

# ***Top-antitop Threshold Production at Electron-Positron Colliders***

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# Topics discussed

- *Why top threshold?*
- *Status of theoretical analysis*
- *Review of experimental simulations*
- *Open questions*

prepared in collaboration with Aurelio Juste (*Universitat Autònoma de Barcelona*)

# Why threshold scan at LC?

## ● Theory

- *top quark width is a natural infrared cutoff*

- ➔ *first principle QCD predictions*

## ● Experiment

- *as clean as possible for a strongly interacting particle*

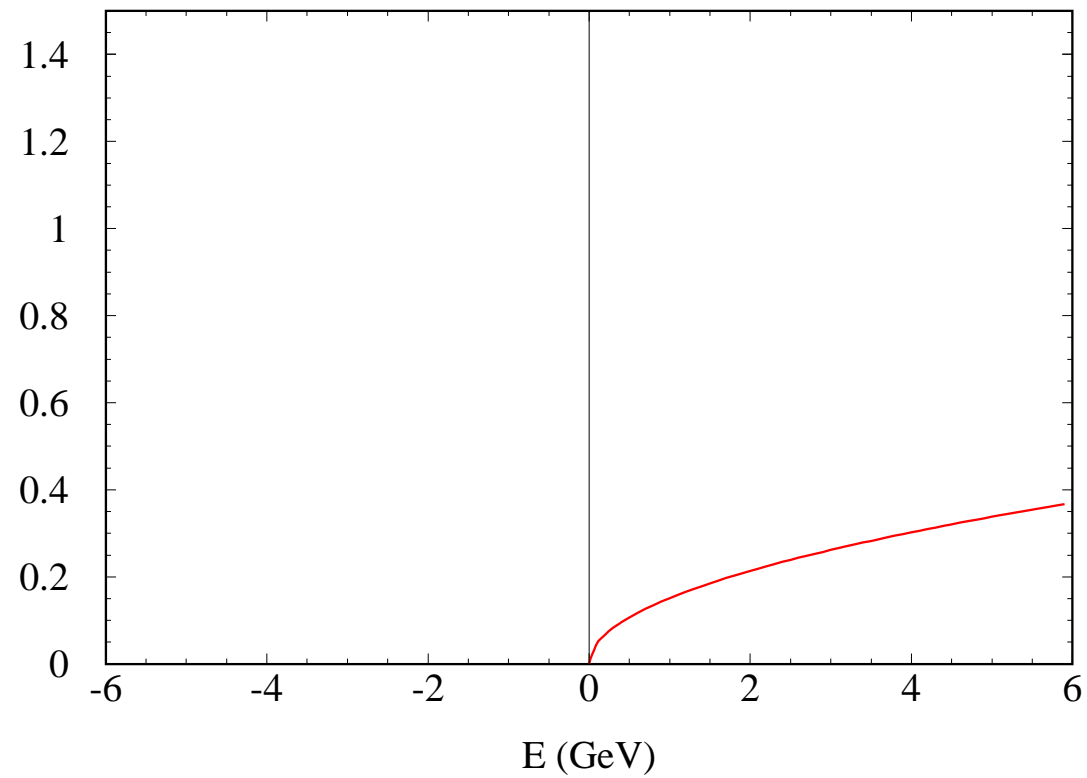
## ● Phenomenology

- *most precise determination of top quark properties such as*

*mass, width, vector couplings*

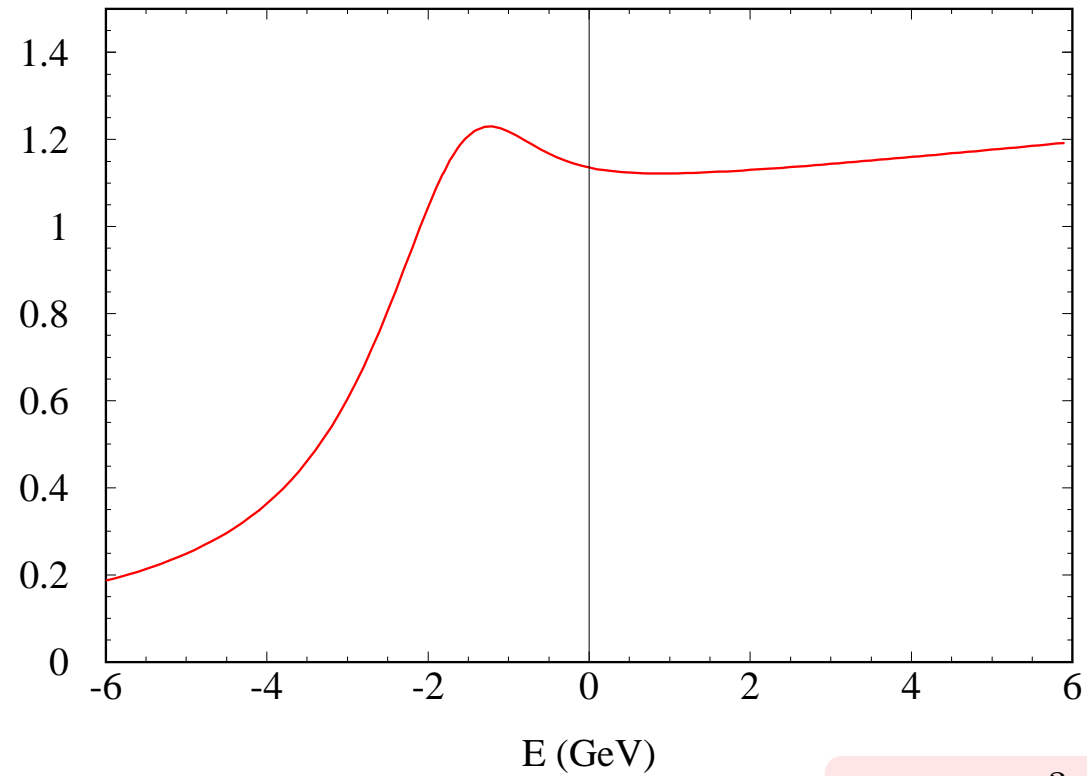
# Born cross section

$$\sigma(e^+e^- \rightarrow t\bar{t})$$



# Coulomb and finite width effects

$\sigma(e^+e^- \rightarrow t\bar{t})$



$$\sigma_{\text{res}} \sim \frac{\alpha_s^3}{m_t \Gamma_t}, \quad E_{\text{res}} - 2m_t \sim \alpha_s^2 m_t$$

# Perturbation theory

- NNLO (end of last century)

- *Apparent slow convergence*

- Possible reasons:

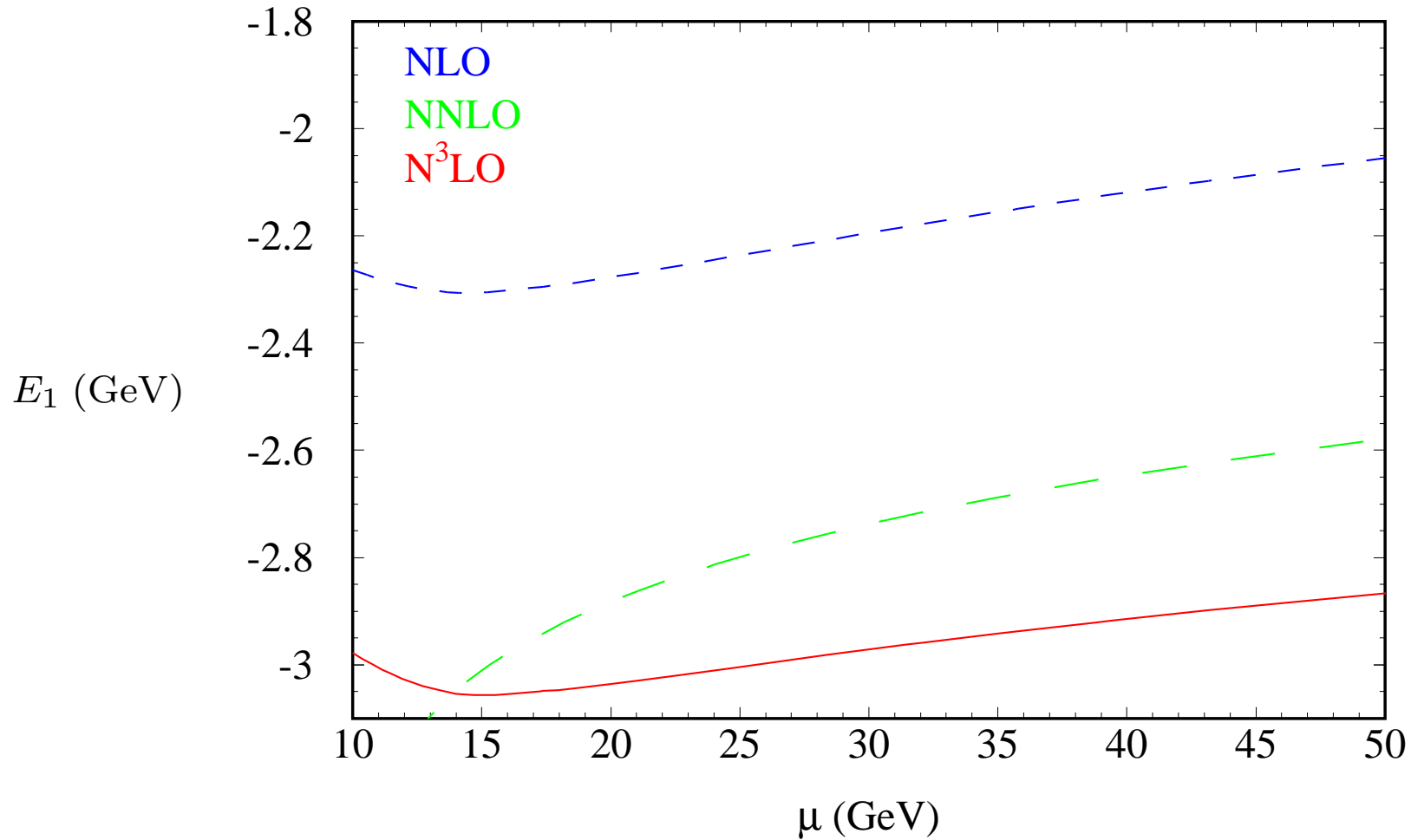
- *Renormalons*  $n!(\beta_0\alpha_s)^n$

- *Threshold logs*  $\alpha_s^n \ln^m \alpha_s$

➔ **Full  $N^3LO$  analysis is mandatory**

# N<sup>3</sup>LO resonance energy

A. Penin, M. Steinhauser Phys.Lett. B538 (2002) 335



# Top mass at N<sup>3</sup>LO

A. Penin, M. Steinhauser Phys.Lett. B538 (2002) 335

Toponium resonance energy:  $E_{\text{res}} = 2m_t + E_1^{N^3LO} + \delta\Gamma_t E_{\text{res}}$

$$E_{\text{res}} = \left( 1.9833 + 0.007 \frac{m_t - 174.3 \text{ GeV}}{174.3 \text{ GeV}} \pm 0.0009 \right) \times m_t$$

