

Hydrodynamics for Relativistic Heavy-Ion Collisions



DEPARTMENT OF
PHYSICS

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References:

arXiv:nucl-th/0305084 (Kolb, UH)
arXiv:hep-ph/0407360 (UH)
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PRL 106 (2011) 192301 (Song, Bass, UH, Hirano, Shen)
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Motivation

- Relativistic viscous hydrodynamics is the backbone of dynamical modeling for heavy ion collisions at RHIC and LHC
- Needed to describe the space time evolution of the matter produced in a heavy ion collision
- Application is justified a priori by the smallness of the shear viscosity of the plasma as measured in RHIC and LHC experiments
- Canonical viscous hydrodynamics relies on a linearization around an isotropic equilibrium state
- Anisotropic viscous hydrodynamics generalizes this to a linear expansion around a spheroidally deformed (anisotropic) local momentum distribution

Three Lecture Plan

Lecture 1

- Motivation and Introduction
- Kinetic Theory vs. Hydrodynamics
- Ideal Fluid Dynamics
- Ideal Fluid Equations of Motion
- 0+1d Boost-Invariant Transversely Homogeneous Systems (Bjorken Solution)

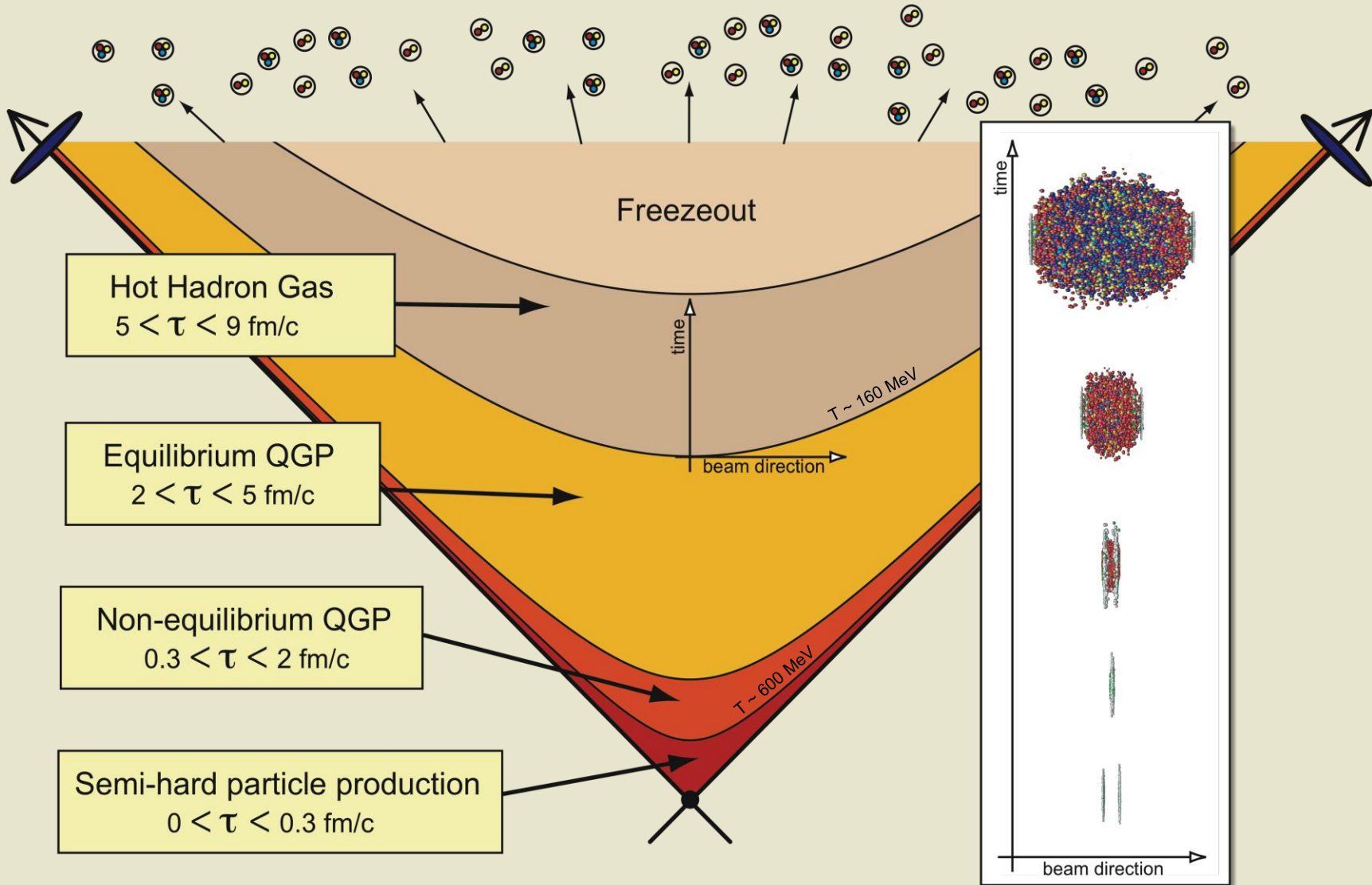
Lecture 3

- Results

Lecture 2

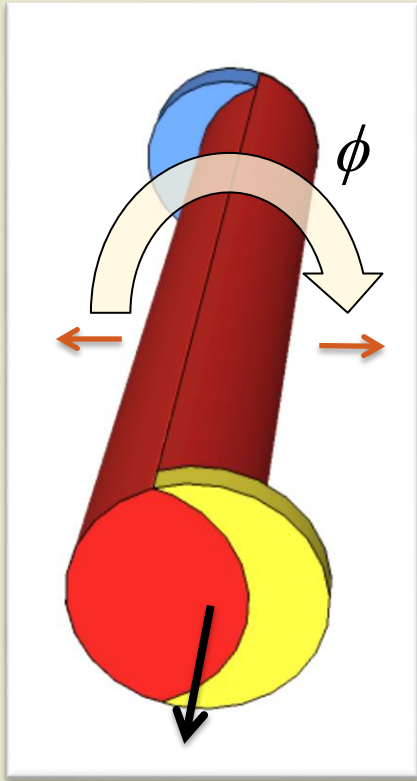
- 1st and 2nd Order Viscous Hydro
- Limitations of Viscous Hydro
- Spheroidal Distribution
- Anisotropic $T^{\mu\nu}$
- Anisotropic Dynamics Equations
- 0+1d Limit
→ Connection to Viscous Hydro

Heavy Ion Collision Timescales



Hydro for collective flow

- During non-central collisions overlap region breaks azimuthal symmetry



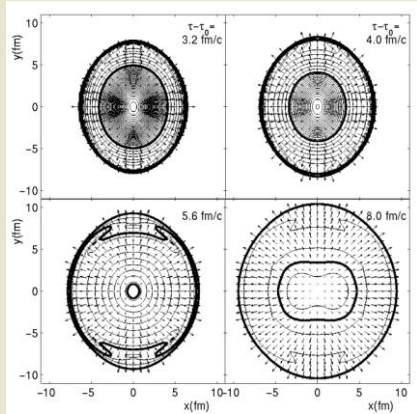
$$\frac{dN}{df} = \frac{1}{2\pi} (v_0 + 2v_1 \cos f + 2v_2 \cos 2f + 2v_3 \cos 3f + \dots)$$

