

# ***ANISOTROPIC FLOW IN RELATIVISTIC HEAVY ION COLLISIONS AS INTERPLAY OF SOFT PHYSICS AND JETS***

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# OUTLINE

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- I. HYDJET++ model (hydro + jets)
- II. Description of elliptic flow in relativistic heavy ion collisions
- III. NCQ-scaling at RHIC and LHC
- IV. Model results for the ratio  $v_4/(v_2)^2$  at RHIC and LHC
- V. High harmonics
- VI. Conclusions

**I. HYDJET++ =  
FASTMS + HYDJET**



# HYDJET++ event generator

I.Lokhtin, L.Malinina, S.Petrushanko, A.Snigirev, I.Arsene, K.Tywoniuk,  
Comp. Phys. Commun.180 (2009) 779-799 (arXiv:0809.2708[hep-ph])

- The soft part of HYDJET++ event represents the "thermal" hadronic state.
  - ✓ multiplicities are determined assuming thermal equilibrium
  - ✓ hadrons are produced on the hypersurface represented by a parameterization of relativistic hydrodynamics with given freeze-out conditions
  - ✓ chemical and kinetic freeze-outs are separated
  - ✓ decays of hadronic resonances are taken into account (360 particles from SHARE data table) with "home-made" decayer

*the model reproduces soft hadroproduction features at RHIC  
(particle spectra, elliptic flow, HBT)*

- The hard, multi-partonic part of HYDJET++ event is identical to the hard part of Fortran written HYDJET (PYTHIA6.4xx + PYQUEN1.5) => **now PYTHIA Pro-Q20 tune !!** PYQUEN event generator is used for simulation of rescattering, radiative and collisional energy loss of hard partons in expanding quark-gluon plasma created in ultrarelativistic heavy ion AA collisions. HYDJET++ includes nuclear shadowing correction for parton distributions (important at LHC!) Impact-parameter dependent parameterization of *nuclear shadowing* (K.Tywoniuk, I.Arsene, L.Bravina, A.Kaidalov and E.Zabrodin, Phys. Lett. B 657 (2007) 170)

## Model parameters.

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1. Thermodynamic parameters at chemical freeze-out:  $T_{ch}$  ,  $\{\mu_B, \mu_S, \mu_Q\}$
2. If thermal freeze-out is considered:  $T_{th}$  ,  $\mu\pi$ -normalisation constant
3. Volume parameters:  $T, \Delta T, R$
1.  $\rho_{\perp}^{\max}$  -maximal transverse flow rapidity for Bjorken-like parametrization
5.  $\eta_{\max}$  -maximal space-time longitudinal rapidity which determines the rapidity interval  $[-\eta_{\max}, \eta_{\max}]$  in the collision center-of-mass system.
6. Impact parameter range: minimal  $b_{\min}$  and maximal  $b_{\max}$  impact parameters
7. Flow anisotropy parameters  $\delta(b), \epsilon(b)$

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## PYTHIA+PYQUEN obligatory parameters

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9. Beam and target nuclear atomic weight  $A$
10.  $\sqrt{s_{NN}}$  –c.m.s. energy per nucleon pair (PYTHIA initialization at given energy)
11. **ptmin** – minimal pt of parton-parton scattering in PYTHIA event (ckin(3) in /pysubs/)
12. **nhsel** flag to include jet production in hydro-type event:

0 - jet production off (pure FASTMC event),  
1 - jet production on, jet quenching off (FASTMC+njet\*PYTHIA events),  
2 - jet production & jet quenching on (FASTMC+njet\*PYQUEN events),  
3 - jet production on, jet quenching off, FASTMC off (njet\*PYTHIA events),  
4 - jet production & jet quenching on, FASTMC off (njet\*PYQUEN events);

13. **ishad** flag to switch on/off nuclear shadowing



## Parameters of energy loss model in PYQUEN

(default, but can be changed from the default values by the user)

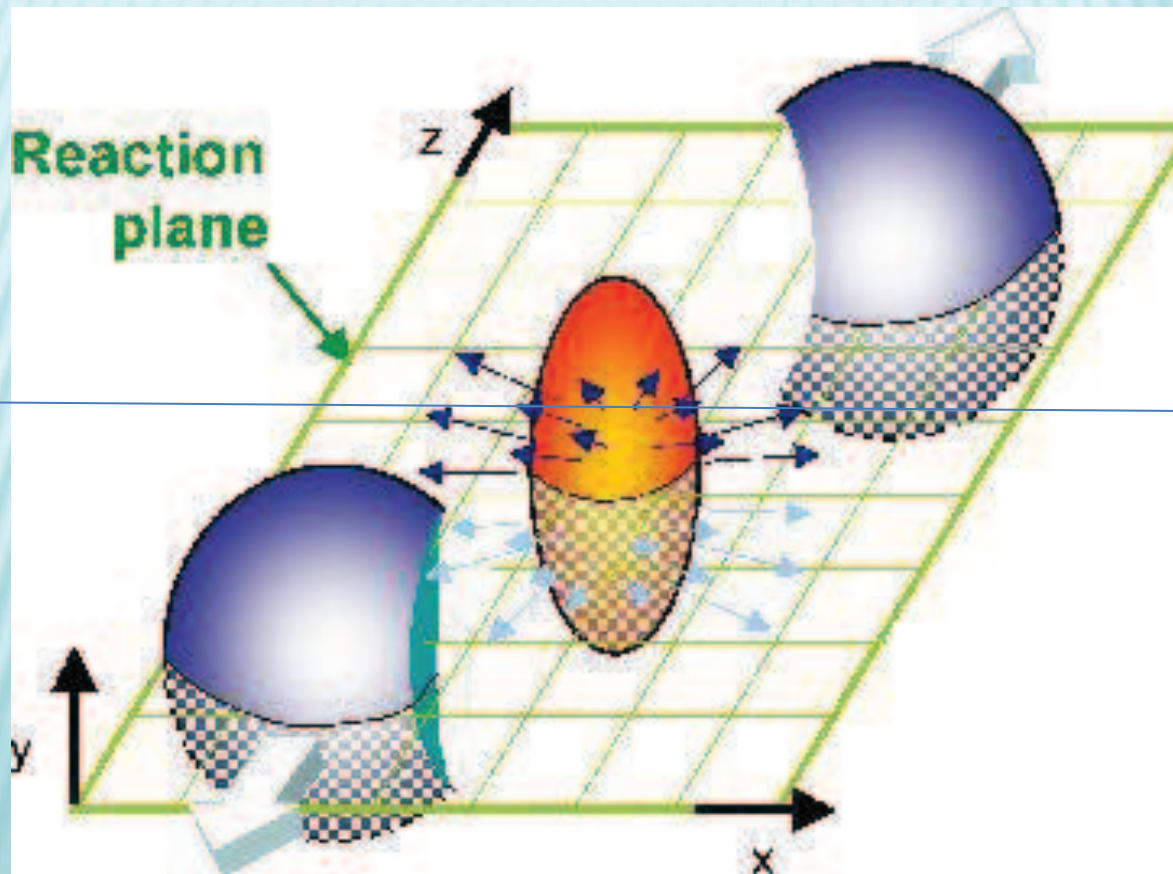
1. **T0** - initial temperature of quark-gluon plasma for central Pb+Pb collisions at mid-rapidity (initial temperature for other centralities and atomic numbers will be calculated automatically)  
at LHC: **T0=1 GeV**, at RHIC(200 AGeV) **T0=0.300 GeV**
2. **tau0** - proper time of quark-gluon plasma formation  
at LHC: **tau0=0.1 fm/c**, at RHIC(200 AGeV) **tau0=0.4 fm/c**
3. **nf** - number of active quark flavours in quark-gluon plasma (nf=0, 1, 2 or 3) at LHC: **nf=0**, at RHIC(200 AGeV) **nf=2**
4. **ienglu** - flag to fix type of medium-induced partonic energy loss (ienglu=0 - radiative and collisional loss, ienglu=1 - radiative loss only, ienglu=2 - collisional loss only, default value is ienglu=0);  
**ianglu** - flag to fix type of angular distribution of emitted gluons (ianglu=0 - small-angular, ianglu=1 - wide-angular, ianglu=2 - collinear, default value is ianglu=0).  
**ienglu=0**

## **II. Description of elliptic flow in relativistic heavy ion collisions**

# Anisotropic flow

S.Voloshin and Y.Zhang, Z.Phys.C70 (1996) 665

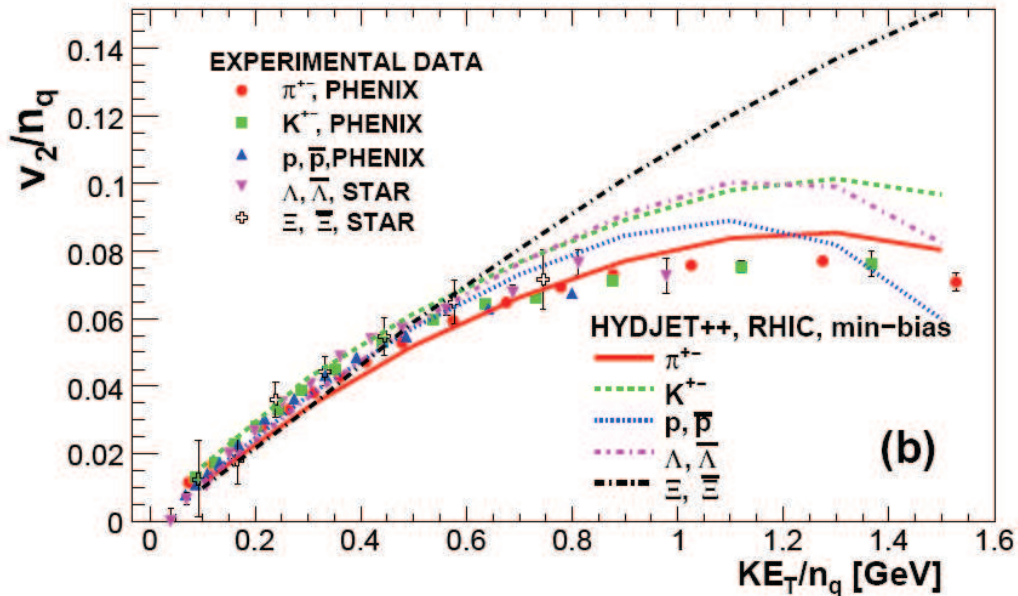
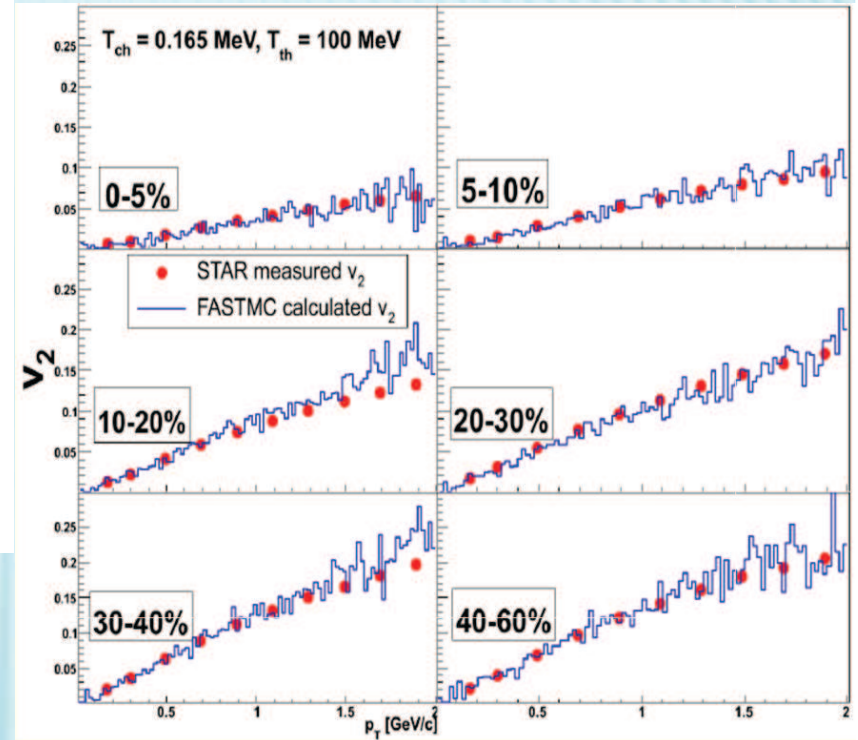
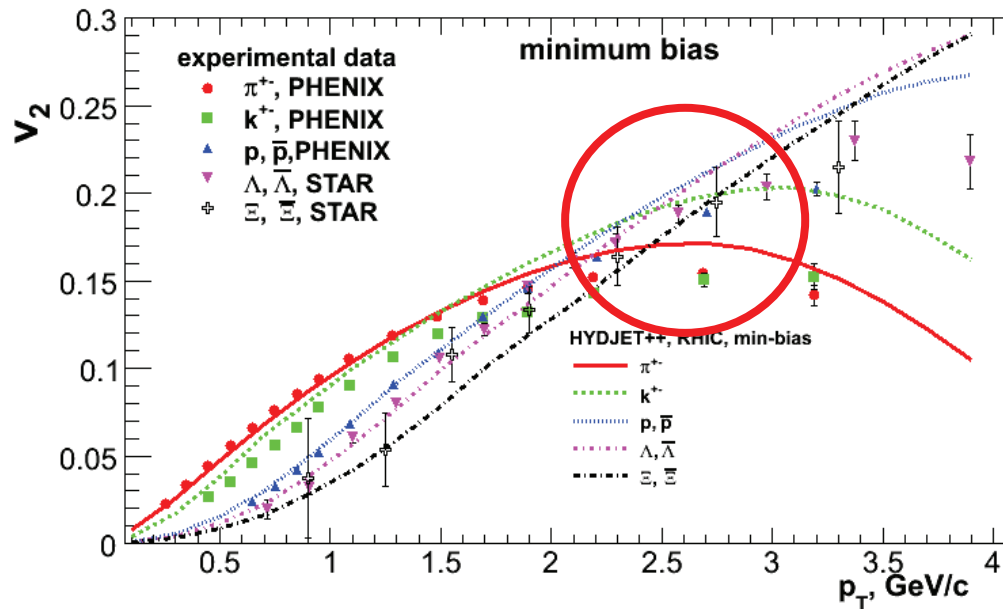
$$\frac{dN}{d\varphi} = \frac{1}{2\pi} \left( 1 + \sum_{n=1}^{\infty} 2v_n(p_t) \cos[n(\varphi - \psi_r)] \right)$$





