
ELEMENTARY PARTICLES AND FIELDS
Theory

Scaling of Semi-inclusive Events in pp Interactions

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Abstract—The normalized single-particle semi-inclusive double-differential spectrum of π^- mesons from pp interactions at 6.6–400 GeV/ c and the relative concentration of π^0 and K_S^0 mesons in such events of fixed multiplicity of π^- mesons are completely determined by specifying any feature of this spectrum—for example, $\langle y^2 \rangle_n$ or $\langle E \rangle_n$. Therefore, a two-parameter sample of semi-inclusive events that depends on the energy and the multiplicity reduces to a one-parameter sample. © 2004 MAIK “Nauka/Interperiodica”.



**Sasha Golokhvastov
Dubna, ≈1980**

**Dedicated idealist
in physics and life**

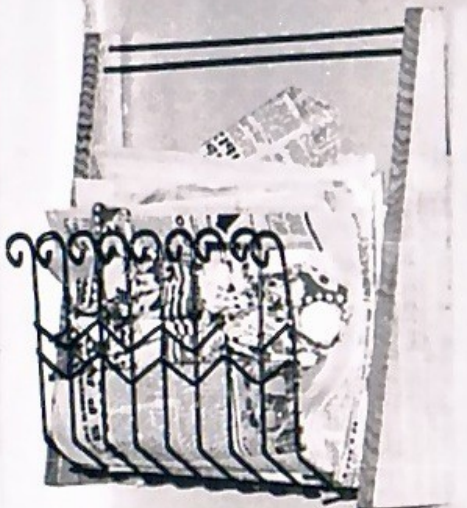
**Proponent of
"slow science" [AB]
(= thinking about
and discussing
your idea before
publishing in
10 papers)**

*AB – Andrzej Bialas,
SQM 2011, Krakow
After dinner talk*





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The term “semi-inclusive” was introduced by Kobayashi, Nielsen, and Olesen [1], who studied the scaling of semi-inclusive spectra (this is so-called KNO-II scaling, which was not confirmed, however, in experiments [2, 3]). A semi-inclusive spectrum is a kinematical spectrum of particles of some sort in events where the number of these particles is fixed.

**e.g., π^- rapidity spectrum in
 $p+p \rightarrow n \pi^- + X$ processes
at a given collision energy**



The richest data on semi-inclusive spectra concern rapidity distributions of negatively charged pions (or hadrons) in p+p interactions at the SPS (NA61/SHINE) energies.

