# A partonic description of "soft" interactions at the LHC



Alexei Kaidalov (1940 – 2010) Alan Martin (IPPP, Durham) International Workshop on Particle Phys.Phenomenology in memory of Alexei Kaidalov Moscow, 21-25 July 2013 Aliosha made many pioneering contributions to the understanding of diffractive processes in high-energy hadron interactions:

He was the first to evaluate the effects low mass (N\*) diffractive dissociation (1971)

Kaidalov et al. performed the first triple-Regge analysis (1973) Pioneering model for soft high-energy hadron interactions

A.B. Kaidalov, L.A. Ponomarev, K.A. Ter-Martirosyan

Sov. J. Nucl. Phys. 44 (1986)

included multi-Pomeron diagrams in global description, for first time, with vertices

$$g(nP \rightarrow mP) = g_N \lambda^{n+m-2}$$



Basis of models of soft interactions, used to this day: Durham model (Khoze-Martin-Ryskin) Tel-Aviv model (Gotsman-Levin-Maor) Ostapchenko M. Poghosyan, A.B. Kaidalov 2007-2010 (ALICE coll<sup>bn</sup>)

# No unique definition of diffraction

- Diffraction is elastic (or quasi-elastic) scattering caused, via s-channel unitarity, by the absorption of components of the wave functions of the incoming particles
  - e.g. pp→pp,

 $pp \rightarrow pX$  (single proton dissociation, SD),  $pp \rightarrow XX$  (both protons dissociate, DD)

Good for quasi-elastic proc.

– but not high-mass dissoc<sup>n</sup>





quantum no. of p

2. A diffractive process is characterized by a large rapidity gap (LRG), which is caused by t-channel "Pomeron" exch. (or, to be more precise, by the exchange corresponding to the rightmost singularity in the complex angular momentum plane with vacuum quantum numbers).
Only good for very LRG events – otherwise Reggeon/fluctuation contaminations





Can we describe all "soft" HE data

 $\sigma_{tot}$ ,  $d\sigma_{el}/dt$ ,  $\sigma_{low M}$ , (+  $\sigma_{high M}$ ) from CERN-ISR  $\rightarrow$  Tevatron  $\rightarrow$  LHC in terms of a single "effective" pomeron ?

Low-mass dissociation is a consequence of the internal for the internal for the structure of proton. A constituent can scatter & destroy coherence of |p>

Good-Walker:  $|p\rangle = \sum a_i |\phi_i\rangle$ 

where  $\phi_i$  diagonalize T -- have only "elastic-type" scatt

Usually GW eigenstates assumed independent of t & s KMR (2013) parametrize form factor  $F_i(t)$  for each  $\phi_{i=1,2}$ 

• Allows for  $B_{el} \sim 10 \text{ GeV}^{-2}$  at CERN-ISR  $diff^{ve} dip diff^{ve} dip$  $B_{el} \sim 20 \text{ GeV}^{-2}$  at LHC (7 TeV)

 $\rightarrow$  smaller |t| at LHC, |p> less distorted, so  $\sigma_{low M}$  smaller

model 1

Pomeron is a (BFKL) cut, not a pole
Iow k<sub>t</sub> Image in the probability is a pole
Iow k<sub>t</sub> Image intermediate parton in log k<sub>t</sub>
abs. corr<sup>ns</sup> between intermediate parton-parton inter<sup>ns</sup>  $\sigma_{abs} \sim 1/k_t^2$ , suppress low k<sub>t</sub>  $\rightarrow$  mean k<sub>t</sub> increases with s  $k_{min}^2 \sim s^{0.12}$ Image intermediate parton inter<sup>ns</sup>

(enhanced multi-pom effects introduce dynamical infrared cutoff)

Elastic amp. 
$$T_{el}(s,b)$$
  

$$Im T_{el} = \prod_{k=1}^{\infty} = 1 - e^{-\Omega/2} = \sum_{n=1}^{\infty} \prod_{k=1}^{\infty} \frac{\Omega/2}{(s-ch unitarity)}$$
Low-mass diffractive dissociation  $\prod_{k=1}^{p^*} \rightarrow$  multichannel eikonal introduce diff<sup>ve</sup> estates  $\phi_i, \phi_k$  (comb<sup>ns</sup> of p,p<sup>\*</sup>,...) which only undergo "elastic" scattering (Good-Walker)  

$$Im T_{ik} = \prod_{k=1}^{i} = 1 - e^{-\Omega_{ik}/2} = \sum_{k=1}^{\infty} \prod_{k=1}^{\infty} \frac{\Omega_{ik}}{2}$$