# RHIC DATA VS. HYDJET++ MODEL

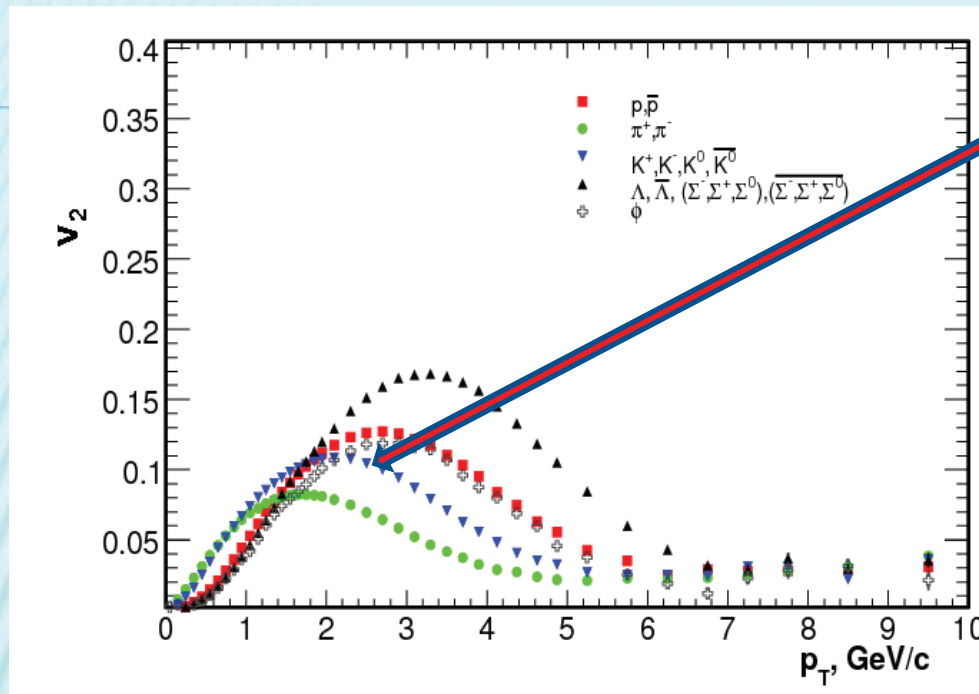
Au+Au @ 200 AGeV



Elliptic flow

G. Eyyubova et al., PRC 80 (2009) 064907;  
N.S. Amelin et al., PRC 77 (2008) 014903

## $V_2$ in HYDJET++ for different particles (centrality 30%)

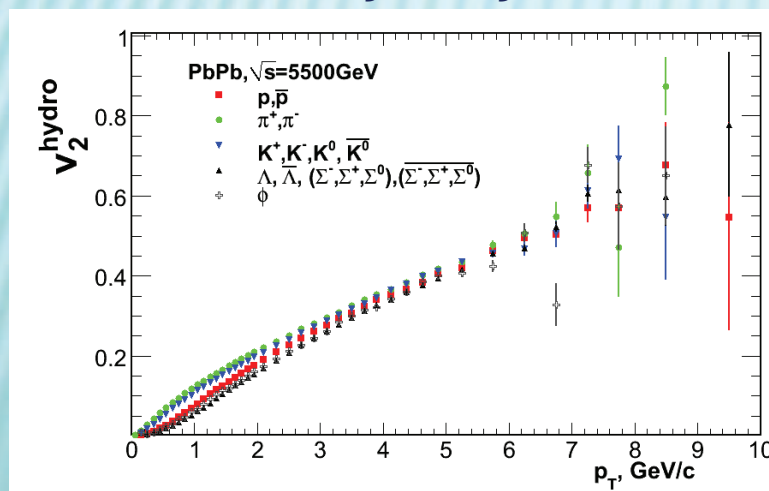


*Mass ordering in soft  $p_T$  regions then breaks.*

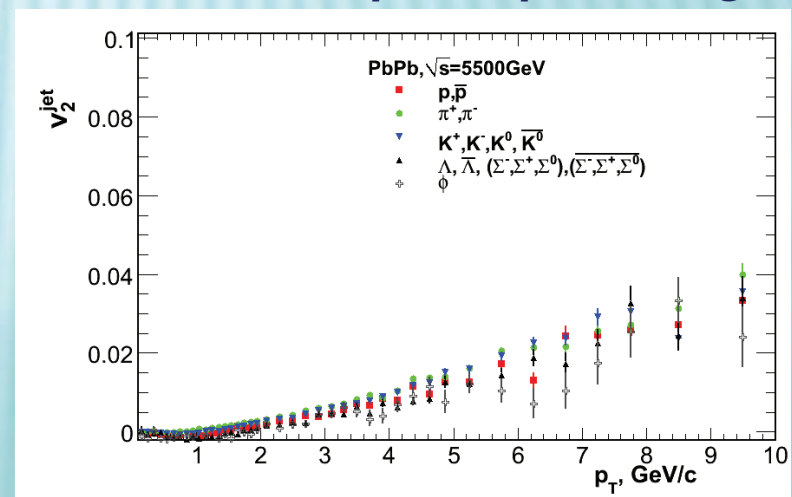
Why?

Hydrodynamics gives **mass ordering** of  $v_2$ .  
The model possesses **crossing of baryon and meson branches.**

*Hydrodynamics*



*Jet part +quenching*



Interplay between hydrodynamics and jets



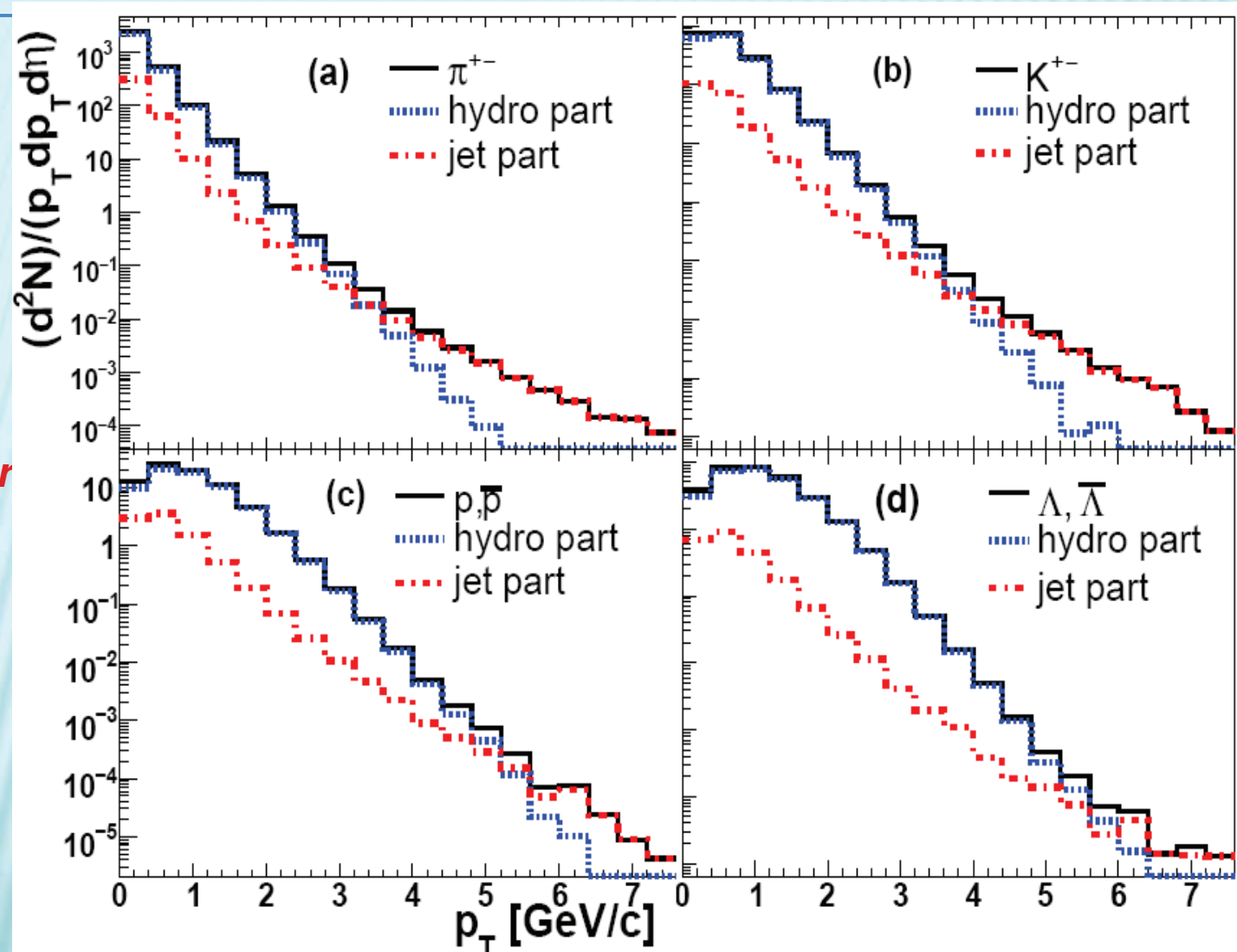
# The $p_T$ spectra of $\pi$ , $K$ , $p$ , $\Lambda$ with HYDJET++ model, $\sqrt{s}=200\text{GeV}$

The slope for the hydro part depends strongly on mass:

