

Hadronic collisions: cross sections, diffraction, and multi-parton interactions

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Particle Physics Phenomenology Workshop
devoted to the memory of Alexei B. Kaidalov

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- 1 Introduction: RFT approach & Quark-Gluon String model
- 2 Enhanced Pomeron diagrams
 - resummation
 - 'loops' & 'nets' – relative importance
 - non-eikonal rap-gap suppression & diffractive cross sections
- 3 QGSJET-II Monte Carlo model
 - 'semihard Pomeron'
 - enhanced graphs: assumptions & MC implementation
- 4 Inelastic diffraction
 - M_X -shape for high mass diffraction
 - LHC puzzles
- 5 Total cross section & multi-parton interactions
 - multi-Pomeron interactions & multi-parton correlations
 - contribution from perturbative splitting: how important?

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- at colliders:
 - underlying event
 - interesting by themselves (total & elastic cross sections, diffraction, multi-particle production)

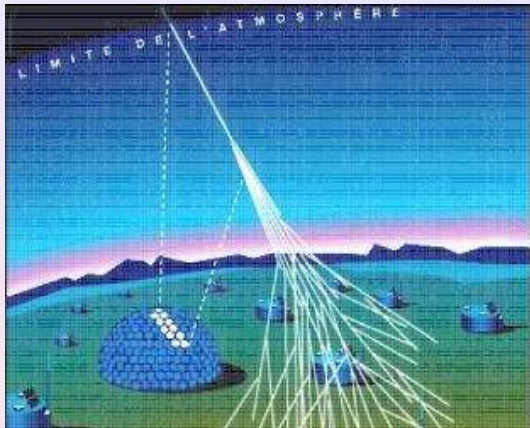
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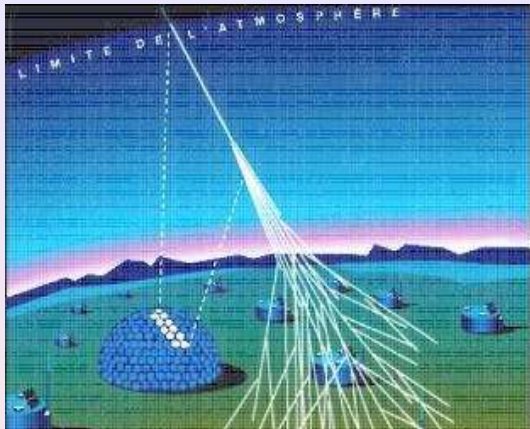
Cosmic ray studies with extensive air shower techniques



ground-based observations (= thick target experiments)

- primary CR energy \iff charged particle density at ground
- CR composition \iff muon density at ground

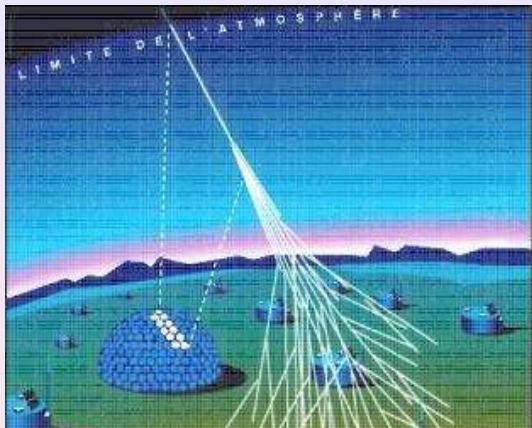
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measurements of EAS fluorescence light

- primary CR energy \iff integrated light
- CR composition \iff shower maximum position X_{\max}

Cosmic ray studies with extensive air shower techniques



CR composition studies – most dependent on interaction models

- e.g. predictions for X_{\max} depend on $\sigma_{p\text{-air}}^{\text{inel}}$, $\sigma_{p\text{-air}}^{\text{diffr}}$
- predictions for muon density – on the multiplicity $N_{\pi\text{-air}}^{\text{ch}}$

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RFT approach & Quark-Gluon String model

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- high energy hadronic collisions – **multiple scattering processes**
- may be treated using the Reggeon Field Theory (RFT)
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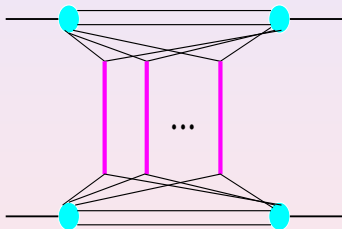
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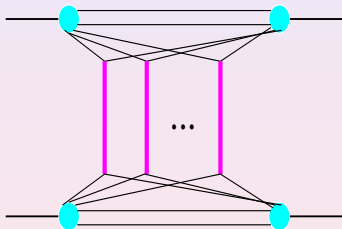
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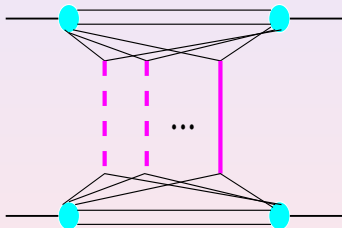
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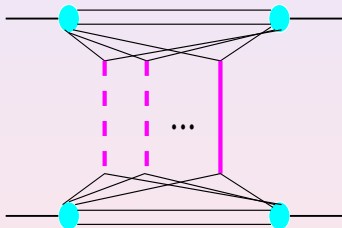
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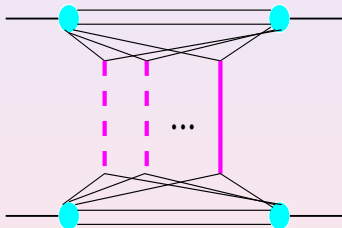
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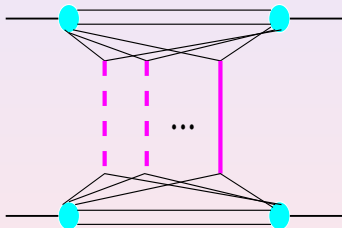
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Why not using an effective (quasi-)eikonal model?

- absorptive effects **stronger at small b , weaker at large b**
 - requires a bit of parametrising \Rightarrow loss of predictive power
- including HMD via Good-Walker (GW) formalism?
 - energy-dependent structure of GW states

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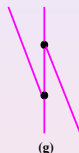
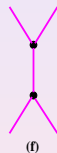
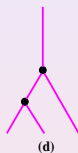
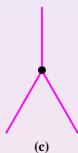
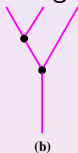
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Pomeron-Pomeron interactions important
[Kancheli, 1973; Cardi, 1974; Kaidalov et al., 1986, ...]

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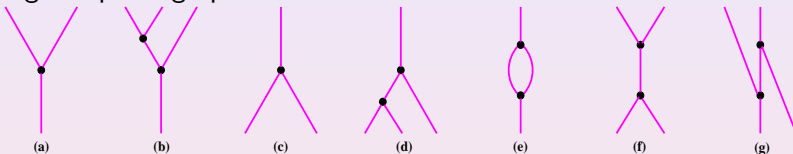
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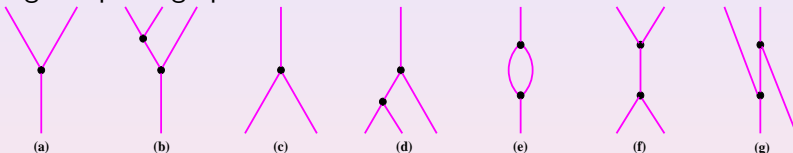


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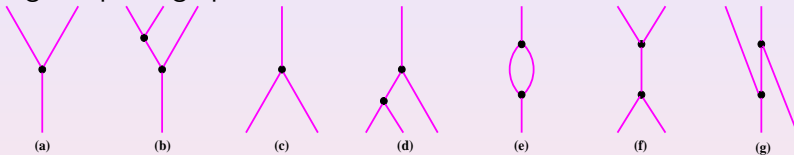
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- describe elastic re-scattering of intermediate partons off the projectile/target hadrons & off each other
- why all-order resummation?**
 - higher order (wrt $G_{3\mathbb{P}}$) contributions rise quicker with energy
 - have altering signs

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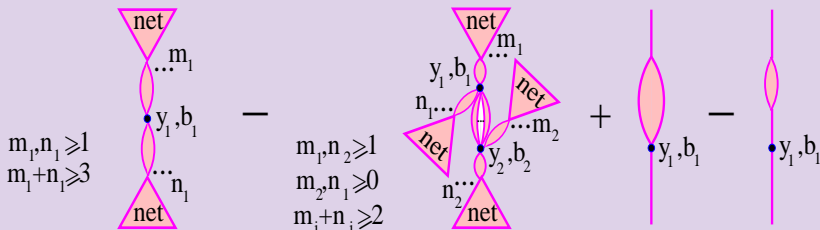


