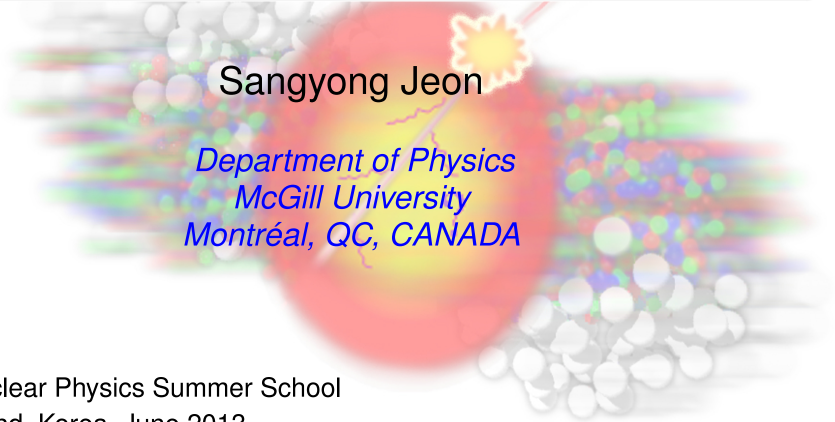
Introduction to Hard Probes in Heavy Ion Collisions



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11th Nuclear Physics Summer School
Jeju Island, Korea, June 2013

McGill is in Montréal, Québec, Canada

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QC
Canada

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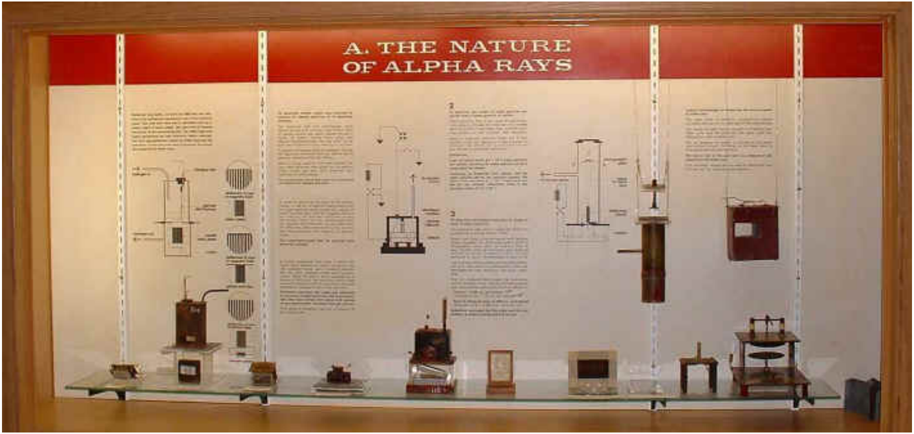
Mr. McGill going home after a hard day's work.

McGill is in Montréal, Québec, Canada



Rutherford carried out his Nobel (1908) winning work at McGill (1898-1907).
His *original* equipments on display

McGill Team

- Charles Gale
- Sangyong Jeon
- *Björn Schenke*
  (Formerly McGill, now BNL)
- *Clint Young*
  (Formerly McGill, Now UMinn)
- *Gabriel Denicol*
- *Matt Luzum*
- Sangwook Ryu
- Gojko Vujanovic
- Jean-Francois Paquet
- Michael Richard
- Igor Kozlov
- Khadija El Berhoumi
- Jean-Bernard Rose

Before I begin...
Some thoughts I'd like to share

Success in your Physics career

Disclaimer: These are my own thoughts. Everyone is different. Take these with a grain of salt.

- Passion for Physics!
- Communication skill – Improve your English
  - Writing skill – Writing guide books help
    A good one: *BUGS in Writing: A Guide to Debugging Your Prose*, by Lyn Dupre
  - Presentation skill – Have a look at R. Geroch's *"Suggestions for Giving Talks"*, arXiv:gr-qc/9703019v1.
  - Debate skill – Practice thinking in English
  - Social communication skill – Read novels (paperbacks are better), watch sitcoms, know the culture, slang, ...

Writing/Presentation skill

Approach it as if you're writing a story

Story

- Introduction – Make the reader interested in the rest of the story
- Expanding the story – Main characters, main events, conflicts, puzzles, ...
- Resolution – Story escalates to the ultimate resolution by a big battle, saved by the heroes/heroines.
- Ending – Tie up loose ends. Make the reader want to read the sequel.

