

# Multi-boson production and searches for anomalous gauge couplings at CMS

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On behalf of the CMS Collaboration

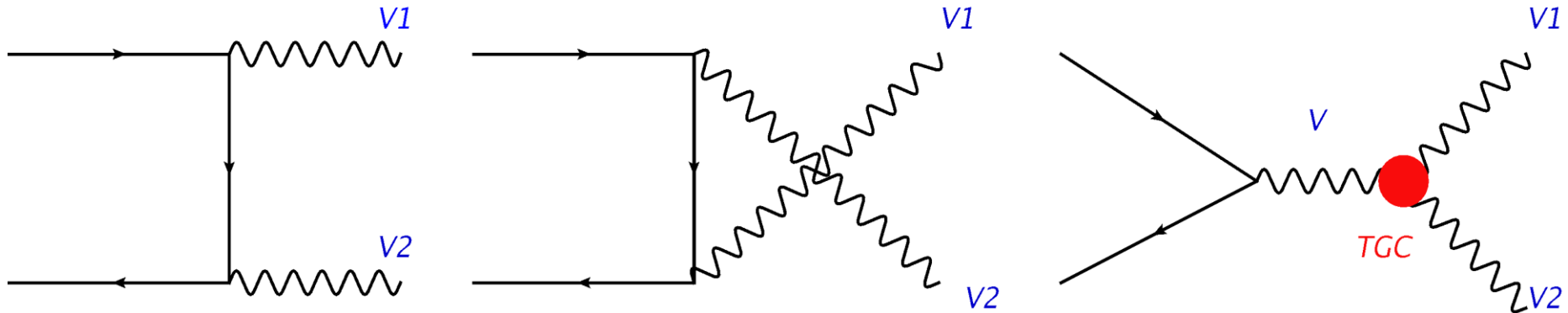


XXIV Workshop on Weak Interactions and Neutrinos

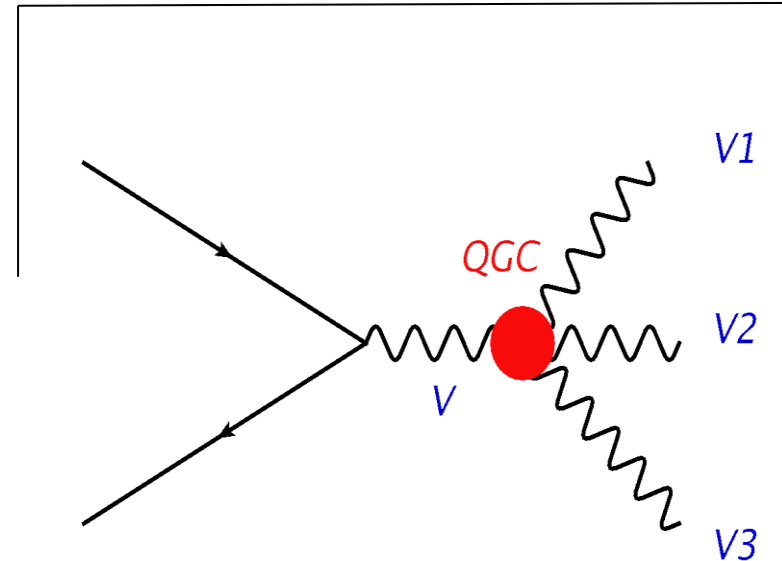
**WIN 2013**

Sep. 16 to 21, 2013

Natal, Brazil



- **Crucial test of the SM:**  
e.g. on the non-Abelian gauge symmetry part of the SM
- **Important backgrounds to Higgs and new physics searches**
- **Sensitive to anomalous Triple (Quartic) Gauge Couplings**  
Indirect probe on new physics



# Overview of CMS results

$$\sigma_S = \frac{N_S}{A_S \cdot \epsilon_S \cdot L}$$



Process (l=e,μ)	Int. Luminosity(fb <sup>-1</sup> )		Xsec Measurement Phase space	aTGC/QGC
	@7TeV	@8TeV		
Wγ → lvγ	5.0	-	E <sub>T</sub> <sup>γ</sup> > 15/60/90 GeV & ΔR(l, γ) > 0.7	WWγ
Zγ → llγ	5.0	-	E <sub>T</sub> <sup>γ</sup> > 15/60/90 GeV & ΔR(l, γ) > 0.7 & M <sub>ll</sub> > 50 GeV	ZZγ, Zγγ
WW+WZ → lvjj	5.0	-	Full	WWγ, WWZ
WW → lvlv	4.9	3.5	Full	WWγ, WWZ
<b>WZ → 3lv</b>	4.9	<b>19.6</b>	71 GeV < MZ < 111 GeV	WWZ
<b>ZZ → 4l, 2l2τ</b>	4.9	<b>19.6</b>	60 GeV < MZ <sub>1,2</sub> < 120 GeV	ZZZ, ZZγ
<b>WWγ+WZγ → lvjjγ</b>	-	<b>19.3</b>	E <sub>T</sub> <sup>γ</sup> > 15 GeV & ΔR(l, γ) > 0.7	WWγγ, WZγγ
<b>γγ</b>	<b>5.0</b>	-	E <sub>T</sub> <sup>γ<sub>1,2</sub></sup> > 40, 25 GeV, ΔR(γ, γ) > 0.7  η <sub>γ</sub>   < 1.44 or 1.57 <  η <sub>γ</sub>   < 2.5	

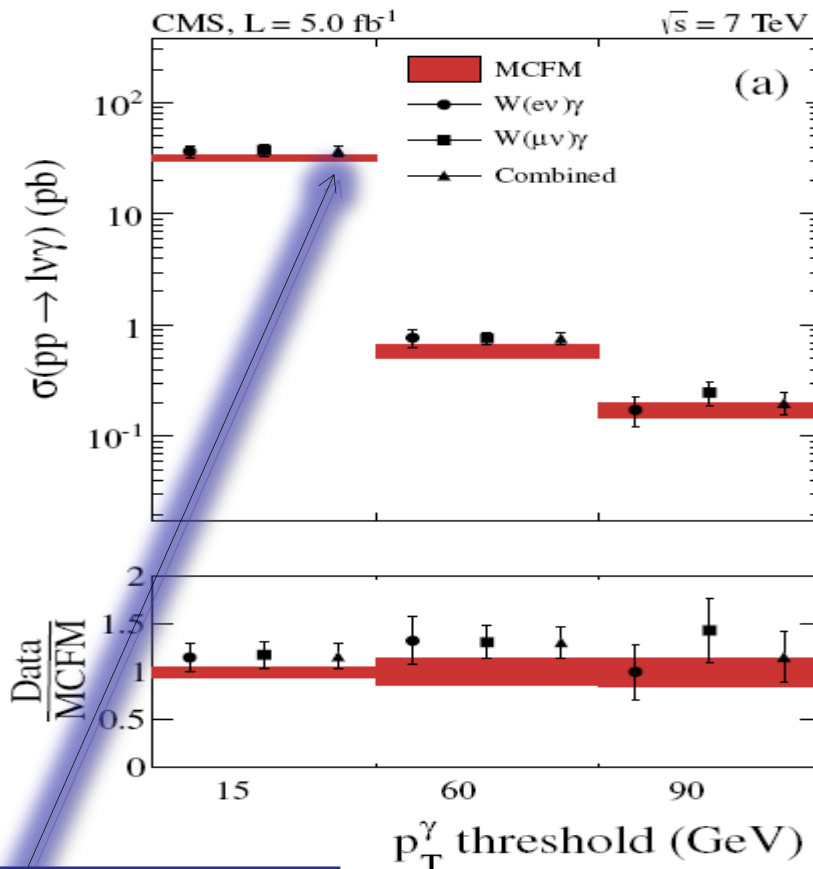
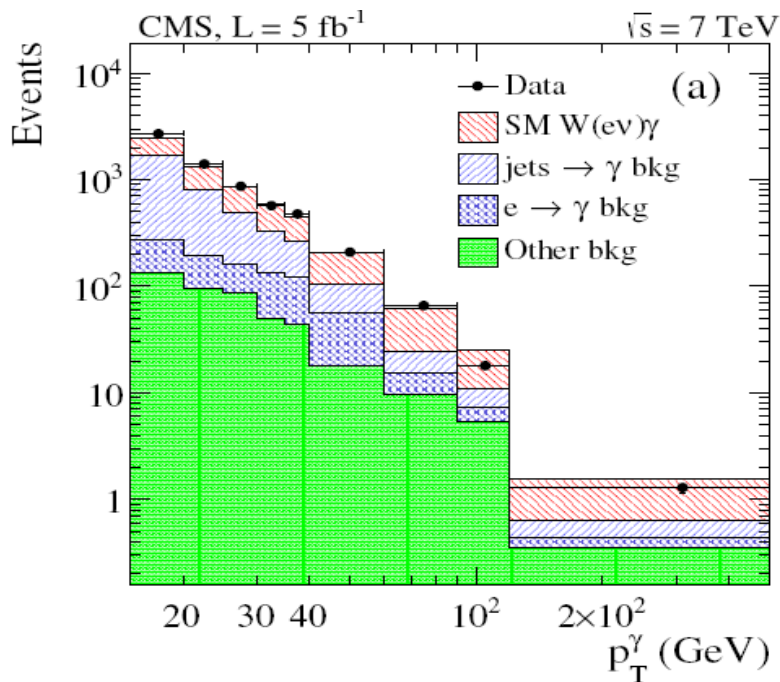
Exclusive γγ → W<sup>+</sup>W<sup>-</sup> not covered here, but will be shown in aQGC comparison

### Events selections:

- ① **Exactly one isolated lepton:**  
 Single Lepton trigger &  $P_T^l > 35\text{GeV}$  &  
 $(|\eta^e| < 2.5 \parallel |\eta^\mu| < 2.1)$
- ② **One isolated photon:**  
 $E_T^\gamma > 15\text{GeV}$  &  $|\eta^\gamma| < 2.5$  &  $\Delta R(l, \gamma) > 0.7$
- ③ **Veto 2<sup>nd</sup> same flavor Lepton**
- ④ **Large W transverse mass:  $M_T^W > 70\text{GeV}$**

### Main Backgrounds from Data-Driven:

- **W+Jets: Jet fake photon**  
→ dominate systematics
- **DY, VV: Electron fake photon**



**MCFM NLO:  $31.8 \pm 1.8 \text{ pb}$**

$\sigma(pp \rightarrow W\gamma) \times \mathcal{B}(W \rightarrow l\nu) = 37.0 \pm 0.8 \text{ (stat.)} \pm 4.0 \text{ (syst.)} \pm 0.8 \text{ (lum.) pb.}$



