

Optimisation of single bunch linac for FERMI upgrade

Alexej Grudiev, CERN

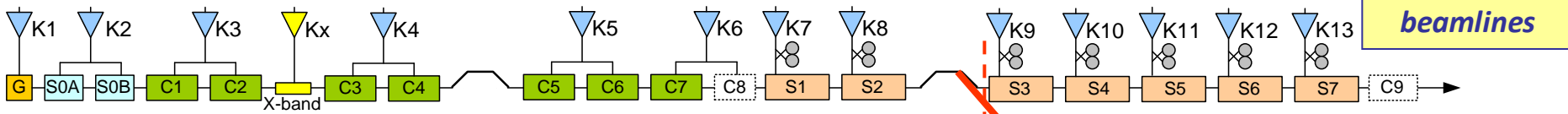
5/06/2013

HG2013, ICTP Trieste, Italy

Motivation from Gerardo D'Auria

Present machine layout

- E_{beam} up to 1.5 GeV
- FEL-1 at 80-20 nm and FEL-2 at 20-4 nm
- Seeded schemes
- Long e-beam pulse (up to 700 fs), with "fresh bunch technique"



FEL-1 & FEL-2 beamlines

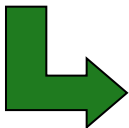
Beam input energy ≥ 750 MeV

New FEL beamline $\lambda < 1$ nm

Energy upgrade

- Space available for acceleration 40 m
- Accelerating gradient @12 GHz 60 MV/m
- X-band linac energy gain 2.4 GeV
- Injection energy .75 GeV
- Linac output energy 3.15 GeV

~50 m available
40 m (80%) available for acceleration



For short bunch (< 100 fs) and low charge (< 100pC) operation

Aperture scaling and BBU

Growth rate of the BBU due to wakefield kick from head to tail:

$$\gamma = \int_0^{L_t} \frac{Ne^2 W'_\perp(s)}{4k_\beta E(z)} dz \Big|_{s=0}^* ; \quad k_\beta \sim \frac{1}{\langle \beta \rangle}$$

$$W'_\perp(s) = \frac{4Z_0 c}{\pi a^4} s_1 \left(1 - \left[1 + \sqrt{\frac{s}{s_1}} \right] e^{-\sqrt{\frac{s}{s_1}}} \right)^{**}$$

$$\frac{dW'_\perp(s)}{ds} = \frac{4Z_0 c}{\pi a^4} e^{-\sqrt{\frac{s}{s_1}}}$$

$$W'_\perp(\sigma_z) = \frac{dW'_\perp(s)}{ds} \Big|_{s=0} \sigma_z = \frac{4Z_0 c}{\pi a^4} \sigma_z$$

$$E(z) = E_0 + eGz;$$

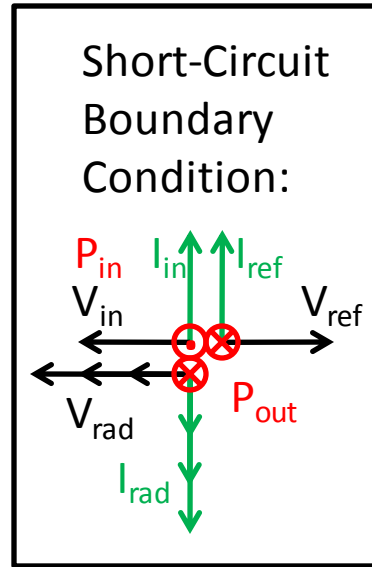
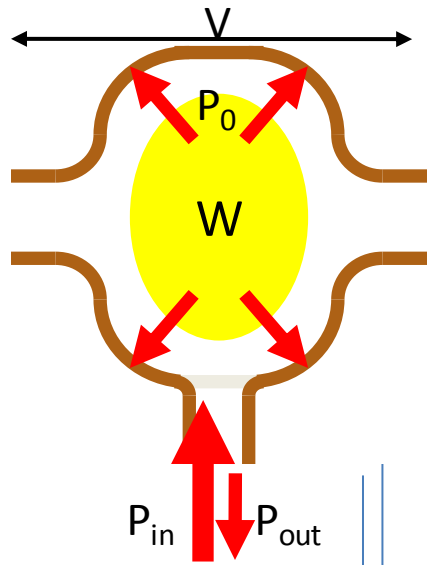
$$\gamma = \frac{Z_0 c}{\pi} \frac{eN\sigma_z}{\langle \beta \rangle a^4 G} \ln \left(\frac{E_L}{E_0} \right)$$

	Present	Upgrade	Scaling factor γ'/γ
L_t [m]	40	40	
$\langle \beta \rangle$ [m]	~ 10	~ 10	
E_0 [GeV]	0.75	0.75	
E_L [GeV]	1.5	3.15	1/2
σ_z [fs]	700	100	1/7
eN [pC]	500	100	1/5
			↓
a [mm]	5	$5 * 0.35 = \mathbf{1.75} \leftarrow$	$1/(2 * 7 * 5)$
γ	0.02	0.02	Keep const

* Alex Chao, "Physics of collective beam instabilities in high energy accelerators", 1993

** Karl Bane, "Short-range Dipole Wakefields in Accelerating structures for the NLC", SLAC-PUB-9663, 2003

Transient in a cavity -> pulse compression



$$P_{out} = P_{in}(t=0) \left(\frac{V_{out}}{V_{in}} \right)^2$$

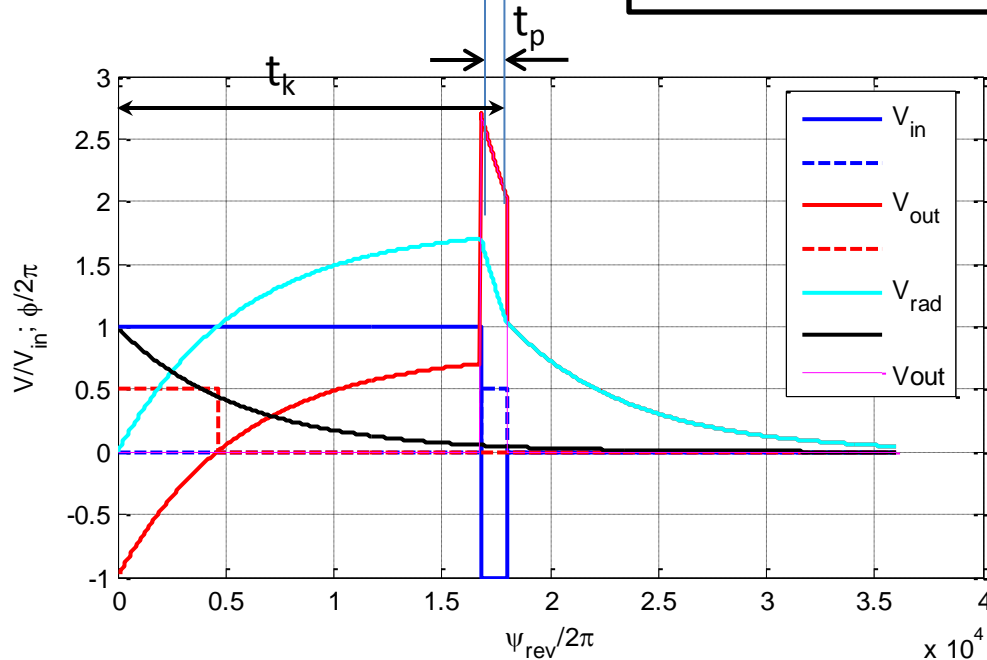
$$V_{out} = V_{rad} + V_{ref} = V_{rad} - V_{in}$$

$$V_{rad} = (V_{in} * C_{resp})$$

$$V_{in} = V_{in}(t=0) \exp(\omega t)$$

$$C_{resp} = \frac{1}{Q_e} \exp\left(-\frac{\omega_0 t}{2Q_l}\right)$$

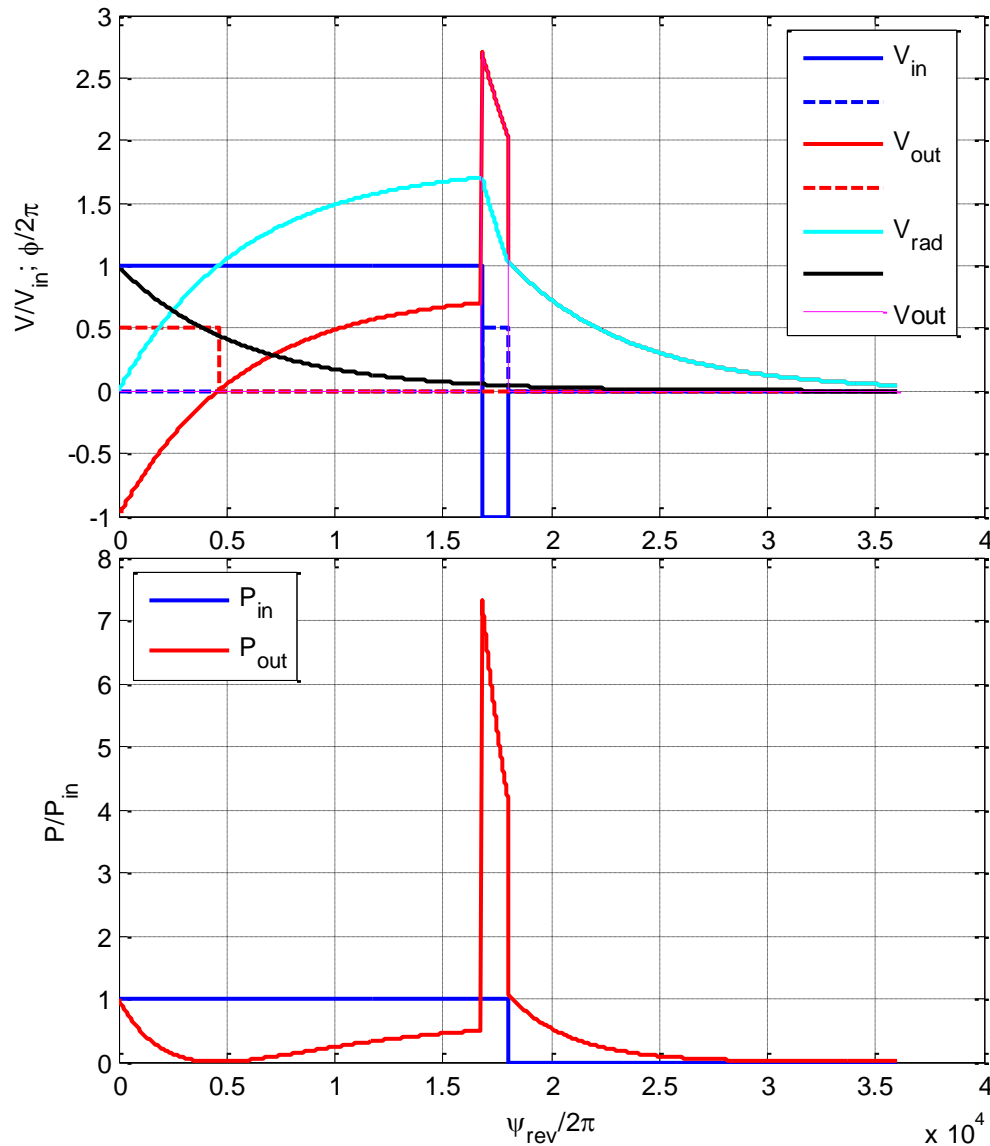
$$Q_l = \frac{Q_0 Q_e}{Q_0 + Q_e}$$



Analytical expression for the pulse shape

$$\left. \frac{V_{out}}{V_{in}}(t) \right|_{t_0=t_k-t_p}^{t_k} = f(\omega = \omega_0; t_k; t_p; Q_0; Q_e)$$