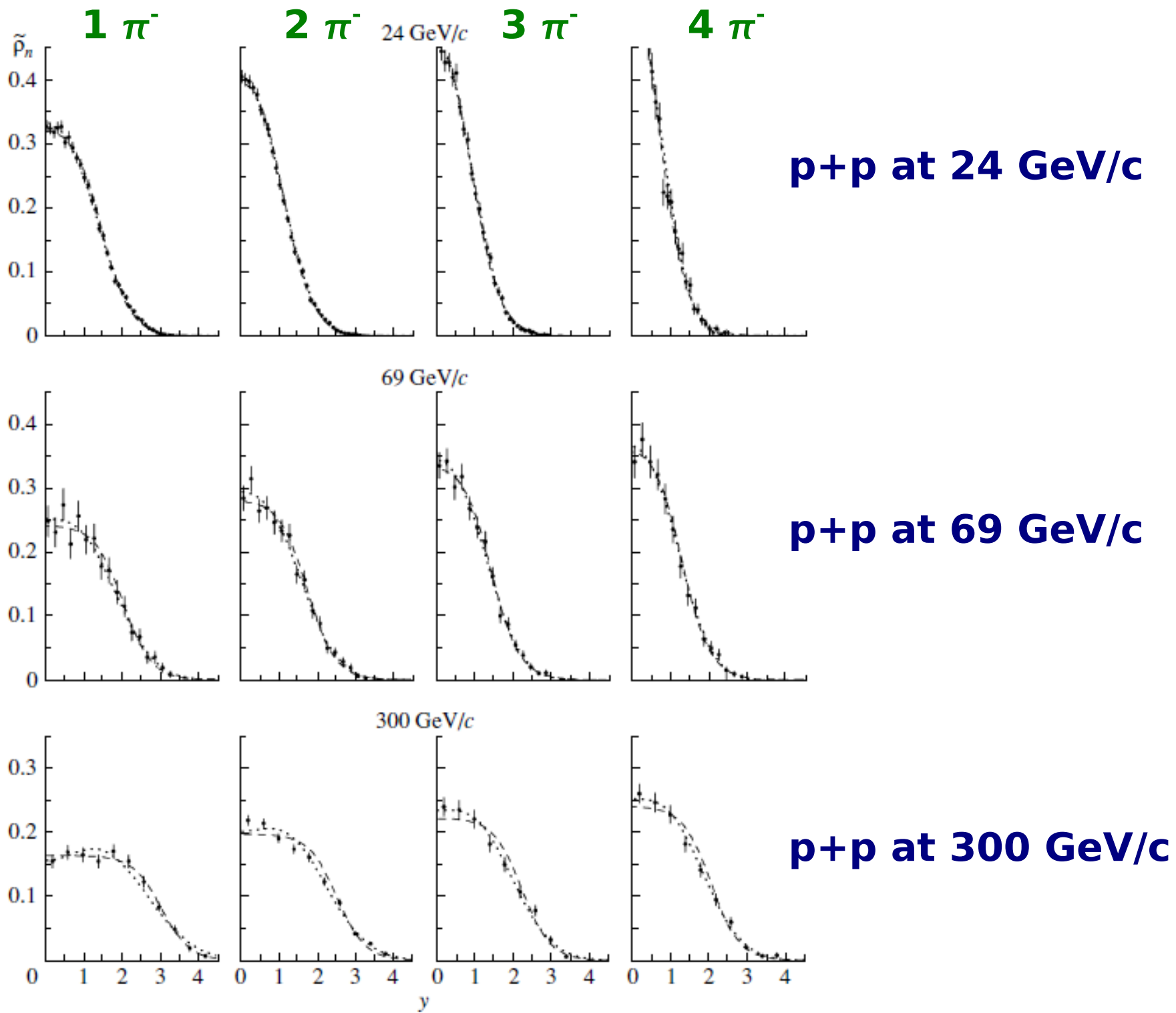
Data at higher collision energies are poor as collider experiments have typically small acceptance.



$$P(y \mid \sqrt{s}, n) = \tilde{\rho}_n(y) = \frac{1}{n\sigma_n} \frac{d\sigma_n}{dy}, \quad \int \tilde{\rho}_n(y) dy = 1 \quad (1)$$

(the tilde symbol is used here to indicate that ρ is normalized to unity [4, 11]). Thus, the quantity $\tilde{\rho}_n(y)$ is the density of the probability that an arbitrarily chosen π^- meson in any event featuring $n \pi^-$ mesons has a rapidity y .

Rapidity probability density



Obviously semi-inclusive spectra depend on both experimental parameters,

- **particle multiplicity** and
- **collision energy.**



Sasha Golokhvastov found that the two parameter dependence can be reduced to a single parameter dependence:

Golokhvastov scaling of semi-inclusive spectra

$$P(y | \sqrt{s}, n) = P(y | f(\sqrt{s}, n))$$

Golokhvastov scaling of semi-inclusive spectra

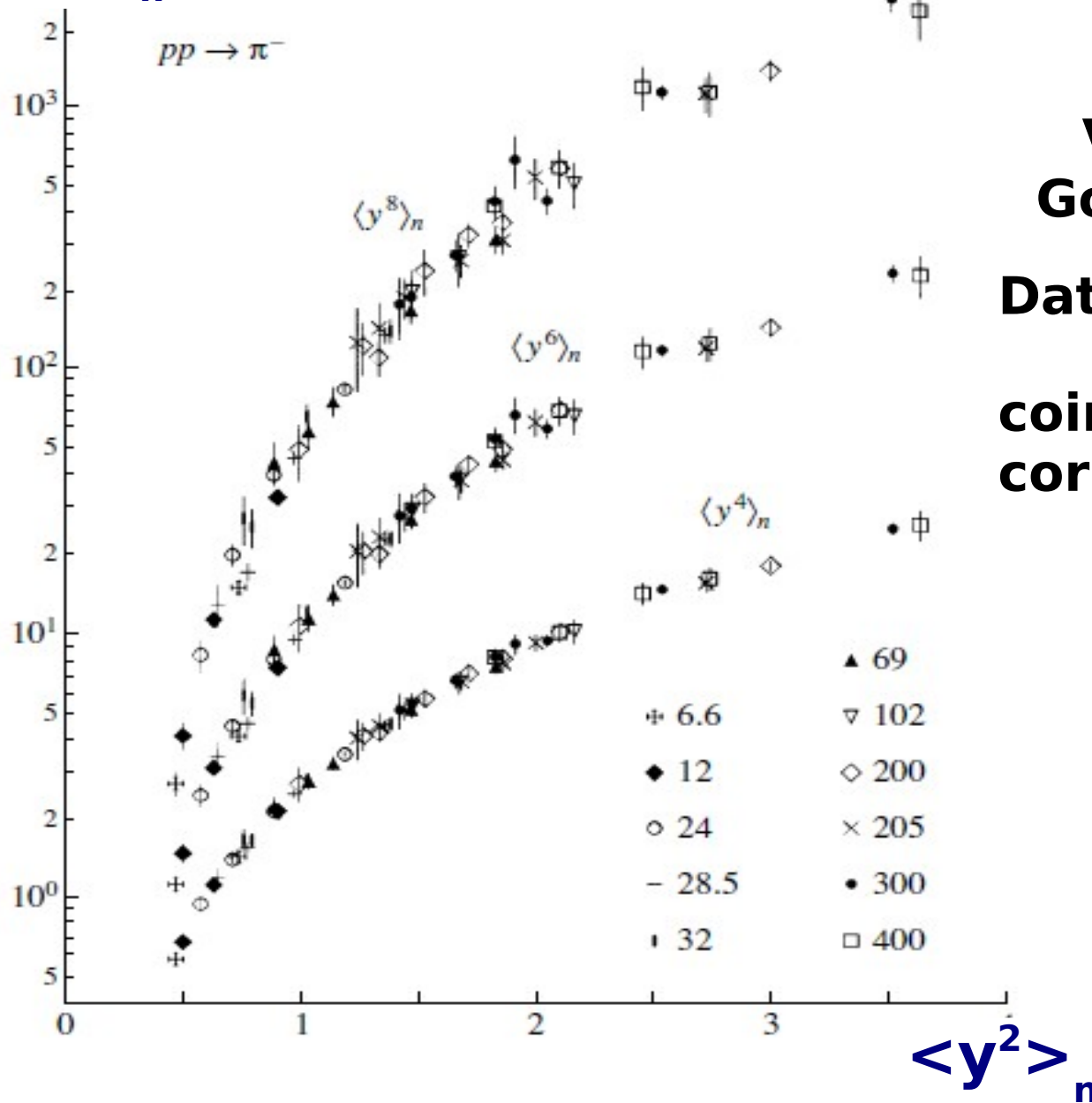
$$P(y | \sqrt{s}, n) = P(y | f(\sqrt{s}, n))$$



In particular $f(\sqrt{s}, n)$ can be selected as any parameter characterizing rapidity spectrum, e.g., its variance $\langle y^2 \rangle$ and the scaling can be tested using higher moments of y