Article/Talk

- Introduction – Make the reader interested in the rest of the paper/talk
- Expanding the point – Main physics points, main data, conflicts, puzzles, ...
- Resolution – What big physics the new data/theory illuminates/resolves. Saved by the heroes/heroines.
- Conclusion – Tie up loose ends. Make the reader want to read the sequel.

On to Physics

Relativistic Heavy Ion Collisions

- Why do it?
  - To study QGP
  - Most extreme environment ever created: $T \sim 1$ GeV.
    This existed only at around 1 microsecond after the Big Bang
- How do we understand it?
  - Theory: Many-body QCD
  - Experimental probes:
    - Soft
    - Hard

Hard Probes are useful

- Hard Probes $\sim$ Large momentum/energy phenomena
- pQCD applies – We know how to do this
- Produced *before* QGP is formed in the same way as in hadron-hadron collisions
- Difference between *pp*, *pA* and *AA* tells us about the medium.
- Caveat: How well do we know the *nuclear initial state?*

What do we want to learn?

- Medium properties
  - What is it made of? Quarks? Gluons? Hadrons?
  - Thermodynamic properties – Temperature, Equation of state, etc.
  - Transport properties – Mean-free-path, transport coefficients, etc.
- Tools
  - Jets
  - Hard Photons

Outline

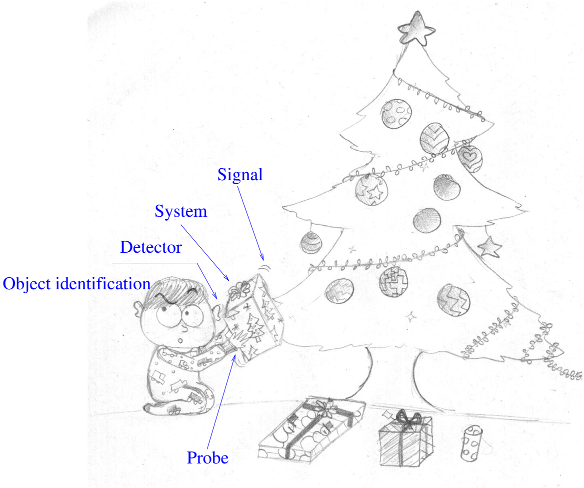
1. pQCD
2. Jet Quenching
3. Hard Photons

What is a hard probe?

- Early hard probe experiments

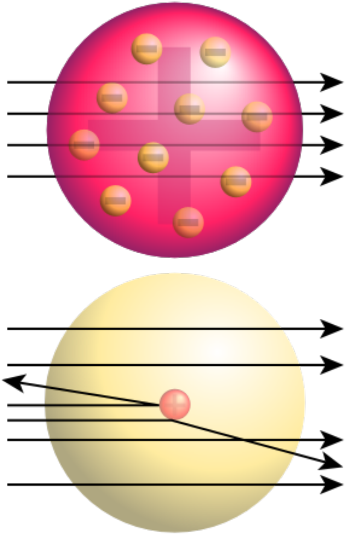
What is a hard probe?

- Early hard probe experiments



What is a hard probe?

- Early hard probe experiments

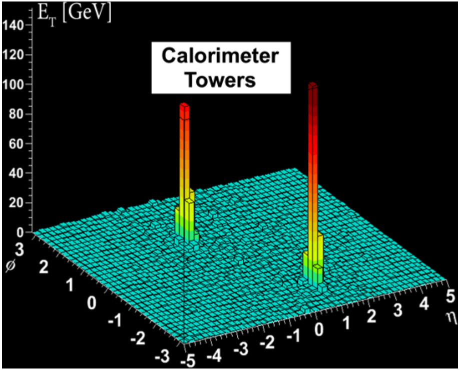


- Rutherford's α scattering experiment

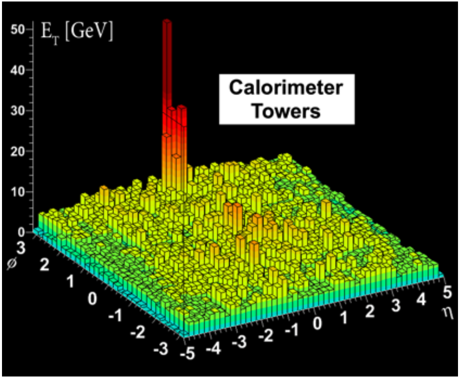
$$\frac{d\sigma}{d\cos\theta} = \frac{\pi}{2} Z^2 \alpha_{\rm EM}^2 \left(\frac{\hbar c}{E_{\rm kin}}\right)^2 \times \frac{1}{(1-\cos\theta)^2}$$

- Small angle scattering dominates $d\sigma/d\cos\theta \propto 1/\theta^4$
- But backscattering prob. is finite, favoring Rutherford's model over Thompson's (which causes no backscattering)

Fast-forward to the present



ATLAS: Intact dijets in Pb+Pb



ATLAS: One jet is fully quenched in Pb+Pb

- Simplest conclusion to draw: The medium is *opaque*.
- We want to know much more than that!