Diagrammatic resummation *[SO, 2006, 2008, 2010]*

- define some elementary 'building blocks'
- construct arbitrary enhanced graphs out of them
- correct for double (triple, etc.) counting
- similarly for cut diagrams (based on AGK-rules)

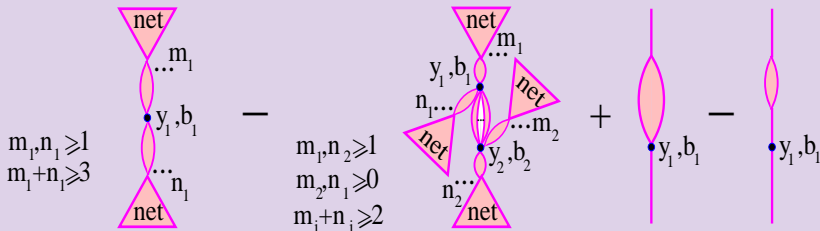
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E.g. sum of irreducible contributions to elastic amplitude

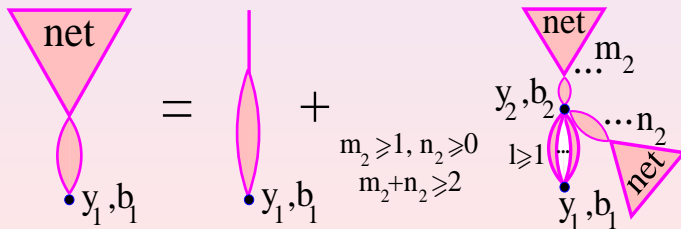


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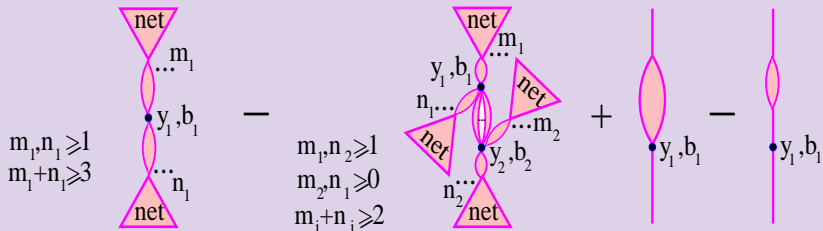


- expressed via 'net-fans' – 'reaction-dependent PDFs':

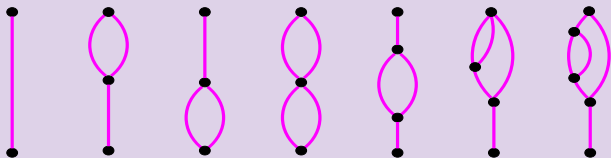


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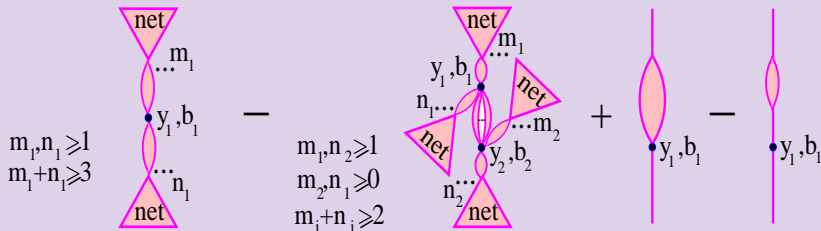


In turn, contain Pomeron 'loop' sequences (examples)

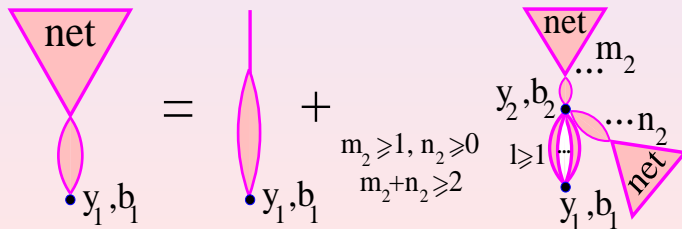


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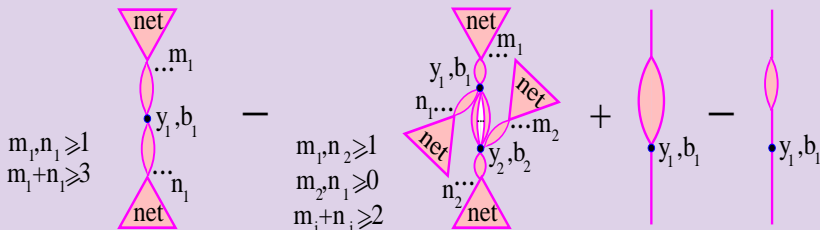


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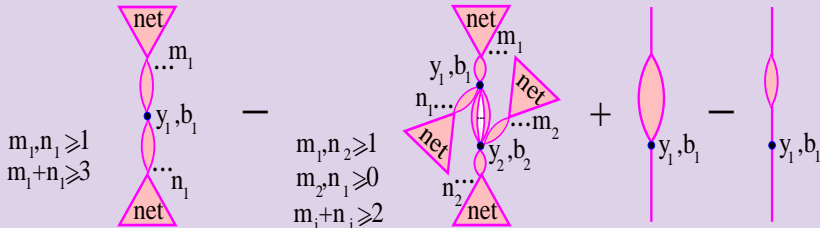
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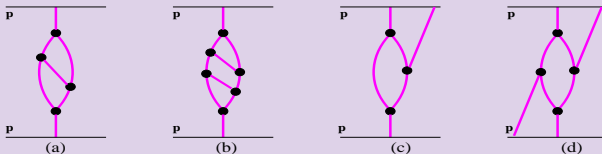
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Examples of graphs not included in the procedure



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- \Rightarrow positive-definite cross sections for various final states
- **neglected contributions – negligible** (smaller than 1/mille)

Particular toy model [SO, 2010]

- interesting case – **model with 2 Pomerons**:
 - 'soft' Pomeron: smaller $\alpha_{\mathbb{P}\text{soft}}$, larger $\alpha'_{\mathbb{P}\text{soft}}$
 - 'hard' Pomeron: larger $\alpha_{\mathbb{P}\text{hard}}$, smaller $\alpha'_{\mathbb{P}\text{hard}}$

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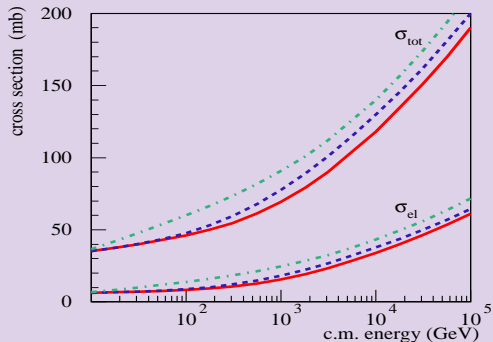
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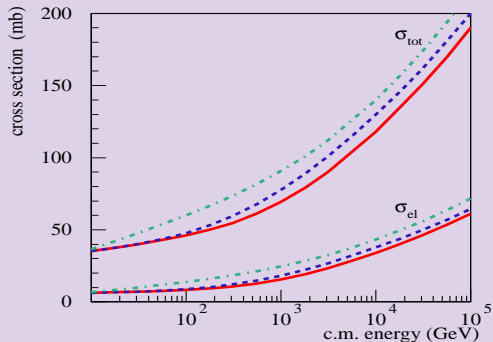
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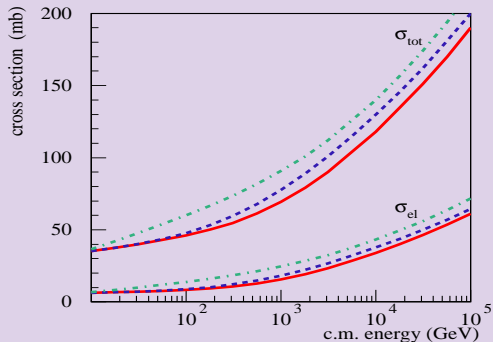
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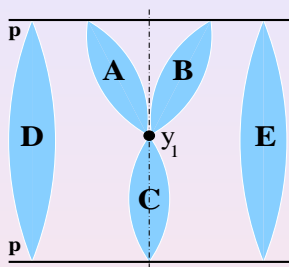


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- NB: relative contribution of \mathbb{P} -loops strongly depends on $\alpha'_{\mathbb{P}}$
 - simplest loop contribution $\propto G_{3\mathbb{P}}^2/\alpha'_{\mathbb{P}}$
 - $\Rightarrow \rightarrow \infty$ for $\alpha'_{\mathbb{P}} \rightarrow 0$ (assuming the slope for the $3\mathbb{P}$ -vertex $\simeq 0$)
- in the above example, $\alpha'_{\mathbb{P}\text{soft}} = 0.14 \text{ GeV}^{-2}$ was used