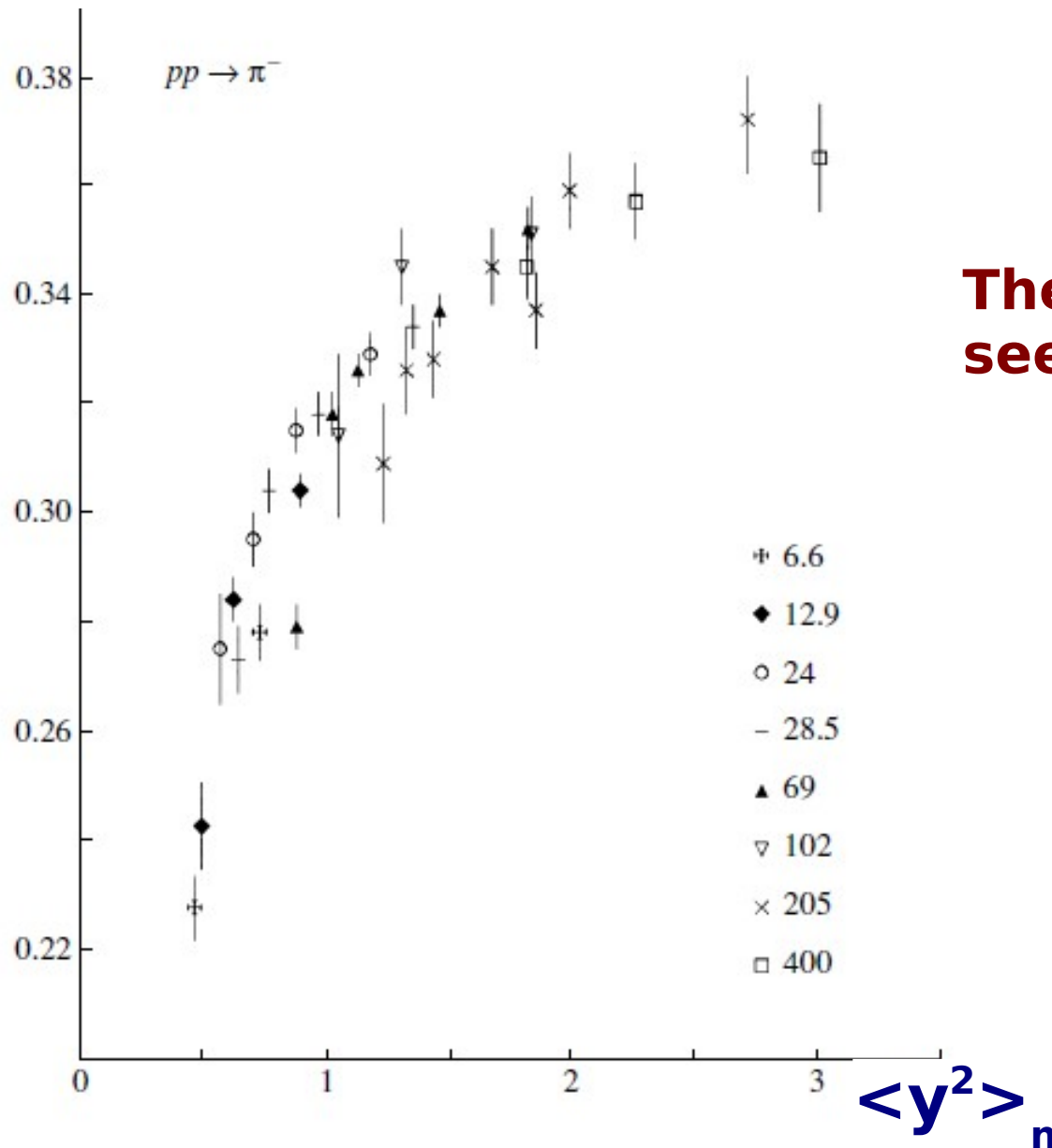
$$\langle y^q \rangle_n \equiv \int y^q \tilde{\rho}_n(y) dy. \quad (2)$$

$$\langle y^q \rangle_n$$



Verification of the Golokhvastov scaling:
Data points for various \sqrt{s} and n coincide providing they correspond to the same $\langle y^2 \rangle_n$

