

# bending and focusing with plasmas and crystals - potential and challenges

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# outline

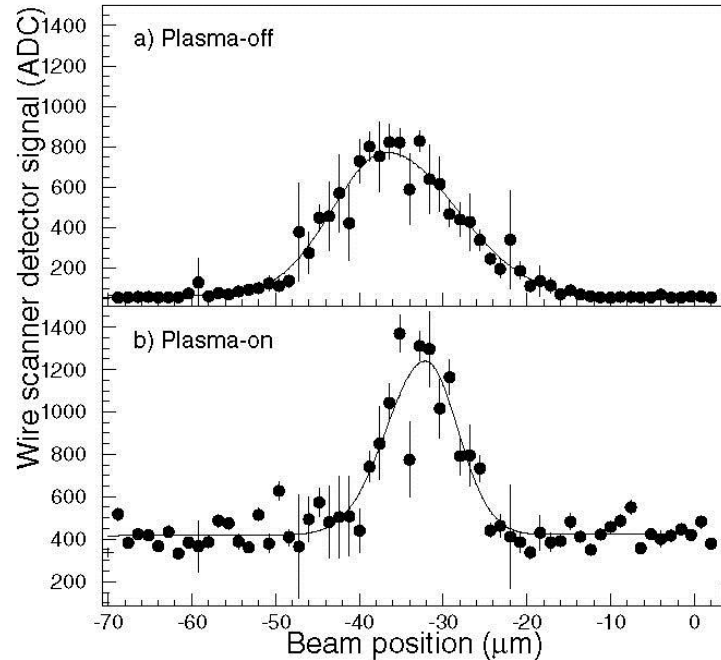
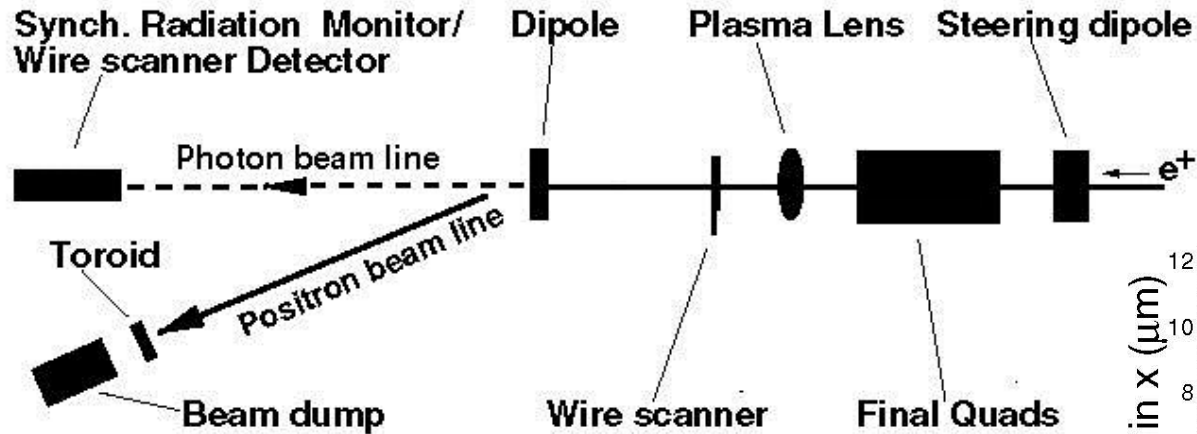
- plasmas
  - plasma lenses
  - plasma wiggler
  - plasma dipole
- crystals
  - crystal channeling & reflection
  - leptons in crystals
  - crystal accelerators
  - crystalline beams

# plasma focusing: plasma lens

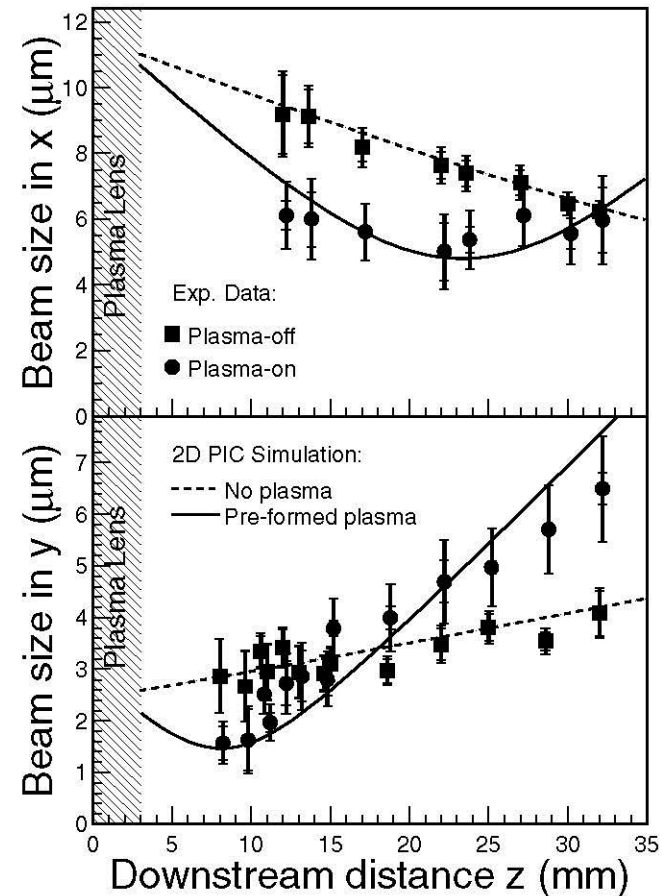
- proposed as **final focusing element for future high energy electron-positron colliders**
  - P. Chen, 1987
- early experiments with  $e^-$  at low energy (50 MeV)
  - J. Rosenzweig, H, Nakanishi etc, 1990, 1991
- **SLAC FFTB experiment** (2001): focusing of **28.5 GeV  $e^+$  beam** using plasma formed by ionizing a 3-mm  $N_2$  gas jet; **simultaneous focusing in both transverse dimensions**
- effective focusing strength:  **$10^6$  T/m** plasma density  
 $n \approx 5 \times 10^{17} \text{ cm}^{-3}$

# plasma lens @ FFTB (2001)

J. S. T. Ng et al,  
Phys. Rev. Letters  
87, 24 (2001)

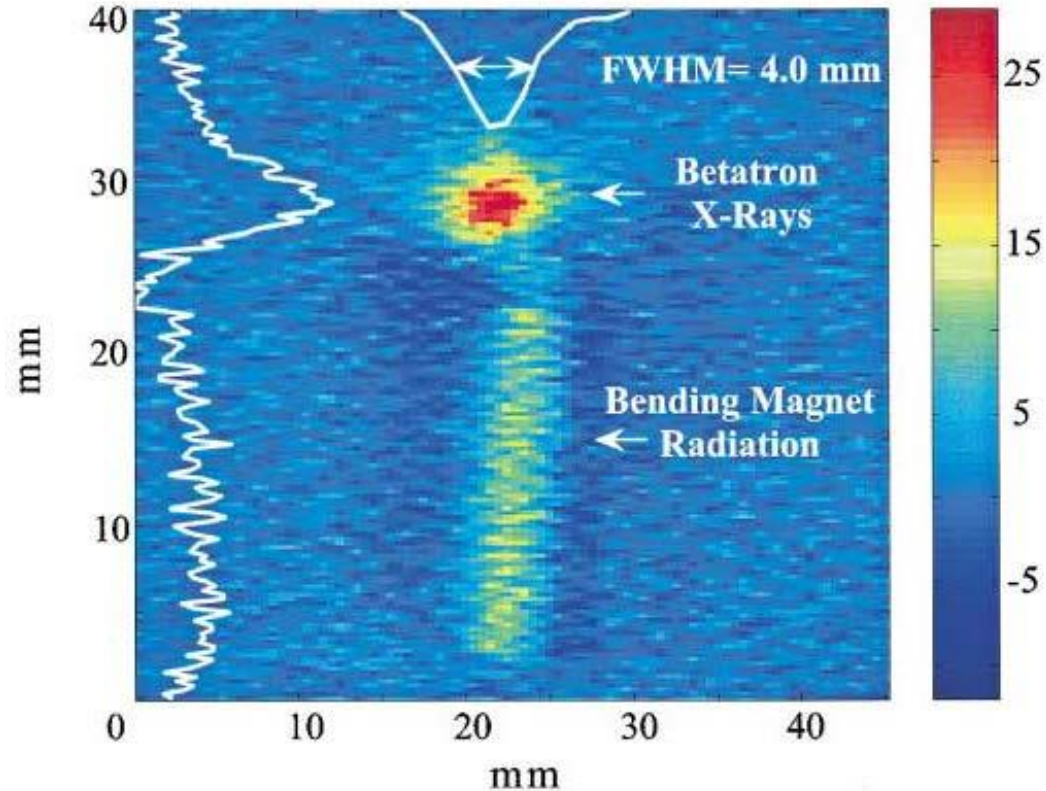
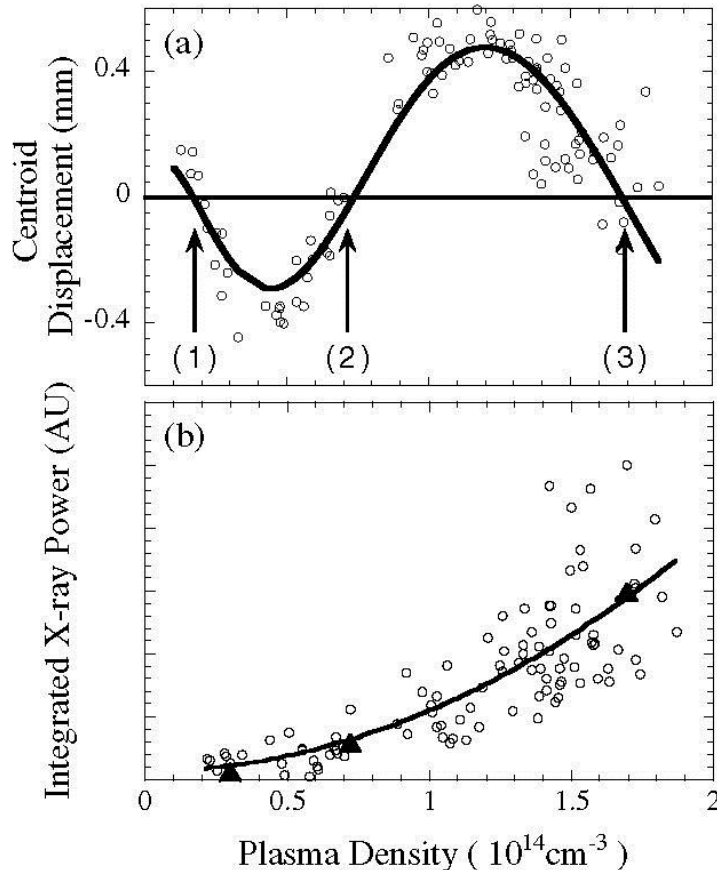