Hard Probe Requirements

- Must be known & calculable using pQCD.
- Must be created *before* QGP forms

Both requirements satisfied if the energy scale is much large compared to $\Lambda_{\rm QCD} \approx 200\,\mathrm{MeV}$ and the length (time) scale is much shorter than $\sim 1\,\mathrm{fm}$.

Hard Probes

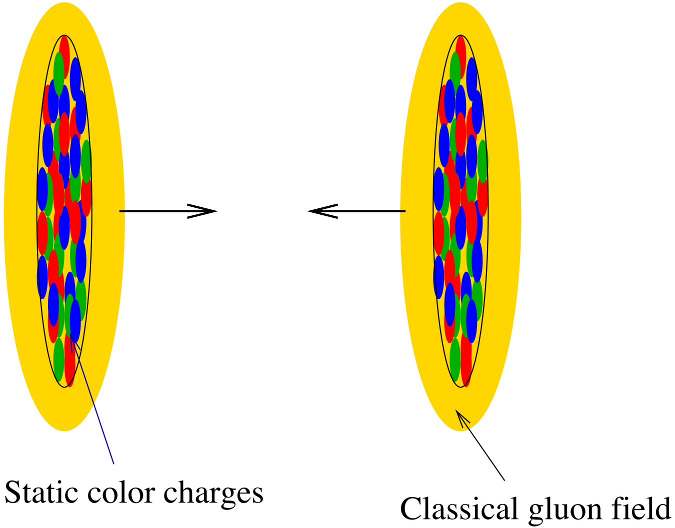
Probes

- Propagation of hard partons or “Jets”
- Quarkonium suppression
- High p_T electromagnetic probes (real and virtual photons)

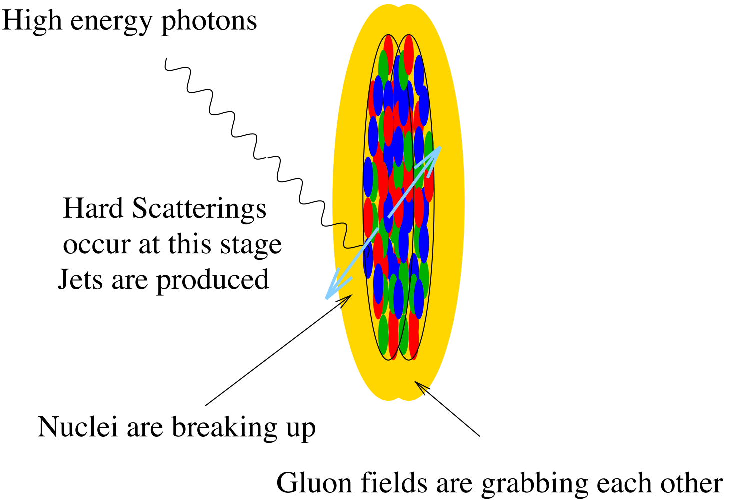
Goal

- To characterize *QGP*
- To characterize initial state (nPDF, CGC?)