Т



reggeon at ISR $\rightarrow$ 1mb?)







but screening even more important

Elastic amp.  $T_{el}(s,b)$ 

 $\Omega$ 

bare amp.  $\Omega/2 =$ 

(SD -80%)

Im 
$$T_{\rm el} = \underbrace{1 - e^{-\Omega/2}}_{\text{(s-ch unitarity)}} = \sum_{n=1}^{\infty} \underbrace{1 \cdots \Omega/2}_{p^*}$$
 (-20%)  
Low-mass diffractive dissociation

introduce diff<sup>ve</sup> estates  $\phi_i$ ,  $\phi_k$  (comb<sup>ns</sup> of p,p<sup>\*</sup>,..) which only undergo "elastic" scattering (Good-Walker)

Im 
$$T_{ik} = \prod_{k=1}^{i} = 1 - e^{-\Omega_{ik}/2} = \sum \prod_{k=1}^{i} \dots \Omega_{ik}/2$$
 (-40%)

include high-mass diffractive dissociation

$$_{ik} = \underbrace{\longrightarrow}_{k}^{i} + \underbrace{\bigvee}_{k}^{i} M + \underbrace{\bigvee}_{k}^{i} + \cdots + \underbrace{\bigvee}_{k}^{i} + \cdots$$





Yes, it is possible to describe all "soft" HE data  $\sigma_{tot}$ ,  $d\sigma_{el}/dt$ ,  $\sigma_{low M}$ , (+  $\sigma_{high M}$ ) from CERN-ISR  $\rightarrow$  Tevatron  $\rightarrow$  LHC in terms of a single "effective" pomeron ?

Energy dep. of  $\sigma_{el}$ ,  $\sigma_{tot}$  controlled by intercept and slope of "effective" pomeron trajectory

Diffractive dip and  $\sigma_{\text{low M}}$  controlled by properties of GW eigenstates

High-mass diss<sup>n</sup> driven by multi-pomeron effects

# Can we go further and consider

## a partonic model of the pomeron?

## Could this be the basis of a Monte Carlo

which describes "soft" (as well as "hard")

high energy pp interactions ?

High-energy pp interactions

soft



Reggeon Field Theory with phenomenological soft Pomeron



pQCD partonic approach

smooth transition using QCD / "BFKL" / hard Pomeron

There exists only one Pomeron, which makes a smooth transition from the hard to the soft regime

Can this be the basis of a unified partonic model for both soft and hard interactions ??

"Soft" and "Hard" Pomerons?

A vacuum-exchange object drives soft HE interactions. Not a simple pole, but an enigmatic non-local object. Rising  $\sigma_{tot}$  means multi-Pom diags (with Regge cuts) are necessary to restore unitarity.  $\sigma_{tot}$ ,  $d\sigma_{el}/dt$  data, described, in a limited energy range, by eff. pole  $\alpha_{P}^{eff} = 1.08 + 0.25t$ 

Sum of ladders of Reggeized gluons with, in LLx BFKL, a singularity which is a cut and not a pole. When HO are included the intercept of the BFKL/hard Pomeron is  $\alpha_P^{\text{bare}}(0) \sim 1.3$ 

 $\Delta = \alpha_{P}(0) - 1 \sim 0.3$ 

 $\alpha_{P}^{\text{bare}} \sim 1.3 + 0 \text{ t}$ 

 $\alpha_{P}^{eff} \sim 1.08 + 0.25 t$ up to Tevatron energies

 $(\sigma_{tot} \sim S^{\Delta})$ 

with absorptive (multi-Pomeron) effects Aside: absorption needed at LHC

 $ds_{el}/dt \sim |ImT_{el}(s,t)|^2$  (r=|Re/Im|<<1)

so can get impact parameter profile  $ImT_{el}(s,b)$ , via a Fourier transform  $q \rightarrow b$  space (t=q<sup>2</sup>), "direct" from data for elastic diff. x-sect:

$$\operatorname{Im} T_{\text{el}}(b) = \int \sqrt{\frac{d\sigma_{\text{el}}}{dt}} \frac{16\pi}{1+\rho^2} J_0(qb) \frac{qdq}{2\pi}$$

$$\uparrow$$

$$\operatorname{data}$$



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 $\Delta = \alpha_{\mathsf{P}}(0)$ - 1



Small-size "BFKL" Pomeron is natural object to continue from "hard" to "soft" domain



Phenomeno<sup>logical</sup> hints that R<sub>bare Pom</sub> << R<sub>proton</sub>

small slope  $\alpha'_{bare} \sim 0$ success of Additive QM small size of triple-Pomeron vertex small size of BEC at low N<sub>ch</sub>

Pomeron is a parton cascade which develops in ln(1/x) space, and which is not strongly ordered in  $k_t$ .