minimum  
area of  
beam  
spot  
reduced  
by factor  
 $\sim 2$



# plasma betatron wiggler: FFTB (2001)

$n=1.7 \times 10^{14} \text{ cm}^{-3}$ : focusing force  $\sim 5 \times 10^6 \text{ T/m}$ ,  
shrinking beam size from  $40 \mu\text{m}$  to  $<5 \mu\text{m}$



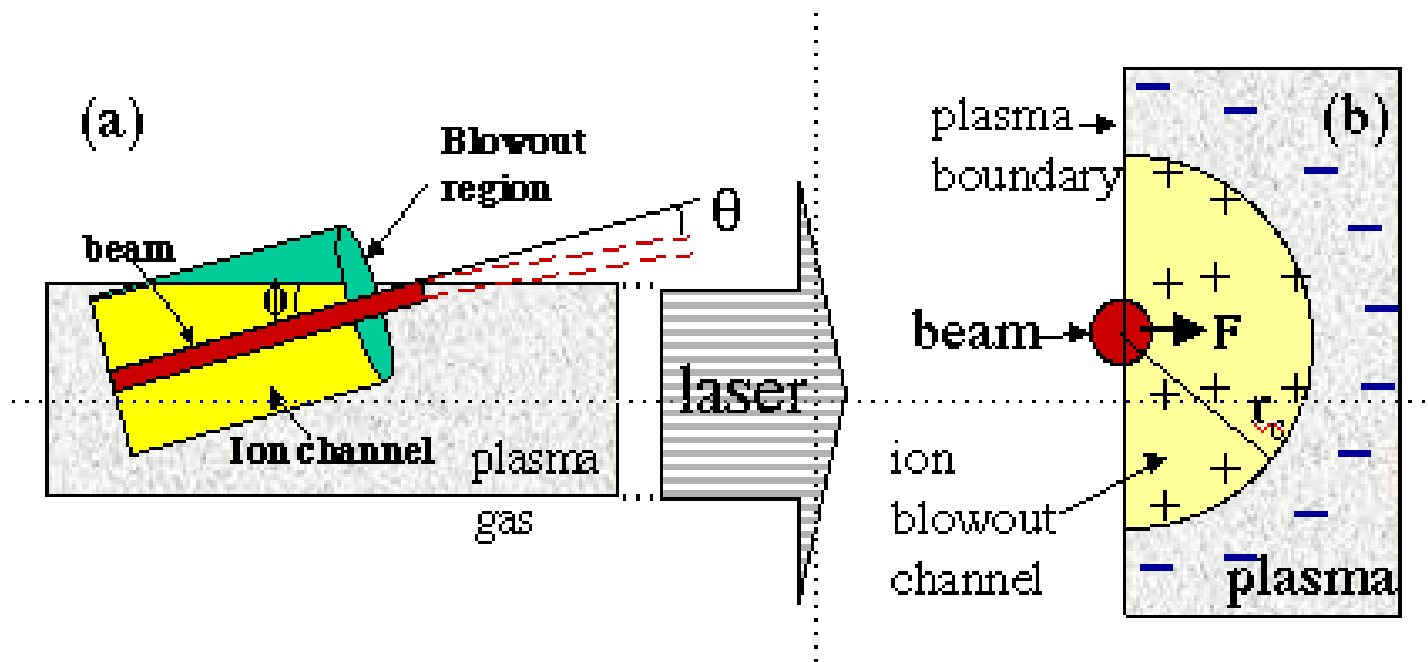
S. Wang et al, Phys. Rev. Letters, 88, 13 (2002);  
also see M. Litos, S. Corde, SLAC-PUB-15215 (2012)

# plasma bending: FFTB (2000)

## Collective Refraction of a Beam of Electrons at a Plasma-Gas Interface

*Nature* **411**, 43 (3 May 2001)

collective response of the plasma produces a deflection of the electron beam of the order of one millirad



P. Muggli,  
T. Katsouleas,  
et al

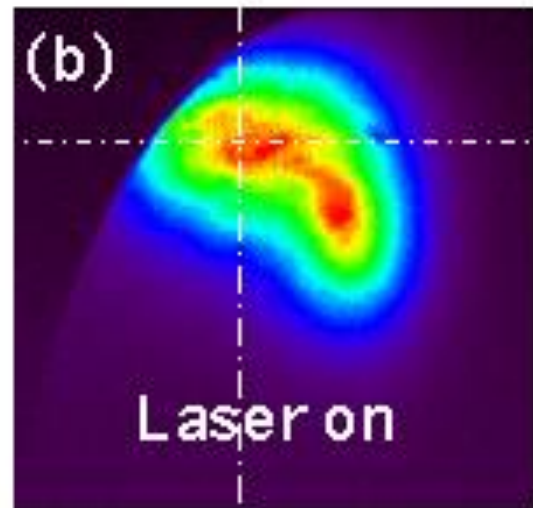
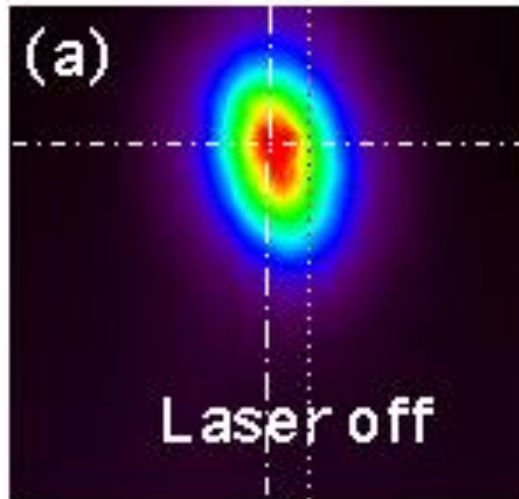
$1.9 \times 10^{10}$  electrons at 28.5 GeV in a Gaussian bunch of length  $\sigma_z = 0.7$  mm and spot size  $\sigma_x \sim \sigma_y \sim 40 \mu\text{m}$



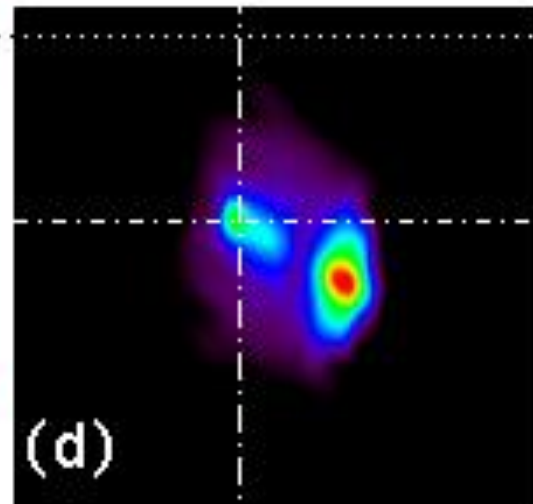
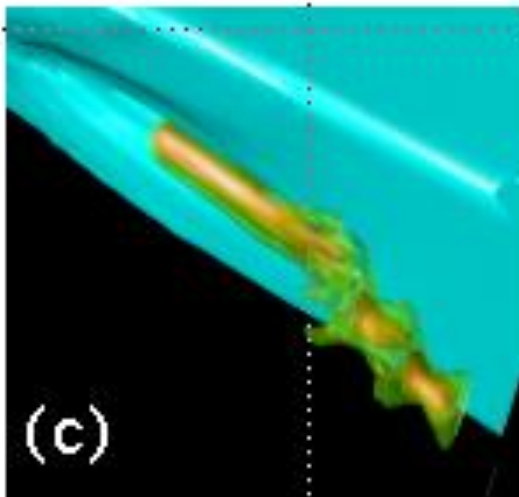
# plasma bending at FFTB