Pulse compression: example



Example at 12 GHz:

$$Q_0 = 180000; Q_e = 20000$$

$t_k = 1500$ ns klystron pulse length

$t_p = 100$ ns compressed pulse length

Average power gain =
 = average power in compressed pulse
 / input power = 5.6

Average power efficiency =
 = compressed pulse energy
 / input pulse energy = 34.7 %

Effective shunt impedance of Acc. Structure + Pulse Compressor

Time - dependent gradient*: $G(z, t') = G_0[t' - \tau(z)]g(z)$;

$$\tau(z) = \int_0^z \frac{dz'}{v_g(z')}; \quad t_f = \tau(L_s); \quad t' = t - t_0$$

$$G_0(t') = \sqrt{\frac{\omega}{v_{g0}} \frac{R}{Q} P_{out}(t')} = \sqrt{\frac{\omega}{v_{g0}} \frac{R}{Q} P_{in}} \frac{V_{out}}{V_{in}}(t')$$

$$V_a = \int_0^{L_s} dz' G(z', t' = t_f = t_p); \quad \tau_s = \alpha L_s = \frac{\omega}{2v_g Q} L_s$$

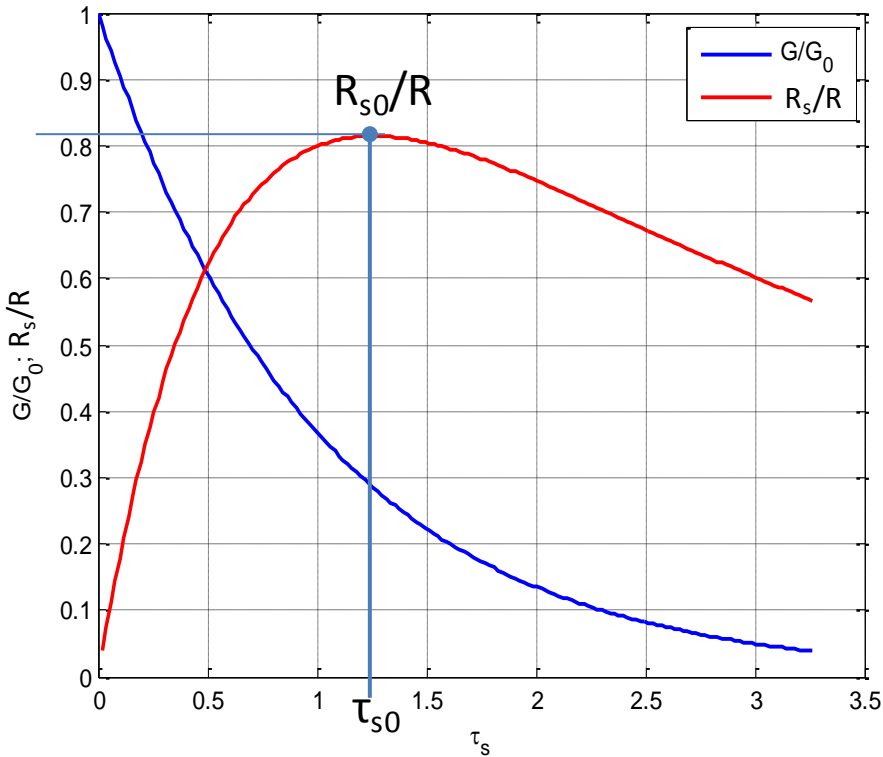
Effective shunt impedance**: $R_s = \frac{V_a^2}{P_{in} L_s} [\Omega / m]; \quad P_{tot} = \frac{V_{tot} \langle G \rangle}{R_s}$

* i.e. A. Lunin, V. Yakovlev, A. Grudiev, PRST-AB 14, 052001, (2011)

** R. B. Neal, Journal of Applied Physics, V.29, pp. 1019-1024, (1958)

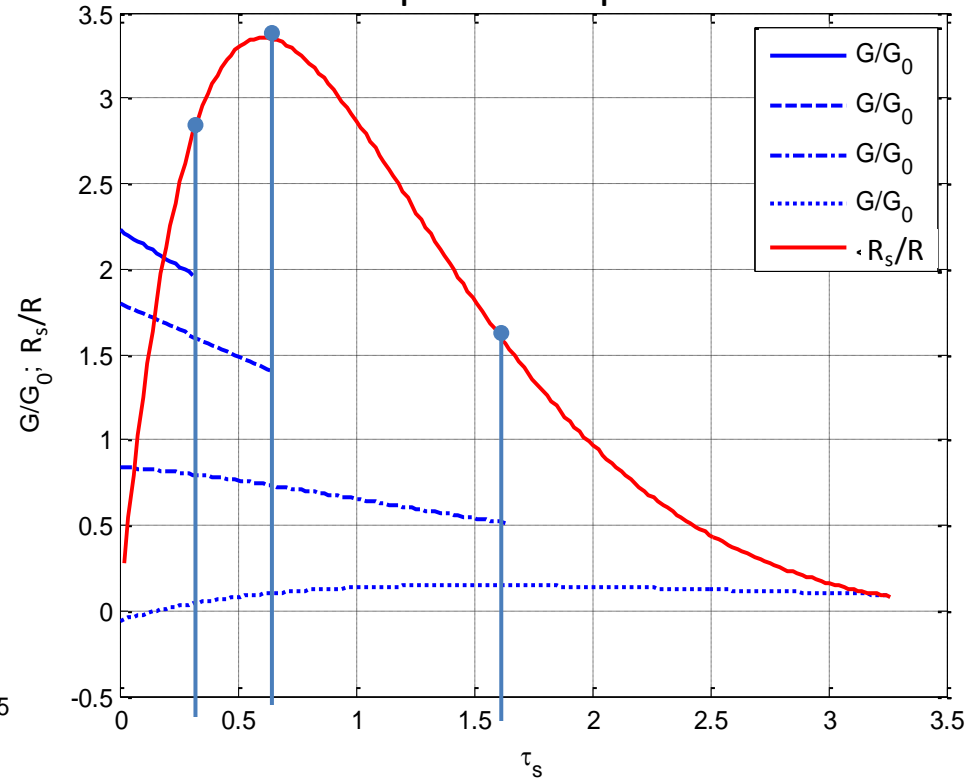
Effective Shunt impedance in Const Impedance (CI) AS

No pulse compression



$$\tau_{s0} = 1.2564 \Rightarrow R_{s0}/R = 0.8145$$

With pulse compression



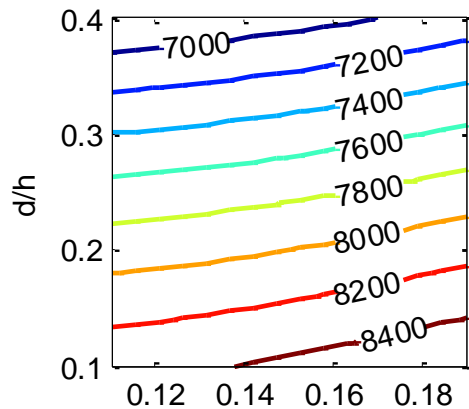
For $Q = 8128; Q_0 = 180000; Q_e = 20000$

$$\tau_{s0} = 0.6078 \Rightarrow R_{s0}/R = 3.3538$$

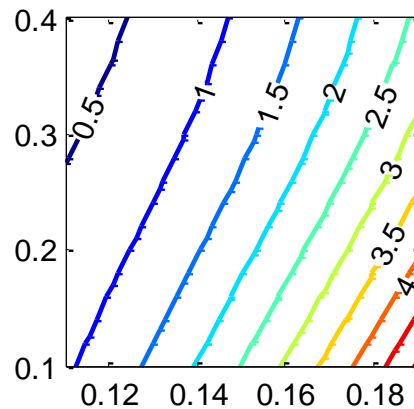
But in general it is function all 3 Qs: Q, Q_0, Q_e

Undamped cell parameters for $d\phi=150^\circ$

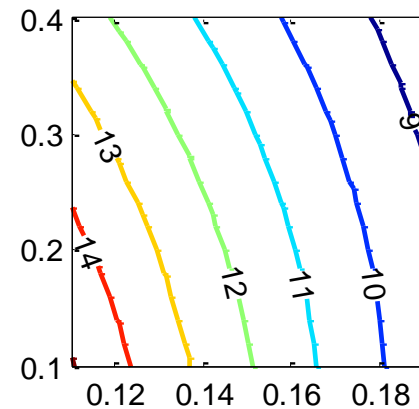
$d\phi = 150 \text{ deg}$ Q_0



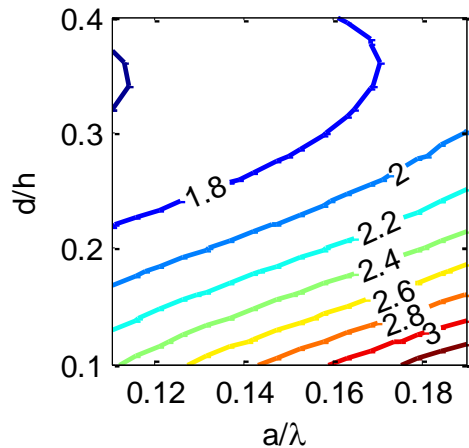
v_g/c [%]



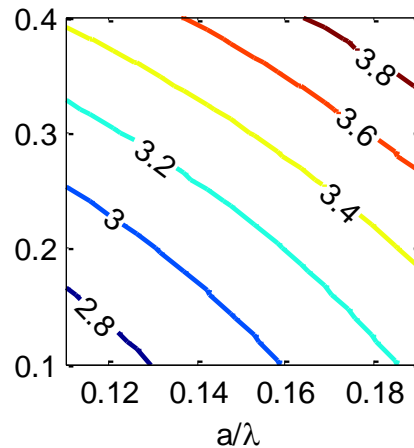
R/Q [$k\Omega/m$]



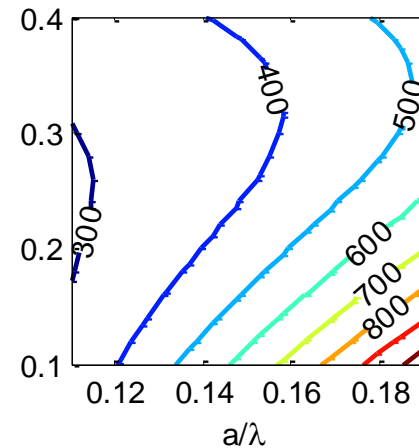
E_s^{\max}/E_a



H_s^{\max}/E_a [mA/V]



S_c^{\max}/E_a^2 [$\mu A/V$]