# $Z\gamma \rightarrow l\bar{l}\gamma$ 7TeV

CMS-PAS-EWK-10-008, Phys. Lett. B 701 (2011) 535,  
arXiv:1105.2758; CMS-PAS-EWK-11-009, arXiv:1308.6832,  
submitted to Phys. Rev. D



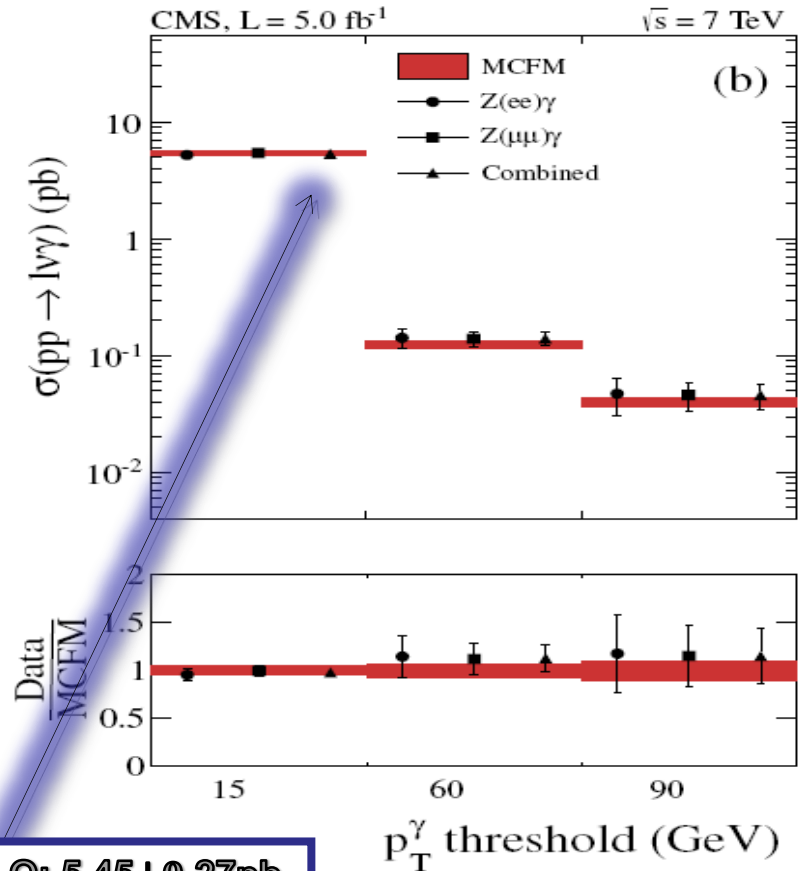
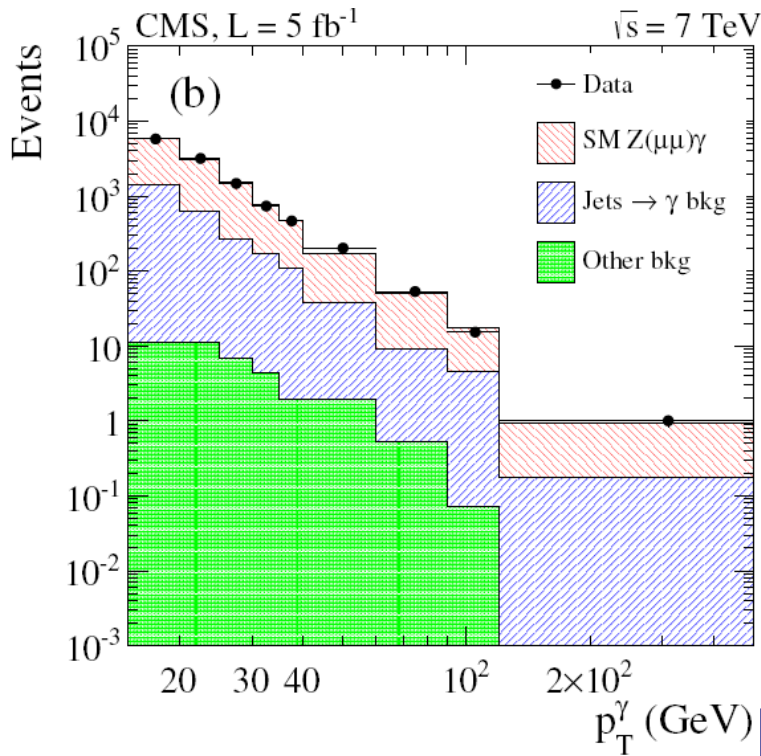
## Events selections:

- ① **Two isolated lepton:**  
Double Lepton trigger &  $P_T^l > 20\text{GeV}$  &  
( $|\eta^e| < 2.5 \parallel |\eta^\mu| < 2.4$ )
- ② **One isolated photon:**  
 $E_T^\gamma > 15\text{GeV}$  &  $|\eta^\gamma| < 2.5$  &  $\Delta R(l, \gamma) > 0.7$
- ③  **$M_{ll} > 50\text{GeV}$**

## Main Backgrounds from Data-Driven:

➤ **Z+Jets: Jet fake photon**

Lep ID/ISO Unc. → dominate systematics



**MCFM NLO:  $5.45 \pm 0.27\text{ pb}$**

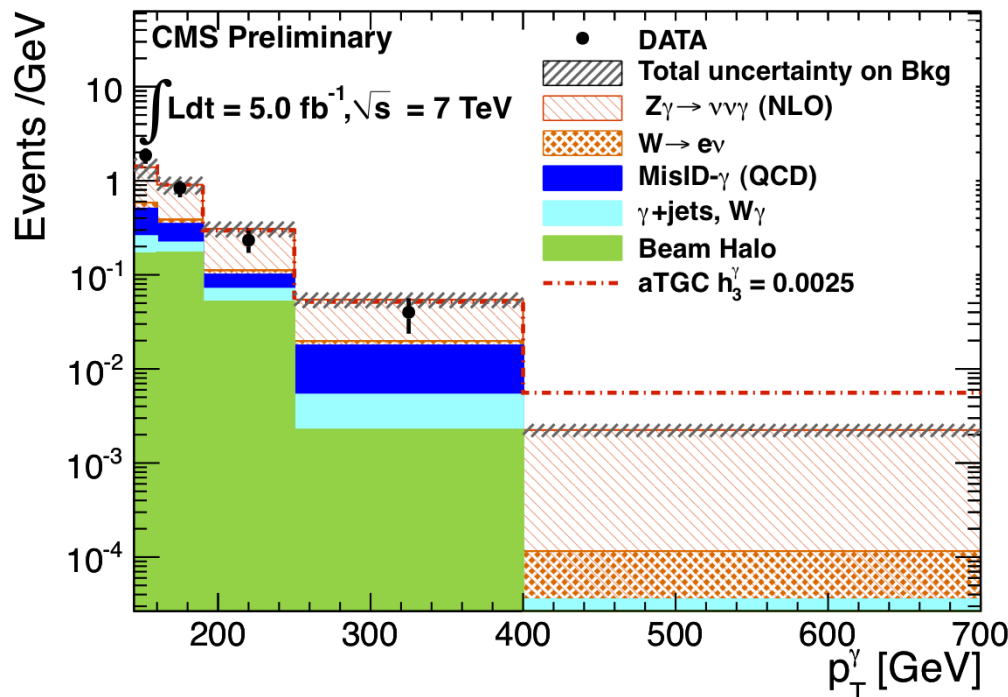
$$\sigma(pp \rightarrow Z\gamma) \times \mathcal{B}(Z \rightarrow l\bar{l}) = 5.33 \pm 0.08 (\text{stat.}) \pm 0.25 (\text{syst.}) \pm 0.12 (\text{lum.}) \text{ pb.}$$

## Events selections:

- ① **One isolated photon:**  
Single  $\gamma$  Trigger &  $E_T^\gamma > 145\text{GeV}$  &  $|\eta^\gamma| < 1.4$
- ② **MET > 130 GeV**
- ③ **Veto additional energetic track**
- ④ **Veto additional energetic Jets near  $\gamma$**

## Main Backgrounds from Data-Driven:

- **Multi-Jets: Jet fake photon**
- **Beam-gas**
- **$W \rightarrow e\nu$  with e fake photon**



Source	Estimate
Misidentified jets	$11.2 \pm 2.8$
Beam-gas processes	$11.1 \pm 5.6$
Misidentified electrons	$3.5 \pm 1.5$
$W\gamma$	$3.3 \pm 1.0$
$\gamma\gamma$	$0.6 \pm 0.3$
$\gamma$ +jet	$0.5 \pm 0.2$
<b>Total</b>	<b><math>30.2 \pm 6.5</math></b>
$Z\gamma \rightarrow \nu\nu\gamma$ (NLO)	$45.3 \pm 6.9$
data	73

$$\sigma_{\text{CMS}} (pp \rightarrow \nu\nu\gamma) = 21.3 \pm 4.2 \text{ (stat.)} \\ \pm 4.3 \text{ (syst.)} \pm 0.5 \text{ (lumi.) fb}$$

$$\sigma_{\text{NLO}} (pp \rightarrow \nu\nu\gamma) = 21.9 \pm 1.1 \text{ fb (from BAUR)}$$



## Events selections:

- ① **Exactly one isolated lepton:**  
Single Lepton trigger &  
( $P_T^e > 35\text{GeV}$  &  $|\eta^e| < 2.5$ ) ||  
( $P_T^\mu > 25\text{GeV}$  &  $|\eta^\mu| < 2.1$ )
- ② **Exactly two PF AK5 Jets with b veto:**  
 $P_T^j > 35\text{GeV}$  &  $|\eta^j| < 2.4$
- ③ **MET > 25 (30) GeV for  $\mu$  (e) channel**
- ④ **Veto additional loose lepton:**  
 $P_T^j > 10$  (20) GeV for  $\mu$  (e) channel
- ⑤  **$M_T^W > 30$  (50) GeV for  $\mu$  (e) channel**