(Very) Schematic view of heavy ion collisions



(Very) Schematic view of heavy ion collisions



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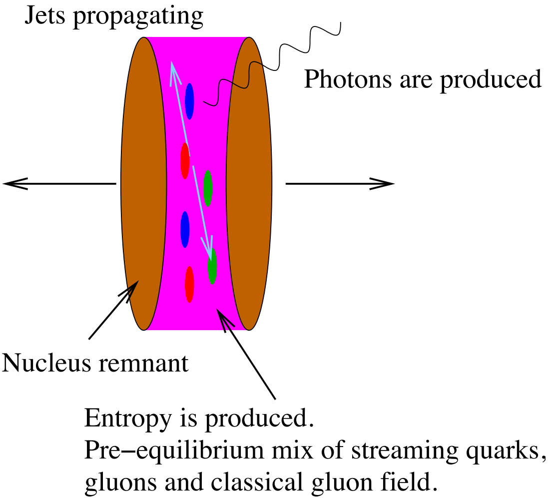
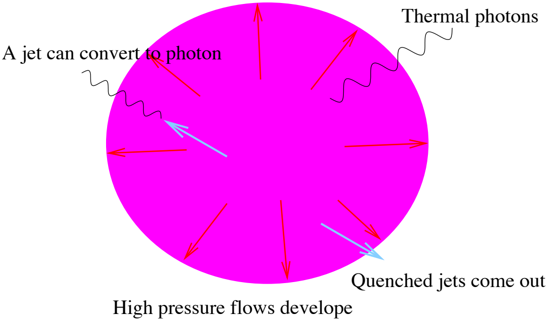
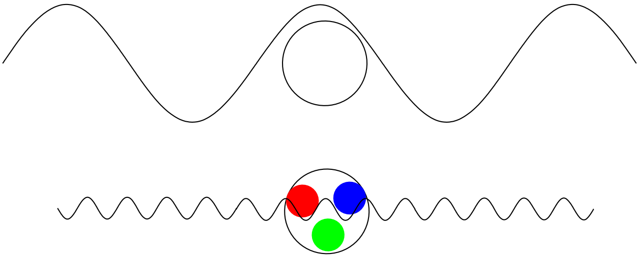


(Very) Schematic view of heavy ion collisions



Review of some basic concepts

- Spatial resolution: $\Delta x \Delta p \geq 1/2$



- Shorter the wavelength (larger the momentum) sees spatial details up to $\Delta x \approx \lambda$.

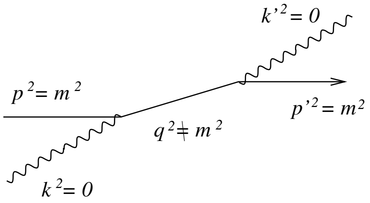
Review of some basic concepts

Energy-Time uncertainty: $|\Delta E|\Delta t \geq 1/2$

- $\Delta E = p^0 - \sqrt{\mathbf{p}^2 + m^2}$.
- If $\Delta E = 0$, then $p^\mu p_\mu = m^2$: On-shell
- If $\Delta E \neq 0$, the $p^\mu p_\mu \neq m^2$: Off-shell

Interpretation

- An off-shell state can exist only for $\Delta t \sim 1/|\Delta E|$.

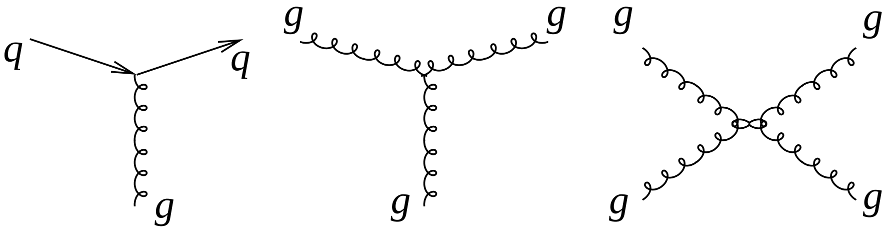


This interaction lasts $\Delta t \sim 1/|(|\mathbf{p}| + |\mathbf{k}| - \sqrt{(\mathbf{p}+\mathbf{k})^2})|$

Perturbative QCD

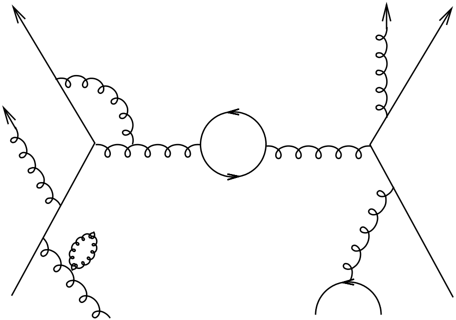
QCD

– Interaction of quarks and gluons



- N_f flavors of quarks
- $N_c^2 - 1$ gluons

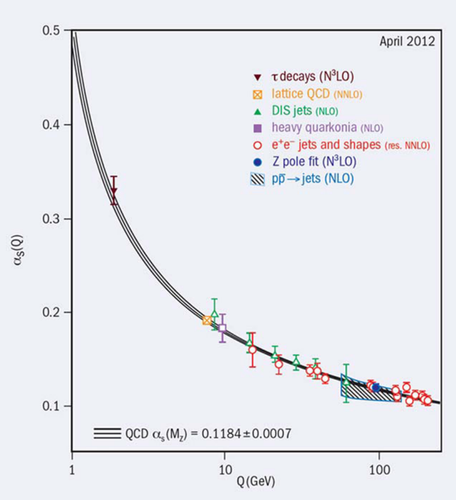
Perturbative QCD (pQCD)



Of course, things can get complicated.