Directed Flow

Elliptic Flow

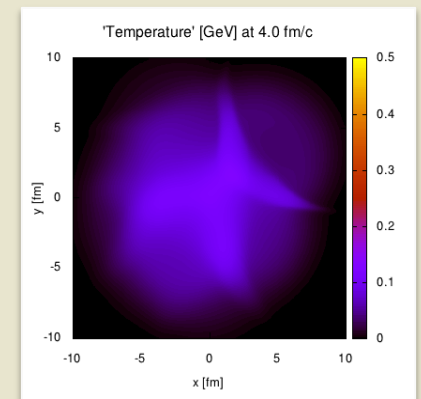
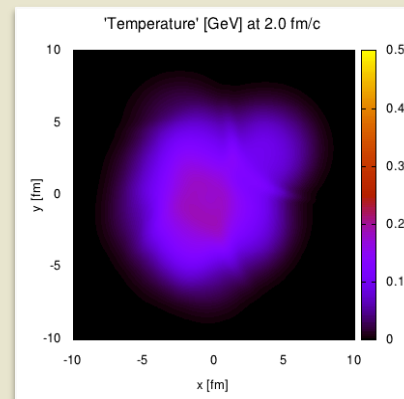
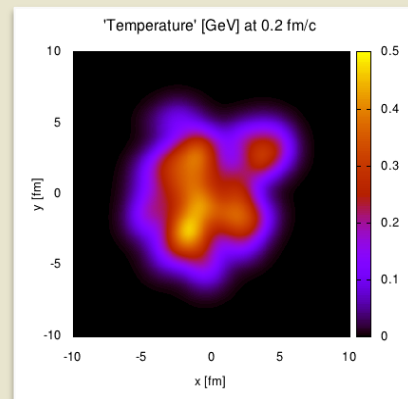
Triangular Flow

