

MWT: chirally rotated Schrödinger functional scheme

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A. Patella, A. Rago, S. Sint, P. Vilaseca

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CP³ - Origins



Particle Physics & Origin of Mass



DIAS

Danish Institute
for Advanced Study

Outline

- ✦ MWT model
- ✦ Chirally rotated SF scheme
- ✦ Preliminary results (tuning + coupling)

Minimal Walking Technicolor

- L. Del Debbio, B. Lucini, A. Patella, CP, A.Rago, Phys. Rev. D82, 014509 (2010)
L. Del Debbio, B. Lucini, A. Patella, CP, A.Rago, Phys. Rev. D82, 014510 (2010)
F. Bursa, L. Del Debbio, L. Keegan, CP, T. Pickup, Phys. Rev. D81 (2010) 014505
E. Kerrane, et al. , Phys.Rev. D84, 034506 (2011)
L. Del Debbio, B. Lucini, A. Patella, CP, A. Rago, PoS LATTICE2011 (2011) 084

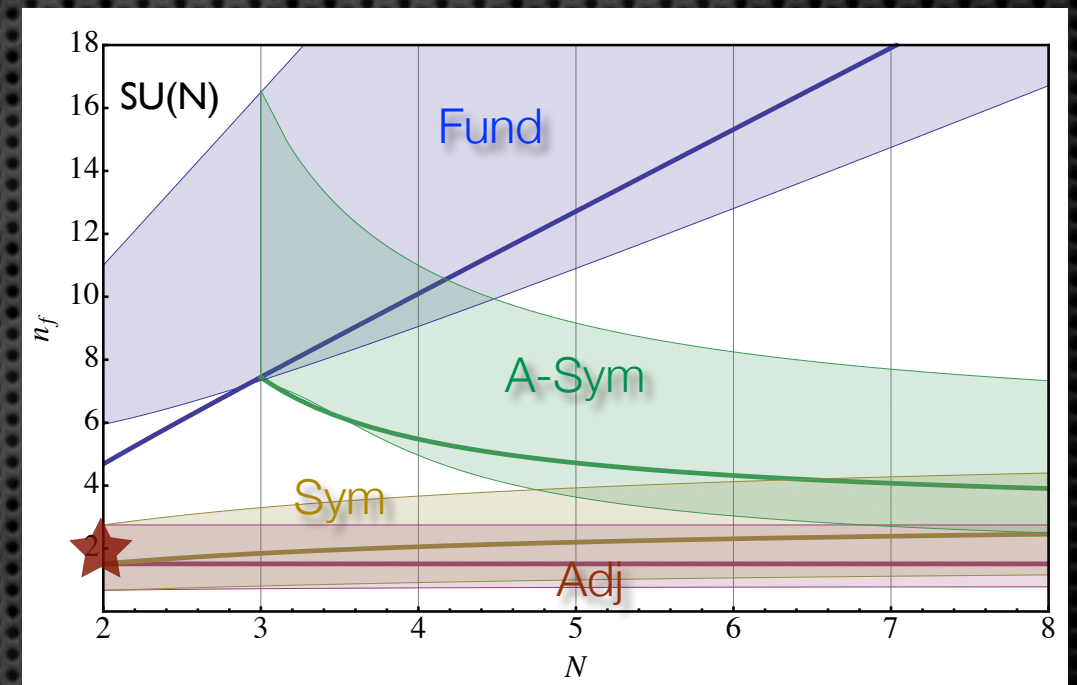
Minimal Walking Technicolor

$SU(2)_{TC} + 2$ Dirac Adjoint fermions

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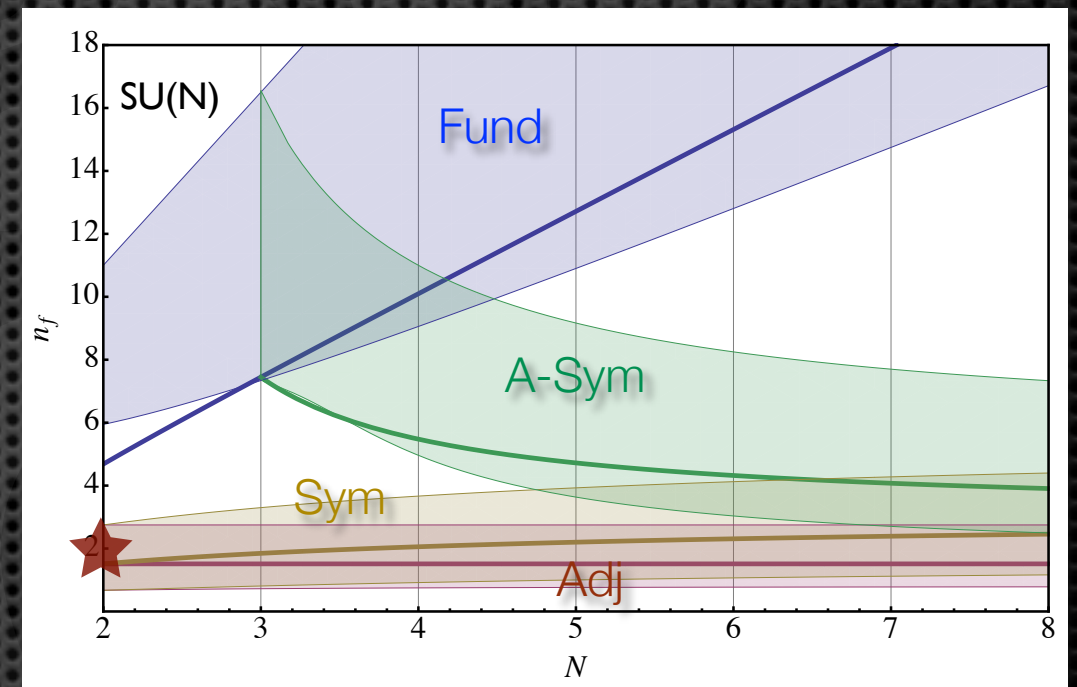
- close/inside the conformal window by analytic estimates



Minimal Walking Technicolor

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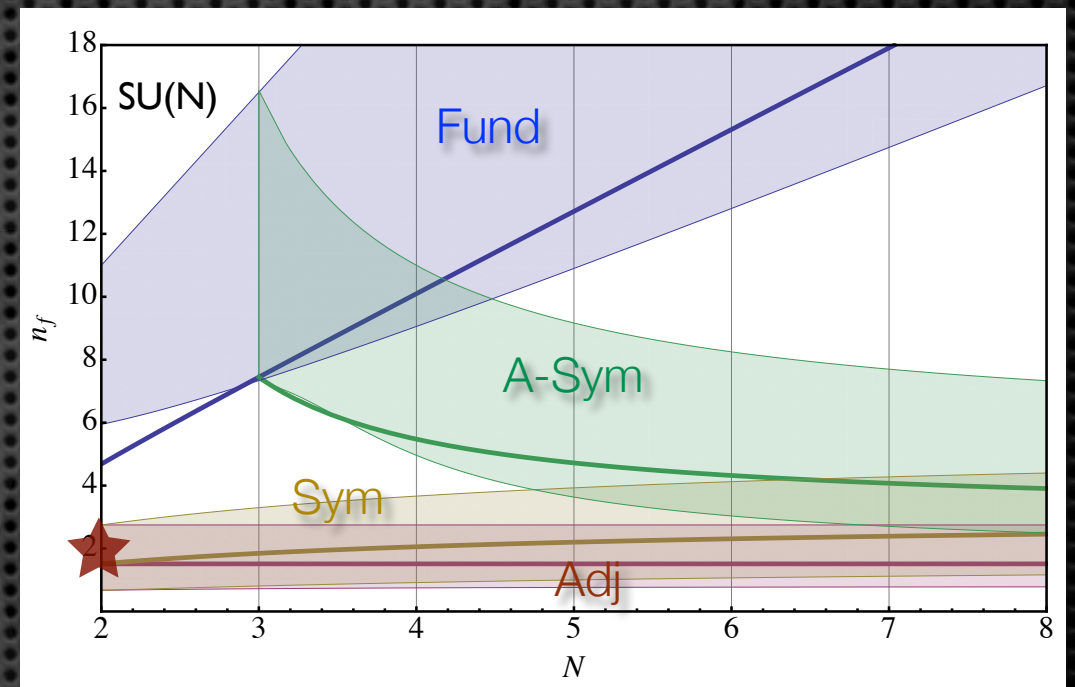


- minimum value of the naïve S-parameter: $S = \frac{N_D d_R}{6\pi}$

Minimal Walking Technicolor

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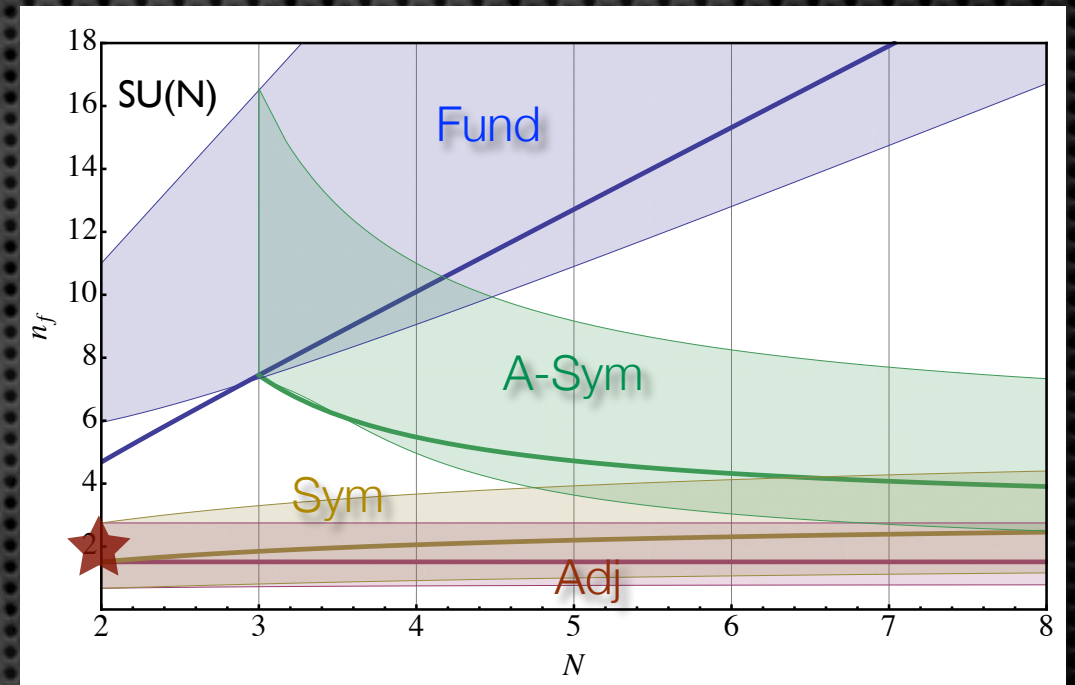