- Tree diagrams of $n \leftrightarrow m$ processes
- Corrections to vertices
- Corrections to propagators

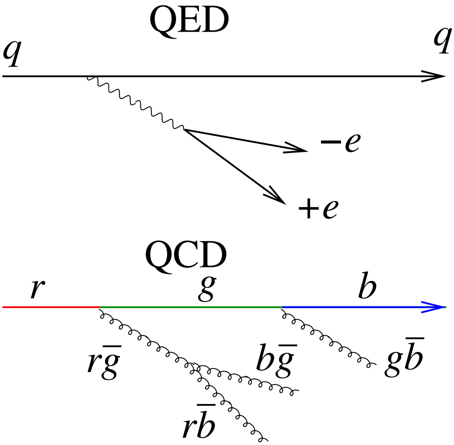
Perturbative QCD (pQCD)



S. Bethke, arXiv:1210.0325.

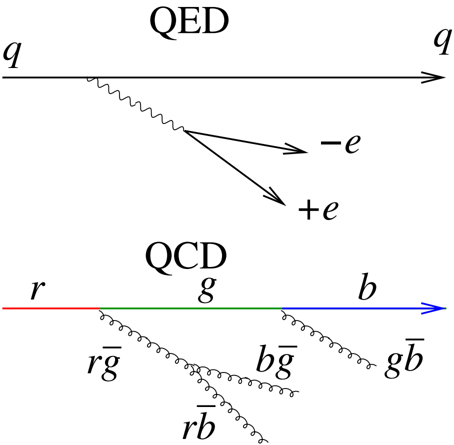
- Perturbative expansion possible because of asymptotic freedom
- $Q^2 \dfrac{\partial \alpha_S}{\partial Q^2} = -\beta_0 \alpha_S^2 - \beta_1 \alpha_S^3 + \cdots$
- $\alpha_S(Q^2) \approx \dfrac{1}{((33-2n_f)/12\pi)\ln(Q^2/\Lambda_{\rm QCD}^2)}$
- pQCD reliable for $Q \gtrsim 1$ GeV

Intuitive understanding of asymptotic freedom



- QED: Surrounded by virtual $e\bar{e}$ cloud
- Virtual $-e$ cloud drawn closer to $q > 0$ $\Longrightarrow$ Screening
- Larger Q $\Longrightarrow$ smaller distance $\Longrightarrow$ Sees less of the cloud $\Longrightarrow$ Closer to bare charge
- Possible because the original q never changes and photons do not carry charges

Intuitive understanding of asymptotic freedom



- QCD: Can resolve more soft virtual gluons at larger Q
- The color of the real particle can change whenever a gluon is emitted.
- Larger Q $\Longrightarrow$ More frequent changes $\Longrightarrow$ Less average color charge $\Longrightarrow$ Asymptotic freedom

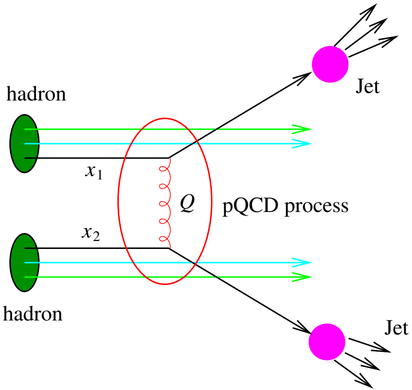
Difficulties with QCD

- As $Q \to \Lambda_{\rm QCD}$,

$$\alpha_S(Q^2) \approx \frac{1}{((33 - 2n_f)/12\pi)\ln(Q^2/\Lambda^2_{\rm QCD})} \to \infty$$

- Hadrons are $O(\Lambda_{\rm QCD})$ objects.
- Anything that has to do with hadron properties such as color confinement and hadronization is *non-perturbative.*
- In the IR limit, perturbation theory does not work $\Longrightarrow$ Factorize what can be calculated with pQCD (UV) and what cannot be calculated (IR)

Factorization Theorem



Hadron-Hadron Jet production scheme:

$$\sigma = \int_{abcd} f_{a/A}(x_a, Q_f) f_{b/B}(x_b, Q_f) \times \sigma_{ab\to cd} D_{C/c}(z_C, Q)$$

Factorization Theorem

- How realistic pQCD calculations are done

$$\sigma_{hh' \to C+X} = \int_{abcd} dx_1 dx_2 f_{a/h}(x_1, Q_f) f_{b/h'}(x_2, Q_f) \sigma_{ab \to cd}(Q_R) D_{C/c}(z_C, Q_f')$$

- $f_{a/h}(x_1, Q_f)$: Parton distribution function. Probability to have a parton type a with the momentum fraction x_1 in a hadron h. Depends on the factorization scale Q_f.
- $D_{C/c}(z_C, Q_f')$: Fragmentation function. Probability to create a hadron type C our of parton type c carrying the momentum fraction z_c.
- $\sigma_{ab \to cd}(Q_R)$: Parton-parton scattering cross-section.