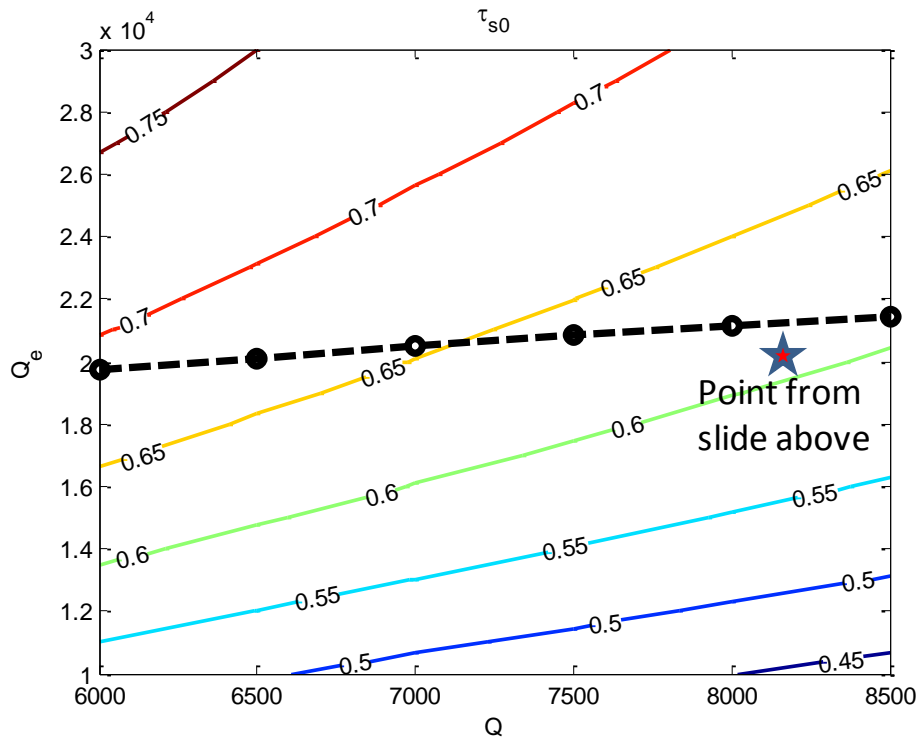


CIAS pulse compression optimum

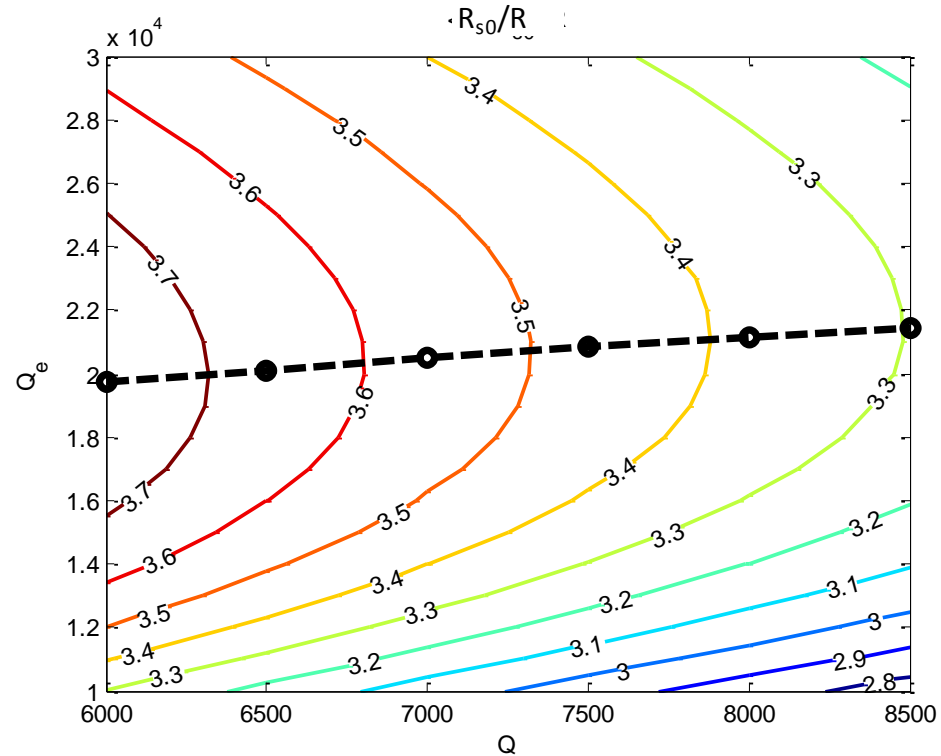
$Q_0 = 180000$ – Q-factor of the pulse compressor cavity(s)

$t_k = 1500$ ns – klystron pulse length

Optimum attenuation: τ_{s0}



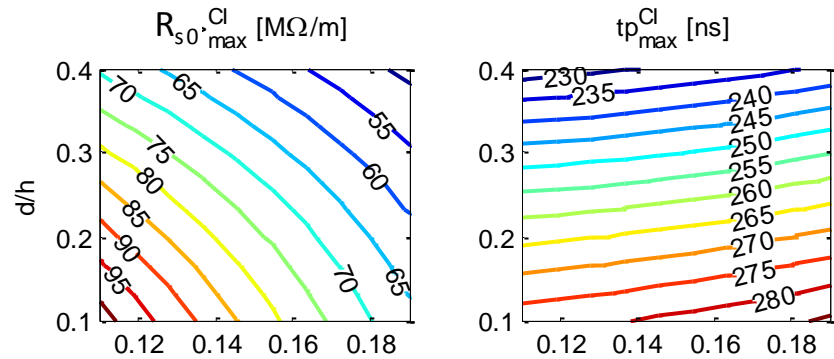
Averaged Shunt Impedance R_{s0}/R



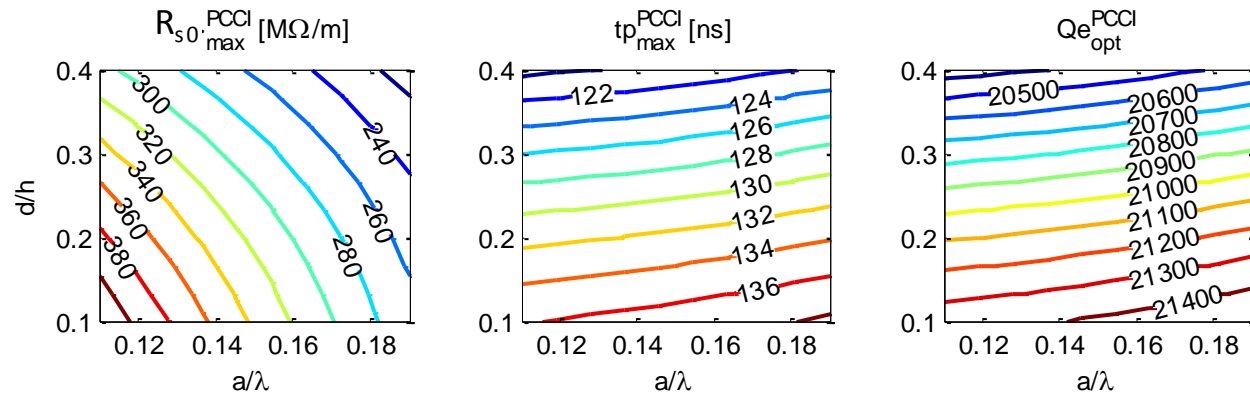
Optimum value of $Q_e \sim \text{const}$: ranges from 20000 for $Q=6000$ up to 21000 for $Q=8000$

CIAS Effective Shunt Impedance: w/o and with pulse compression

No pulse
compression



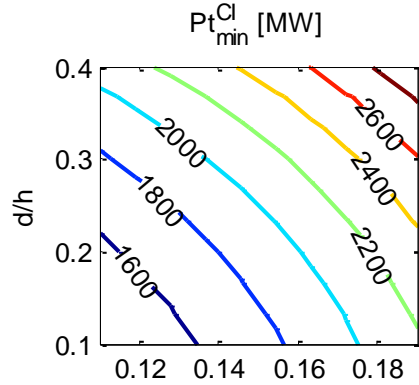
With pulse
compression



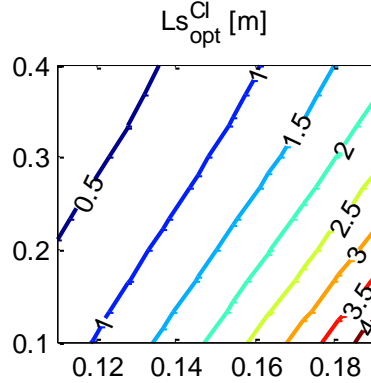
- As expected ~ 4 times higher effective shunt impedance with pulse compression
- Optimum pulse length is \sim two times longer no pulse compression is used, still it is much shorter than the klystron total pulse length

CIAS linac 40 m long, $\langle G \rangle = 60 \text{ MV/m}$: w/o and with PC

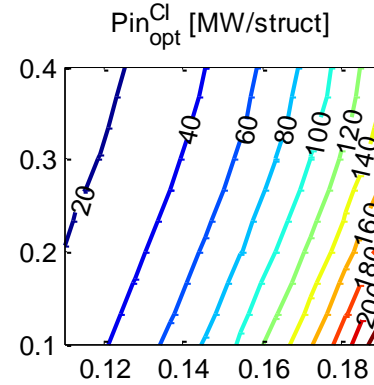
Total klystron power



Optimum structure length



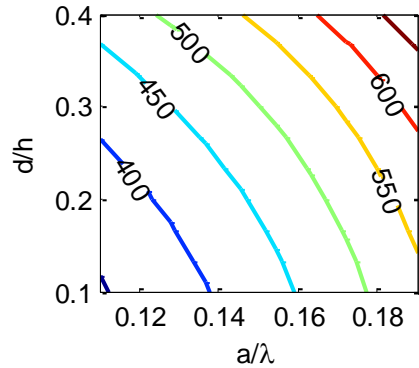
Klystron power per structure



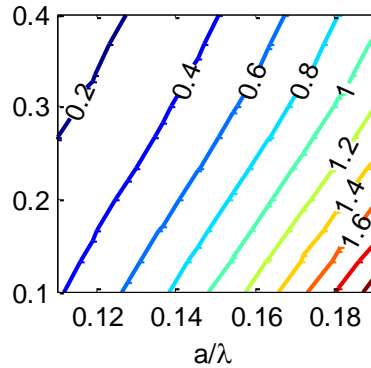
~# of structures per 0.8x50 MW klystron

2 -> 1/5

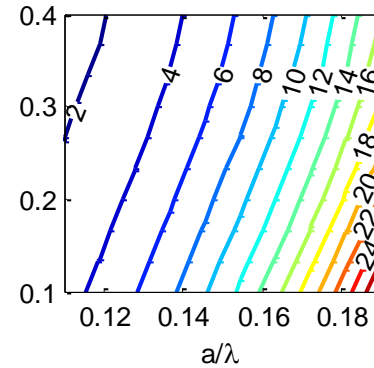
$P_{t_{\min}}^{\text{PCCI}}$ [MW]



$L_{s_{\text{opt}}}^{\text{PCCI}}$ [m]

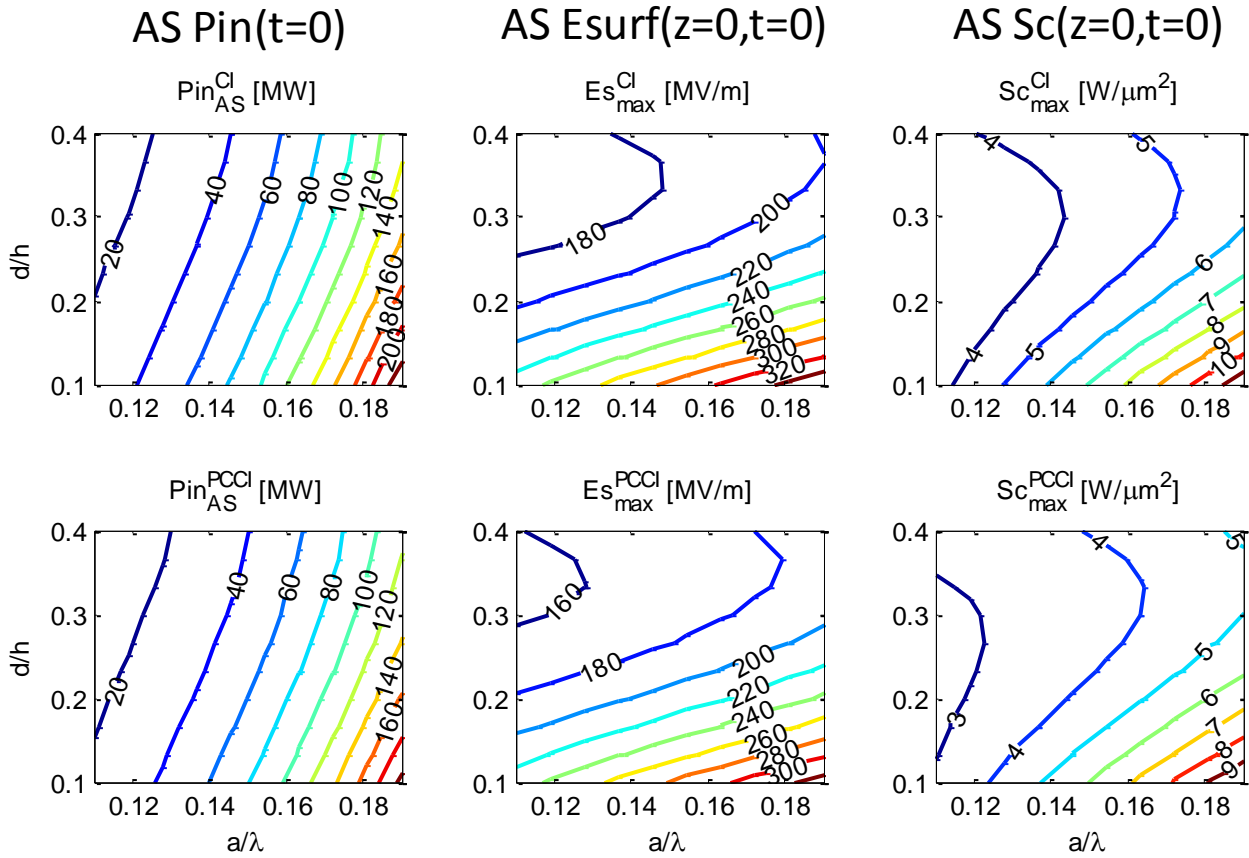


$P_{in_{\text{opt}}}^{\text{PCCI}}$ [MW/struct]