Cerenkov images of  $e^-$  beam showing refraction of a portion of the beam with the plasma (i.e., laser on) & PIC simulation

Experiment

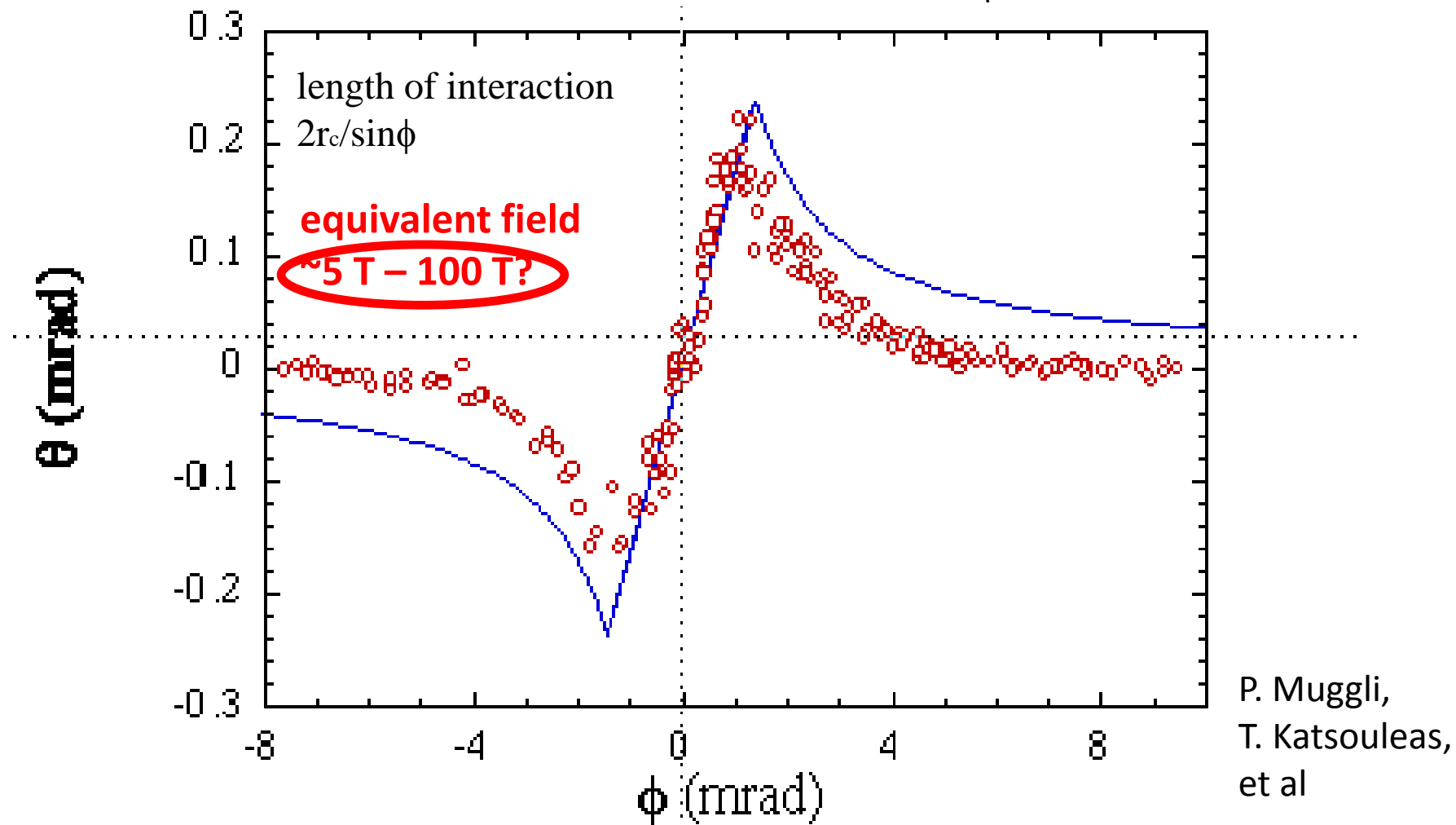


PIC Simulation



# plasma bending at FFTB

Measured e- beam deflection  $\theta$  versus angle  $\phi$  between laser and e- beam/ Solid curve is an analytical model prediction. The bunch length & plasma density were 0.7 mm and  $1 \times 10^{14} \text{ cm}^{-3}$  ( $\lambda_p \sim 3 \text{ mm}$ ,  $r_c \sim 0.2 \text{ mm}$ ?)





# from plasmas to crystals !?

## maximum field in a plasma

$$G \approx 100 \text{ GV/m } (n_0 [10^{18} \text{ cm}^{-3}])^{1/2} ;$$
$$n_0 \approx 10^{17} - 10^{18} \text{ cm}^{-3}$$

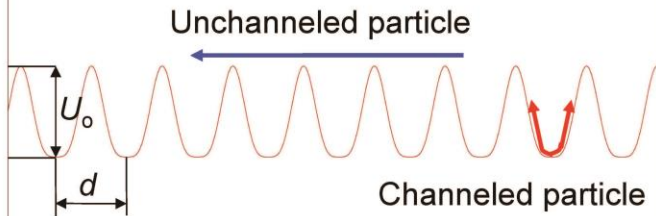
## maximum field in a crystal

$$G \approx 10 \text{ TV/m } (n_0 [10^{22} \text{ cm}^{-3}])^{1/2} ;$$
$$n_0 \approx 10^{22} - 10^{23} \text{ cm}^{-3}$$

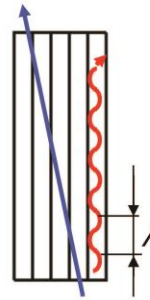
crystals are also more regular and could be cooled → less beam interaction with nuclei, etc.

# crystals - world's strongest “magnets”

(a) **straight crystal**



(c)



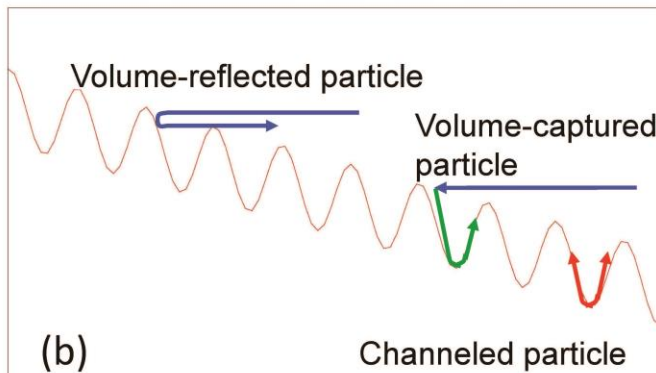
crystal focusing strength

$$\phi \sim 20-60 \text{ eV/\AA}^2$$

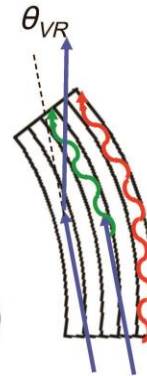
$$B_{\text{max}} \approx 2000 \text{ T !}$$

(b)

