

# Neutrinos and Physics Beyond the Standard Model



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# Overview

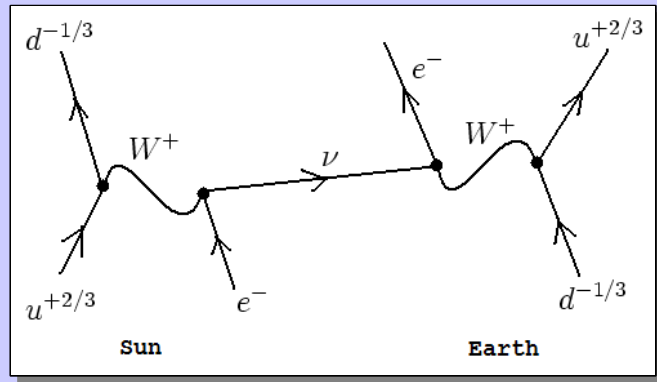
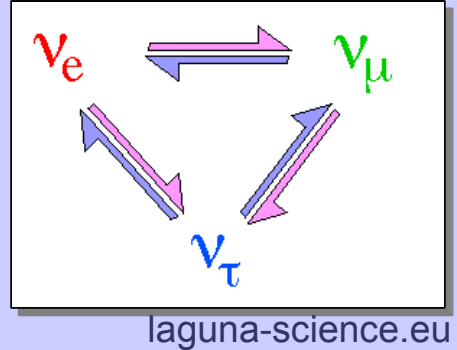
- **Neutrinos**
  - Oscillations
  - Absolute Mass
- **Neutrinoless Double Beta Decay**
- **Lepton Flavour Violation**
- **Neutrino Mass Generation**
  - Effective Operator and Seesaw Mechanism
  - SUSY Seesaw
  - Left-Right Symmetry
- **Conclusion**

# Neutrino Oscillations

- **Neutrino interaction states different from mass eigenstates**  
Neutrino flavour can change through propagation

$$\nu_i = \sum_{\alpha} U_{i\alpha} \nu_{\alpha}, \quad \nu_i(t) = e^{-i(E_i t - p_i x)} \nu_i$$

$$\Rightarrow P_{\alpha \rightarrow \beta} = \sin^2(2\theta) \sin^2\left(1.27 \frac{\Delta m^2}{\text{eV}^2} \frac{L/\text{km}}{E/\text{GeV}}\right)$$



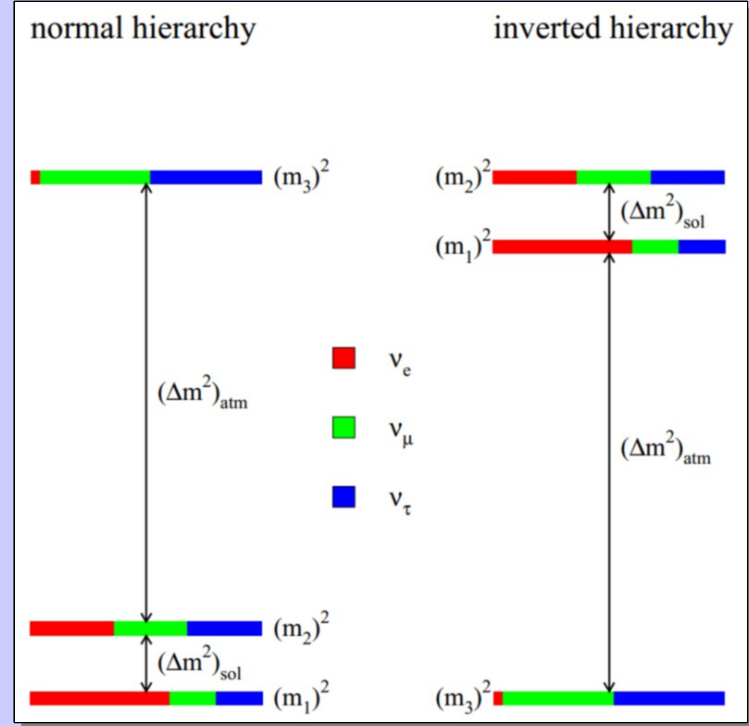
- **Solar neutrino oscillations**  
Large mixing
- **Atmospheric oscillations**  
 $\approx$  Maximal mixing
- **Reactor and accelerator neutrinos**  
Small, but significantly different from zero
- **Mixing Pattern very different from quarks**

$$\sin^2(2\theta_{13}) = 0.092 \pm 0.021$$

# Neutrino Oscillations

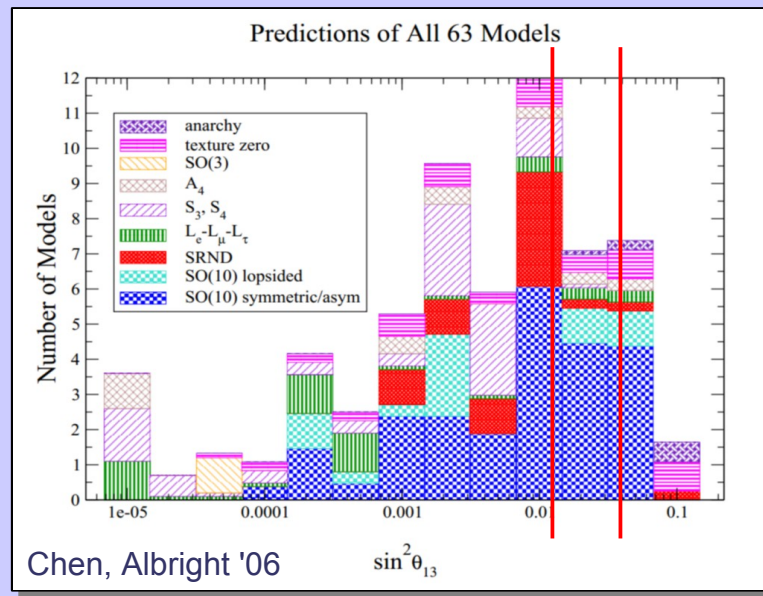
- Neutrino mixing matrix and mass differences

$$U \approx \begin{pmatrix} \sqrt{2/3} & \sqrt{1/3} & 0.15 e^{i\delta} \\ -\sqrt{1/6} & \sqrt{1/3} & -\sqrt{1/2} \\ -\sqrt{1/6} & \sqrt{1/3} & \sqrt{1/2} \end{pmatrix} \times \begin{pmatrix} e^{i\phi} & 0 & 0 \\ 0 & e^{i\theta} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



De Gouvea '04

- Constraining the model space



- Experimental unknowns and anomalies

CP violation? Sign of  $\Delta m_{23}$ ? Sterile Neutrinos?