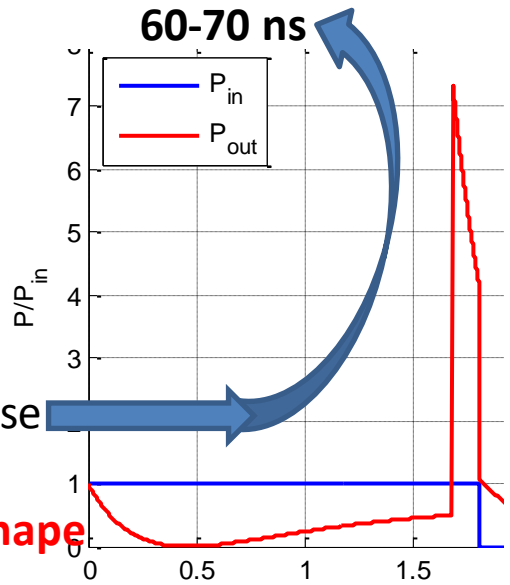
~20 -> ~2

CIAS high gradient related parameters: w/o and with PC



Typical Pulse length
Flat pulse: 230-290 ns
Above the HG limits
for larger apertures

Peaked pulse:
122-136 ns
60-70 ns



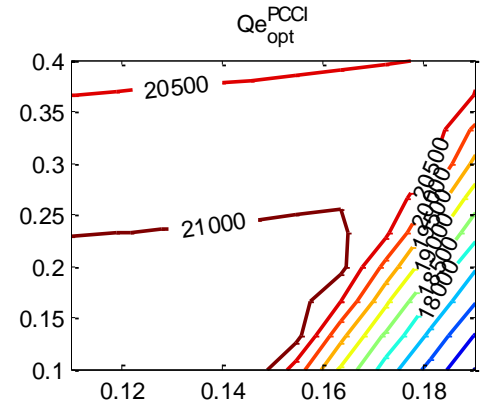
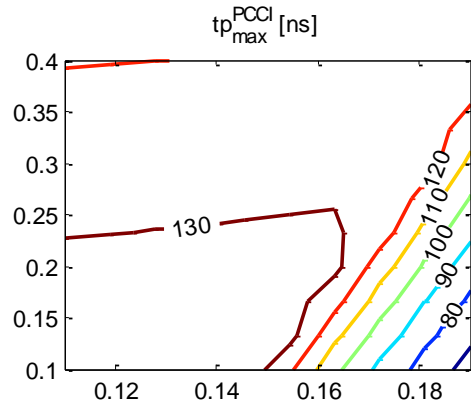
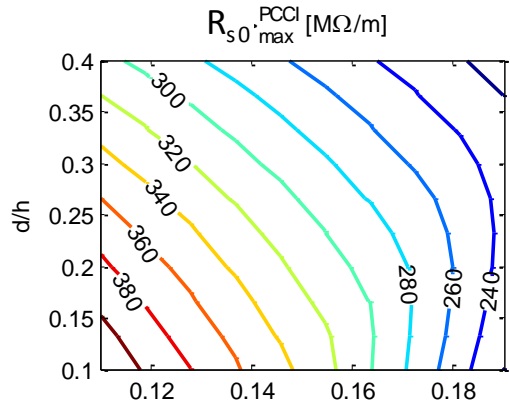
Assumption:

Effective pulse length for breakdowns is \sim half of the compressed pulse

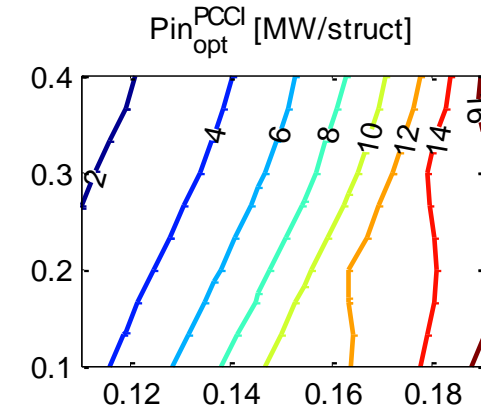
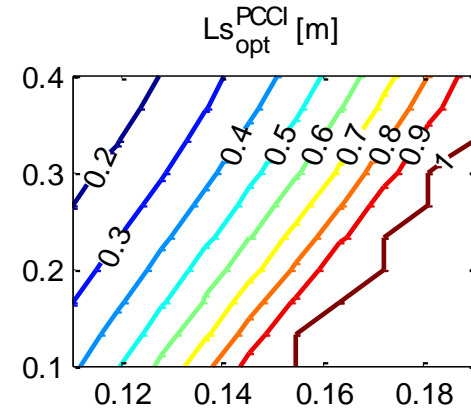
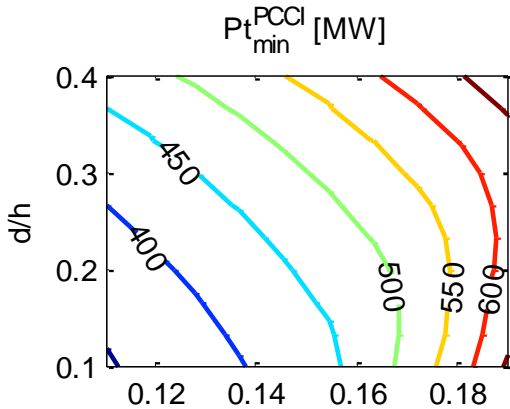
\Rightarrow Breakdown limits are very close for large a/λ and thin irises

A dedicated BDR measurements are needed for compressed pulse shape

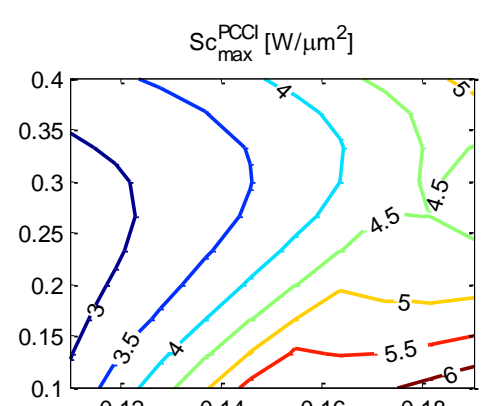
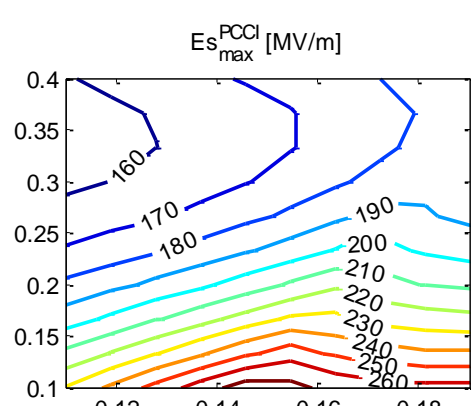
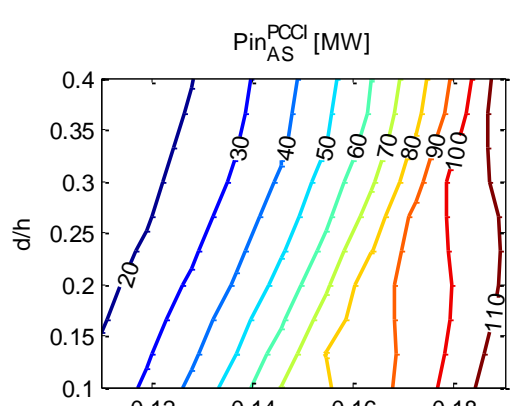
CIAS with PC: max. Lstruct < 1m




For high
vg corner
Shorter tp
Lower Qe



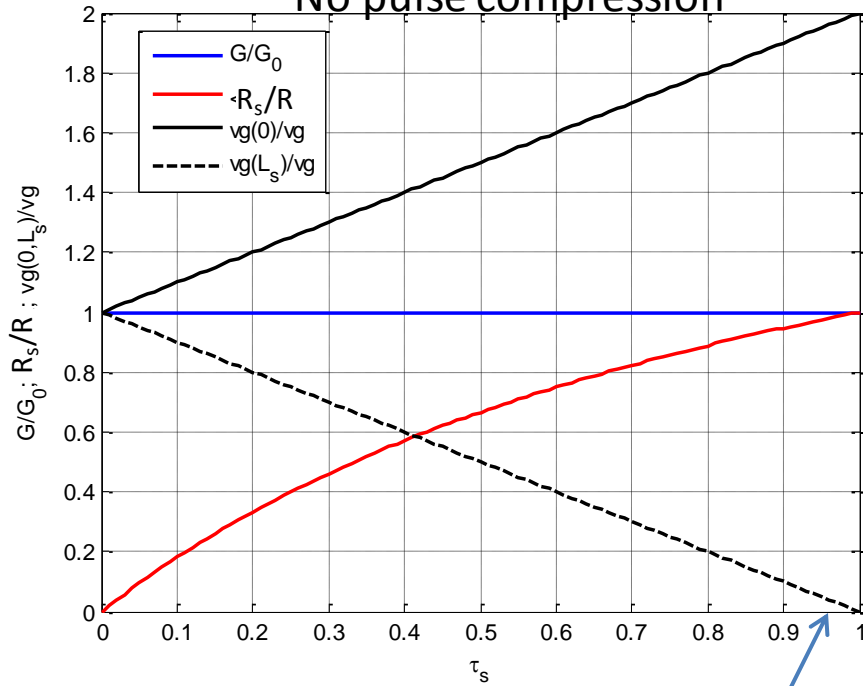
More Pt_{total} 
Less $Pin/klust.$



Lower
field and
power
quantities 

Const Gradient (CG) AS

No pulse compression

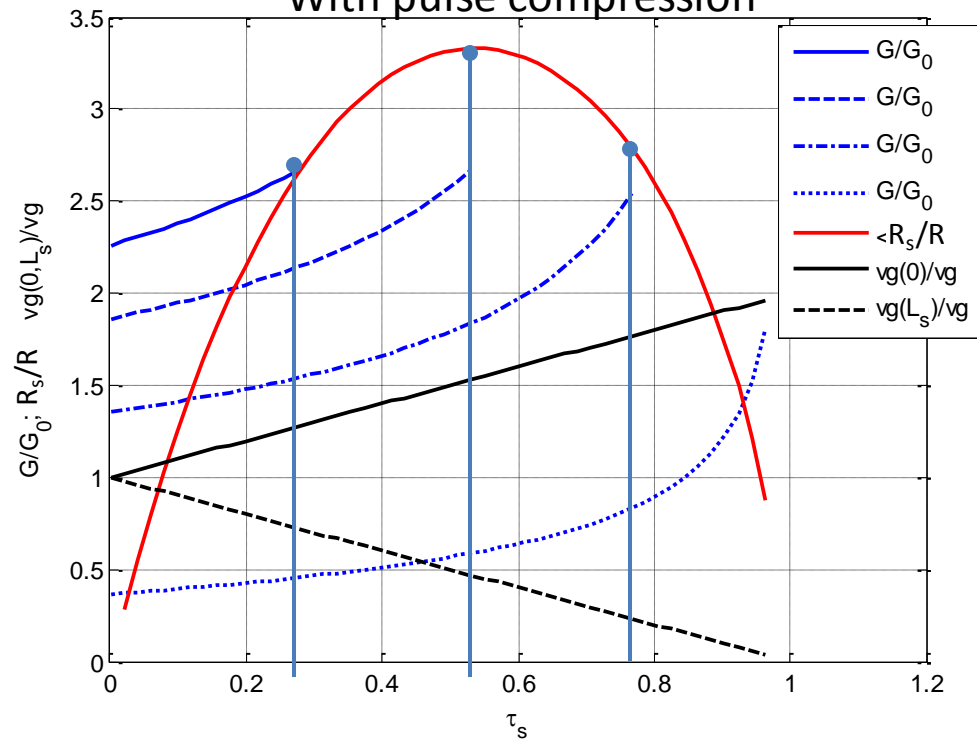


If the last cell ohmic and diffraction losses are equal => minimum vg.