“Average” analysis

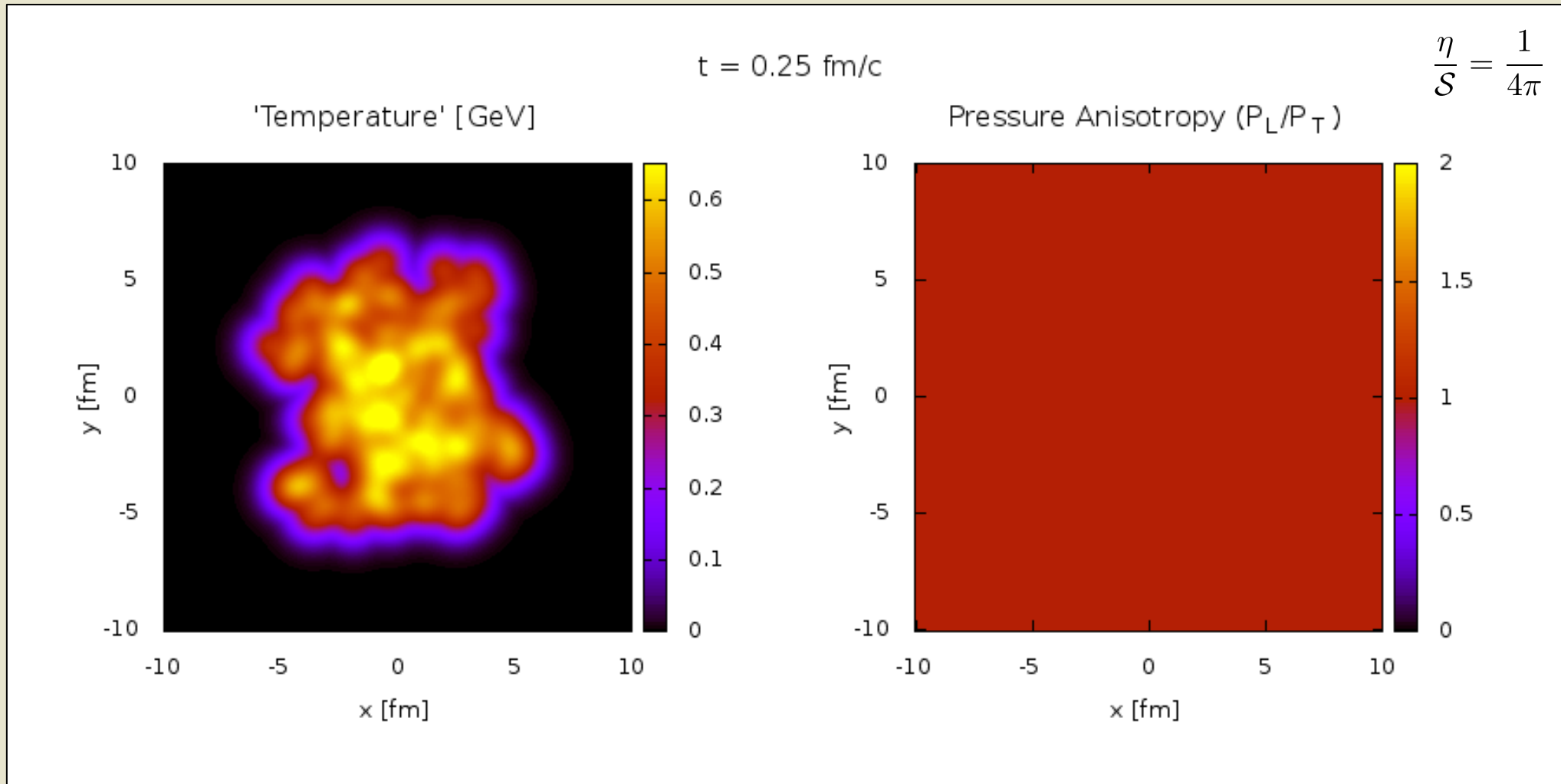


Kolb, Sollfrank, Heinz, Phys. Rev. C 62, 054909 (2000).