Large Branch Ratio

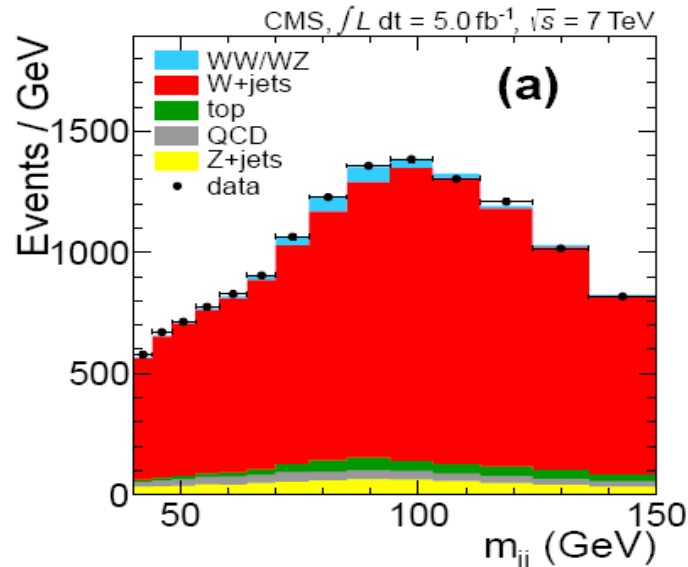
Large Background

Due to Jet resolution, can't distinguish  
WW from WZ

Signal and background yields determined  
with an unbinned likelihood fit to the dijet  
mass spectrum

$$\sigma_{\text{CMS}}(pp \rightarrow WW+WZ) = 68.9 \pm 8.7 \text{ (stat.)} \\ \pm 9.7 \text{ (syst.)} \pm 1.5 \text{ (lumi.) pb}$$

$$\sigma_{\text{NLO}}(pp \rightarrow WW+WZ) = 65.6 \pm 2.2 \text{ pb (from MCFM)}$$



Process	Shape	Constraint on normalization
Diboson (WW+WZ)	MC	Unconstrained
W+jets	MC	$31.3 \text{ nb} \pm 5\%$ (NLO) [30]
$t\bar{t}$	MC	$163 \text{ pb} \pm 7\%$ (NLO) [31]
Single top	MC	$85 \text{ pb} \pm 5\%$ (NNLL) [32–34]
Drell–Yan+jets	MC	$3.05 \text{ nb} \pm 4.3\%$ (NNLO) [35]
Multijet (QCD)	data	$E_T^{\text{miss}}$ fit in data

W+jets: float factorization/renorm & ME-PS matching  
scales to get good modeling of data



7 & 8TeV

qqb, gg(3%) → WW → lνlν

CMS-PAS-SMP-12-013, Phys. Lett. B 721 (2013) 190, arXiv:1301.4698; CMS-PAS-SMP-12-005, arXiv:1306.1126, submitted to EPJC; CMS-PAS-EWK-10-009, Phys. Lett. B 699 (2011) 25, arXiv:1102.5429; CMS-PAS-EWK-11-010



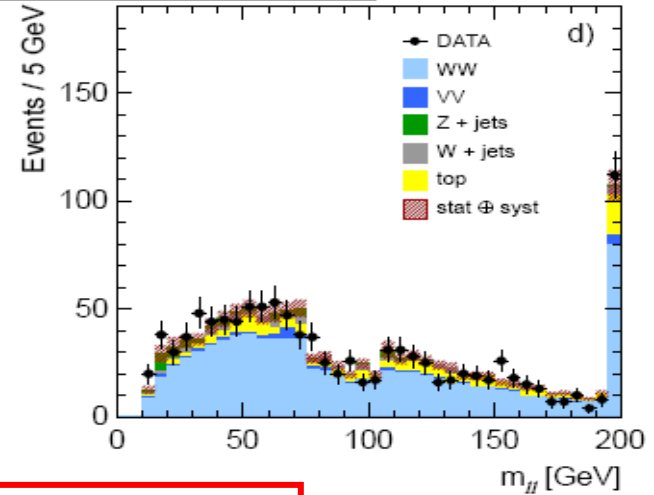
Events selections:

- 1 Two oppositely Charged isolated lepton: Single/Double Lepton trigger & P\_T^l > 20 GeV & (|η^e| < 2.5 || |η^μ| < 2.4)
2 Veto any Jets with: P\_T^j > 30 GeV & |η^j| < 4.7
3 Projected MET > 45 (20) GeV for OF (SF) channel
4 Veto additional loose lepton: P\_T^j > 10 GeV
5 Reject el consistent with a photon conversion
6 Φ(II, J1) < 165 degree, with J1 as the hardest Jet with P\_T^j > 15 GeV
7 Veto |M\_II - M\_Z| < 15 GeV or M\_II < 12 GeV
8 Veto top bkg with b-veto (arXiv:1211.4462)

Table with 2 columns: Channel, l'νl''ν. Rows include W+W-, tt and tW, W+jets, WZ and ZZ, Z/γ\*+jets, Wγ(\*), Total background, Signal + background, Data.

Sys. dominated by Jet veto eff ~4.6%

8 TeV, L = 3.5 fb^-1



Main Backgrounds :

- V+Jets: 3 6 7
Top: 2 8
Di-Boson: 4 5
Driven/Corrected by DATA

Table with 3 columns: Energy, σ\_CMS [pb], σ\_NLO [pb] (MCFM). Rows for 7 TeV and 8 TeV.

Contributions from Higgs ~4% Not included



## Events selections:

### ① Two SF & OC leptons:

Double Lepton trigger

$P_{T11} > 20 \text{ GeV}$  &  $P_{T12} > 10 \text{ GeV}$  &  $|M_{ll} - M_Z| < 20 \text{ GeV}$

In case of multi-Z, choose the one closest to  $M_Z$

### ② A 3<sup>rd</sup> lepton $P_{T13} > 20 \text{ GeV}$

### ③ MET > 30 GeV

### Main Backgrounds from Data-Driven:

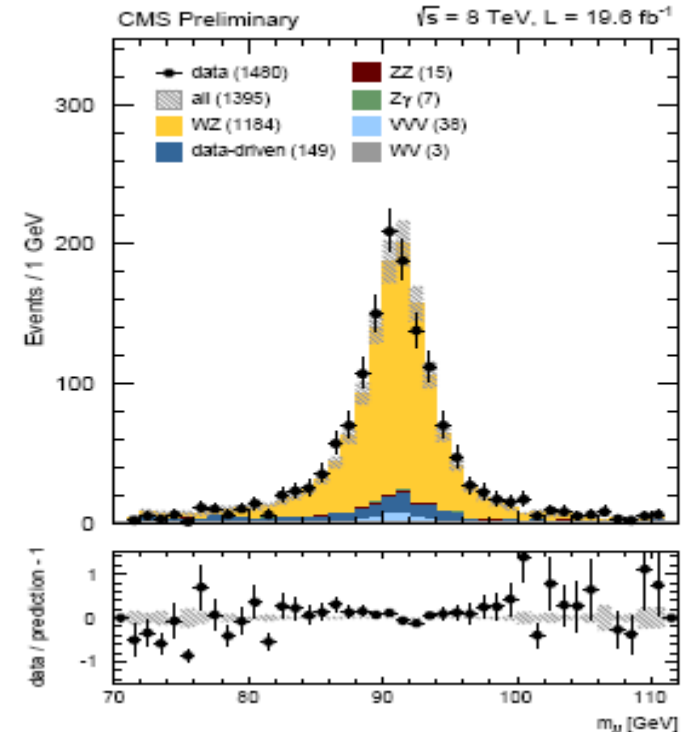
**Z+Jets:** fake or non-isolated lepton from Jets

**ZZ  $\rightarrow$  4l** with one lepton lost

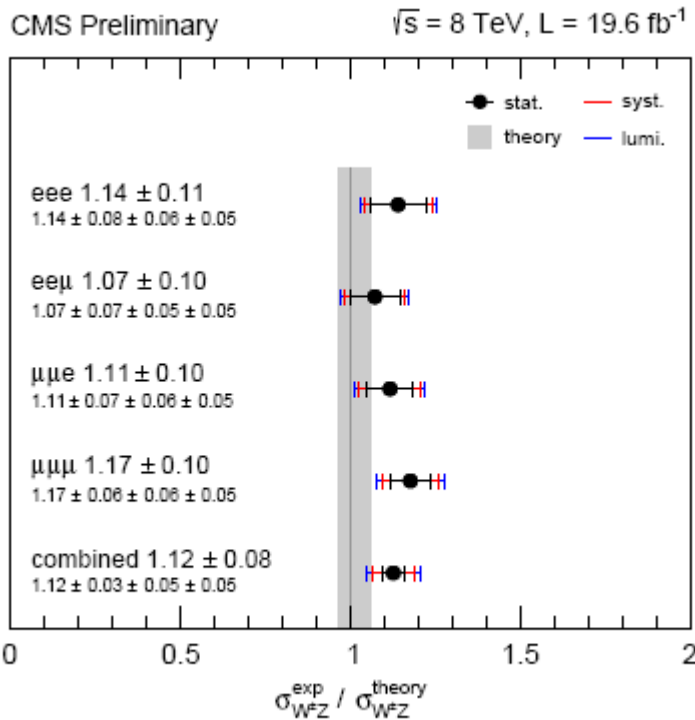
### ZZ/ Z $\gamma$ /VVV from MC

Yields of selected events in data at 8 TeV

sample	eee	ee $\mu$	$\mu\mu e$	$\mu\mu\mu$
Z+jets	$9.8 \pm 4.4$	$16.9 \pm 6.0$	$14.5 \pm 5.4$	$13.8 \pm 4.5$
top	$1.4 \pm 0.4$	$2.7 \pm 0.3$	$6.2 \pm 0.7$	$9.1 \pm 1.0$
ZZ	$2.4 \pm 0.1$	$3.1 \pm 0.1$	$3.9 \pm 0.1$	$5.8 \pm 0.1$
Z $\gamma$	$2.4 \pm 0.9$	$0.4 \pm 0.4$	$3.8 \pm 1.2$	0
WV	$0.1 \pm 0.1$	$0.1 \pm 0.1$	$0.2 \pm 0.1$	$2.2 \pm 0.7$
VVV	$6.1 \pm 0.3$	$7.9 \pm 0.3$	$10.4 \pm 0.4$	$13.4 \pm 0.4$
WZ	$193.9 \pm 1.4$	$245.8 \pm 1.6$	$315.9 \pm 1.9$	$428.0 \pm 2.2$
total MC	$216.0 \pm 4.7$	$277.0 \pm 6.3$	$354.9 \pm 6.0$	$472.3 \pm 5.2$
data-driven	$14.8 \pm 1.4$	$27.1 \pm 2.9$	$47.9 \pm 3.4$	$59.0 \pm 4.6$
data	235	288	400	557



# WZ → 3lv



$$\left(\frac{\sigma_{W+Z}}{\sigma_{W-Z}}\right)_{7 \text{ TeV}} = 1.94 \pm 0.25 \text{ (stat.)} \pm 0.04 \text{ (syst.)}$$

$$\left(\frac{\sigma_{W+Z}}{\sigma_{W-Z}}\right)_{8 \text{ TeV}} = 1.81 \pm 0.12 \text{ (stat.)} \pm 0.03 \text{ (syst.)}$$