# Absolute Neutrino Mass

- Energy endpoint in Beta decay

$$m_{\beta}^2 = \sum_i |U_{ei}|^2 m_i^2 < (2.2 \text{ eV})^2$$

Katrin:  $m_{\beta} \approx 0.2 \text{ eV}$

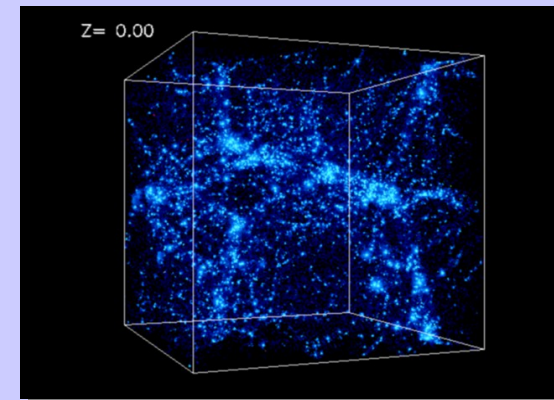
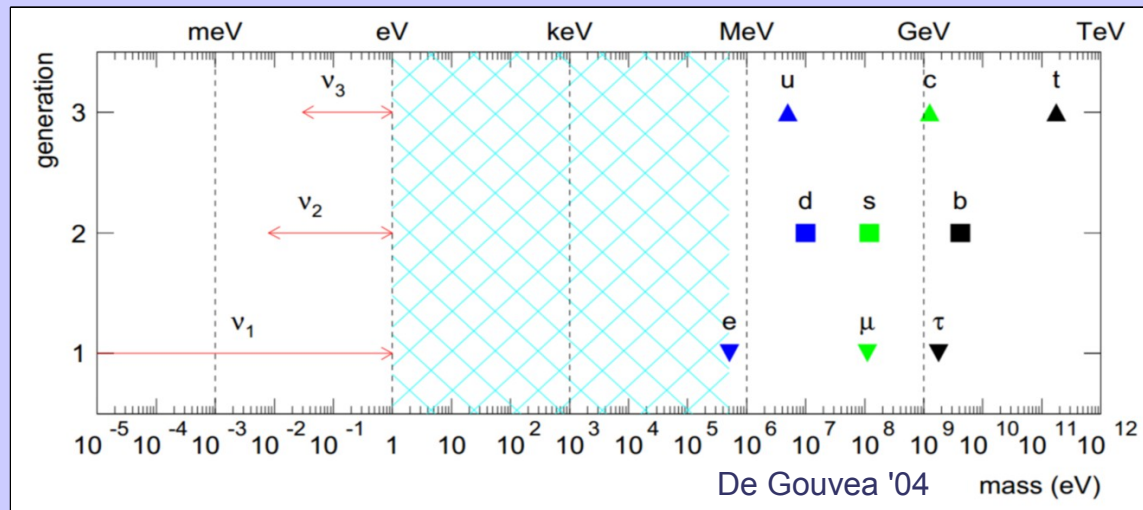
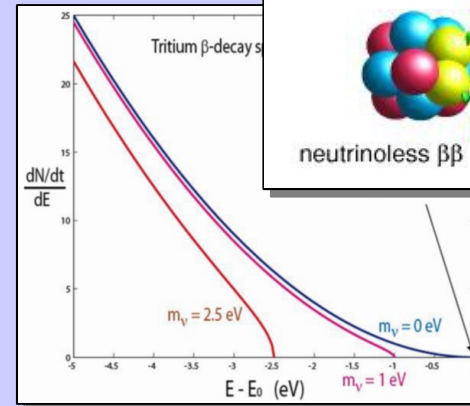
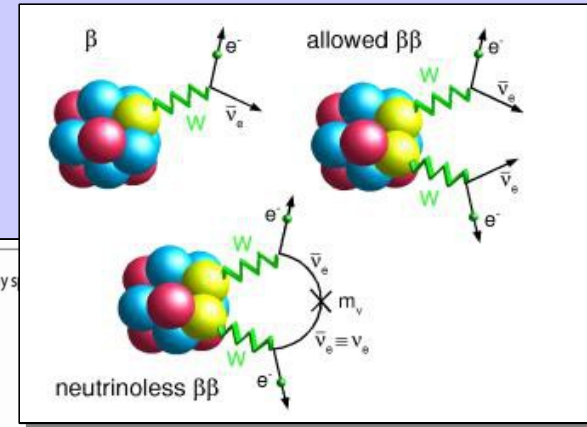
- Impact on Large Scale Structure

$$\Sigma = \sum_i m_i < 0.4 - 1 \text{ eV}$$

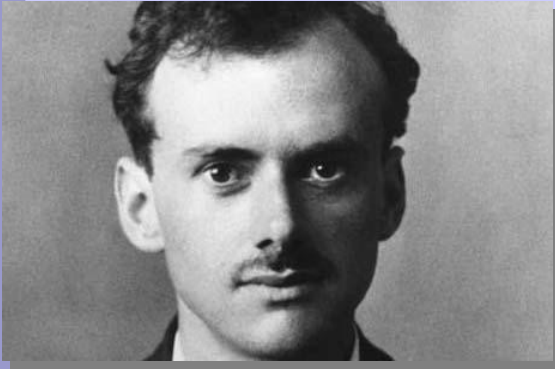
- Neutrinoless Double Beta Decay

$$m_{\beta\beta} = \left| \sum_i U_{ei}^2 m_{\nu_i} \right| < 0.2 - 2.0 \text{ eV}$$

Future:  $m_{\beta\beta} \approx 0.01 \text{ eV}$



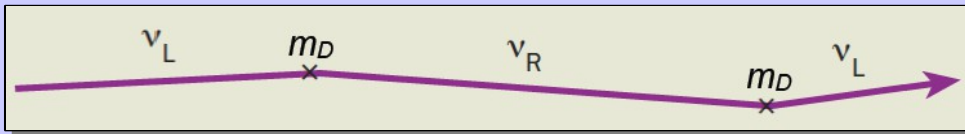
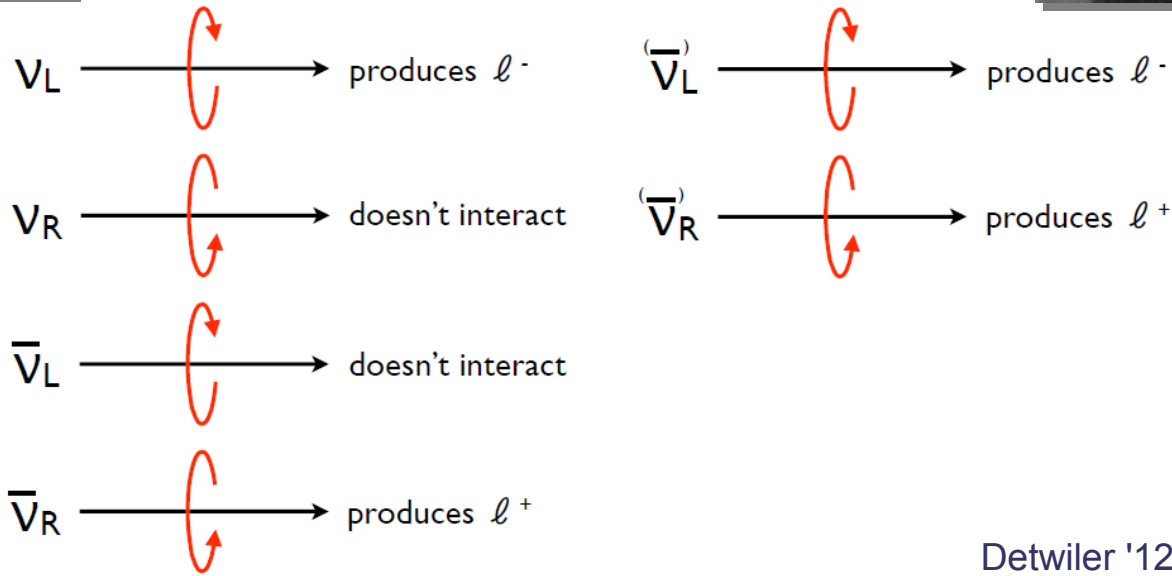
# Dirac vs Majorana