- minimum value of the naïve S-parameter: $S = \frac{N_D d_R}{6\pi}$
- expected SB pattern: $SU(4) \rightarrow SO(4) \Rightarrow 3+6$ GBs

Minimal Walking Technicolor

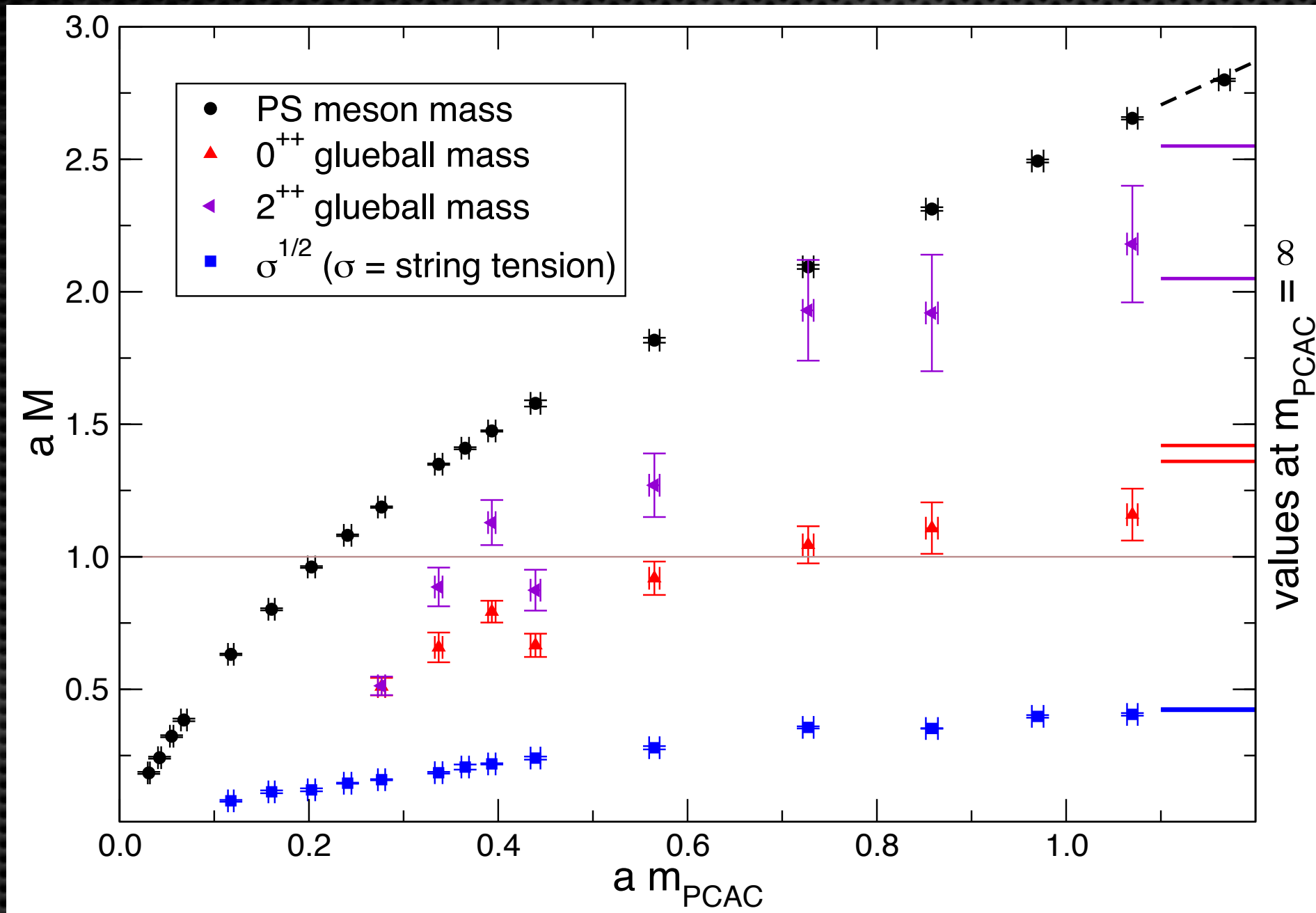
$SU(2)_{TC} + 2$ Dirac Adjoint fermions

- close/inside the conformal window by analytic estimates

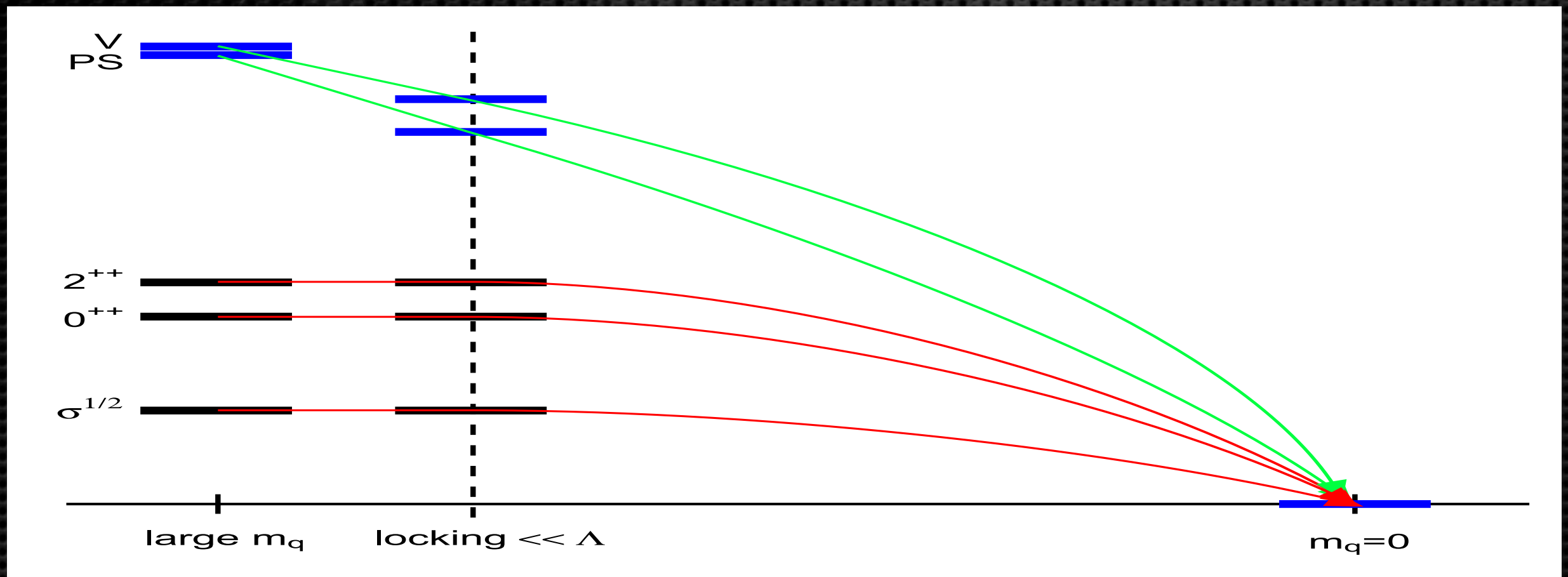


- minimum value of the naïve S-parameter: $S = \frac{N_D d_R}{6\pi}$
- expected SB pattern: $SU(4) \rightarrow SO(4) \Rightarrow 3+6$ GBs
- glue-fermion composite states