σ_{SD} & non-eikonal rap-gap suppression

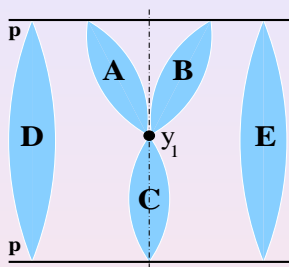
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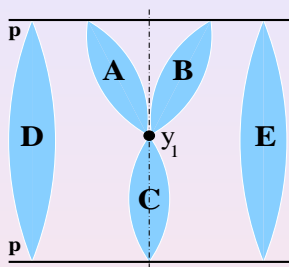
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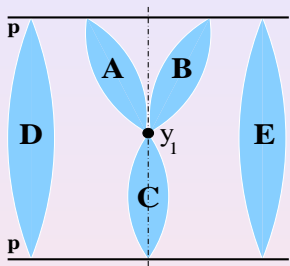
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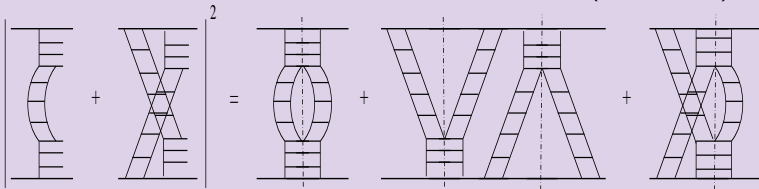
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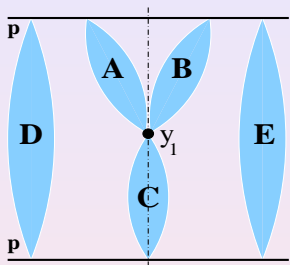
NB: generally, also multiple exchanges of the ABC subgraph

- e.g. **required by s -channel unitarity for DD** (at small b)



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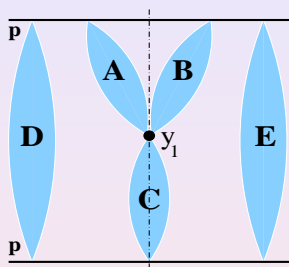
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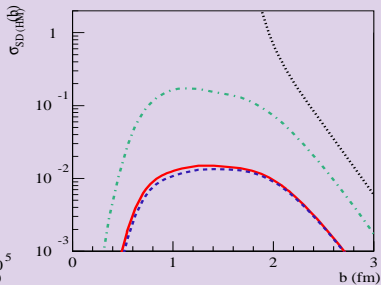
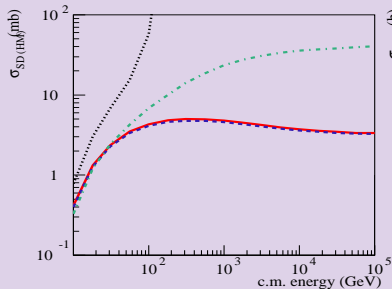


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Impact on σ_{SD} (high mass) & diffraction profile at 14 TeV c.m.



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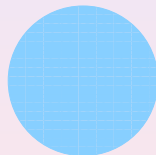
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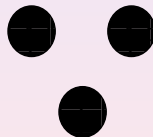
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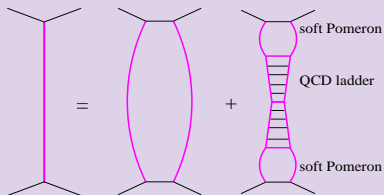
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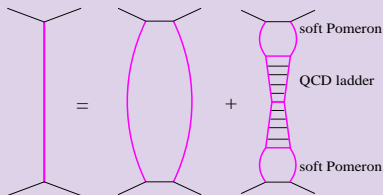
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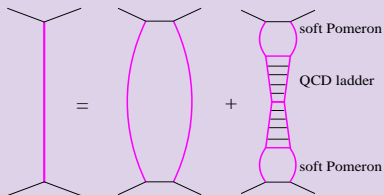
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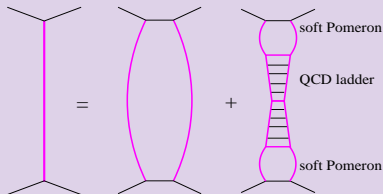
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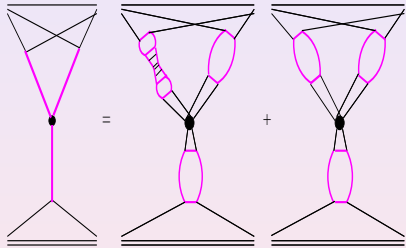


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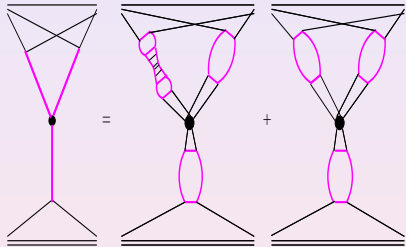
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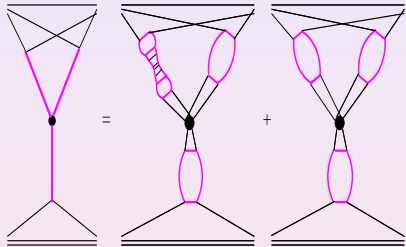
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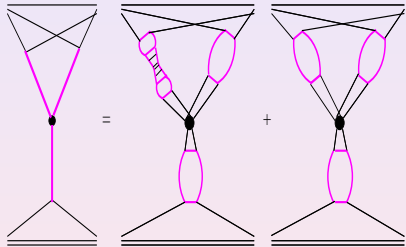
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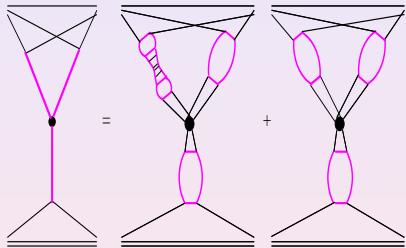
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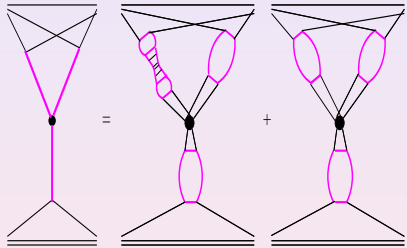
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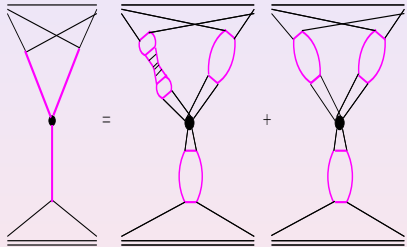
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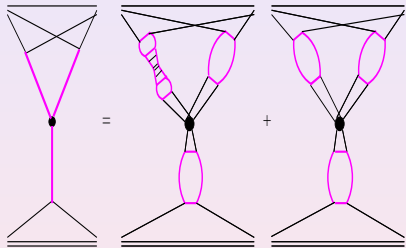
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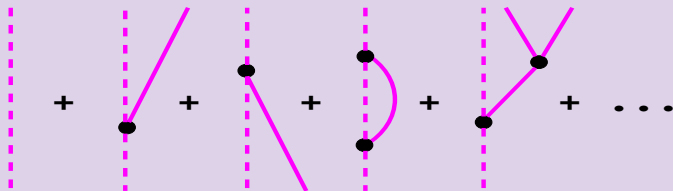


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Generation of final states

- based on the structure of cut diagrams (positive-definite partial cross sections)
- e.g. diagrams for a single scattering process
 - dashed thick line = 'cut' Pomeron = real parton cascade
 - thick solid lines = uncut Pomerons = virtual parton cascades (elastic re-scattering of intermediate partons)

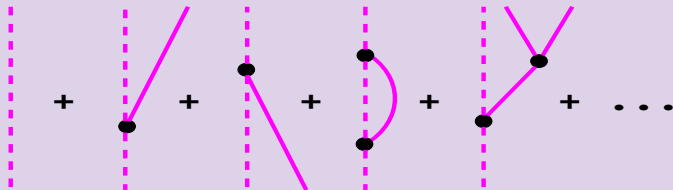


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 - thick solid lines = uncut Pomerons = virtual parton cascades (elastic re-scattering of intermediate partons)

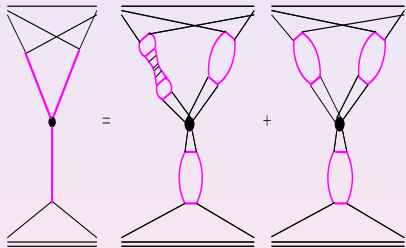


Treatment of nonlinear processes: assumptions

- basic assumption: multi- \mathbb{P} vertices – due to soft ($|q^2| < Q_0^2$) parton processes
- based on soft Pomeron coupling
- vertex for $m\mathbb{P} \rightarrow n\mathbb{P}$:

$$G^{(m,n)} = G_{3\mathbb{P}} \gamma_{\mathbb{P}}^{m+n-3}$$
- in dense limit (large s , small b) 'renormalized' soft Pomeron
[Kaidalov et al., 1986]:

$$\alpha_{\mathbb{P}\text{soft}}^{\text{ren}} = \alpha_{\mathbb{P}\text{soft}} - G_{3\mathbb{P}}/\gamma_{\mathbb{P}}$$
- choose $G_{3\mathbb{P}}/\gamma_{\mathbb{P}} > \alpha_{\mathbb{P}\text{soft}} - 1$