$\langle p_T \rangle_n$



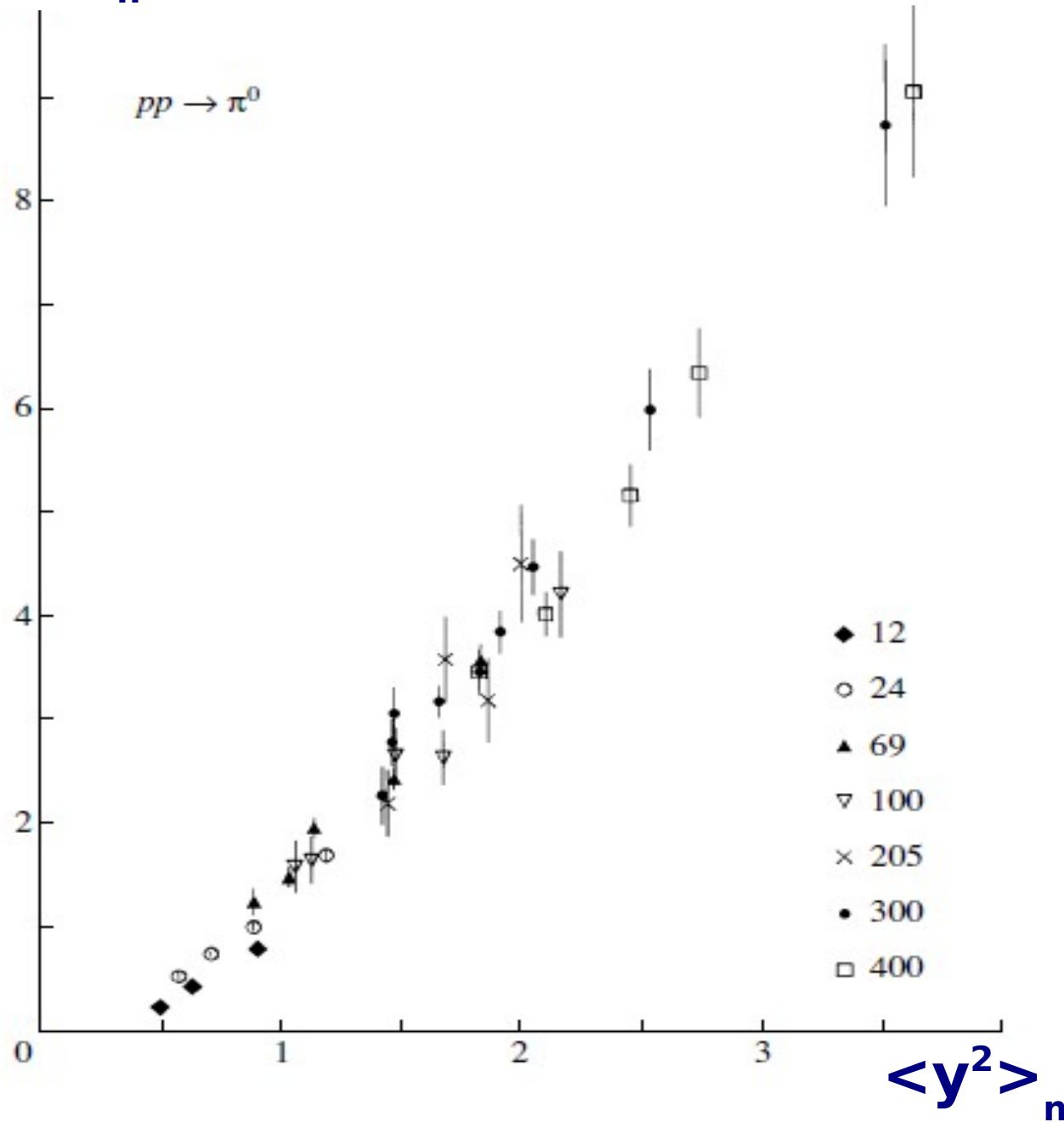
The Golokhvastov scaling seems to be valid also for p_T spectra