For 12 GHz, $Q=8000$, $l_c = 10\text{mm}$: $\tau_{s0} = 0.96$;
 $\min(vg/c) = 0.032$ - very low vg at the end
 BUT CGAS can reach higher R_s/R than CIAS

Lowest group velocity limits the CGAS performance

With pulse compression



$Q = 8128$; $Q_0 = 180000$; $Q_e = 20000$

$\tau_{s0} = 0.5366 \Rightarrow R_{s0}/R = 3.328$ – function Q-factors

Roughly the same as for CIAS with pulse compression

$vg_{\max} = vg(1+0.5366)$; $vg_{\min} = vg(1-0.5366)$

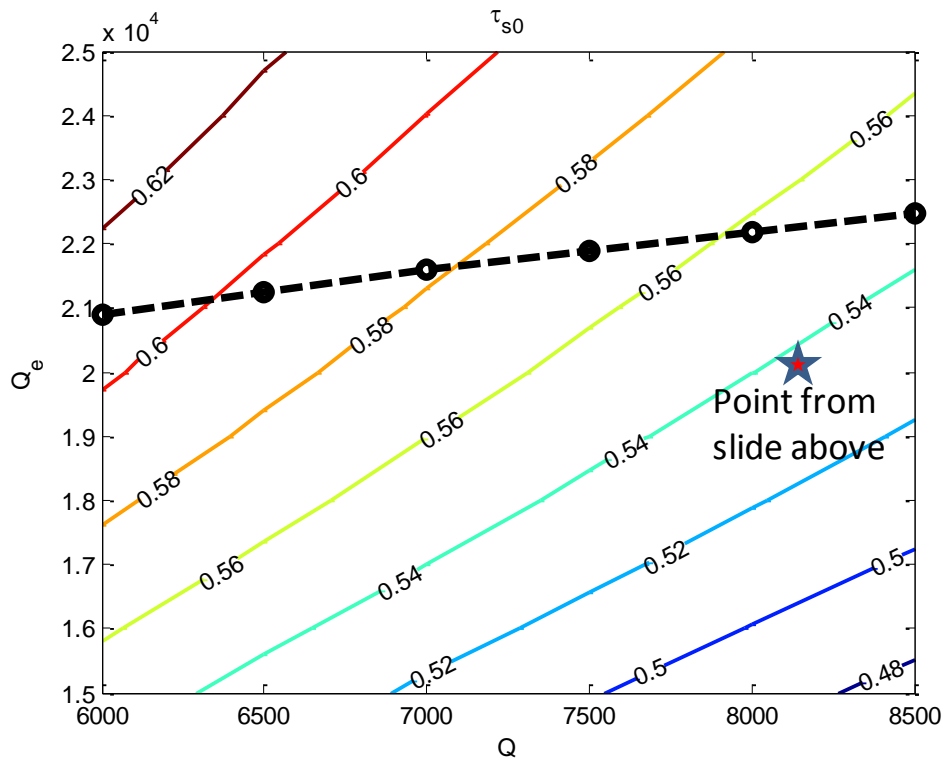
Optimum vg variation is about factor 3.3

CIAS pulse compression optimum

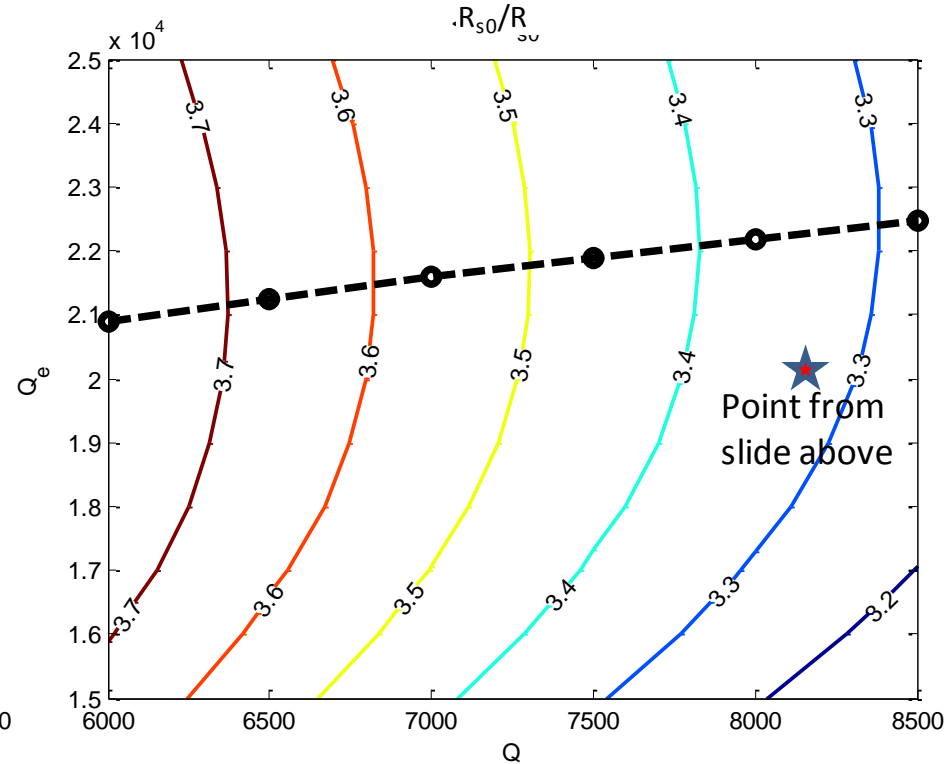
$Q_0 = 180000$ – Q-factor of the pulse compressor cavity(s)

$t_k = 1500$ ns – klystron pulse length

Optimum attenuation: τ_{s0}



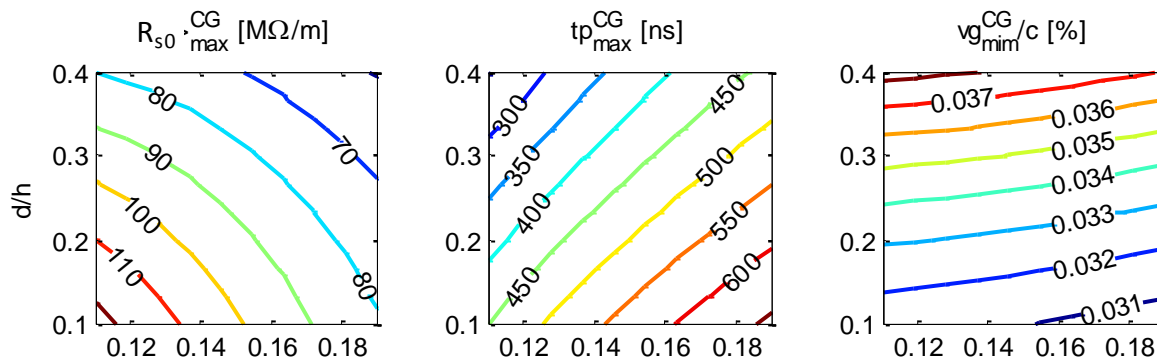
Averaged Shunt Impedance R_{s0}/R_c



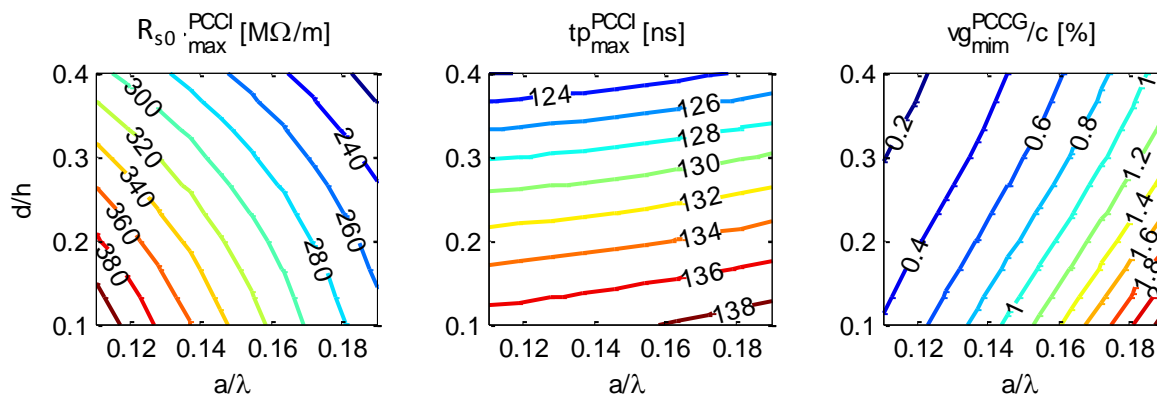
Optimum value of $Q_e \sim \text{const}$: ranges from 21000 for $Q=6000$ up to 22000 for $Q=8000$

CGAS Effective Shunt Impedance: w/o and with pulse compression

No pulse
compression



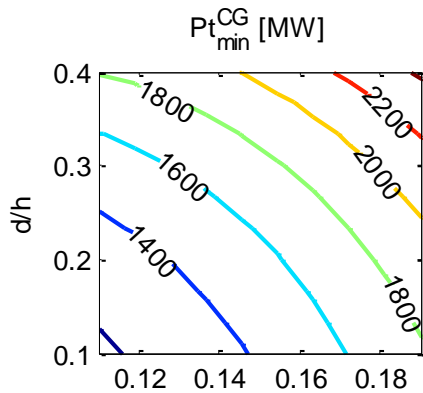
With pulse
compression



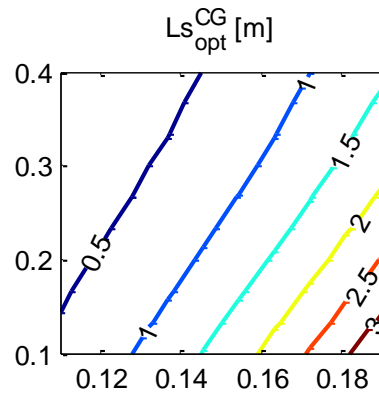
- CGAS has higher R_s compared to CIAS if no pulse compression is used and the **same R_s with pulse compression**
- Optimum pulse length is ~ 4.5 times longer if no pulse compression is used, still it is significantly shorter than the klystron total pulse length

