Introduction to Hard Probes in Heavy Ion Collisions

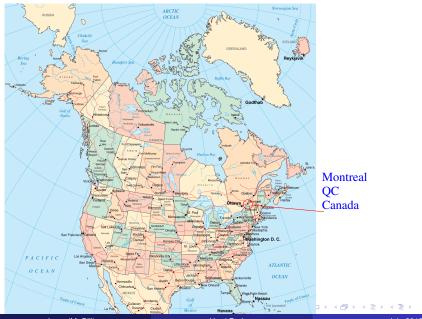
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11th Nuclear Physics Summer School Jeju Island, Korea, June 2013

Jeon (McGill)

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Hard Probes

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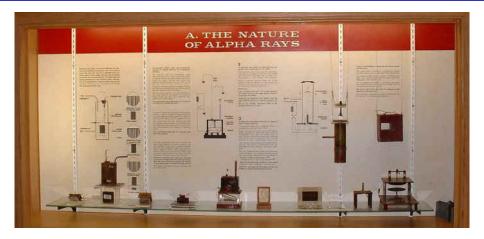






Mr. McGill going home after a hard day's work.

Jeon (McGill)



Rutherford carried out his Nobel (1908) winning work at McGill (1898-1907). His *original* equipments on display

Jeon (McGill)

Hard Probes

- Charles Gale
- Sangyong Jeon
- Björn Schenke (Formerly McGill, now BNL)
- Clint Young (Formerly McGill, Now UMinn)
- Gabriel Denicol
- Matt Luzum

- Sangwook Ryu
- Gojko Vujanovic
- Jean-Francois Paquet
- Michael Richard
- Igor Kozlov
- Khadija El Berhoumi
- Jean-Bernard Rose

Before I begin... Some thoughts I'd like to share

Disclaimer: These are my own thoughts. Everyone is different. Take these with a grain of salt.

- Passion for Physics!
- Communication skill Improve your English
 - Writing skill Writing guide books help A good one: *BUGS in Writing: A Guide to Debugging Your Prose*, by Lyn Dupre
 - Presentation skill Have a look at R. Geroch's *"Suggestions for Giving Talks"*, arXiv:gr-qc/9703019v1.
 - Debate skill Practice thinking in English
 - Social communication skill Read novels (paperbacks are better), watch sitcoms, know the culture, slang, ...

Approach it as if you're writing a story Story <u>Arti</u>

- Introduction Make the reader interested in the rest of the story
- Expanding the story Main characters, main events, conflicts, puzzles, ...
- Resolution Story escalates to the ultimate resolution by a big battle, saved by the heroes/heroines.
- Ending Tie up loose ends. Make the reader want to read the sequel.

<u>Árticle/Talk</u>

- Introduction Make the reader interested in the rest of the paper/talk
- Expanding the point Main physics points, main data, conflicts, puzzles, ...
- Resolution What big physics the new data/theory illuminates/resolves. Saved by the heroes/heroines.
- Conclusion Tie up loose ends. Make the reader want to read the sequel.

On to Physics

Jeon ((McGill)

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• Why do it?

- To study QGP
- Most extreme environment ever created: $T \sim 1 \, \text{GeV}$. This existed only at around 1 microsecond after the Big Bang
- How do we understand it?
 - Theory: Many-body QCD
 - Experimental probes:
 - Soft
 - Hard

- Hard Probes \sim Large momentum/energy phenomena
- pQCD applies We know how to do this
- Produced *before* QGP is formed in the same way as in hadron-hadron collisions
- Difference between *pp*, *pA* and *AA* tells us about the medium.
- Caveat: How well do we know the nuclear initial state?

Medium properties

- What is it made of? Quarks? Gluons? Hadrons?
- Thermodynamic properties Temperature, Equation of state, etc.
- Transport properties Mean-free-path, transport coefficients, etc.
- Tools
 - Jets
 - Hard Photons

pQCD

- 2 Jet Quenching
- Hard Photons

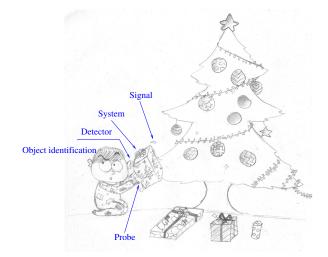
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• Early hard probe experiments



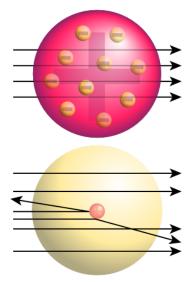
What is a hard probe?

Early hard probe experiments



What is a hard probe?

• Early hard probe experiments

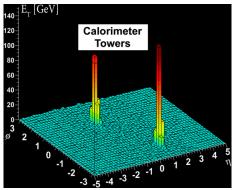


• Rutherford's α scattering experiment

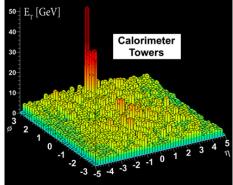
$$\frac{d\sigma}{d\cos\theta} = \frac{\pi}{2}Z^2\alpha_{\rm EM}^2\left(\frac{\hbar c}{E_{\rm kin}}\right)^2 \times \frac{1}{(1-\cos\theta)^2}$$

- Small angle scattering dominates $d\sigma/d\cos\theta \propto 1/\theta^4$
- But backscattering prob. is finite, favoring Rutherford's model over Thompson's (which causes no backscattering)

Fast-forward to the present



ATLAS: Intact dijets in Pb+Pb



ATLAS: One jet is fully quenched in Pb+Pb

- Simplest conclusion to draw: The medium is opaque.
- We want to know much more than that!

- Must be known & calculable using pQCD.
- Must be created *before* QGP forms

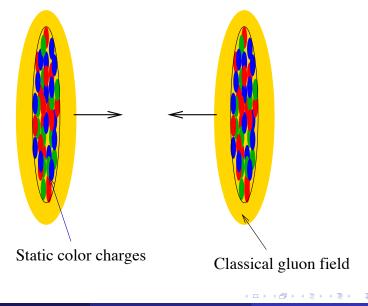
Both requirements satisfied if the energy scale is much large compared to $\Lambda_{QCD}\approx 200\,MeV$ and the length (time) scale is much shorter than \sim 1 fm.

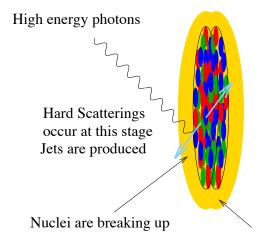
Probes

- Propagation of hard partons or "Jets"
- Quarkonium suppression
- High p_T electromagnetic probes (real and virtual photons)

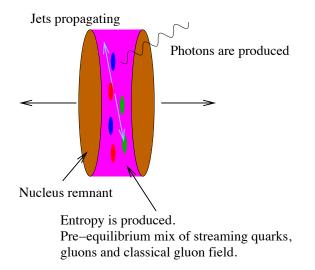
Goal

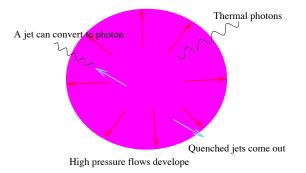
- To characterize QGP
- To characterize initial state (nPDF, CGC?)





Gluon fields are grabbing each other

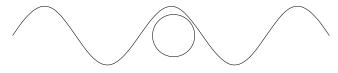




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Review of some basic concepts

• Spatial resolution: $\Delta x \Delta p \ge 1/2$





Shorter the wavelength (larger the momentum) sees spatial details up to Δ*x* ≈ λ.

Review of some basic concepts

Energy-Time uncertainty: $|\Delta E|\Delta t \ge 1/2$

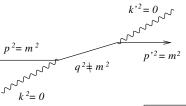
•
$$\Delta E = p^0 - \sqrt{\mathbf{p}^2 + m^2}$$
.

• If
$$\Delta E = 0$$
, then $p^{\mu}p_{\mu} = m^2$: On-shell

• If
$$\Delta E
eq 0$$
, the $p^{\mu}p_{\mu}
eq m^2$: Off-shell

Interpretation

• An off-shell state can exist only for $\Delta t \sim 1/|\Delta E|$.



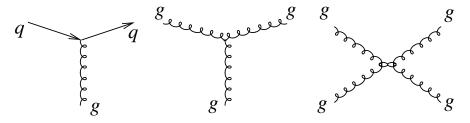
This interaction lasts $\Delta t \sim 1/|(|\mathbf{p}| + |\mathbf{k}| - \sqrt{(\mathbf{p} + \mathbf{k})^2})|$

Perturbative QCD

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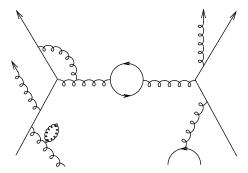
Perturbative QCD (pQCD)

QCD – Interaction of quarks and gluons



- N_f flavors of quarks
- $N_c^2 1$ gluons

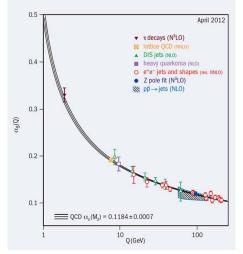
Perturbative QCD (pQCD)



Of course, things can get complicated.

- Tree diagrams of $n \leftrightarrow m$ processes
- Corrections to vertices
- Corrections to propagators

Perturbative QCD (pQCD)



S. Bethke, arXiv:1210.0325.

 Perturbative expansion possible because of asymptotic freedom

•
$$Q^2 \frac{\partial \alpha_S}{\partial Q^2} = -\beta_0 \alpha_S^2 - \beta_1 \alpha_S^3 + \cdots$$

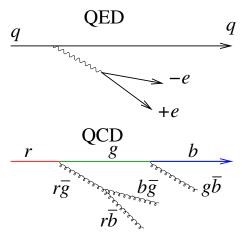
•
$$\alpha_{\mathcal{S}}(Q^2) \approx$$

 $\overline{((33-2n_f)/12\pi)\ln(Q^2/\Lambda_{\rm QCD}^2)}$

• pQCD reliable for $Q \gtrsim 1 \, {
m GeV}$

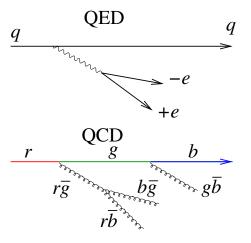
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Intuitive understanding of asymptotic freedom



- QED: Surrounded by virtual *ee* cloud
- Virtual −e cloud drawn closer to q > 0 ⇒ Screening
- Larger Q ⇒ smaller distance ⇒ Sees less of the cloud ⇒ Closer to bare charge
- Possible because the original *q* never changes and photons do not carry charges

Intuitive understanding of asymptotic freedom



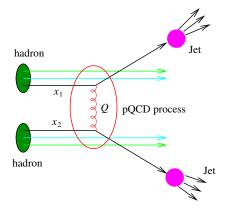
- QCD: Can resolve more soft virtual gluons at larger *Q*
- The color of the real particle can change whenever a gluon is emitted.
- Larger Q
 —> More frequent changes
 —> Less average color charge
 —> Asymptotic freedom

• As $Q \rightarrow \Lambda_{QCD}$,

$$lpha_{\mathcal{S}}(\boldsymbol{Q}^2) pprox rac{1}{((33-2n_f)/12\pi)\ln(\boldsymbol{Q}^2/\Lambda_{
m QCD}^2)}
ightarrow \infty$$

- Hadrons are $O(\Lambda_{QCD})$ objects.
- Anything that has to do with hadron properties such as color confinement and hadronization is *non-perturbative*.
- In the IR limit, perturbation theory does not work —> Factorize what can be calculated with pQCD (UV) and what cannot be calculated (IR)

Factorization Theorem



Hadron-Hadron Jet production scheme:

$$\sigma = \int_{abcd} f_{a/A}(x_a, Q_f) f_{b/B}(x_b, Q_f) \\ \times \sigma_{ab \rightarrow cd} D_{C/c}(z_C, Q)$$

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Factorization Theorem

How realistic pQCD calculations are done

 $\sigma_{hh'\to C+X} = \int_{abcd} dx_1 dx_2 f_{a/h}(x_1, Q_f) f_{b/h'}(x_2, Q_f) \sigma_{ab\to cd}(Q_R) D_{C/c}(z_C, Q_f')$

- *f_{a/h}(x*₁, *Q_f)*: Parton distribution function. Probability to have a parton type *a* with the momentum fraction *x*₁ in a hadron *h*. Depends on the factorization scale *Q_f*.
- D_{C/c}(z_C, Q'_f): Fragmentation function. Probability to create a hadron type C our of parton type c carrying the momentum fraction z_c.
- $\sigma_{ab \rightarrow cd}(Q_R)$: Parton-parton scattering cross-section.