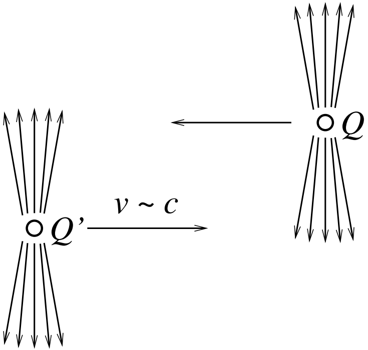
Factorization Theorem

- How realistic pQCD calculations are done

$$\sigma_{hh' \to C+X} = \int_{abcd} dx_1 dx_2 f_{a/h}(x_1, Q_f) f_{b/h'}(x_2, Q_f) \sigma_{ab \to cd}(Q_R) D_{C/c}(z_C, Q'_f)$$

- pQCD controls the *evolutions* of $f_{a/h}(x_1, Q_f)$ and $D_{C/c}(z_C, Q'_f)$. But pQCD cannot determine the initial data because this is dominated by IR processes.
- pQCD *can* calculate $\sigma_{ab \to cd}(Q_R)$ when the renormalization scale Q_R can be set high (that is, when $\sqrt{s}$ is large)

How to think about the initial state factorization – QED analogy



- Weizsäcker-Williams field – Highly contracted in the z direction
- Coulomb potential in the rest frame of the charge

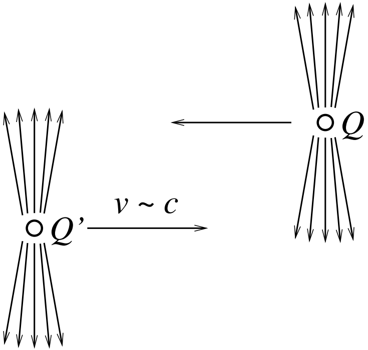
$$\varphi = Q/|\mathbf{r}|$$

- In the moving frame

$$A^\mu(x') = \Lambda^\mu_\nu A^\nu(x(x'))$$

- The coordinate in the moving frame $x' = (t, x, y, z)$. This corresponds to the rest frame position $x = (t\gamma - z\gamma v, x, y, z\gamma - t\gamma v)$.

How to think about the initial state factorization – QED analogy



- Weizsäcker-Williams field – Highly contracted in the z direction
- Coulomb potential in the rest frame of the charge

$$\varphi = Q/|\mathbf{r}|$$

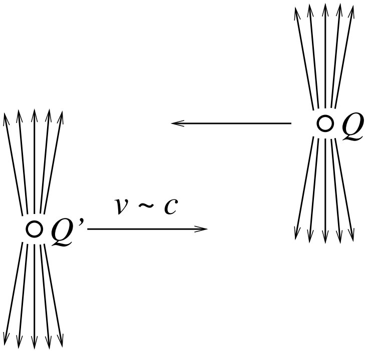
- In the moving frame

$$A^\mu = \frac{Q(\gamma, 0, 0, \gamma v)}{\sqrt{(z - vt)^2\gamma^2 + \Delta\mathbf{x}_\perp^2}}$$

- Pure gauge in the $v \to 1$ limit

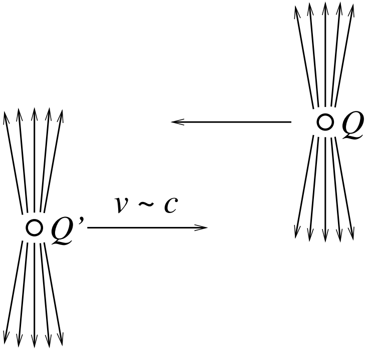
$$A^\mu \approx \frac{Q(1, 0, 0, 1)}{|z - vt|} = Q\partial_\mu \ln|z - vt|$$

How to think about the initial state factorization – QED analogy



- Weizsäcker-Williams field – Highly contracted in the z direction
  $F^{\mu\nu} \approx 0$ unless $z \approx vt$
- In the rest frame: Coulomb field is made up of space-like virtual photons
  $q^\mu q_\mu = -\mathbf{q}^2$ with $q_0 = 0$.
- In the Lab frame:
  $q'^\mu = (q^z \sinh\eta, \mathbf{q}_\perp, q^z \cosh\eta)$
- For large η,
  $|\Delta E| = |q^- - |\mathbf{q}|| \sim e^{-\eta}\mathbf{q}^2/q_z$
  $\Longrightarrow \Delta t \sim 1/|\Delta E| \sim e^\eta q_z/\mathbf{q}^2 \Longrightarrow$ virtual photons look almost like real photons.