The SM prediction for this ratio

at  $\sqrt{s} = 7 \text{ TeV}$  is  $1.776^{+0.006}_{-0.003}$ ,

$1.724 \pm 0.003$  at  $\sqrt{s} = 8 \text{ TeV}$

71 GeV < MZ < 111 GeV

Statistical Uncertainty dominates

MCFM NLO

$$\sigma(\text{pp} \rightarrow \text{WZ} + \text{X}; \sqrt{s} = 7 \text{ TeV}) = 20.76 \pm 1.32 \text{ (stat.)} \pm 1.13 \text{ (syst.)} \pm 0.46 \text{ (lumi.) pb}$$

$$17.8^{+0.7}_{-0.5} \text{ pb}$$

$$\sigma(\text{pp} \rightarrow \text{WZ} + \text{X}; \sqrt{s} = 8 \text{ TeV}) = 24.61 \pm 0.76 \text{ (stat.)} \pm 1.13 \text{ (syst.)} \pm 1.08 \text{ (lumi.) pb}$$

$$21.91^{+1.17}_{-0.88} \text{ pb}$$



7 & 8 TeV NEW

# ZZ → 4l, 2l2τ

CMS-PAS-SMP-13-005; CMS-PAS-SMP-12-014, Phys. Lett. B 721 (2013) 190, arXiv:1301.4698; JHEP 01(2013)063, arXiv:1211.4890; CMS-PAS-EWK-11-010

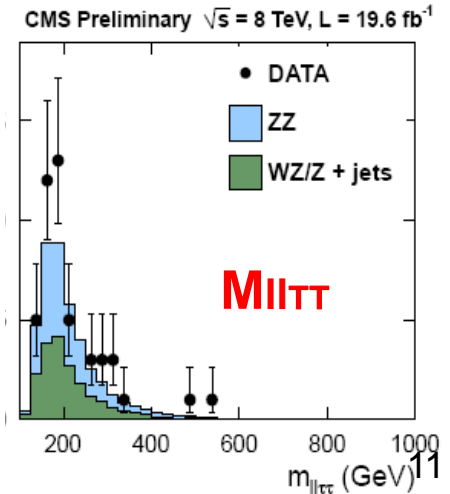
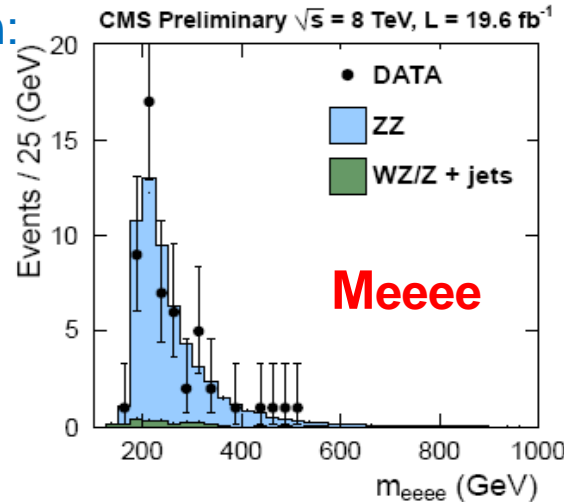


4l	2l2τ
<b>Double lepton or Triple-electron triggers</b>	
$60\text{GeV} < M_{Z_{1,2}} < 120\text{GeV}$	$60\text{GeV} < M_{ll} < 120\text{GeV}$
$M_{ll} > 4\text{GeV}$	$20(30)\text{GeV} < M^{\text{vis}}_{\tau\tau} < 120\text{GeV}$ for $\tau_e\tau_\mu$ (all others)
$P_T^{l1} > 20\text{GeV}, P_T^{l2} > 10\text{GeV},$	$P_T^{l1} > 20\text{GeV}, P_T^{l2} > 10\text{GeV},$ $P_T(\tau_e, \tau_\mu) > 10\text{GeV}, P_T(\tau_h) > 20\text{GeV}$
FSR Photon Recovered with $M_{ll\gamma} < 100\text{GeV}$	No FRS photon recovery

## Main Backgrounds from Data-Driven:

- **Z/WZ+Jets:**  
Jet fake l or τ
- **Ttbar and Zbb:**  
Heavy Flavor Jets

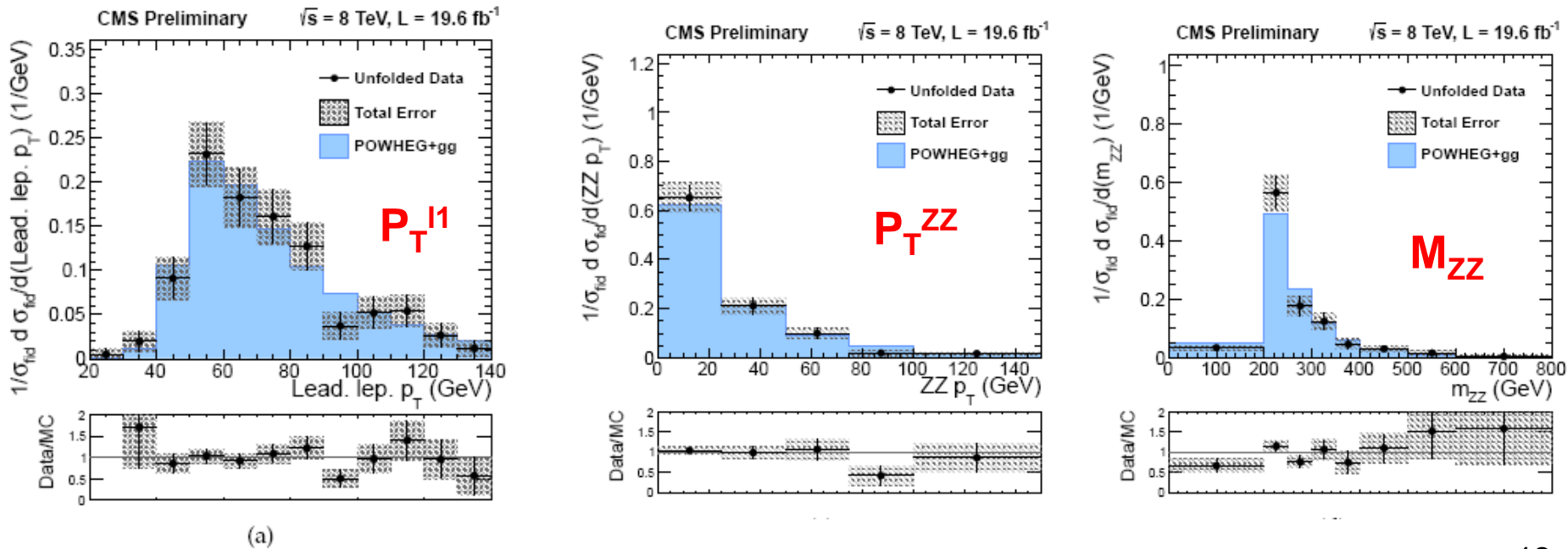
**Main systematic uncertainty:**  
tau reconstruction



# ZZ → 4l, 2l2τ

		<b>MCFM NLO qq + LO gg</b>	
<b>7 TeV</b>	$6.24^{+0.86}_{-0.80}(\text{stat.})^{+0.41}_{-0.32}(\text{sys.}) \pm 0.14(\text{lumi.})$	<b>6.3 ± 0.4</b>	<b>pb</b>
<b>8 TeV</b>	$7.7 \pm 0.5(\text{stat.}) \pm 0.6(\text{syst.}) \pm 0.4(\text{theo.}) \pm 0.3(\text{lumi.})$	<b>7.7 ± 0.6</b>	<b>pb</b>

The differential distributions normalized to fiducial cross sections



## Events selections:

① Exactly one isolated lepton:

Single Lepton trigger &  
 $(P_T^e > 35\text{GeV} \ \& \ |\eta^e| < 2.5)$  ||  
 $(P_T^\mu > 25\text{GeV} \ \& \ |\eta^\mu| < 2.1)$

② Two PF AK5 Jets with b veto:

$P_T^j > 30\text{GeV} \ \& \ |\eta^j| < 2.4$

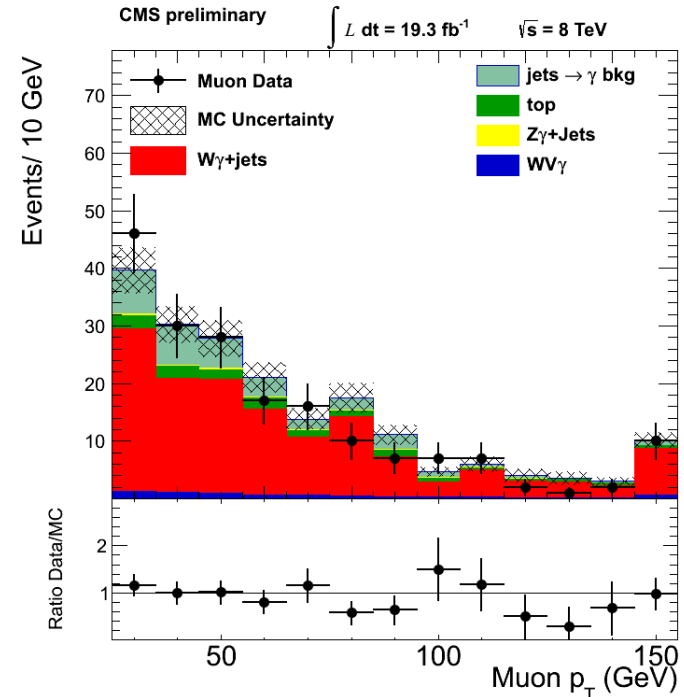
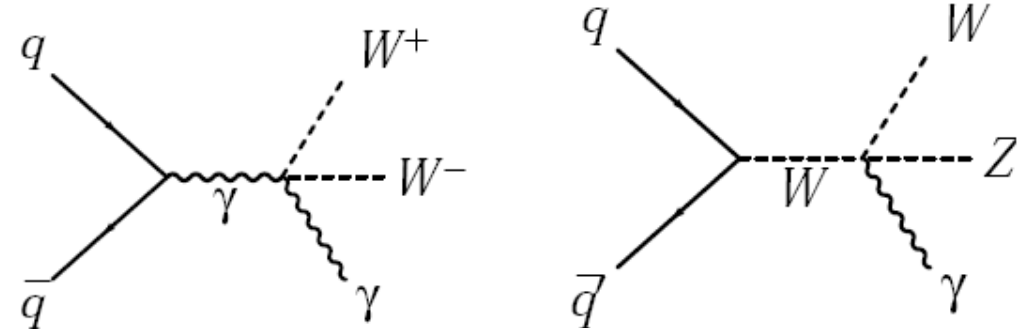
③ MET > 35 GeV