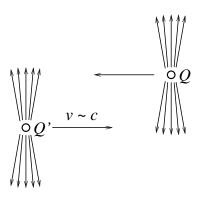
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Factorization Theorem

How realistic pQCD calculations are done

 $\sigma_{hh'\to C+X} = \int_{abcd} dx_1 dx_2 f_{a/h}(x_1, Q_f) f_{b/h'}(x_2, Q_f) \sigma_{ab\to cd}(Q_R) D_{C/c}(z_C, Q_f')$

- pQCD controls the *evolutions* of $f_{a/h}(x_1, Q_f)$ and $D_{C/c}(z_C, Q'_f)$. But pQCD cannot determine the initial data because this is dominated by IR processes.
- pQCD *can* calculate $\sigma_{ab \to cd}(Q_R)$ when the renormalization scale Q_R can be set high (that is, when \sqrt{s} is large)



- Weizsäcker-Williams field Highly contracted in the *z* direction
- Coulomb potential in the rest frame of the charge

$$\varphi = \mathbf{Q}/|\mathbf{r}|$$

In the moving frame

$$A^{\mu}(x') = \Lambda^{\mu}_{\nu}A^{\nu}(x(x'))$$

• The coordinate in the moving frame x' = (t, x, y, z). This corresponds to the rest frame position

$$\boldsymbol{x} = (t\gamma - z\gamma \boldsymbol{v}, \boldsymbol{x}, \boldsymbol{y}, z\gamma - t\gamma \boldsymbol{v}).$$

Hard Probes

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- Weizsäcker-Williams field Highly contracted in the z direction
- Coulomb potential in the rest frame of the charge

$$arphi = \mathbf{Q}/|\mathbf{r}|$$

In the moving frame

$$\mathcal{A}^{\mu} = rac{Q(\gamma, \mathbf{0}, \mathbf{0}, \gamma \mathbf{v})}{\sqrt{(z - vt)^2 \gamma^2 + \Delta \mathbf{x}_{\perp}^2}}$$

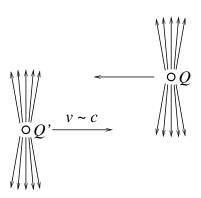
• Pure gauge in the $v \rightarrow 1$ limit

$$A^{\mu} \approx \frac{Q(1,0,0,1)}{|z - vt|} = Q\partial_{\mu} \ln |z - vt|$$

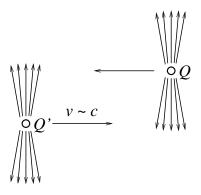
$$(1)$$

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Hard Probes



- Weizsäcker-Williams field Highly contracted in the *z* direction
 F^{µν} ≈ 0 unless *z* ≈ *vt*
- In the rest frame: Coulomb field is made up of space-like virtual photons q^μq_μ = -q² with q₀ = 0.
- In the Lab frame: $q'^{\mu} = (q^z \sinh \eta, \mathbf{q}_{\perp}, q^z \cosh \eta)$
- For large η , $|\Delta E| = |q^- - |\mathbf{q}|| \sim e^{-\eta} \mathbf{q}^2/q_z$ $\implies \Delta t \sim 1/|\Delta E| \sim e^{\eta} q_z/\mathbf{q}^2 \implies$ virtual photons look almost like real photons.



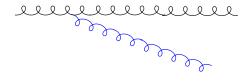
- Weizsäcker-Williams field Highly contracted in the *z* direction $F^{\mu\nu} \approx 0$ unless $z \approx vt$
- To a first approximation, the approaching particles *do not* know about each other until they are on top of each other.
- Initial photon momentum distribution factorizes: $F(x_1, x_2) = f(x_1)f(x_2)$ but this is not exact.
- In QCD, color neutrality of hadrons help.

• $f(x, Q_f)$: Probability density of partons with the virtuality *less than* Q_f .

 Q_0 : Coarse grained. You see one almost on-shell parton.

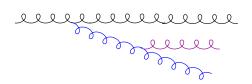
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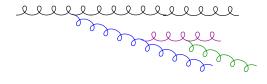
$Q_0 < Q_1$: Start to resolve another parton

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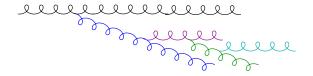


$Q_0 < Q_1 < Q_2$: And another

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$Q_0 < Q_1 < Q_2 < Q_3$: And another



You get the idea

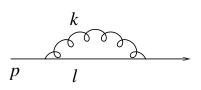
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• $f(x, Q_f)$: Probability density of partons with the virtuality *less than* Q_f .

$$Q^2 rac{\partial}{\partial Q^2} \left(egin{array}{c} q^S \ g \end{array}
ight) = rac{lpha_{\mathcal{S}}(Q^2)}{2\pi} \left(egin{array}{c} P_{qq} & 2n_f P_{qg} \ P_{gg} & P_{gg} \end{array}
ight) \otimes \left(egin{array}{c} q^S \ g \end{array}
ight)$$

where P_{ij} : Splitting function \sim Probability to end up with *ij* in the final state.

A (1) > A (2) > A



- p is on-shell: $p^2 = 0$
- Diverges when either k or l is on-shell
- This happens either *k* is very soft so that

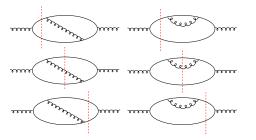
$$l^2 = (p-k)^2 \approx p^2$$

• or p and k are almost collinear

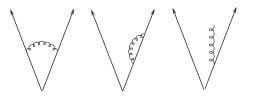
$$l^2 = (p-k)^2 = p^2 + k^2 - 2pk$$

$$\approx 0$$

Splitting can cause IR divergence



- g
 ightarrow q ar q and g
 ightarrow q ar q g
- Only the *sum* is IR finite because soft and collinear divergences
- Splitting functions know about this



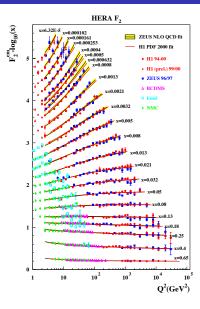
- Observables must be IR safe.

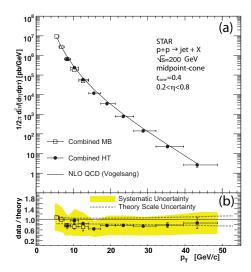
- Splitting function similarly runs
- 3 different scales: Q_f for the pdf, Q_R for σ(Q_R) and Q'_f for the fragmentation function
- In principle, physical observables should not depend on these scales. However, factorization theorem is only *approximate*.
- Lots of freedom to choose the scales. Usually something like

$$Q_f = Q_R = Q'_f = \# p_T$$

works OK where p_T is the momentum of the *final* state particle.

pQCD & Factorization at work





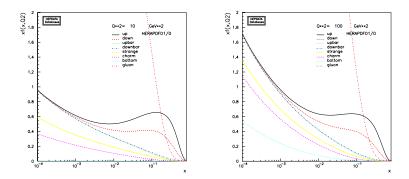
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pQCD & Factorization at work



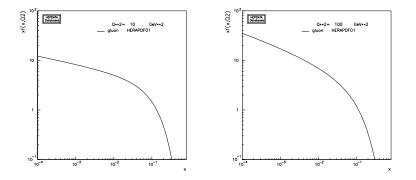
CTEQ 06 Proton PDF's

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pQCD & Factorization at work



• Gluon distributions for $Q^2 = 10 \text{ GeV}^2$ and $Q^2 = 100 \text{ GeV}^2$.

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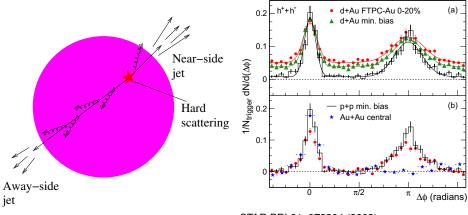
Jet Quenching

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Medium properties

- What is it made of? QGP or HG?
- Thermodynamic properties Temperature, Equation of state, etc.
- Transport properties Mean-free-path, transport coefficients, etc.
- Tools Change in jet properties
 - Jet Quenching
 - Jet Broadening

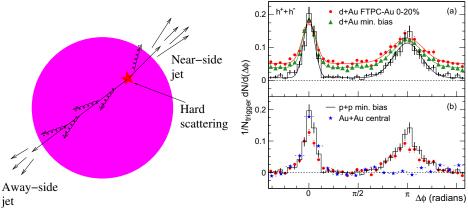
Away side jet disappears! – Proof of principle



STAR PRL91, 072304 (2003)

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Away side jet disappears! – Proof of principle

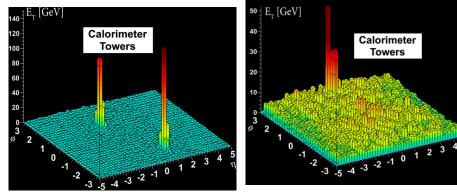


STAR PRL91, 072304 (2003)

Now we need more informative observables to study detailed properties of the medium.