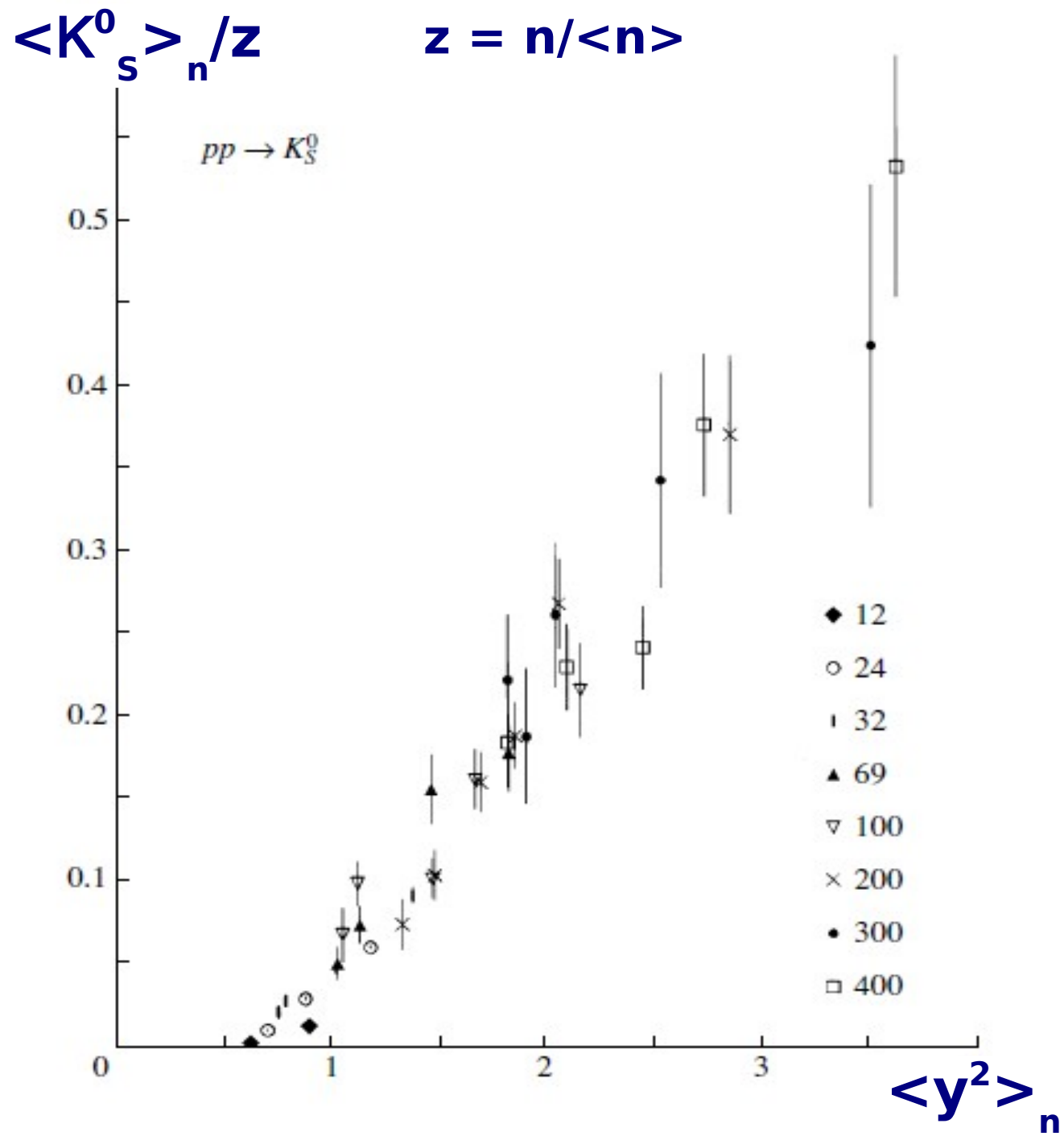
Thus Sasha formulated the hypothesis of the scaling validity for the two-dimensional y, p_T spectrum:

$$\frac{1}{n\sigma_n} \frac{d^2\sigma_n}{dydp_T}(\sqrt{s}, n) = \frac{1}{n\sigma_n} \frac{d^2\sigma_n}{dydp_T}[f(\sqrt{s}, n)]. \quad (3)$$

and possibly, for other properties of hadron production e.g., mean multiplicity of neutral pions and kaons.