MWT Spectrum



IR conformal scaling



$$\sigma \simeq \sigma^{(YM)}$$

$$M_G \simeq M_G^{(YM)}$$

$$M_V / M_{PS} \simeq 1$$

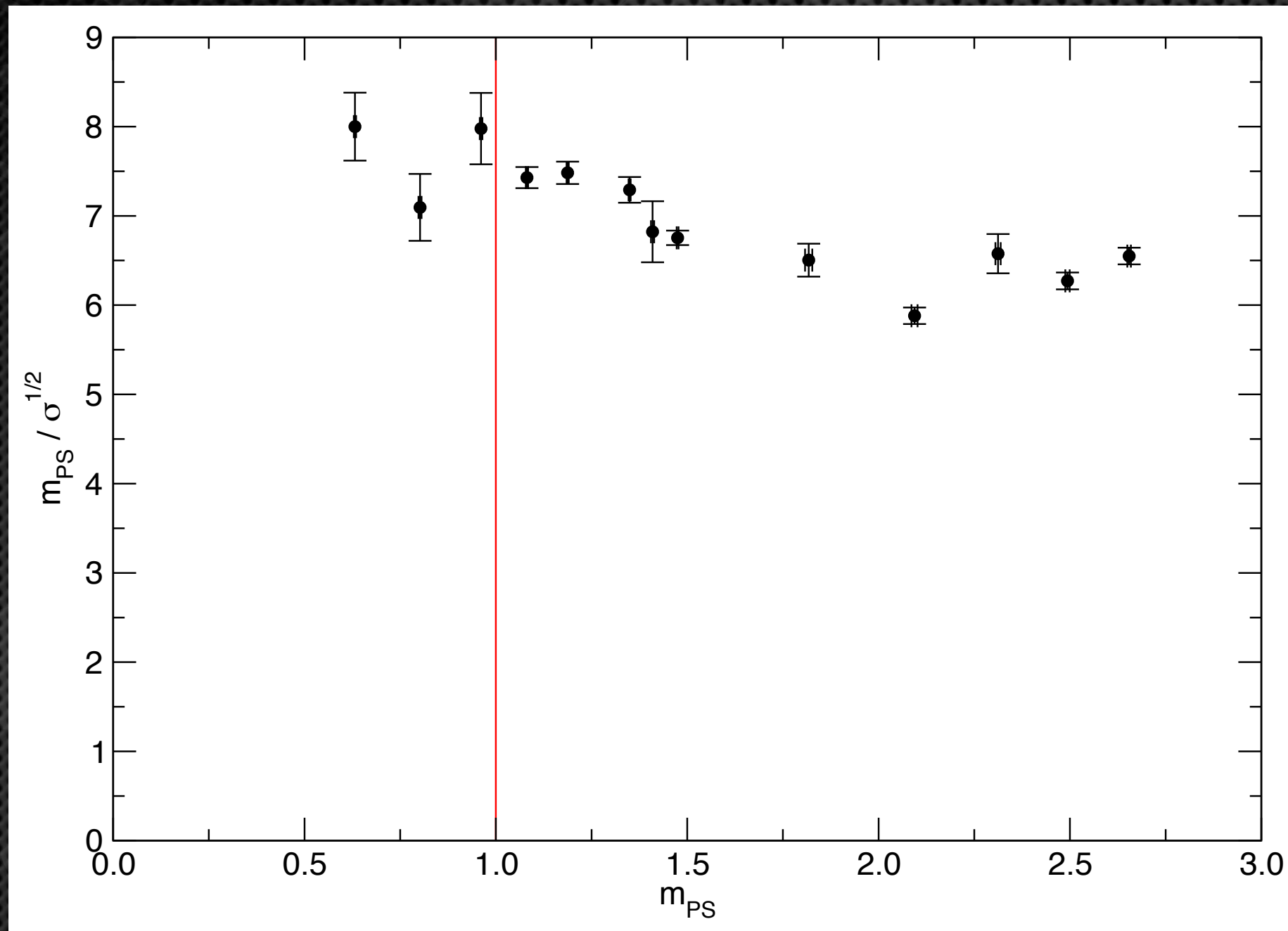
$$M_{PS} \simeq M_V \simeq 2m_q$$

$$M_V / M_{PS} \simeq 1 + \epsilon$$

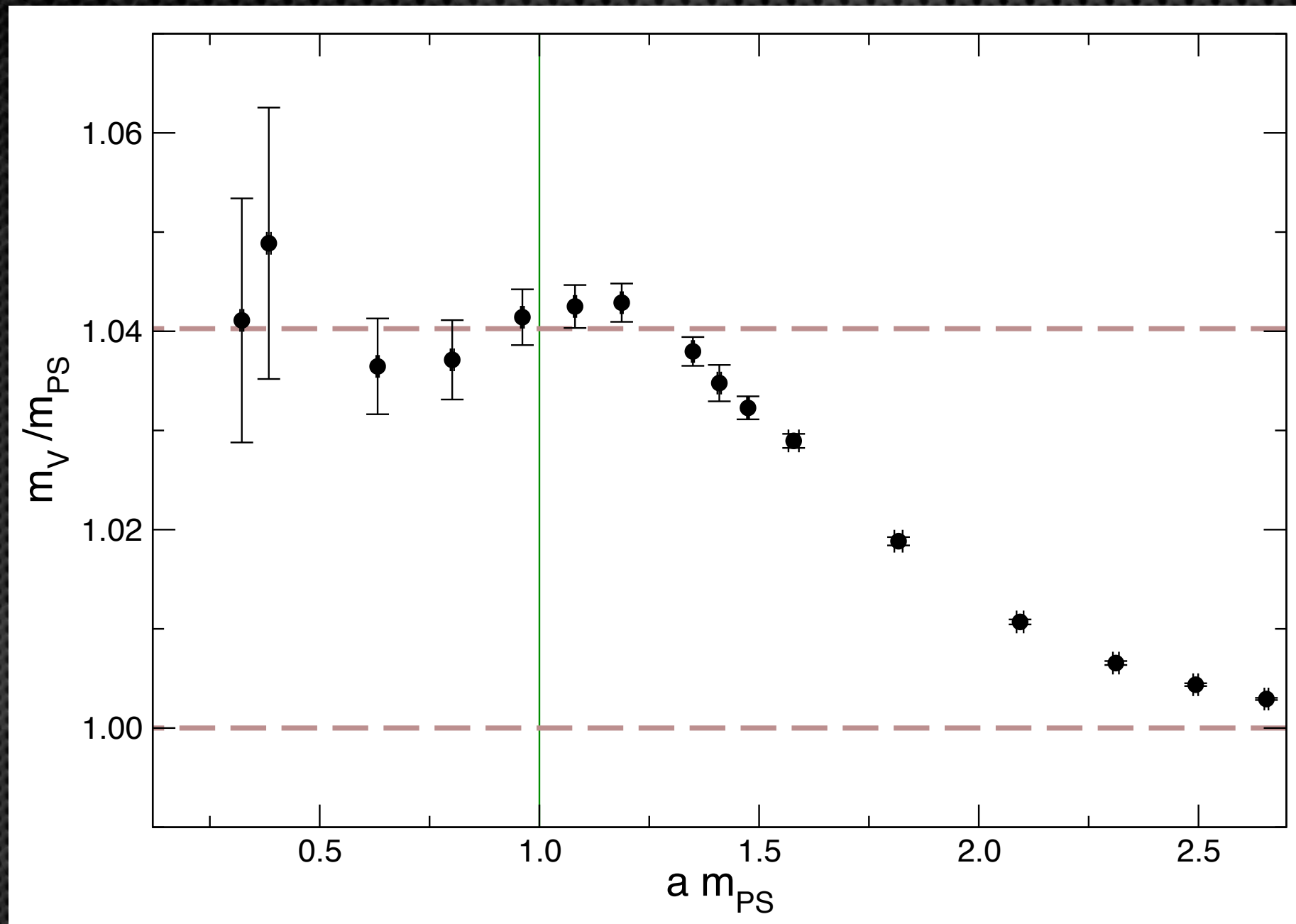
$$M_{PS} \gg \sigma^{1/2}$$

$$M_G / \sigma^{1/2} \simeq [M_G / \sigma^{1/2}]^{(YM)}$$

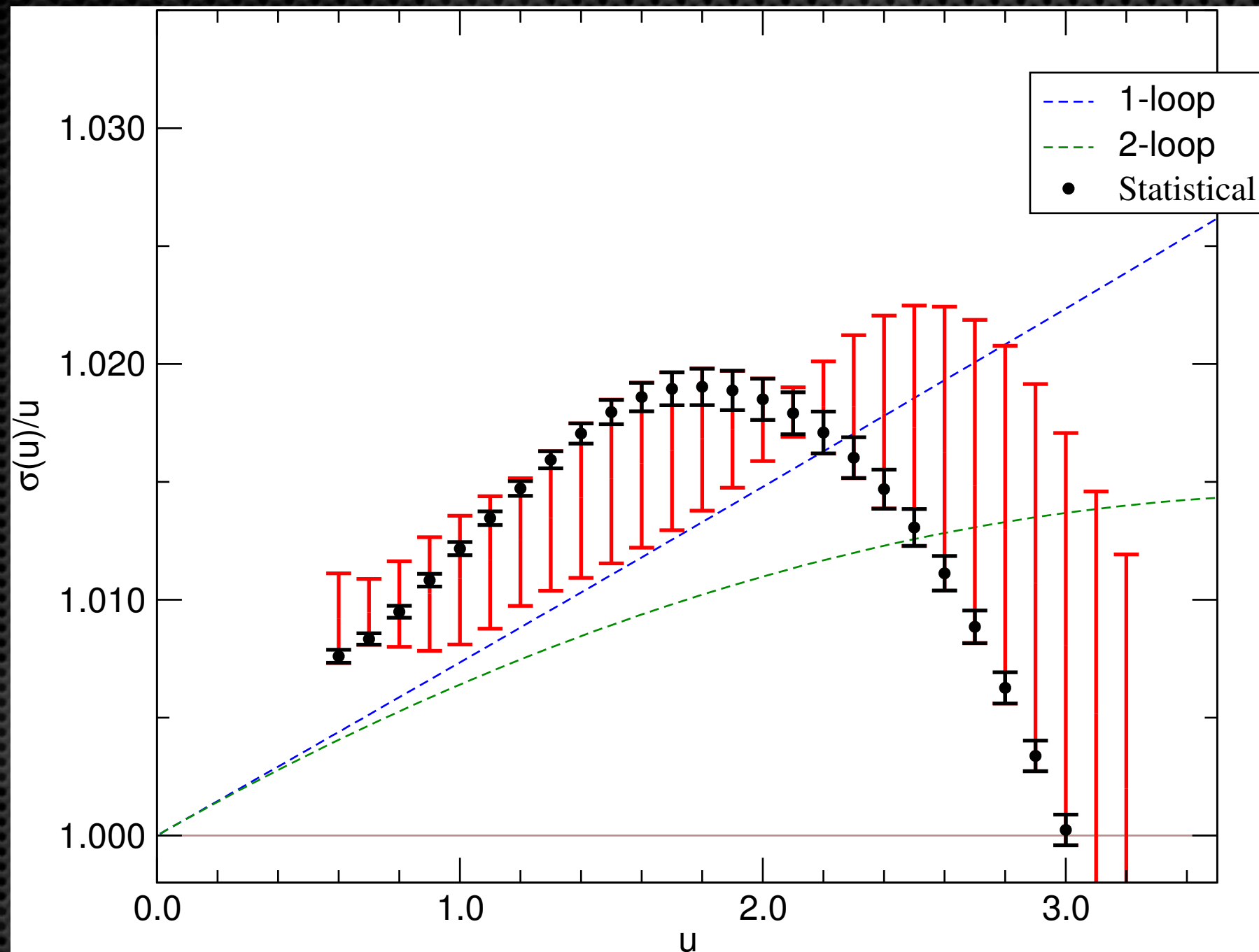
String Tension vs m_{PS}



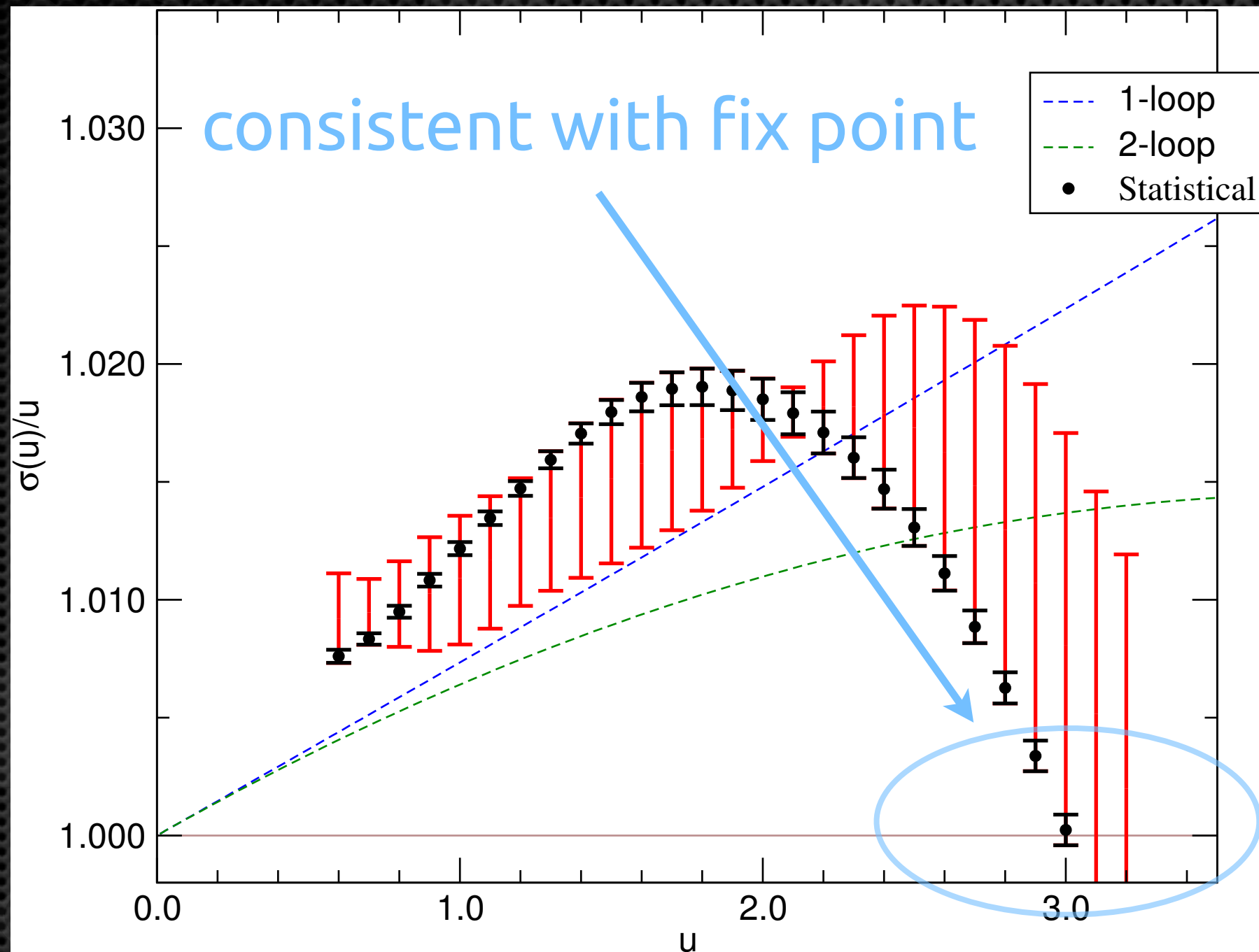
Vector vs Pseudoscalar



Schrödinger Functional coupling



Schrödinger Functional coupling



Chirally rotated Schrödinger Functional

S. Sint, PoS LAT2005 (2006) 235

S. Sint, Nucl. Phys. B847 (2011) 491-531

S. Sint & P. Vilaseca, PoS LATTICE2011 (2011) 091

S. Sint & P. Vilaseca, PoS LATTICE2012 (2012) 031

χ S F