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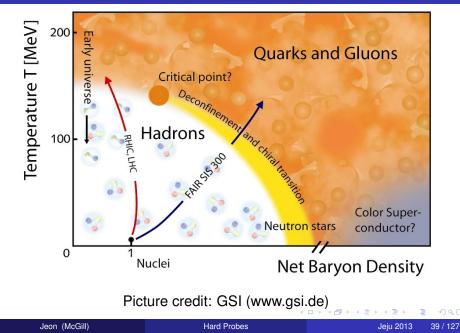
Away side jet disappears! - Proof of principle



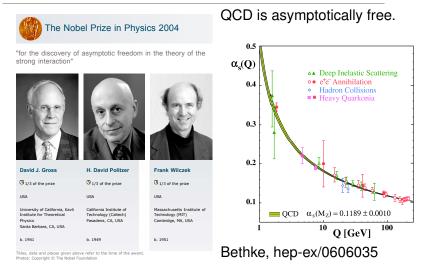
ATLAS: Intact dijets in Pb+Pb

ATLAS: One jet is fully quenched in Pb+Pb

QCD Phase Diagram



Nobelprize.org



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Hard Probes

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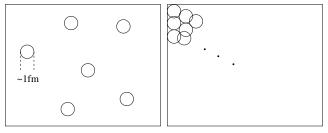
At high T

Running coupling

$$\alpha_{s}(\mu^{2}) = \frac{12\pi}{(33 - 2N_{f})\ln(\mu^{2}/\Lambda_{\text{QCD}}^{2})}$$

- When $\mu \sim \Lambda_{\rm QCD} \sim$ 200 MeV, the above expression blows up: Not physical. Indicates breakdown of perturbation theory.
- Perturbative QCD is a theory of quarks and gluons *not* hadrons.
- At high *T*, $\mu \sim T$.
- Possible phase transition around $T \sim \Lambda_{QCD}$?
- If $\mu \sim T \rightarrow \infty$, $\alpha_s \rightarrow$ 0: Weakly coupled
- At $\mu \sim$ few GeV, $\alpha_{s} \sim$ 0.2 0.4

Another estimate of $T_{transition}$





T~200 MeV

• Density: Consider a pion gas.

$$n = 3 \int rac{d^3 p}{(2\pi)^3} \, rac{1}{e^{E_p/T} - 1} \propto T^3$$

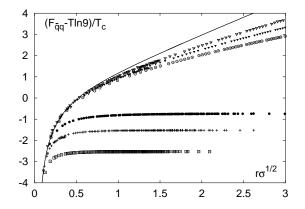
As *T* becomes larger, more and more pair creation results.Inter particle distance:

$$l_{\rm inter} = n^{1/3} \approx 1/T$$

At T= 200 MeV, $\mathit{I}_{\mathrm{inter}} pprox$ 1 fm $pprox \mathit{r}_{\pi}$

- Perturbative calculation possible much above $\mu = \Lambda_{QCD}$
- $\mu \sim T$ at high T
- If *T* is much above the binding energy of hadrons
 Deconfinement
- At high enough *T*, the system is a plasma of weakly interacting quarks and gluons
- All the above arguments are plausible but not a proof

Lattice QCD Evidence

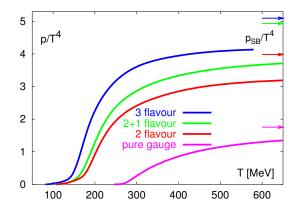


• F. Karsch, hep-lat/0403016. The color averaged heavy quark free energy at temperatures $T/T_c = 0.9, 0.94, 0.98, 1.05, 1.2, 1.5$ (from top to bottom) obtained in quenched QCD.

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Lattice QCD – QGP



- QCD is an asymptotically free theory High T => Free quarks and gluons
- Phase transition happens Hadrons should 'melt' at around $T = 170 \text{ MeV} = 2 \times 10^{12} \text{ K}$ [F.Karsch et al.] "Cross-over"

Expected properties

High number density

$$n \approx (24+16) \int \frac{d^3p}{(2\pi)^3} e^{-p/T} \approx 4 T^3$$
$$= 4 \left(\frac{T}{200 \text{ MeV}}\right)^3 \text{ fm}^{-3}$$

• High energy density

$$\varepsilon \approx (24+16) \int \frac{d^3p}{(2\pi)^3} p e^{-p/T} \approx 12 T^4$$
$$= 2.4 \left(\frac{T}{200 \text{ MeV}}\right)^4 \text{ GeV/fm}^3$$

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Simple Estimate

- 1 mole of hydrogen atom: 6.2×10^{23} atoms = 1 g (Avogadro's number)
- 1 hydrogen atom $m_{
 m p} pprox (1/6) imes 10^{-23}\,{
 m g}$
- $m_p = 940 \, {
 m MeV} pprox 1 \, {
 m GeV}$
- $E = mc^2$: 1 GeV $\approx (1/6) \times 10^{-23}$ g

$$\begin{array}{rcl} 2.4\,\text{GeV}/\text{fm}^3 &=& 0.4\times10^{-23}\,\text{g}/(10^{-13}\,\text{cm})^3\\ &=& 0.4\times10^{-23+39}\,\text{g/cm}^3\\ &=& 0.4\times10^{16}\,\text{g/cm}^3\\ &=& 4\times10^{12}\,\text{kg/cm}^3 \end{array}$$

• Typical human: $\sim 100 \, \text{kg}$

$$2.4\,GeV/fm^3~\sim~4\times10^{10}\,human/cm^3$$

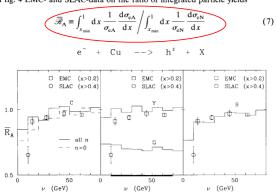
How do you achieve high temperature?

- Temperature = energy (1 eV \approx 12,000K)
- More usefully, the energy density:

$$arepsilon = g \int rac{d^3
ho}{(2\pi)^3} \, extsf{E}_{
ho} \, extsf{e}^{- extsf{E}_{
ho}/ au} pprox rac{3g}{\pi^2} extsf{T}^4$$

- To get high temperature: Get high energy density --> Cram maximum possible energy into the smallest possible volume while randomizing the momenta --> Relativistic heavy ion collisions.
- What to expect: *dN*/*dη* and *dE*/*dη* grow something like (ln s)ⁿ with n ~ 1 ⇒ T should behave something like (ln s)ⁿ with n ~ 1

- High temperature —> Thermal photons
- High density *Jet quenching*
- High pressure → Hydrodynamic flow
 - The size of the eliptic flow depends on the shear viscosity η .
 - If weakly coupled, $\eta/s \gg$ 1 : pprox Ideal gas
 - If stronly coupled, $\eta/s \ll 1$: \approx Perfect (Ideal) fluid.
- Neutrality —> Tight unlike-sign correlation
- Critical point —> Large momentum fluctuations



In fig. 4 EMC- and SLAC-data on the ratio of integrated particle yields



Miklos Gyulassy and Michael Plümer *Jet quenching in lepton nucleus scattering* in Nuclear Physics B Volume 346, 1 (1990).

Key Idea: Compare high p_T spectrum in sth-*N* and sth-*A* by plotting the ratio.

How jets are disappearing in hot/dense medium can tell us about the medium

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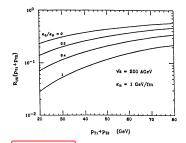


Fig. 7 Dijet reduction factor for central U + U collisions at $\sqrt{s} = 200$ GeV/n as a function of the dijet energy $E = P_{T1} + P_{T2}$, for different values of κ_Q/κ_H assuming $\kappa_H = 16$ GeV/fm.

transverse coordinate, ϕ the azimuthal angle of the jet and $\tau_f(r, \phi)$ the escape time. Assuming only Bjorken[31] scaling longitudinal expansion and a Bag model equation of state[31], one can find the time dependence of $dE(\tau)/dx$ and get the reduction rate of jet production at fixed P_T by averaging over the initial coordinates $(r, \phi)[22]$,

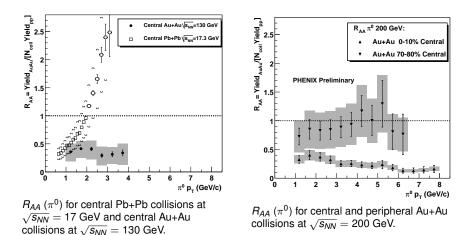
$$R_{AA}(E) = \frac{\sigma^{jet}(E)_{quenching}}{\sigma^{jet}(E)_{no-quenching}}.$$
(11)

In the plasma phase, the temperature decreases as $T(\tau)/T_c = (\tau_Q/\tau)^{1/3}$. According to Eq. 9, $dE/dx \approx \kappa_Q (\tau_Q' \tau)^{2/3}$, denoting the energy loss in the plasma phase by

Xin-Nian Wang and Miklos Gyulassy, Jets in relativistic heavy ion collisions in BNL RHIC Workshop 1990:0079-102 (QCD199:R2:1990)

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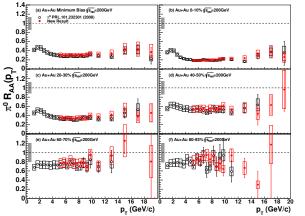
QM 2002 (PHENIX)



Presented by S. Mioduszewski at QM 2002

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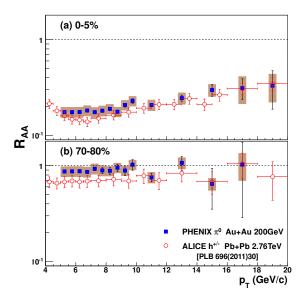
PHENIX, arXiv:1208.2254

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 $\frac{dN_{AA}/dp_T}{N_{\rm coll}dN_{pp}/dp_T}\approx {\rm Const.}$

Slight rising is becoming evident at high p_T .

In 2012



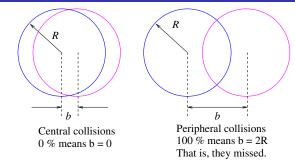
PHENIX, arXiv:1208.2254

 $\frac{dN_{AA}/dp_T}{N_{\rm coll}dN_{pp}/dp_T}\approx {\rm Const.}$

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Jeon (McGill)

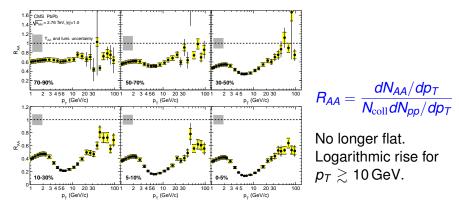
Centrality



For instance:

- 0 5% means top 5% of all collisions in terms of the number of particles produced (multiplicity).
- 70 80% means the collection of events whose multiplicity ranks between bottom 30% and bottom 20%.
- Centrality and impact parameter b not strictly 1 to 1, but very close.

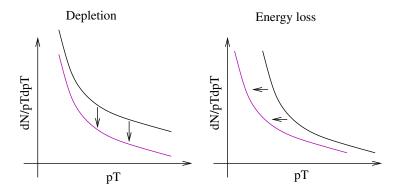
Jeon (McGill)



CMS, 1208.6218v1

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Two ways to understand $R_{AA} < 1$



- The spectrum can shift down when particles actually disappear (depletion)
- The spectrum can shift to the left by energy loss *This is the more realistic scenario.*

Jeon (McGill)

- For high p_T , $dN_{\rm pp}/dp_T \approx 1/p_T^n$.
- Suppose, on average, a particle with *p_T* loses Δ*p_T* while traversing QGP.
- Then the number of particles with *p_T* in AA is the same as the number of particles with *p_T* + Δ*p_T* in pp.

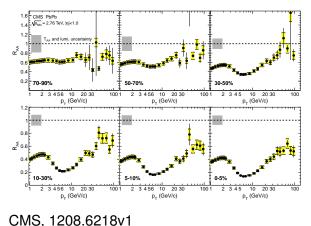
$$R_{AA} = \frac{dN_{AA}/dp_T}{N_{\rm col}dN_{\rho\rho}/dp_T} \approx \frac{dN_{\rho\rho}/dp_T|_{\rho_T + \Delta p_T}}{dN_{\rho\rho}/dp_T|_{p_T}}$$

- What we want to learn: Behavior of Δp_T in the medium
- Shape of R_{AA} depends very much on the shape of dN_{pp}/dp_T

• Suppose $dN_{pp}/dp_T = 1/p_T^n$ (realistic for high p_T)

$$R_{AA} \approx \left(rac{
ho_T}{
ho_T + \Delta
ho_T}
ight)^n = \left(rac{1}{1 + \Delta
ho_T /
ho_T}
ight)^n$$

- Let $\Delta p_T \propto p_T^s$.
- R_{AA} constant if s = 1
- R_{AA} approaches 1 as $p_T \rightarrow \infty$ if s < 1.
- R_{AA} approaches 0 as $p_T \rightarrow \infty$ if s > 1.



• Let $\Delta p_T \propto p_T^s$.

- R_{AA} constant if s = 1
- R_{AA} approaches 1 as $p_T \rightarrow \infty$ if s < 1.

• R_{AA} approaches 0 as $p_T \rightarrow \infty$ if s > 1.