**bent crystal**

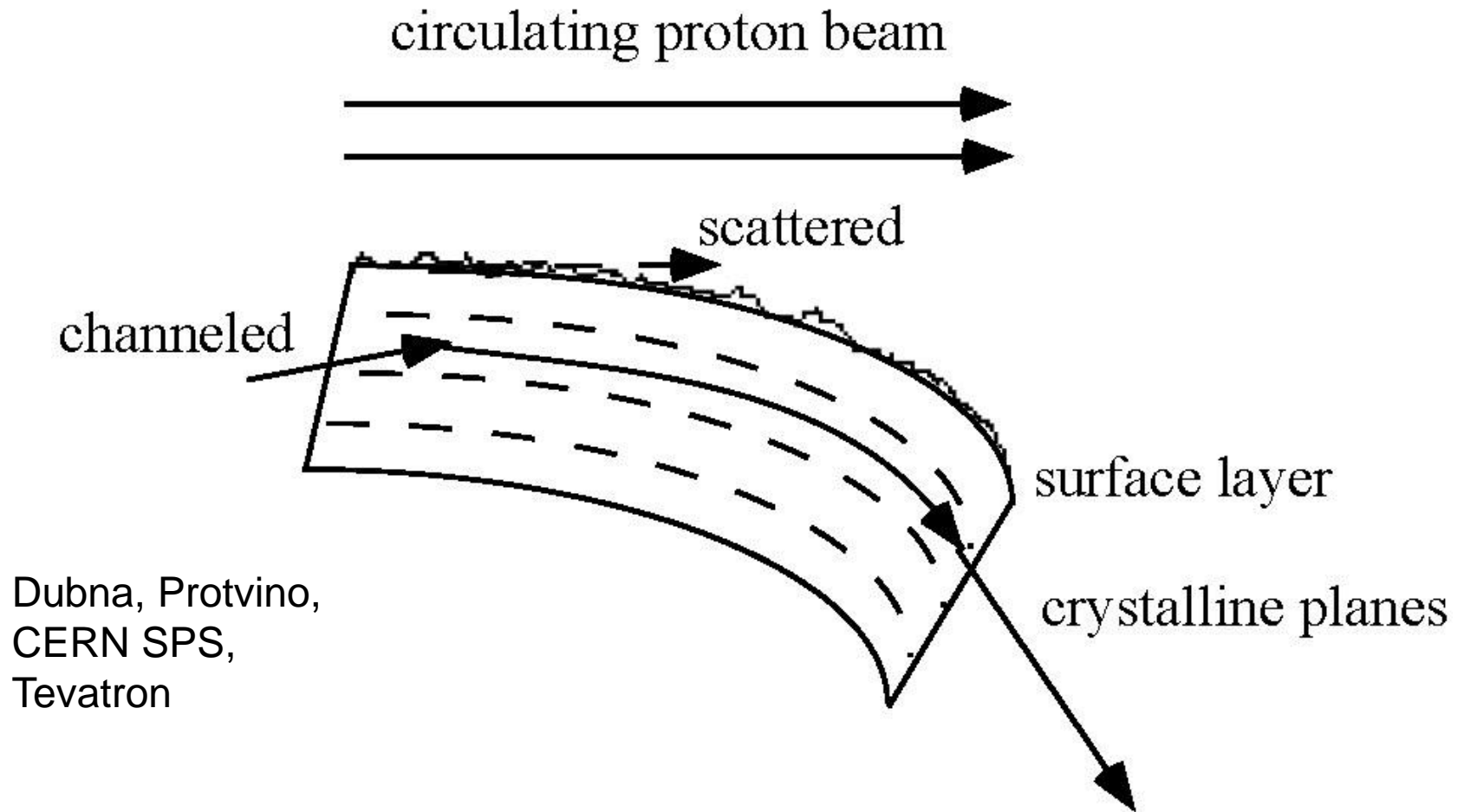


(d)



$$\lambda = 2\pi\beta = 2\pi (E/\phi)^{1/2}$$

# crystal extraction from stored proton/ion beam



since 1978 crystals are used for extracting high-energy protons or ions from storage rings; **can they also be used for a circular collider?!**

channeling condition: angle of incidence < Lindhard  
**critical angle  $\sim 5 \mu\text{rad} (Z/p [\text{TeV}/c])^{1/2}$**

thermal vibrations, discreteness of lattice, electrons  
→ **dechanneling** (exponential decrease of channeled protons)

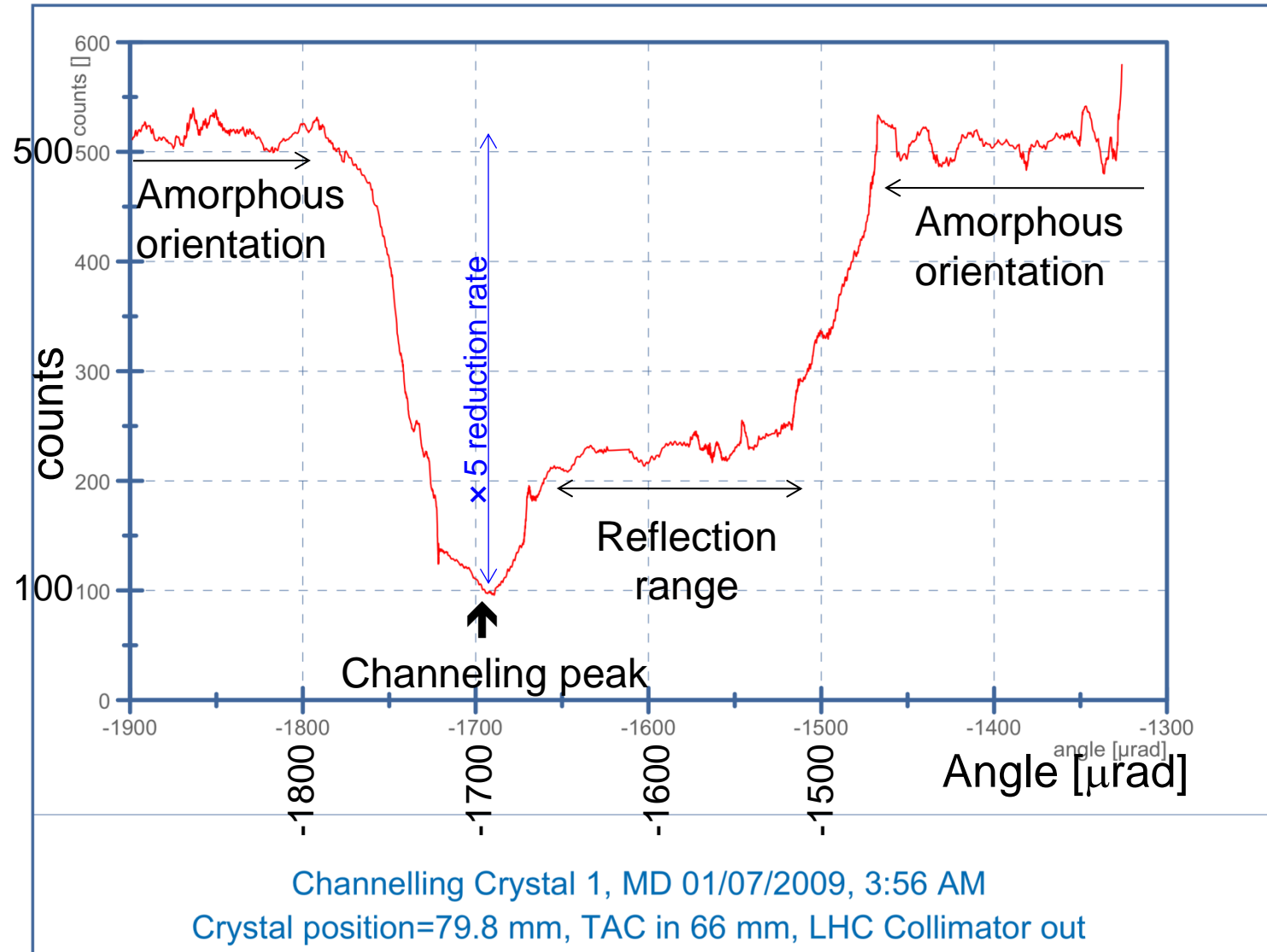
**dechanneling length  $L_0 \sim 0.9 \text{ m } p[\text{TeV}/c]$**

**cooling of crystal increases  $L_0$**

**minimum bending radius** for channeling  
 **$R_c \sim 0.4 p [\text{TeV}/c] \text{ meter}$**

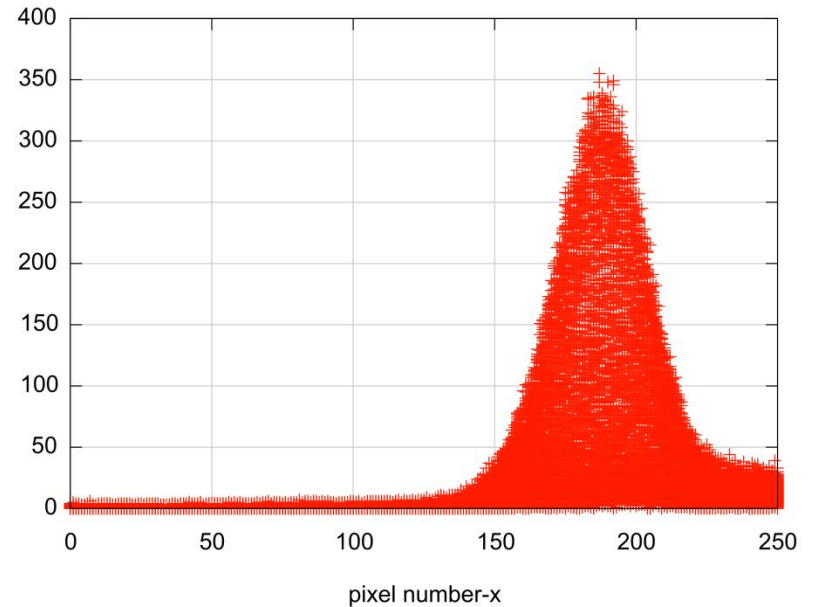
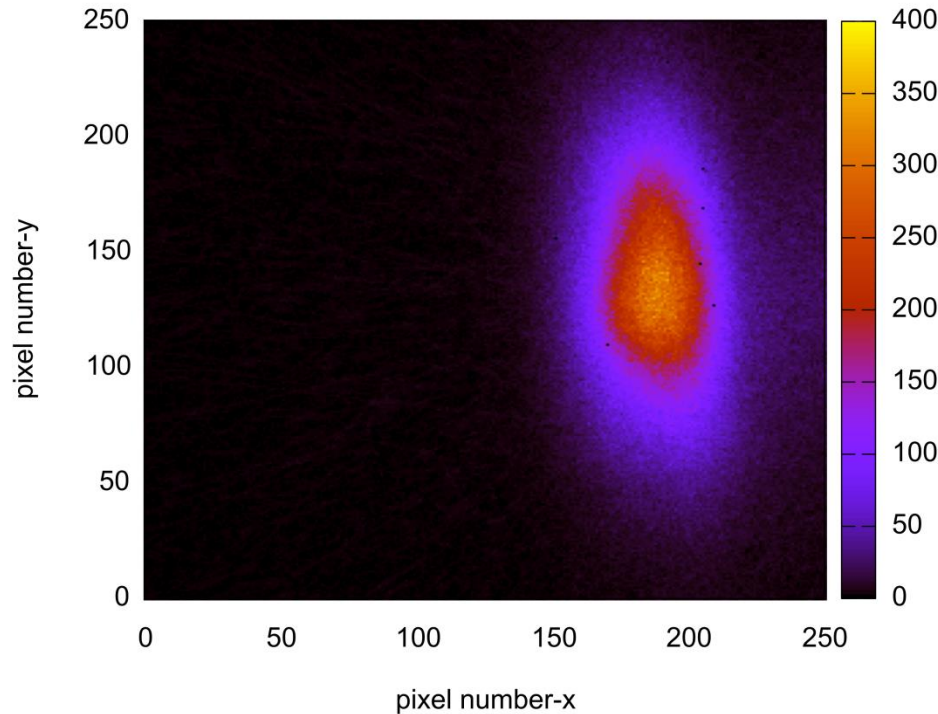
# crystal extraction experiment UA9 at SPS (2009)