*- the heavier the particle -- the harder the spectrum*



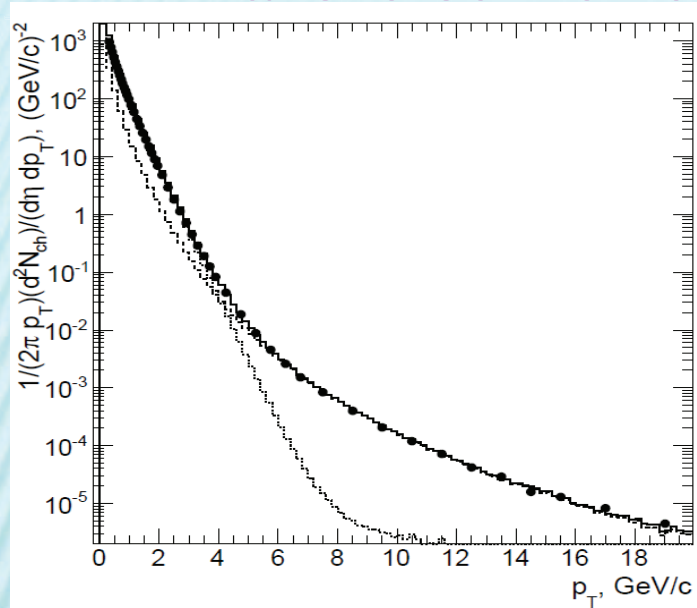
The hydro part dies out earlier for light particles than for heavy ones



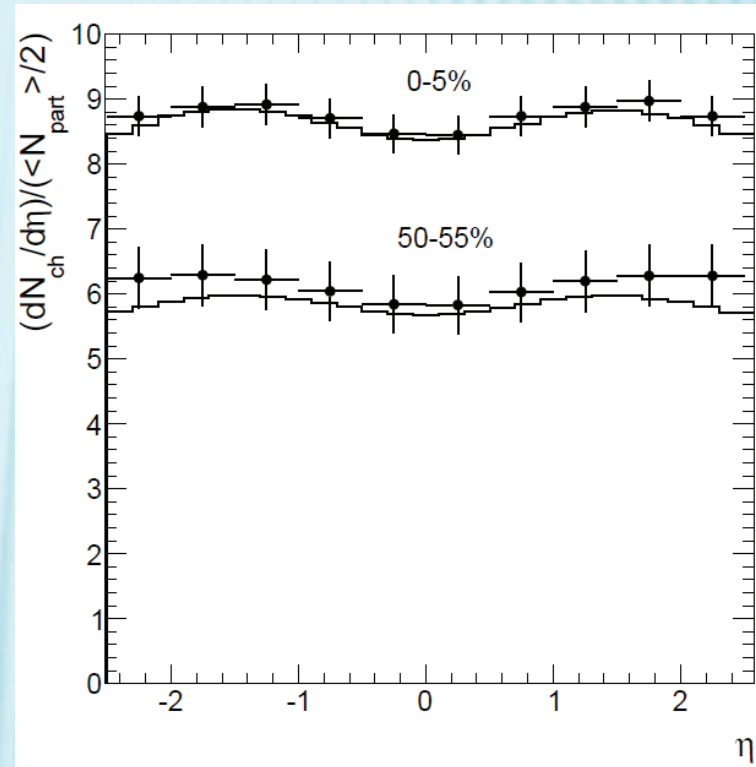
# LHC DATA VS. HYDJET++ MODEL

Transverse momentum

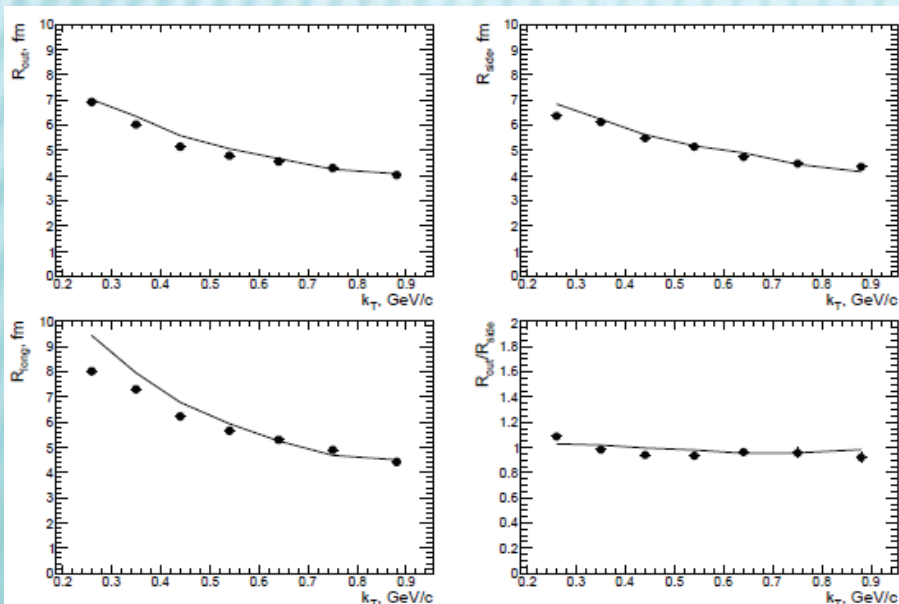
Pb+Pb @ 2.76 ATeV



Rapidity



I. Lokhtin et al., Eur. Phys. J C72 (2012) 2045



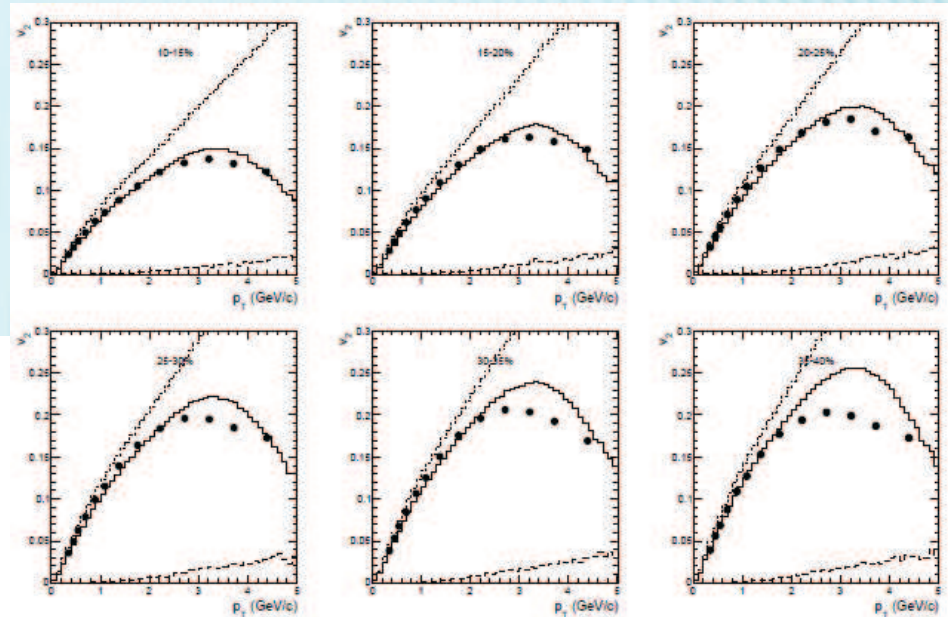
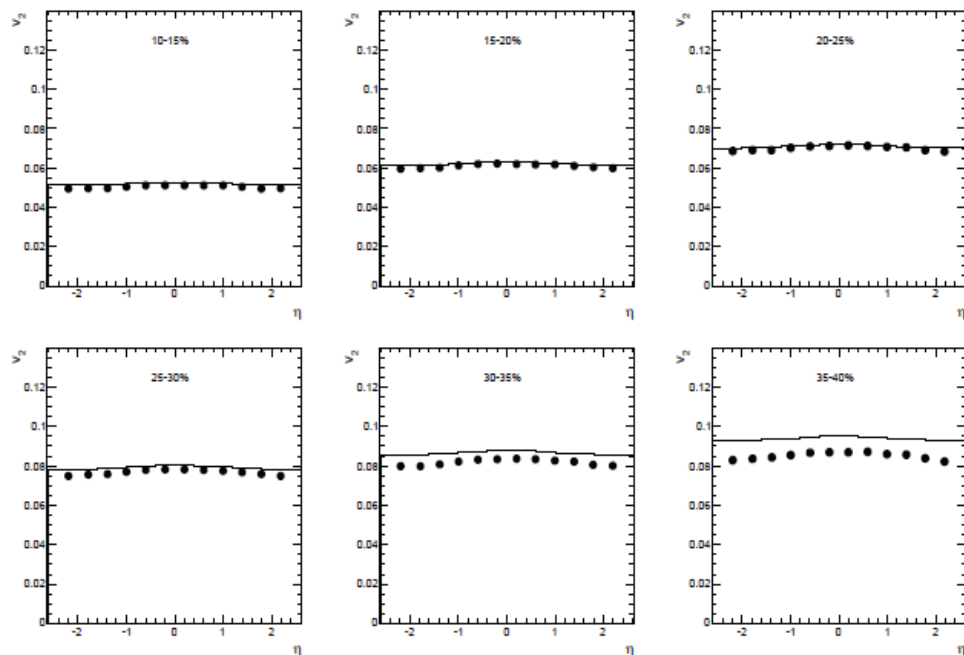
Correlation radii (femtometry)



# LHC DATA VS. HYDJET++ MODEL

Pb+Pb @ 2.76 ATeV

## Elliptic flow



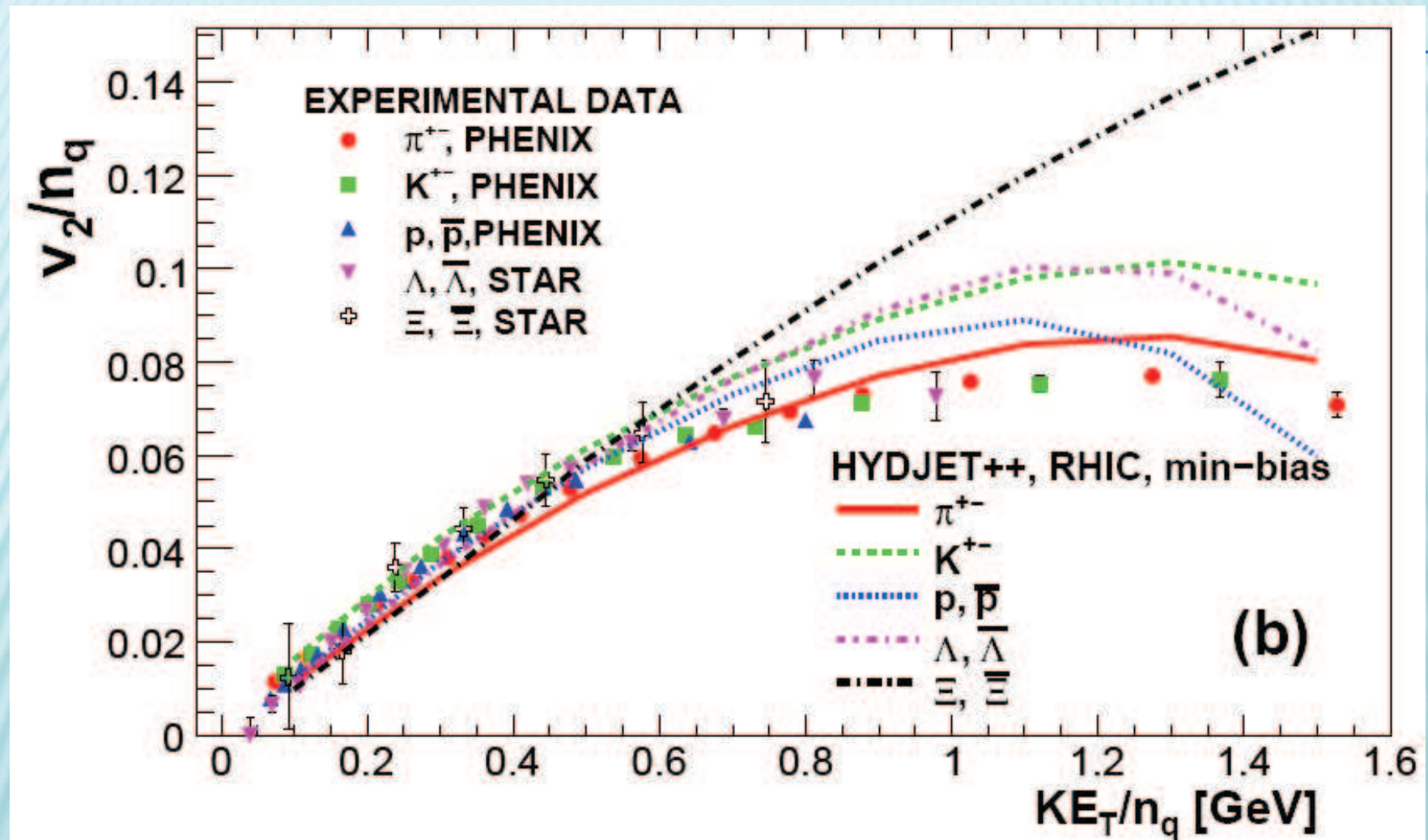
I. Lokhtin et al., Eur. Phys. J C72  
(2012) 2045