• \Rightarrow undercritical soft \mathbb{P} ($\Lambda_{\mathbb{P}} = \alpha_{\mathbb{P}\text{soft}}^{\text{ren}} - 1 < 0$) in dense limit
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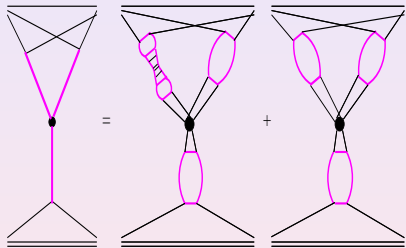
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'renormalized' soft Pomeron

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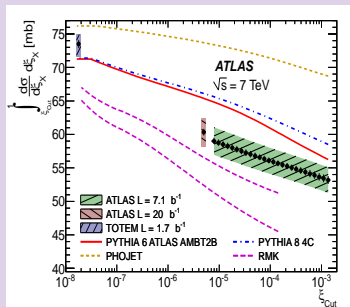
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- NB: M_X^2 -distribution for HMD – **strongly modified by absorptive effects** [SO, 2011]

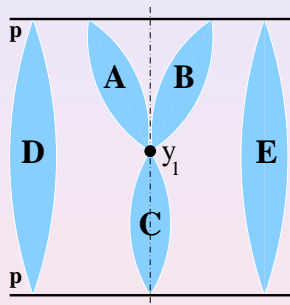
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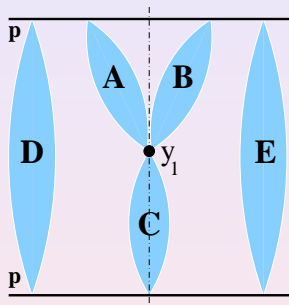


M_X^2 -distribution for single high mass diffraction



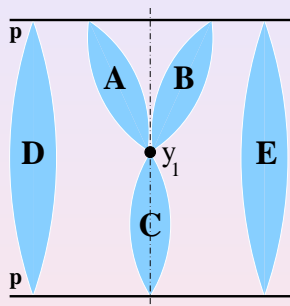
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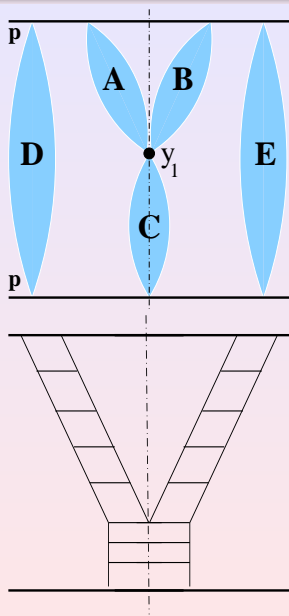
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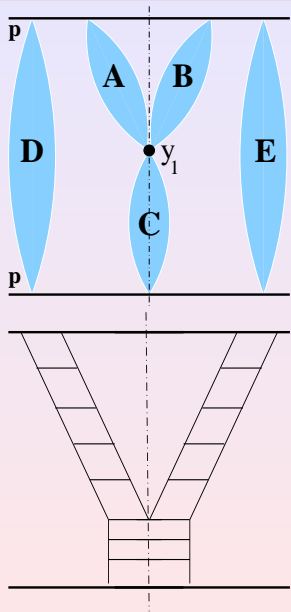
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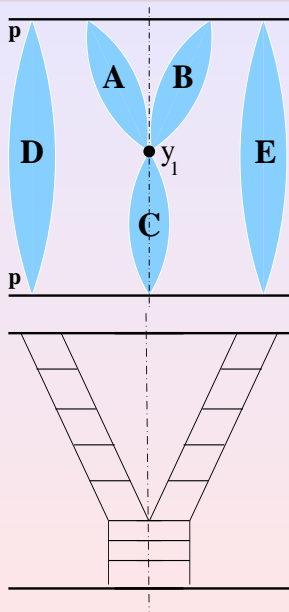
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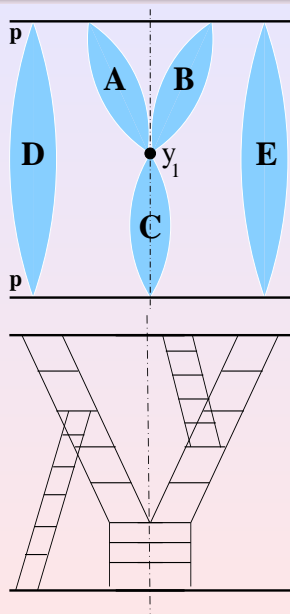
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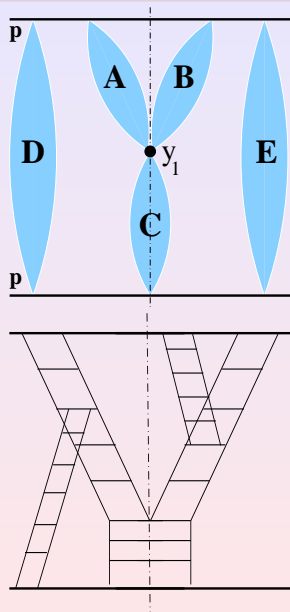
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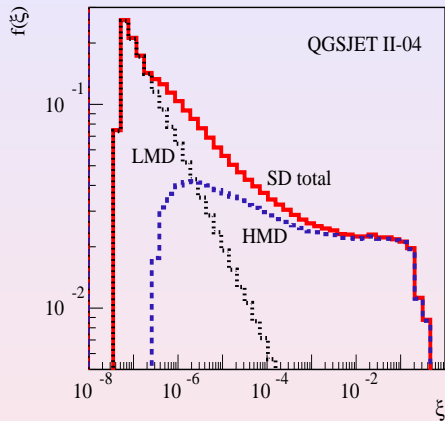
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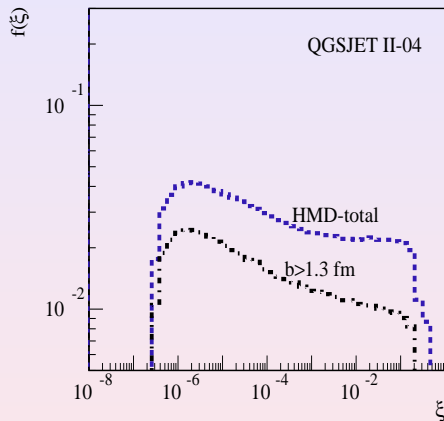
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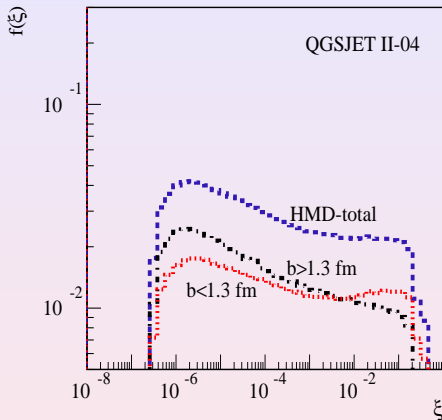
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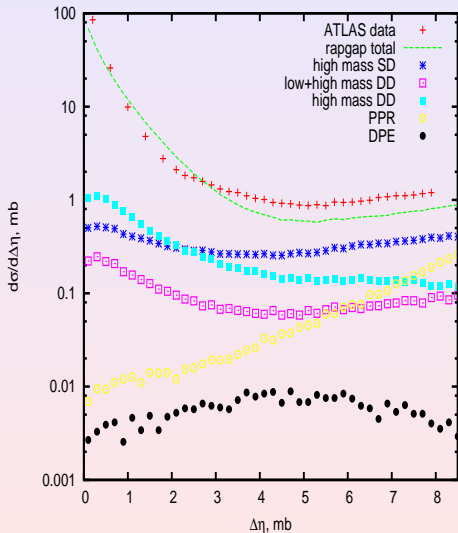
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Diffraction at LHC

