

We are now working supplementing these anisotropic hydro equations for λ, ξ (equivalently for $\pi_{RS}^{\mu\nu}$) by IS equations for the remaining (smaller)

$\tilde{\pi}^{\mu\nu}$ components \rightarrow viscous anisotropic hydrodynamics

7) Viscous 0+1D expansion (viscous Bjorken solution)

$$u^\mu = (dt/d\tau, 0, 0, dz/d\tau) = \left(\frac{t}{\tau}, 0, 0, \frac{z}{\tau}\right)$$

$$\pi_{NS}^{\mu\nu} = 2\eta \nabla^{\langle\mu} u^{\nu\rangle} = \eta \left(\nabla^\mu u^\nu + \nabla^\nu u^\mu - \frac{1}{3} \Delta^{\mu\nu} \theta \right)$$

$$\Rightarrow \pi_{NS}^{xx} = \pi_{NS}^{yy} = \frac{2\eta}{3\tau} > 0 \quad \pi_{NS}^{zz} = -(\pi_{NS}^{xx} + \pi_{NS}^{yy}) = -\frac{4\eta}{3\tau} < 0$$

$$\Rightarrow \begin{aligned} p_\perp &= p + \pi_{NS}^{xx} \rightarrow p + \frac{2\eta}{3\tau} \\ p_L &= p_L + \pi_{NS}^{zz} \rightarrow p - \frac{4\eta}{3\tau} \end{aligned}$$

no other non-zero components at $z=0$

\leftarrow can become negative!

anisotropic pressure!

Ignore bulk pressure π ,

Viscous hydro equation:

$$\begin{aligned} \dot{\epsilon} &= -(\epsilon + p)\theta + \pi_{\mu\nu} \sigma^{\mu\nu} = -\frac{\epsilon + p}{\tau} + 2 \frac{\pi_{xx}}{\tau} \\ &= -\frac{\epsilon}{\tau} (1 + c_s^2) + \frac{2}{\tau} \pi_{xx}(\tau) \end{aligned} \quad \left. \vphantom{\begin{aligned} \dot{\epsilon} &= -(\epsilon + p)\theta + \pi_{\mu\nu} \sigma^{\mu\nu} = -\frac{\epsilon + p}{\tau} + 2 \frac{\pi_{xx}}{\tau} \\ &= -\frac{\epsilon}{\tau} (1 + c_s^2) + \frac{2}{\tau} \pi_{xx}(\tau) \end{aligned}} \right\} \text{IS}$$

I-S equation for π_{xx} :

$$\dot{\pi}_{xx} = -\frac{1}{\tau} \left(\pi_{xx} - \frac{2\eta}{3\tau} \right) - \frac{4}{3} \frac{\pi_{xx}}{\tau}$$

Anisotropic hydro equations:

$$\begin{aligned} \frac{1}{1+\xi} \partial_z \xi - \frac{z}{\tau} - 6 \partial_z \log \lambda &= \frac{4}{\tau} \left(1 - R^{3/4}(\xi) \sqrt{1+\xi} \right) \\ \frac{R(\xi)}{R(\xi)} \partial_z \xi + 4 \partial_z \log \lambda &= \frac{1}{\tau} \left(\frac{1}{\xi(1+\xi)R(\xi)} - \frac{1}{\xi} - 1 \right) \end{aligned} \quad \left. \vphantom{\begin{aligned} \frac{1}{1+\xi} \partial_z \xi - \frac{z}{\tau} - 6 \partial_z \log \lambda &= \frac{4}{\tau} \left(1 - R^{3/4}(\xi) \sqrt{1+\xi} \right) \\ \frac{R(\xi)}{R(\xi)} \partial_z \xi + 4 \partial_z \log \lambda &= \frac{1}{\tau} \left(\frac{1}{\xi(1+\xi)R(\xi)} - \frac{1}{\xi} - 1 \right) \end{aligned}} \right\} \text{AHYDRO}$$