Model gives a fair description of various observables at both RHIC and LHC

# III. Number-of- constituent- quark (NCQ) scaling



## COMPARISON WITH RHIC DATA

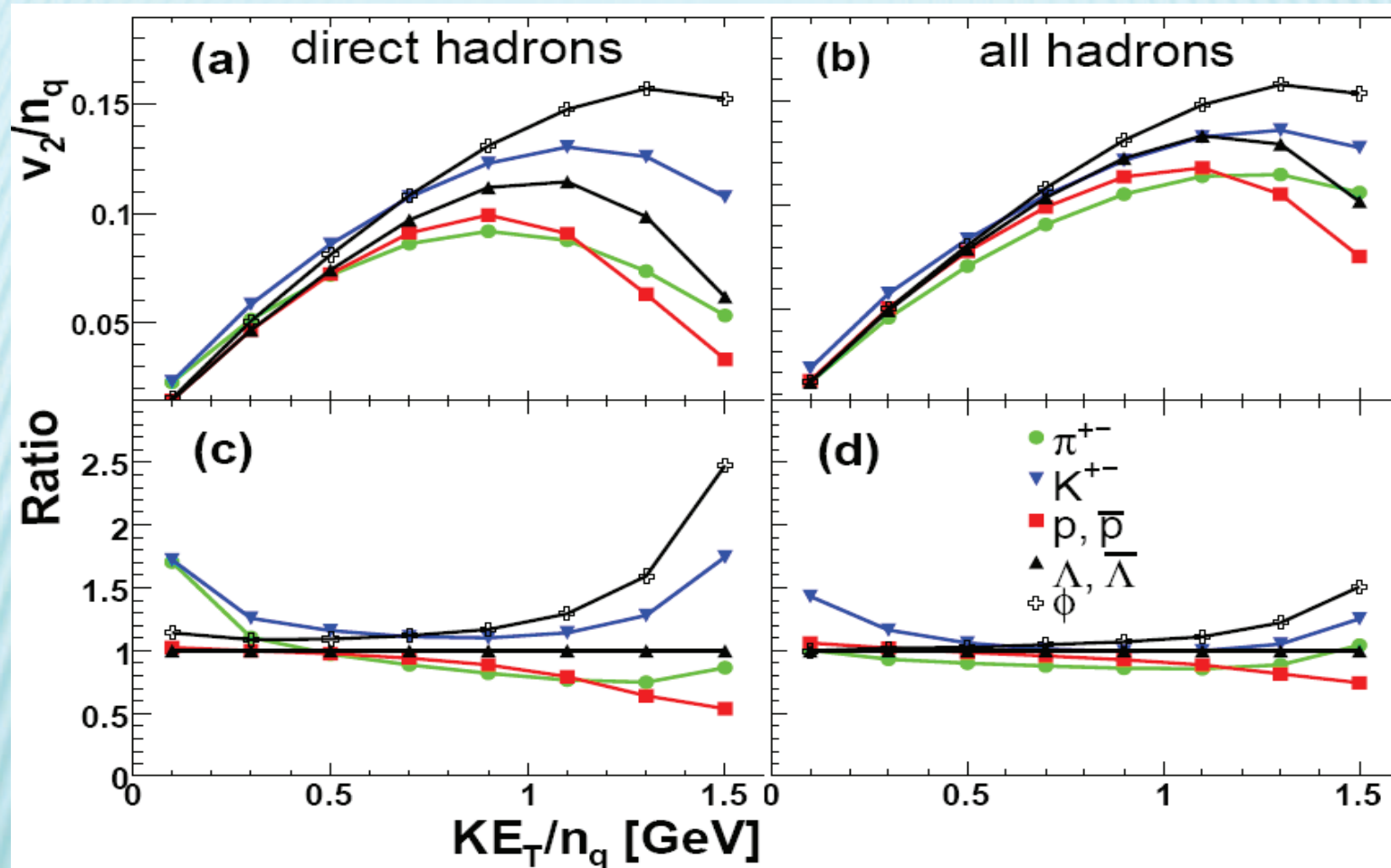


The agreement seems to be good at  $KE_T/n_q < 0.7$  GeV

# Number-of-constituent-quark scaling at RHIC

Direct particles: scaling is not good.

All particles:  $KE_T/n_q$  scaling



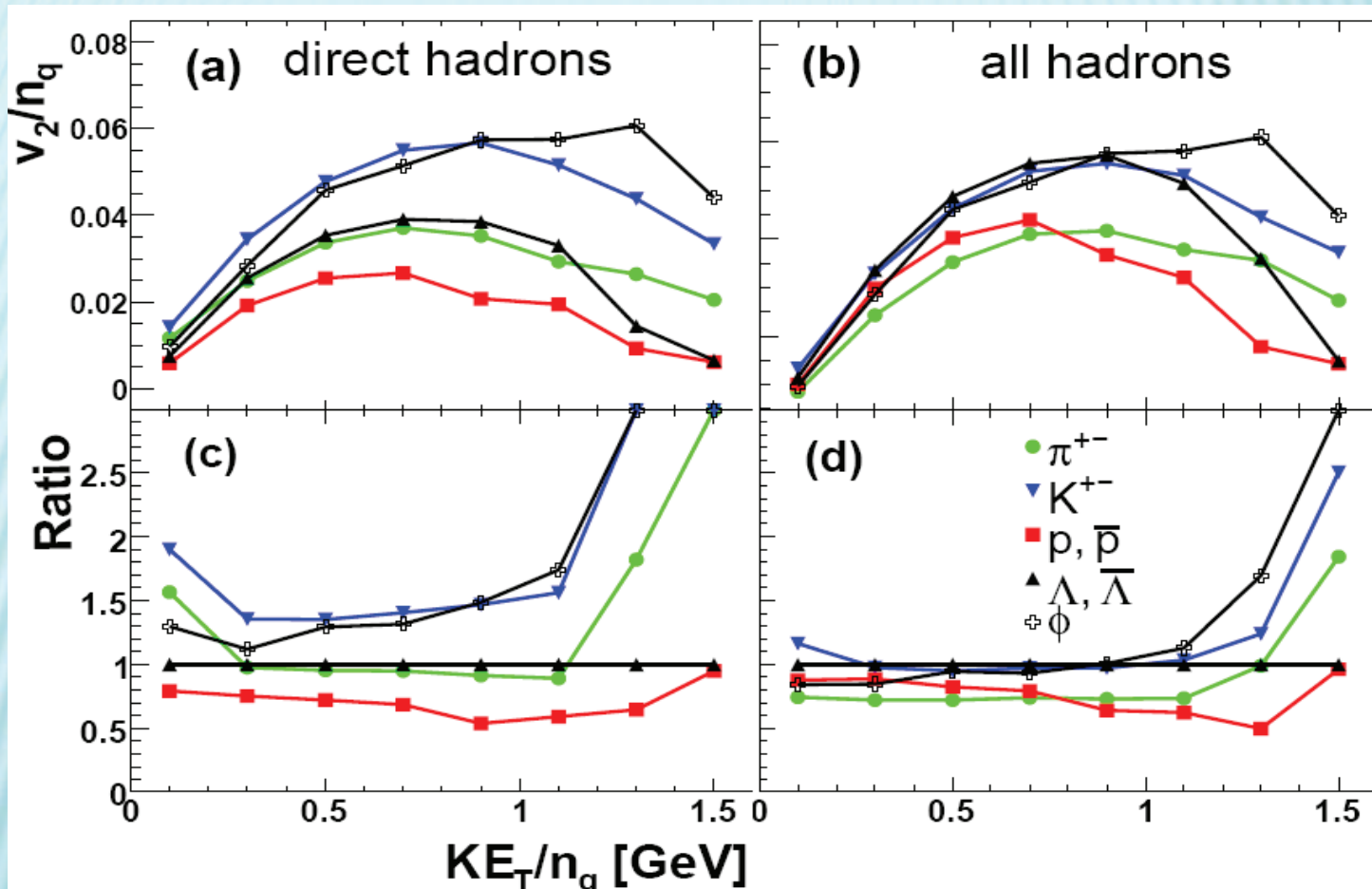
One of the explanations of  $KE_T/n_q$  scaling is partonic origin of the elliptic flow.

*However, final state effects (such as resonance decays and jets) may also lead to appearance of the scaling*