$$\langle \pi^0 \rangle_n / z \quad z = n / \langle n \rangle$$





Golokhvastov scaling of semi-inclusive spectra

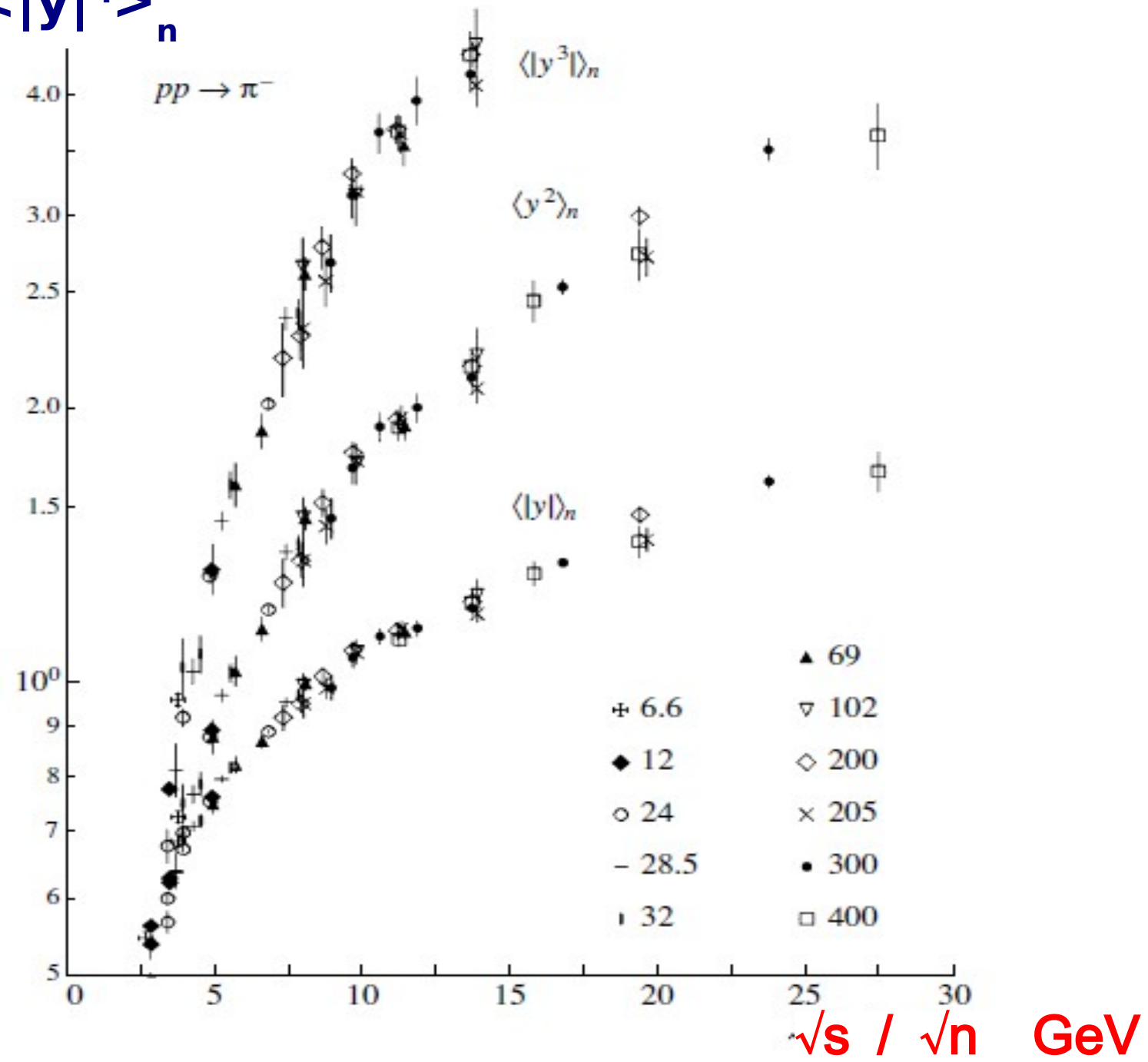
$$P(y, \dots | \sqrt{s}, n) = P(y, \dots | f(\sqrt{s}, n))$$