Nuclear loss rate seen by a scintillator  
telescope downstream of the crystal



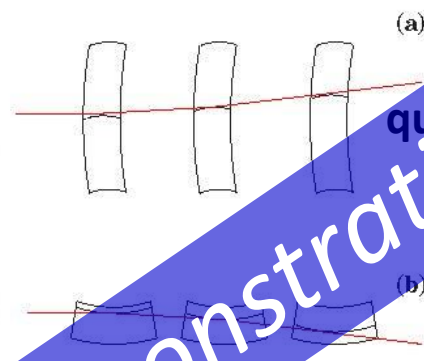
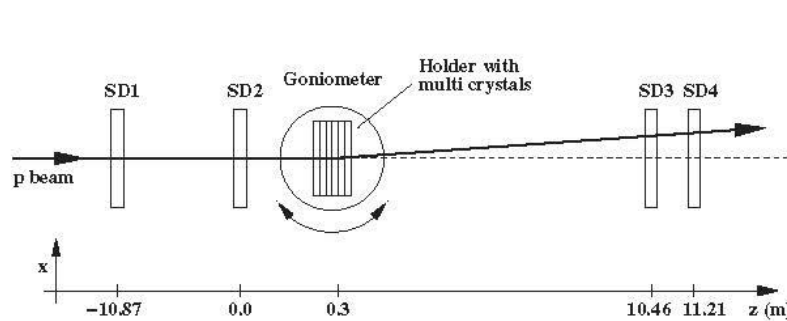
- ◆ Nuclear loss rate (including diffractive) strongly depressed

# profile of "beam" deflected by crystal

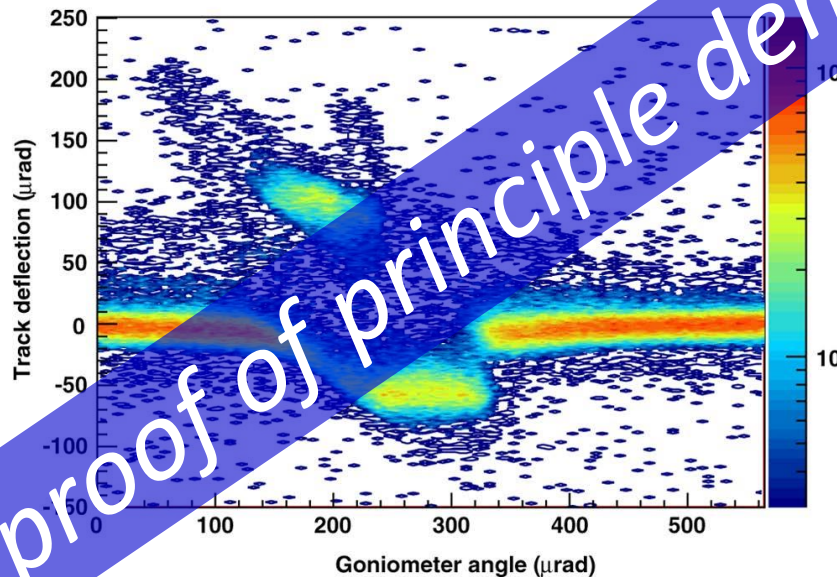


- ◆ 256×256 square pixels
- ◆ 1 pixel size = 55  $\mu\text{m}$
- ◆ 1 frame integration time 1 s

# staging of crystal deflectors



schematic layout of the experimental setup used to study multiple volume reflection at the H8 beam line of the CERN SPS



**6 strip crystals in series**  
 (each 2 mm long):  
**400 GeV/c protons**  
 reflected by  $40 \pm 2 \mu\text{rad}$   
 [effective field **16 T**]  
 with **efficiency  $0.93 \pm 0.04$**

W. Scandale et al, Observation of Multiple Volume Reflection of Ultrarelativistic Protons by a Sequence of Several Bent Silicon Crystals, Phys.Rev.Lett. 102 (2009) 084801



# crystal channeling efficiency

for single crystal traversal: **present deflection efficiency**  
**>0.8-0.9 t.b.c.w. 1990's : 0.1-0.2**

**gain in deflection probability over last decades:**

- now short crystals bent with constant curvature (anticlastic bending); crystal length in the 1990's was 5 cm or more and now it is 5 mm or less

**multi-reflection / multi-strip crystal - drawbacks:**

1. difficult to produce a multi-crystal with coherent reflections (alignment imperfections )
2. for high energy the multi-crystal length should be large
  - large production of diffractive protons !
3. larger radiation damage of the crystal (larger ionization energy deposition again because of longer paths)

# radiation damping in ideal crystal

## transverse radiation damping

- independent of particle energy!

## no quantum excitation

## decay to transverse ground state

## minimum beam emittance: $\gamma\epsilon_{\min} = \hbar/2mc$

- limited only by the uncertainty principle

particle can be accelerated along focusing channel  
in its ground state without any energy loss

Z.Huang, P.Chen, R.D.Ruth, Radiation reaction in a continuous focusing channel, Phys.Rev.Lett. 74 (1995) 1759-1762

# crystal accelerators

## acceleration in crystal channels

$G \approx 10 \text{ TV/m } (n_0 [10^{22} \text{ cm}^{-3}])^{1/2} ; n_0 \approx 10^{22} - 10^{23} \text{ cm}^{-3}$

driven by x-ray laser

*now/soon available!*

*LCLS, Spring-8, XFEL, SwissFEL ...*

max. energy set by radiation emission due to betatron oscillations between crystal planes, excited by multiple scattering off channel  $e^-$

$E_{\text{max}} \approx 300 \text{ GeV for } e^+$ ,  $10^4 \text{ TeV } \mu$ ,  $10^6 \text{ TeV for } p$  ?!

Chen & Noble 1997; Dodin & Fisch 2008; Shiltsev '12

10 TV/m – disposable crystal accelerator

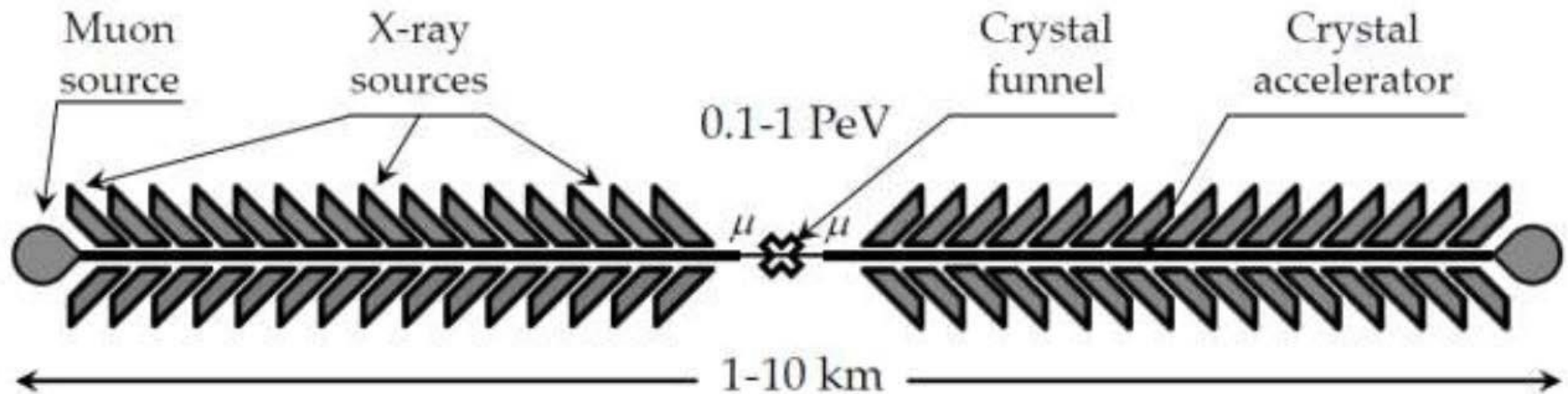
or 0.1 TV/m – reusable crystal accelerator

side injection of x-ray pulses using long fibers

$e^\pm$  may soon run out of steam in the high-gradient world!