Data suggests that for up to about 5 GeV, $\Delta p_T \propto p_T^{1+a}$ and after that $\Delta p_T \propto p_T^{1-b}$

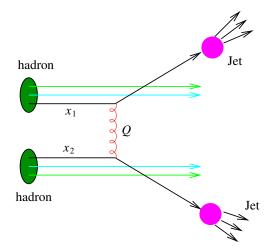
Jet Quenching – Schematic Ideas

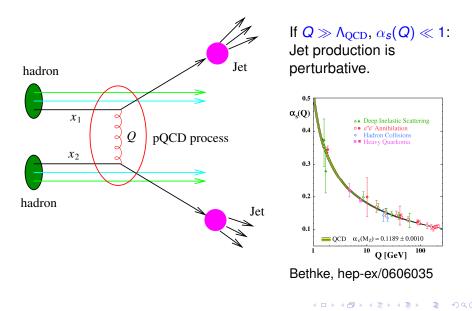
Jeon (McGill)

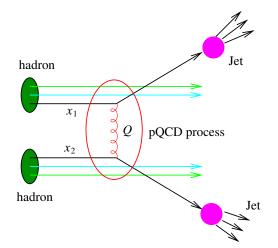
Hard Probes

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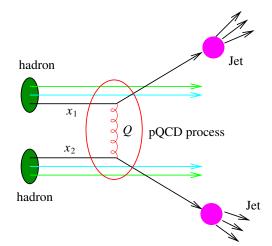






If $Q \gg \Lambda_{QCD}$, $\alpha_s(Q) \ll 1$: Jet production is perturbative.

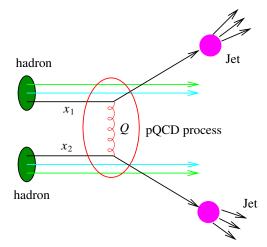
→ Calculation is possible.



If $Q \gg \Lambda_{QCD}$, $\alpha_s(Q) \ll 1$: Jet production is perturbative.

→ Calculation is possible.

➡ We understand this process in hadron-hadron collisions.

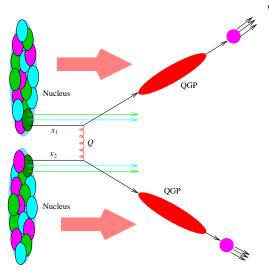


Hadron-Hadron Jet production scheme:

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$$\begin{aligned} \frac{d\sigma}{dt} &= \\ \int_{abcd} f_{a/A}(x_a, Q_f) f_{b/B}(x_b, Q_f) \\ &\times \frac{d\sigma_{ab \to cd}}{dt} D(z_c, Q) \end{aligned}$$

Heavy Ion Collisions



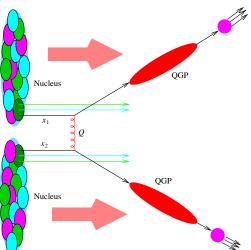
What we want to study:

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 How does QGP modify jet property?

Jeon (McGill)

Heavy Ion Collisions



What we want to study:

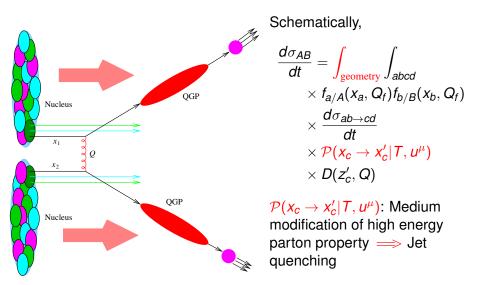
 How does QGP modify jet property?

Complications: How well do we know the *initial* condition?

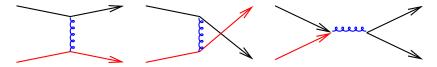
- Nuclear initial condition?
- What happens to a jet between the production and the formation of (hydrodynamic) QGP?

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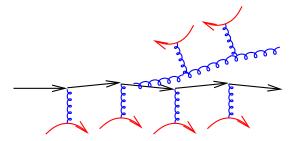
Heavy Ion Collisions



Relevant processes for E-loss



Elastic scatterings with thermal particles



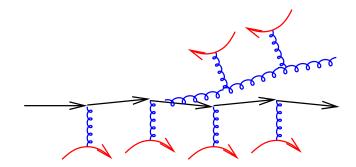
Collinear radiation

- Hot and dense system Requires resummation: HTL & LPM
- Finite size system
- System is evolving

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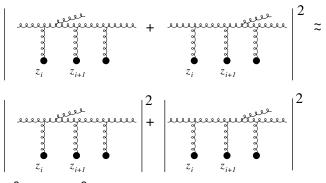
Radiational Energy Loss – Why coherence matters

Process to study



• Radiative (Inelastic) energy loss via collinear gluon emission

Incoherent emission



- $|\sum_n T_n|^2 \approx \sum |T_n|^2$
- Interference terms $T_n^* T_m$ with $n \neq m$ negligible.
- Single emission probabilist scales like the number of scatterers:

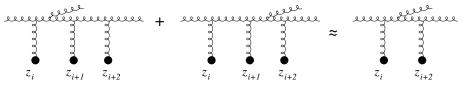
$$\mathcal{P}_{N_{sc}} \approx N_{sc} \mathcal{P}_{1}$$

• In a unit length, there are $N_{sc} = \frac{1}{l_{mfp}}$ number of scatterers. MFP = mean free path.

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Coherent emission

If there is a destructive interference.



Single emission probability scales like

$$\mathcal{P}_{N_{\rm sc}} \approx rac{N_{\rm sc}}{N_{\rm coh}} \mathcal{P}_1$$

where $N_{\rm coh}$ is the number of scattering centers that destructively interfere.

- The medium's power to induce radiation is reduced.
- In the unit length, there are effectively,

$$N_{\rm eff. sc} = \frac{1}{I_{\rm coh}} = \frac{1}{I_{\rm mfp}} \frac{1}{N_{\rm coh}} = \frac{1}{I_{\rm coh}}$$
Hard Probes

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Effective Emission rate

• Coherent Emission rate:

$$rac{d\mathcal{P}}{dt}pproxrac{c}{I_{\mathrm{coh}}}\mathcal{P}_{1}$$

Incoherent Emission rate:

$$rac{d\mathcal{P}}{dt} pprox rac{c}{I_{\mathrm{mfp}}} \mathcal{P}_{1}$$

• Here, \mathcal{P}_1 : Bethe-Heitler

$$\mathcal{P}_1 \approx rac{lpha_{\mathcal{S}} N_c}{\pi \omega}$$

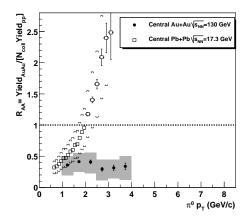
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Understanding the radiative energy loss

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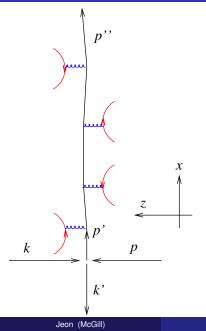


- R_{AA} < 1: Energy loss
- R_{AA} > 1: Energy gain

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$R_{AA} < 1$

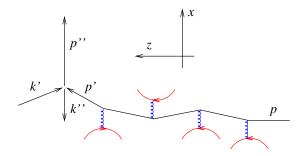


- High energy particle
- Initial energy $E_p = p_z$
- Just after collision: $p'_x = p_z$
- *Final state interactions* with the QGP medium add little bits to p'_z but *subtract little bits* from p'_x .
- Resulting in:

Hard Probes

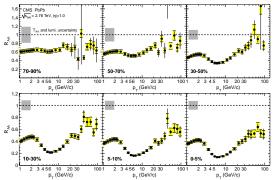
$$E_{\text{jet}} = \sqrt{p''_{x}^{2} + p''_{z}^{2}} \approx p''_{x} < E_{p}$$

$$\implies \text{Energy loss}$$



- Low energy particle
- Initial state interactions with other nucleons add not-so-small momentum (compared to the original energy) in both directions.
- |p'| > |p|
- After the hard collision:
 p''_x ≈ |p'| > p_z ⇒ Energy gain

CMS: Up to $p_T = 100 \text{ GeV}$



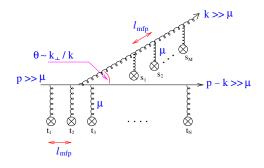
Can we understand these features in terms of microscopic processes in QGP?

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Radiational (Inelastic) Energy Loss – Qualitative understanding

Coherent scattering can be important

Following BDMPS



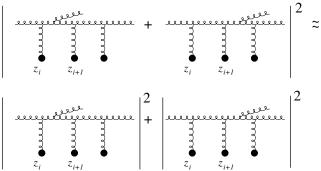
• What we need to calculate R_{AA} : Differential gluon radiation rate $\omega \frac{dN_g}{d\omega dz}$

Medium dependence comes through a scattering length scale

$$\omega \frac{dN_g}{d\omega dz} \approx \frac{1}{I} \omega \left. \frac{dN_g}{d\omega} \right|_{\rm B}$$

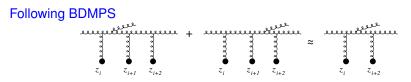
 $l \approx t$

Following BDMPS



• If all scatterings are incoherent $(I_{mfp} > I_{coh})$,

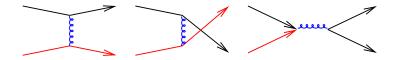
$$I = I_{\rm mfp} = 1/\rho\sigma$$



• If $I_{coh} \ge I_{mfp} \implies$ LPM effect:

All scatterings within $l_{\rm coh}$ effectively count as a single scattering.

• $I = I_{\rm coh}$



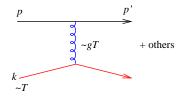
• Mean free path (textbook definition)

$$\frac{1}{l_{\rm mfp}} \equiv \int d^3 k \,\rho(k) \,\int dq^2 \,(1 - \cos\theta_{\rho k}) \frac{d\sigma^{\rm el}}{dq^2}$$

where

- $\rho(k)$: density, $(1 \cos \theta_{\rho k}) \Delta E \approx q^2/2k$: flux factor
- Elastic cross-section (Coulombic) $\frac{d\sigma}{dq^2} \approx C_R \frac{2\pi\alpha_s^2}{(q^2)^2}$

Estimation of Imfp



• Mean free path (textbook definition)

$$\frac{1}{l_{\rm mfp}} \equiv \int d^3 k \,\rho(k) \,\int dq^2 \,(1 - \cos\theta_{\rho k}) \frac{d\sigma^{\rm el}}{dq^2}$$

where

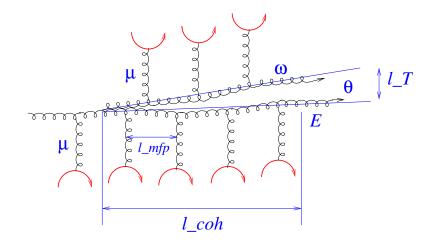
- $\rho(k)$: density, $(1 \cos \theta_{\rho k}) \Delta E \approx q^2/2k$: flux factor
- Elastic cross-section (Coulombic) $\frac{d\sigma}{dq^2} \approx C_R \frac{2\pi\alpha_s^2}{(q^2)^2}$

• With thermal $\rho(k)$, this yields

$$\frac{1}{I_{\rm mfp}} \sim \int d^3 k \rho(k) \int_{m_D^2}^{\infty} dq^2 \frac{\alpha_S^2}{q^4} \sim T^3 \alpha_S^2 / m_D^2 \sim \alpha_S T$$