We consider the functional integral on a hypercylinder with periodic spacial B.B. and Dirichlet B.C. in time with boundary fields $C(\eta)$ and $C'(\eta)$:

$$Z[\eta] = e^{-\Gamma[\eta]} = \int_{\eta} DUD\psi D\bar{\psi} e^{-S[U,\psi,\bar{\psi}]}$$

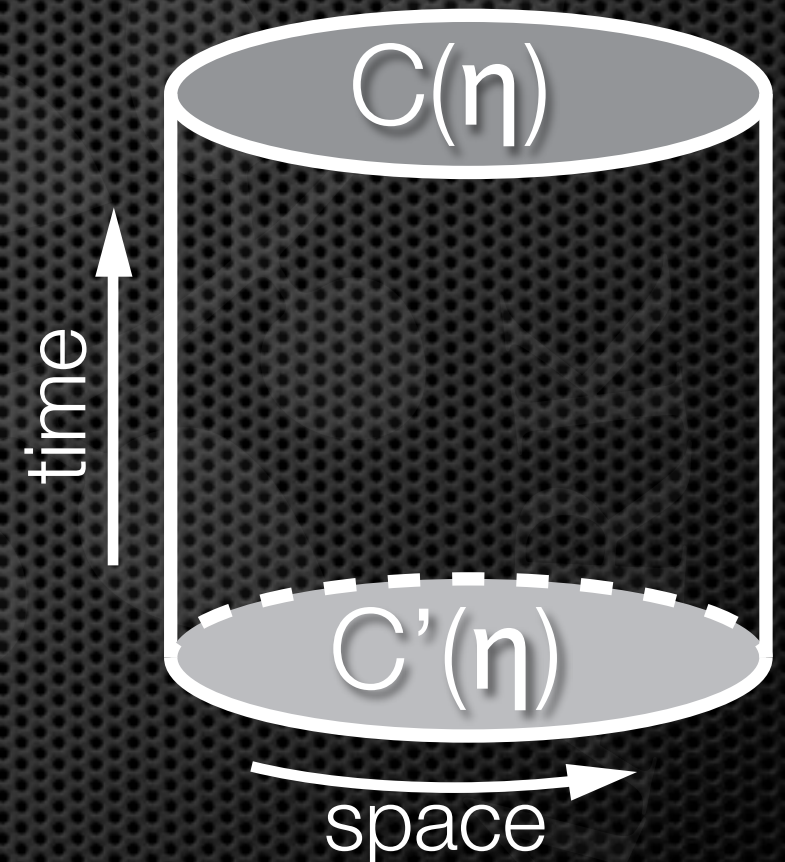
For SU(2) we use:

$$C : U_k(t=0) = \exp[-i\phi\tau^3/L]$$

$$C' : U'_k(t=0) = \exp[-i\phi'\tau^3/L]$$

with

$$\phi = \eta \quad ; \quad \phi' = \pi - \eta$$



We will also consider HALF background field configurations with:

$$\phi_{HB} = \phi/2 \quad ; \quad \phi'_{HB} = \phi'/2$$

χ S F

For the fermions B.C. we have for $N_f=2$:

$$\tilde{Q}_+ \Psi(t=0) = 0 = \tilde{Q}_- \Psi(t=L)$$

$$\bar{\Psi}(t=0) \tilde{Q}_+ = 0 = \bar{\Psi}(t=L) \tilde{Q}_-$$

with:

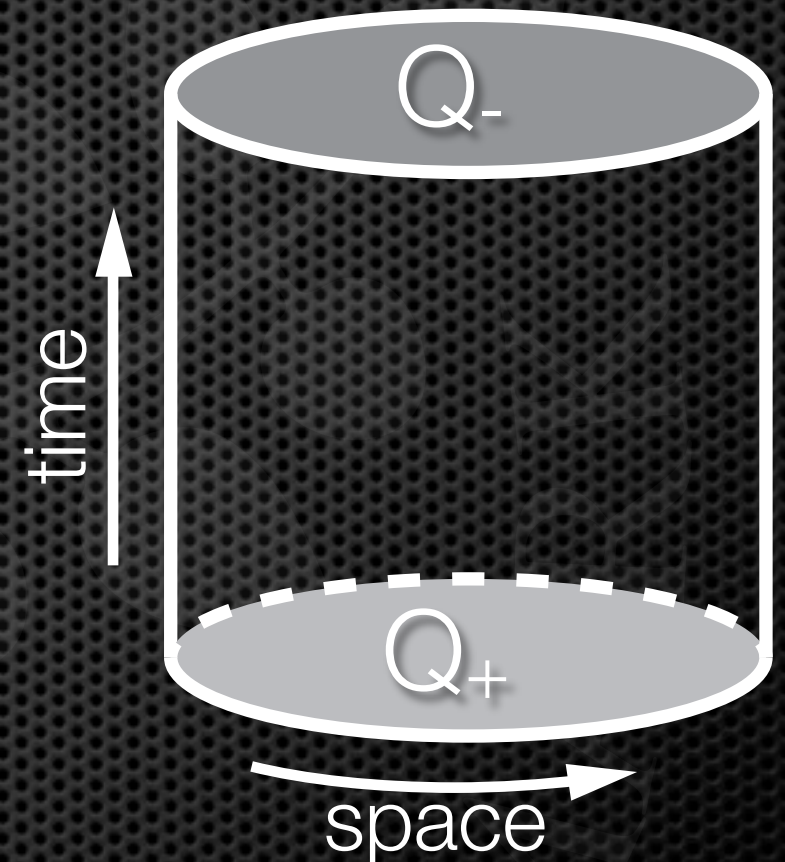
$$\tilde{Q}_\pm = \frac{1}{2} (1 \pm i\gamma_0 \gamma_5 \tau^3)$$