Two possibilities to define mass

Dirac  $\nu$

Majorana  $\nu$

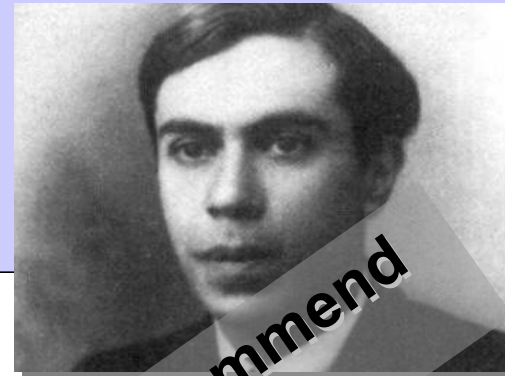
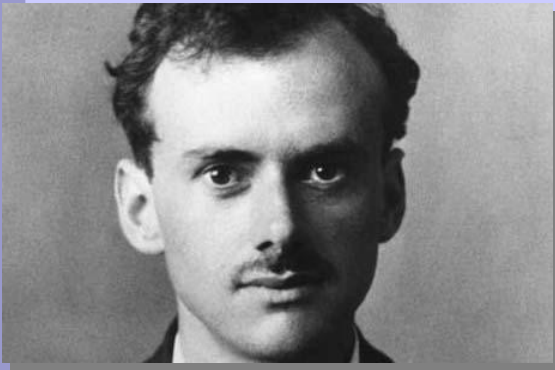


Dirac mass, analogous to other fermions (but with tiny coupling to Higgs)



Majorana mass, using only a left-handed neutrino → Lepton Number Violation

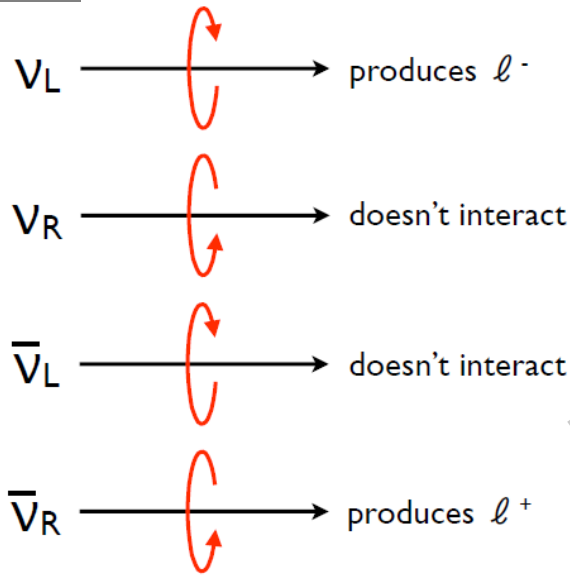
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Two possibilities to define mass

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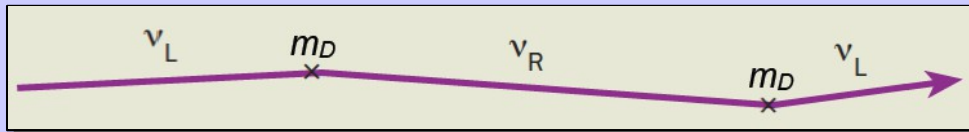
Majorana  $\nu$



9 out of 10 theorists recommend Majorana neutrinos



Detwiler



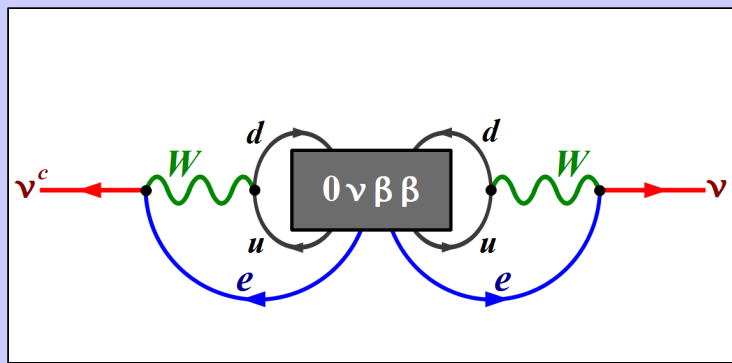
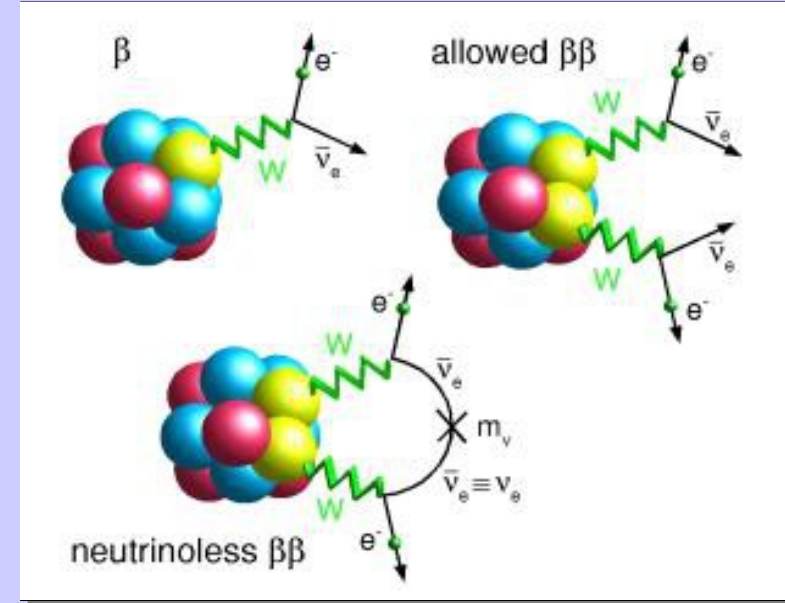
Dirac mass, analogous to other fermions (but with tiny coupling to Higgs)



Majorana mass, using only a left-handed neutrino → Lepton Number Violation

# Neutrinoless Double Beta Decay

- **Two neutrino double beta decay**  
Allowed in the SM, Observed
- **Neutrinoless double beta decay**  
 $(A, Z) \rightarrow (A, Z+2) + 2e^-$
- **Uncontroversial detection of  $0\nu\beta\beta$  of utmost importance**
  - Signal of New Physics
  - Prove lepton number to be broken
  - Prove neutrinos to be Majorana particles (Schechter, Valle '82)

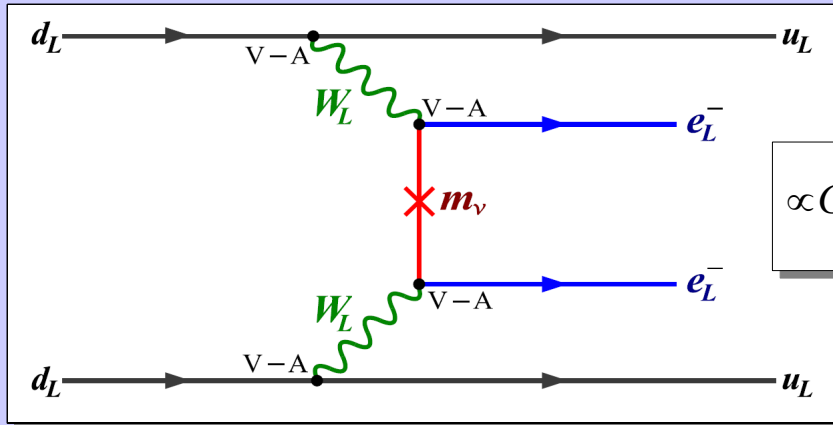


$$\delta m_\nu \approx \frac{1}{(16\pi^2)^4} \frac{\text{MeV}^5}{M_W^4} \approx 10^{-23} \text{ eV}$$