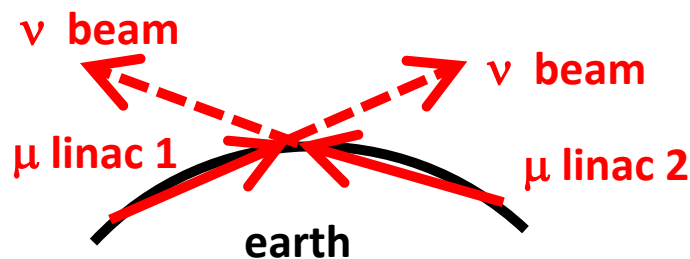
→ need to change particle type

linear X-ray crystal  $\mu$  collider



issues:

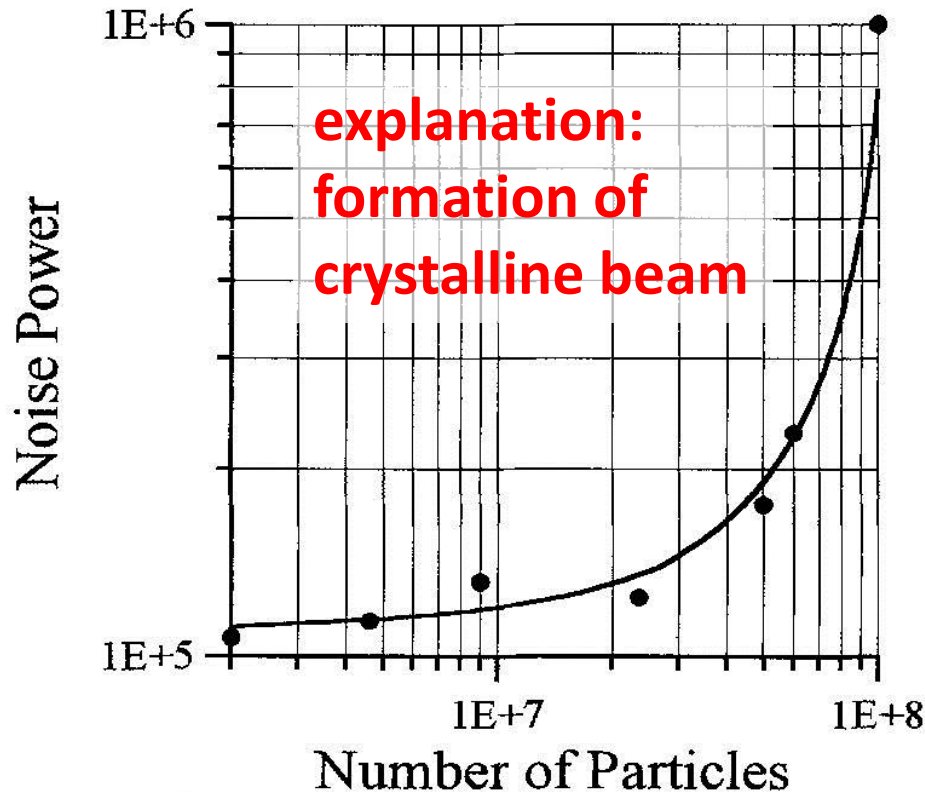
$\mu$  production rate  
neutrino radiation



Vladimir Shiltsev, 2012

# crystalline beams

e-cooled  $p$  beam at BINP NAP-M, 1980



$$\sigma^2 = \frac{\sigma_0^2}{1 - N/N_{th}}$$

$$\sigma_0 = 1.4 \times 10^{-6}$$
$$N_{th} = 1.2 \times 10^8$$

Schottky noise power vs number of particles in the beam ( $N$ )

E.N. Dementiev et al., Sov. J. Tech. Phys. 50 (1980) 1717.

V.V. Parkhomchuk and D.V. Pestrikov, Sov. J. Tech. Phys. 50 (1980) 1411.

D. Pestrikov, NIM A 379, 1996

## **theoretical studies:**

constant gradient rings, alternating focusing,  
effect of bending-magnets shear... :

A. Rahman and J.P. Schiffer, Phys. Rev. Letts. 57, 1133 (1986);

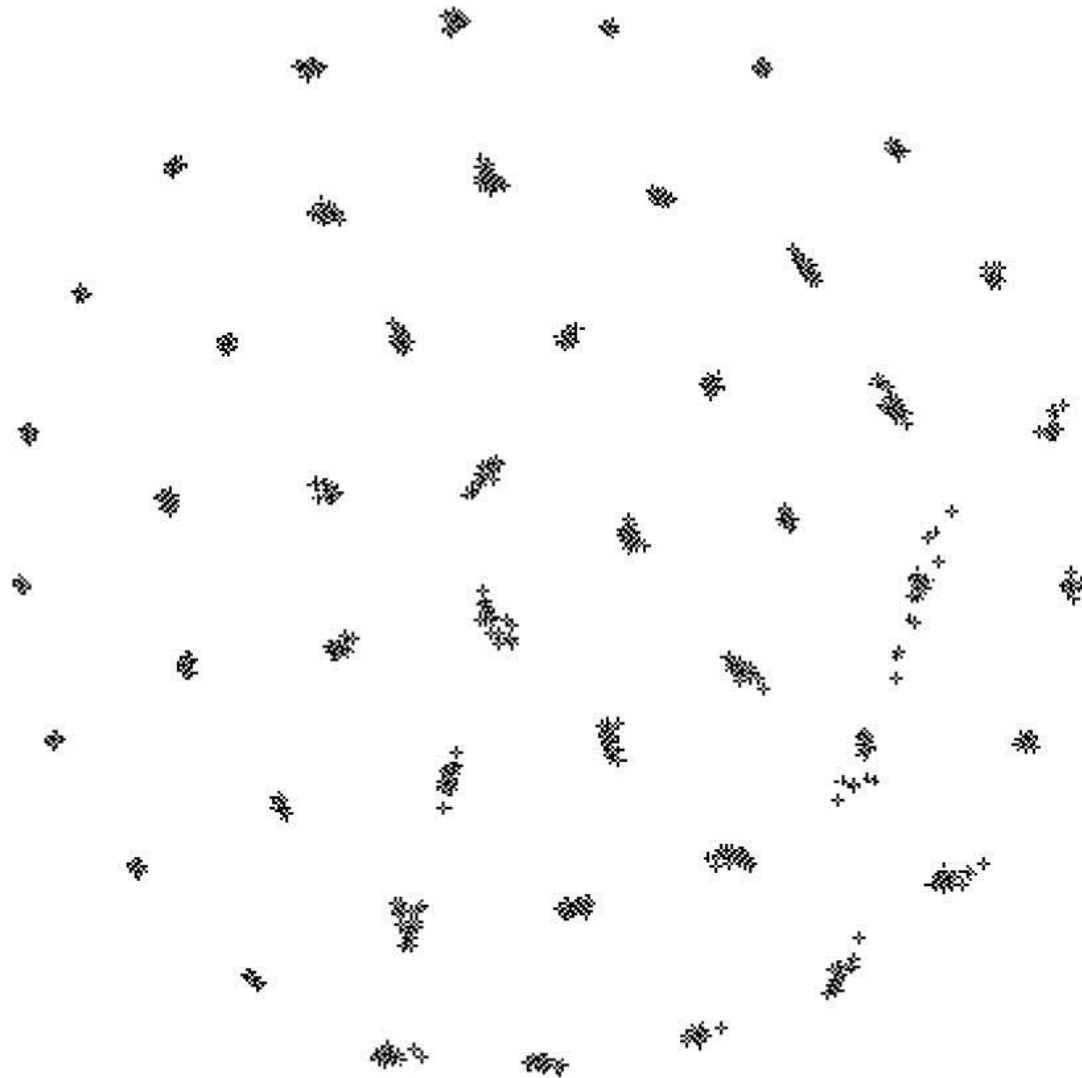
R.W. Hasse and J.P. Schiffer Annals, of Physics 203, 419 (1990).