④  $\Delta\phi(\text{MET}, J1) > 0.4, \ R_{j\gamma} > 0.5, \ R_{l\gamma} > 0.5$

⑤  $M_T^W > 30 \text{ GeV}$

⑥  $|M_{\nu e} - M_z| > 10\text{GeV}$

⑦  $|\Delta\eta_{jj}| < 1.4, \ 70\text{GeV} < M_{jj} < 110\text{GeV}$



## Main Backgrounds from Data-Driven:

- $W\gamma + \text{Jets}$ : sideband
- Fake Photon: ratio method

$\sigma(WV\gamma) < 241\text{fb}, \ 3.4 \text{ times SM } (70.3\text{fb})$   
 $E_T^\gamma > 15\text{GeV}$

## YY

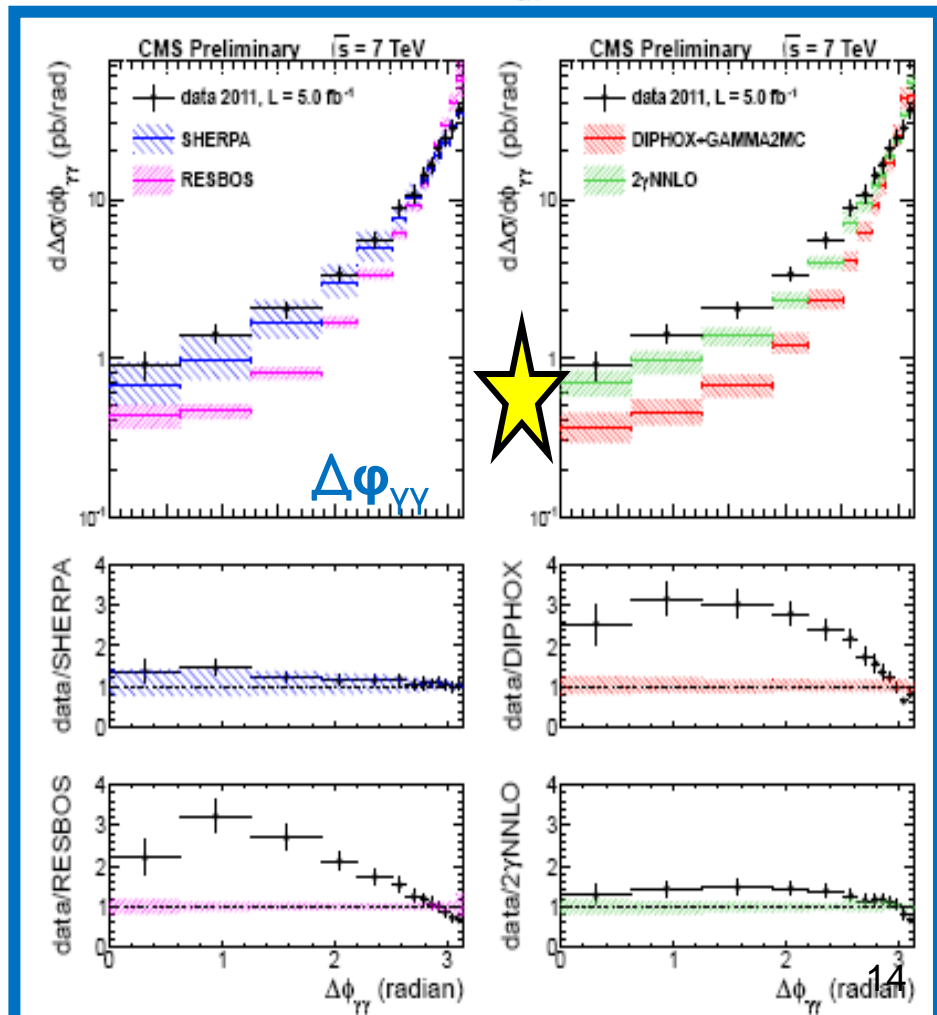
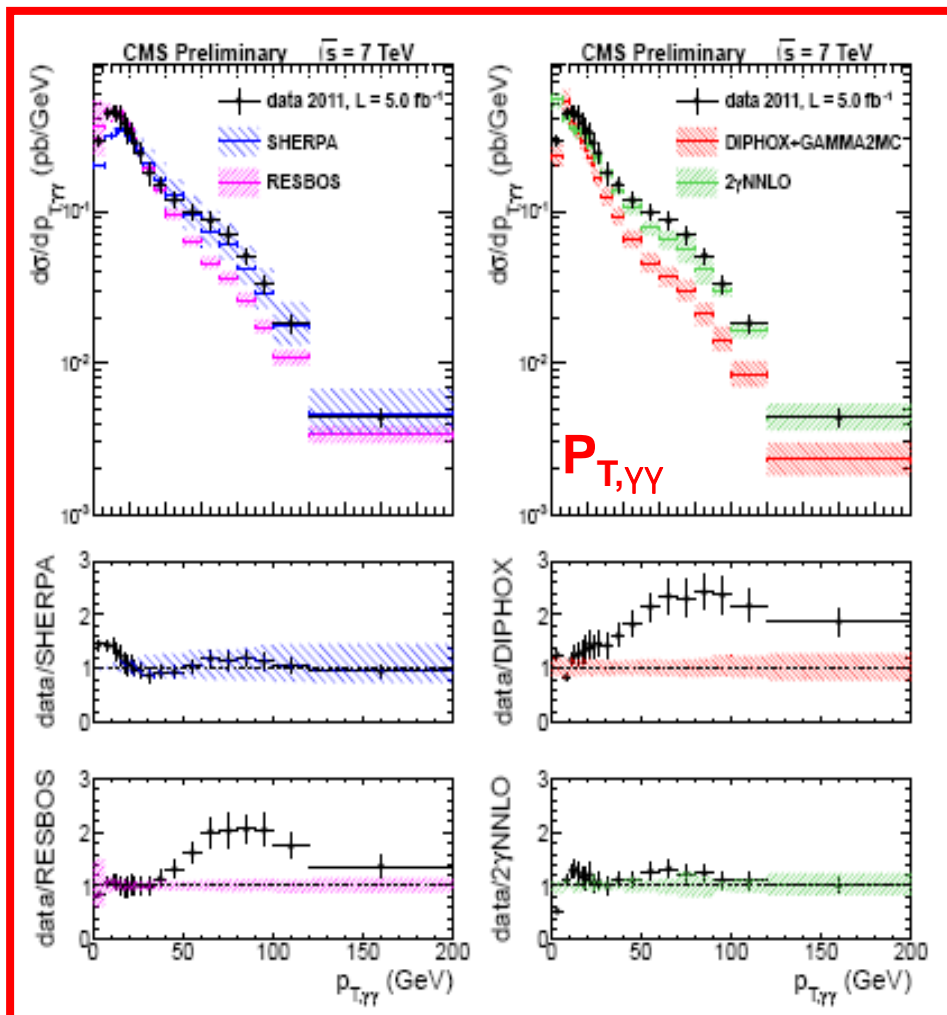
$$\sigma_{data} = 16.8 \pm 0.2 \text{ (stat.)} \pm 1.8 \text{ (syst.)} \pm 0.4 \text{ (lumi) pb}$$

$$\sigma_{NNLO(2\gamma NNLO)} = 16.2^{+1.5}_{-1.3} \text{ (scale) pb}$$

$$\sigma_{NLO(DIPHOX+GAMMA2MC)} = 12.8^{+1.6}_{-1.5} \text{ (scale)}^{+0.6}_{-0.8} \text{ (pdf} + \alpha_s) \text{ pb}$$

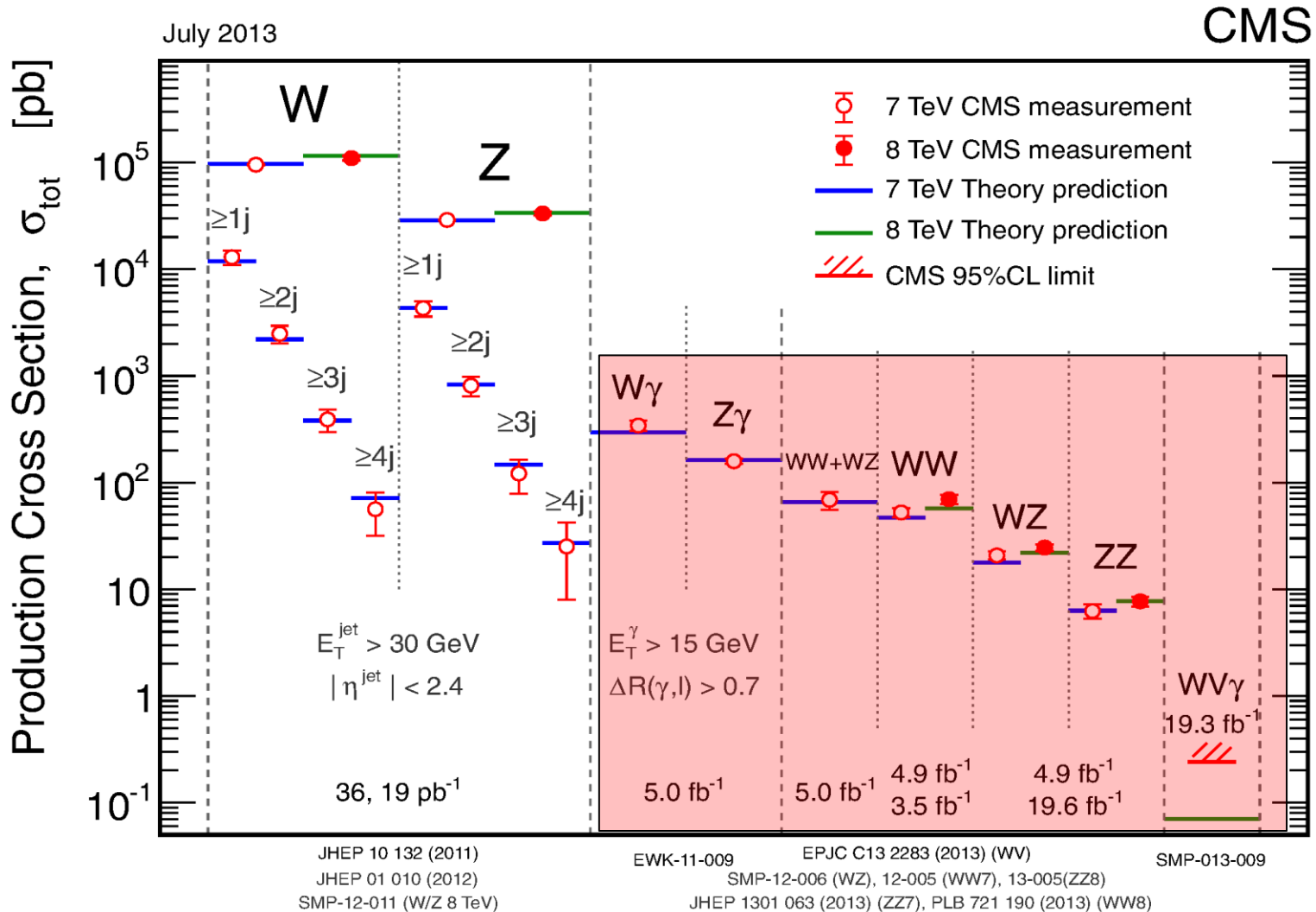
$$\sigma_{NLO(RESBOS)} = 14.9^{+2.2}_{-1.7} \text{ (scale)} \pm 0.6 \text{ (pdf} + \alpha_s) \text{ pb}$$

$$\sigma_{LO(SHERPA)} = 15.2^{+3.2}_{-1.9} \text{ (scale) pb}$$





# Summary of the Xsec Measurement



- **ATGC and AQGC are less well measured in EWK**
- **They are signature of New Physics**
- **At hard tail of phase space, they increase Xsec significantly**