# NCQ scaling at LHC

No scaling for direct particles

Appearance of the approximate scaling for all particles



**LHC: NCQ scaling will be only approximate (prediction, 2009)**

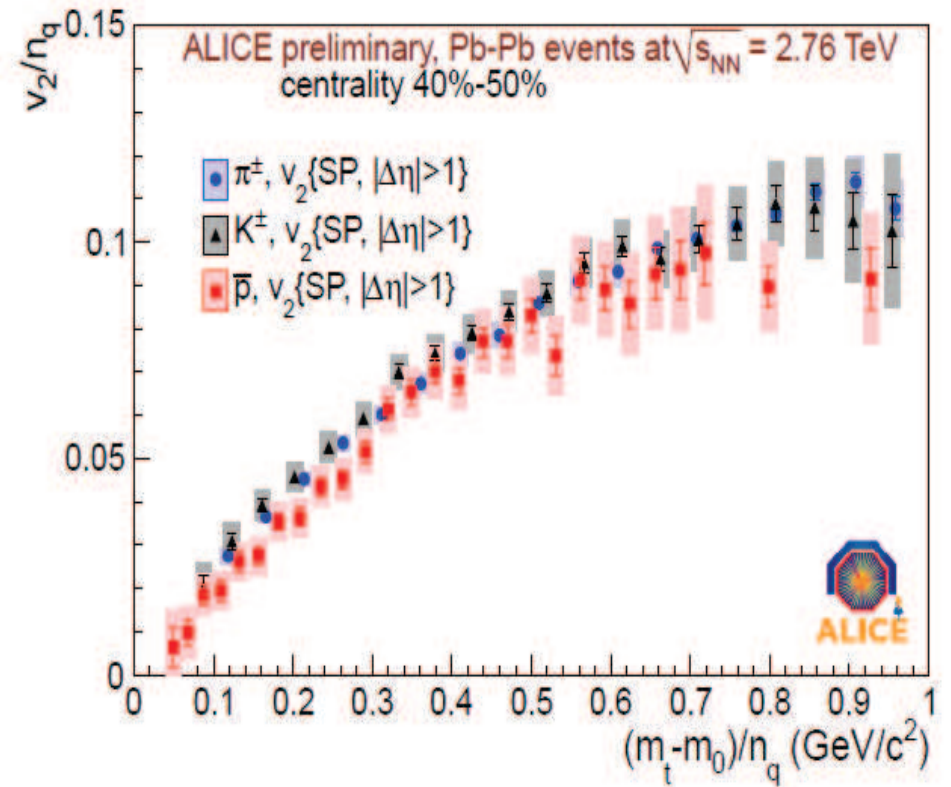
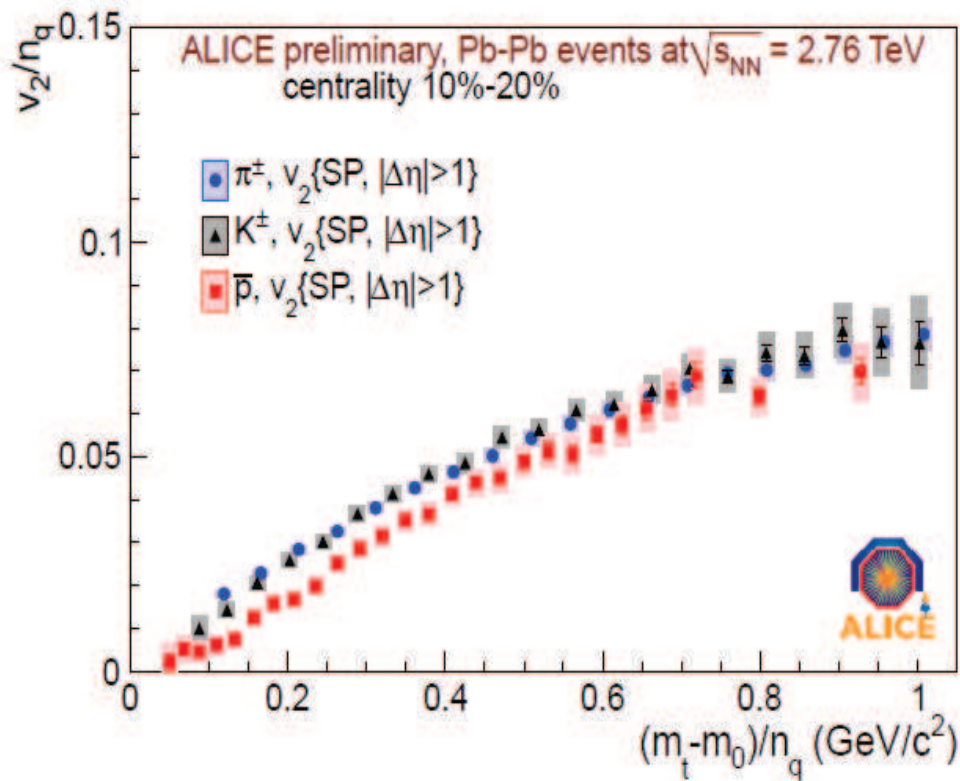


## Experimental results (LHC)

ALICE Collaboration, M. Krzewicki et al., JPG 38 (2011) 124047

Semi-central collisions

Semi-peripheral collisions



**The NCQ scaling is indeed only approximate (2011)**

## IV. $V_4/(V_2*V_2)$ RATIO

# Predictions

*N. Borghini, J.-Y. Ollitrault, PLB 642 (2006) 227*

- Within the *approximation* that the particle momentum  $\mathbf{p}$  and the fluid velocity  $\mathbf{v}$  are parallel (valid for *large momentum*  $p_{\uparrow}$  and *low freeze-out temperature*  $T$ )

$$dN/d\varphi = \exp(2\varepsilon p_{\uparrow} \cos(2\varphi)/T)$$

- Expanding to order  $\varepsilon$ , the  $\cos(2\varphi)$  term is

$$v_2 = \varepsilon p_{\uparrow}/T$$

- Expanding to order  $\varepsilon^2$ , the  $\cos(4\varphi)$  term is

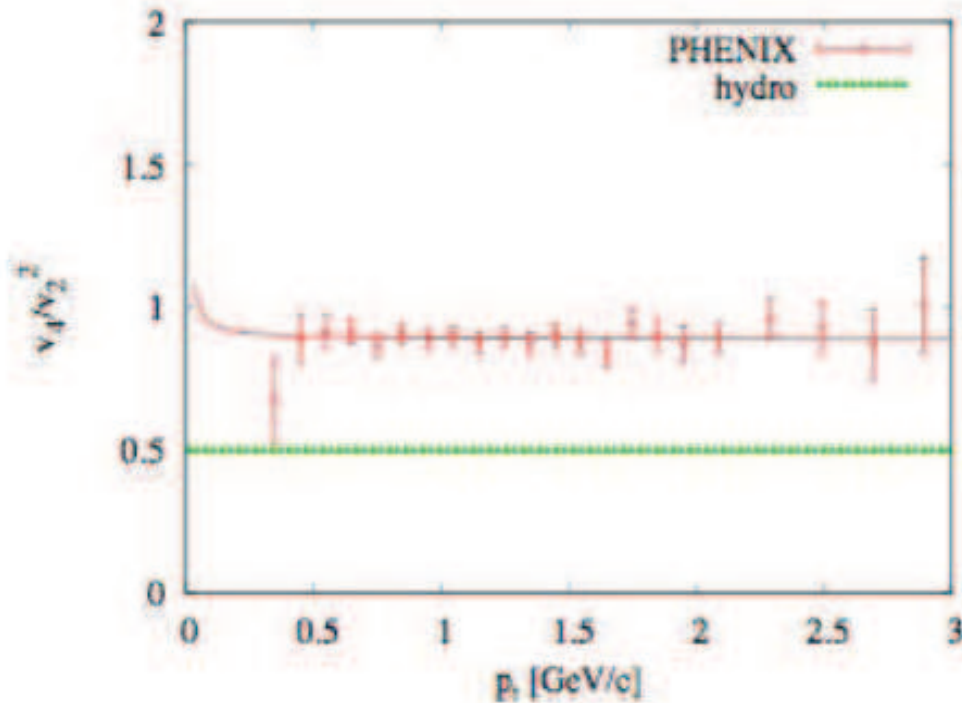
$$v_4 = \frac{1}{2} (v_2)^2$$

**Hydrodynamics has a universal prediction for  $v_4/(v_2)^2$  !**

Should be independent of equation of state, initial conditions, centrality, rapidity, particle type



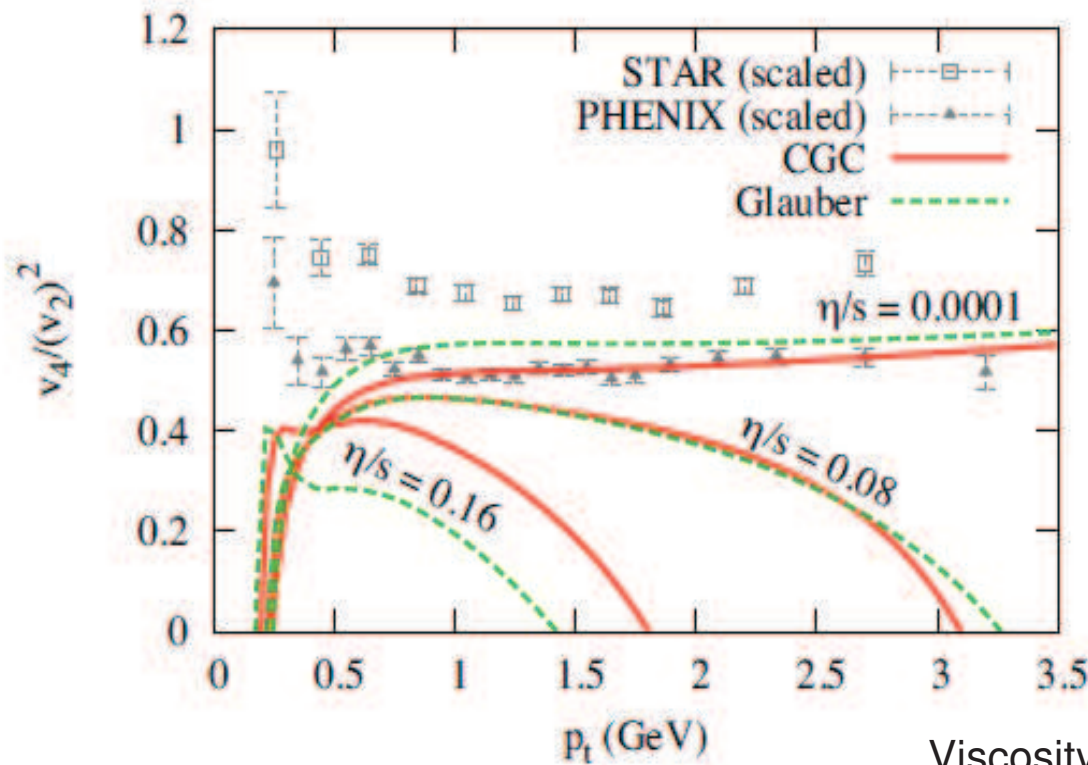
## Comparison with data



PHENIX data for charged pions  
Au-Au collisions at 100+100 GeV  
20-60% most central

The ratio is significantly larger than 0.5.  
Can this be explained by viscous corrections?

# Effects of initial profile and viscosity

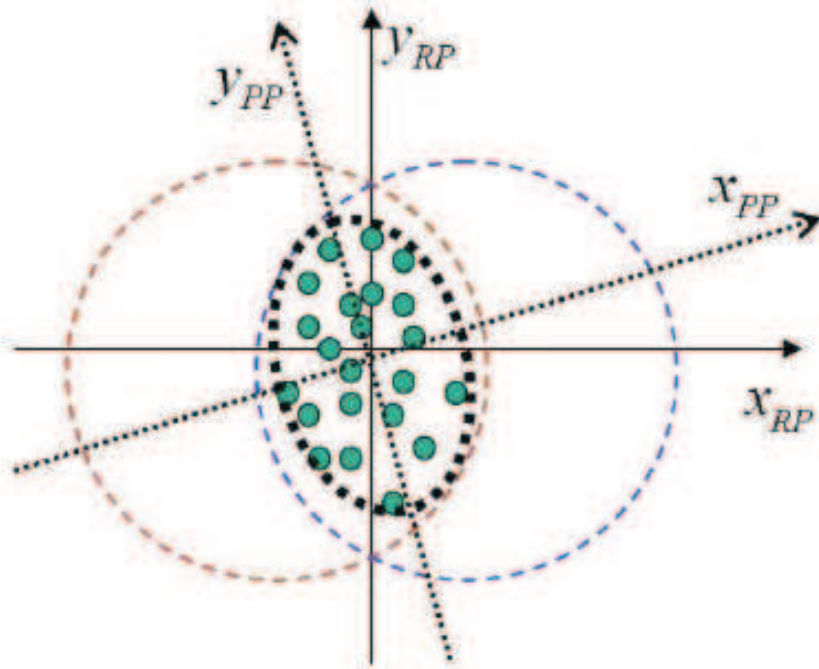


Initial profile has little effect although eccentricities differ.

results strongly depend on viscosity

Viscosity lowers  $v_4/(v_2)^2$  for a realistic  $T_f$

## Eccentricity fluctuations



Depending on where the participant nucleons are located within the nucleus at the time of the collision, the actual shape of the overlap area may vary: the **orientation and eccentricity** of the ellipse defined by participants fluctuates.

Assuming that  $v_2$  scales like the eccentricity, **eccentricity fluctuations** translate into  **$v_2$  fluctuations**

Eccentricity fluctuation can be computed in MC Glauber model or derived from experiment by comparing different methods for flow calculation.