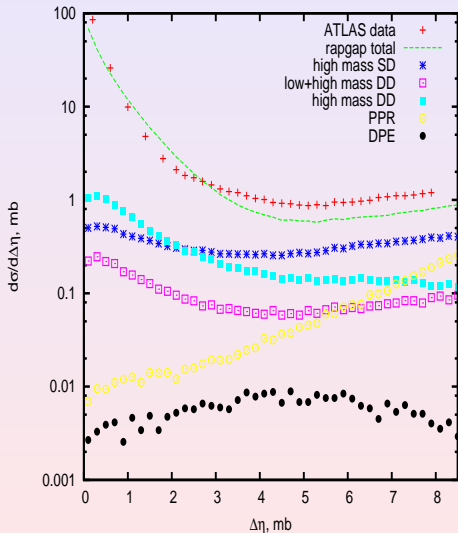
- forward rap-gap (η_F) distribution: QGSJET-II-04 wrt ATLAS



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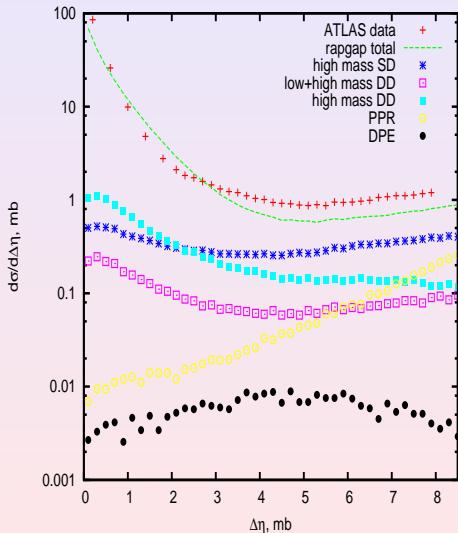
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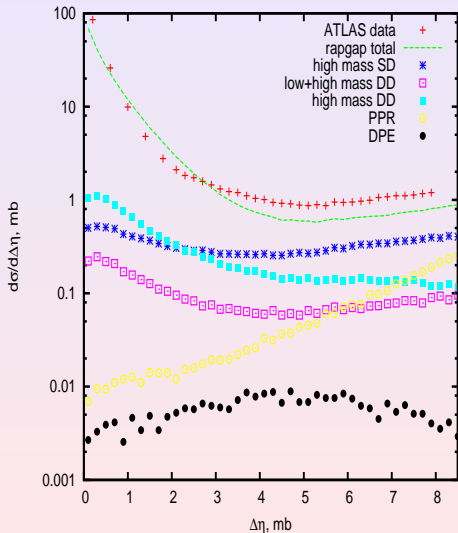
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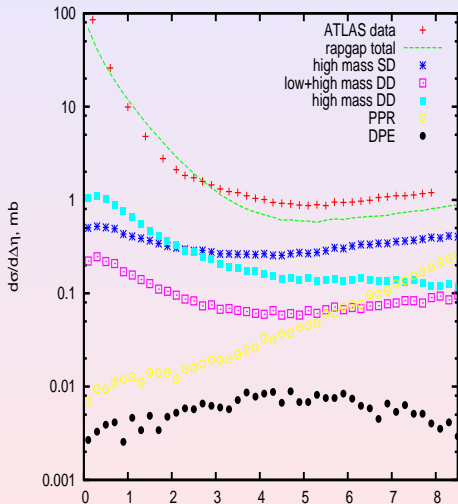
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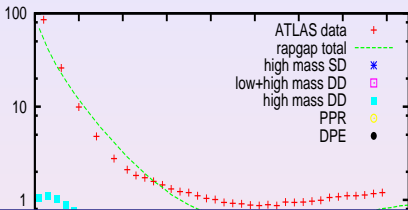


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But: the model misses $\sim 30\%$ of HMD seen by ATLAS!

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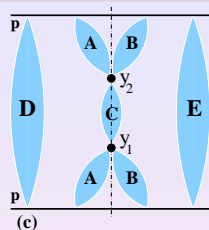
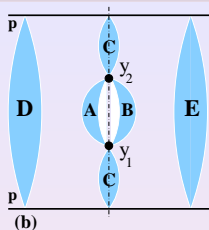
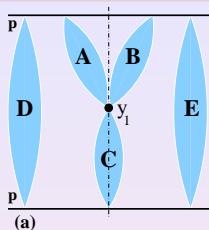
- overall η_F -dependence:

Comparison to preliminary TOTEM results for SD

| M_X , GeV | 3.4 – 7 | 7 – 350 | 350 – 1100 |
|-------------|----------------------------|-------------------------------|----------------------------|
| ξ_X | $(2.4 - 10) \cdot 10^{-7}$ | $10^{-6} - 2.5 \cdot 10^{-3}$ | $(2.5 - 25) \cdot 10^{-3}$ |
| TOTEM | 1.8 | 3.3 | 1.4 |
| model | 2.3 | 4.8 | 1.6 |
| model/data | 1.3 | 1.5 | 1.2 |

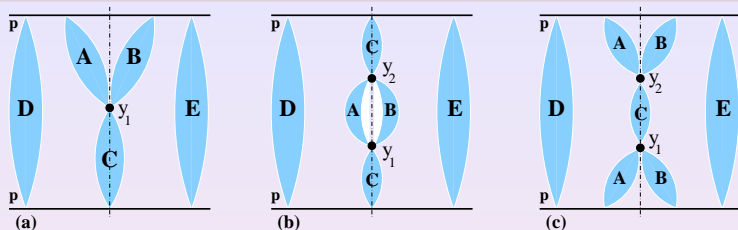
- overall trend – similar
- but: rate in variance with ATLAS

SD, DD, CD: b -profiles



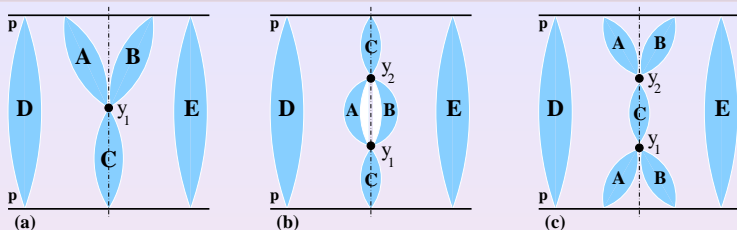
- DD contribution (b) – comparable to SD (a)
 - at lowest order: Pomeron 'loop'
 - $\sim G_{3\mathbb{P}}^2/\alpha'_{\mathbb{P}} \sim G_{3\mathbb{P}}$
 - involves only 2 Pomerons coupled to proj. & target
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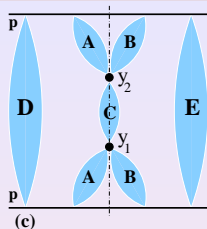
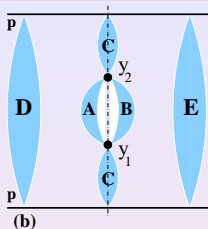
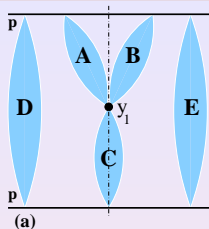
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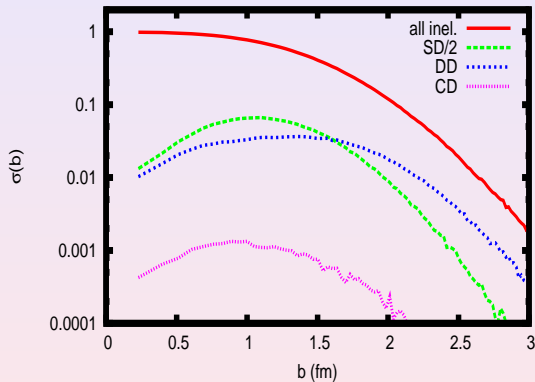
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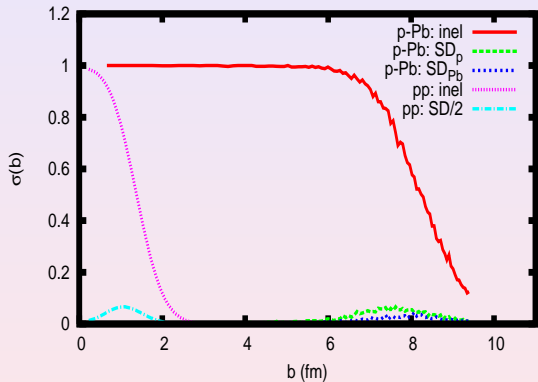
Example: b profiles for pp at $\sqrt{s} = 5$ TeV:



- σ_{SD} : $\sim 15\%$ of σ_{inel}
- σ_{DD} : $\sim 7\%$
- σ_{CD} : $\sim 0.1\%$

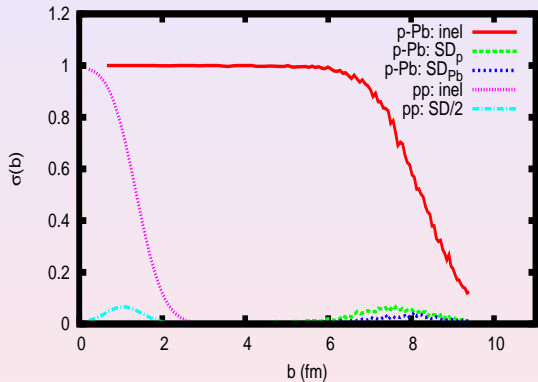
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Cf.: b profiles for $p - Pb$ at $\sqrt{s} = 5$ TeV:



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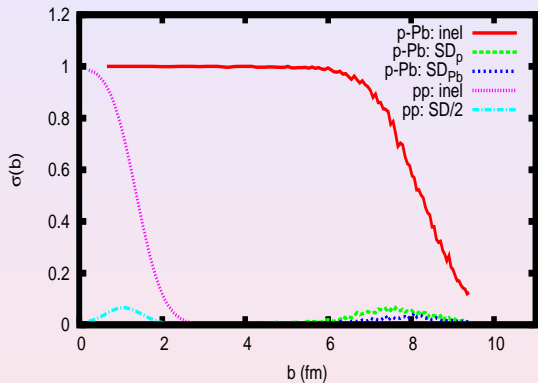
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Diffraction on nuclear target – comparable to the pp case

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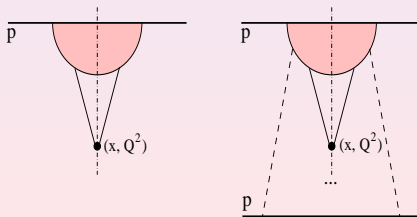
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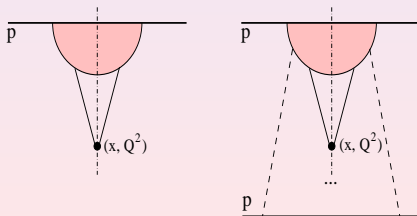
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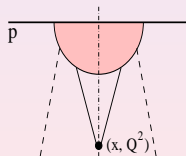
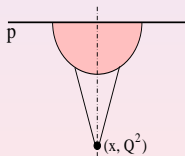
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 - what is different in pp compared to DIS?

- in DIS: rescattering of intermediate partons off the parent hadron



- in pp : rescattering off the

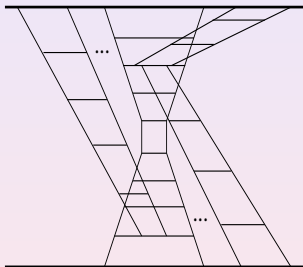
non-inclusive observables can't be described with universal PDFs
(additional screening corrections are process-dependent)

From SFs to σ_{pp}^{tot} : nonfactorizable contributions

- How strong is the effect?

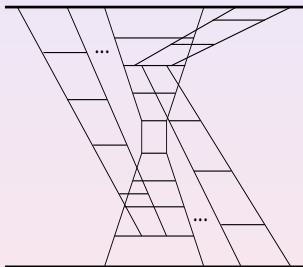
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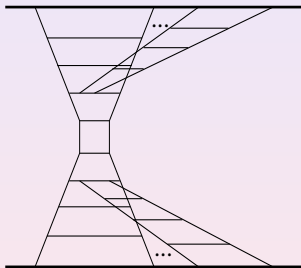
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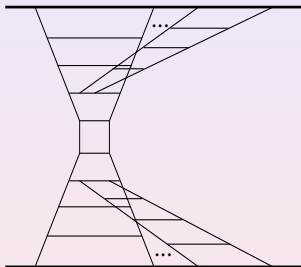
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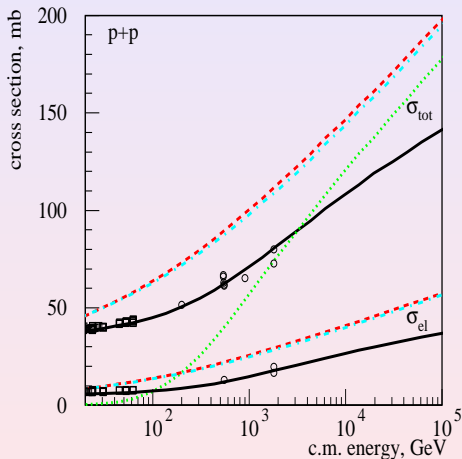
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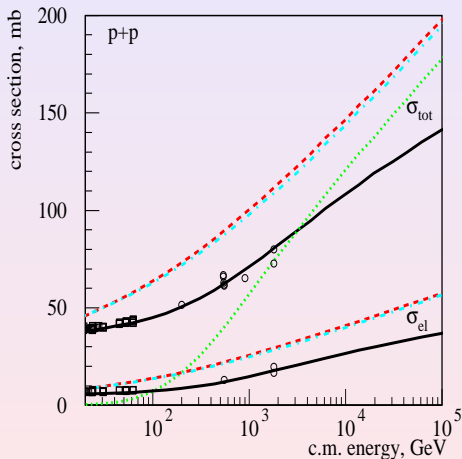
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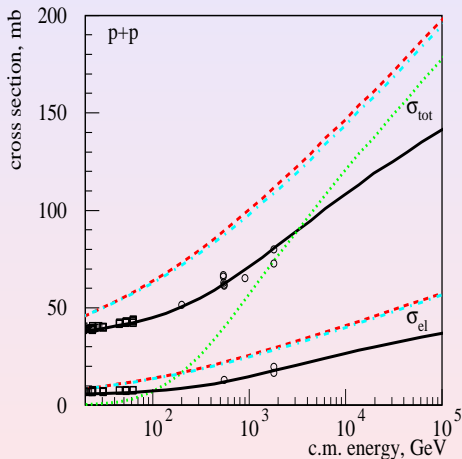
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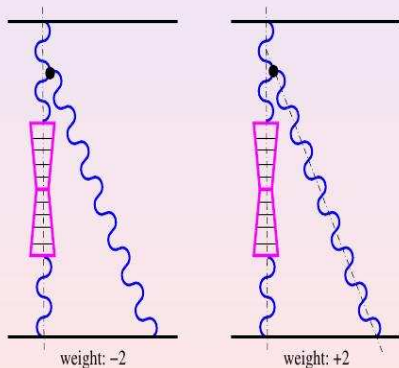
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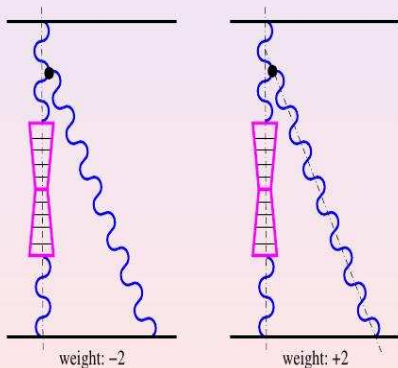
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- corrections to single hard process **due to soft rescattering**
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- equal weights \Rightarrow zero effect for inclusive spectra & σ_{pp}^{tot} ('soft' can't screen 'hard'!)