**Charged aTGCs**  $WW_\gamma/WWZ$   
 HISZ (LEP) parametrization  
 $\lambda_\gamma = \lambda_z = \lambda$   
 $\Delta K_Z = \Delta g^Z_1 - \Delta K_\gamma \cdot \tan^2 \theta_w$   
 NPB282 (1987) 253; PRD41 (1990) 2113

**aQGCs**  $WW_\gamma\gamma/WWZ_\gamma$  EPJC 13 (2000) 283  
 Now under Dim8 Framework, where operators can be recombined to get the same Lorentz structure Dim6 operators as in LEP  
 $\mathbf{a}_0^W, \mathbf{a}_c^W$  as well as other pure Dim8 ones:  

$$\mathcal{L}_{aQGC} = \frac{a_0^W}{4g^2} \mathcal{W}_0^\gamma + \frac{a_c^W}{4g^2} \mathcal{W}_c^\gamma + \sum_i \kappa_i^W \mathcal{W}_i^Z + \mathcal{L}_{T,0} + \mathcal{L}_{T,1} + \mathcal{L}_{T,2}$$

**Neutral aTGCs**  
 Zy channel:  $Z\gamma\gamma/ZZ\gamma$   
 $\mathbf{h}_3^{Z,\gamma}, \mathbf{h}_4^{Z,\gamma}$   
 PRD47 (1993) 4889  
 ZZ channel:  $ZZ\gamma/ZZZ$   
 $\mathbf{f}_4^{Z,\gamma}, \mathbf{f}_5^{Z,\gamma}$   
 NPB282 (1987) 253

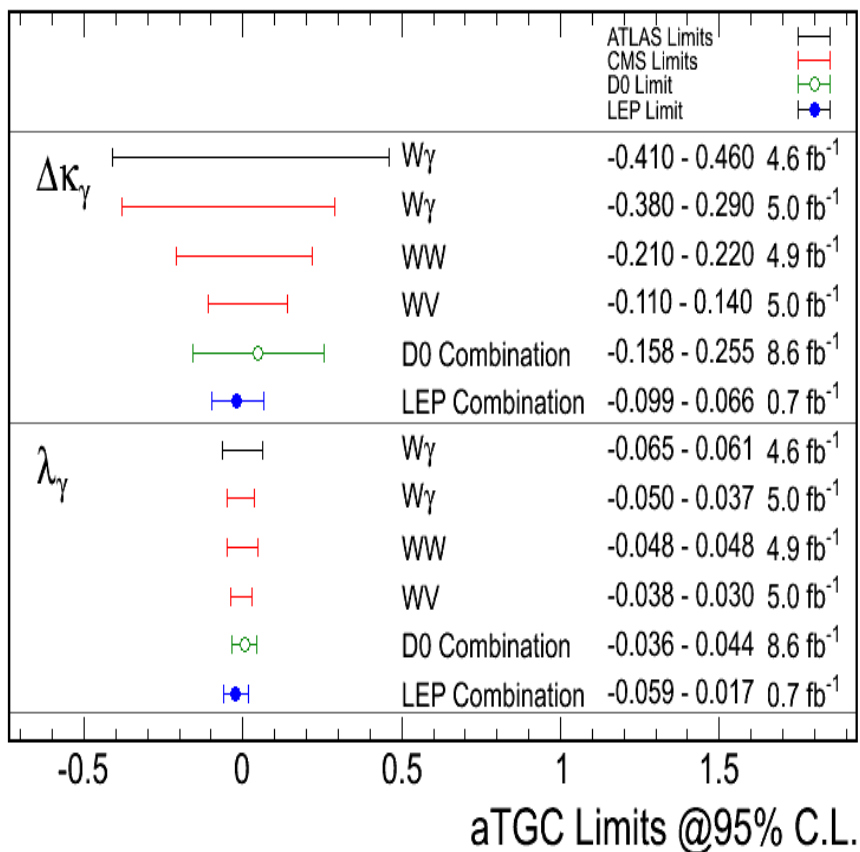
- *Without Form factor for aTGC*
- *With and Without for aQGC*
- *CLs and profile likelihood methods used to set the upper limit*

# Triple and Quartic Anomalous Gauge Couplings

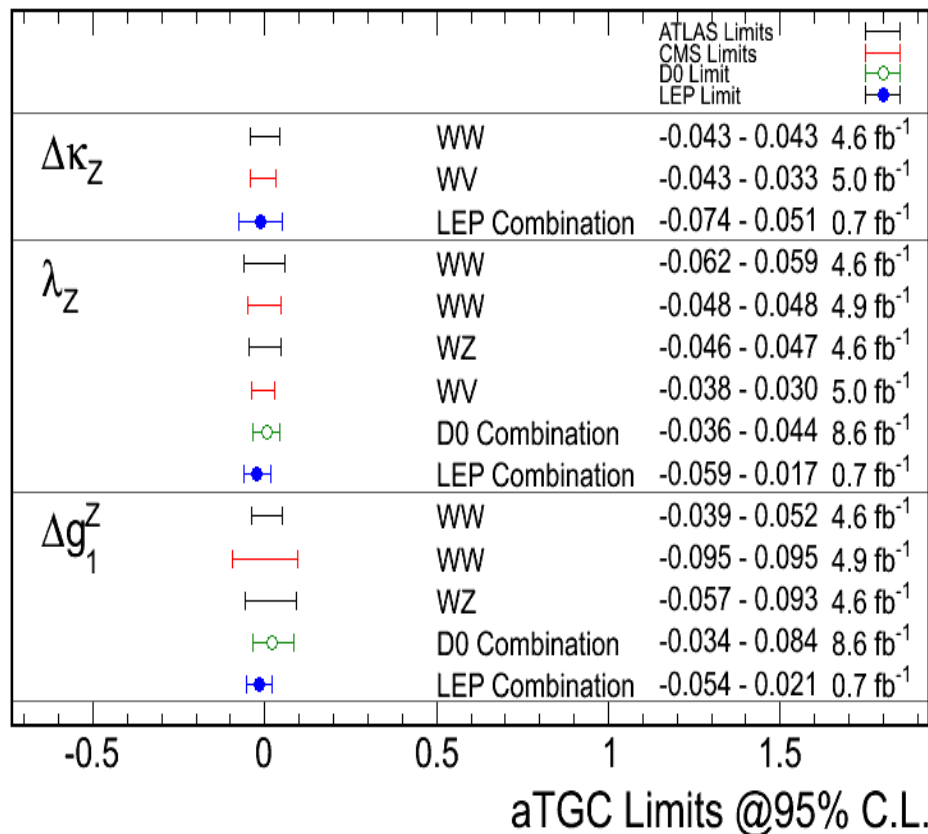
Process ( $l=e,\mu$ )	aTGC/QGC Parameters		Limit Setting variable
$W\gamma \rightarrow l\nu\gamma$	$WW\gamma$	$\lambda_\gamma, \Delta K_\gamma$	$E_T^\gamma$
$Z\gamma \rightarrow ll\gamma$	$ZZ\gamma, Z\gamma\gamma$	$h_3^{Z,\gamma}, h_4^{Z,\gamma}$	$E_T^\gamma$
$Z\gamma \rightarrow \nu\nu\gamma$	$ZZ\gamma, Z\gamma\gamma$	$h_3^{Z,\gamma}, h_4^{Z,\gamma}$	$E_T^\gamma$
$WW+WZ \rightarrow l\nu jj$	$WW\gamma, WWZ$	$\lambda_z, \Delta K_\gamma$	$P_T^{jj}$
$WW \rightarrow l\nu l\nu$	$WW\gamma, WWZ$	$\lambda_z, \Delta K_\gamma, \Delta g_1^Z$	Max $P_T^l$
$ZZ \rightarrow 4l, 2l2\tau$	$ZZZ, ZZ\gamma$	$f_4^{Z,\gamma}, f_5^{Z,\gamma}$	$M_{4l}$
$WW\gamma+WZ\gamma \rightarrow l\nu jj\gamma$	$WW\gamma\gamma, WZ\gamma\gamma$	$a_0^w, a_c^w, f_0^T, K_0^w, K_c^w$	$E_T^\gamma$
$\gamma\gamma \rightarrow W^+W^-$	$WW\gamma\gamma$	$a_0^w, a_c^w$	$P_T^{ll}$