How to think about the initial state factorization – QED analogy



- Weizsäcker-Williams field – Highly contracted in the z direction
  $F^{\mu\nu} \approx 0$ unless $z \approx vt$
- To a first approximation, the approaching particles *do not* know about each other until they are on top of each other.
- Initial photon momentum distribution *factorizes*: $F(x_1, x_2) = f(x_1)f(x_2)$
  but this is not exact.
- In QCD, color neutrality of hadrons help.

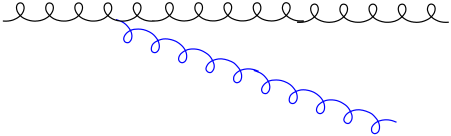
DGLAP Equation

- $f(x, Q_f)$: Probability density of partons with the virtuality *less than* Q_f.

Q_0: Coarse grained. You see one almost on-shell parton.

DGLAP Equation

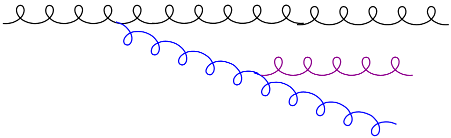
- $f(x, Q_f)$: Probability density of partons with the virtuality *less than* Q_f.



$Q_0 < Q_1$: Start to resolve another parton

DGLAP Equation

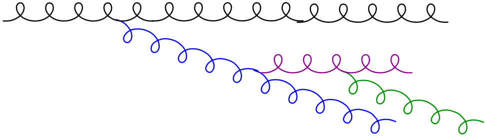
- $f(x, Q_f)$: Probability density of partons with the virtuality *less than* Q_f.



$Q_0 < Q_1 < Q_2$: And another

DGLAP Equation

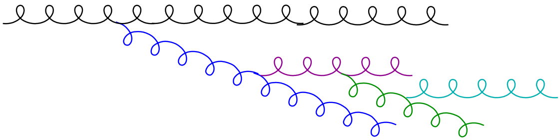
- $f(x, Q_f)$: Probability density of partons with the virtuality *less than* Q_f.



$Q_0 < Q_1 < Q_2 < Q_3$: And another

DGLAP Equation

- $f(x, Q_f)$: Probability density of partons with the virtuality *less than* Q_f.



You get the idea

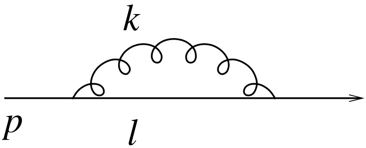
DGLAP Equation

- $f(x, Q_f)$: Probability density of partons with the virtuality *less than* Q_f.

$$Q^2 \frac{\partial}{\partial Q^2} \begin{pmatrix} q^S \\ g \end{pmatrix} = \frac{\alpha_S(Q^2)}{2\pi} \begin{pmatrix} P_{qq} & 2n_f P_{qg} \\ P_{gq} & P_{gg} \end{pmatrix} \otimes \begin{pmatrix} q^S \\ g \end{pmatrix}$$

where P_{ij}: Splitting function $\sim$ Probability to end up with ij in the final state.

Splitting can cause IR divergence



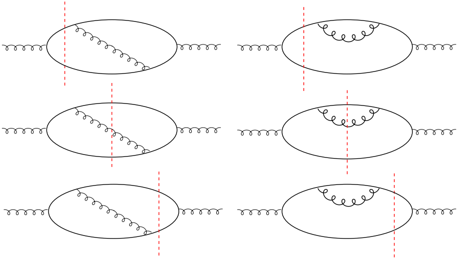
- p is on-shell: $p^2 = 0$
- Diverges when either k or l is on-shell
- This happens either k is very soft so that

$$l^2 = (p - k)^2 \approx p^2$$

- or p and k are almost collinear

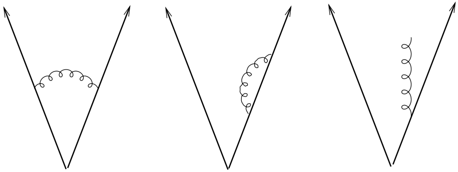
$$l^2 = (p - k)^2 = p^2 + k^2 - 2pk$$
$$\approx 0$$