CGAS linac 40 m long, $\langle G \rangle = 60 \text{ MV/m}$: w/o and with PC

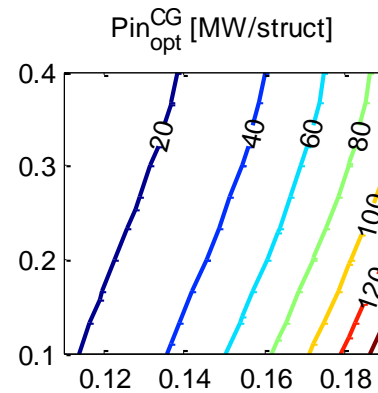
Total klystron power



Optimum structure length



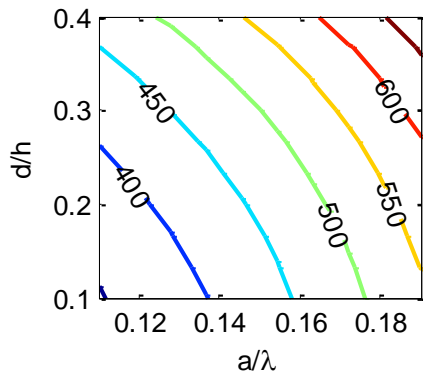
Klystron power per structure



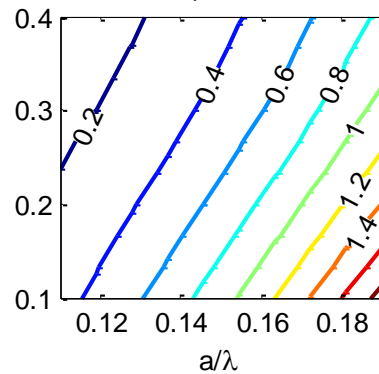
~# of structures per 0.8x50 MW klystron

2 -> 1/3

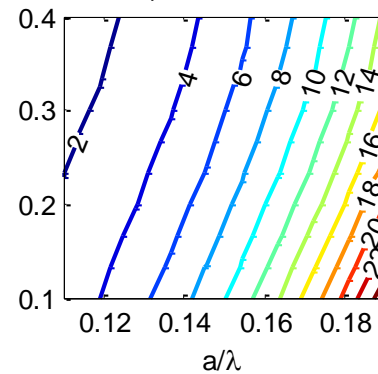
Total klystron power



Optimum structure length



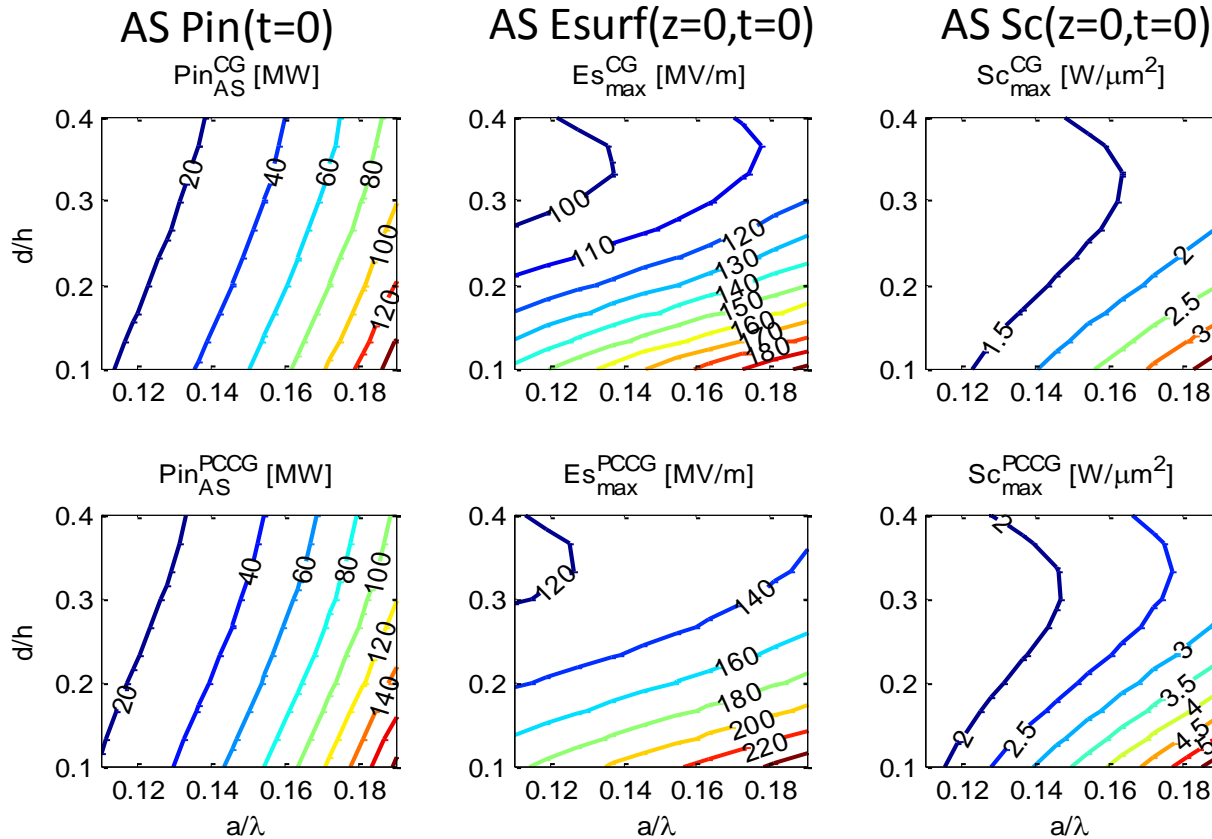
Klystron power per structure



~20 -> ~2

Optimum structure length and input power per structure are very similar to the CIAS

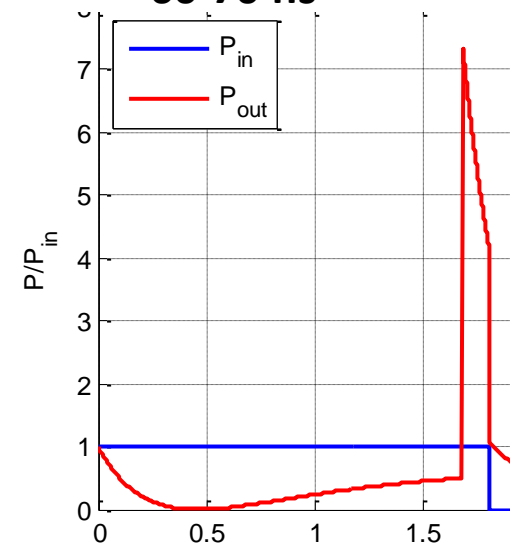
CGAS high gradient related parameters: w/o and with PC



Typical Pulse length

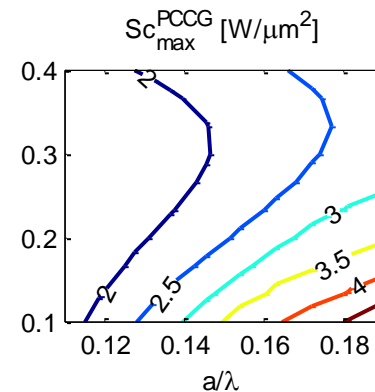
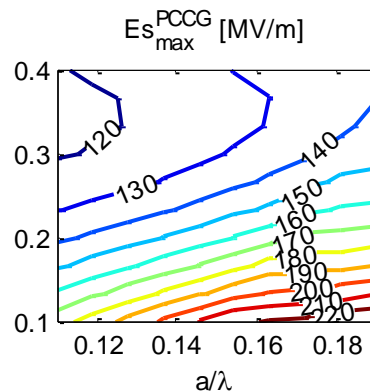
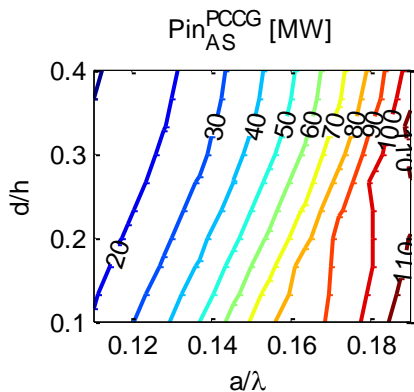
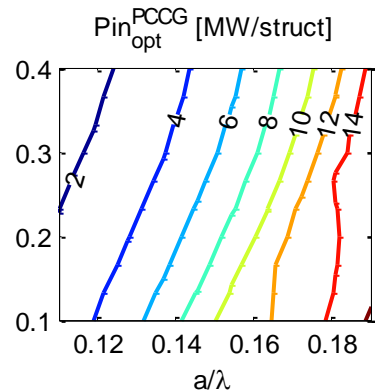
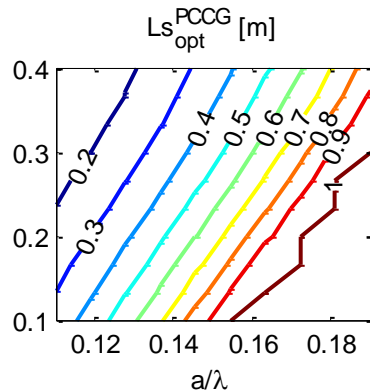
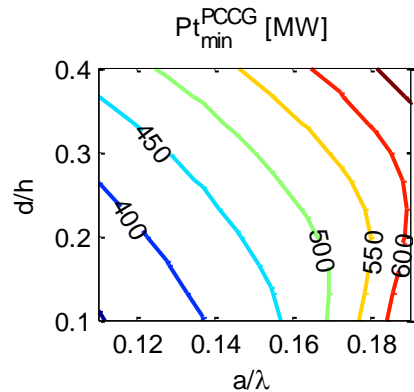
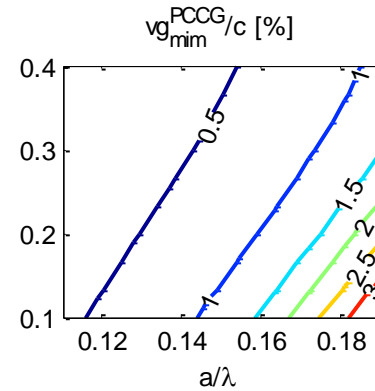
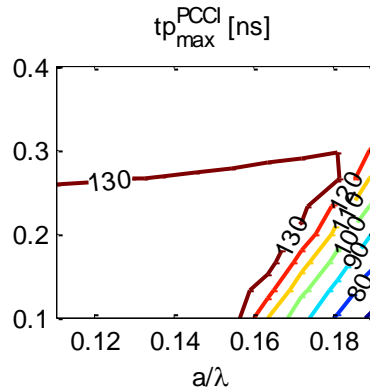
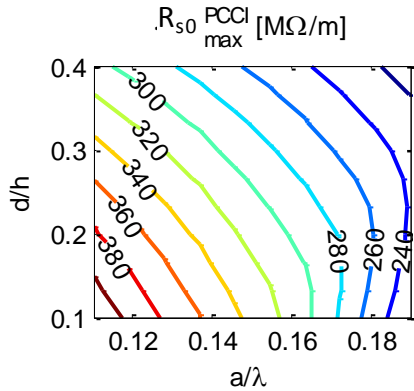
Flat pulse: 250-650 ns
Above the HG limits for larger apertures

Peaked pulse:
122-138 ns
60-70 ns





- Due to much shorter **compressed pulse** the **CGAS with PC is safer** in terms of high gradient related parameters than w/o PC
- Also due to CG profile it is significantly safer than CIAS with PC