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Estimation of $I_{\rm coh}$

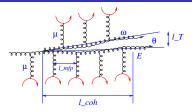


• $E \gg \omega_g \gg \mu$

2

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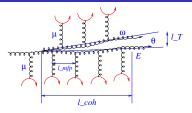
Estimation of Icoh



- ω « E ⇒ The radiated gluon random walks away from the original parton. Original parton's trajectory is less affected.
- From the geometry $\frac{\omega_g}{k_T^g} \approx \frac{I_{\rm coh}}{I_T}$
- Separation condition: I_T is longer than the transverse size of the radiated gluon. $I_T \approx 1/k_T^g$
- Putting together,

$$I_{
m coh} pprox rac{\omega_g}{(k_T^g)^2}$$

Estimation of Icoh



• Putting together,

$$I_{\rm coh} \approx rac{\omega_g}{(k_T^g)^2}$$

• After suffering *N*_{coh} collisions (random walk),

$$\left\langle (k_T^g)^2 \right\rangle = N_{\rm coh} \mu^2 = \frac{I_{\rm coh}}{I_{\rm mfp}} \mu^2$$

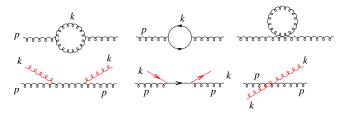
• Becomes, with $\hat{q} = \mu^2 / I_{\rm mfp}$ and $E_{\rm LPM} = \mu^2 I_{\rm mfp}$,

$$I_{\rm coh} \approx I_{\rm mfp} \sqrt{\frac{\omega_g}{E_{\rm LPM}}} = \sqrt{\frac{\omega_g}{\hat{q}}}$$

Jeon (McGill)

Estimation of μ^2

Debye mass



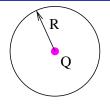
- Second row: Physical forward scattering with particles in the medium
- The last term is easiest to calculate:

$$m_D^2 \propto g^2 \int rac{d^3k}{E_k} f(k) \propto g^2 T^2$$

● Effectively add m²_DA²₀ ⇒ NOT gauge invariant ⇒ Gauge invariant formulation: Hard Thermal Loops

Jeon (McGill)

Physical origin of Debye mass



E & M

- Let Q > 0. Within the range R
 - Positive charges are pushed away: $Q_+ = Q_0 = \delta Q$
 - Negative charges are pulled in: $Q_{-} = Q_0 + \delta Q$
- At position R, apparent net charge is reduced

$$Q_{\text{net}} = Q + (Q_0 - \delta Q) - (Q_0 + \delta Q) = Q - 2\delta Q$$

This is screening.

 When it's moving, there is a net potential energy associated with Q even in charge neutral medium
Acts like a "mass"

Physical origin of Debye mass

E & M

Potential in a thermal system

$$\nabla^2 \Phi(\mathbf{r}) = -\rho(\mathbf{r})$$

• Medium composed of many charged particles

$$\rho(\mathbf{r}) = qn_+(\mathbf{r}) - qn_-(\mathbf{r})$$

• Boltzmann Density:

$$n_{\pm}(\mathbf{r}) = \int \frac{d^{3}k}{(2\pi)^{3}} e^{-E/T} \\
= \int \frac{d^{3}k}{(2\pi)^{3}} e^{-\sqrt{k^{2}+m^{2}}} e^{\mp q\Phi(\mathbf{r})/T} \\
= n_{0}(T) e^{\mp q\Phi(\mathbf{r})/T} \\
\approx n_{0}(T) (1 \mp q\Phi(\mathbf{r})/T)$$

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- E & M
- Boltzmann Density:

$$n_{\pm}(\mathbf{r}) \approx n_0(T)(1 \mp q\Phi(\mathbf{r})/T)$$

• Linearized equation for the potential:

$$abla^2 \Phi - m_D^2 \Phi pprox 0$$

where

$$m_D^2 = 2q^2(n_0(T)/T)$$

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What we learned so far

Coherence length

$$I_{
m coh} pprox I_{
m mfp} \sqrt{rac{\omega_g}{E_{
m LPM}}} = \sqrt{rac{\omega_g}{\hat{q}}}$$

where $\hat{q} = \mu^2 / I_{\rm mfp}$ (average momentum transfer squared per collision) If your chosen process is

• Soft gluon emission, $\omega_g < \mu^2 I_{\rm mfp}$,

• Hard gluon emission, $E \gg \omega_g > \mu^2 I_{\rm mfp}$,

→ Coherence matters. Resummation needed.

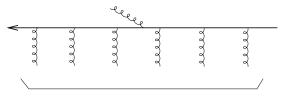
Both

> Need the cross-section that is correct in both limits.

- Key quantity: $E_{\text{LPM}} = \mu^2 I_{\text{mfp}} \sim T$ in pert. thermal QCD
- Key quantity: $\hat{q} \sim \alpha_S^2 T^3$ in pert. thermal QCD

Rough Idea – Multiple Emission (Poisson ansatz)

After each collision, there is a finite probability to emit



Number of effective collisions

- Let the emission probability be p
- Total number of *effective* collisions N_{trial} taking into account of I_{mfp} and I_{coh}.
- Average number of emissions $\langle n \rangle = N_{\text{trial}} p$
- Probability to emit *n* gluons

$$P(n) = \frac{N_{\text{trial}}!}{n!(N_{\text{trial}}-n)!} \rho^n (1-\rho)^{N_{\text{trial}}-n}$$

Rough Idea – Multiple Emission (Poisson ansatz)

• Poisson probability: Limit of binary process as $\lim_{N_{trial} \to \infty} N_{trial} p \to \langle n \rangle$

$$P(n) = e^{-\langle n
angle} rac{\langle n
angle^n}{n!}$$

• Average number of gluons emitted up to $t_i < t$

$$\langle n \rangle = \int_{-\infty}^{E} d\omega \int_{t_{i}}^{t} dz \frac{dN}{dzd\omega} = \int_{-\infty}^{E} d\omega \frac{dN}{d\omega}(t)$$

• Probability to lose ϵ amount of energy by emitting *n* gluons:

$$\langle n \rangle^{n} \rightarrow D(\epsilon, t)$$

$$= \int_{-\infty}^{E} d\omega_{1} \frac{dN}{d\omega_{1}} \int_{-\infty}^{E} d\omega_{2} \frac{dN}{d\omega_{2}} \cdots \int_{-\infty}^{E} d\omega_{n} \frac{dN}{d\omega_{n}} \delta(\epsilon - \sum_{k=1}^{n} \omega_{k})$$

$$= \sum_{k=1}^{n} \delta(\epsilon) + \sum_{k=1}$$

Rough Idea – Multiple Emission (Poisson ansatz)

Parton spectrum at t

$$P(p,t) = \int d\epsilon D(\epsilon,t) P_0(p+\epsilon)$$

where

$$D(\epsilon, t) = e^{-\int d\omega \frac{dN}{d\omega}(\omega, t)} \sum_{n=0}^{\infty} \frac{1}{n!} \left[\prod_{i=1}^{n} \int d\omega_{i} \frac{dN}{d\omega_{i}}(\omega_{i}, t) \right] \delta\left(\epsilon - \sum_{i=1}^{n} \omega_{i}\right)$$

Can easily show that this Poisson ansatz solves:

$$\frac{dP(p,t)}{dt} = \int d\omega \, \frac{dN_{\text{Poiss.}}}{d\omega dt}(\omega) P(p+\omega,t) - P(p,t) \int d\omega \, \frac{dN_{\text{Poiss.}}}{d\omega dt}(\omega)$$

with the p (jet energy) independent rate

$$\frac{dN}{d\omega}(\omega,t) = \int_{t_0}^t dt' \, \frac{dN_{\text{Poiss.}}}{d\omega dt}(\omega,t')$$

Rough Idea - The behavior of R_{AA}

Use $R_{AA} \approx 1/(1 + \epsilon/p)^n \approx e^{-n\epsilon/p}$ when $n \gg 1$. Include gain by absoprtion or $\omega < 0$:

$${\cal R}_{AA}(p)=rac{P(p)}{P_0(p)}pprox \exp\left(-\int_{-\infty}^\infty d\omega\,\int_0^t dt'\,(dN_{
m inel+el}/d\omega dt)(1-e^{-\omega n/p})
ight)$$

For the radiation rate, use simple estimates

$$\begin{split} \frac{dN}{d\omega dt} &\approx \frac{\alpha}{\pi \omega} \frac{N_c}{I_{\rm mfp}} & \text{for } 0 < \omega < I_{\rm mfp} \mu^2 \\ \frac{dN}{d\omega dt} &\approx \frac{\alpha}{\pi \omega} N_c \sqrt{\frac{\mu^2}{I_{\rm mfp} \omega}} & \text{for } I_{\rm mfp} \mu^2 < \omega < I_{\rm mfp} \mu^2 (L/I_{\rm mfp})^2 \\ \frac{dN}{d\omega dt} &\approx \frac{\alpha}{\pi \omega} \frac{N_c}{L} & \text{for } I_{\rm mfp} \mu^2 (L/I_{\rm mfp})^2 < \omega < E \\ \frac{dN}{d\omega dt} &\approx \frac{\alpha}{\pi |\omega|} \frac{N_c}{I_{\rm mfp}} e^{-|\omega|/T} & \text{for } \omega < 0 \end{split}$$

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Rough Idea - The behavior of R_{AA}

For elastic energy loss,

$$\begin{aligned} \mathcal{R}_{AA}^{\text{el}} &\approx & \exp\left(-\int_{-\infty}^{\infty} d\omega \int_{0}^{t} dt' \, (d\Gamma_{\text{el}}/d\omega dt)(1-e^{-\omega n/p})\right) \\ &\approx & \exp\left(-t\left(\frac{dE}{dt}\frac{K(\omega_{0})}{|\omega_{0}|}\right)\right) \\ &\approx & \exp\left(-t\left(\frac{dE}{dt}\right)\left(\frac{n}{p}\right)\left(1-\frac{nT}{p}\right)\right) \end{aligned}$$

valid for p > nT and we used

$$\begin{aligned} \mathcal{K}(\omega_0) &= (1+n_B(|\omega_0|))(1-e^{-|\omega_0|n/p}) + n_B(|\omega_0|)(1-e^{|\omega_0|n/p}) \\ &\approx |\omega_0|\left(\frac{n}{p}\right)\left(1-\frac{nT}{p}\right) \quad \text{for small } \omega_0 \end{aligned}$$

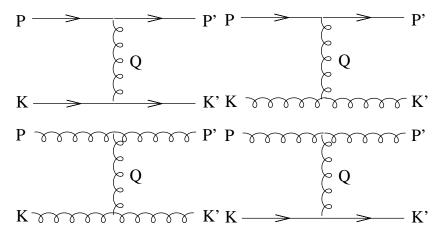
where ω_0 is the typical gluon energy

Jeon (McGill)

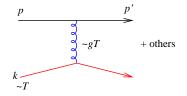
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Elastic scattering rate

Coulombic t-channel dominates



Rough Idea - Elastic energy loss(Following Bjorken)



Mean free path (textbook definition)

$$\frac{1}{I_{\rm mfp}} \equiv \int d^3k \,\rho(k) \,\int dq^2 \,(1 - \cos\theta_{pk}) \frac{d\sigma^{\rm el}}{dq^2}$$

Energy loss per unit length

$$\frac{dE}{dz} = \int d^3k \,\rho(k) \,\int dq^2 \,(1 - \cos\theta_{pk}) \Delta E \frac{d\sigma^{\rm el}}{dq^2}$$

where

•
$$\rho(k)$$
: density, $(1 - \cos \theta_{pk}) \Delta E \approx q^2/2k$: flux factor

• Elastic cross-section (Coulombic) $\frac{d\sigma}{d\sigma^2} \approx C_R \frac{2\pi\alpha_s^2}{(\sigma^2)^2}$

Jeon (McGill)

• With thermal ρ , this yields

$$\left(\frac{dE}{dz}\right)_{\rm coll} \sim \int d^3 k \rho(k)/k \int dq^2 \alpha_S^2/q^2 \sim \alpha_S^2 T^2 \ln(ET/m_D^2)$$

Upper limit determined by

$$q^2=(p-k)^2=p^2+k^2-2pkpprox-2pk\sim ET$$

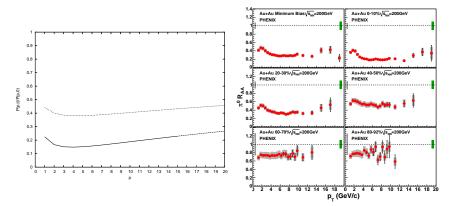
when $|\mathbf{p}| = E$ (emitter) and $|\mathbf{k}| = O(T)$ (thermal scatterer) Lower limit determined by the Debye mass $m_D = O(gT)$. More precisely,

$$\frac{dE}{dt} = \frac{1}{2E} \int_{k,k',p'} \delta^4(p+k-p'-k') (E-E') |M|^2 f(E_k) [1 \pm f(E'_k)] \\ = C_r \pi \alpha_s^2 T^2 \left[\ln(ET/m_g^2) + D_r \right]$$

where C_r and D_r are channel dependent O(1) constants.