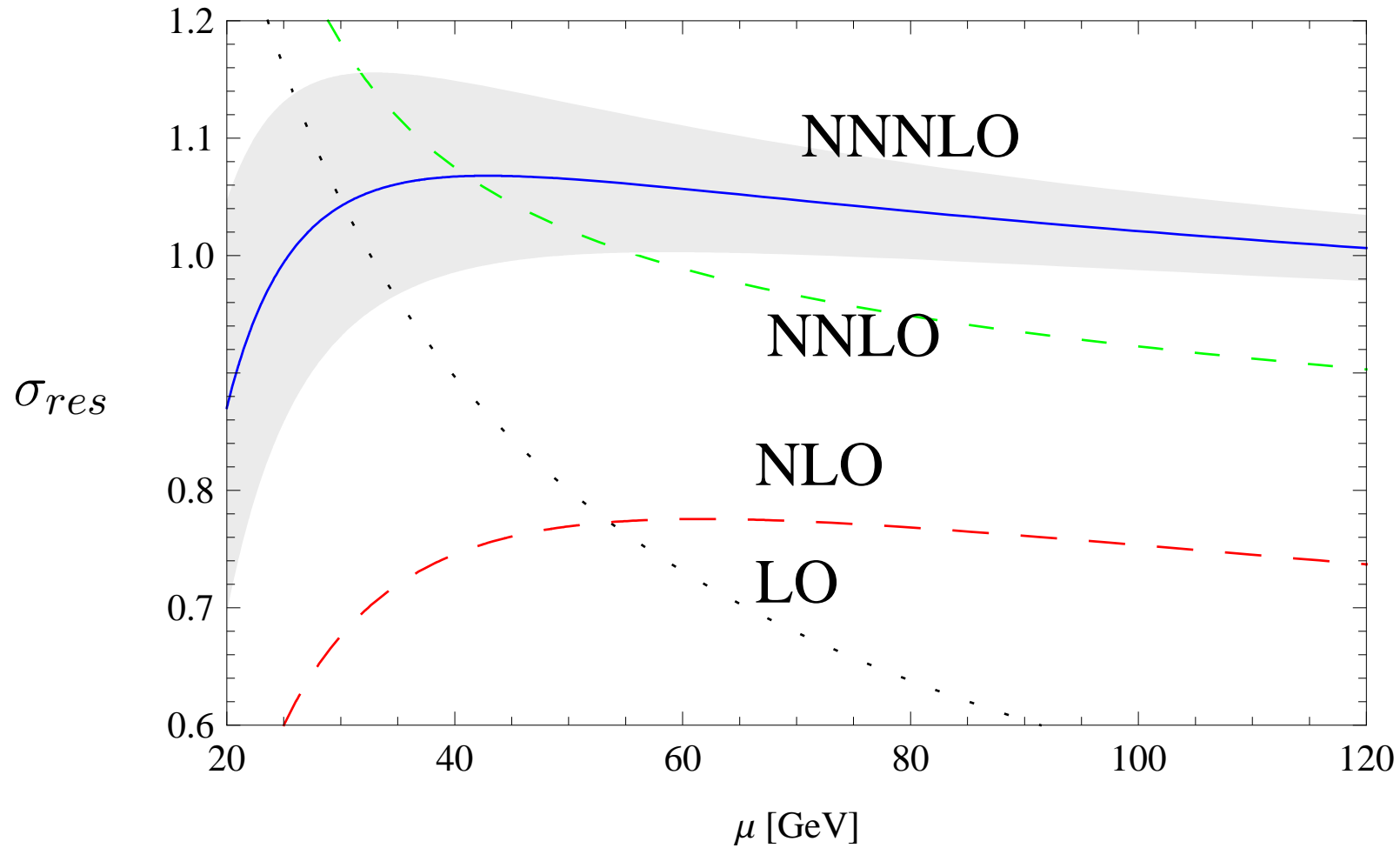
- *Top quark mass  $m_t$  with 80 MeV accuracy (renormalons?)*
- *Short distance mass  $\bar{m}_t(\bar{m}_t)$  with 50 MeV accuracy\**