CGAS with PC: max. Lstruct < 1m



For high
vg corner

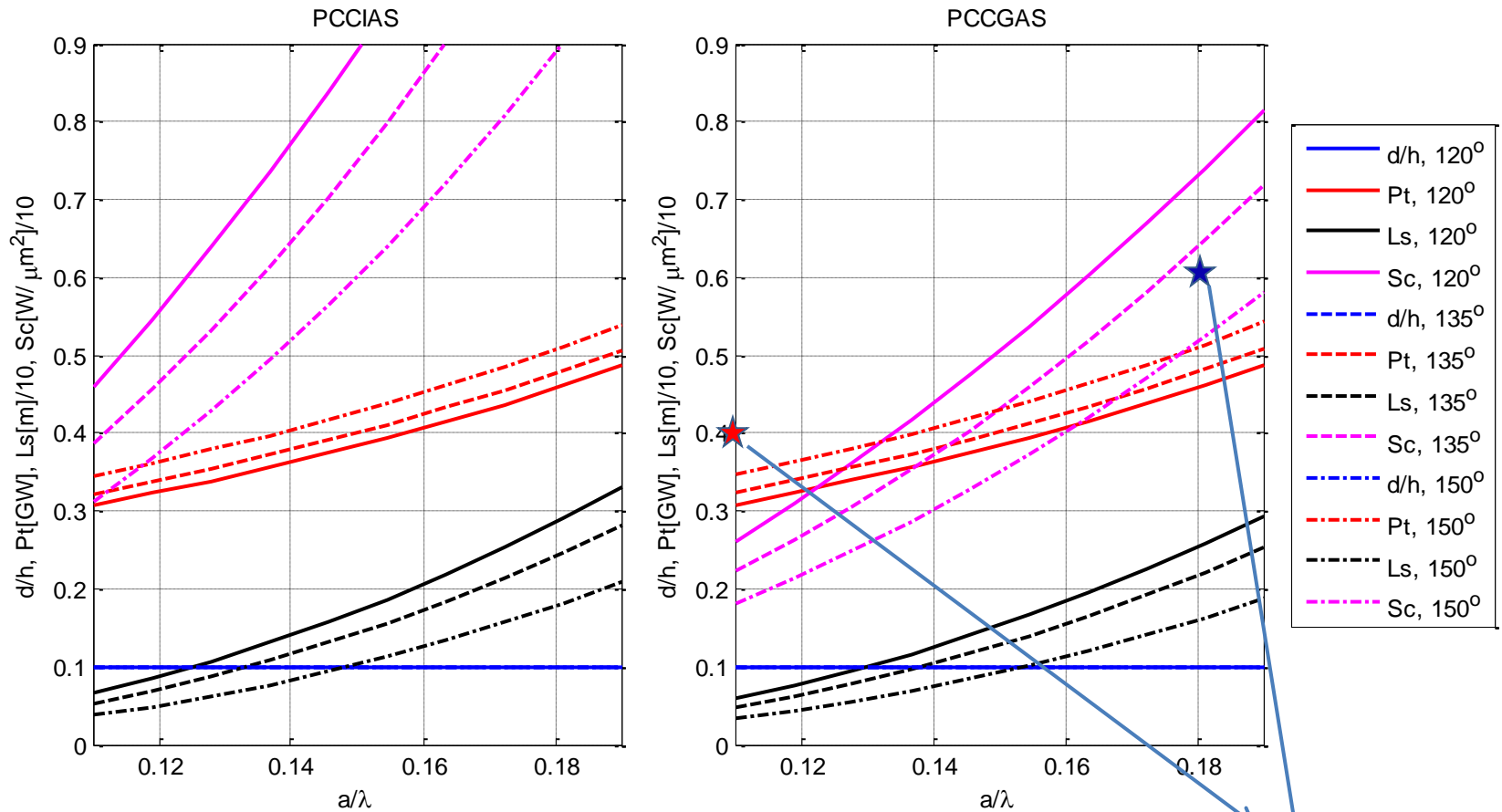
Shorter tp
Higher
vg_min

More Ptotal 
Less
Pin/klyst.


A little bit
lower
field and
power
quantities

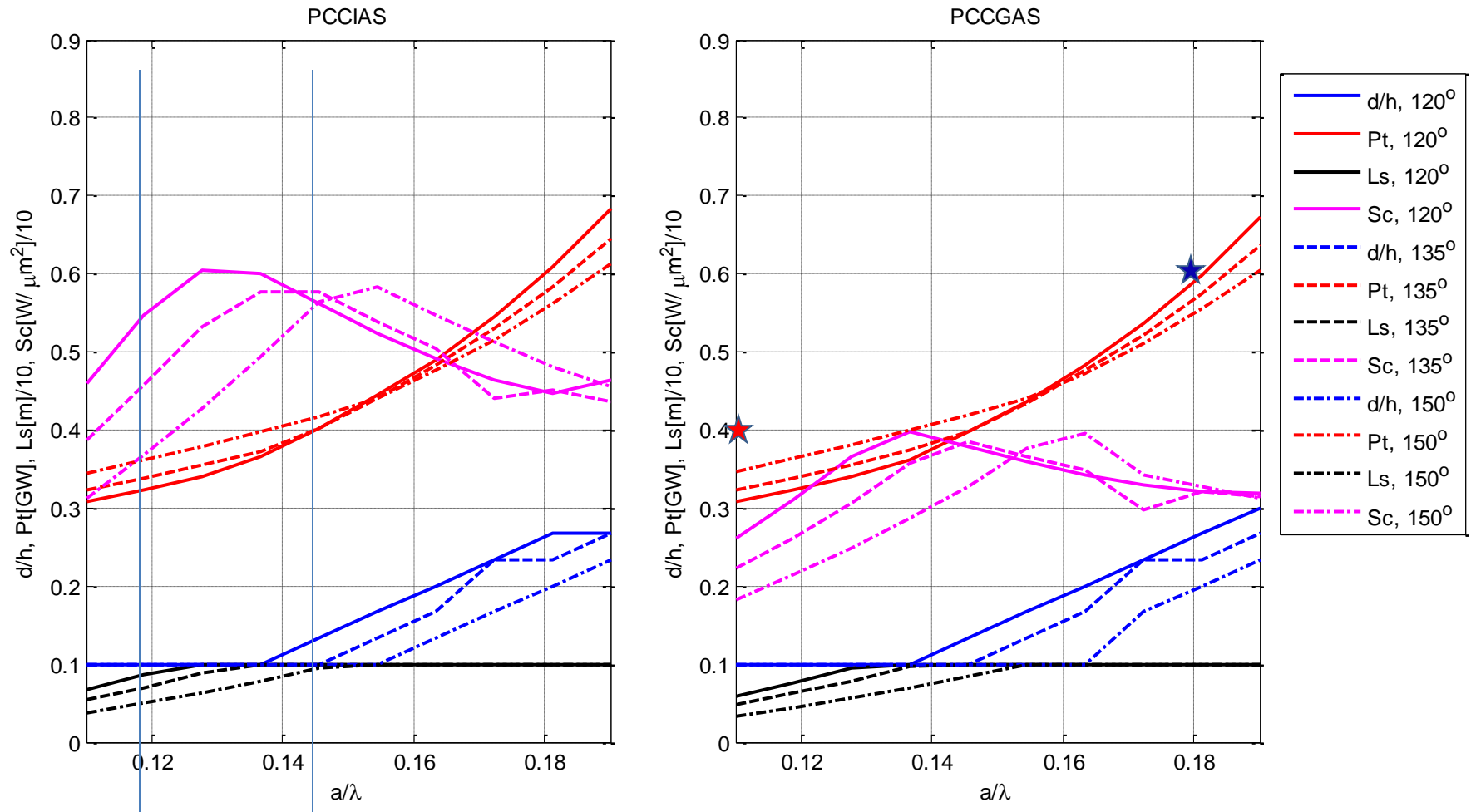


CIAS and CGAS with PC, different RF phase advance, no constraints



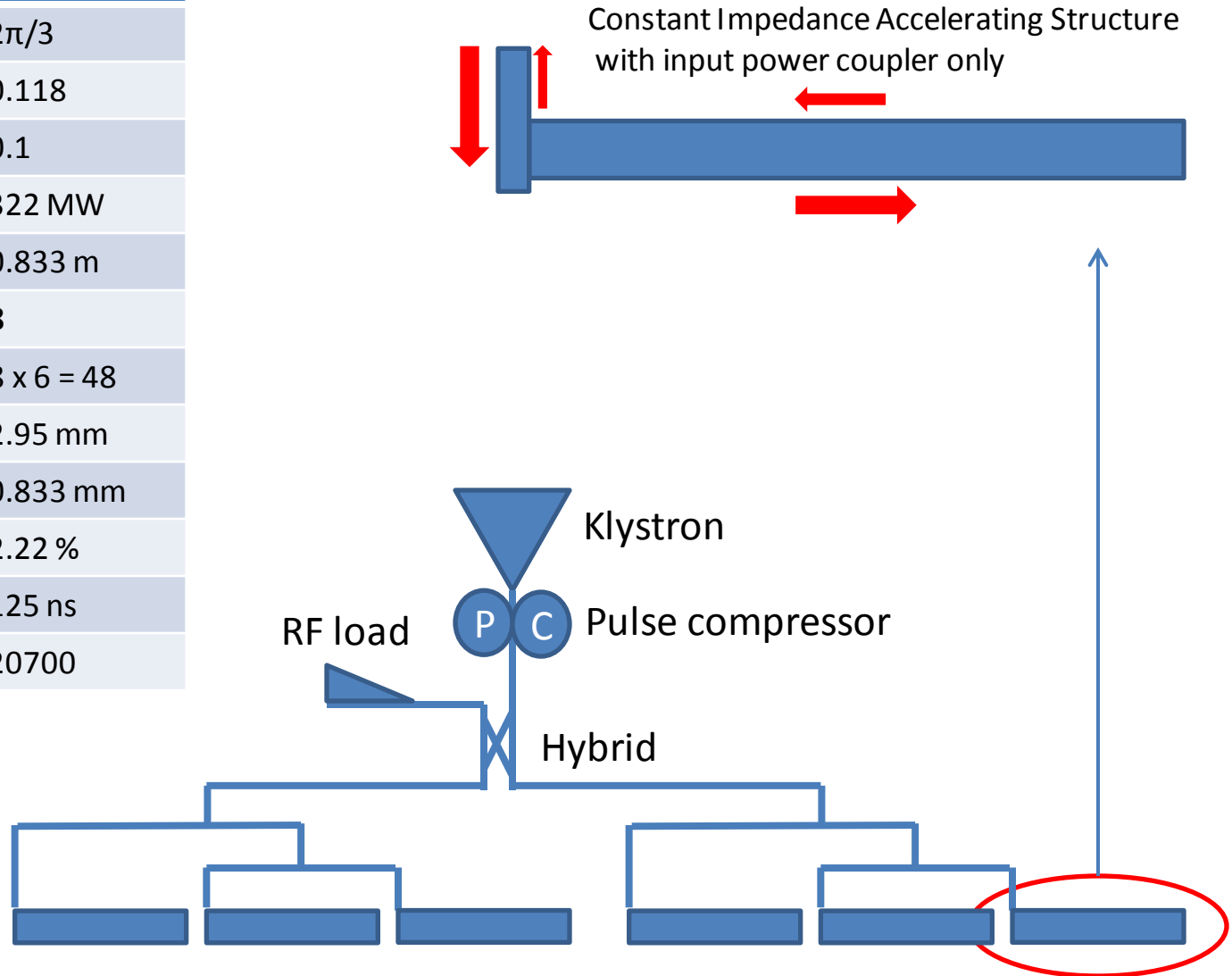
CLIC_G_undamped: $\tau_s = 0.31 < \tau_{s0} = 0.54$; $Ls = 0.25\text{m}$; $Qe = 15700$; $Pt = 400\text{MW}$
 H75 : $\tau_s = 0.50 \sim \tau_{s0} = 0.54$; $Ls = 0.75\text{m}$; $Qe = 20200$; $Pt = 613\text{MW}$