# Charged aTGCs

Feb 2013

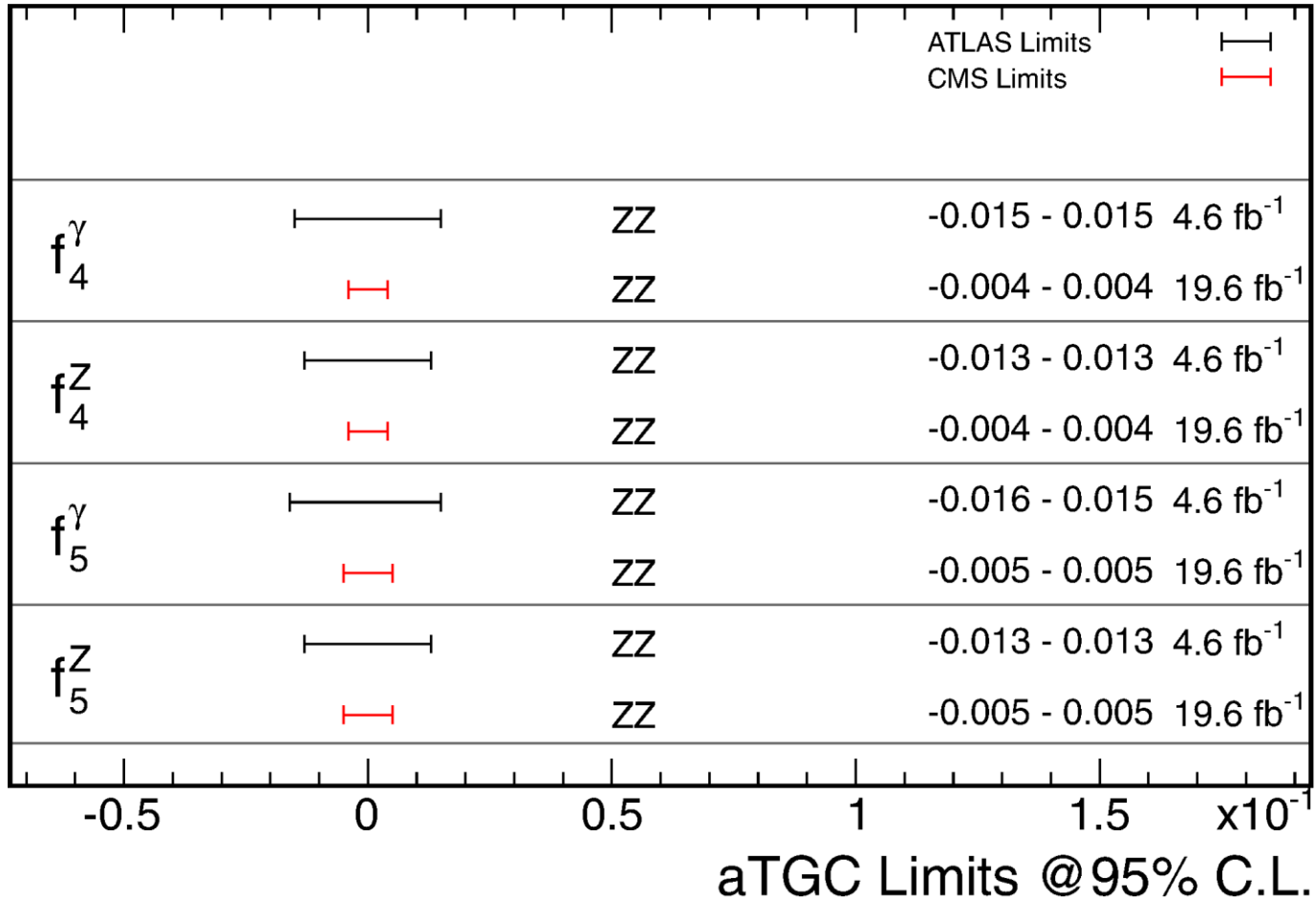


Feb 2013

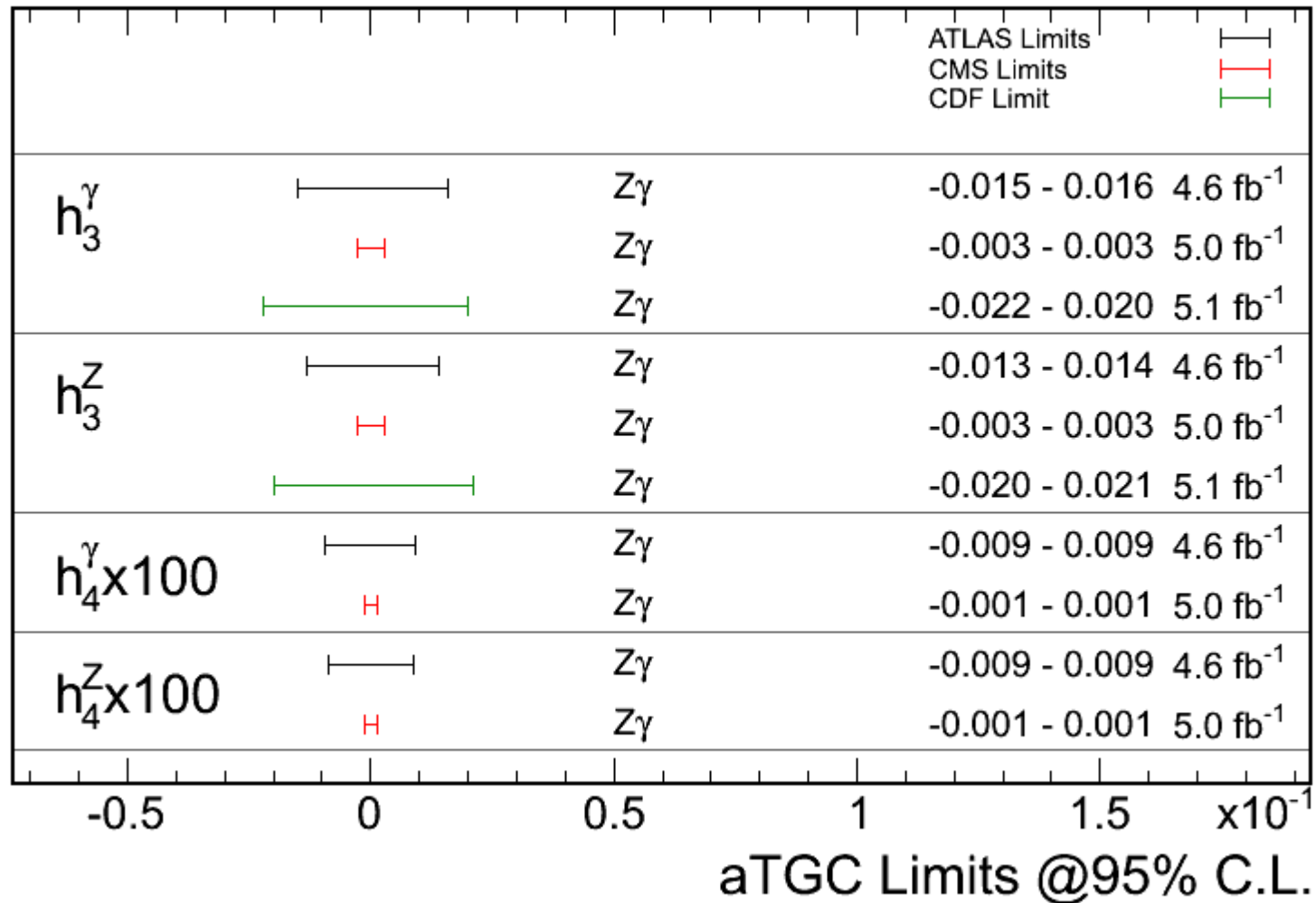


# Neutral aTGCs

July 2013



Feb 2013





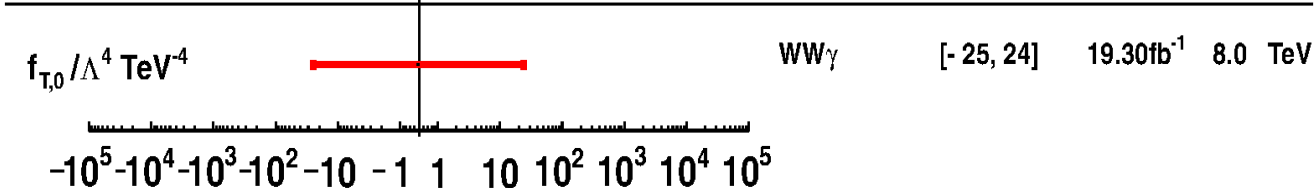
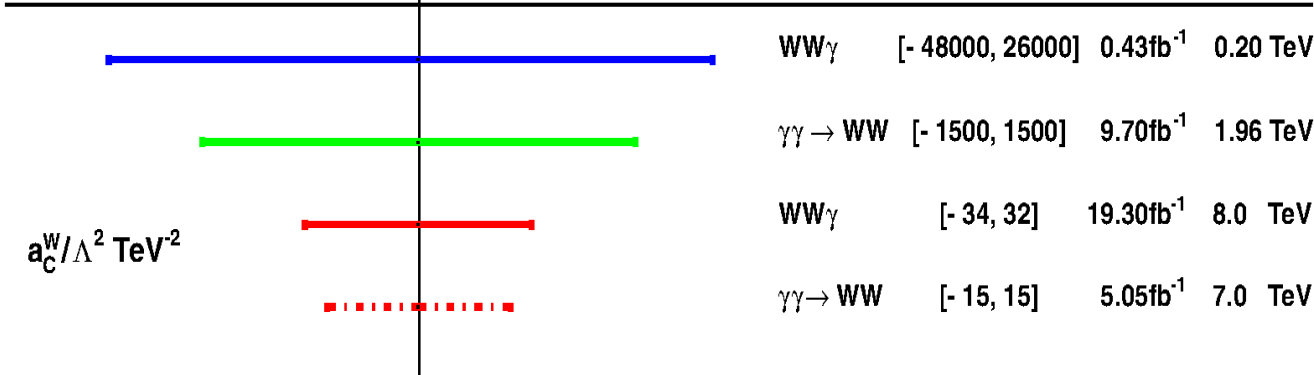
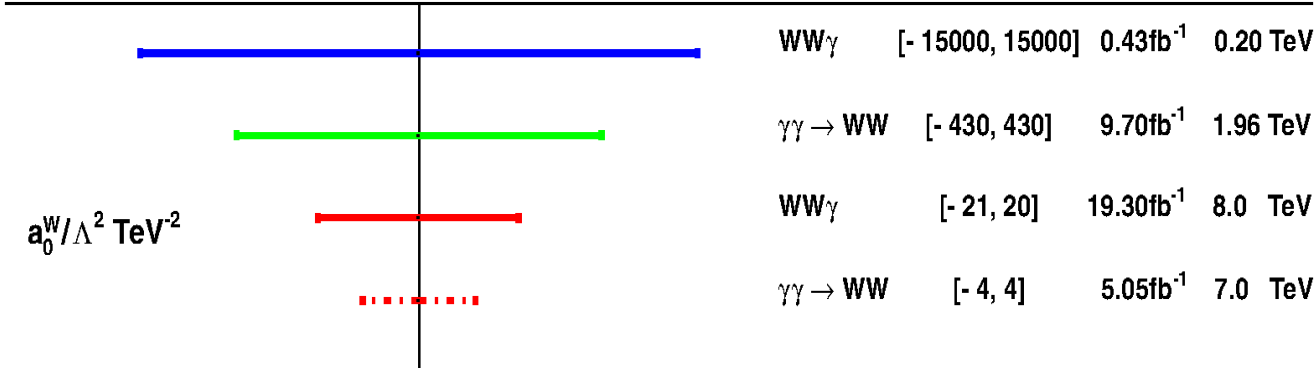
July 2013

LEP L3 limits  
D0 limits

— CMS  $WW\gamma$  limits  
— CMS  $\gamma\gamma \rightarrow WW$  limits

Anomalous  $WW\gamma\gamma$  Quartic Coupling limits @95% C.L.