This is related to the standard SF via a chiral rotation:

$$\Psi \rightarrow R(\alpha) \Psi \quad , \quad R(\alpha) = \exp(i\alpha \gamma_5 \tau^3 / 2)$$

and the projections are:

$$P_\pm(\alpha) = \frac{1}{2} [1 \pm \gamma_0 \exp(i\alpha \gamma_5 \tau^3)]$$



χ S F

O(a) improving requires 3 boundary counterterms: c_t, z_f, d_s

In perturbation theory: $c_t = 1 + c_t^{(1)} g_0^2 + \mathcal{O}(g_0^4)$

$$d_s = 1/2 + d_s^{(1)} g_0^2 + \mathcal{O}(g_0^4)$$

We use $d_s=1/2$ and the 1-loop expression for c_t .

We remain with one parameter z_f we tuned non-perturbatively.

This is done tuning to zero a $\gamma_5 \tau^1$ -odd operator.

In this work we use $g_{A+}^{ud}(x_0)$

χ S F

The χ SF coupling is defined as usual: $\bar{g}^2 = \frac{\Gamma'_0(\eta)}{\Gamma'(\eta)} \Big|_{\eta=\pi/4}$

From the step scaling function:

$$\Sigma(u, s, a/L) = \bar{g}^2(g_0, sL/a) \Big|_{\bar{g}^2(g_0, L/a)=u}$$

we can obtain the beta function:

$$\sigma(u, s) = \lim_{a/L \rightarrow 0} \Sigma(u, s, a/L) \quad -2 \log s = \int_u^{\sigma(u, s)} \frac{dx}{\sqrt{x} \beta(\sqrt{x})}$$

$$\beta(u) = 0 \quad \Rightarrow \quad \sigma(u, s) = u$$

Preliminary Lattice results

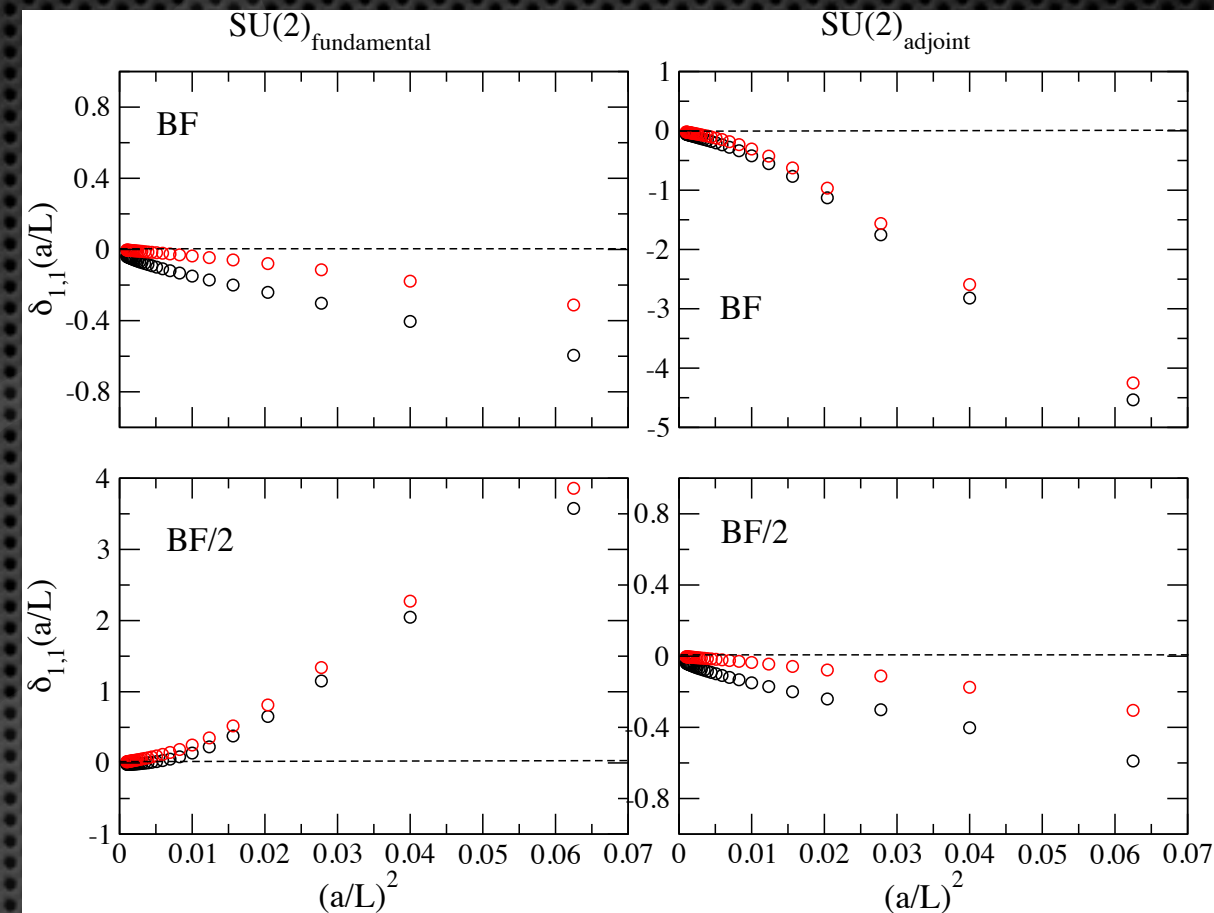
R. Arthur, L. Del Debbio, B. Lucini, A. Patella, CP, A.Rago, S. Sint, P. Vilaseca *in preparation*

Simulation details

$$\Sigma(u, 2, a/L) = u + \Sigma_1(a/L)u^2 + \mathcal{O}(u^3)$$

$$\sigma(u, 2) = u + \sigma_1 u^2 + \mathcal{O}(u^3)$$

$$\delta_1(a/L) = \frac{\Sigma_1(a/L) - \sigma_1}{\sigma_1}$$



For fermion fields we use spatial B.C. periodic up to a phase:

$$\Psi(x + L\hat{k}) = e^{i\theta}\Psi(x) \quad ; \quad \bar{\Psi}(x + L\hat{k}) = e^{-i\theta}\bar{\Psi}(x)$$