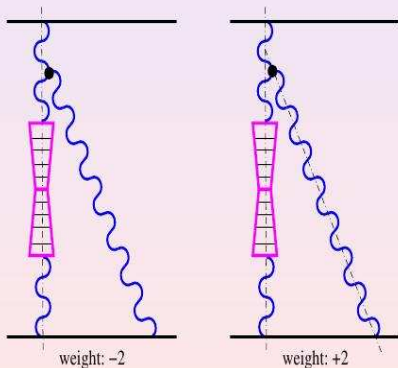
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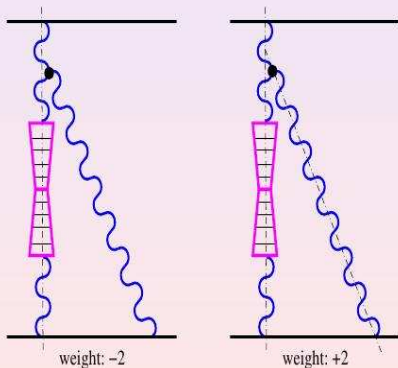
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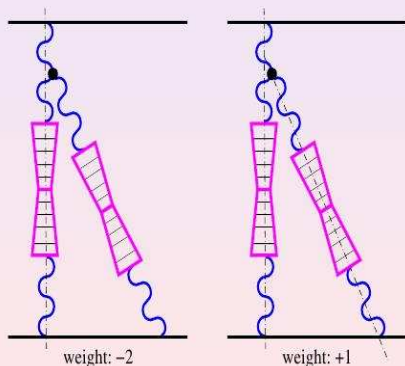
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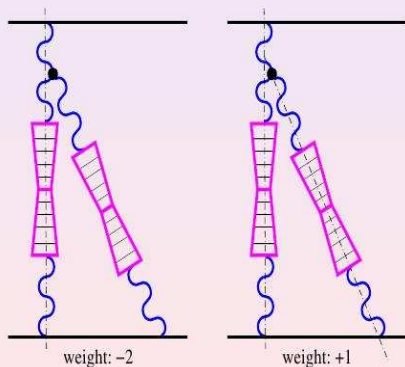
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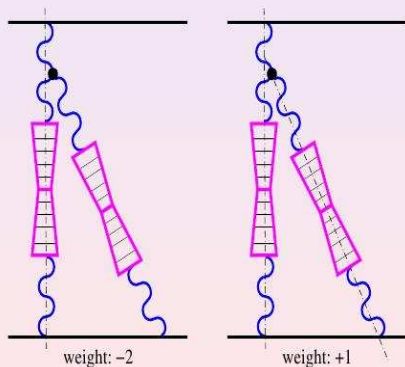
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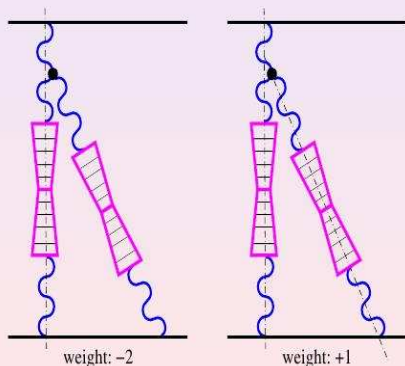
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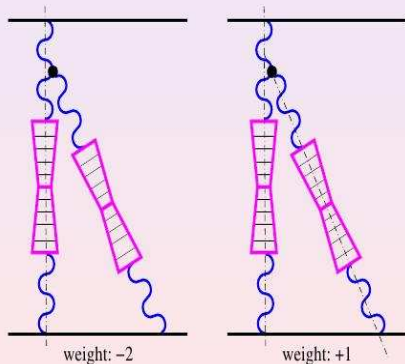
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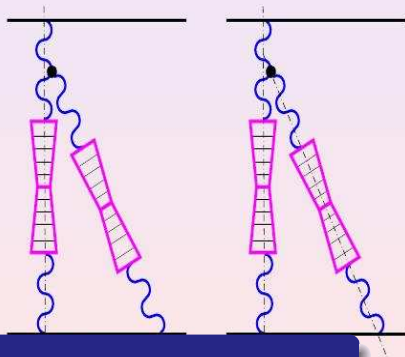


additional screening caused by multi-parton correlations

- two hard parton cascades **originate from the same soft parent**

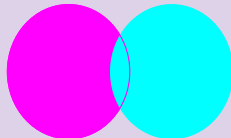
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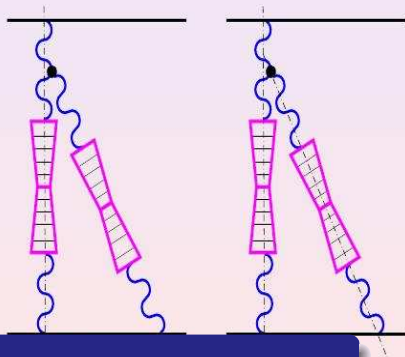
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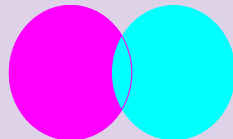
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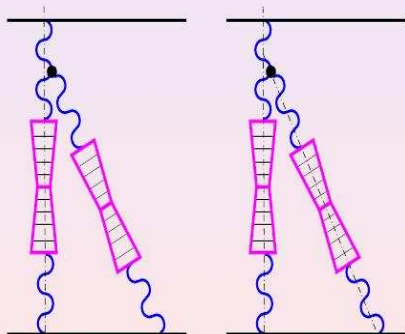
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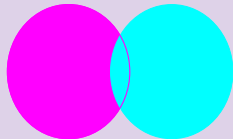
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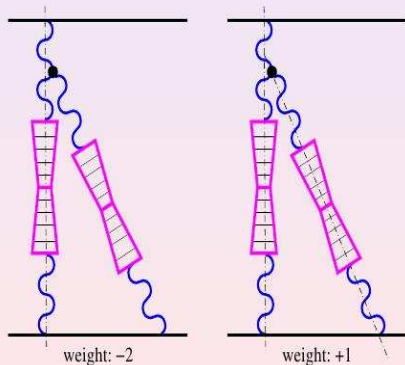
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⇒ multi-parton interactions provide a key to understand σ_{pp}^{tot}
(and vice versa)

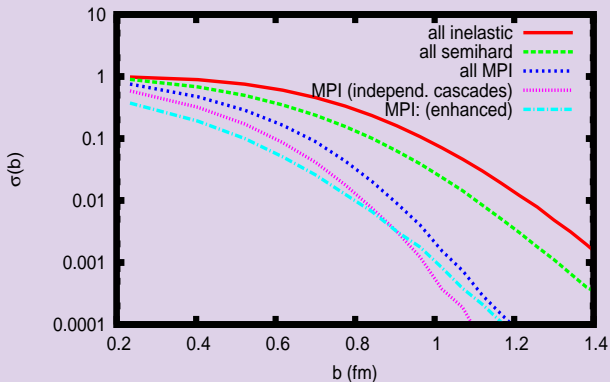
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Illustration: b -profiles for MPI for pp at 14 TeV c.m. (QGSJET-II)

- NB: more stringent limits on Q_0 from N_{ch} data

- $\Rightarrow Q_0^2 = 3 \text{ GeV}^2$ used
- \Rightarrow factor of 10 weaker effect here



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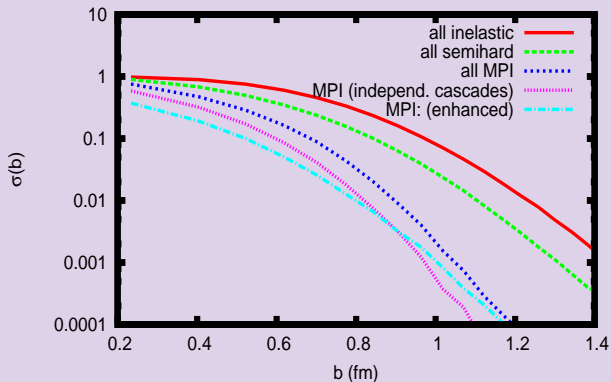
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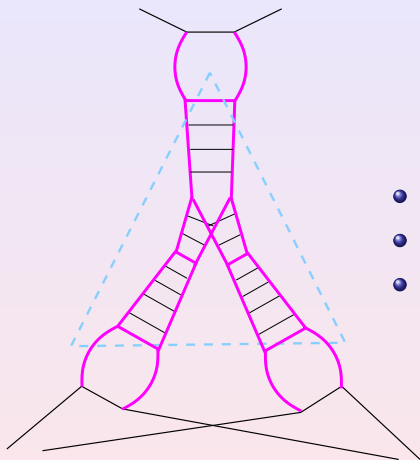
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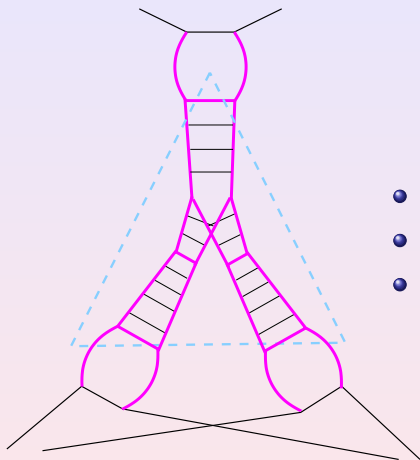
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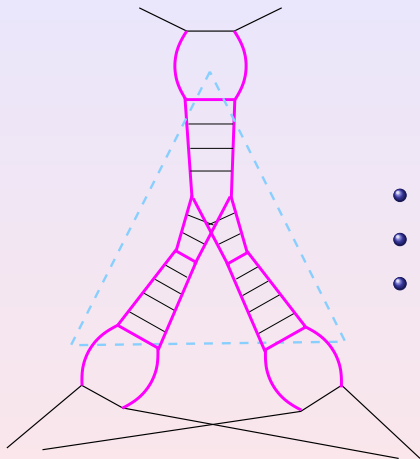
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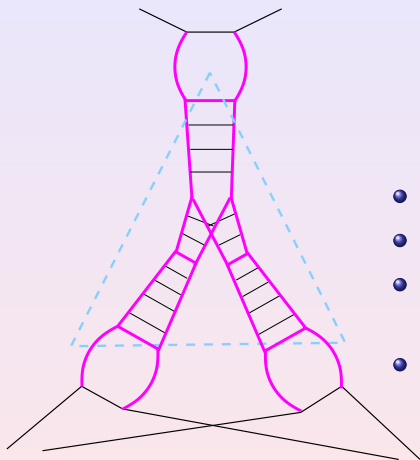
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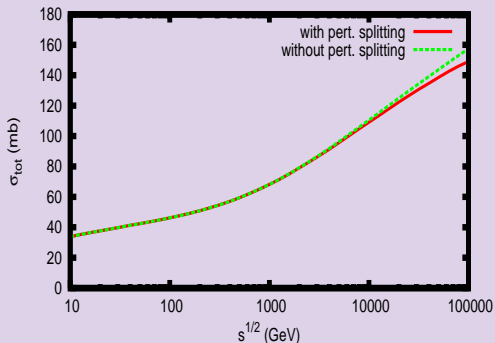
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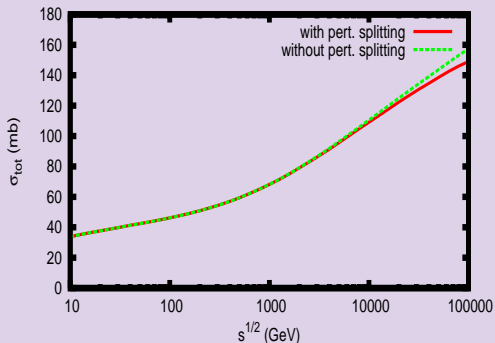