# Light Neutrino Exchange

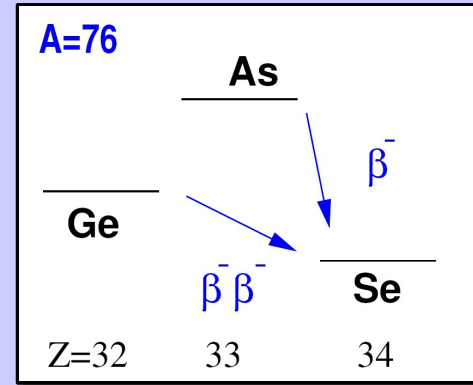
- Standard Mass Mechanism



## Heidelberg-Moscow

$T_{1/2}({}^{76}\text{Ge}) \approx 1.9 \cdot 10^{25} \text{ y}$   
 $\langle m_\nu \rangle \approx (0.3 - 0.6) \text{ eV}$

$$\propto G_F^2 \sum_i U_{ei}^2 \gamma_\mu P_L \frac{\cancel{A} + m_{\nu_i}}{q^2 - m_{\nu_i}^2} \gamma_\nu P_L$$



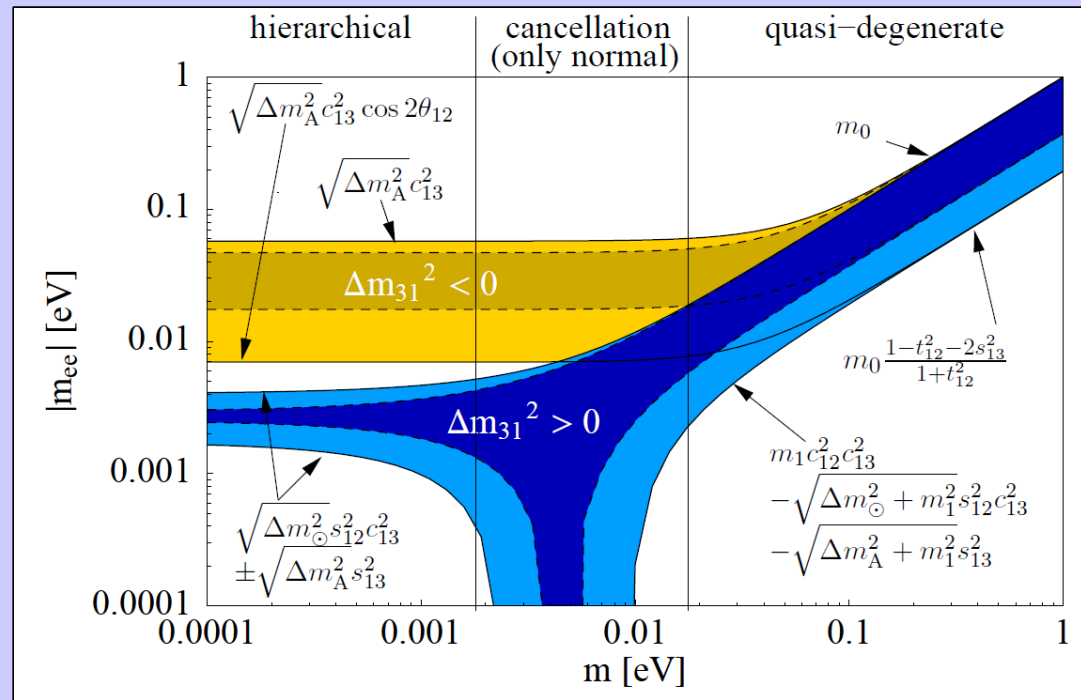
- Decay Rate

$$\Gamma = T_{1/2}^{-1} = \frac{m_{\beta\beta}^2}{m_e^2} G^{0\nu} |M^{0\nu}|^2$$

- Effective Mass

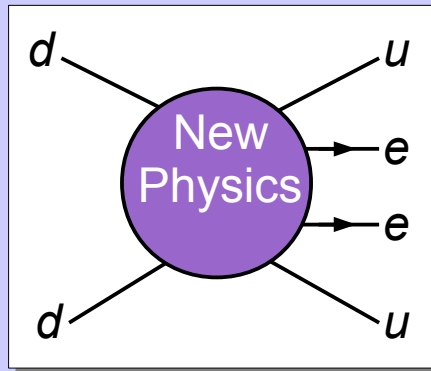
$$m_{\beta\beta} = \left| \sum_i U_{ei}^2 m_{\nu_i} \right| \equiv (m_\nu)_{ee}$$

Lindner, Merle, Rodejohann (2005)

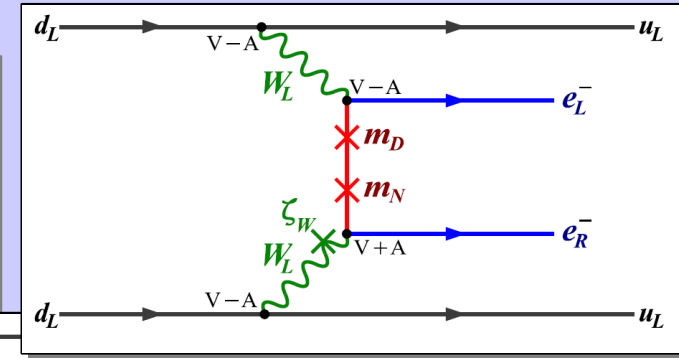
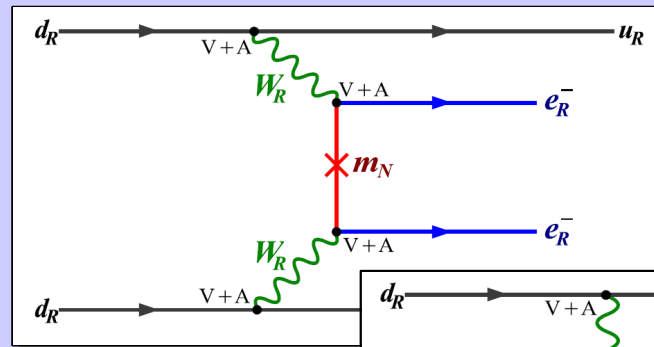


# New Physics Contributions to $0\nu\beta\beta$

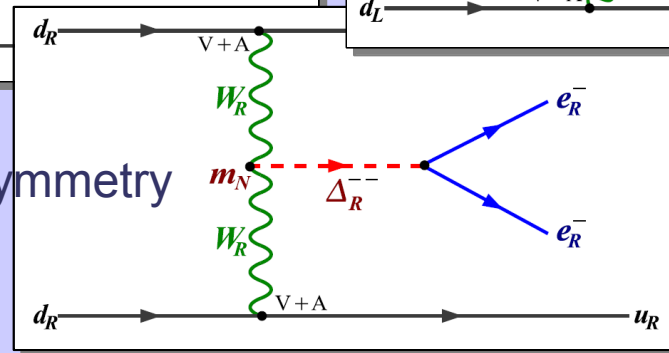
## • Plethora of New Physics Scenarios



$$T_{1/2}^{-1} \approx 10^{25} \text{ y} \rightarrow M \approx 1 \text{ TeV}$$



Left-Right Symmetry



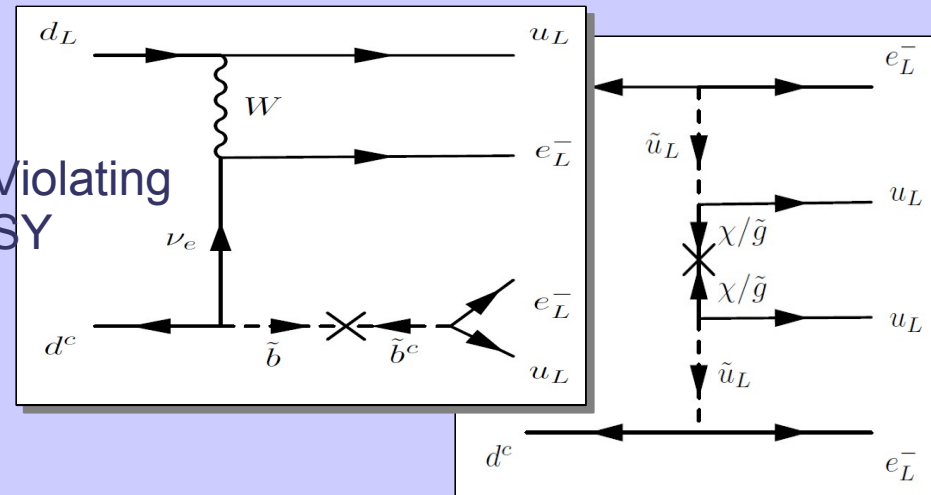
Extra Dimensions

Majorons

R-Parity Violating SUSY

Leptoquarks

...