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Rough Idea - The behavior of R_{AA}

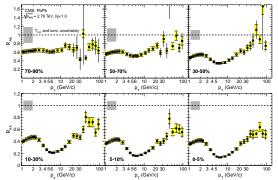


- Upper line: Without elastic
- Lower line: With elastic
- Flat *R* is produced in both cases up to *O*(10 *T*).
- *R* just not that sensitive to *p* in the RHIC-relevant range.

Jeon (McGill)

Hard Probes

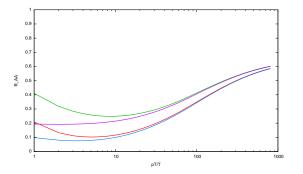
CMS: Up to $p_T = 100 \text{ GeV}$



No longer flat. Logarithmic rise for $p_T \gtrsim 10 \,\text{GeV}$. Can we understand these features?

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Rough Idea - The behavior of R_{AA}



- Red: Elastic on, thermal absorption on
- Blue: Elastic on, thermal absorption off
- Green: Elastic off, thermal absorption on
- Magenta: Elastic off, thermal absorption off
- Dip, rise, leveling-off roughly reproduced
- No dip if thermal absorption is turned off

Jeon (McGill)

For other features, first recall

Use $R_{AA} \approx 1/(1 + \epsilon/p)^n \approx e^{-n\epsilon/p}$ when $n \gg 1$. Include gain by absoprtion or $\omega < 0$:

$$\mathcal{R}_{AA}(p) = rac{P(p)}{P_0(p)} pprox \exp\left(-\int_{-\infty}^{\infty} d\omega \, \int_{0}^{t} dt' \, (dN_{
m inel+el}/d\omega dt)(1-e^{-\omega n/p})
ight)$$

For the radiation rate, use simple estimates

$$\begin{split} \frac{dN}{d\omega dt} &\approx \frac{\alpha}{\pi \omega} \frac{N_c}{I_{\rm mfp}} & \text{for } 0 < \omega < I_{\rm mfp} \mu^2 \\ \frac{dN}{d\omega dt} &\approx \frac{\alpha}{\pi \omega} N_c \sqrt{\frac{\mu^2}{I_{\rm mfp} \omega}} & \text{for } I_{\rm mfp} \mu^2 < \omega < I_{\rm mfp} \mu^2 (L/I_{\rm mfp})^2 \\ \frac{dN}{d\omega dt} &\approx \frac{\alpha}{\pi \omega} \frac{N_c}{L} & \text{for } I_{\rm mfp} \mu^2 (L/I_{\rm mfp})^2 < \omega < E \\ \frac{dN}{d\omega dt} &\approx \frac{\alpha}{\pi |\omega|} \frac{N_c}{I_{\rm mfp}} e^{-|\omega|/T} & \text{for } \omega < 0 \end{split}$$

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Interpretation

With E = p (original parton energy) and the system size L and $(1 - e^{-n\omega/E}) \approx n\omega/E$: • If $E < E_{\text{LPM}} = \mu^2 l_{\text{mfp}}$, $\ln R_{AA} \approx -L \int_0^E d\omega \frac{dN}{d\omega dt} \left(\frac{n\omega}{E}\right) \approx \frac{nL}{E} \int_0^E d\omega \omega \left(\frac{\alpha_S}{\pi \omega} \frac{N_c}{l_{\text{mfp}}}\right) \sim \text{Const.}$ Flat R_{AA}

• If
$$E_{\text{LPM}} < E < E_L = L^2 \mu^2 / l_{\text{mfp}}$$
,
 $\ln R_{AA} \approx -\frac{nL}{E} \int_0^{E_{\text{LPM}}} d\omega \omega \left(\frac{\alpha_S}{\pi \omega} \frac{N_c}{l_{\text{mfp}}}\right)$
 $-\frac{nL}{E} \int_{E_{\text{LPM}}}^E d\omega \omega \left(\frac{\alpha_S}{\pi \omega} N_c \sqrt{\frac{\mu^2}{l_{\text{mfp}}\omega}}\right)$

Jeon (McGill)

 $= -\frac{nL\alpha_{S}N_{c}}{\pi I_{mfn}} \left(2\sqrt{\frac{E_{LPM}}{E} - \frac{E_{LPM}}{E}}\right)$

Plateau at high p_T

- If $E > E_L = L^2 \mu^2 / \lambda$,

$$\ln R_{AA} \approx -\frac{nL}{E} \int_{0}^{E_{\rm LPM}} d\omega \omega \left(\frac{\alpha_{\rm S}}{\pi \omega} \frac{N_c}{I_{\rm mfp}}\right) \\ -\frac{nL}{E} \int_{E_{\rm LPM}}^{E_{\rm L}} d\omega \omega \left(\frac{\alpha_{\rm S}}{\pi \omega} N_c \sqrt{\frac{\mu^2}{I_{\rm mfp}\omega}}\right) \\ -\frac{nL}{E} \int_{E_{\rm L}}^{E} d\omega \omega \left(\frac{\alpha_{\rm S}}{\pi \omega} \frac{N_c}{L}\right) \\ \approx -n \frac{\alpha_{\rm S} N_c}{\pi} \left(1 + \frac{E_{\rm L}}{E} (1 - I_{\rm mfp}/L)\right)$$

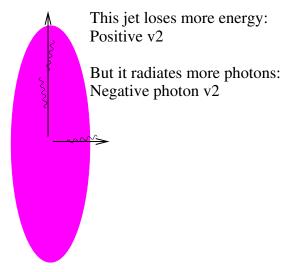
This is approximately constant for large *E*.

Jeon (McGill)

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- Dip-rise-flat feature qualitatively understandable
- Opaque medium
- Density of the medium
- Dip in *R_{AA}*: Could be an indirect indication of the initial temperature.
- Plateau at high p_T: Could be an indication that *I*_{coh} > *L* is reached.
 ⇒ Extract *q̂* from *I*_{coh} ≈ √ω/*q̂*?

Understanding high p_T part of v_2



Jeon (McGill)

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Understanding high p_T part of v_2

• For $E \lesssim E_{\text{LPM}}$, $\Delta E \propto E \ln R_{AA} \propto LE$ Roughly speaking,

$$v_2 = \frac{p_x - p_y}{p_x + p_y} \propto (L_y - L_x)$$

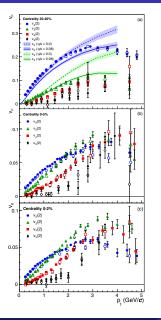
• For $E_{\text{LPM}} \lesssim E \lesssim E_L$, $\Delta E \propto E \ln R_{AA} \propto \sqrt{\hat{q}E}L$ then

$$v_2 = rac{p_x - p_y}{p_x + p_y} \propto (L_y - L_x) rac{\sqrt{\hat{q}}}{\sqrt{E}}$$

• For $E \gtrsim E_L \Delta E \propto (E + E_L)$ then

$$v_2 \sim rac{(L_y^2 - L_x^2)}{E}$$

LHC Data



- Data: ALICE, 1105.3865v2
- High $p_T v_2$: Flat, then falls like $1/\sqrt{p_T}$ and then $1/p_T$.
- Can understand high p_T data qualitatively although $1/p_T$ behavior may not be visible since this is for $E > E_L$.
- The slope $dv_2/dp_T \propto -\sqrt{\hat{q}}$
- Of course, this is very rough: Viscosity also curves it down and p_T ≥ 3 GeV may not be high enough.

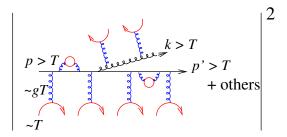
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Thermal QCD calculation of the radiation rate

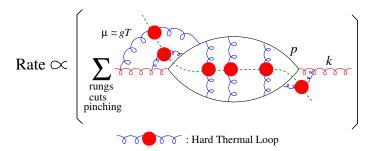
Jeon (McGill)

Hard Probes

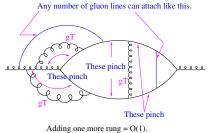
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- Medium is weakly coupled QGP with thermal quarks and gluons
- Requires *g* << 1, *p* > *T*, *k* > *T*



- Medium is weakly coupled QGP with thermal quarks and gluons
- Requires *g* ≪ 1, *p* > *T*, *k* > *T*
- Sum all interactions with the medium including the self-energy



Need to resum.

- Medium is weakly coupled QGP with thermal quarks and gluons
- Requires *g* << 1, *p* > *T*, *k* > *T*
- Sum all interactions with the medium including the self-energy
- Leading order: 3 different kinds of collinear pinching poles

• • • • • • • • • • • • •

• What pinching does: Let

$$P = \left(\frac{i}{p_1^2 + m_2^2 + 2iE_1\Gamma_1}\right)^* \frac{i}{p_2^2 + m_1^2 + 2iE_2\Gamma_2}$$

• Poles for positive energies at $p_1^0 = E_1 - i\Gamma_1$ and $p_2^0 = E_2 + i\Gamma_2$

• If $p_1^0 = E_1 - i\Gamma_1$ puts p_2 also almost on-shell,

$$P\propto rac{1}{E_1E_2}\delta(p_1^0-E_1)rac{1}{\delta E+i\Gamma_2+i\Gamma_1}$$

where δE : difference in the real part of the energy

 Physically, this means that an almost on-shell particle lives a long time Δt ~ 1/δE ~ 1/Γ ⇒ Introduces a secular divergence

• Pinching poles occur when

• $p_1 \approx p_2$: Soft momentum exchange or radiation.

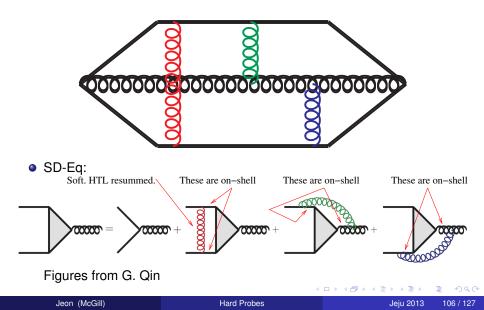
If
$$p_1^2 + m^2 = O(g^2 T^2)$$
, so is $p_2^2 + m^2 = O(g^2 T^2)$.