Event-by-Event analysis

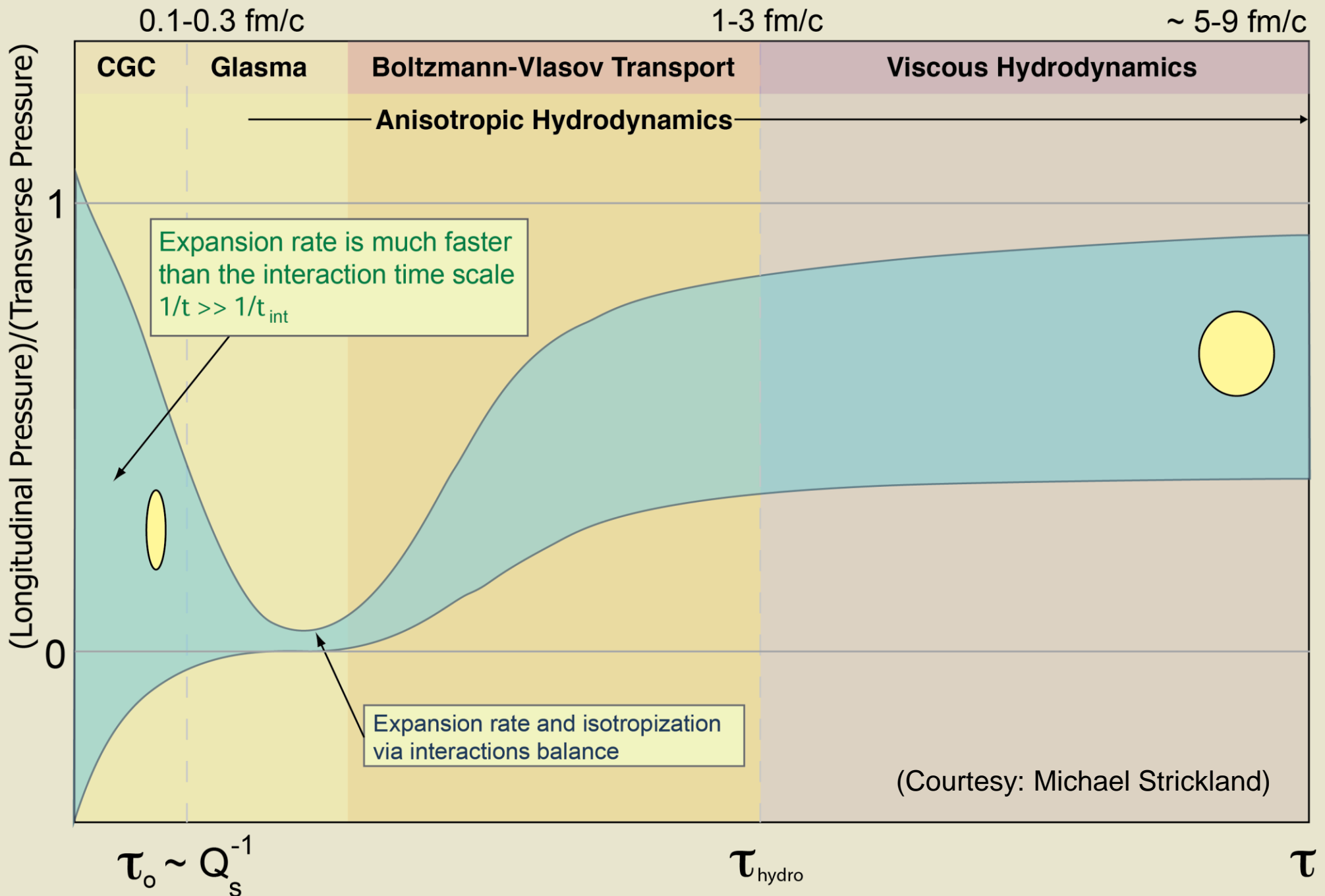


Spatiotemporal Evolution



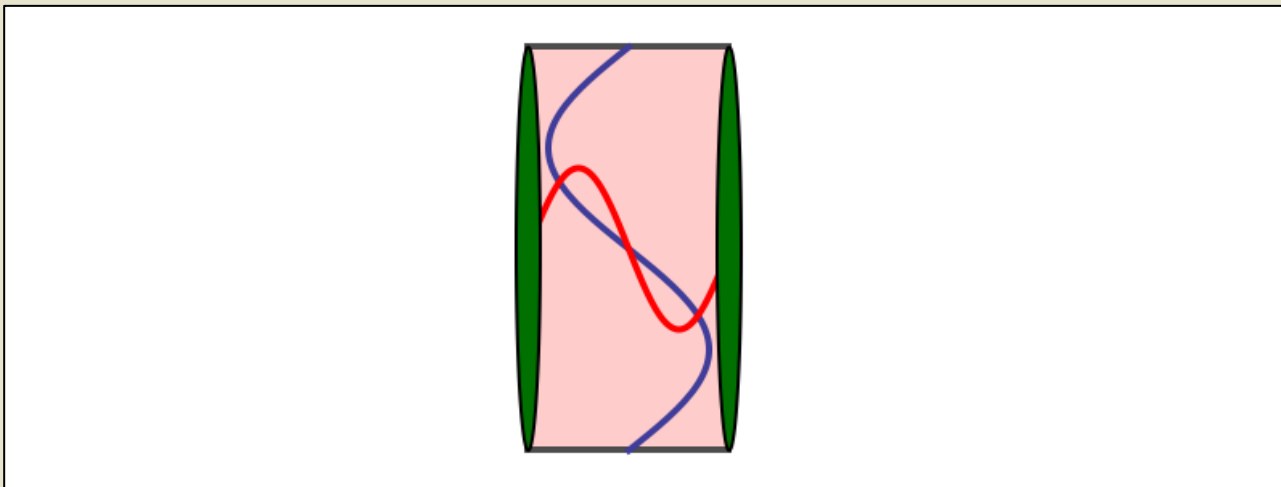
- Pb-Pb, $b = 7 \text{ fm}$ collision with Monte-Carlo Glauber initial conditions
 $T_0 = 600 \text{ MeV}$ @ $\tau_0 = 0.25 \text{ fm}/c$
- Left panel shows temperature and right shows pressure anisotropy