# Why $\varepsilon$ fluctuations change $v_4/v_2^2$

Experimentally, no direct measure of  $v_2$  and  $v_4$

$v_2$  and  $v_4$  are measured via azimuthal correlations

$$v_2 \text{ from } \langle \cos(2\phi_1 - 2\phi_2) \rangle = \langle (v_2)^2 \rangle$$

$$v_4 \text{ from } \langle \cos(4\phi_1 - 2\phi_2 - 2\phi_3) \rangle = \langle v_4 (v_2)^2 \rangle$$

Experimentally measured

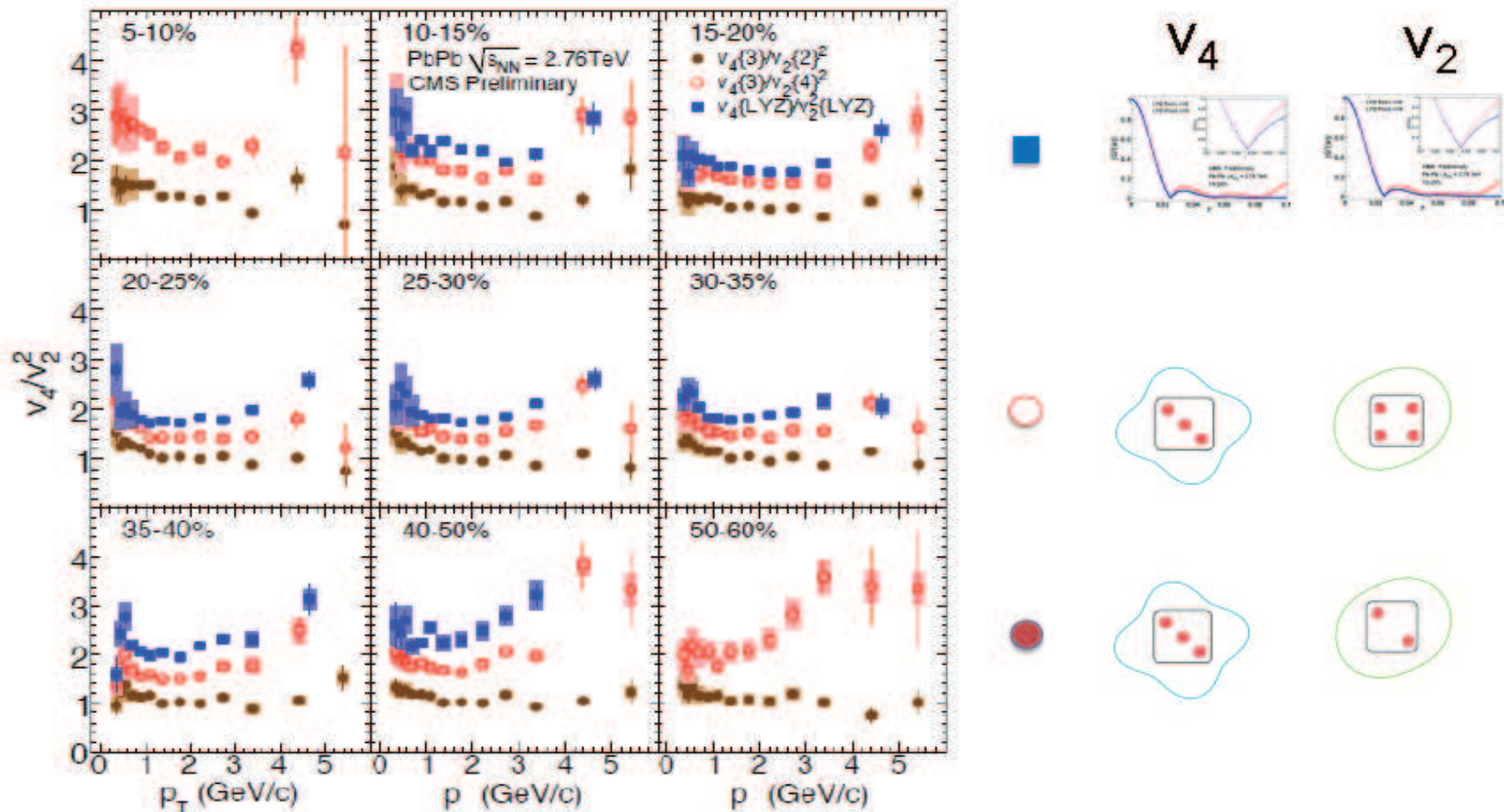
$$\frac{v_4}{v_2^2} = \frac{\langle v_4 (v_2)^2 \rangle}{\langle (v_2)^2 \rangle^2} = \frac{1}{2} \frac{\langle (v_2)^4 \rangle}{\langle (v_2)^2 \rangle^2} > \frac{1}{2}$$

fluctuations

hydro

Similar results obtained using Event Plane method

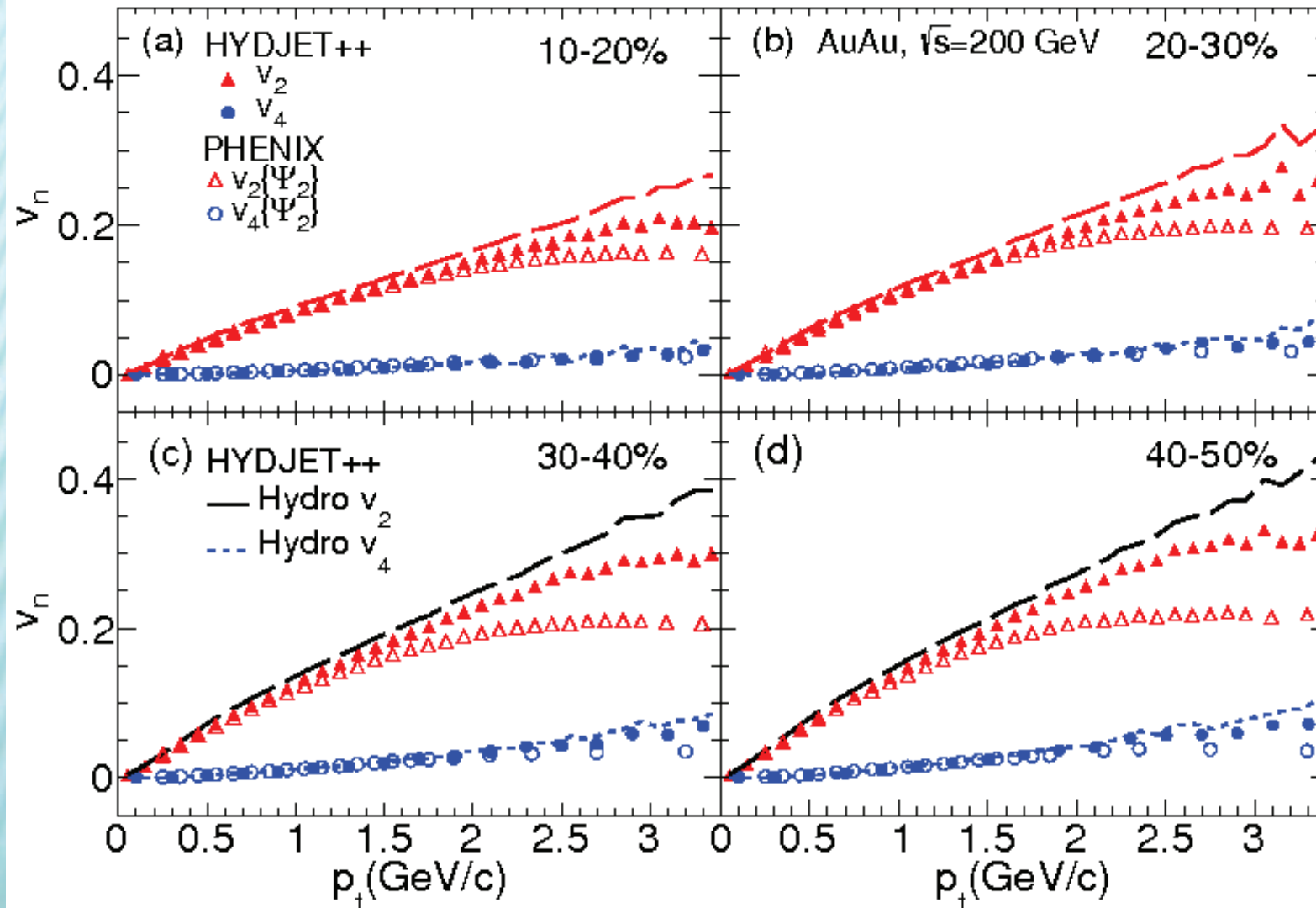
# $v_4 / v_2^2(p_T)$ at mid-rapidity $|\eta| < 0.8$



Significantly higher than RHIC: experimental method dependent

# HYDJET++ (RHIC)

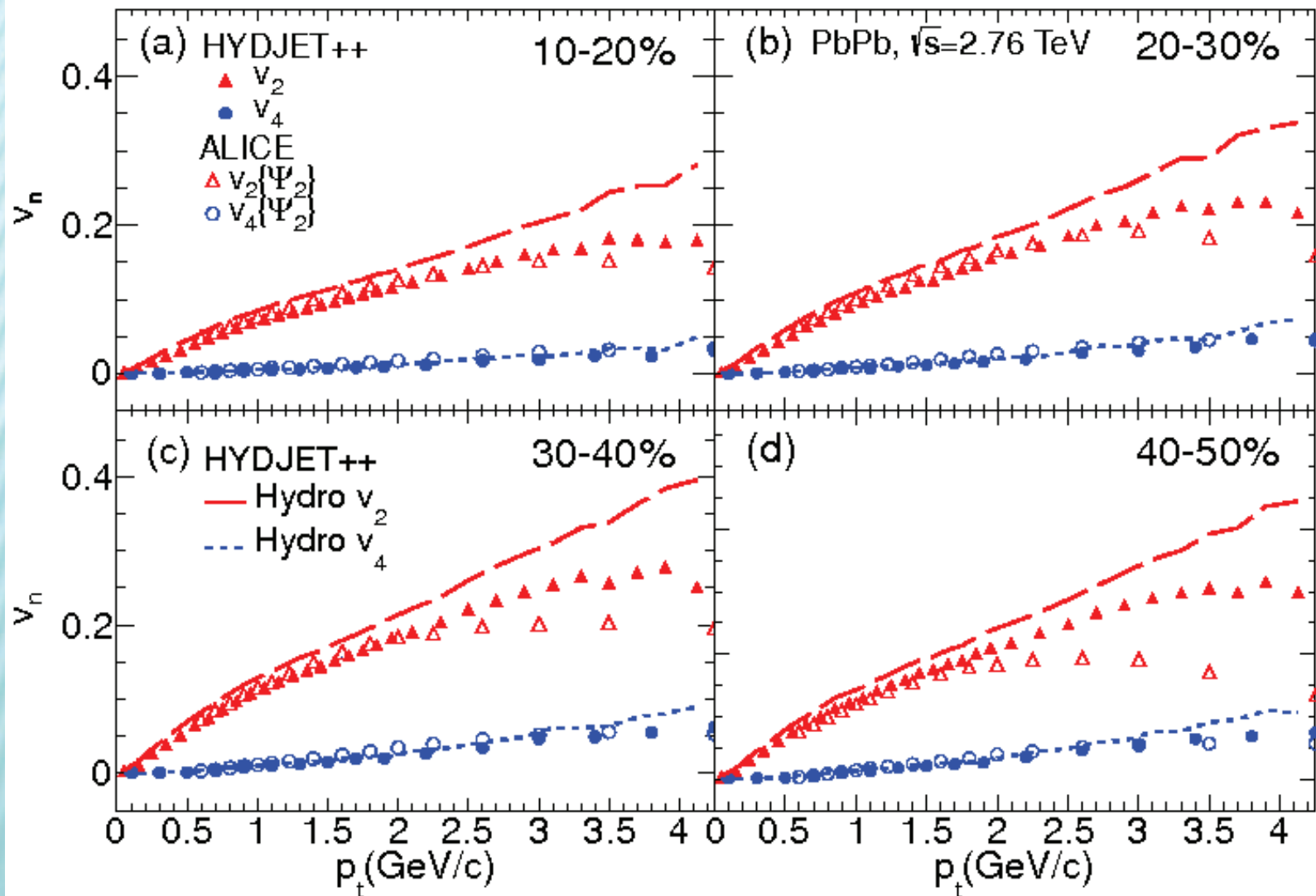
Effects to be studied: resonance decay and hard part influence