J. Wei, T.P. Li, and A. Sessler, Phys. Rev. Letts. 73, 3089 (1994).

## **increasing beam density:**

**1-D crystal → 2-D crystal → 3-D crystal**

# molecular dynamics simulations



J.P. Schiffer  
IEEE 1996

projection onto x-y plane with strong continuous cooling



# experiments on crystalline beams

J. S. Hangst et al., Phys. Rev. Letts. 67, 1238 (1991).

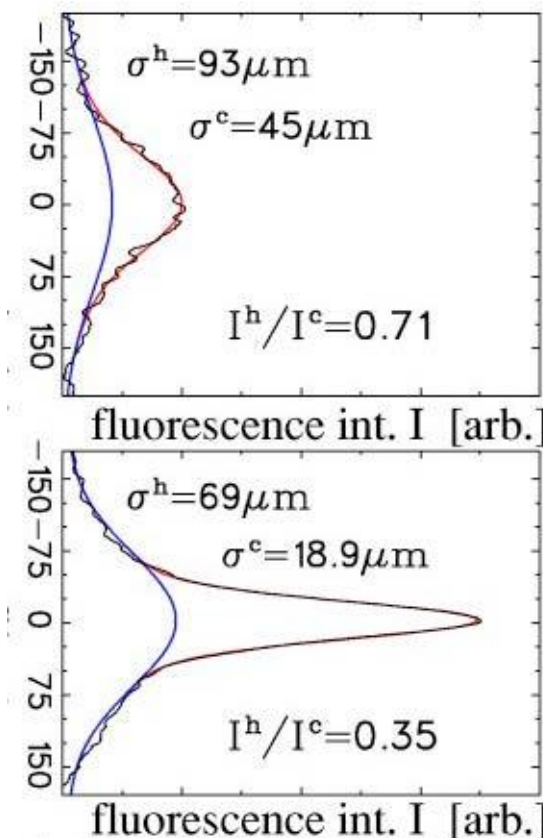
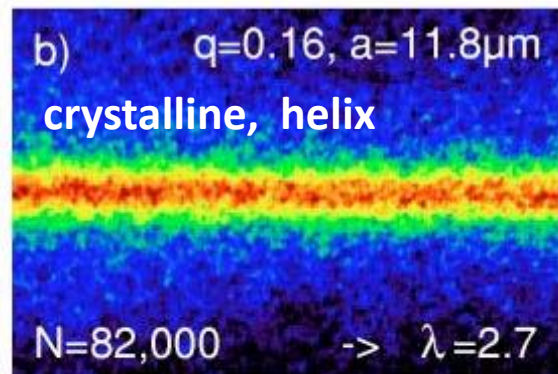
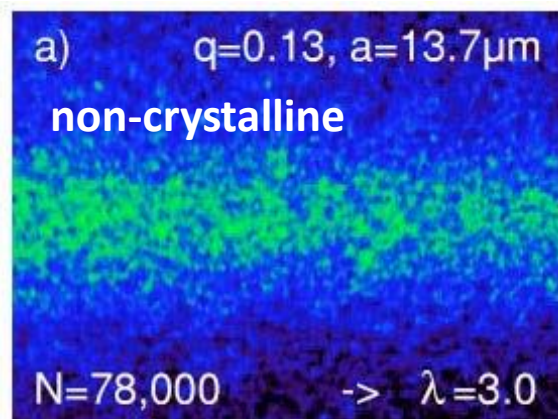
BINP NAP-M, e-cooling

TSR Heidelberg, laser cooling,  $< 1$  K

**ASTRID Aarhus, laser cooling Laser,  $\sim$  mK**

**PALLAS, LMU Munich**

U. Schramm et al,  
PRE 66 (2002)

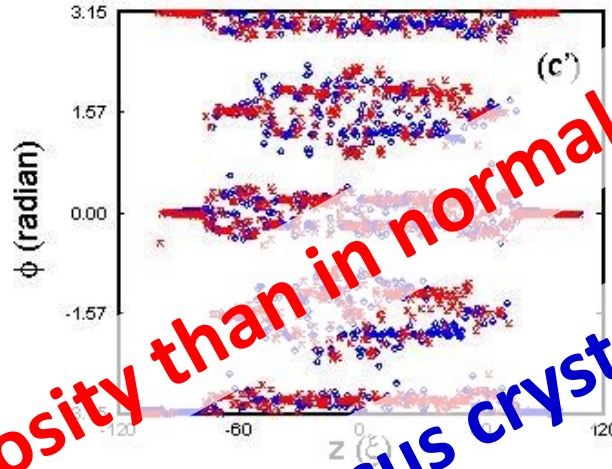
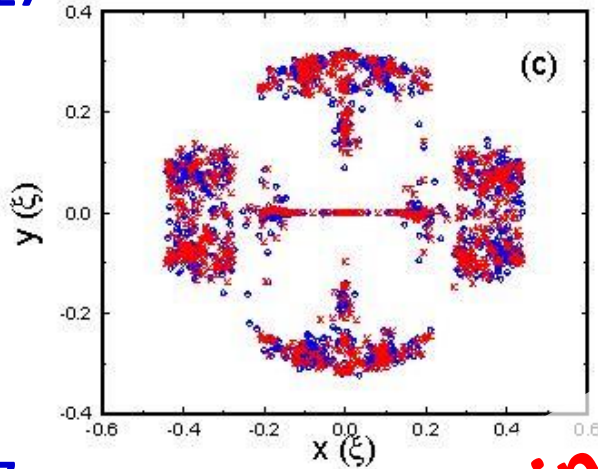


higher line density

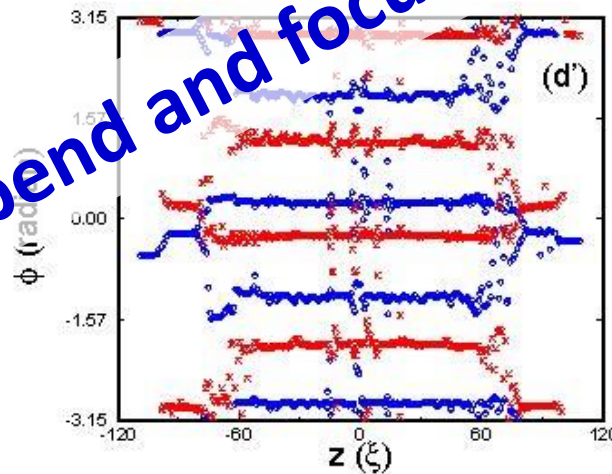
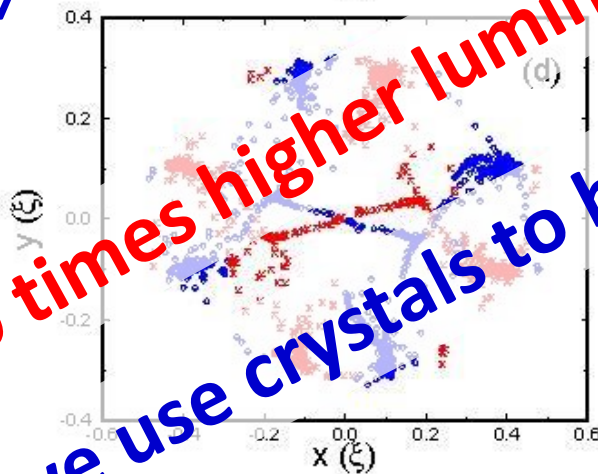
lower line density

# colliding crystalline beams

$$\Delta Q_{bb}=0.27$$



$$\Delta Q_{bb}=2.7$$

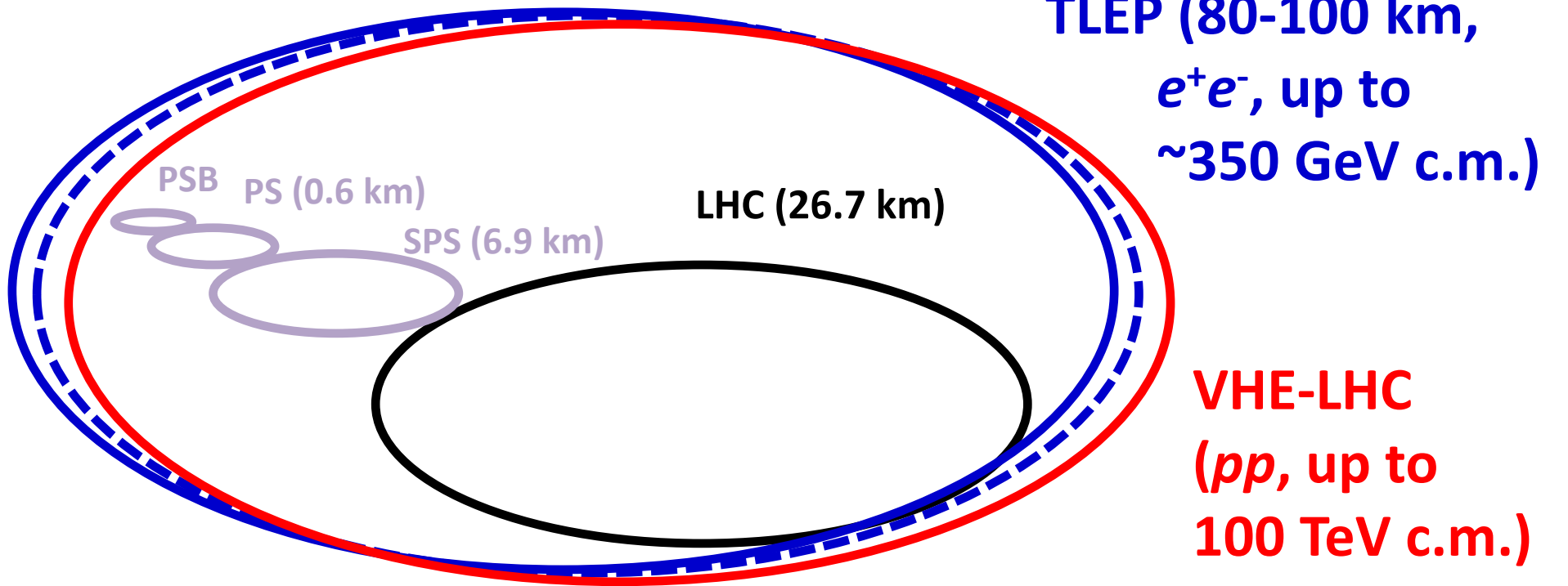


100 times higher luminosity than in normal colliders!  
can we use crystals to bend and focus crystalline beams?