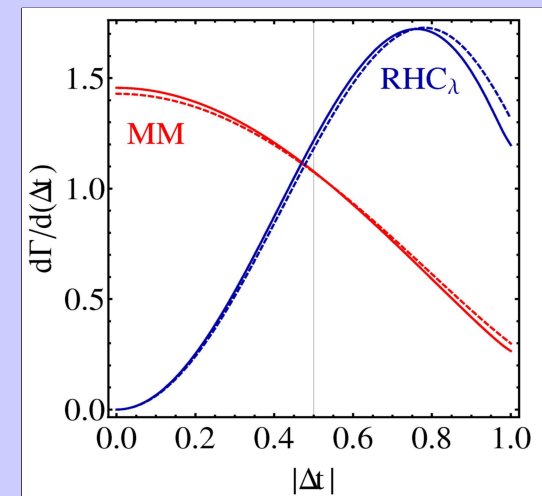
# Disentangling New Physics Scenarios

- **Angular and Energy distribution of emitted electrons**

(Doi et al. '83; Ali et al. '06; Arnold et al. '10; FFD, Jackson, Nasteva, Söldner-Rembold '10)

$$\frac{d\Gamma}{dE_1 dE_2 d\cos\theta} = \frac{\Gamma}{2} (1 - k(E_1, E_2) \cos\theta) \quad -1 < k < 1$$

- Linear in  $\cos\theta$
- $k(E_1, E_2)$  depends on  $0\nu\beta\beta$  mechanism



- **Comparison of  $0\nu\beta\beta$  in multiple isotopes**

(FFD, Päs PRL 2007)

$$\frac{T_{1/2}({}^A X)}{T_{1/2}({}^B Y)} = \frac{G({}^B Y) |M({}^B Y)|^2}{G({}^A X) |M({}^A X)|^2}$$

- Depends on  $0\nu\beta\beta$  mechanism
- Independent of details of new physics (if one mechanism dominates)

# Effective Mass and Seesaw Mechanism

- Effective operator for Majorana neutrino mass

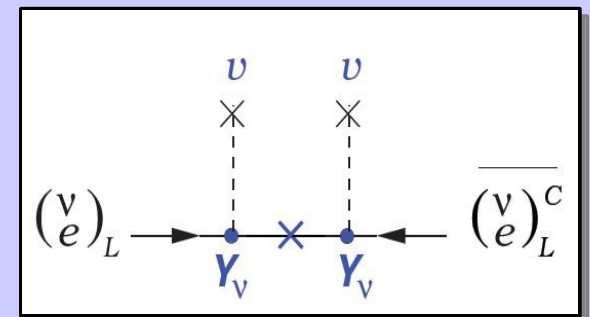
$$L = \frac{1}{2} \frac{h_{ij}}{\Lambda_{\text{LNV}}} (\bar{L}_i^c \cdot \tilde{H}) (\tilde{H}^T \cdot L_j) \rightarrow \frac{1}{2} (m_\nu)_{ij} \bar{\nu}_i^c \nu_j$$

Unique dim-5  
Operator

- Seesaw Mechanism

Add right-handed neutrinos to the Standard Model particle content,  $M \approx 10^{14}$  GeV

$$L = L_{\text{SM}} - \frac{1}{2} \bar{\nu}_R M \nu_R^c + \bar{\nu}_R Y_\nu L \cdot H_u$$



- Light neutrino mass matrix at low energies

$$m_\nu = m_D^T M^{-1} m_D \text{ for } m_D \ll M_R \quad m_\nu \approx 0.1 \text{ eV} \left( \frac{m_D}{100 \text{ GeV}} \right)^2 \left( \frac{M}{10^{14} \text{ GeV}} \right)^{-1}$$

# Effective Mass and Seesaw Mechanism

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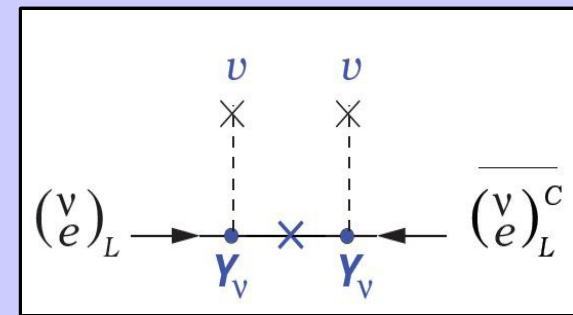
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Unique dim-5  
Operator

- Seesaw Mechanism

- Sterile Neutrino Mass Scale Unknown

- $\approx 10^{14}$  GeV: Naive Seesaw, GUTs
- $> 10^9$  GeV: Thermal Leptogenesis
- $\approx 10^2$  GeV: Resonant Leptogenesis, Production at LHC
- $\approx 1$  keV: Dark Matter Candidate
- $\approx 1$  eV: Oscillation, Cosmology, (Double) Beta Decay



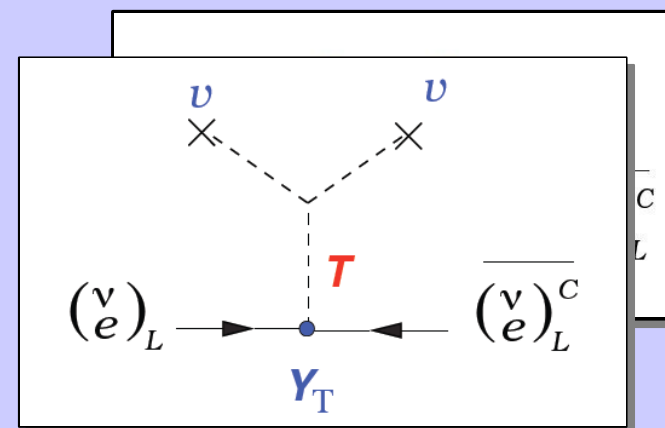
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Unique dim-5 Operator