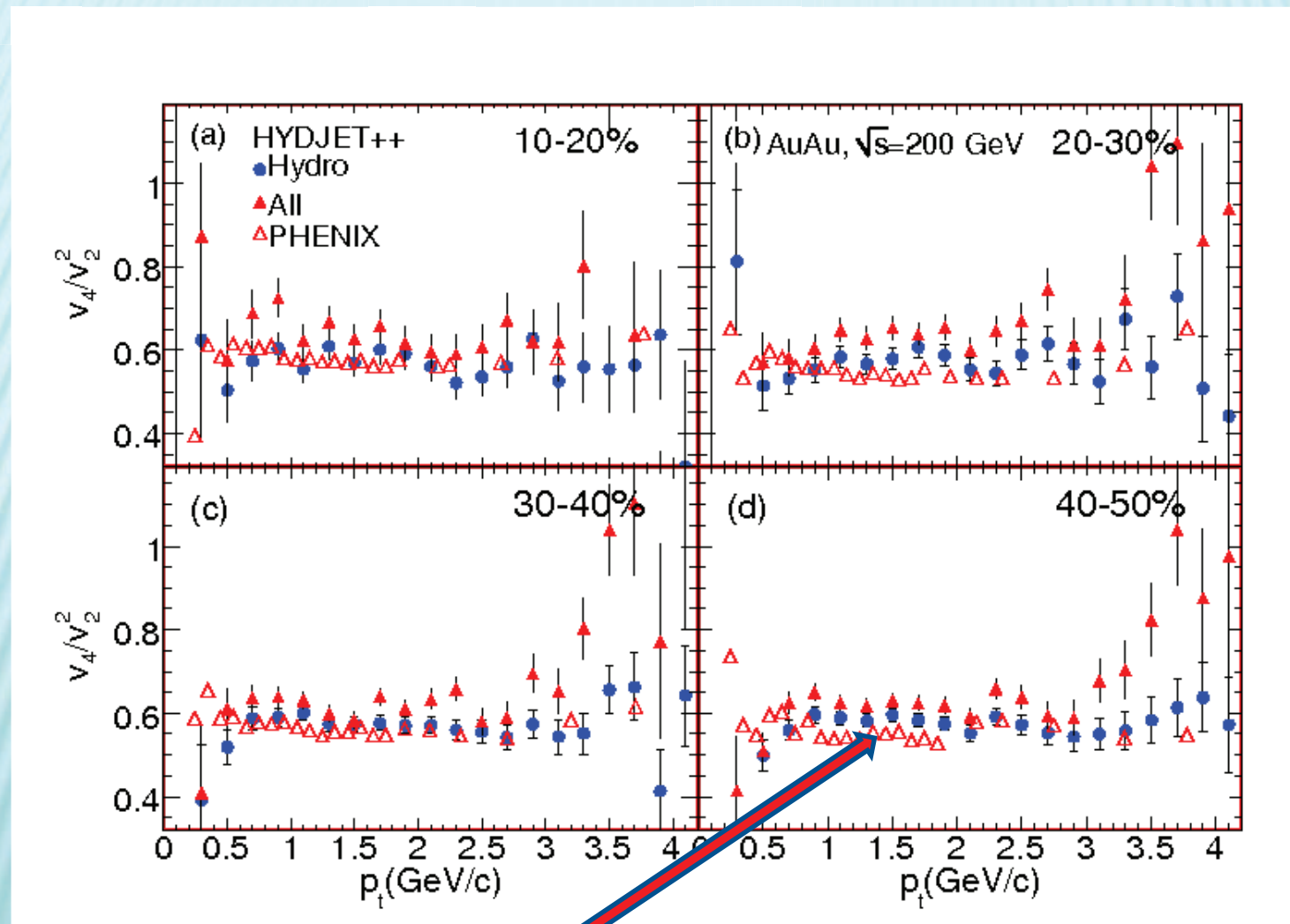


# HYDJET++ (LHC)

## Pure hydrodynamics vs hydro+jets

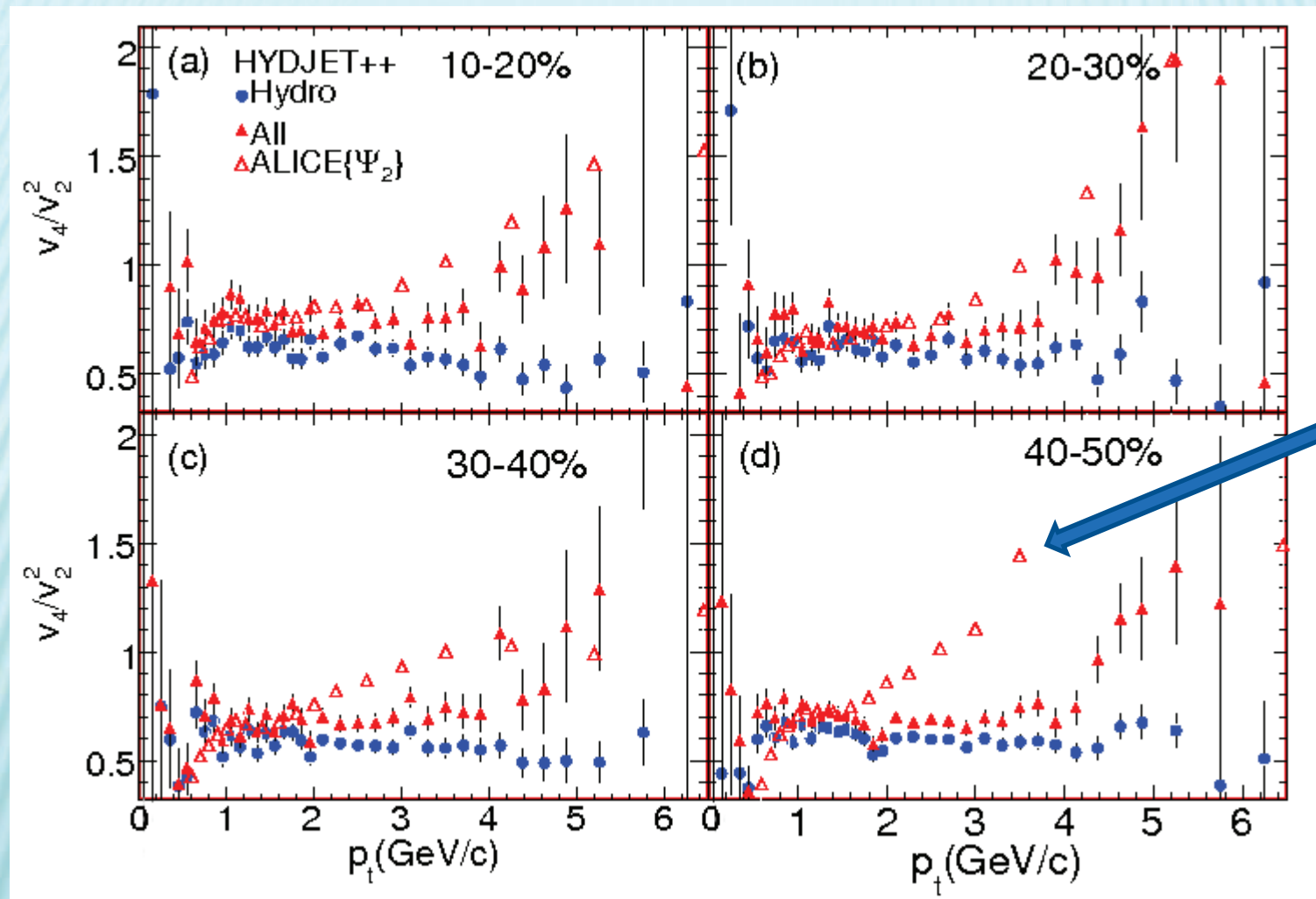


# HYDJET++ RESULTS FOR RHIC



**Jets increase the ratio**

# HYDJET++ RESULTS FOR LHC



Jets !

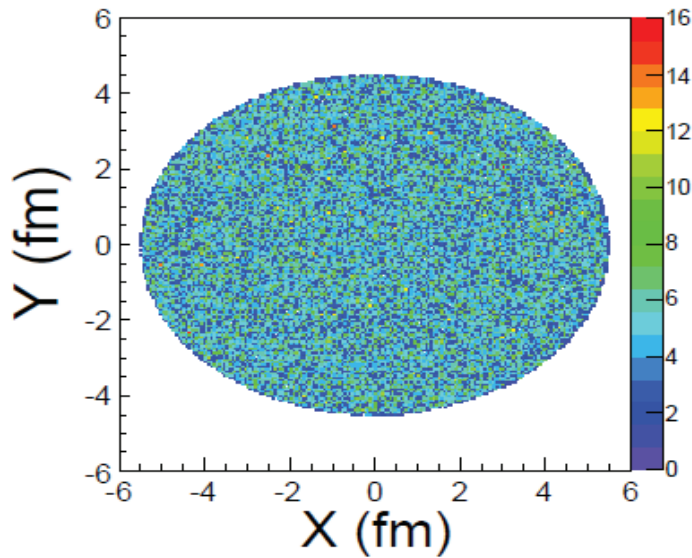
The same tendency is observed in Pb+Pb at LHC



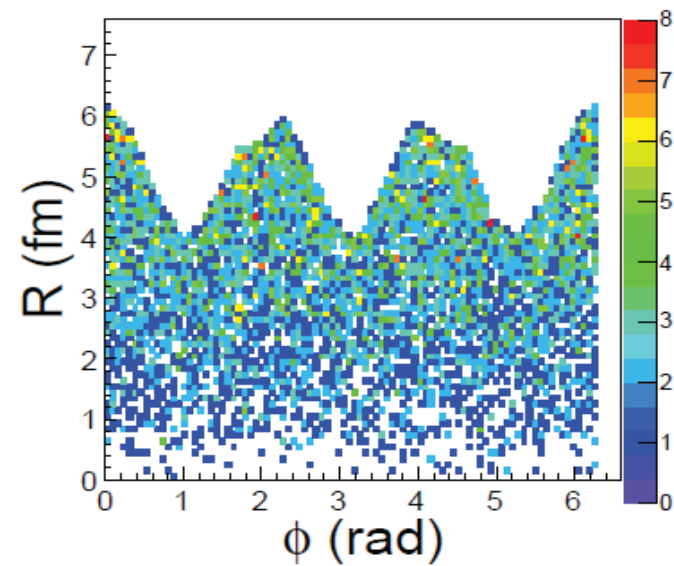
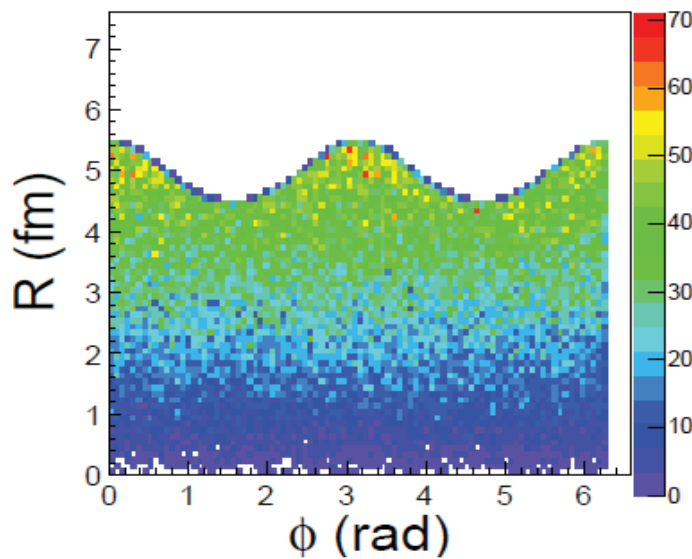
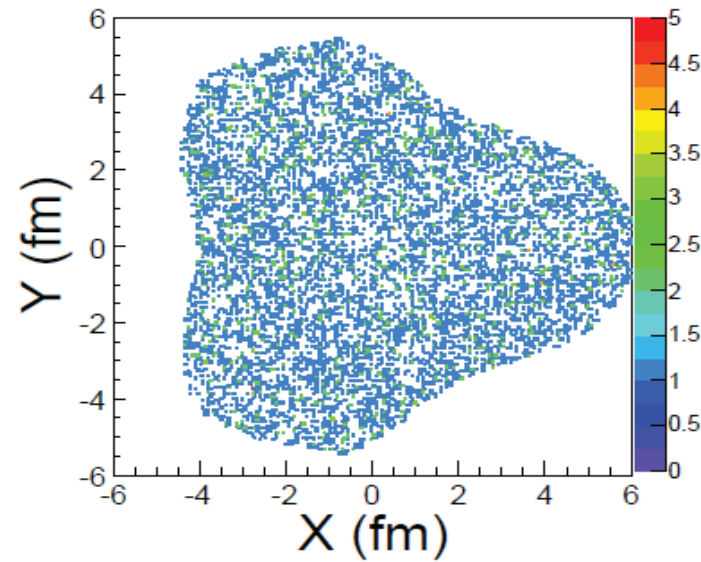
# V. High harmonics