Channel Limits L  $\sqrt{s}$



$WW\gamma+WZ\gamma \rightarrow l\nu jj\gamma$

$$-25 < f_{T,0}/\Lambda^4 < 24 \text{ TeV}^{-4},$$

$$-12 < \kappa_0^W/\Lambda^2 < 10 \text{ TeV}^{-2}, \text{ and}$$

$$-18 < \kappa_C^W/\Lambda^2 < 17 \text{ TeV}^{-2}.$$

# Summary

- **Various Multi (2 or 3) boson processes have been measured by CMS with 2011 or 2012 dataset.**

WZ/ZZ updated with 8TeV full dataset

$\gamma\gamma$  7TeV measurement public now

Xsec in agreement with NLO/NNLO theoretical results

First measurement on triple gauge boson productions:  $WV\gamma$

- **Stringent limits set on charged and neutral aTGC**
- **First measurement on aQGC at the LHC from two channels**

First ever limits on  $f_T^0$ ,  $K_0^W$ ,  $K_C^W$



# Backup

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## CMS bkg from data determination methods



Used for:

### Fake rate method (often used for fake leptons, jets misidentified as leptons)

- Select data control sample dominated with background to measure the probability ("fake rate"=FR) for a loose lepton object (fake lepton) to pass the tight requirements used in the selection
- Use the FR to extrapolate the yield from a loose lepton sample (background enriched) to the fully selected leptons

WW (*W+jet bkg*)  
ZZ (*Z+jet, WZ+jet, tt bkg*)

### Template fit method (often used for fake photons, jets misidentified as photons)

- Perform a two component fit using the signal and background templates in discriminating observable

Vgamma (*V+jet bkg*)  
WW+WZ→2l2j  
(*W+jets bkg*)

### Data/MC scale factor

- Using the data control sample dominated with background to rescale the simulation

WW (*W $\gamma$ \* bkg*)

### Measurement of efficiency

- Measurement of the selection efficiency and applying it to background dominated data control sample

WW (*tt bkg*)

5

# $W\gamma \rightarrow l\nu\gamma$ ( $l=e,\mu$ )

## RAZ (Radiation-amplitude Zero) Measurement:

**Veto Jets with  $P_T > 30\text{GeV}$ ,  
 $M_T(l\gamma \text{ MET}) > 110\text{GeV}$**

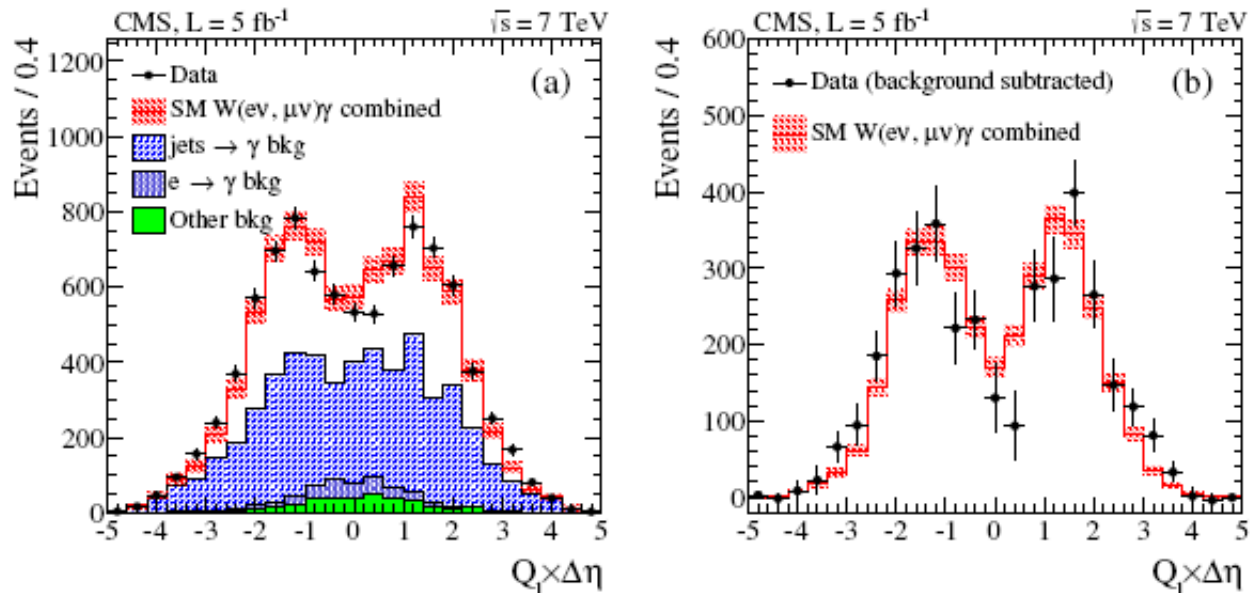
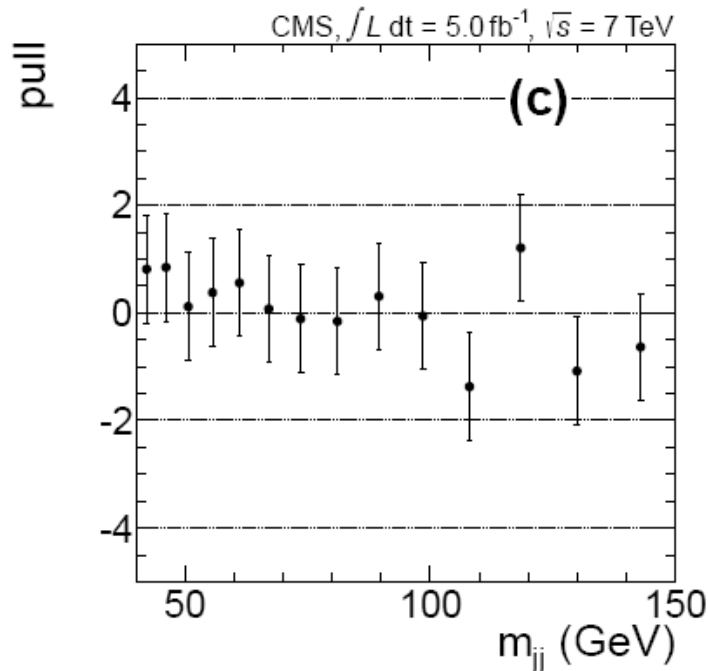


Figure 7: Charge-signed rapidity difference  $Q_\ell \times \Delta\eta$  between the photon candidate and a lepton for  $W\gamma$  candidates in data (filled circles) and expected SM signal and backgrounds (shaded regions) normalized to (a) data, and (b) background-subtracted data. The hatched bands illustrate the full uncertainty in the MC prediction.



W+jets: float factorization/renorm & ME-PS matching scales to get good modeling of data

$$F_{W+\text{jets}} = \alpha \mathcal{F}_{W+\text{jets}}(\mu_0^2, q'^2) + \beta \mathcal{F}_{W+\text{jets}}(\mu'^2, q_0^2) + (1 - \alpha - \beta) \mathcal{F}_{W+\text{jets}}(\mu_0^2, q_0^2),$$

validate the fit procedure by performing pseudo-experiments.

where  $\mathcal{F}_{W+\text{jets}}$  denotes the  $m_{jj}$  shape from simulation. The parameters  $\mu_0$  ( $\mu'$ ) and  $q_0$  ( $q'$ ) correspond to the default (alternative) values of  $\mu$  and  $q$ , respectively. The parameters  $\alpha$  and  $\beta$  are free to vary during the fit and remain within the physical ranges ( $0 \leq \alpha, \beta \leq 1$  and  $1 - \alpha - \beta \geq 0$ ). We take  $\mu' = 2\mu_0$  or  $0.5\mu_0$  ( $q' = 2q_0$  or  $0.5q_0$ ), depending on which alternative sample provides a better fit to the data. Thus, the fit probes variations of a factor of two in both  $\mu$  and  $q$  (with the corresponding shape fluctuations accounted for when setting exclusion limits).



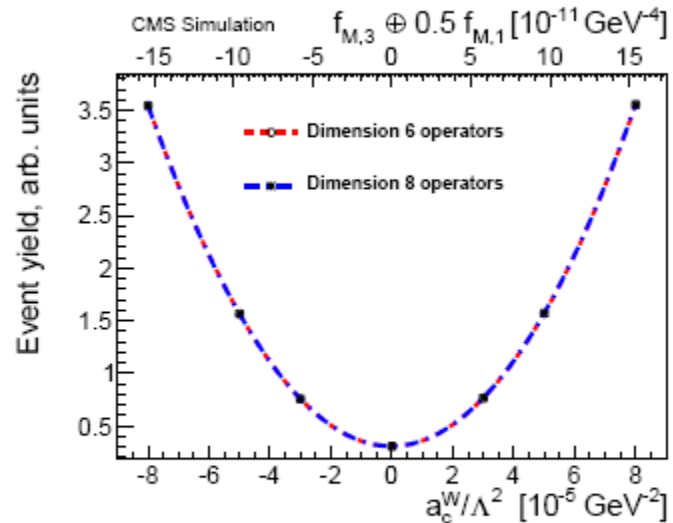
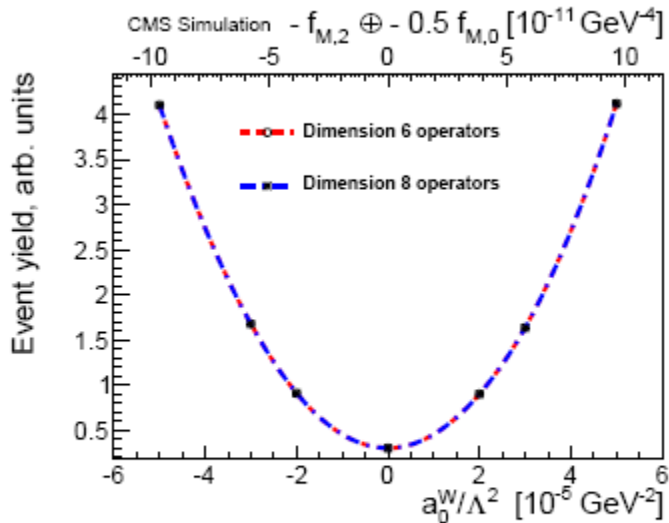


Figure 2: Dimension 8 parameters  $f_{M,i}$  are related to dimension 6 parameters  $a_0^W, a_C^W$  via a simple linear transformation.