• $p_2 = xp_1$: Collinear radiation. When $p_1^2 + m^2 = O(g^2T^2)$,

$$p_2^2 + m^2 = x^2 p_1^2 + m^2 + O(g^2 T^2) = (1 - x^2)m^2 + O(g^2 T^2)$$

When $m \approx gT$, the whole expression is $O(g^2T^2)$.

→ Ξ →



• SD Equation for the vertex F

$$2\mathbf{h} = i\delta E(\mathbf{h}, p, k)\mathbf{F}_{s}(\mathbf{h}) + g^{2} \int \frac{d^{2}\mathbf{q}_{\perp}}{(2\pi)^{2}} C(\mathbf{q}_{\perp}) \times \\ \times \Big\{ (C_{s} - C_{A}/2)[\mathbf{F}_{s}(\mathbf{h}) - \mathbf{F}_{s}(\mathbf{h} - k \mathbf{q}_{\perp})] \\ + (C_{A}/2)[\mathbf{F}_{s}(\mathbf{h}) - \mathbf{F}_{s}(\mathbf{h} + \rho \mathbf{q}_{\perp})] \\ + (C_{A}/2)[\mathbf{F}_{s}(\mathbf{h}) - \mathbf{F}_{s}(\mathbf{h} - (p - k) \mathbf{q}_{\perp})] \Big\}, \\ \delta E(\mathbf{h}, p, k) = \frac{\mathbf{h}^{2}}{2pk(p-k)} + \frac{m_{k}^{g2}}{2k} + \frac{m_{p-k}^{s2}}{2(p-k)} - \frac{m_{p}^{s2}}{2p}.$$

h = (p × k) × e_{||} — Must keep track of both p_⊥ and k_⊥ now. For photons, we could just set k_⊥ = 0.

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• SD Equation for the vertex F

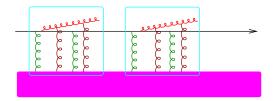
$$2\mathbf{h} = i\delta E(\mathbf{h}, p, k)\mathbf{F}_{s}(\mathbf{h}) + g^{2} \int \frac{d^{2}\mathbf{q}_{\perp}}{(2\pi)^{2}} C(\mathbf{q}_{\perp}) \times \\ \times \Big\{ (C_{s} - C_{A}/2)[\mathbf{F}_{s}(\mathbf{h}) - \mathbf{F}_{s}(\mathbf{h} - k \mathbf{q}_{\perp})] \\ + (C_{A}/2)[\mathbf{F}_{s}(\mathbf{h}) - \mathbf{F}_{s}(\mathbf{h} + \rho \mathbf{q}_{\perp})] \\ + (C_{A}/2)[\mathbf{F}_{s}(\mathbf{h}) - \mathbf{F}_{s}(\mathbf{h} - (\rho - k) \mathbf{q}_{\perp})] \Big\}, \\ \delta E(\mathbf{h}, p, k) = \frac{\mathbf{h}^{2}}{2pk(\rho - k)} + \frac{m_{k}^{g2}}{2k} + \frac{m_{\rho - k}^{s2}}{2(\rho - k)} - \frac{m_{\rho}^{s2}}{2p}.$$

- s: Process dependence. $q \rightarrow qg, g \rightarrow gg, g \rightarrow q\bar{q}$.
- g
 ightarrow q ar q: Exchange coeff. of the first and second line
- m_s^2 : Medium induced thermal masses of the emitter.

• Rate for p > T, k > T (valid for $p \gg T$ and $k \gg T$ as well)

$$\begin{split} \frac{dN_g(p,k)}{dkdt} &= \frac{C_s g_s^2}{16\pi p^7} \frac{1}{1\pm e^{-k/T}} \frac{1}{1\pm e^{-(p-k)/T}} \times \\ &\times \begin{cases} \frac{1+(1-x)^2}{x^3(1-x)^2} & q \to qg \\ N_f \frac{x^2+(1-x)^2}{x^2(1-x)^2} & g \to q\bar{q} \\ \frac{1+x^4+(1-x)^4}{x^3(1-x)^3} & g \to gg \end{cases} \\ &\times \int \frac{d^2 \mathbf{h}}{(2\pi)^2} 2\mathbf{h} \cdot \operatorname{Re} \mathbf{F}_s(\mathbf{h},p,k) \,, \end{split}$$

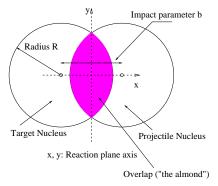
• s: Process dependence.



• Evolution - Medium enters through $T(t, \mathbf{x})$ and $u^{\mu}(t, \mathbf{x})$

$$\begin{aligned} \frac{d\mathcal{P}_{q}(p)}{dt} &= \int_{k} \mathcal{P}_{q}(p+k) \frac{dN_{qg}^{g}(p+k,k)}{dkdt} - \mathcal{P}_{q}(p) \int_{k} \frac{dN_{qg}^{g}(p,k)}{dkdt} \\ &+ \int_{k} 2\mathcal{P}_{g}(p+k) \frac{dN_{q\bar{q}}^{g}(p+k,k)}{dkdt} , \\ \frac{d\mathcal{P}_{g}(p)}{dt} &= \int_{k} \mathcal{P}_{q}(p+k) \frac{dN_{qg}^{g}(p+k,p)}{dkdt} + \int_{k} \mathcal{P}_{g}(p+k) \frac{dN_{gg}^{g}(p+k,k)}{dkdt} \\ &- \mathcal{P}_{g}(p) \int_{k} \left(\frac{dN_{q\bar{q}}^{g}(p,k)}{dkdt} + \frac{dN_{gg}^{g}(p,k)}{dkdt} \Theta(k-p/2) \right) \end{aligned}$$

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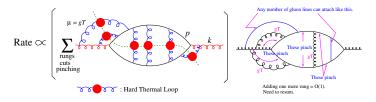


Modified fragmentation function with jet initial condition s, n, p_i

$$\begin{split} \bar{D}_{\pi^0,c}(z,Q;\mathbf{s},\mathbf{n}) &= \int dp_f \frac{z'}{z} \left(\mathcal{P}_{qq/c}(p_f;p_i) D_{\pi^0/q}(z',Q) + \mathcal{P}_{g/c}(p_f;p_i) D_{\pi^0/g}(z',Q) \right) ,\\ \tilde{D}(z,Q) &= \int d^2 s \, \frac{T_A(\mathbf{s}) T_B(\mathbf{s}+\mathbf{b})}{T_{AB}(\mathbf{b})} \, \bar{D}_{\pi^0,c}(z,Q;\mathbf{s},\mathbf{n}) \end{split}$$

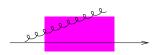
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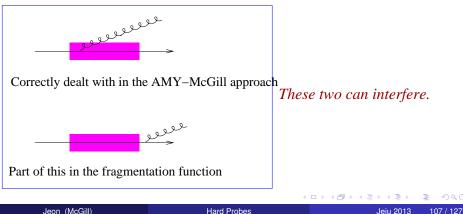


- Collision geometry including path length fluctuations are all included.
- Both BH and LPM limits included
- Includes all leading order splittings
- Includes thermal absorption
- All produced quarks and gluons fragment
- Medium evolution (T(t, x), u_µ(t, x)) fully taken into account including the effect of flow vector
- Easy to add other process such as elastic coll. γ production within leading order QCD/QED.

What is not included yet (vacuum-medium interference)



Included in the PDF scale dependence



What is not included yet (vacuum-medium interference)

• The *L*² dependence in the heuristic BDMPS expression we got before

$$\ln R_{AA} \approx -n \frac{\alpha_{S} N_{c}}{\pi} \left(1 - \frac{L \mu^{2}}{E} + \frac{E_{L}}{E} \right)$$

cannot be reproduced since original AMY always assumes $L > I_{\rm coh}$.

• Finite size effect is being worked on (Caron-Huot and Gale).

The Evolving Medium

- E - N

Hydrodynamic evolution

- As the jets propagate, medium undergoes an evolution of its own.
- Best modeling tool we have: Ideal Hydrodynamics. It solves

 $\partial_{\mu}T^{\mu\nu} = 0$ and $\partial_{\mu}j^{\mu}_{B} = 0$

with the Ideal hydro ansatz

 $T^{\mu\nu} = (\varepsilon + P)u^{\mu}u^{\nu} + Pg^{\mu\nu}$ and $j^{\mu}_{B} = \rho_{B}u^{\mu}$

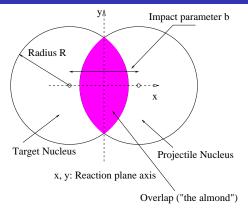
and an EoS

 $\boldsymbol{P} = \boldsymbol{f}(\varepsilon, \rho_{\boldsymbol{B}})$

with suitable initial conditions.

- Medium evolution: $\epsilon(t, \mathbf{x}), u^{\mu}(t, \mathbf{x})$
- Equivalently, $T(t, \mathbf{x}), u^{\mu}(t, \mathbf{x})$

Geometry



Density function

$$T_A(\mathbf{s}) = \int dz \,
ho_A(\mathbf{s}, z)$$

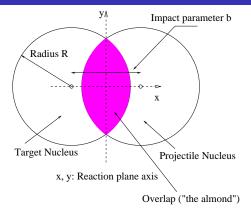
• Overlap function:

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T_{AB}(\mathbf{s},\mathbf{b}) = T_A(\mathbf{s})T_B(\mathbf{b}+\mathbf{s})
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Jeon (McGill)

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Geometry

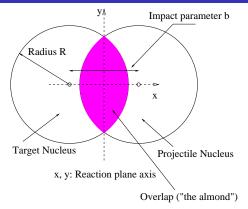


- Participants: $N_{\text{part}}(\mathbf{s}, \mathbf{b}) \propto T_A(\mathbf{s}) + T_B(\mathbf{b} + \mathbf{s})$
- Binary scatterings: $N_{\rm bin}(\mathbf{s}, \mathbf{b}) \propto T_{AB}(\mathbf{s}, \mathbf{b})$ ٠
- Initial energy density ٠

 $\varepsilon(\mathbf{s}, \mathbf{b}) = c_1 \left[T_A(\mathbf{s}) + T_B(\mathbf{b} + \mathbf{s}) \right] + c_2 T_{AB}(\mathbf{s}, \mathbf{b})$

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Geometry



- Ultimately, initial geometry determines the initial conditions and the final flow pattern.
- Initial geometry also determines number of jets at s and the path conditions for those jets.

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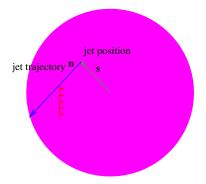
- Three places where "Dynamic" medium enters.
 - Cross-section

$$rac{d\sigma_{GW}}{dq^2} = rac{C}{(q^2 + \mu^2)^2}$$
 vs $rac{d\sigma_{QCD-HTL}}{dq^2} = rac{C}{q^2(q^2 + m_D^2)}$

- Space-time dependence of T or μ , \hat{q} .
- The effect of flow

• $\frac{dN}{d\omega dt}$ is independent of the jet energy

- Determine the position of the jet s.
- Fix the direction n to get the straight line trajectory.



Jeon	(McGill)
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• $\frac{dN}{d\omega dt}$ is independent of the jet energy

- Determine the position of the jet s.
- Fix the direction **n** to get the straight line trajectory.
- Calculate the average number of emitted gluons

$$\langle N_g
angle = \int d\omega \int_{t_0}^{t_f} dt \, rac{dN_g}{d\omega dt}$$

along the trajectory. $dN_g/d\omega dt$ depends on (t, \mathbf{x}) through T or (μ, \hat{q}) .