# GENERATION OF TRIANGULAR FLOW

V2

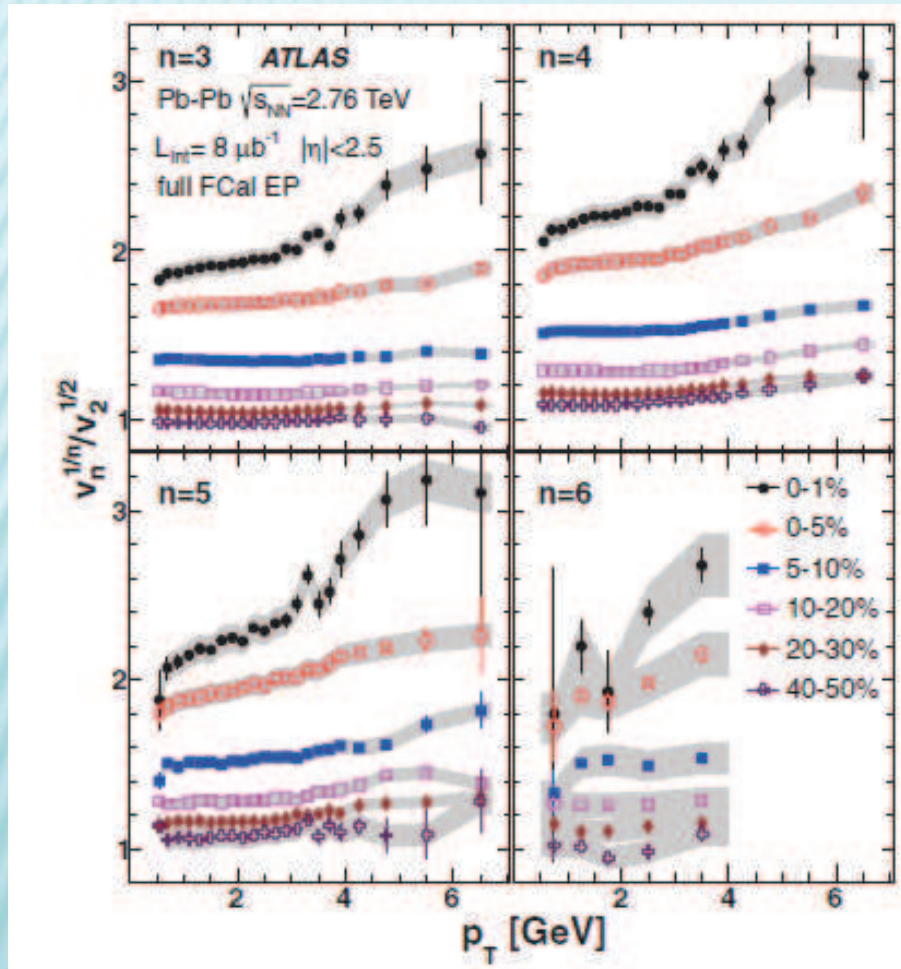


V3

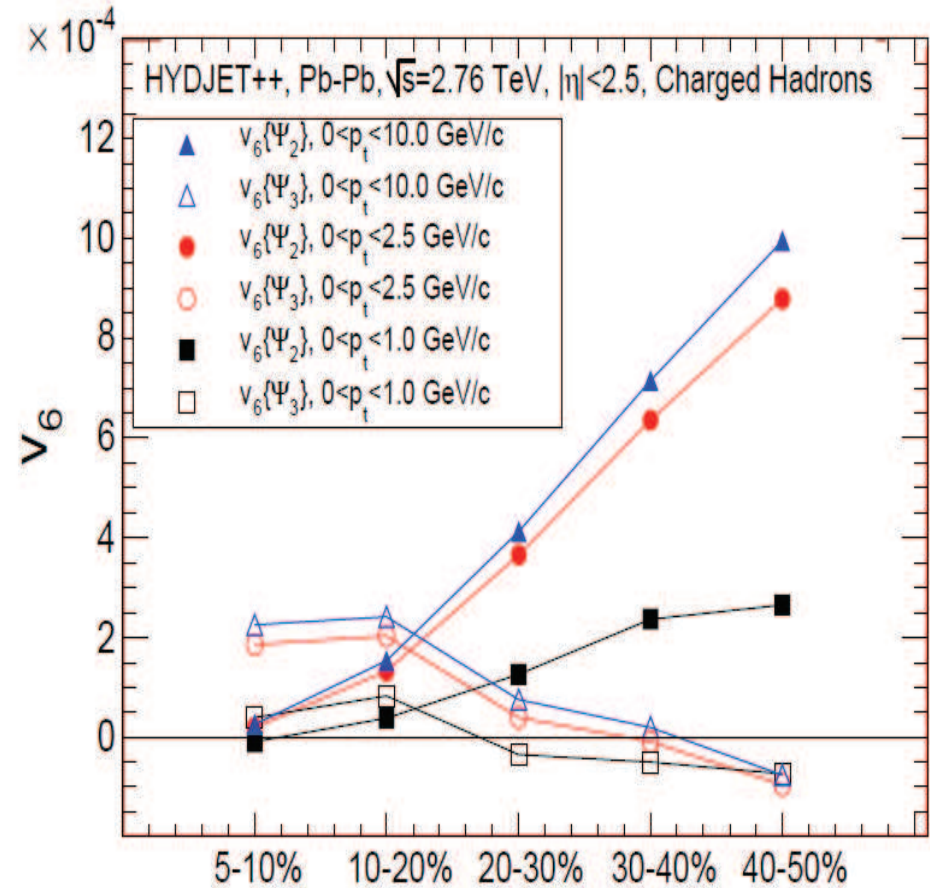


# Hexagonal flow: $V_6 \propto \alpha V_2^3 + \beta V_3^2$

ATLAS, PRC 86 (2012) 014907

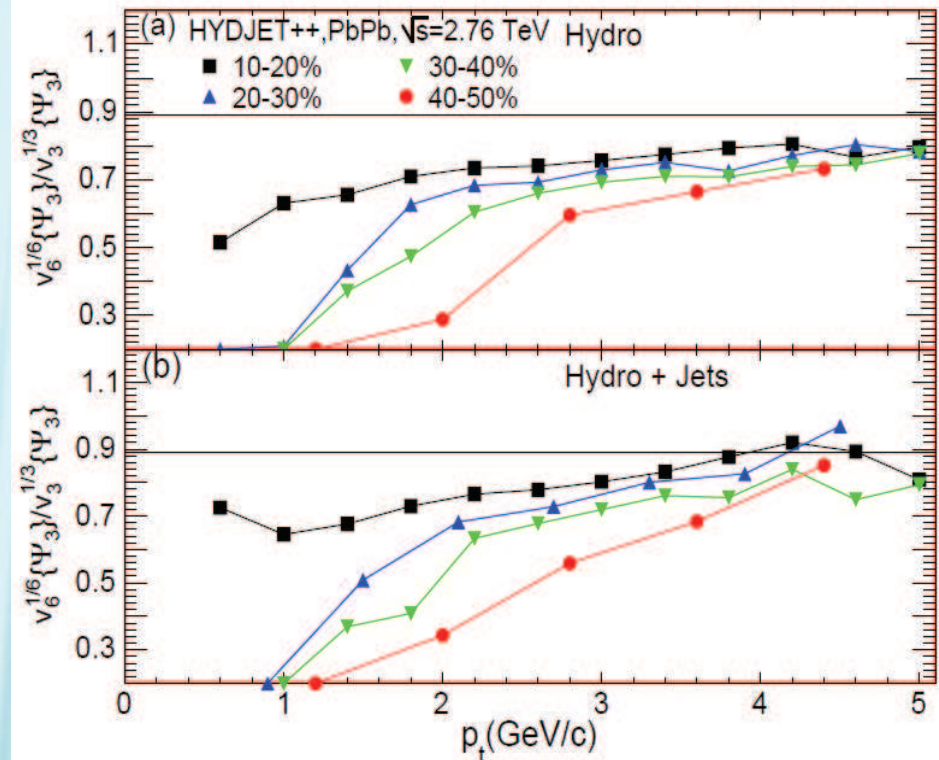
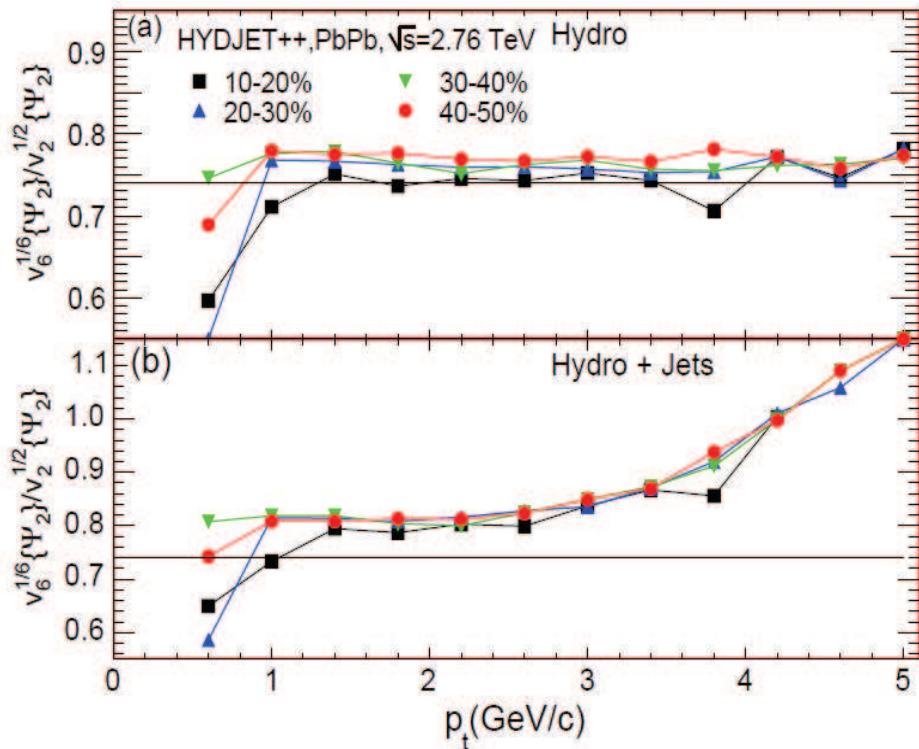


Higher order harmonics scaling





# Hexagonal flow: $V_6 \propto \alpha V_2^3 + \beta V_3^2$



$\Psi_2$

$\Psi_3$

It would be interesting to study  $V_6(\Psi_2)$  and  $V_6(\Psi_3)$  in experiment

# CONCLUSIONS

The HYDJET++ model allows to investigate flow of hydro and jet parts separately, to look at reconstruction of pure hydro flow and its modification due to jet part.

- *Jets result to increase by 25% - 30% of the ratio  $v_4/(v_2*v_2)$*
- *Jets + eccentricity fluctuations are enough to explain both RHIC and LHC data*
- *Jets lead to rise of the high- $p_T$  tail of the ratio*
- *The predicted violation of the NCQ scaling at LHC is observed*
- *Higher order harmonics – just interplay between hydrodynamics and jets ?*

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# Back-up Slides