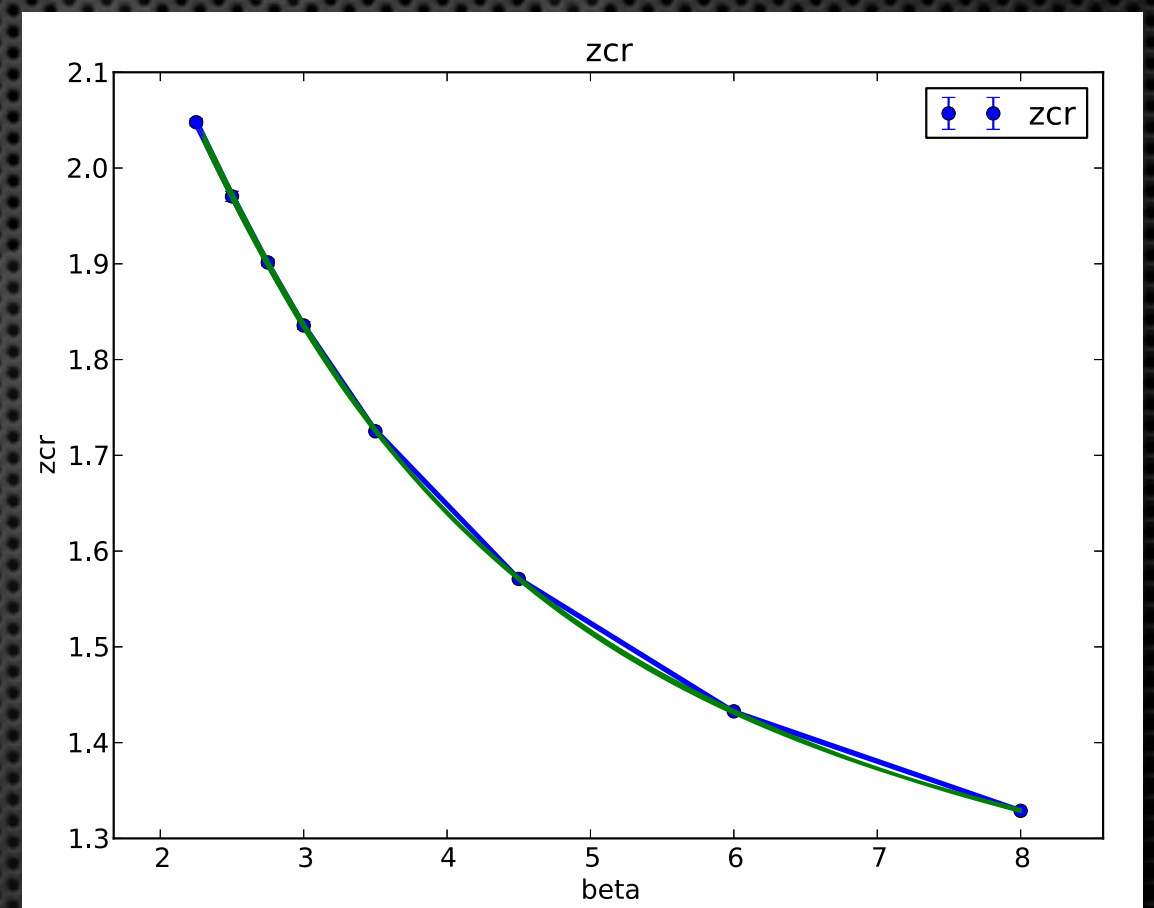
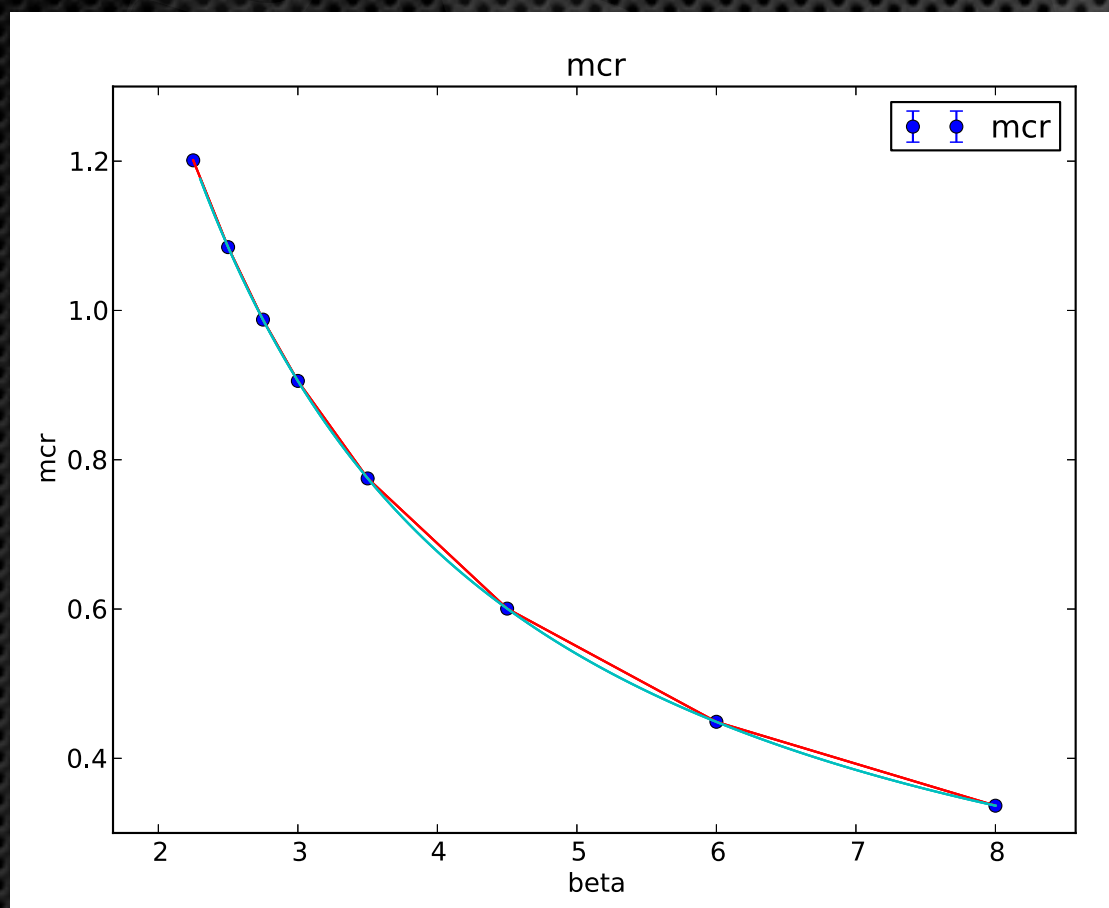
to maximise the lowest eigenvalue of the Dirac operator.

Simulation details

$L = 6, 8, 12, 16$; we plan also $L = 24$

$\beta = 2.25 \dots 8$

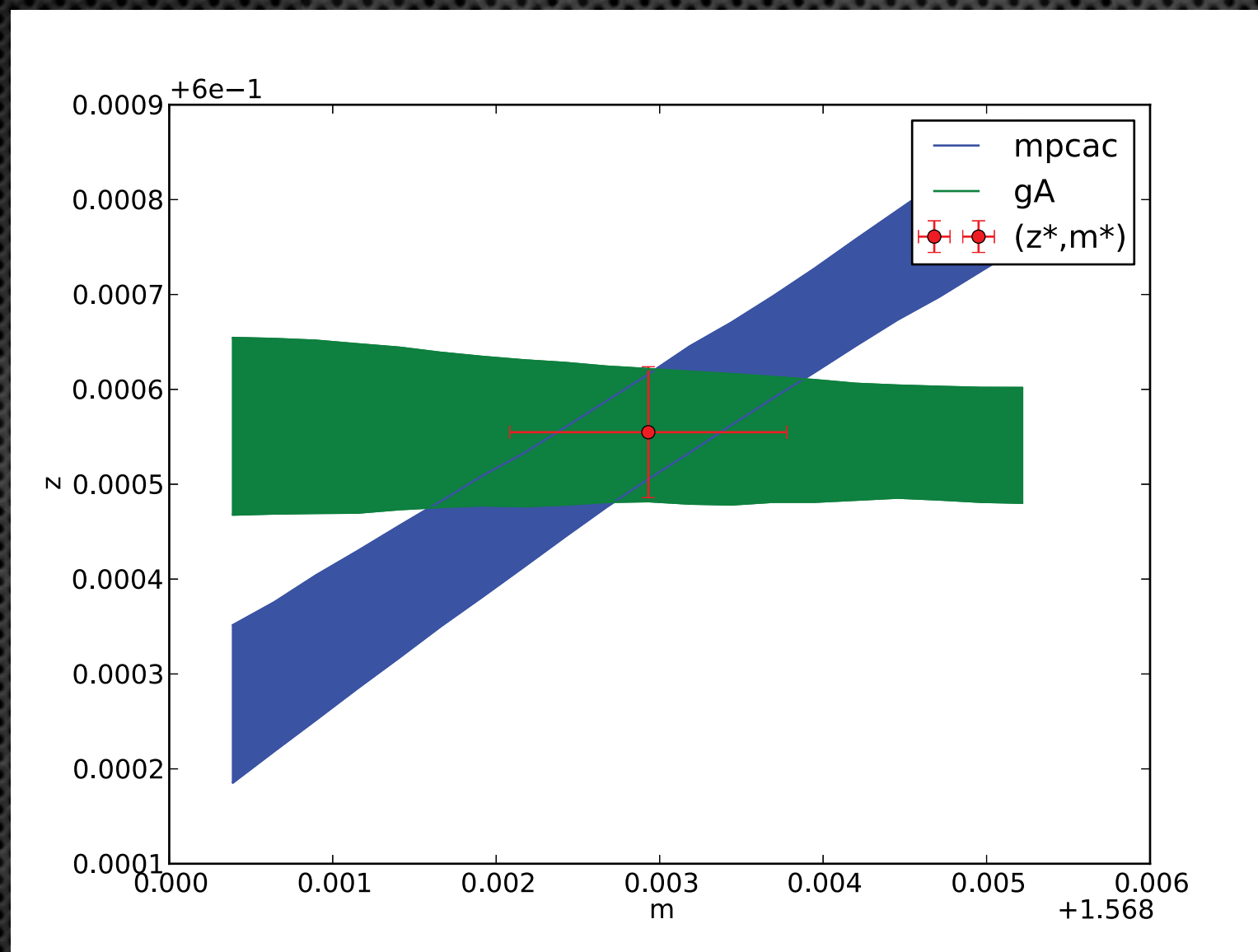
$s = 2$ (scaling factor)