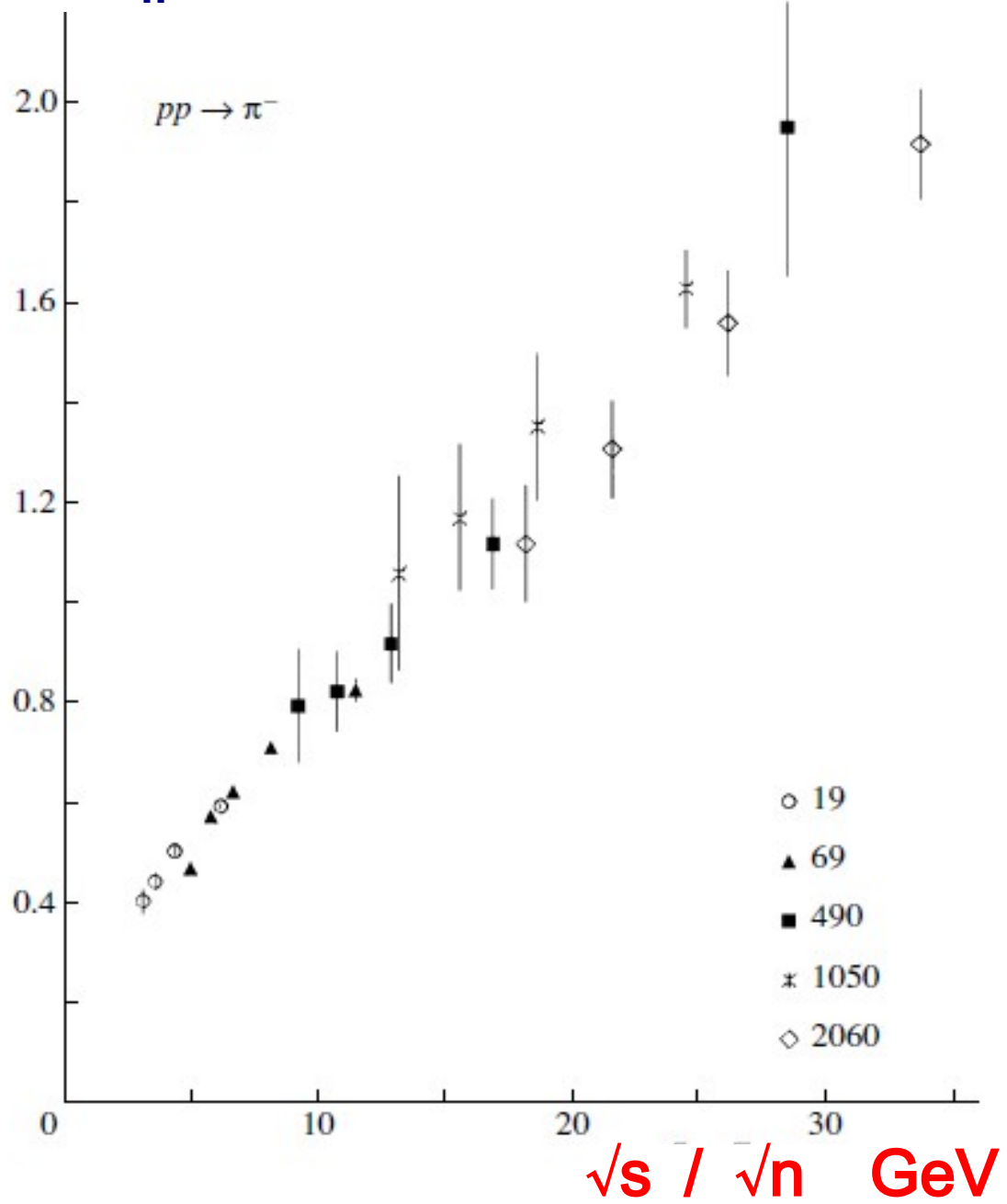
Finally Sasha proposes a simple form of the $f(\sqrt{s}, n)$ function:

$$f(\sqrt{s}, n) = \sqrt{s} / \sqrt{n}$$

$$\langle |y|^q \rangle_n$$



$\langle E \rangle_n$ GeV



Possible next steps:

- **understanding origin of the scaling within statistical models - clearly it reflects conservation laws, thus the MCE-based models should be considered,**
- **based on the Golokhvastov and the KNO-Golokhvastov scalings construct a Monte Carlo model which should allow for precise predictions of negatively charged pion spectra in p+p interactions.**

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