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- · Calculate the average number of emitted gluons

$$\langle N_g \rangle = \int d\omega \int_{t_0}^{t_f} dt \, \frac{dN_g}{d\omega dt}$$

along the trajectory. $dN_g/d\omega dt$ depends on (t, \mathbf{x}) through T or (μ, \hat{q}) .

• Use the Poisson ansatz to get probability to emit *n* gluons

$$P_n = e^{-\langle N_g
angle} \, rac{\left< N_g
ight>^n}{n!}$$

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• $\frac{dN}{d\omega dt}$ is independent of the jet energy

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$$P_n = e^{-\langle N_g
angle} \, rac{\left< N_g
ight>^n}{n!}$$

• Can express it as $P_n(\epsilon)$ using an energy conserving δ -function

• $\frac{dN}{d\omega dt}$ is independent of the jet energy

- Determine the position of the jet s.
- Fix the direction **n** to get the straight line trajectory.
- Calculate the average number of emitted gluons

$$\langle N_g \rangle = \int d\omega \int_{t_0}^{t_f} dt \, \frac{dN_g}{d\omega dt}$$

along the trajectory. $dN_g/d\omega dt$ depends on (t, \mathbf{x}) through T or (μ, \hat{q}) .

Use the Poisson ansatz to get probability to emit n gluons

$$P_n = e^{-\langle N_g \rangle} \frac{\langle N_g \rangle^n}{n!}$$

• Works as long as one can easily calculate $\frac{dN_g}{dw}$ along the trajectory

• $\frac{dN}{d\omega dt}$ is independent of the jet energy

- Determine the position of the jet s.
- Fix the direction **n** to get the straight line trajectory.
- · Calculate the average number of emitted gluons

$$\langle N_g \rangle = \int d\omega \int_{t_0}^{t_f} dt \, \frac{dN_g}{d\omega dt}$$

along the trajectory. $dN_g/d\omega dt$ depends on (t, \mathbf{x}) through T or (μ, \hat{q}) .

• Use the Poisson ansatz to get probability to emit *n* gluons

$$P_n = e^{-\langle N_g
angle} \, rac{\left< N_g
ight>^n}{n!}$$

• Relatively simple to implement

Jeon (M	AcGill)
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• $\frac{dN}{d\omega dt}$ is independent of the jet energy

- Determine the position of the jet s.
- Fix the direction **n** to get the straight line trajectory.
- Calculate the average number of emitted gluons

$$\langle N_g \rangle = \int d\omega \int_{t_0}^{t_f} dt \, \frac{dN_g}{d\omega dt}$$

along the trajectory. $dN_g/d\omega dt$ depends on (t, \mathbf{x}) through T or (μ, \hat{q}) .

• Use the Poisson ansatz to get probability to emit *n* gluons

$$P_n = e^{-\langle N_g
angle} \, rac{\left< N_g
ight>^n}{n!}$$

• BDMS, (D)GLV, AWS, ...

Jeon (McGill)

Two possible approaches

• $\frac{dN_g}{d\omega dt}$ depends on the jet energy

- Determine the position s
- Determine the direction n
- Solve (numerically)

$$\frac{dP(p,t)}{dt} = \int_{k} \frac{dN}{d\omega dt} (p+k,k) P(p+k,t) - P(p,t) \int_{k} \frac{dN}{d\omega dt} (p,k)$$

4 A N

- Determine the position s
- Determine the direction n
- Solve (numerically)

$$\frac{dP(p,t)}{dt} = \int_{k} \frac{dN}{d\omega dt} (p+k,k) P(p+k,t) - P(p,t) \int_{k} \frac{dN}{d\omega dt} (p,k)$$

• Can deal with changing environment and changing trajectory

- Determine the position s
- Determine the direction n
- Solve (numerically)

 $\frac{dP(p,t)}{dt} = \int_{k} \frac{dN}{d\omega dt} (p+k,k) P(p+k,t) - P(p,t) \int_{k} \frac{dN}{d\omega dt} (p,k)$

- Can deal with changing environment and changing trajectory
- Can keep track of both quarks and gluons at the same time

- Determine the position s
- Determine the direction n
- Solve (numerically)

 $\frac{dP(p,t)}{dt} = \int_{k} \frac{dN}{d\omega dt} (p+k,k) P(p+k,t) - P(p,t) \int_{k} \frac{dN}{d\omega dt} (p,k)$

- Can deal with changing environment and changing trajectory
- Can keep track of both quarks and gluons at the same time
- Easy to add other processes including γ production

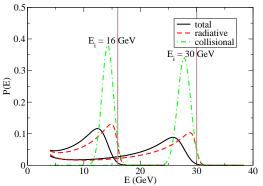
- Determine the position s
- Determine the direction n
- Solve (numerically)

 $\frac{dP(p,t)}{dt} = \int_{k} \frac{dN}{d\omega dt} (p+k,k) P(p+k,t) - P(p,t) \int_{k} \frac{dN}{d\omega dt} (p,k)$

- Can deal with changing environment and changing trajectory
- Can keep track of both quarks and gluons at the same time
- Easy to add other processes including γ production
- McGill-AMY

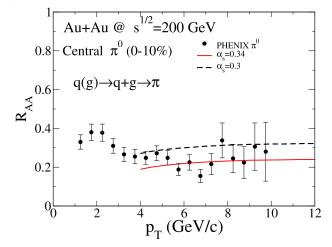
Example evolution of a single jet (Qin)

 The final momentum distribution P(E, t_f) of a single quark jet after passing through RHIC medium (b = 2.4 fm)



- Medium described by (3+1)D ideal hydrodynamics.
- The jet starts at the center and propagates in plane.
- Jet energy loss turned off in hadronic phase.

R_{AA} at RHIC - π^0 - Radiation only (Turbide)

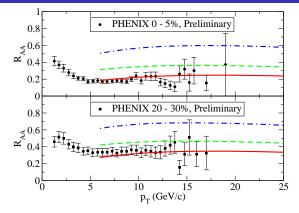


 $T_i = 370$ MeV, dN/dy = 1260. 1-D Bjorken expansion. Best $\alpha_s = 0.33$ s.Turbide, C.Gale, S.J. and G.Moore, PRC72:014906,2005

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R_{AA} at RHIC – π^0 - Full (Qin)



• 3+1D hydro

• Includes radiational and collisional energy loss: rad+coll, rad, coll

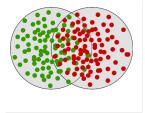
• Strong coupling α_s : 0.33 (rad) and 0.27 (rad+coll)

Guangyou Qin, J. Ruppert, C. Gale, S. Jeon, G.D. Moore, M.G. Mustafa

Phys.Rev.Lett.100: 072301, 2008

Jeon (McGill)

Monte Carlo Approach - MARTINI



- Sample overlapping region for binary collisions
- Produce high p_T partons by PYTHIA 8.1

Jeon (McGill)

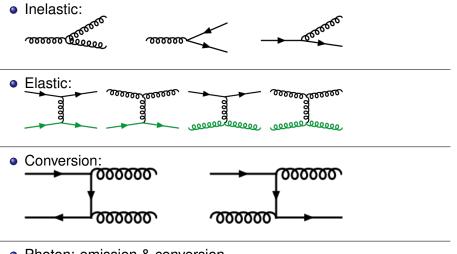
- Put them in the hydro background. Sample the total collision rate at each time step according to the local environment and decide whether to interact with the medium.
- If yes, decide which process to enact according to the branching ratio.
- Sample the chosen process to simulate change 4-momentum of the jet parton
- Hadronize by PYTHIA 8.1 when the parton is outside QGP. Hard Probes

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Monte Carlo Approach - MARTINI

Process include in MARTINI (all of them can be switched on & off):

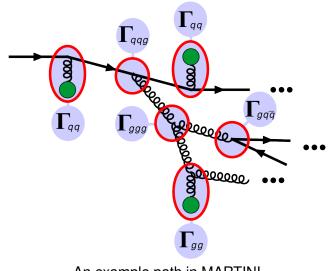


Photon: emission & conversion

Jeon (McGill)	Hard Probes	

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Monte Carlo Approach - MARTINI



An example path in MARTINI

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• While this is happening in the background ...

Image: A math a math

Projection on to the longitudinal plane

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Hard Probes

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Projection onto the transverse plane

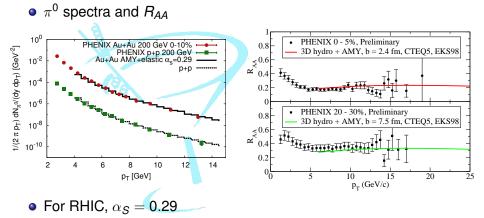
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Hard Probes

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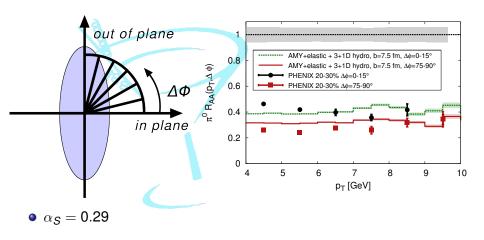
Pion production

[Schenke, Jeon and Gale, Phys. Rev. C 80, 054913 (2009)]



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• $R_{AA}(p_T, \Delta \phi)$



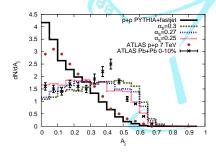
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MARTINI – LHC dN/dA

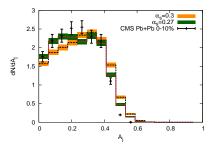
[Young, Schenke, Jeon, Gale, Phys. Rev. C 84, 024907 (2011)].

•
$$A = (E_t - E_a)/(E_t + E_a)$$

- This is with ideal hydro with a smooth initial condition
- Full jet reconstruction with FASTJET
- $\alpha_S = 0.27$ seems to work.



ATLAS, PRL 105 (2010) 252303



CMS, arXiv: 1102.1957 (2011)

Jeon (McGill)

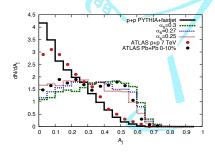
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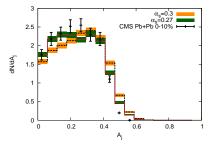
MARTINI – LHC dN/dA

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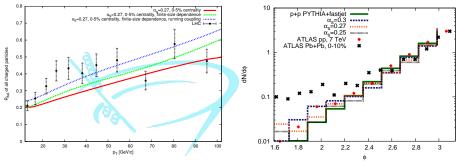
CMS, arXiv: 1102.1957 (2011)

ATLAS, QM 2011 Jeon (McGill)

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Not the full story

[Clint's HP2012 Proceedings]



- R_{AA} For LHC, constant α_S suppresses jets too much.
- Need to incorporate finite length effect (Caron-Huot-Gale) and running α_s . This is with maximum $\alpha_s = 0.27$.
- Don't quite get azimuthal dependence yet. Δφ broadening may be due to the background fluctuations → Need to combine UrQMD background?

- So many nuclear experiments are being done/planned. RHIC, LHC, Raon, FRIB, FAIR, JPARC, Dubina,...
- There never have been a time in history so much information is so readily available.
- This is a great time to be/become a nuclear physicist.
- Work hard. Think hard. Dream big.
- Never say/think, that that should be good enough. Make sure that it is *always excellent*!
- Attention to details, but don't lose sight of the big picture.
- Look around you.