- Seesaw Mechanism
- Three possible mediators at tree level



Seesaw II

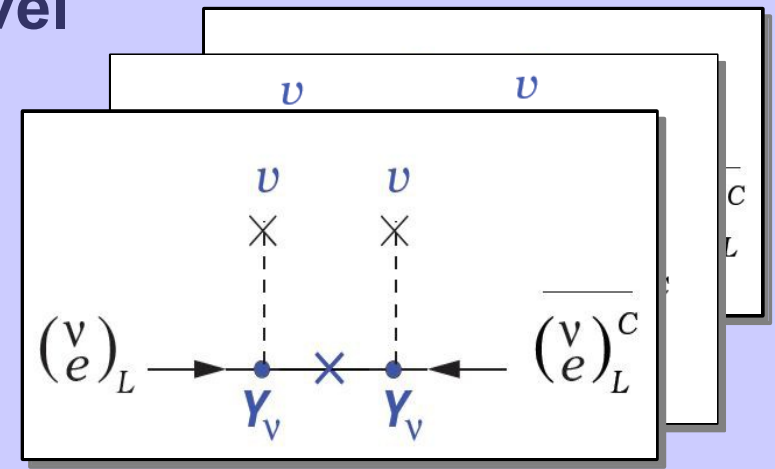
# Effective Mass and Seesaw Mechanism

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Seesaw III

# Effective Mass and Loops

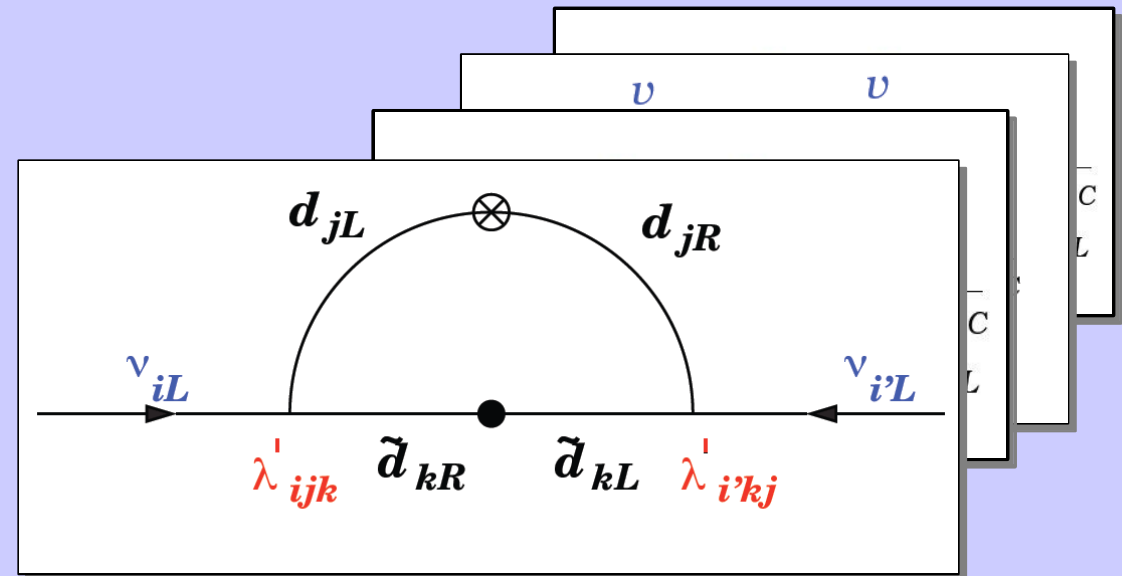
- Effective operator for Majorana neutrino mass

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Unique dim-5  
Operator

- Radiative Generation via Loops

Alternative to Seesaw Mechanism



R-Parity Violating SUSY



# Charged Lepton Flavour Violation

- **Lepton flavour practically conserved in the Standard Model**

$$Br(\mu \rightarrow e \gamma) = \frac{3\alpha}{32\pi} \left| \sum_i U_{\mu i}^* U_{ei} \frac{\Delta m_{1i}^2}{m_W^2} \right|^2 \approx 10^{-56}$$

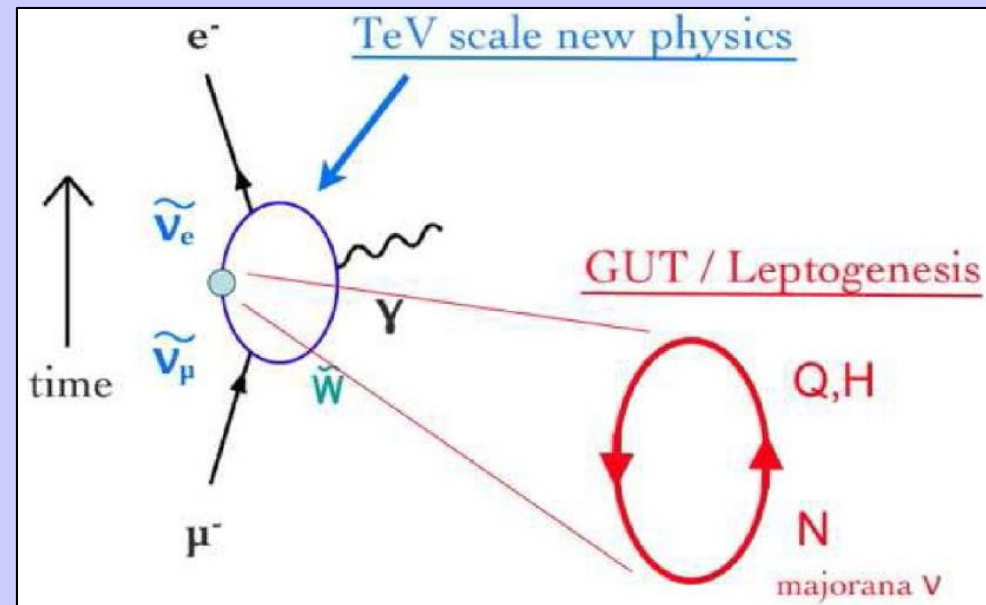
LFV is clear sign for BSM physics

- **Flavour violation in quark and neutrino sector**

Strong case to look for charged LFV

- **LFV can shed light on**

- Grand Unification models
- Flavour symmetries
- Origin of flavour
- Connection to neutrino mixing