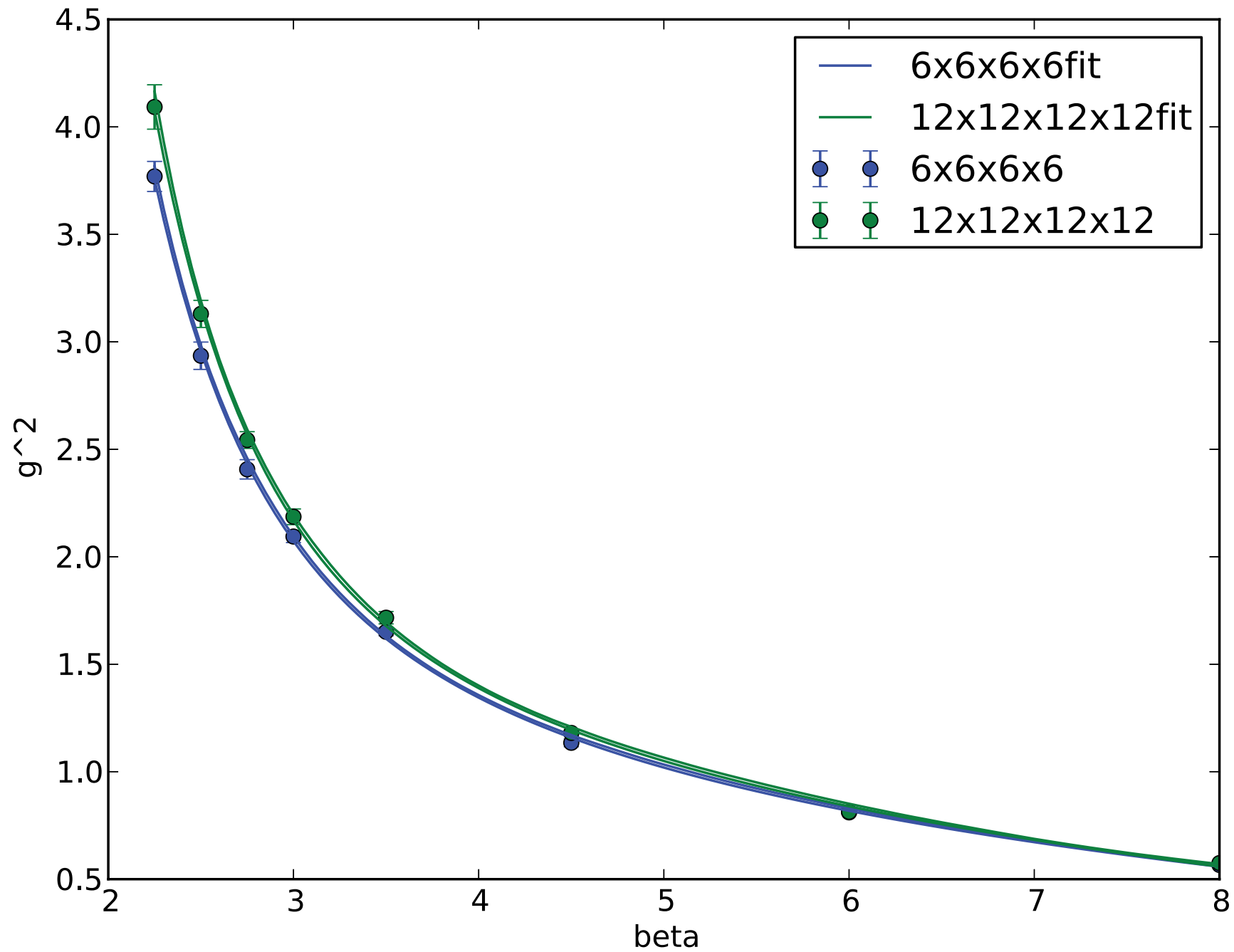
Tuning

For each volume and bare coupling, we tune 2 parameters: m_0 and z_f .

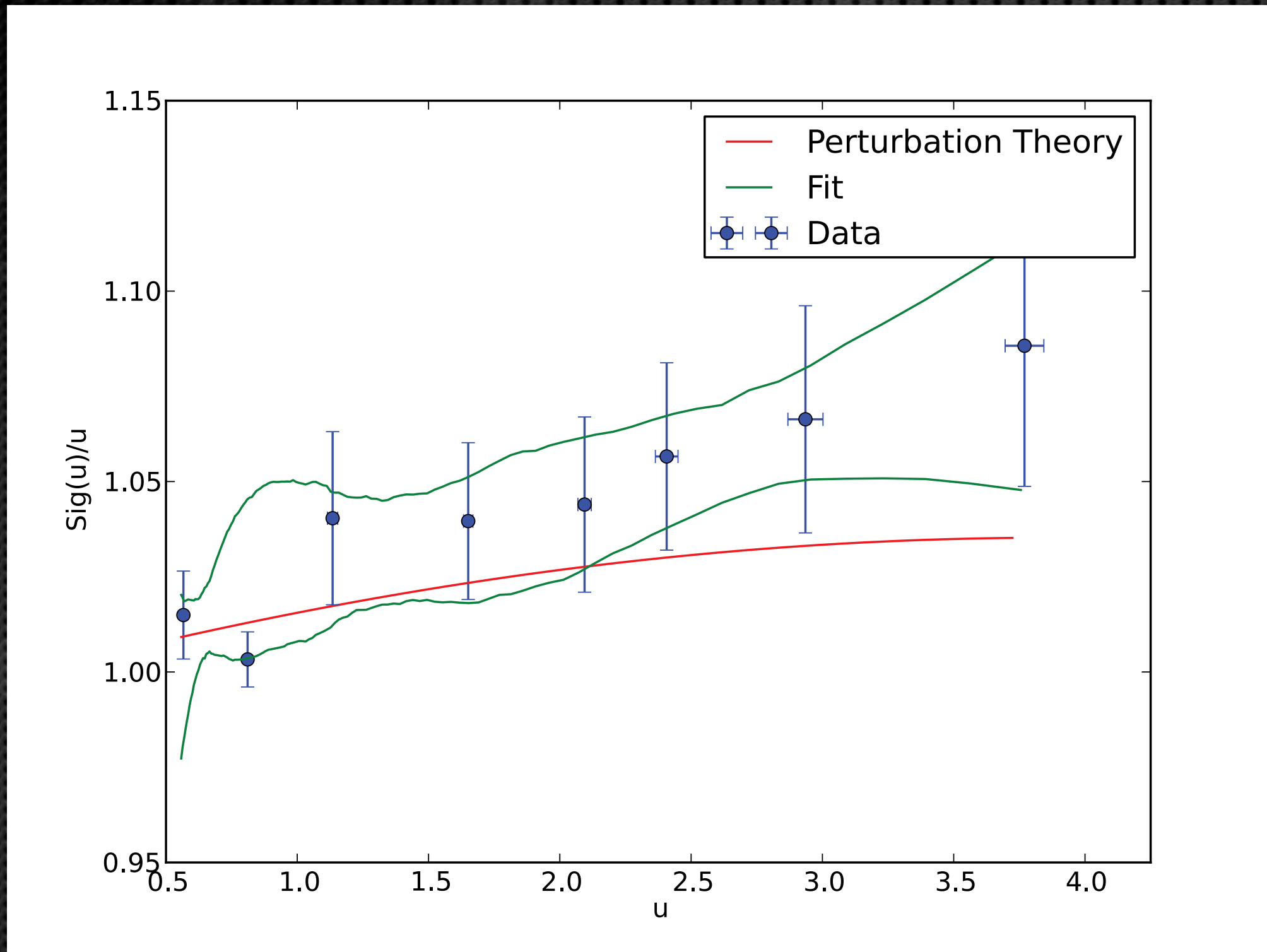
This is done by imposing the vanishing of the PCAC mass and of g_{A+}^{ud}