simulations showing formation of crystalline ground states with 1000 macro-particles / beam

# *possible long-term strategy*

(CERN implementation)



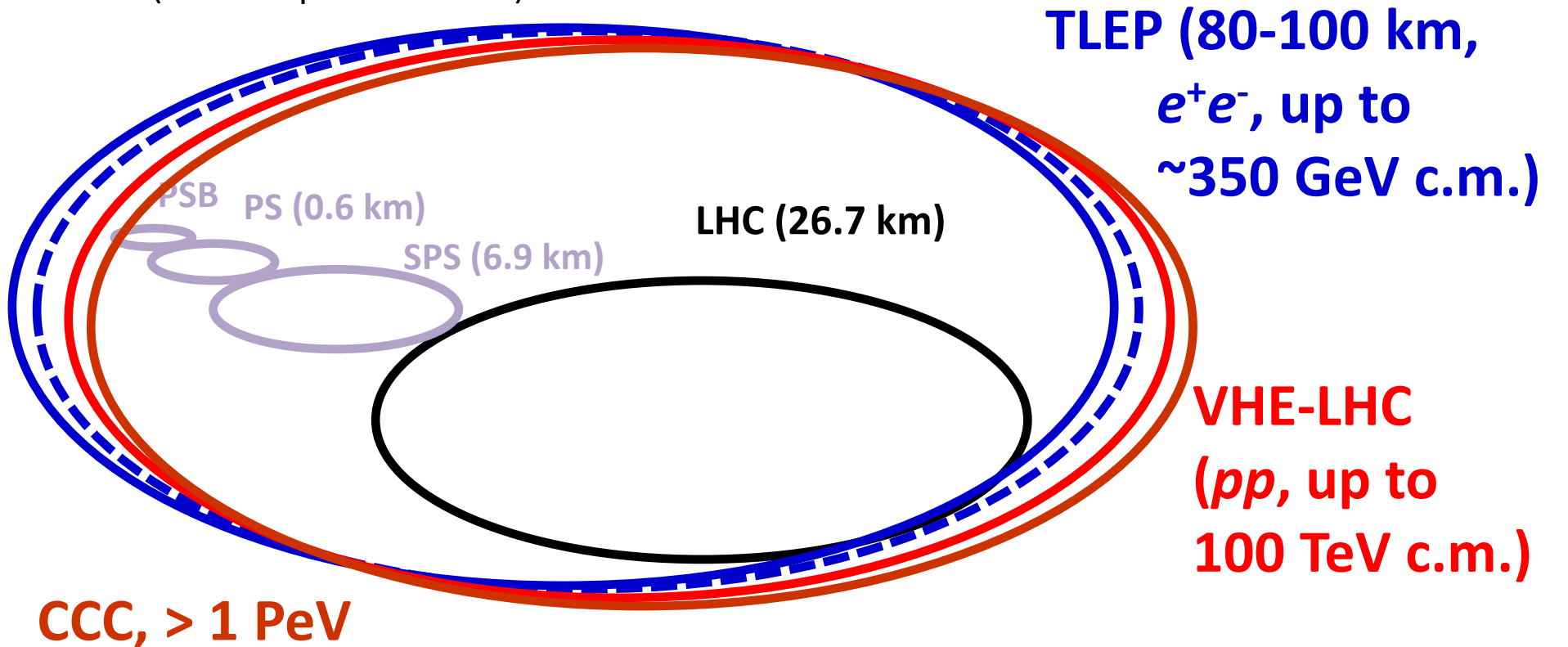
&  $e^\pm$  (120 GeV) –  $p$  (7, 16 & 50 TeV) collisions ([V]HE-]TLHeC)

≥50 years of  $e^+e^-$ ,  $pp$ ,  $ep/A$  physics at highest energies

100 TeV  $pp$  collider may not be enough ?! (D. Schulte)

# *possible longer-term strategy*

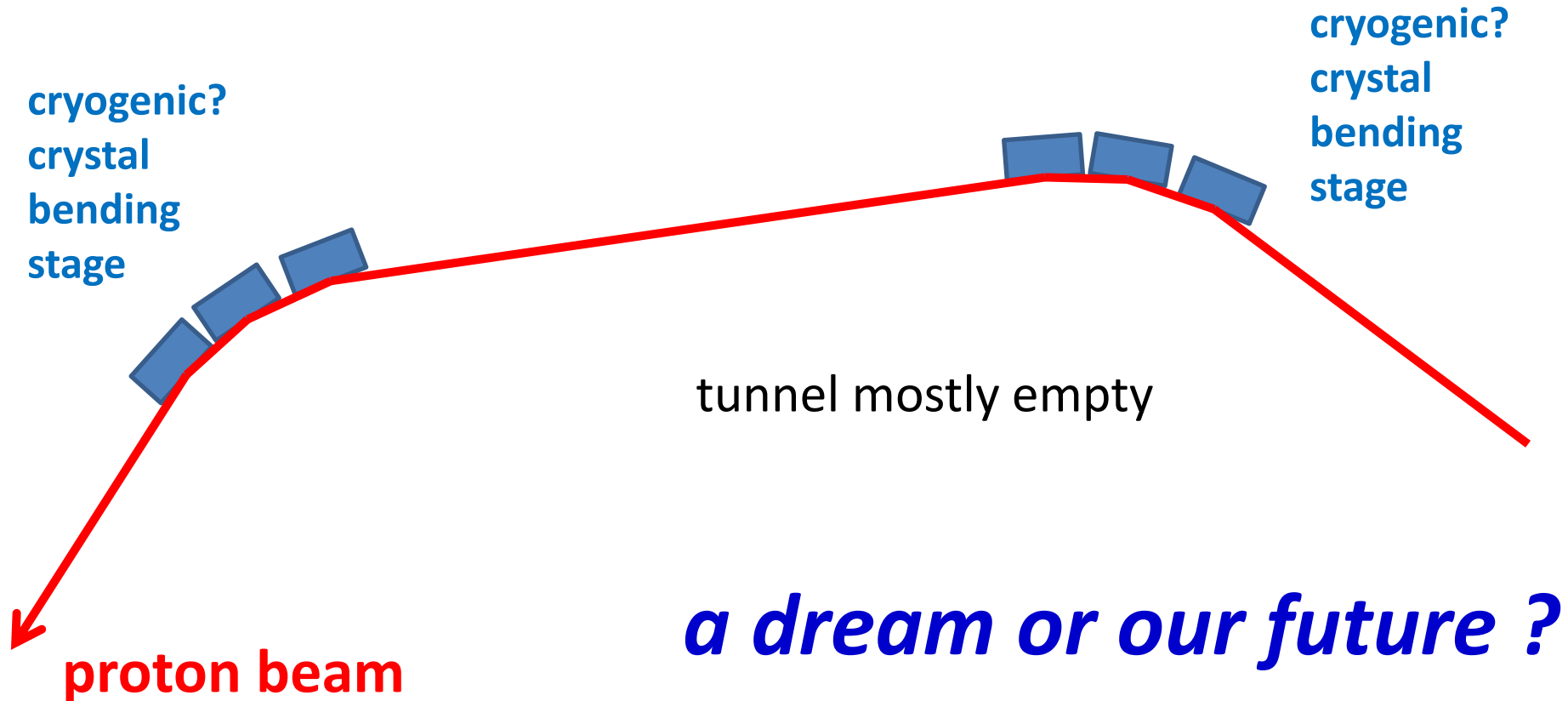
(CERN implementation)



&  $e^\pm$  (120 GeV) –  $p$  (7, 16 & 50 TeV) collisions ([V]HE-]TLHeC)

$\geq 50$  years of  $e^+e^-$ ,  $pp$ ,  $ep/A$  physics at highest energies  
followed by  $>1$  PeV circular crystal collider (CCC)?!?

# circular crystal collider?



energy ramp using induction acceleration?

# conclusions

- **plasmas & crystals demonstrate large focusing forces,  $10^3$ - $10^4$ x stronger than SC quadrupoles**
- they could also provide large **dipole field**; so far bending fields of **5-100 T** demonstrated
- **beam-matter interaction & efficiency** are the critical issues for circular ring applications
- straightforward **use in single-pass systems**
- **incentive to strengthen crystal R&D!**

... and how about plasma crystals?

**many thanks for your attention!**