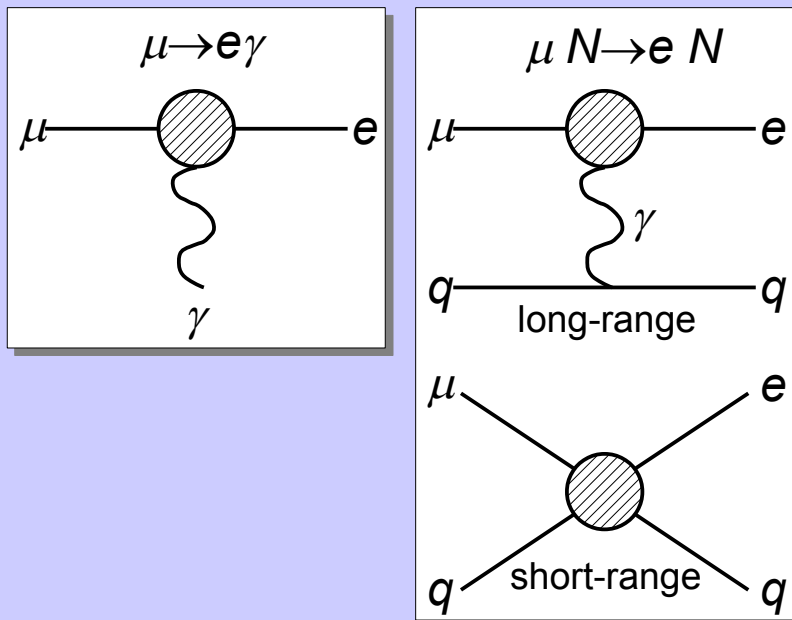


# Rare LFV Processes

- **Current bounds**

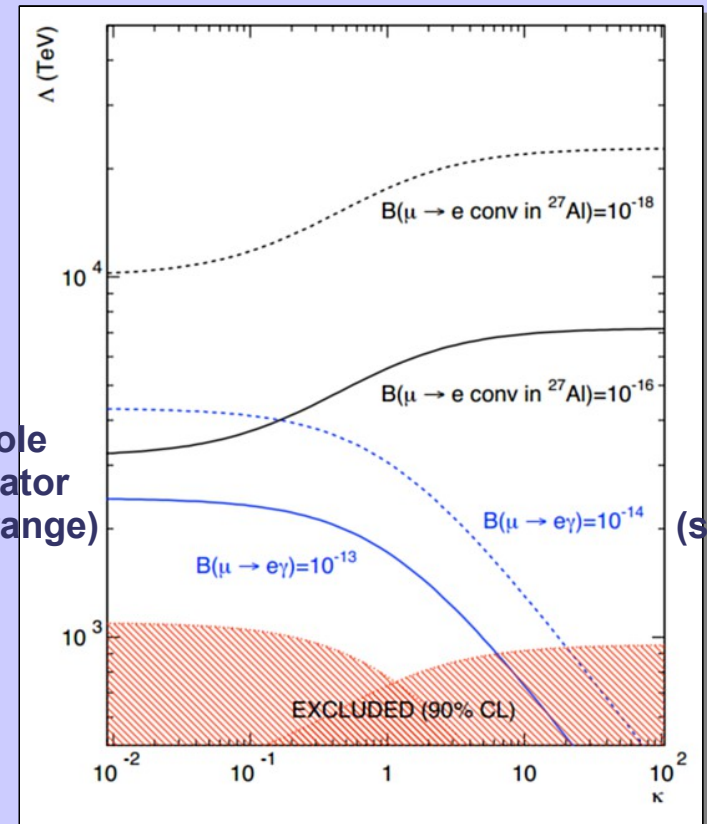
- $\text{Br}(\mu \rightarrow e \gamma) < 6.0 \cdot 10^{-13}$  (MEG)
- $\text{Br}(\tau \rightarrow \mu \gamma) < 6.8 \cdot 10^{-8}$  (Belle)
- $\text{Br}(\tau \rightarrow e \gamma) < 3.7 \cdot 10^{-7}$  (BaBar)
- $R(\mu N \rightarrow e N) < 7 \cdot 10^{-13}$  (Sindrum)
- $\mu \rightarrow 3e, \tau \rightarrow 3\mu$  (LHC), etc.

- **Effective Operators**



- **and future sensitivities**

- $10^{-13}$  (MEG, 2018)
- $10^{-8}$  (Super-B Factory, LHC?)
- $10^{-8}$  (Super-B Factory)
- $10^{-16}$  (COMET),  $\mu$ - $e$  conversion in nuclei

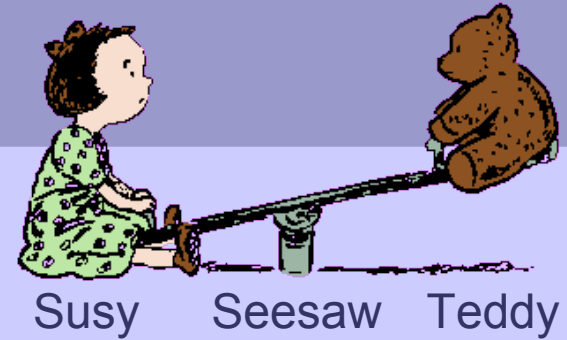


Contact Operator (short-range)

Dipole Operator (long-range)

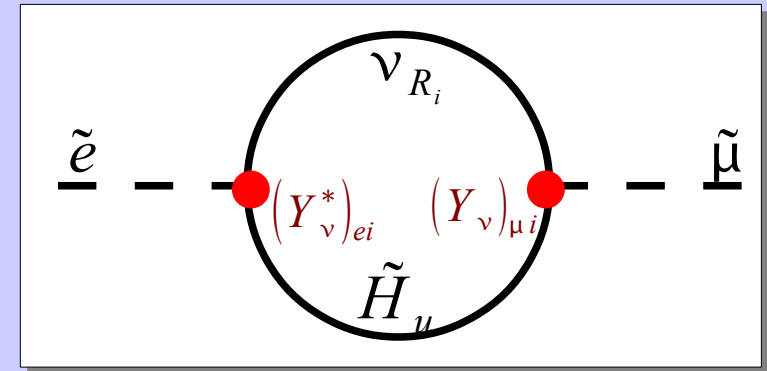
de Gouvea, Vogel, 2013

# SUSY Seesaw



## Achieve testability via impact on sleptons

- Neutrino flavour mixing radiatively induces slepton flavour mixing (Masiero, Borzumati)
- Correlation between slepton and neutrino flavour mixing



$$(\delta m_{\tilde{L}}^2)_{ij} = \begin{pmatrix} \delta_{11} & \delta_{12} & \delta_{13} \\ \delta_{12}^* & \delta_{22} & \delta_{23} \\ \delta_{13}^* & \delta_{23}^* & \delta_{33} \end{pmatrix} \propto Y_{\nu}^+ \cdot Y_{\nu} \log(M_{\text{GUT}}/M_R)$$

$\Im(\delta_{ij}) \Rightarrow$  EDMs  $d_e, d_{\mu}$

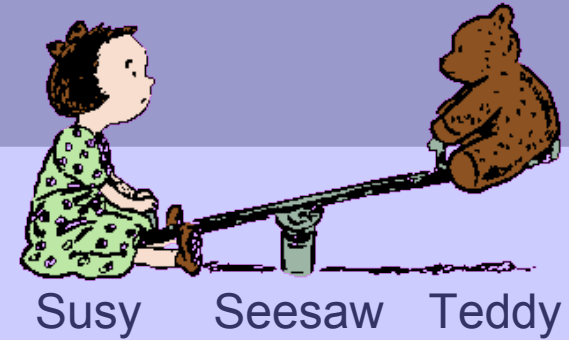
Slepton mass differences (Colliders)

$|\delta_{12}| \Rightarrow Br(\mu \rightarrow e \gamma), \text{ etc.}$

$\Rightarrow$  9 potential observables

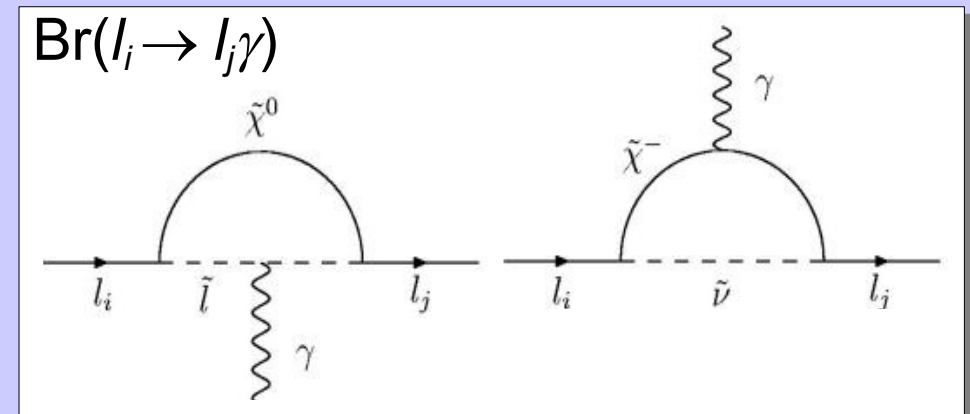
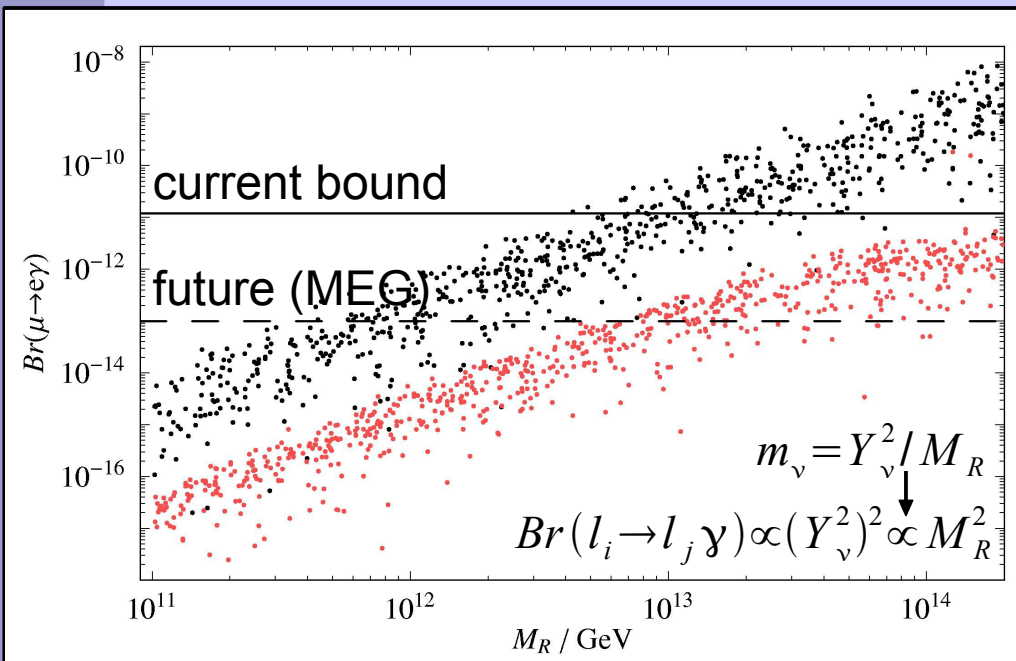
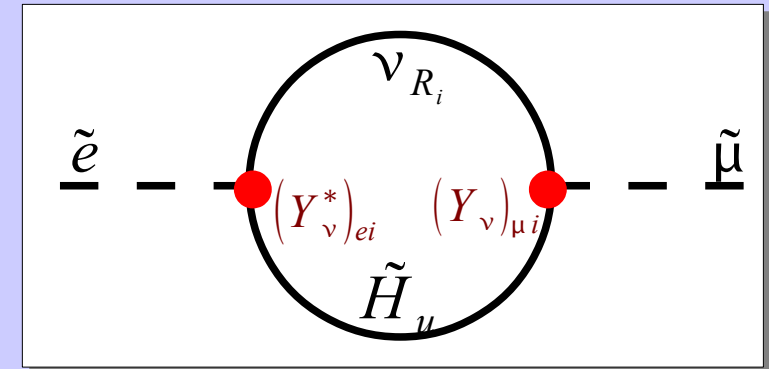
$\Rightarrow$  SUSY Seesaw testable (in principle)