Y. Kiyo, Y. Sumino, Phys. Rev. D 67 (2003) 071501



# $N^3$ LO resonance cross section

M. Beneke Y. Kiyo, A. Penin, K. Schuller, arXiv:0710.4236 [hep-ph]



# Finite width effect

## ● Resonant approximation

V.Fadin, V.Khoze, JETP Lett. 46 (1987) 525

$$\delta(\mathbf{p}^2 - m_t E) \rightarrow \frac{1}{\pi} \frac{\Gamma_t}{(\mathbf{p}^2/m_t - E)^2 + \Gamma_t^2},$$

*not consistent in pNRQCD beyond LO!*

## ● Nonresonant contribution (up to 10%)

### ● NLO

M. Beneke, B. Jantzen, P. Ruiz-Femenía, Nucl. Phys. B840 (2010) 186

### ● NNLO

A. Penin, J. Piclum, JHEP 1201 (2012) 034

# Theory summary

## ● Top mass

- *NNNLO QCD*

➔ *80 MeV (50 MeV) accuracy*

## ● Total cross section

- *NNNLO QCD (coming soon)*

- *NNLO finite width*

➔ *3% accuracy*

## ● Differential observables

- *momentum distribution, forward-backward asymmetry*

A. H. Hoang, T. Teubner, Phys. Rev. D **60** (1999) 114027;

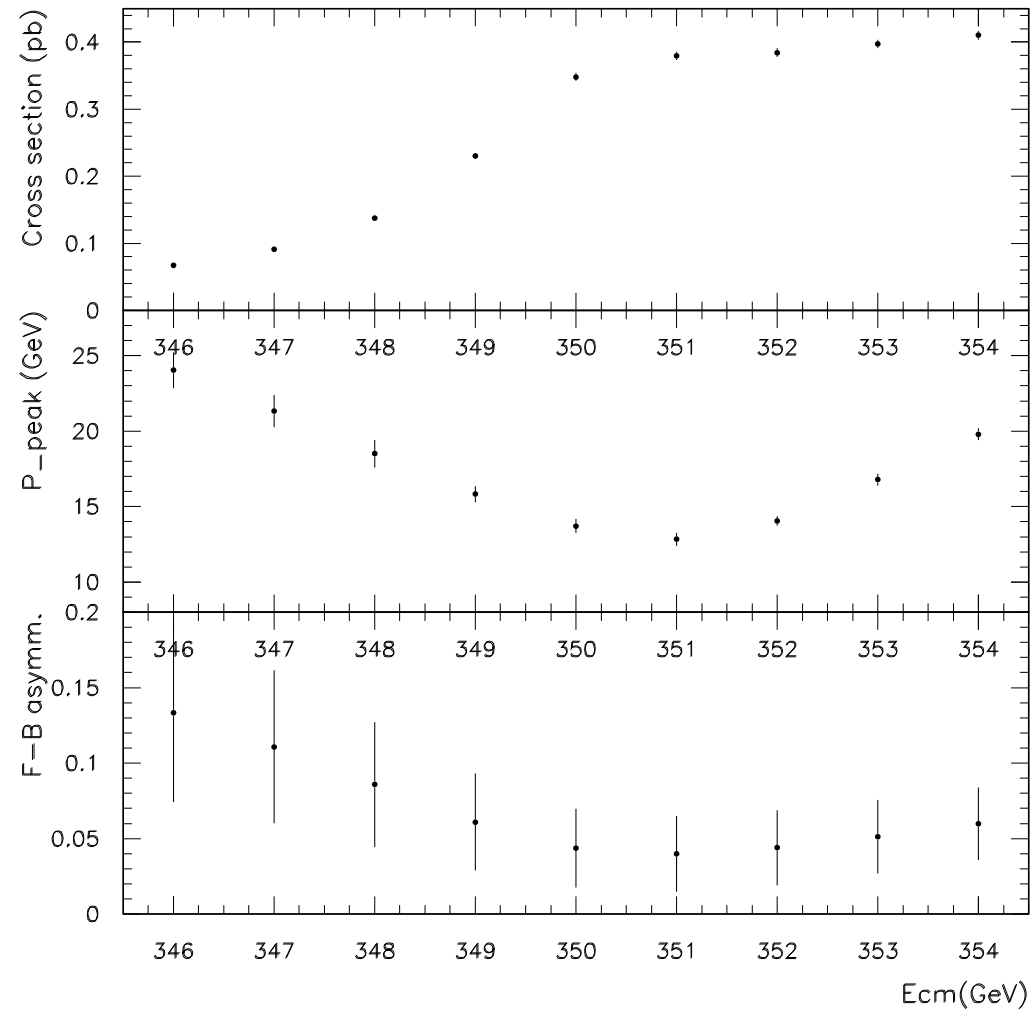
T. Nagano, A. Ota, Y. Sumino, Phys. Rev. D **60** (1999) 114014