QGP momentum anisotropy

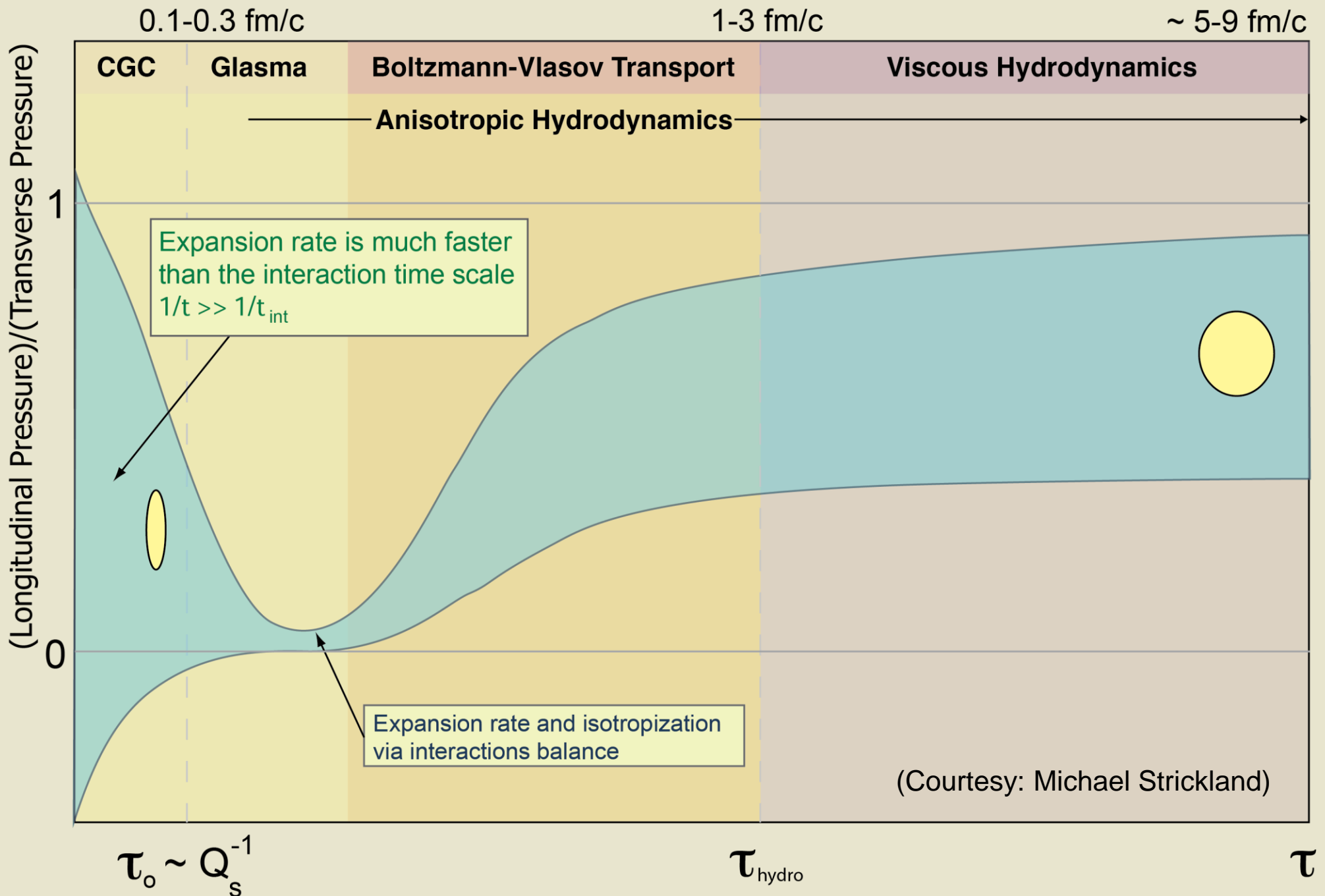


Longitudinal Expansion

- The nearly speed of light expansion of the quark gluon plasma along the beamline direction causes “longitudinal cooling” of the plasma during the first few fm/c of the plasma’s lifetime.
- One can think of the system as a tiny one-dimensionally expanding universe in which momenta are red-shifted along the beamline direction.



QGP momentum anisotropy



- Hydro From Transport -