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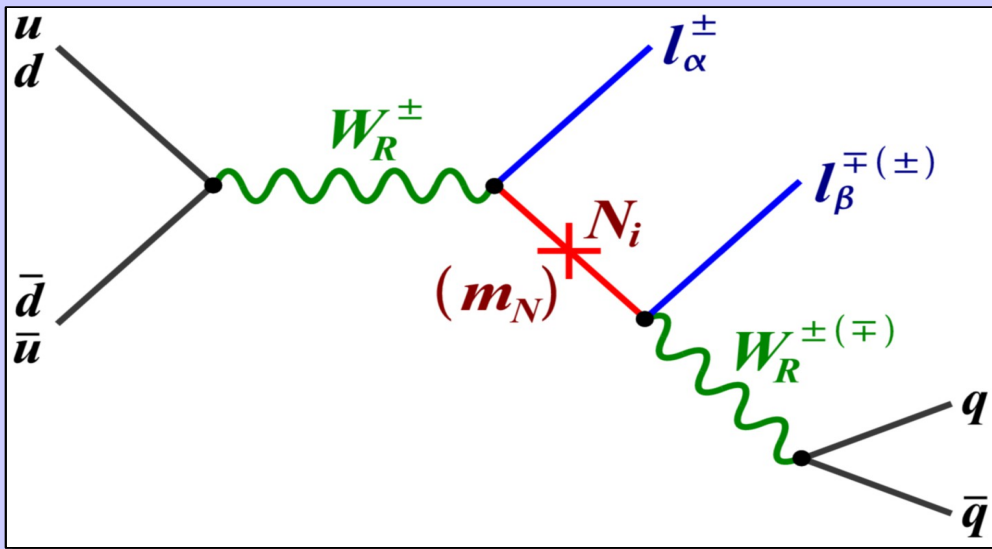
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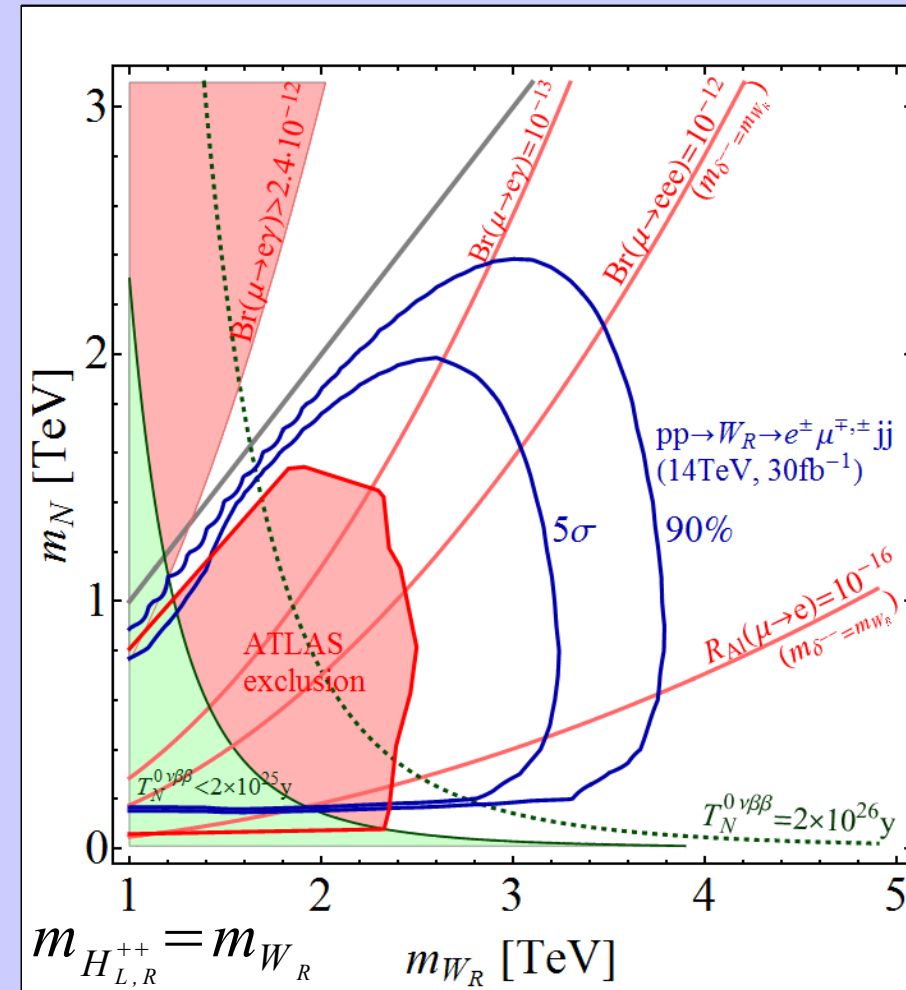
# Light Right-Handed Neutrinos



- Inverse Seesaw mechanism
- “Anti”-Seesaw mechanism
- Left-Right symmetric models  
Right-handed neutrinos couple with gauge strength to charged leptons



Probing right-handed neutrino mixing,  
Large LFV and LNV rates at LHC



Aguila, Aguilar-Saavedra, Das, FFD,  
Kittel, Valle '12

# Conclusion

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Strong experimental program to probe absolute mass

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Lepton Number Violation with  $0\nu\beta\beta$  as crucial probe

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- **Rich phenomenology in models of neutrino mass generation**
  - Charged lepton flavour violation
  - LFV and LNV processes at the LHC
  - Baryogenesis via Leptogenesis