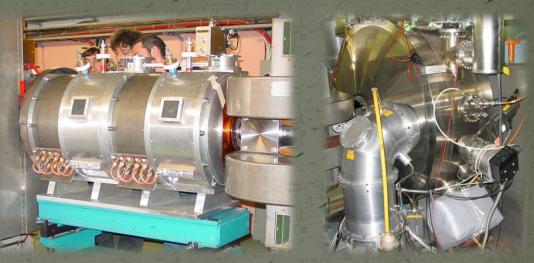
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CERN PS RF Systems



10 MHz system, *h*=7...21



13/20 MHz system, *h*=28/42

40 MHz system, *h*=84





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CERN SPS 200 MHz system

"Siemens" plant

EJ:

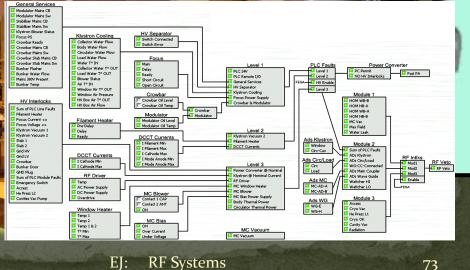
"Philips" plant

LHC RF System (ACS400)

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aver



Finemet RF System (MedAustron & PSB)

MedAustron

 $(0.2 \div 10)$ MHz, 1 kW solid state amplifier

Prototype system installed in ring 4

6-gap finemet cavity

dB CL Gain - Spice simulation Measured -5 -10 -15 -20 0.01 0.1 1 10 100

Large instantaneous bandwidth!-

CERN PSB

5-gap finemet cavity

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Thank you for your attention!

... Questions?

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