CIAS and CGAS with PC, different RF phase advance, $L_s < 1m$



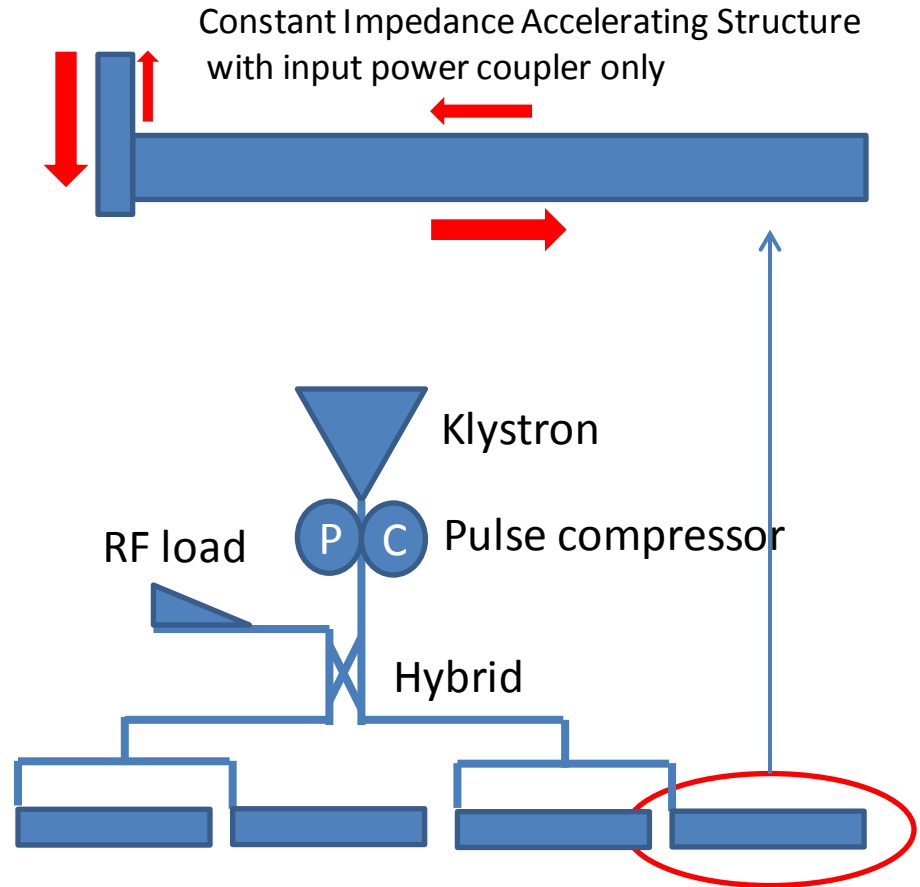
Small aperture linac, 2.4 GeV, 40m

RF phase advance	$2\pi/3$
a/λ	0.118
d/h	0.1
P_t	322 MW
L_s	0.833 m
# klystrons	8
# structures	$8 \times 6 = 48$
a	2.95 mm
d	0.833 mm
v_g/c	2.22 %
t_p	125 ns
Q_e	20700



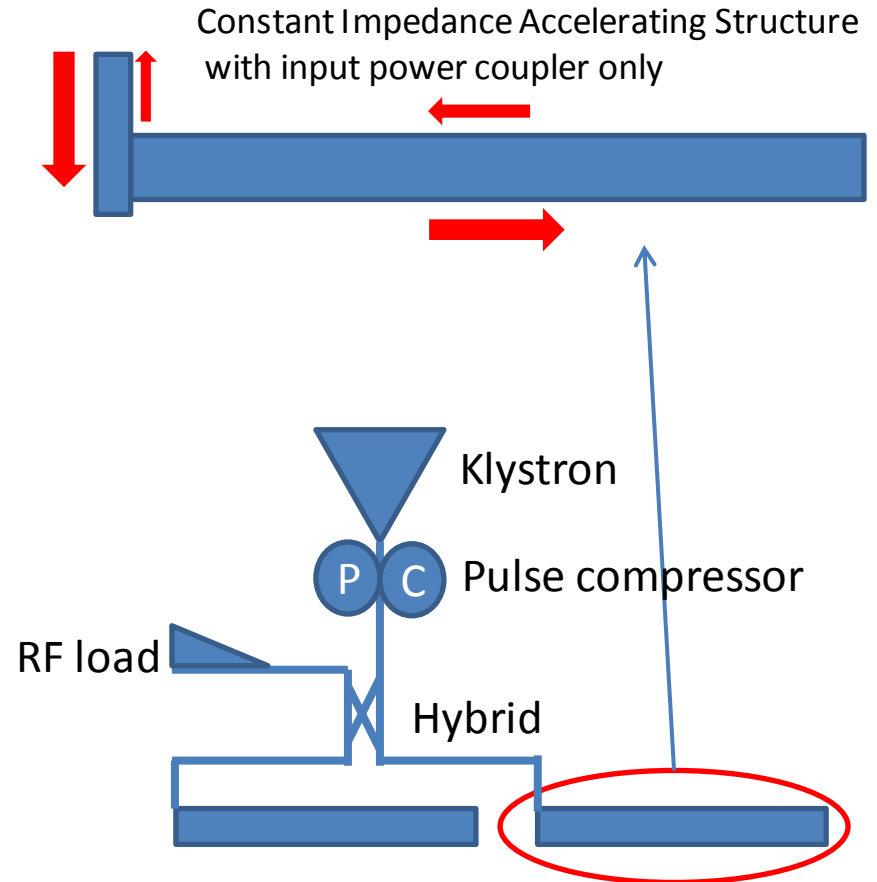
Middle aperture linac, 2.4 GeV, 40m

RF phase advance	$2\pi/3$	$3\pi/4$
a/lambda	0.145	0.145
d/h	0.1313	0.1
Pt	401 MW	401 MW
Ls	1 m	1 m
# klystrons	10	10
# structures	10 x 4 = 40	10 x 4 = 40
a	3.62 mm	3.62 mm
d	1.09 mm	0.937 mm
vg/c	3.75 %	3.29%
tp	90 ns	102 ns
Qe	18000	19000

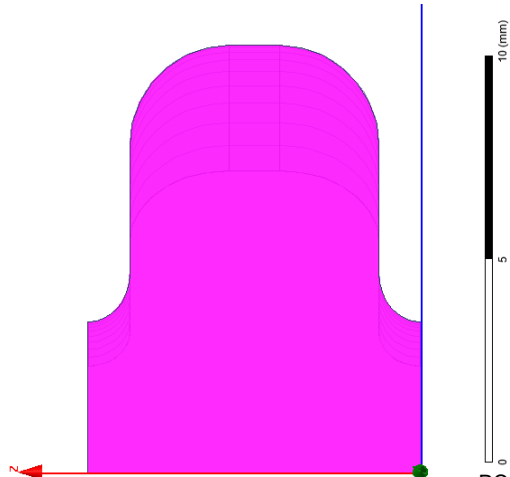
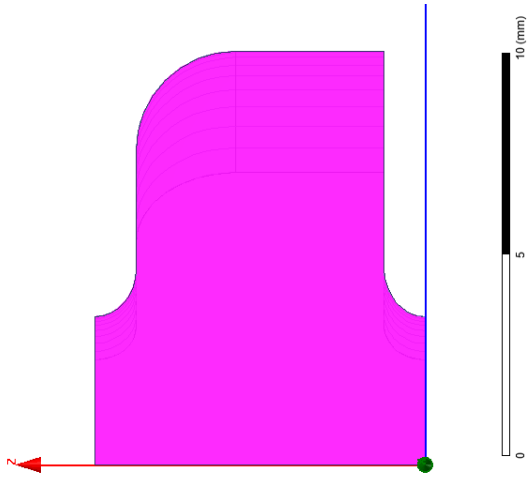


Large aperture linac, 2.4 GeV, 40m

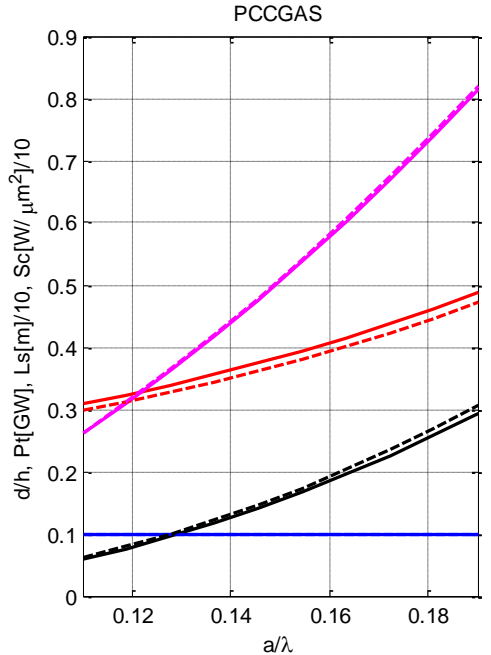
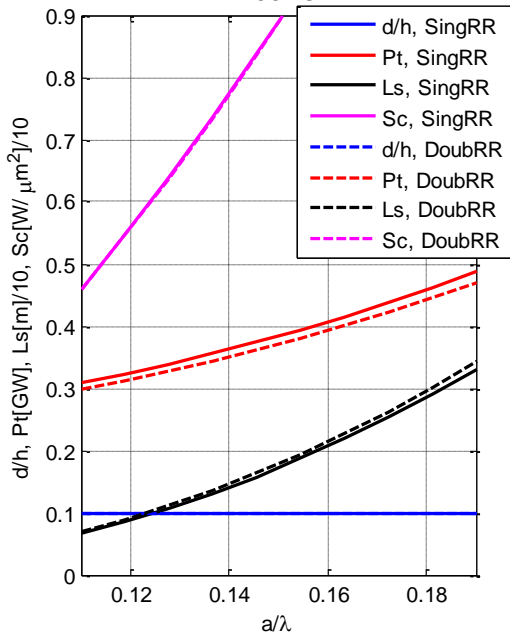
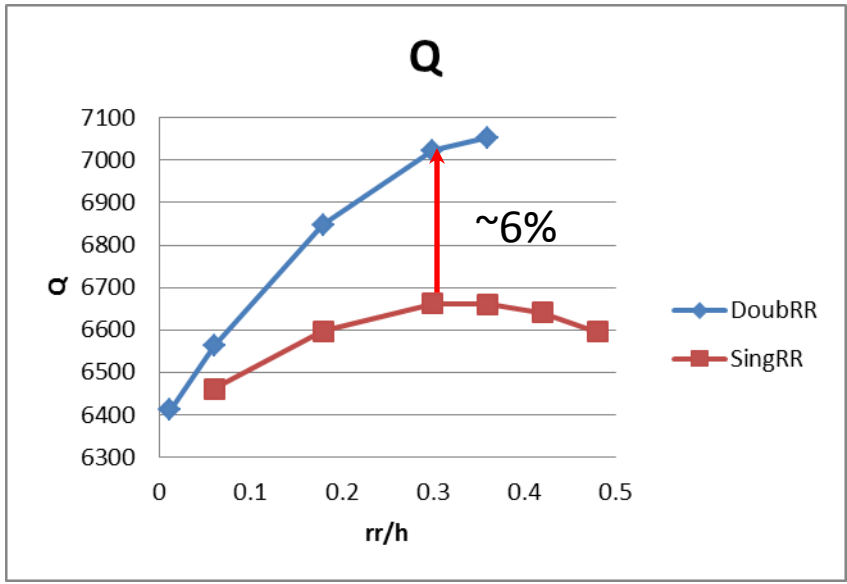
RF phase advance	$5\pi/6$
a/λ	0.195
d/h	0.183
Pt	602 MW
Ls	1.333 m
# klystrons	15
# structures	15 x 2 = 30
a	4.87 mm
d	1.90mm
v_g/c	4.425 %
tp	101 ns
Qe	18500



Single- versus Double-rounded cells



- By doing double rounded cells instead of single rounded cells Q-factor is increased by 6%
- The total linac power is reduced only by 3.7% (not 6%) because optimum is adapted to the Q
- No tuning will be possible



Conclusions

- An analytical expression for effective shunt impedance of the CI and CG AS without and with pulse compression have been derived.
- Maximizing effective shunt impedance for a given average aperture gives the optimum AS+PC design of a single bunch linac
- Different constraints have been applied to find practical solutions for a FERMI energy upgrade based on the X-band 2.4 GeV, 60 MV/m linac