However, above evidence indicates

the cascade is compact in b space and so the parton  $k_t$ 's are not too low. We may regard the cascade as a hot spot inside the two colliding protons

eikonal: Pomerons well separated in b-plane



enhanced: interactions with partons in an individual cascade



despite  $g_{3P} \sim 0.2 g_N$ , enhanced by phase space, which grows with s

 $\rightarrow$  see next slide



 $\leftarrow$  why is  $\lambda$  sufficiently large, that enh.  $g_{3P} = \lambda g_N \qquad \lambda \sim 0.2$  multi-Pom diagrams important at HE ?

naïve argument without absorptive effects:



so at HE collider energies  $\sigma_{SD(high mass)} \sim \sigma_{el}$ SD is "enhanced" by larger phase space available at HE.

Partonic structure of "bare" Pomeron

BFKL evol<sup>n</sup> in rapidity generates ladder

$$\frac{\partial \Omega(y,k_t)}{\partial y} = \bar{\alpha}_s \int d^2 k'_t \ K(k_t,k'_t) \ \Omega(y,k'_t)$$

• At each step  $k_t$  and b of parton can be be changed – so, in principle, we have 3-variable integro-diff. eq. to solve Khoze, Martin, Ryskin



- Inclusion of k<sub>t</sub> crucial to match soft and hard domains.
   Moreover, embodies less screening for larger k<sub>t</sub> comp<sup>ts</sup>.
- We use a simplified form of the kernel K with the main features of BFKL diffusion in log  $k_t^2$ ,  $\Delta = \alpha_P(0) 1 \sim 0.3$
- b dependence during the evolution is prop' to the Pomeron slope α', which is v.small (α'<0.05 GeV<sup>-2</sup>) -- so ignore.
   Only b dependence comes from the starting evol<sup>n</sup> distrib<sup>n</sup>

Evolution gives

$$\Omega = \Omega_{ik}(y, k_t, b)$$

#### How are Multi-Pomeron contrib<sup>ns</sup> included?

Now include rescatt of intermediate partons with the "beam" i and "target" k (KMR)

evolve up from y=0

$$\frac{\partial \Omega_k(y)}{\partial y} = \bar{\alpha}_s \int d^2 k'_t \exp(-\lambda(\Omega_k(y) + \Omega_i(y'))/2) K(k_t, k'_t) \Omega_k(y)$$
  
evolve down from y'=Y-y=0  
$$\frac{\partial \Omega_i(y')}{\partial y'} = \bar{\alpha}_s \int d^2 k'_t \exp(-\lambda(\Omega_i(y') + \Omega_k(y))/2) K(k_t, k'_t) \Omega_i(y')$$

where  $\lambda \Omega_{i,k}$  reflects the different opacity of protons felt by intermediate parton, rather the proton-proton opacity  $\Omega_{i,k} = \lambda \sim 0.2$ 

#### solve iteratively for $\Omega_{ik}(y,k_t,b)$ inclusion of $k_t$ crucial

Note: data prefer  $exp(-\lambda\Omega) \rightarrow [1 - exp(-\lambda\Omega)] / \lambda\Omega$ Form is consistent with generalisation of AGK cutting rules In principle, knowledge of  $\Omega_{ik}(y,k_t,b)$  (and hadronization) allows the description of all soft, semi-hard pp high-energy data:  $\sigma_{tot}$ ,  $d\sigma_{el}/dt$ ,  $d\sigma_{SD}/dtdM^2$ , DD, DPE... LRG survival factors S<sup>2</sup> (to both eikonal, enhanced rescatt) PDFs and diffractive PDFs at low x and low scales

Indeed, such a model can describe the main features of all the data, in a semi-quantitative way, with just a few physically motivated parameters. (KMR, EPJ C71)

early work on survival factors  $\rightarrow$ 

#### Kaidalov + KMR Durham (2001)



Paper also discussed possible  $\beta$  dependence, and emphasized enhanced rescatt. effects

E<sub>T</sub><sup>Jet1,2</sup> > 7 GeV 0.035 < ξ < 0.095 | t | < 1.0 GeV<sup>2</sup> (b) DGLAP-based MC



Existing all-purpose MCs describe inclusive spectra with hard parton-parton interaction in central region, with secondaries from backward evol<sup>n</sup>.