Splitting can cause IR divergence



- $g \to q\bar{q}$ and $g \to q\bar{q}g$
- Only the *sum* is IR finite because soft and collinear divergences
- Splitting functions know about this

Splitting can cause IR divergence



- Observables must be IR safe.
- 3rd diagram must be treated as 2-jet when the radiation is soft or collinear $\Longrightarrow$ IR-safe Jet definitions

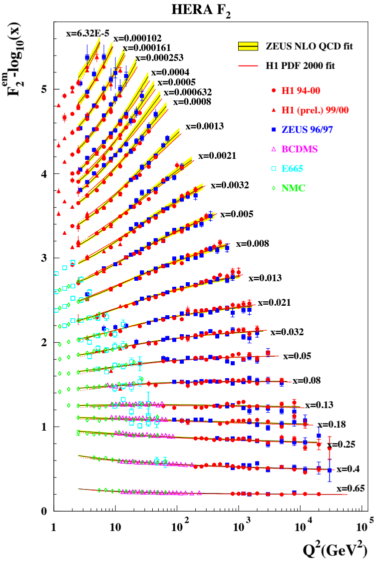
Factorization Theorem

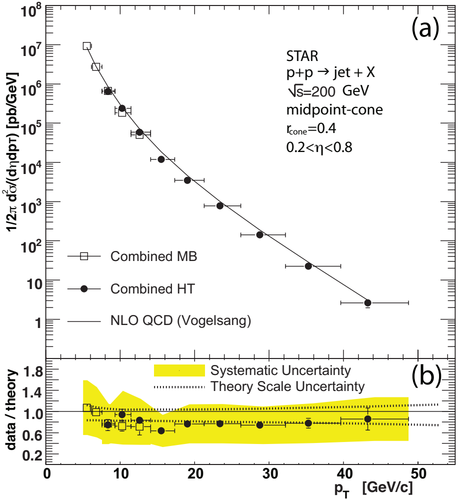
- Splitting function similarly runs
- 3 different scales: Q_f for the pdf, Q_R for $\sigma(Q_R)$ and Q'_f for the fragmentation function
- In principle, physical observables should not depend on these scales. However, factorization theorem is only *approximate*.
- Lots of freedom to choose the scales. Usually something like

$$Q_f = Q_R = Q'_f = \#p_T$$

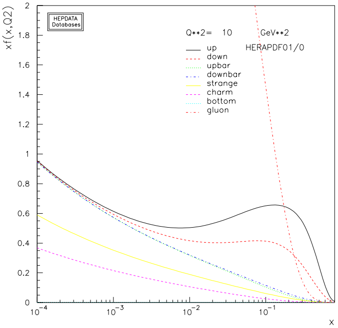
works OK where p_T is the momentum of the *final* state particle.

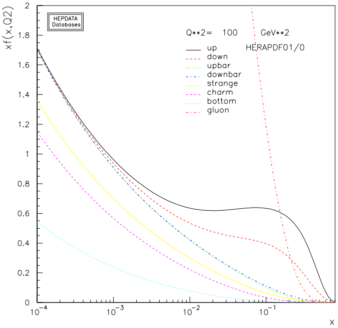
pQCD & Factorization at work





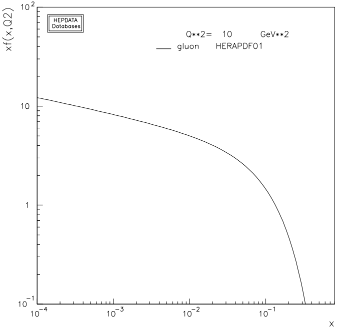
pQCD & Factorization at work

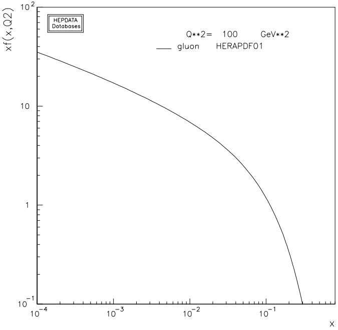




- CTEQ 06 Proton PDF's
- Larger $Q \Longrightarrow$ More soft partons

pQCD & Factorization at work





- Gluon distributions for $Q^2 = 10\,\text{GeV}^2$ and $Q^2 = 100\,\text{GeV}^2$.