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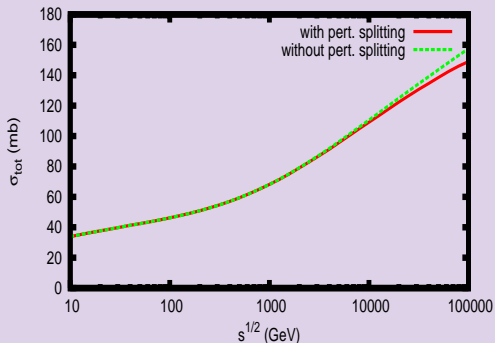


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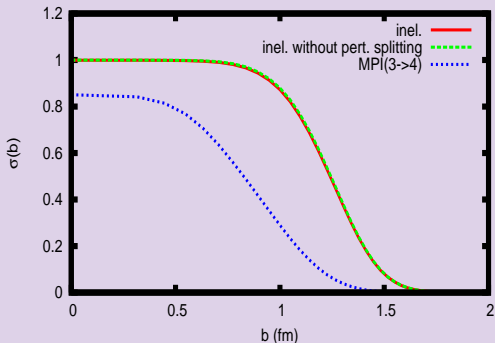


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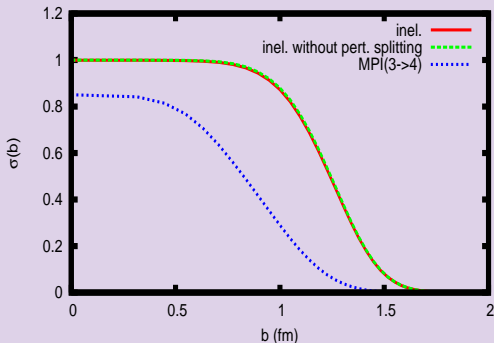


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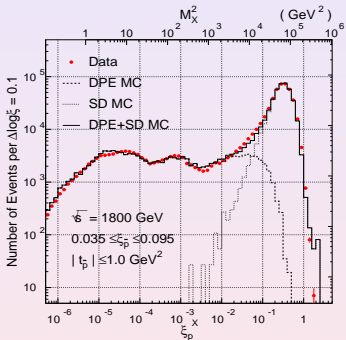


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Backup

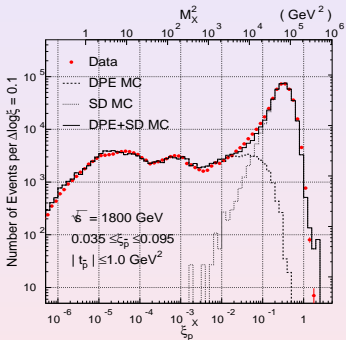
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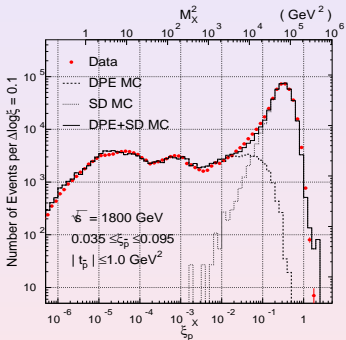
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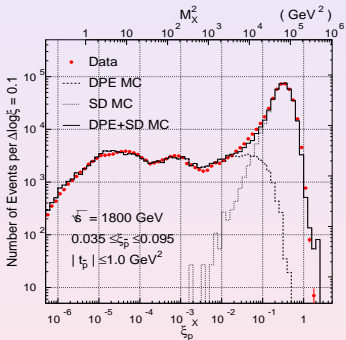
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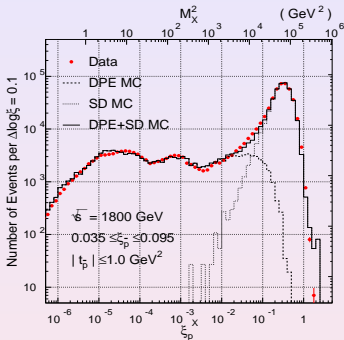
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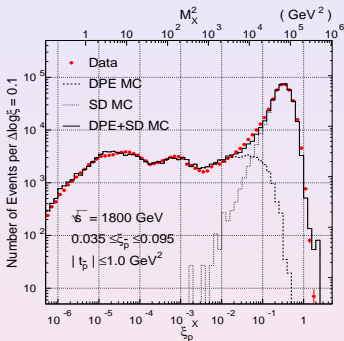
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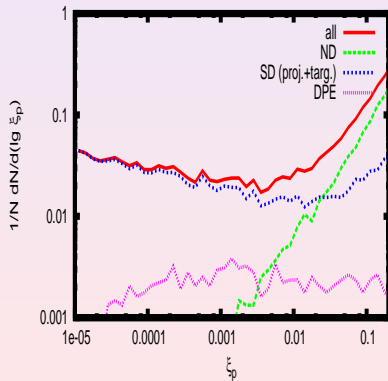
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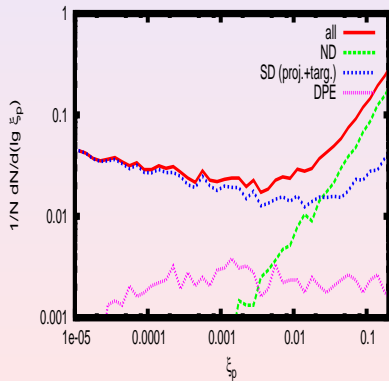
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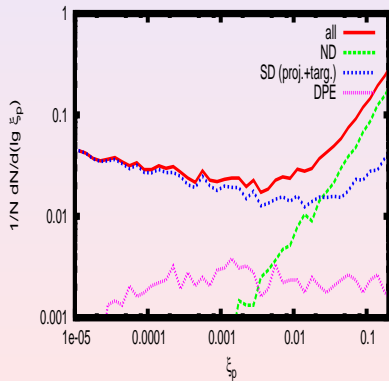


- similar fraction of events with $\xi_p < 0.02$ obtained ($\simeq 0.2$)

Double Pomeron exchange (DPE) & CDF data

Caveat: the small rap-gap ($y_{\text{gap}} = \ln \xi_{\bar{p}} \simeq 2 \div 3$) may be formed by fluctuations in particle production

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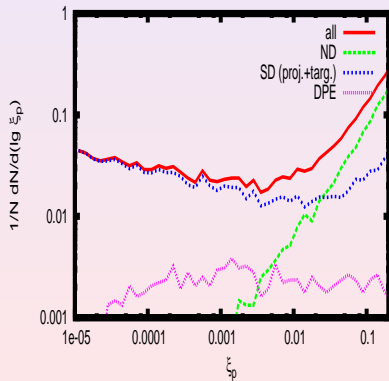


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- but: **dominated by SD** (p & \bar{p} contributions)

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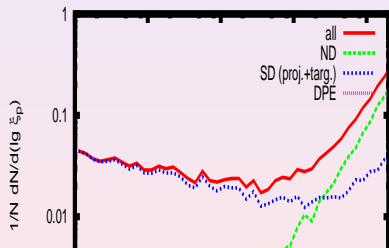


- similar fraction of events with $\xi_p < 0.02$ obtained ($\simeq 0.2$)
- but: dominated by SD (p & \bar{p} contributions)
- **DPE: only $\sim 10\%$ contribution at $\xi_p < 0.02$**

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Caveat: the small rap-gap ($y_{\text{gap}} = \ln \xi_{\bar{p}} \simeq 2 \div 3$) may be formed by fluctuations in particle production

- check with QGSJET-II simulation: all events with $0.035 < \xi_{\bar{p}} < 0.095$ (exp. triggers NOT implemented)



- similar fraction of events with $\xi_p < 0.02$ obtained ($\simeq 0.2$)
- but: dominated by SD

Bottom line:

- **accurate studies of t -dependence necessary** for a reliable determination of DPE cross section