Infrared cutoff  $k_{min}$ ~3 GeV at LHC(7 TeV) compared to cutoff  $k_{min}$ ~2.15 GeV at Tevatron.

Understood in pQCD: in relevant low x region, prob of rescatt. large, corresponding  $abs^{ve} corr^n$ ,  $\sigma_{abs} \sim 1/k_t^2$ , suppress low  $k_t$ .

model  $\rightarrow$  d $\sigma$ /dy ~ s<sup>0.2</sup> like the LHC data for 0.9 to 7 TeV



# Can conclude from the LHC data:

The  $<p_T>$  of hadrons measured by ATLAS, CMS, ALICE is smaller than that expected from the **DGLAP-based** MC's (which have strong-ordering in  $k_T$  going from the protons to the central region).

After tuning the MC's to lower energy data, find smaller  $<p_T>$  and larger particle density dN/dy at LHC.

This indicates the need for a **BFKL-based** MC (with multi-Pomeron absorptive corrections), where we have diffusion in log  $k_T$  and a growth of particle density as we go to large initial energy, that is smaller x.

Ostapchenko (based on Kaidalov and co-workers) Lund dipole cascade model (Flensburg,Gustafson,Lonnblad) SHRiMPS (SHERPA) based on KMR model Existing "all purpose" (DGLAP) Monte Carlos split eikonal

$$\Omega(s,b) = \Omega_{soft} + \Omega_{hard(pQCD)}$$

Seek MC that describes all aspects of minimum bias -- total, differential elastic Xsections, diffraction, jet prod... in a unified framework; capable of modelling exclusive final states.

SHERPA Monte Carlo based on KMR framework

"SHRIMPS" MC = Soft-Hard Reactions involving Multi-Pomeron Scatt.

Krauss, Hoeth, Zapp et al

# OUTLINE of SHRiMPS:

Solve coupled evol eqs. in y to generate  $\Omega(y,k_t,b)$ , specifying boundary conditions of GW eigenstates. Eigenstates give elastic, quasi-elastic scatt.

Select no. of ladders exchanged (according to Poisson distribution with parameter  $\Omega_{ik}(b)$ ) to simulate inelastic state

Incoming protons dissolved into val. q, diquark and gluons

A random pair chosen to exchange next ladder

Gluon emissions from ladder according to Markov chain, ordered in y, with pseudo Sudakov form factor

t-ch propagators are reggeized gluon in either colour singlets or octets. Prob(singlet) =  $P_1 = (1 - \exp(-\delta\Omega/2))^2$ 

Each gluon emission leads to two new propagators--allowed combinations  $P_1P_8$ ,  $P_8P_1$ ,  $P_8P_8$ -----singlet propagators give rise to rapidity gaps associated with elastic scatt.

Also rescatt. can give inelastic interaction of secondaries, producing new ladders with Poisson prob.  $exp(-\delta\Omega)(\delta\Omega)^n/n!$ 

single gluon emission iterated until active interval is colour singlet or no further emissions are kinematically allowed in rapidity interval

Finally usual hadronization, plus hadron decays, plus QED, to produce final scatter of observed particles.

A few typical plots from SHRiMPS Monte Carlo (in SHERPA)  $\rightarrow$ 









 $d\sigma/d(\Delta \eta)$ 



### Conclusions on soft-hard high energy pp interactions

- s-ch unitarity is important for elastic, quasi-elastic scatt ; multi-Pomeron exchange diagrams restore unitarity:
- Altho'  $g_{3P} \sim 0.3 g_N$ , high-mass dissoc<sup>n</sup> is enhanced:  $\sigma_{highM} \sim \sigma_{el}$  at high energy
- Soft data can be described by single "effective" pomeron (bare QCD pomeron + multi-pomeron contributions that is, QCD/BFKL pomeron → framework for "soft" physics
- Partonic struct. of pom, with multi-pom contrib<sup>ns</sup> can describe all soft (σ<sub>tot,el,SD</sub>..) and semihard (PDFs, minijets..) physics-KMR
- Forms the basis of "all purpose" MC SHRiMPS Krauss et al, which unifies description of particle prod. from soft/hard inter<sup>ns</sup>
   Gives excellent description of observable pts of soft HE inter<sup>ns</sup>.