- *NNLO QCD, LO finite width, > 10% uncertainty*

# Simulations

M. Martinez, R. Miquel, Eur. Phys. J. C 27 (2003) 49

Expected scan results



# Estimated experimental accuracy

- Detectors, event selection efficiency, statistics ( $300 \text{ fb}^{-1}$ )

M. Martinez, R. Miquel, Eur. Phys. J. C 27 (2003) 49; F. Simon (LCD-Note-2013-013)

- *total cross section 3%*
- *differential observables significantly worse*
- *resonance energy 31 MeV*

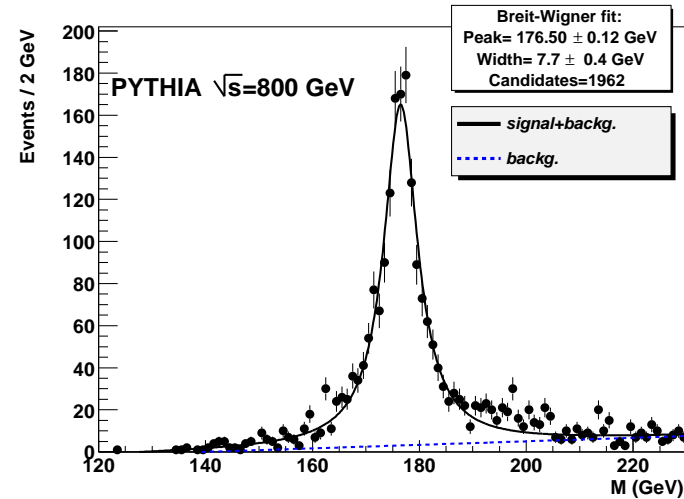
- Beam effects in resonance energy determination

F. Gournaris (PhD thesis 2009)

- *nominal beam energy induced uncertainty 35 MeV*
- *luminosity spectrum induced uncertainty 50 MeV*

# Direct reconstruction of top quark mass

S.V. Chekanov, Eur. Phys. J. C 26 (2002) 13; F. Simon (LCD-Note-2013-013)



- Experimental errors in hadronic (semileptonic) channels
  - *statistical*  $100 \text{ fb}^{-1}$ : 100 MeV (140 MeV)
  - *systematical (hadronization model)*: 400 MeV (250 MeV)

# Top precision measurements from threshold scan

## ✓ Top quark mass

*total uncertainty  $\sim 100 \text{ MeV} \Rightarrow$  beats direct reconstruction*

## ✓ Top quark width

*total uncertainty  $\sim 34 \text{ MeV}$*

## ✓ Top quark vector couplings

*total uncertainty  $\sim 3\%$*

## ✗ Top quark Higgs coupling (from Yukawa potential)

*factor 2 uncertainty  $\Rightarrow$  cannot compete with Higgs production*

# Problems to solve

## ● Theory

- *Renormalization group improved NNNLO analysis*
- *Four-loop relation between pole and  $\overline{MS}$  mass*

## ● Experiment

- *Systematic uncertainty budget for direct top mass reconstruction*