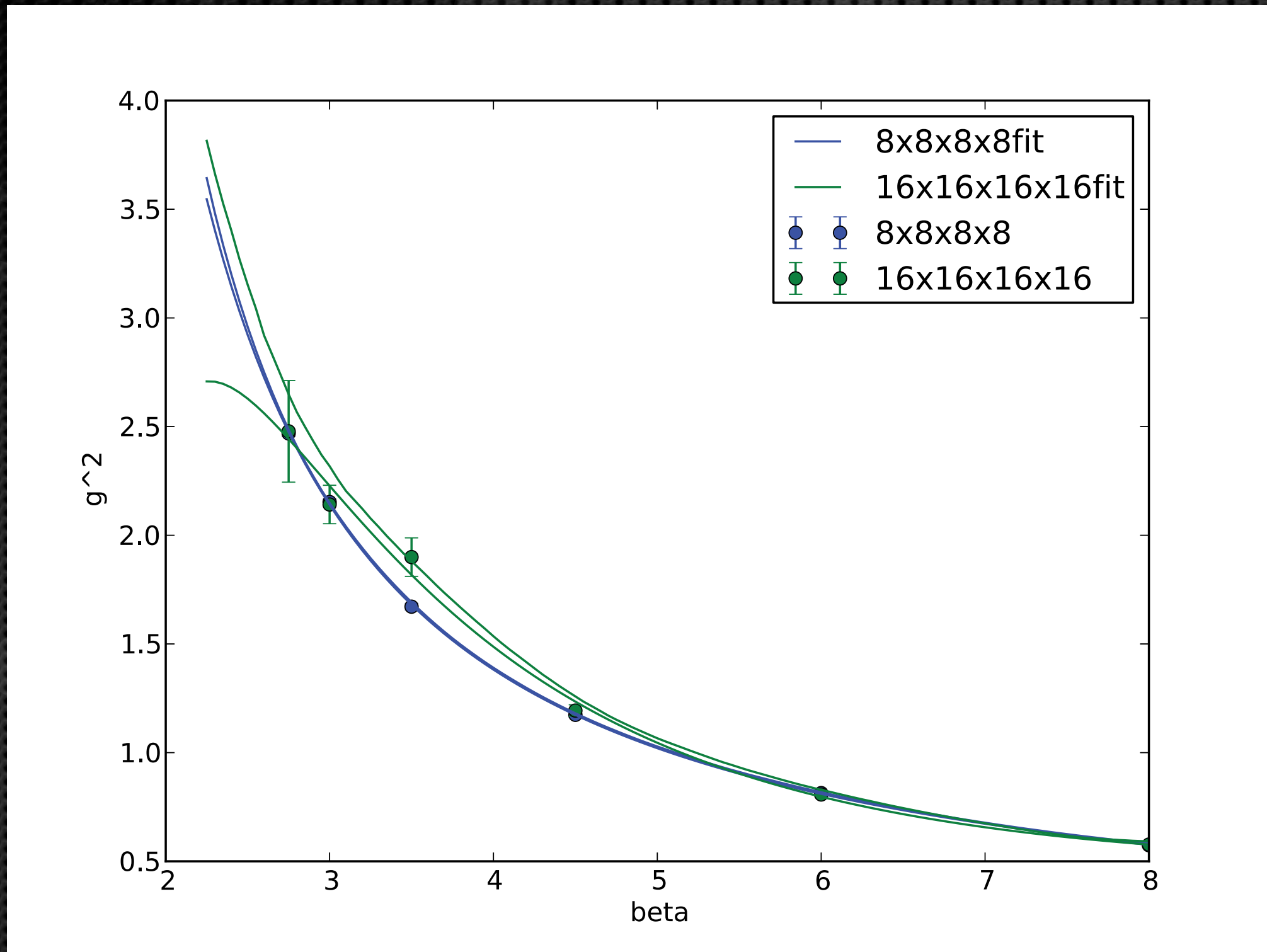
Coupling



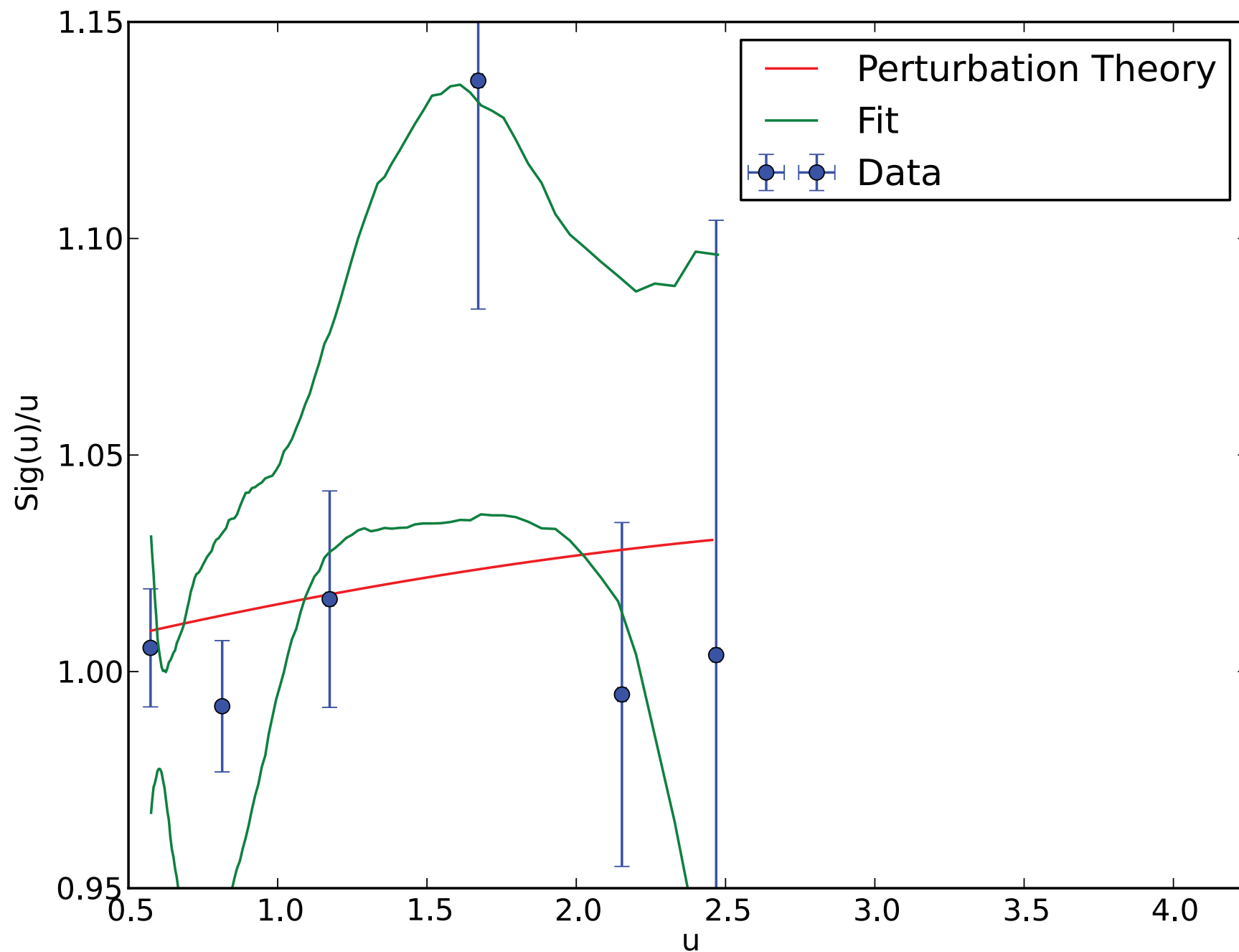
Step scaling



Coupling

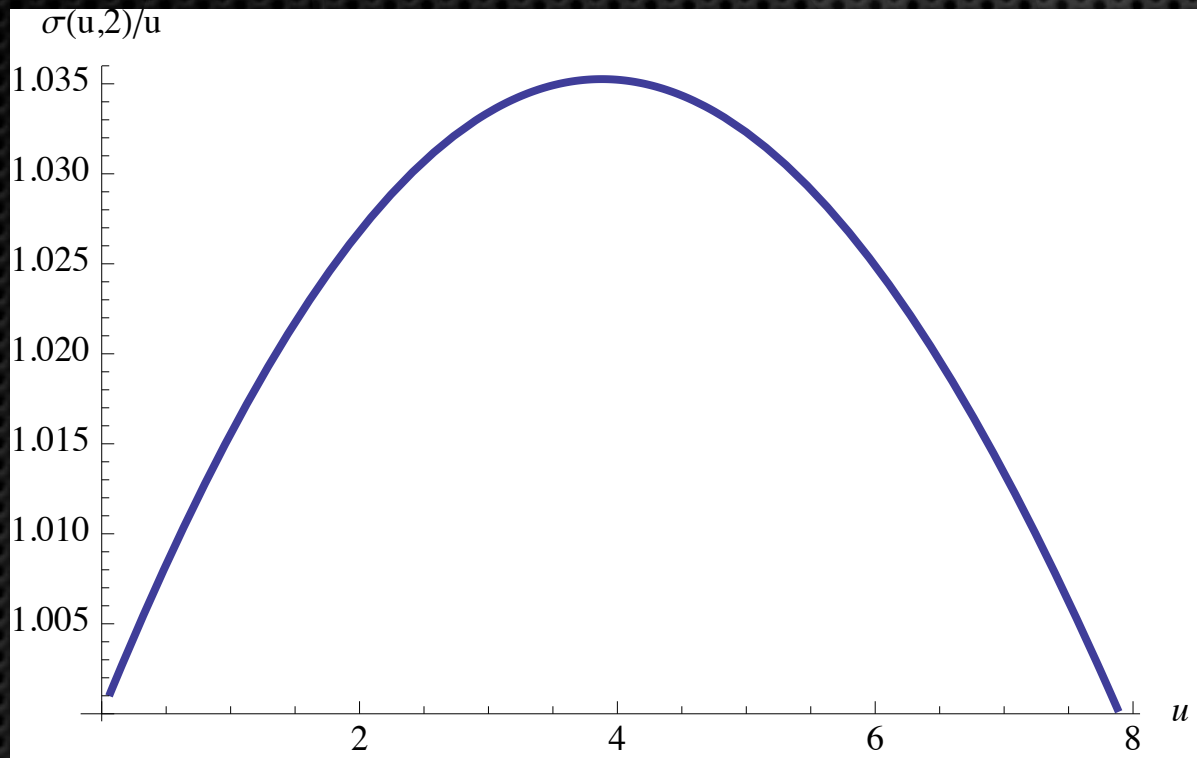


Step scaling

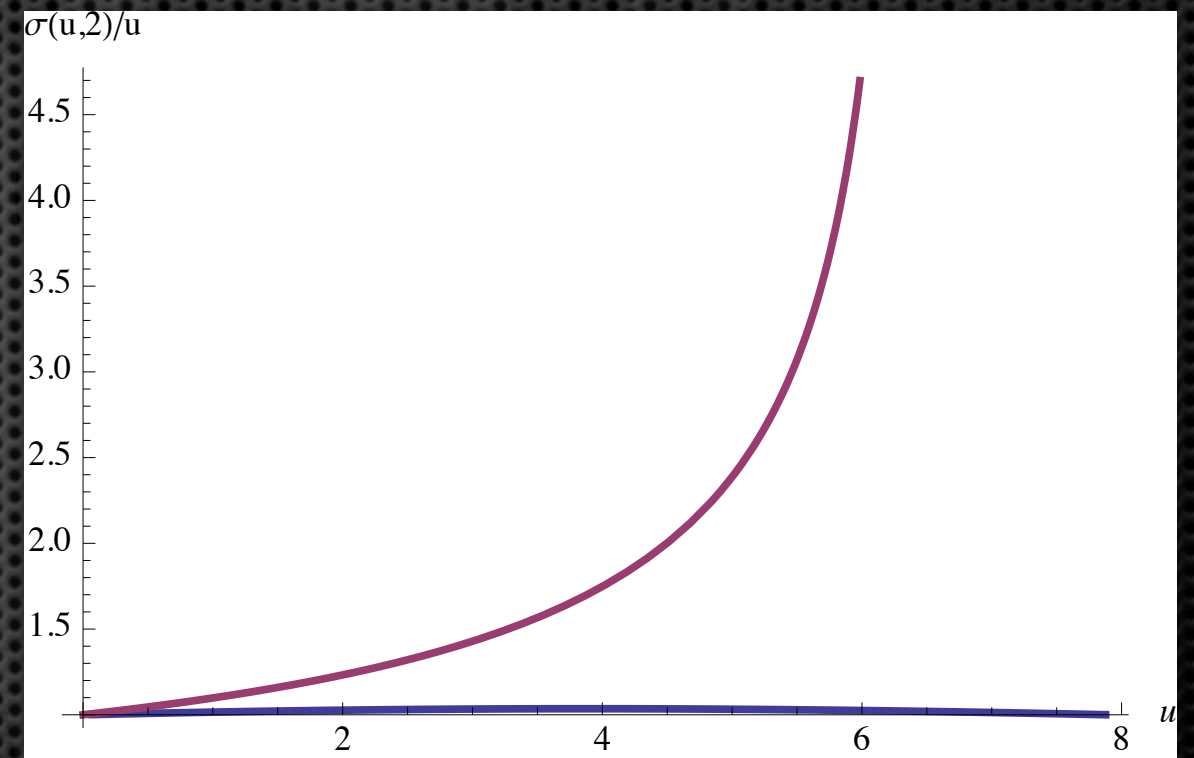


2-loop beta function

MWT



QCD $n_f=2$



Conclusions

- χ SF tuning seems to work as expected, but expensive at stronger couplings
- need more statistics to reduce errors on the step scaling functions
- continuum extrapolation is needed to investigate the presence of the IR fixed point
- models close or inside the CW are expensive to study on the Lattice!